

A Lattice-Boltzmann model for simulating bedform-induced hyporheic exchange

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Key Points:

- Lattice-Boltzmann model successfully represents bedform-induced hyporheic exchange flow
- A fully-coupled surface-subsurface model for HE is proposed
- temporal variability in hyporheic flow patterns is observed

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Abstract

The Lattice-Boltzmann (LB) method is applied here for the first time to simulate bedform-induced hyporheic exchange flow in a reduced complexity model. The flexibility of the LB allows surface and hyporheic flows to be resolved together, in contrast to other approaches for similar model domains, in which surface flow is usually solved independently, and then the solution of the surface flow provides the boundary conditions to model the hyporheic exchange flow. At the same time, the superior computational efficiency of LB allows the use of Large Eddy Simulations within transient simulations. Numerical results show a faithful reproduction of pressure along the bedform surface—especially, the pressure drop leeward to the dune. Results also show short-time-dependent phenomena which were previously described only in the context of DNS studies over reduced-size computational domains. Short-time-dependent phenomena include pressure oscillations and time-dependence of hyporheic zone morphology, with the latter eventually extending beyond the limits of a single bedform element.

1 Introduction

Hyporheic exchange fluxes (HEF) play an important role in riverine environments as they affect streambed and river temperature dynamics (Wu et al., 2020), stream metabolism and biogeochemical cycling, with deep implications in ecosystem resilience (S. Krause et al., 2013). The spatial patterns and temporal dynamics of HEF are controlled by streambed topography and sediment properties (e.g., hydraulic conductivity patterns) and hydrodynamics and hydrostatic forcings from the surface flow. The morphology of stream bedforms and river corridor features such as meanders, ripples, dunes, gravel bars and pool-riffle structures create nested HEF patterns at the interface between surface and groundwater (S. Krause et al., 2022).

In addition to site-specific field studies (Marçais et al., 2018; Zarnetske et al., 2011; S. Krause et al., 2013; Angermann et al., 2012), the mechanisms and principal drivers of HEF have been studied in reduced-complexity flume experiments reproducing a series of triangular dunes (Fehlman, 1985; Elliott & Brooks, 1997; Salehin et al., 2004; Arnon et al., 2010; Fox et al., 2014; Blois et al., 2014), and using numerical modelling (Cardenas & Wilson, 2007a,b; Gomez et al., 2012; Jesson et al., 2013; Trauth et al., 2013; Gomez-Velez et al., 2014). The main mechanism of hyporheic exchange has been identified as the hydraulic

56 forcing of the streamflow acting on the upstream side of a dune, which causes streamwater
57 downwelling at the upstream side of the dune and upwelling further downstream.

58 Numerical models routinely follow the approach of modelling surface flow via the Navier-
59 Stokes equation, whilst groundwater flow is modelled through a Darcy solver. A limitation of
60 current approaches consists of the fact that turbulence in the surface flow is modelled through
61 time-averaging techniques (Reynolds-Averaged Navier-Stokes, RANS) which remove the de-
62 pendence of turbulent phenomena over time, instead of time-dependent approaches (viz.:
63 Large Eddy Simulations, LES)—this despite the fact that short-timed perturbations are
64 shown to affect HEF; for instance, dissolved oxygen conditions respond over time scales of
65 hours-to-days when subjected to practically instantaneous surface flow perturbations (Kauf-
66 man et al., 2017). Furthermore, with few exceptions (Li et al., 2020), surface-groundwater
67 coupling occurs one-way only, from surface to groundwater. surface flow is typically solved
68 first; then, the output pressure field across the riverbed is informed to a separate simulations
69 for groundwater flow as a boundary condition, with no mass transfer between surface and
70 groundwater flows.

71 The aim of this work is to introduce the first-ever Lattice-Boltzmann (LB) numerical
72 model, which specifically addressed the two limitations mentioned above. contrarily to the
73 work mentioned above, single numerical runs simulate both surface and groundwater flows
74 as part of the same computational domain, the difference between the two zones being
75 defined only in terms of local porosity and permeability fields. this allows simultaneous,
76 time-dependent resolution of surface and groundwater flow, as well as mass transfer. The
77 Lattice-Boltzmann methodology (Kruger et al., 2017) was adopted because of its superior
78 performance in terms of high numerical efficiency and parallelizability: indeed, previous work
79 in other disciplines shows that lattice-Boltzmann outperforms Finite-Volume analogues by
80 a factor of 100—1000 (Dapelo et al., 2019, 2020), and OpenLB’s implementation of Lattice-
81 Boltzmann (www.openlb.net) has been shown to maintain effective weak scaling over more
82 than 10,000 cores (M. J. Krause et al., 2021).

83 Results show a time-dependent variation of the morphology of the hyporheic zone, which
84 shrinks and extends possibly beyond the limits of a single beform element over short time
85 periods. This behaviour, which is attributed to the time-dependent nature of the simulations
86 presented here, was never observed in previous numerical work, and is in qualitative agree-
87 ment with complex, short-timed flow variations observed in Direct Numerical Simulations

88 (DNS) work over reduced-sized computational domains (Shen et al., 2020, 2022). Also, the
 89 pressure field across the riverbed is shown to drop smoothly leeward of the bedform element.
 90 This is in contrast to previous numerical work (Cardenas & Wilson, 2007a,b; Gomez et al.,
 91 2012; Jesson et al., 2013; Trauth et al., 2013; Gomez-Velez et al., 2014), where a sharp cusp
 92 was observed, but in agreement with historical experimental observations (Fehlman, 1985).
 93 A more recent experimental work (Blois et al., 2014) shows that sharp cusps in riverbed
 94 pressure occur when no mass exchange is allowed between surface and groundwater flows,
 95 whilst smooth drops are observed when mass exchange is allowed. The model presented
 96 here qualitatively captures this behaviour.

