

8 Abstract

9 Extreme heat under global warming is a concerning issue for the growing tropical population.
10 However, model projections of extreme temperatures, a widely used metric for extreme heat,
11 are uncertain on regional scales. In addition, humidity also needs to be taken into account
12 in order to estimate the health impact of extreme heat. Here we show that an integrated
13 temperature-humidity metric for the health impact of heat, namely the extreme wet-bulb
14 temperature (TW), is controlled by established atmospheric dynamics and thus can be ro-
15 bustly projected on regional scales. For each 1°C of tropical mean warming, global climate
16 models project extreme TW (the annual maximum of daily-mean or 3-hourly values) to in-
17 crease roughly uniformly between 20°S and 20°N latitude by about 1°C . This projection is
18 consistent with theoretical expectation based on tropical atmospheric dynamics, and obser-
19 vations over the past 40 years, which gives confidence to the model projection. For a 1.5°C
20 warmer world, the likely (66 per cent confidence interval) increase of regional extreme TW
21 is projected to be $1.33\text{-}1.49^{\circ}\text{C}$, whereas the uncertainty of projected extreme temperatures is
22 3.7 times as large. These results suggest that limiting global warming to 1.5°C will prevent
23 most of the tropics from reaching a TW of 35°C , the limit of human adaptation.

24 Main

25 The impact of global warming on local extreme heat is projected to be detectable earliest in
26 the tropics¹⁻³ where baseline temperatures are already high. In addition, countries located
27 between 20°S and 20°N latitude will soon become major contributors to the global population
28 growth,⁴ and there is thus a pressing need for accurate projections of extreme heat in the
29 tropics down to regional scales.

30 The most widely used metric for extreme heat has been the extreme temperature. How-
31 ever, projections of extreme temperatures have large regional uncertainty arising from in-
32 sufficient model representation of important land processes.⁵ Moreover, to facilitate the
33 estimation of heat-induced health impact (or heat stress), the effect of humidity should also
34 be included,^{6,7} and this is because the major way for humans to lose metabolic heat in hot
35 weather is evaporative cooling (sweating),^{8,9} the efficiency of which anti-correlates with hu-
36 midity. In particular, the inclusion of humidity is necessary for assessing heat stress in the
37 tropics, the warmest and the most humid places on the Earth.

38 The importance of humid heat has been increasingly recognized.^{10,11} Studies have shown
39 that increased humidity with temperature following the Clausius-Clapeyron relationship can
40 worsen summer heat stress in the tropics,^{12,13} while other work has noticed a reduction
41 in either relative humidity¹⁴ or specific humidity¹⁵ on the hottest days (not limited to the
42 tropics). Given the possibility that humidity can interact with temperature in extreme heat,
43 it is necessary to better quantify and improve our mechanistic understanding for the control
44 of humid heat.

45 Here, we use the extreme wet-bulb temperature (TW), an integrated temperature-humidity

46 metric for heat stress (see Methods). TW by definition is the lowest temperature that hu-
47 man skin can be cooled to through evaporation of sweat. Therefore, the closer TW is to
48 the upper limit of human skin temperature (around 35°C), the more intolerable the heat is,
49 with a survival limit of $TW=35^{\circ}C$ ¹⁶ (Note that high TW values below this survival limit
50 also have adverse health impact). Furthermore, TW is a major component in the wet-bulb
51 globe temperature (WBGT; See Methods)¹⁷ which is the standard metric for workplace heat
52 stress. In this paper, we argue that the regional extreme TW in the tropics is mainly con-
53 trolled by robust atmospheric dynamics that have been established previously,¹⁸⁻²¹ rather
54 than local processes that are of more uncertainty. Therefore, tropical extreme TW can be
55 robustly projected on regional scales under global warming.