97 In Section 2, the model and numerical setup are presented. The results are reported in
 98 Section 3. Conclusions are reported in Section 4.

99 **2 Methods**

100 **2.1 Numerical Model**

101 *2.1.1 The Lattice-Boltzmann Method*

102 The Lattice-Boltzmann is a mesoscopic method insofar as the macroscopic observable
 103 fields (viz.: pressure p , density ρ , velocity \mathbf{u} and shear rate σ) are not solved directly; what
 104 is actually solved is a statistical quantity—the probability $f(\mathbf{x}, \mathbf{c}, t)$ of finding an abstract
 105 particle-like portion of fluid with position within $[\mathbf{x}, \mathbf{x} + \delta\mathbf{x}]$, velocity within $[\mathbf{c}, \mathbf{c} + \delta\mathbf{c}]$ and
 106 at a time within $[t, t + \delta t]$. Then, the macroscopic observable fields are calculated as f 's
 107 first three momenta:

$$108 \quad \rho := \int f d\mathbf{c}; \quad \rho\mathbf{u} := \int f\mathbf{c} d\mathbf{c}; \quad \rho\mathbf{u} \otimes \mathbf{u} := \sigma + \int f\mathbf{c} \otimes \mathbf{c} d\mathbf{c} \quad (1)$$

109 where \otimes is the tensor product. f evolves according to a conservation equation in the phase
 110 space:

$$111 \quad (\partial_t + \mathbf{c} \cdot \nabla) f = \mathcal{C}[f] \quad (2)$$

112 where the “collision operator” \mathcal{C} accounts for inter-particle collisions. Under diluted gas
 113 conditions (which hold for riverine flows), only binary conditions are relevant. Furthermore,
 114 under the Bhatnagar-Gross-Krook (BGK) hypothesis Bhatnagar et al. (1954), binary colli-
 115 sions are assumed to occur isotropically and bear the effect of relaxing f towards a Maxwell
 116 equilibrium distribution f^{eq} :

$$117 \quad \mathcal{C}[f] = -\frac{f - f^{\text{eq}}}{\tau} \quad (3)$$

118 and f^{eq} is defined as:

$$119 \quad f^{\text{eq}}(\mathbf{x}, t) := \rho(\mathbf{x}, t) \left(\frac{1}{2\pi c_s^2} \right)^{3/2} \exp \left\{ -\frac{[\mathbf{u}(\mathbf{x}, t)]^2}{2c_s^2} \right\}, \quad (4)$$

120 where c_s is the sound speed.

121 Time and space are discretized in respectively in a succession of times of timesteps δt ,
 122 and in a cubic lattice of size δx . Velocity is discretized by allowing only a small set of discrete
 123 velocities \mathbf{c}_i , $i = 0, \dots, p - 1$, symmetrically directed from a given lattice site to its first,
 124 second or third neighbour, and with magnitude $0, \sqrt{1}, \sqrt{2}, \sqrt{3}, \dots$ times $\delta x/\delta t$. Different
 125 choices of space dimensionality and velocity discretization (schemes) are available, and are
 126 conventionally labelled as $DnQp$. After discretization, the continuous quantity $f(\mathbf{x}, \mathbf{c}, t)$ is
 127 converted to a set $f_i(\mathbf{x}, t)$, each representing the probability of finding a fluid particle at the
 128 site \mathbf{x} with velocity \mathbf{c}_i . The speed of sound c_s is proportional to $\delta x/\delta t$, with the constant
 129 of proportionality depending on the choice of lattice. Equation 1 becomes:

$$130 \quad \rho := \sum_i f_i, \quad \rho \mathbf{u} := \sum_i \mathbf{c}_i f_i, \quad \rho \mathbf{u} \otimes \mathbf{u} := \sigma + \sum_i \mathbf{c}_i \otimes \mathbf{c}_i f_i; \quad (5)$$

131 Equation 2 becomes:

$$132 \quad f_i(\mathbf{x} + \mathbf{c}_i \delta t, t + \delta t) - f_i(\mathbf{x}, t) = \mathcal{C}_i(\mathbf{x}, t); \quad (6)$$

133 and Equation 3:

$$134 \quad \mathcal{C}_i(\mathbf{x}, t) = -\frac{1}{\tau} [f_i(\mathbf{x}, t) - f_i^{\text{eq}}(\mathbf{x}, t)]. \quad (7)$$

135 The velocity discretization error is removed by writing f^{eq} as a series of Hermite polynomials.
 136 The Truncation to the second order reads as follows:

$$137 \quad f_i^{\text{eq}} = t_i \rho \left[1 + \frac{\mathbf{u} \cdot \mathbf{c}_i}{c_s^2} + \frac{(\mathbf{u} \cdot \mathbf{c}_i)^2 - c_s^2 u^2}{2c_s^4} \right] \quad (8)$$

138 and is shown through Chapman-Enskog perturbative analysis (Kruger et al., 2017) that it
 139 grants conservation of mass and momentum, and allows the reformulation of Equation 6
 140 into weakly-compressible Navier-Stokes equations (Kruger et al., 2017), with macroscopic
 141 pressure and kinematic viscosity being respectively defined as:

$$142 \quad p := \rho c_s^2, \quad \nu := c_s^2 \left(\tau - \frac{1}{2} \right) \delta t. \quad (9)$$

143 The truncation error corresponds to a small compressibility error and is proportional to
 144 Ma^2 , with $\text{Ma} \equiv |\mathbf{u}|/c_s$ being the Mach number and $|\mathbf{u}|$ the problem's velocity scale. In
 145 low-Mach number problems (such as the one presented in this work), the solution is not

146 affected by the actual value of Ma , as long as the condition $Ma \ll 1$ is observed. This allows
 147 the use of Ma , δx and δt as tuning parameters to strike the best balance between, accuracy,
 148 incompressibility and computational expense (Kruger et al., 2017).

149 **2.1.2 Representative-Elementary-Volume (REV) porosity Model for Lattice-**
 150 **Boltzmann**

151 The method described in Section 2.1.1 can be adapted to describe flows through porous
 152 media. Guo & Zhao (2002) proposed a REV model, where the pore structure is represented
 153 by a scalar field $\varepsilon(\mathbf{x}, t) \in (0, 1)$, called porosity, with $\varepsilon = 0$ representing a solid node, and
 154 $\varepsilon = 1$ a free-flowing fluid node. Guo & Zhao (2002) also introduced a Darcy force:

$$155 \quad \mathbf{F} = -\frac{\varepsilon\nu}{K}\mathbf{u}, \quad (10)$$

156 where K is the permeability coefficient. The equilibrium density function (Equation 8) is
 157 modified as follows:

$$158 \quad f_i^{\text{eq}} = t_i \rho \left[1 + \frac{\mathbf{u} \cdot \mathbf{c}_i}{c_s^2} + \frac{(\mathbf{u} \cdot \mathbf{c}_i)^2 - c_s^2 u^2}{2\varepsilon c_s^4} \right], \quad (11)$$

159 and a force term is added to the collision operator in the lattice-Boltzmann equation (Equa-
 160 tion 6):

$$161 \quad f_i(\mathbf{x} + \mathbf{c}_i \delta t, t + \delta t) - f(\mathbf{x}, t) = \mathcal{C}_i(\mathbf{x}, t) + \Phi_i \delta t. \quad (12)$$

162 The force term Φ_i is defined as follows:

$$163 \quad \Phi_i = t_i \rho \left(1 - \frac{1}{2\tau} \right) \left[\frac{\mathbf{F} \cdot \mathbf{c}_i}{c_s^2} + \frac{(\mathbf{u} \cdot \mathbf{c}_i)(\mathbf{F} \cdot \mathbf{c}_i) - c_s^2 \mathbf{u} \cdot \mathbf{F}}{\varepsilon c_s^4} \right]. \quad (13)$$

164 The fluid velocity is no longer the first-order momentum density as it was in Equation 5.
 165 Rather, it is defined as:

$$166 \quad \mathbf{u} := \sum_i \mathbf{c}_i f_i + \frac{1}{2} \rho \mathbf{F} \delta t. \quad (14)$$

167 Through a Chapman-Enskog expansion and the approximation of constant density,
 168 from the model described above it is possible to recover the following governing equations:

$$169 \quad \begin{aligned} \nabla \cdot \mathbf{u} &= 0, \\ \partial_t \mathbf{u} + (\mathbf{u} \cdot \nabla) \frac{\mathbf{u}}{\varepsilon} &= -\nabla(\varepsilon p) + \nu \nabla^2 \mathbf{u} + \mathbf{F}. \end{aligned} \quad (15)$$

170 Equations 15 were proposed by Nithiarasu et al. (1997) to describe flow through porous
 171 media of both constant and variable porosity. Equations 15 reduces to the Navier-Stokes
 172 equations when $\varepsilon \rightarrow 1$. It is also easy to recognise terms reproducing Darcy (Equation 10,
 173 first term on the right side), Brinkmann (Equation 15, second term on the right side) and

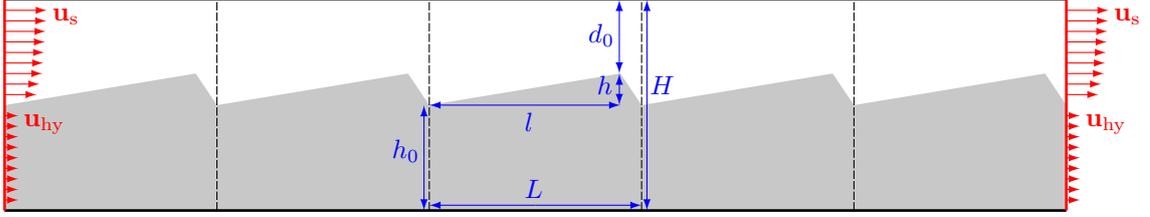


Figure 1: Schematic representation and boundary conditions of the computational domain. Bottom: no slip. Top: free slip. Leftmost and rightmost vertical boundaries: constant velocity.

174 Forchheimer (Equation 10, second term on the right side) models. This makes the model
 175 capable of describing free flow as well as flow through porous media with flexibility especially
 176 in the case of varying porosity, eventually capturing the effects of solid boundaries (through
 177 the Brinkmann component), or of non-linear drag (Forchheimer).

178 2.2 Meshing

179 2.2.1 Physics and Geometry

180 Two two-dimensional computational domains were defined as in Figure 1. The domain
 181 consisted of a succession of five identical dunes in order to mimic an infinite domain. The
 182 third dune was considered to be far away enough from the inlet and outlet to ignore boundary
 183 effects, and was used for the numerical predictions. In each lattice node, the values of the
 184 particle density functions f_i were stored as described in Section 2.1.1. In addition, each cell
 185 also contained the values of the porosity ε and the permeability K as scalar fields. The
 186 porosity field was defined in such a way to model a succession of dunes (filled in grey in
 187 Figure 1) overlaid by a free-flowing water column. The geometry of the dunes is reported
 188 in Table 1, and follows Gomez-Velez et al. (2014).

189 Following Pamuk & Özdemir (2012), porosity and permeability were chosen as $\varepsilon = 0.35$
 190 and $K = 10^{-10} \text{ m}^2$ to reproduce the characteristics of sand. The kinematic viscosity of water
 191 was set to $10^{-6} \text{ m}^2/\text{s}$ for the sake of simplicity. This value approximates the water kinematic
 192 viscosity at 20 °C of $1.004 \cdot 10^{-6} \text{ m}^2/\text{s}$ with a difference of less than 0.5%. The Reynolds

Table 1: Domain geometry.