56 **Global climate model projections**

57 Fig. 1a shows the projections of extreme TW (TW_{\max}) and extreme temperatures (T_{\max})
58 by 22 global climate models (Table S1) from the Coupled Model Intercomparison Project
59 phase 5 (CMIP5)²² under the Representative Concentration Pathway 8.5 (RCP 8.5) emission
60 scenario (Note that TW_{\max} and T_{\max} mostly refer to the annual maximum of *daily* mean
61 values in this paper, and refer to the annual maximum of *3-hourly* values when specifically
62 stated). The multi-model mean of T_{\max} averaged over tropical land within 20°S-20°N warms
63 faster than the tropical mean temperature. However, TW_{\max} closely follows the tropical
64 mean warming, similar to an earlier finding using an atmospheric model coupled to a slab
65 ocean.¹⁶ These results also hold when analysing 3-hourly data that resolve the diurnal cycle
66 from two models (GFDL-CM3 and IPSL-CM5A-LR) (Fig. 1b,c).

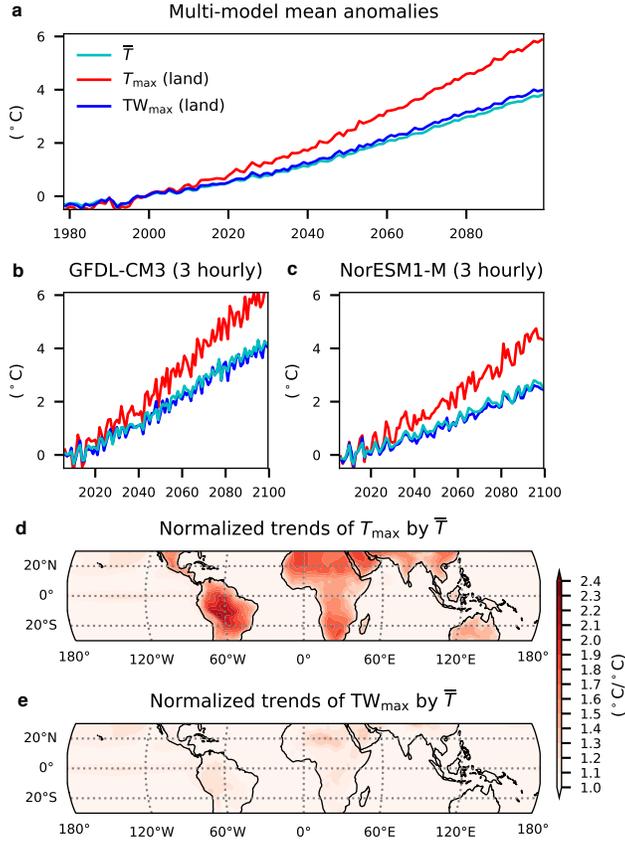


Figure 1: TW_{\max} and T_{\max} trends in climate models under RCP 8.5. **a**, Multi-model-mean time series of the tropical-mean (20°S - 20°N) temperature (\bar{T} ; cyan), land-mean T_{\max} (red), and land-mean TW_{\max} (blue). **b** and **c**, The same as **a** but using the annual-maximum 3-hourly values for T_{\max} and TW_{\max} for two individual models. **d** and **e**, Multi-model-mean location-specific T_{\max} and TW_{\max} trends normalized by \bar{T} trends.

67 Figs. 1d,e show T_{\max} and TW_{\max} trends for all locations normalized by the tropical mean
 68 warming under RCP 8.5. T_{\max} warming is spatially inhomogeneous over land ranging from
 69 1.0°C to 2.3°C for each 1°C of tropical mean warming (Fig. 1d) consistent with previous

70 findings. In contrast, we find that increases of TW_{\max} has no significant land-ocean contrast
 71 ranging from 0.8°C to 1.3°C for each 1°C of tropical mean warming (Fig. 1e). Using the
 72 annual-maximum 3-hourly TW for TW_{\max} does not change this result (Fig. S1).