L	(m)	1
l/L	(-)	0.9
h/L	(-)	0.075
d_0/L	(-)	0.425

193 number rw was $\sim 10^5$ and, consequently, a turbulence model was needed. A Smagorinsky
 194 large eddy simulations model (Hou et al., 1996) was adopted to reproduce the effect of
 195 turbulence. Cardenas & Wilson (2007a) used a definition of the Reynolds number where
 196 h is the relevant length scale. This choice may have been driven by the observation that
 197 the largest vortices appearing in the average figure (Figure 3) are apparently of the size of
 198 h . However, the correct reference length scale to define the Reynolds number is the one
 199 at which the gradients relevant to the problem occur (Kruger et al., 2017). Channel flow
 200 in average follows a sixth-power law, with horizontal gradients changing uniformly across
 201 the whole depth of the surface flow d_0 . As such, d_0 and not h should be considered as the
 202 relevant length scale to define the Reynolds number.

203 The inlet surface average velocity was set to $u_s = 0.3$ m/s, corresponding to a Froude
 204 number of 0.15. u_{hy} assumed the values of $5 \cdot 10^{-7} u_s$, $10^{-6} u_s$, $2 \cdot 10^{-6} u_s$, $5 \cdot 10^{-6} u_s$, $10^{-5} u_s$,
 205 $2 \cdot 10^{-5} u_s$, $5 \cdot 10^{-5} u_s$, $10^{-4} u_s$. The choice of these value is justified *a posteriori* by the fact
 206 that they allow to capture a qualitative change in the hyporheic zone morphology.

207 The boundary conditions consisted of a non-periodic domain with constant velocity at
 208 the inlet and the outlet defined according to a sixth power with average velocity u_s law in
 209 the surface zone, and a constant value u_{hy} in the hyporheic zone:

$$210 \quad u = \begin{cases} u_{hy} , & 0 \leq d \leq h_0 ; \\ \left(\frac{d - h_0}{H - h_0} \right)^{1/6} u_s , & h_0 < d \leq H . \end{cases} \quad (16)$$

211 **2.2.2 Numerical Setup**

212 The D2Q9 lattice scheme was adopted. In such a scheme, four horizontal velocities
 213 (pointing to the first neighbours), four diagonal (to the second neighbours) and a zero
 214 velocity are defined, and the lattice sound speed is $\delta x / (\sqrt{3} \delta t)$.

215 The implementation of the model described in Section 2.1.2 produced a stepwise vari-
 216 ation of the porosity field ε across the dune slopes; this, in turn, resulted into unphysical
 217 oscillations of the instant values of the pressure across the riverbed with a period of the
 218 order of magnitude of the step's amplitude. To minimise this effect, a fine grid was needed,
 219 an accordingly, a regular grid with 800 nodes per metre was adopted, with an overall node
 220 number of 6.4 million. furthermore, the choice of adopting a low value for K meant that
 221 groundwater velocity magnitude was several orders of magnitude smaller than in the sur-
 222 face stream. As such, the truncation error described in Section 2.1.1 (and consequently,
 223 the Mach number Ma) needed to be kept as low as possible. As such, the time step δt
 224 was chosen in such a way that $u_s = 0.01 \delta x / \delta t$, thus obtaining $Ma = 0.0173 \ll 1$. Each
 225 simulation was run in parallel on four to five dual-processor 8-core 64-bit 2.2 GHz Intel
 226 Sandy Bridge E5-2660 worker nodes with 32 GB of memory, for a total of 62 and 80 nodes
 227 respectively. Each run required 30 to 60 hours of real time. Furure work will reduce the
 228 present model's computational demand by: *(i)* introducing a smooth surface-groundwater
 229 transition for the porosity field ε , thus reducing unphysical pressure oscillations across the
 230 riverbed and, consequently, the need for fine grids; and *(ii)* adopting higher values for K ,
 231 as in Blois et al. (2014).

232 60 to 210 s of simulated time were reproduced to keep track of the long-term behaviour
 233 of the computational model. Then, the initial transient period, consisting of the first 10 s of
 234 simulated time, was discarded, and the remaining time steps were averaged node by node
 235 to produce an averaged velocity field for post-processing.

236 **3 Results and Discussion**

237 **3.1 Grid convergence**

238 Grid independence was assessed on an *ad hoc* modified version of the setting described in
 239 Section 2.2: where more meshes are considered (viz.: with 1130, 800, 566 and 400 grid points
 240 per metre respectively), the choice of u_{hy} was limited to $10^{-6} u_s$, and the computational
 241 domain was enlarged to 6 dunes, the third of which was considered for the test results. The
 242 Grid Convergence Index (GCI) test (Roache, 1994; Celik et al., 2008) was performed on the
 243 measure of the hyporheic depth. The results of the test showed that grid independence was
 244 achieved across all the four meshes, that the mesh with 800 grid points per metre was the

245 best compromise between accuracy and numerical expense, and that the relative error in
 246 results produced through that grid was about 3%.