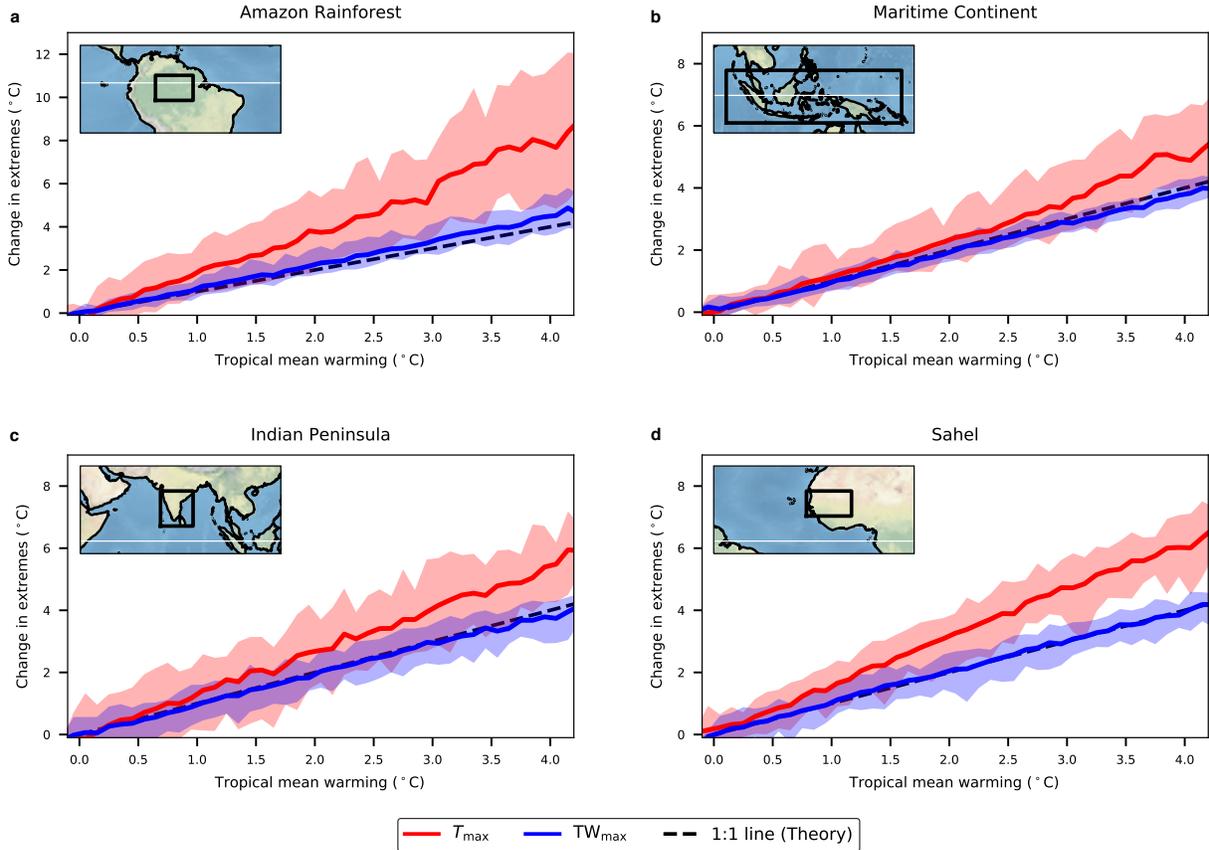


Figure 2: **Model agreement on regional TW_{\max} projections.** Multi-model means (lines) and spreads (2.5-97.5th percentiles; shading) for regional T_{\max} (red) and TW_{\max} (blue) as a function of the tropical mean warming are shown for four regions, namely **a** Amazon rainforest, **b** Maritime Continent, **c** Indian Peninsula, and **d** Sahel (Only land data within the black frames on the maps are sampled). The dashed black lines indicate the 1:1 ratio.