247 3.2 Pressure propagation through the Riverbed

248 Figure 2 shows the pressure propagation through the riverbed surface for $u_{hy} = 10^{-6} u_s$.
 249 The pressure profile is obtained by averaging the instantaneous values of the pressure at each
 250 point of the riverbed over 200 s, as per in Section 2.2.2) and then, compared to literature
 values previously reported by Gomez-Velez et al. (2014) (Figure 2, left). Pressure oscillations

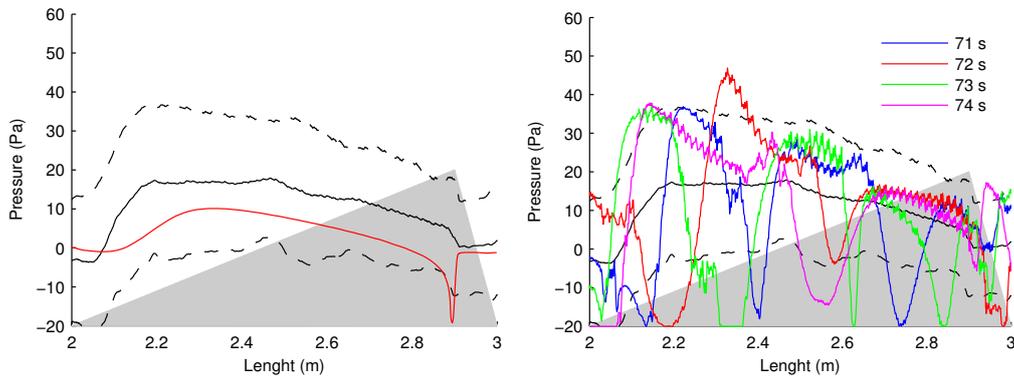


Figure 2: Pressure through the riverbed. Left: average (black) plus and minus standard deviation (dashed); Comparison with literature data of Gomez-Velez et al. (2014) (red). Right: timestep snapshots at 71, 72, 73 and 74 s.

251 were observed as described in Section 2.2.2, but their magnitude was reduced if compared to
 252 the main trend. The simulation results display a strong time-dependence, as shown by the
 253 large standard deviation, and the example timesteps reported in Figure 2, right. Simulation
 254 results show a smooth pressure drop leeward of the bedform, like the experimental results
 255 of Fehlman (1985). In contrast, previous numerical work (Cardenas & Wilson, 2007a,b;
 256 Gomez et al., 2012; Jesson et al., 2013; Trauth et al., 2013; Gomez-Velez et al., 2014; Lee et
 257 al., 2021) display a sharp peak (the result from Gomez-Velez et al. (2014) are reported in
 258 Figure 2 as an example).

260 This qualitatively different behaviour may be explained considering the results of the
 261 experiments conducted by Blois et al. (2014). It is therein shown that a sharp peak occurs
 262 when no mass exchange between surface and groundwater flows is allowed (as in the above-

263 mentioned previous numerical work); by contrast, even a tiny exchange flow is shown to
 264 smooth out the sharp peak into a smooth pressure drop (as in the numerical results reported
 265 within this article). This hypothesis is corroborated by the experimental observation (Blois
 266 et al., 2014) that surface-groundwater mass exchange prompts qualitatively different surface
 267 flow patterns leeward of the bedform element, if compared to the case where no exchange flow
 268 is allowed (viz.: flow reattachment does not occur). Groundwater flow in Blois et al. (2014)
 269 occurs through coarse sediments modelled as a cubical lattice of spherical spheres of 1 cm
 270 diameter, corresponding to a porosity $\varepsilon = 1 - \pi/6 = 0.476$, of the same order of magnitude of
 271 the porosity considered within this work, and a permeability of $K = \varepsilon^3 D^2 / [150 (1 - \varepsilon)^2] =$
 272 $3.797 \cdot 10^{-6} \text{ m}^2$, around four orders of magnitude larger than the permeability used within
 273 this study. As such, this study suggest that Blois et al. (2014)'s conclusions apply at least
 274 to a certain extent, to much finer sediments.

275 3.3 Velocity Patterns and Hyporheic depth

276 Figure 3 reports the average flow patterns of surface (top row) and hyporheic flow (bot-
 tom row). The averaging procedure was performed as per in Section 2.2.2. HEF patterns

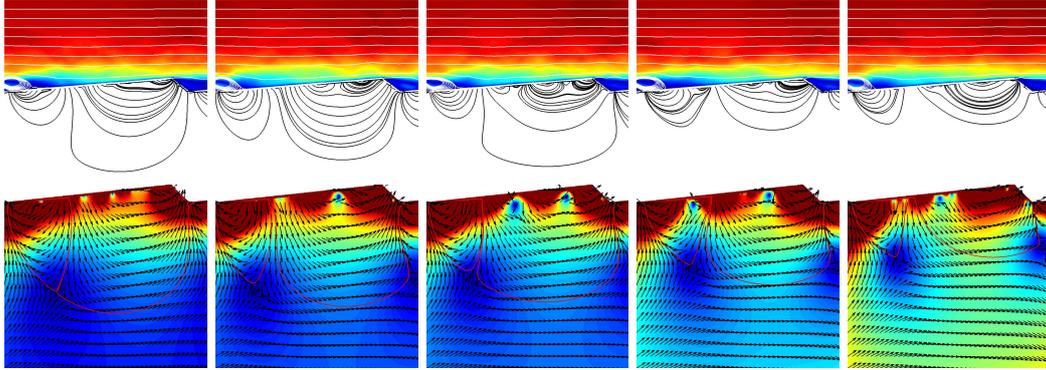


Figure 3: Fluid flow average figure. Top row: surface velocity magnitude and surface-hyporheic streamlines, velocity cutoff: 0.6 m/s. From left to right: $u_{\text{hy}} = 5 \cdot 10^{-6} u_s$, $u_{\text{hy}} = 10^{-5} u_s$, $u_{\text{hy}} = 2 \cdot 10^{-5} u_s$, $u_{\text{hy}} = 5 \cdot 10^{-5} u_s$, $u_{\text{hy}} = 10^{-4} u_s$. Bottom row: Patterns of hyporheic flow velocity and limits of the hyporheic zone, velocity cutoff: 10^{-5} m/s . From left to right: $u_{\text{hy}} = 5 \cdot 10^{-7} u_s$, $u_{\text{hy}} = 10^{-5} u_s$, $u_{\text{hy}} = 2 \cdot 10^{-5} u_s$, $u_{\text{hy}} = 5 \cdot 10^{-5} u_s$, $u_{\text{hy}} = 10^{-4} u_s$.