73 The spatially uniform TW_{\max} trend (Fig. 1e) is not a cancellation of errors among
 74 different models. Instead, all models show good agreement on TW_{\max} trend, even down to

75 regional scales. Fig. 2 shows the model spread (2.5-97.5th percentiles) of T_{\max} and TW_{\max}
76 projections for four selected regions that have caught substantial attention in the literature,
77 namely the Amazon rainforest, the Maritime Continent, the Indian peninsula, and the Sahel.
78 Projected T_{\max} warming has large spread among models, which is especially prominent in
79 the Amazon rainforest, consistent with earlier analysis.⁵ However, for regional TW_{\max} , all 22
80 climate models project a close to 1:1 ratio with the tropical mean warming. Using the annual
81 maximum of 3-hourly TW does not change this result (Fig. S2). Intriguingly, the model
82 spread of T_{\max} tends to grow with the amplitude of the projected warming (pronounced for
83 the Amazon rainforest and the Maritime Continent), whereas the model spread of TW_{\max}
84 does not show evident growth within the range of simulated warming (roughly 4°C). That
85 the inter-model spread is much less for TW_{\max} projections than for T_{\max} is also true for other
86 tropical land regions (Fig. S3).

87 To summarize, global climate models predict that TW_{\max} will increase roughly uniformly
88 in the tropics by about 1°C for each 1°C of tropical mean warming. Models show wide spread
89 on regional T_{\max} projections but agree very well upon regional TW_{\max} .

90 **Theoretical support**

91 For a theoretical projection of TW_{\max} , we argue that tropical atmospheric dynamics exert a
92 strong, tropics-wide control on local TW_{\max} . This control is through the functional relation-
93 ship between TW and moist static energy (MSE; Fig. S4) which is a variable regulated by
94 atmospheric dynamics. In the tropics, the free-tropospheric temperature is roughly uniform
95 in the horizontal as a result of the weak effect of the Earth's rotation. This horizontally

96 uniform temperature, which is determined by the near-surface MSE in regions of deep con-
 97 vection, sets the upper bound for MSE at all locations. Indeed, the maximum near-surface
 98 MSE is roughly uniform within 20°S-20°N (even more uniform than the time-mean MSE;
 99 Fig.S5a,b), and the spatial pattern of TW_{\max} closely follows the uniformity of the maximum
 100 MSE (Fig. S5c). As this upper bound for near-surface MSE and, equivalently, for TW is
 101 a common one over land or over ocean,²¹ we expect that changes in TW_{\max} should also be
 102 roughly equal over land and over ocean under global warming:

$$\Delta TW_{\max, \text{Land}} \approx \Delta TW_{\max, \text{Ocean}} \quad (1)$$

103 Eq. (1) thus provides a handle on TW_{\max} over land which is challenging to predict due to
 104 various land types and land processes, as a theoretical projection for TW_{\max} over ocean can
 105 be made relatively easily. Near the ocean surface, air is close to saturation and TW changes
 106 are approximately equal to temperature changes (exactly equal when air is saturated), and
 107 $\Delta TW_{\max, \text{Ocean}}$ is thus approximately equal to the change in the warmest SSTs. Therefore,
 108 1°C of $\Delta TW_{\max, \text{Land}}$ is accompanied by 1°C of warming of the warmest SSTs according to
 109 Eq. (1). Furthermore, the area dominance of the ocean and the relatively constant shape
 110 of SST histogram under global warming (Fig. S6) together result in a 1:1 correspondence
 111 between warming of the warmest SSTs and the tropical mean temperature (While there is
 112 potential for differences between changes in these relatively warm SSTs and the tropical
 113 mean SST,²³⁻²⁵ we find these differences to be small enough that they do not undermine the
 114 theoretical considerations here). We thus expect $\Delta TW_{\max, \text{Land}}$ roughly equals the tropical
 115 mean warming.

116 Global climate models shown in Figs. 1, 2 are consistent with the above theoretical

117 considerations. For each 1°C of tropical mean warming, models on average give 1.05 °C
118 of $\Delta TW_{\max, \text{Land}}$, 0.93°C of $\Delta TW_{\max, \text{Ocean}}$, and 0.91°C of the warmest-quartile-mean SST
119 increase, all close to 1°C.

120 The non-local control of TW_{\max} by the warmest SSTs seems to be at odds with the
121 perception that these extreme events are driven by rare local meteorology, and this contro-
122 versy deserves some clarification. While TW_{\max} events are driven by local processes, the
123 potential magnitude of TW_{\max} is largely set by the uniform free tropospheric temperature.
124 The effectiveness of this non-local control is evident in the uniformity of TW_{\max} increases in
125 Fig. 1d and the good agreement across models in Fig. 2, neither of which can be explained
126 by the heterogeneity of local processes. Moreover, the existence of such a non-local control
127 within the tropics also explains why the tropics are consistently warm and humid, but the
128 highest TW and WBGT are observed in the subtropics.^{13,26,27} These considerations thus
129 support the picture that the magnitude of ΔTW_{\max} across tropical land regions is set by the
130 warmest SSTs and not local processes or the spatial pattern of SST.

131 **Observational evidence**

132 From 1979 to 2018, the tropical (20°S-20°N) land mean T_{\max} trend has a 95% confidence
133 interval of 0.24-0.31°C/decade, which is almost three times of the tropical mean warming of
134 0.08-0.12°C/decade based on ERA-Interim reanalysis²⁸ (Fig. 3a). TW_{\max} has a trend of 0.05-
135 0.10°C/decade, very similar to the tropical mean warming, and the interannual variabilities
136 of the two are highly correlated with a correlation coefficient of 0.85 (Fig. 3a). Using the
137 annual-maximum 3-hourly TW from ERA-Interim yields very similar anomalies, though the