277 are in general agreement with those previously reported by using other modelling method-
 278 ologies, such as in Cardenas & Wilson (2007a). The surface flow simulated in this study
 279

280 displays a certain degree of regularity, with (turbulent) horizontal flow and velocity increas-
 281 ing with the height from the bottom; a persistent vortex is present after the tip of the dune,
 282 with an apparent flow separation. No dependence on u_{hy} is visible.

283 The hyporheic flow patterns indicate the existence of a down-welling point at around
 284 1/3 of the dune slope before the tip, and a diffuse up-welling zone in the receding zone after
 285 the tip of the dune. Curved streamlines connect the down-welling point and the up-welling
 286 zone, with the flow patterns becoming less intensive as the depth increases.

287 No perceivable or weak dependence on u_{hy} is visible as long as $u_{\text{hy}} \lesssim 2 \cdot 10^{-5} u_{\text{s}}$. Above
 288 that value, the increase of u_{hy} produces an intensification of the hyporheic flow patterns. At
 289 the same time, the hyporheic zone contracts. This observation above is corroborated by the
 290 quantitative calculations of hyporheic depth, area, velocity and residence time. The data are
 291 reported in Table 2 and plotted in Figure 4. Below the threshold value of $u_{\text{hy}} \lesssim 2 \cdot 10^{-5} u_{\text{s}}$,
 292 hyporheic velocity displays fluctuations, while hyporheic depth, area and residence time
 293 show a weak descending trend. Above such threshold, all the quantities present a strong
 descending trend.

Table 2: Hyporheic depth, area of the hyporheic zone, average hyporheic velocity and average residence time. $u_{\text{hy}} = 10^{-6} u_{\text{s}}$.

u_{hy}	d_{hy}	A_{hy}	$\langle v \rangle_{\text{hy}}$	$\langle t \rangle_{\text{hy}}$
	(m)	(m ²)	(mm/s)	(days)
$5 \cdot 10^{-7} u_{\text{s}}$	0.469	0.412	0.506	1,150
$10^{-6} u_{\text{s}}$	0.483	0.426	0.472	1,190
$2 \cdot 10^{-6} u_{\text{s}}$	0.478	0.423	0.436	1,080
$5 \cdot 10^{-6} u_{\text{s}}$	0.453	0.403	0.482	1,110
$10^{-5} u_{\text{s}}$	0.439	0.392	0.501	935
$2 \cdot 10^{-5} u_{\text{s}}$	0.420	0.387	0.502	997
$5 \cdot 10^{-5} u_{\text{s}}$	0.348	0.303	0.588	621
$10^{-4} u_{\text{s}}$	0.232	0.207	0.982	434