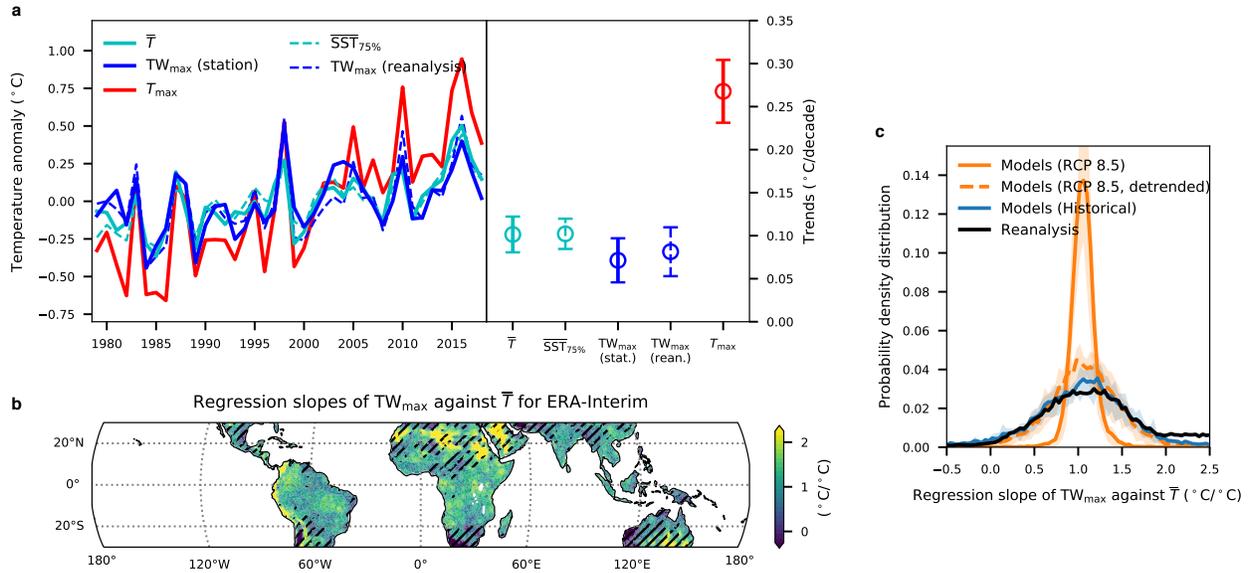


Figure 3: TW_{\max} in observations and reanalysis data. **a**, Time series and corresponding linear trends of tropical mean temperature (\bar{T} ; solid cyan), land-mean T_{\max} (red), land-mean TW_{\max} from stations (solid blue) and ERA-Interim (dashed blue), and the warmest-quartile-mean SST from HadISST (dashed cyan) for 1979-2018 (20°S-20°N). The confidence intervals for the linear trends represent 95% significance assuming that the detrended annual data points are independent. **b**, Linear regression slopes of local TW_{\max} onto \bar{T} in the interannual variabilities (linear trends removed) from ERA-Interim for 1979-2018. Regions where TW_{\max} and \bar{T} are not correlated on a 95% significance level are hatched. **c**. Histograms of regression slopes of local TW_{\max} onto \bar{T} (linear trends removed) for 1979-2005 in ERA-Interim (black solid) and models (blue solid), and for the global warming simulations in models (orange dashed). The same histogram for non-detrended global warming simulations (Fig. 1e) is also shown (orange solid). Shading indicates the 25-75th percentiles of models.

138 longterm trend is smaller (Fig. S7). Furthermore, station measurements of TW provided
139 by HadISD²⁹ (see Methods; Fig. S8) show that TW_{\max} averaged over tropical stations is
140 highly correlated with that from ERA-Interim and has a similar trend of 0.05-0.10°C/decade
141 (Fig. 3a). The consistency of reanalysis data with station observations and the theory lends
142 support to the quality of the reanalysis data over tropical land.

143 The warmest-quartile-mean SST (the average of the top 25% of monthly SST at all grid
144 points within each year) from HadISST³⁰ is highly correlated with land-mean TW_{\max} and
145 has a similar trend of 0.08-0.12°C/decade (Fig. 3a). Satellite SST observations and station
146 TW observations are largely independent, and the very good consistency in their extreme
147 values lends strong support to the aforementioned argument that TW_{\max} over land is coupled
148 to the warmest SSTs. Strong El Niño events have the potential of warming the warmest
149 SSTs and, as a result, affect TW_{\max} over land (e.g., 1998 in Fig. 3a).

150 Location-specific evaluation of long-term TW_{\max} trends for the observations suffers from
151 the smallness of the warming signal, but interannual variability of SST provides room for
152 testing the 1:1 relationship with TW_{\max} . Regression slopes of TW_{\max} (ERA-Interim) onto
153 the tropical mean temperature (linear trends removed) is relatively uniform over most of
154 the land regions within 20°S-20°N (Fig. 3b) with a mode value close to 1 (Fig. 3c). This
155 relationship loosens in the subtropics (indicated by the hatching in Fig. 3b), consistent
156 with the latitudinal range where the theory works.²¹ That the Andes and the southern edge
157 of the Sahara have much higher TW_{\max} sensitivity does not violate the proposed theory,
158 as climatological TW_{\max} in those regions is too low to trigger convection and thus not
159 constrained by the aforementioned mechanism. The standard deviation of these slopes in
160 the reanalysis is larger than that for the global warming simulations shown in Fig. 1e (Fig.

161 3c). A likely explanation is that the spatial pattern of TW_{\max} can change in the interannual
162 variability and such a spatial rearrangement can cause a spread in the regression slopes but
163 does not affect the tropical averages shown in Fig. 3a. Indeed, global climate models also
164 show a similar spread of TW_{\max} trends under historical radiative forcing, and the removal of
165 longterm trends in the global warming simulations for the same set of models also result in a
166 similar spread (Fig. 3c). Therefore, regional TW_{\max} trends diagnosed from reanalysis data
167 over the past 40 years are consistent with global climate models. Also for similar reasons,
168 we do not expect every station to give the same TW_{\max} trend either.

169 While we do not attempt to formulate an attribution statement for the TW_{\max} trend over
170 land seen in Fig. 3a, we note that the tight relationship in the overall trend as well as higher
171 frequency variability strongly suggests that any attribution statements for the tropical mean
172 temperature or SST can also be applied to TW_{\max} .

173 **Implications for the future climate**

174 Consistency of model results with the theory and observations lends strong support to the
175 capability of global climate models in properly simulating regional TW_{\max} increases. In a
176 1.5°C warmer world, the projected 66 per cent confidence interval (equivalent to IPCC’s
177 “likely range”) for TW_{\max} increases across all tropical land regions (20°S-20°N) is 1.33-
178 1.49°C, consistent with the simulated tropical mean warming of $\sim 1.4^\circ\text{C}$ in a 1.5°C warmer
179 climate (Fig. 4). On the other hand, projected T_{\max} increases have a wider distribution, the
180 absolute (relative) standard deviation of which is 3.7 (1.8) times of that of TW_{\max} increases.
181 The reduction in uncertainty is more pronounced for regions where T_{\max} projections are most

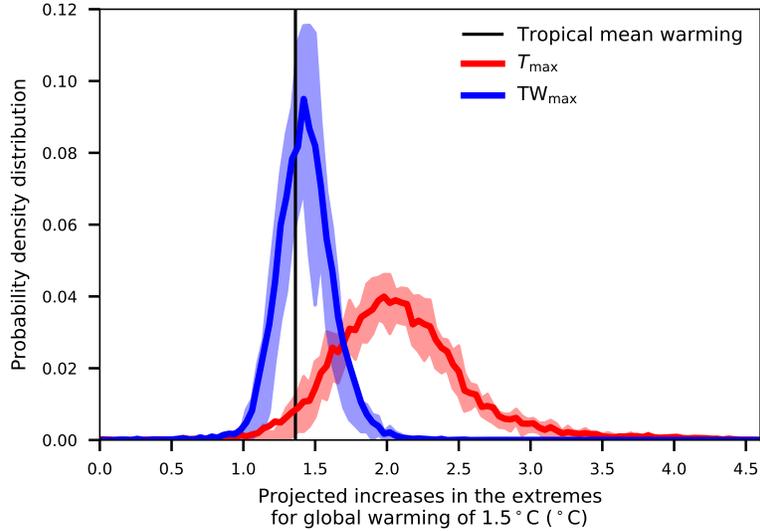


Figure 4: **Uncertainty of T_{\max} and TW_{\max} projection in a 1.5°C warmer world (land between 20°S - 20°N).** Distributions of model projected TW_{\max} increases (blue) and T_{\max} increases (red) under RCP 8.5 at 1.5°C of global mean warming are shown. The distributions are constructed by linearly regressing local T_{\max} and TW_{\max} increases onto global mean warming and taking the regression values at 1.5°C of global mean warming. Solid lines show the average distribution of all models and the shading indicates the 25-75th percentiles across models.

182 uncertain. For example, in the Amazon rainforest and the Maritime Continent (Fig. 2), the
 183 absolute (relative) uncertainty of T_{\max} increases is around 4 (2.5) times of that of TW_{\max}
 184 increases.

185 Our results imply that curtailing global mean warming will have a proportional effect on
 186 regional TW_{\max} in the tropics. The maximum 3-hourly TW (ERA-Interim) ever experienced
 187 in the past 40 years by 99.98% of the land area within 20°S - 20°N is below 33°C . Therefore, a
 188 1.5°C or 2°C warmer world will likely exempt the majority of the tropical area from reaching

189 the survival limit of 35°C. However, there exists little knowledge on safety thresholds for
190 TW besides the survival limit,¹¹ and 1°C of TW increase could have adverse health impact
191 equivalent to that of several degrees of temperature increase. TW will thus have to be
192 better calibrated to health impact before wider societal implementation. Nonetheless, the
193 confidence in TW_{max} projection provided in this work still raises the confidence in projections
194 of other calibrated heat stress metrics that accounts for TW, such as the WBGT.