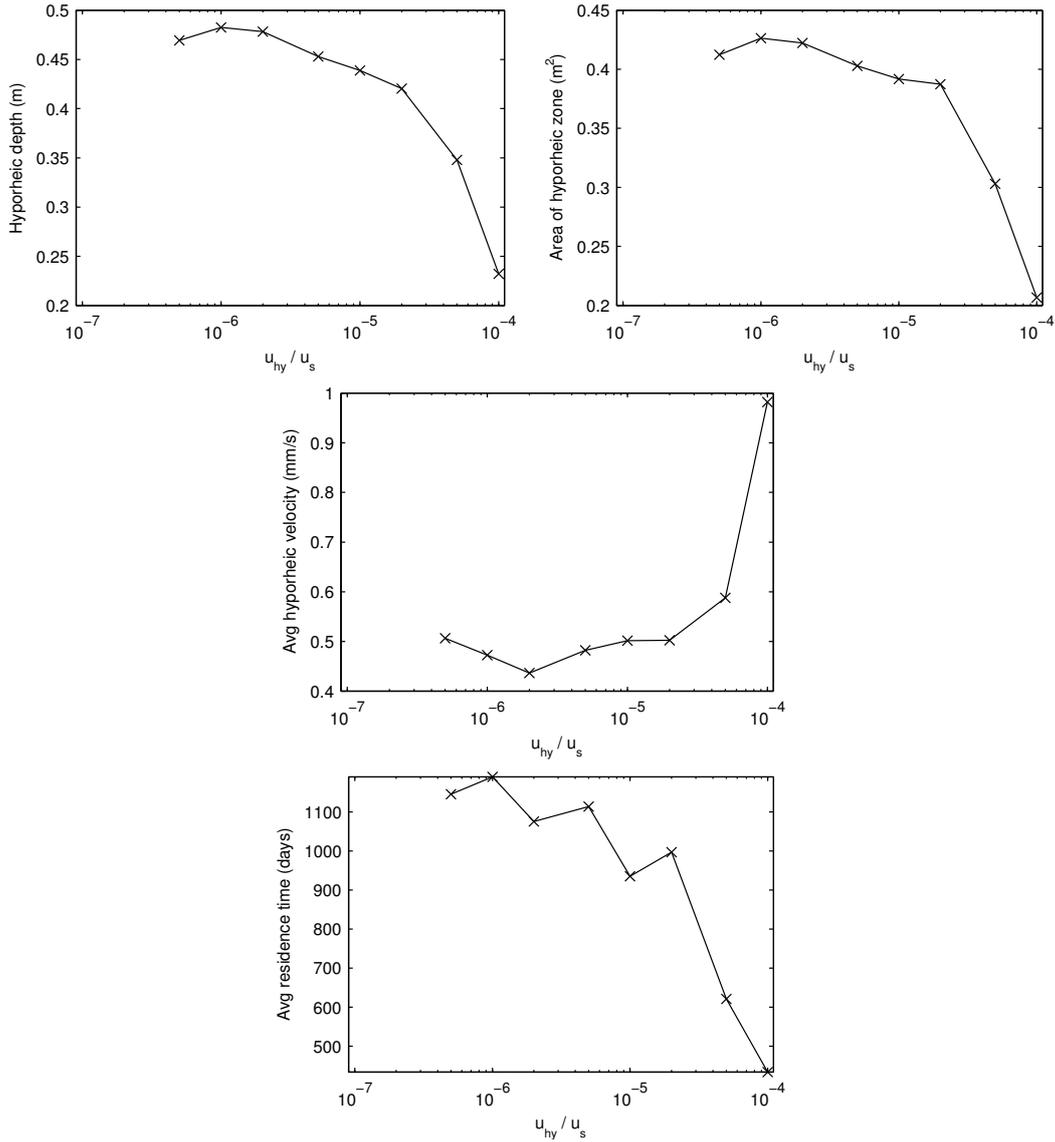


Figure 4: Hyporheic hepth, area of hyporheic zone, average hyporheic velocity and average residence time against u_{hy} to u_s ratio. Logarithmic plot. $u_{hy} = 10^{-6} u_s$.

295 It is clear that the choice of how to set the magnitude of the hyporheic boundary velocity
 296 \mathbf{u}_{hy} affects the outcome of the simulations, for higher velocities as the hyporheic zone is
 297 “squeezed” by an external horizontal flux, as can be seen from Figure 3. In this context, the
 298 meaning of “higher velocities” and, conversely, “lower velocities”, is provided by comparing
 299 the choice of u_{hy} to the values of the average hyporheic velocity. More precisely, “higher”
 300 values of u_{hy} means “ u_{hy} larger than 1/10 of the average hyporheic velocity”.

301

3.4 Time-Dependant Evolution and Turbulence

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In Figure 5, the time evolution of the hyporheic depth and the area of the hyporheic zone are reported. The behaviour of the case $u_{hy} = 10^{-6} u_s$ has been reported as an example

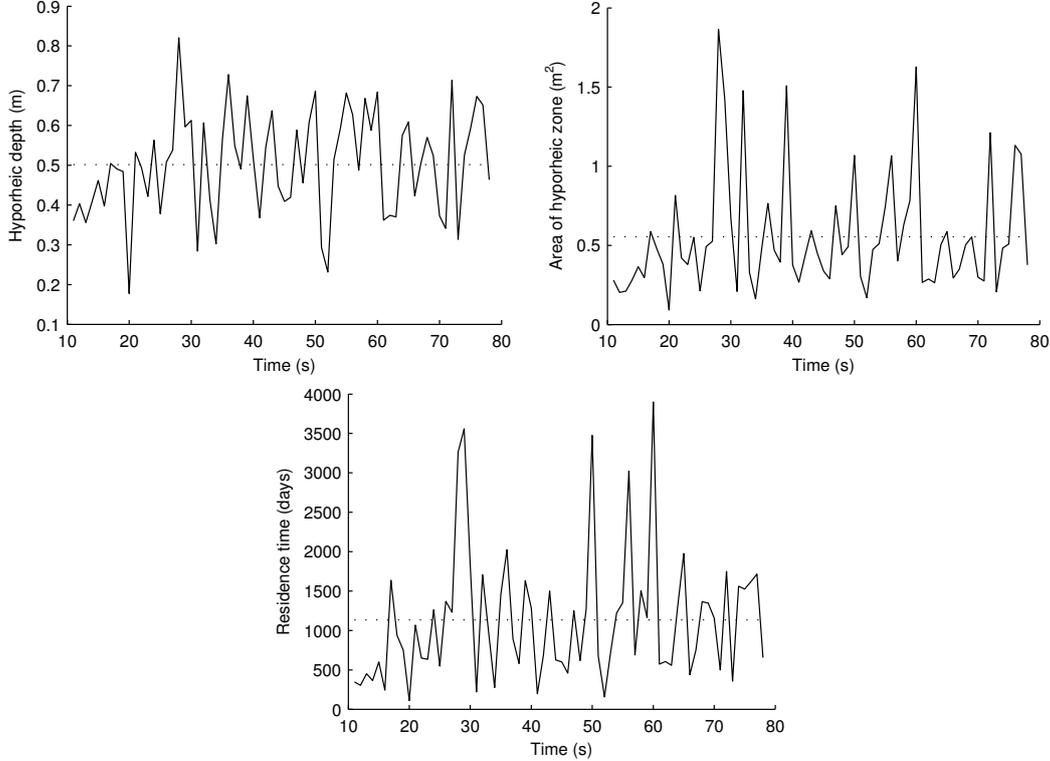


Figure 5: Hyporheic depth, area of hyporheic zone and residence time over time. $u_{hy} = 10^{-6} u_s$.

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here. The values of Hyporheic depth, area and residence time present strong oscillations over time. This suggests that the instantaneous values of hyporheic depth, area and residence time may be influenced by the time variability of the flow patterns. To corroborate this claim, the instantaneous values of the flow patterns are taken into consideration in the following part of this work.

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Figure 6 shows surface velocity magnitude and instantaneous streamlines at different time steps, while in Figure 7 the instantaneous hyporheic flow patterns are reported. Both surface and hyporheic velocity patterns display strong time dependence.

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A comparison between Figure 3 and Figures 6 shows that the instantaneous surface flow patterns are much more complex than their average field, as they comprise strong

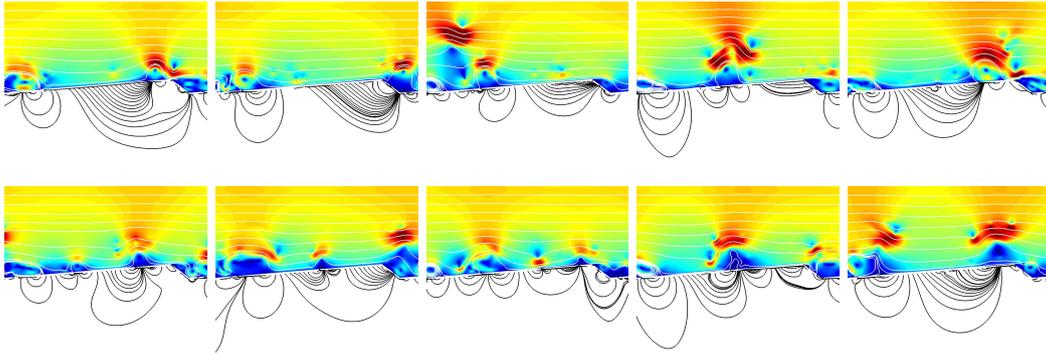


Figure 6: Surface velocity magnitude and surface-hyporheic streamlines. Velocity cutoff: 0.6 m/s. $u_{\text{hy}} = 10^{-6} u_{\text{s}}$. From left to right and from top to bottom: snapshot figures at: 11 s, 12 s, 13 s, 14 s, 15 s, 71 s, 72 s, 73 s, 74 s and 75 s.

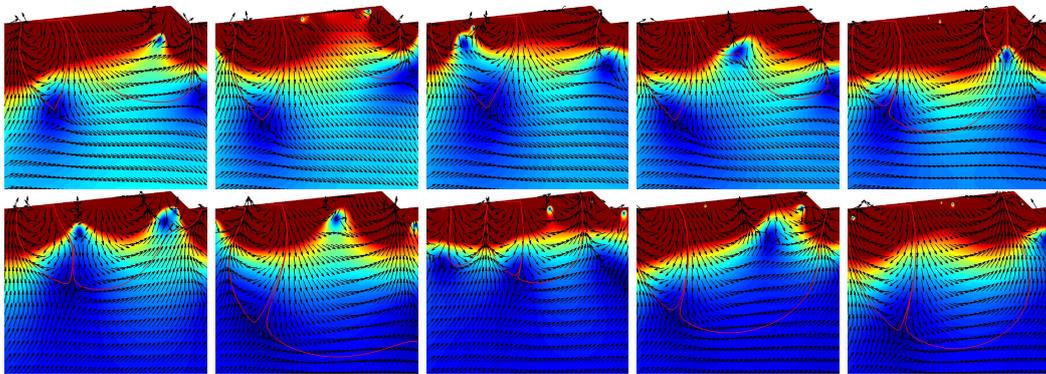


Figure 7: Hyporheic flow patterns. Velocity cutoff: 10^{-5} m/s. $u_{\text{hy}} = 10^{-6} u_{\text{s}}$. From left to right and from top to bottom: snapshot figures at: 11 s, 12 s, 13 s, 14 s, 15 s, 71 s, 72 s, 73 s, 74 s and 75 s.

314 time-dependent structures interpretable as transient vortices flowing with the stream, and
 315 unstable flow separation at the tip of the dune. In the case of average fluid flow fields (Fig-
 316 ure 3), those patterns are not apparent as they have been averaged out over the simulation
 317 period.

318 The snapshots of the hyporheic flow patterns shown in (Figure 7) reveal more similarity
 319 with the average figure (Figure 2). However, it is possible to appreciate that downwelling and
 320 upwelling points change over time—in particular, they tend to be located below transient
 321 vortices in the surface flow.

322 The deepest hyporheic structures similarly reveal time dependence. The shape of the
 323 hyporheic zone does change over time—in particular, the hyporheic zone can comprise more
 324 than one dune extending beyond a single streambed feature, as shown in Figure 8. A more
 complex structure of nested vortices and long-range connections is depicted. In conclusion,

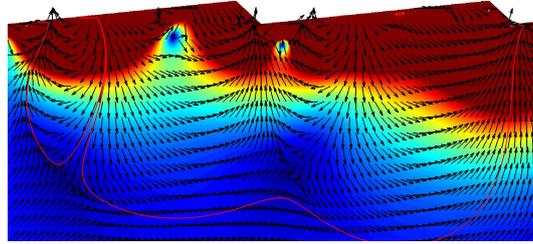


Figure 8: Hyporheic flow patterns. Velocity cutoff: 10^{-5} m/s. $u_{\text{hy}} = 10^{-6} u_s$. Snapshot figure at 72 s.

325
 326 Figure 6 and 7 show that the time-dependent turbulent structure of the surface flow in-
 327 fluences the hyporheic flow patterns significantly, and that their influence is expected to
 328 become less relevant with increasing depth. However, further work is necessary to quantify
 329 this influence.

330 4 Conclusions

331 The first-ever Lattice-Boltzmann model for hyporheic exchange fluxes across groundwater-
 332 surface water interfaces is presented. Elements of novelty include transient simulation pro-
 333 cess, and surface-groundwater two-way mass flux.

334 The introduction of surface-groundwater two-way mass flux leads to more accurate
 335 predictions of pressure across the riverbed than previous numerical models, and allows to
 336 explain the qualitative behaviour of leeway pressure drop in terms of mass flow exchange.

337 The time-dependent nature of the model allow to capture short-time-dependent fluctua-
 338 tions in hyporheic zone's area, shape, extent and average velocity, which were not previously
 339 predicted. Experimental work will be necessary to verify the accuracy of these predictions.

340 Acknowledgments

341 D.D was funded by the NERC grant NE/L003872/1 . J.D.G-V. was funded by the U.S.
 342 Department of Energy, Office of Science, Biological and Environmental Research. This

343 work is a product of two programs: (i) Environmental System Science Program, as part
344 of the Watershed Dynamics and Evolution (WADE) Science Focus Area (SFA) at ORNL
345 and the IDEAS-Watersheds project, and (ii) Data Management Program, as part of the
346 ExaSheds project. Additional support was provided by the National Science Foundation
347 (awards EAR-1830172, OIA-2020814, and OIA-2312326). The code implemented for the
348 analysis is publicly available under GNU GPL 2.0 license in the Supplementary Material.

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