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268 **Methods**

269 **Wet-bulb temperature (TW).** TW is thermodynamically defined as the temperature
270 that an air parcel would have if cooled adiabatically to saturation at constant pressure by
271 evaporation of water into it, all latent heat being supplied by the parcel. This process
272 is enthalpy conserving, therefore $c_p T + Lq = c_p \text{TW} + Lq_{\text{sat}}(\text{TW})$, where T and q are the
273 temperature and the specific humidity of an environmental air parcel.³¹ TW is empirically
274 defined as the temperature read from the wet-bulb thermometer which is a balance between
275 diffusion of sensible heat from the environment to the saturated surface and the latent heat
276 the other way around. Here we adopt the second definition because it is more relevant for the
277 process of evaporative cooling of sweat. The two definitions give the same result due to the
278 coincidence that the diffusivities of sensible and latent heat are the same. TW is calculated by
279 solving the following equation using Newton's iteration: $c_p T + Lq = c_p \text{TW} + \epsilon L e_{\text{sat}}(\text{TW})/p_s$,
280 where T , q , and p_s are temperature, specific humidity, and pressure of the surface-air air, ϵ
281 is the molecular mass ratio of water vapor and air.

282 **Wet-bulb globe temperature (WBGT).** WBGT evaluates the heat stress to which
283 a person is exposed used by workers, athletes, and military. It is defined as $\text{WBGT} =$
284 $0.7\text{TW} + 0.3T_d$ (or $\text{WBGT} = 0.7\text{TW} + 0.2T_g + 0.1T_d$ to take solar insolation into account),
285 where TW is the wet-bulb temperature, T_g is the globe thermometer temperature, and T_d is
286 the dry-bulb temperature (or actual air temperature).

287 **Station data.** Station data from HadISD are selected based on the following procedure:
288 For each station, we first scan through TW measurements for each day and only take the daily
289 averages of those days containing at least 4 measurements. Then, for the years containing

290 more than 300 daily-mean TW, the annual maximum TW is taken. In the end, stations
291 with at least 20 valid annual-maximum TW values are included in this paper which end up
292 to 293 stations (Fig. S8). For those stations, the average TW is subtracted for each station,
293 then the anomalies are averaged among all stations as is shown in Fig. 3.

294 **Daily-mean and 3-hourly TW from CMIP5 models.** CMIP5 models provide
295 surface-air temperature and specific humidity on daily and 3-hourly frequency but not surface
296 pressure. Therefore we interpolate monthly surface pressure piece-wisely to daily frequency
297 for daily TW calculation and ignore the diurnal cycle in surface pressure for 3-hourly TW
298 calculation. The error thus induced in TW is estimated to be less than 0.3°C.

299 **References**

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302 **Data Availability**

303 CMIP5 model data provided by the World Climate Research Programme's Working Group
304 on Coupled Modelling and climate modeling groups can be accessed at [https://esgf-node.](https://esgf-node.llnl.gov/projects/cmip5)
305 [llnl.gov/projects/cmip5](https://esgf-node.llnl.gov/projects/cmip5). ERA-Interim data provided by European Centre for Medium-
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310 fice Hadley Centre can be accessed at <https://www.metoffice.gov.uk/hadobs/hadisst>.

311 **Code Availability**

312 The computer code used in this paper is available from Y.Z. (yz8@princeton.edu).

313 **Corresponding Author**

314 Correspondence and requests for materials should be addressed to Y.Z. at yz8@princeton.edu.

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322 **Author Contributions**

323 Y.Z. conceived the theory, performed the data analysis, and wrote the manuscript. I.H. sug-
324 gested the examination of observations/reanalysis. S.F. interpreted the widening of TW_{\max}

325 trend distribution in reanalysis (Fig. 3c). All authors discussed the results and edited the
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