

# Correcting for artificial heat in coupled sea ice perturbation experiments

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## Keywords

Sea ice, climate models, polar amplification

## Abstract

A common approach to assessing how polar amplification affects lower latitude climate is to perform coupled ocean-atmosphere experiments in which sea ice is perturbed to a future state. A recent critique by M. England and others uses a simple 1-dimensional energy balance model (EBM) to show that sea ice perturbation experiments add artificial heat to the climate system. We explore this effect in a broader range of models and suggest a technique to correct for the artificial heat post-hoc. Our technique successfully corrects for artificial heat in the EBM and a possible generalization of this approach is developed to correct for artificial heat in an albedo modification experiment in a comprehensive earth system model. However, this technique can not be directly generalized to sea ice perturbation methodologies that employ a “ghost flux” seen only by the sea ice model. Applying the correction to the comprehensive albedo modification experiment, we find stronger artificial warming than in the EBM. Failing to account for the artificial heat also leads to overestimation of the climate response to sea ice loss, and can suggest false or artificially strong “tugs-of-war” between low latitude warming and sea ice loss over some fields, for example Arctic surface temperature and zonal wind.

# 1 Introduction

Arctic amplification and sea ice loss are robustly observed features of recent climate change (Stroeve et al., 2012; Sumata et al., 2023), and are expected to continue. In addition to local impacts, Arctic amplification has consequences for lower latitude climate (Cohen et al., 2014; Screen et al., 2018; Shaw & Smith, 2022). Coupled climate model simulations in which the interactive sea ice model is constrained to a target state (e.g. corresponding to a given radiative forcing or a level of global mean warming) in the absence of greenhouse gas (GHG) forcing have been central to understanding the consequences of sea ice loss and Arctic amplification (Deser et al., 2015; Sun et al., 2020). Multiple approaches exist to constraining sea ice in a coupled model, including adding a “ghost flux” seen only by the sea ice model in grid cells where sea ice melt is desired (Deser et al., 2015), nudging the sea ice concentration to a target state at every timestep (Smith et al., 2017), and reducing the albedo of sea ice to melt it (Blackport & Kushner, 2016). We refer to methods like these, which constrain an interactive sea ice model to a state which is not in equilibrium with the climate, as *sea ice perturbation methods*. Other techniques which do not constrain the interactive sea ice model have been used to study the effect of sea ice loss in coupled models (e.g. Dai et al., 2019). These are not the focus of this study.

England et al. (2022) criticize sea ice perturbation methods categorically, arguing that they all induce artificial effects unrelated to sea ice loss. To make this argument, the authors use the one dimensional energy balance model (EBM) introduced by Wagner and Eisenman (2015). The EBM

$$\frac{\partial E}{\partial t} = aS - (A + BT) + D\nabla^2 T + F_b, \quad (1)$$

determines the evolution of upper ocean enthalpy  $E$ , which represents upper ocean heat content for temperatures above freezing and sea ice latent heat content for temperatures below freezing. In equation (1),  $a(x, T)$  is the albedo (which depends on  $x = \sin \theta$  where  $\theta$  is latitude and temperature  $T$ ),  $S$  is the incoming shortwave flux,  $A + BT$  is the outgoing longwave flux,  $D$  is the diffusion coefficient for the diffusive parameterization of meridional heat transport by dynamics, and  $F_b$  is the constant heat flux from the deep ocean into the mixed layer. See section 2 for further details on the model.

48 In the annual mean (denoted  $\bar{\cdot}$ ) equilibrium, equation (1) becomes

$$0 = \bar{aS} - (A + B\bar{T}) + D\nabla^2\bar{T} + F_b. \quad (2)$$

49 If a spatially and temporally constant forcing  $F_{ghg}$  representing an increase in atmospheric GHG  
50 concentration is applied, the response (represented by  $\delta$  symbols) is determined by

$$B\delta\bar{T}_{ghg} - D\nabla^2\delta\bar{T}_{ghg} = \delta\bar{aS}_{ghg} + F_{ghg}. \quad (3)$$

51 The main argument of England et al. (2022) is that by equation (3), the true annual mean temper-  
52 ature response to a given amount of sea ice loss in this EBM is the response required to balance the  
53 increase in absorbed shortwave due to the sea ice albedo feedback, given by  $B\delta\bar{T} - D\nabla^2\delta\bar{T} = \delta\bar{aS}$ .  
54 They then implement three sea ice perturbation methods in the EBM, and show that the warming  
55 in those simulations exceeds the true warming.

56 Insight into the England et al. (2022) argument can be gained by taking the global mean (denoted  
57  $\langle\cdot\rangle$ ) of (3), and using  $\delta\langle\bar{aS}\rangle \approx (\partial\langle\bar{aS}\rangle/\partial\langle\bar{T}\rangle)\delta\langle\bar{T}\rangle > 0$  for a given spatial pattern of forcing (here the  
58 spatially constant  $F_{ghg}$ ), where the partial derivative represents the expected increase of coalbedo  
59 with temperature. In this case

$$B\delta\langle\bar{T}\rangle_{ghg} = \delta\langle\bar{aS}\rangle_{ghg} + F_{ghg} \approx (\partial\langle\bar{aS}\rangle/\partial\langle\bar{T}\rangle)\delta\langle\bar{T}\rangle + F_{ghg}. \quad (4)$$

60 It is easily shown (see the SI) that for a stable equilibrium solution to (2), it is required that

$$B > \partial\langle\bar{aS}\rangle/\partial\langle\bar{T}\rangle. \quad (5)$$

61 In a sea ice perturbation simulation,  $F_{ghg}$  is zero. The inequality (5) therefore implies that without  
62 some other heat flux, the only solution to (4) is  $\delta\langle\bar{T}\rangle = 0$ , which corresponds to no change in sea  
63 ice. To obtain a nonzero change in the sea ice state, there must be an additional forcing term on  
64 the right hand side of equation (4). From the perspective of annual mean energy balance, the role  
65 of any sea ice perturbation method is to add this additional heat flux, which we call  $F_{pert}$ . The  
66 annual mean global mean temperature response in a sea ice perturbation simulation,  $\delta\langle\bar{T}\rangle_{pert}$ , is

67 therefore the response to sea ice loss plus the additional heat flux,

$$B\delta\langle\overline{T}\rangle_{pert} = \delta\langle\overline{aS}\rangle_{ghg} + \delta\langle\overline{F_{pert}}\rangle, \quad (6)$$

68 where  $\delta\langle\overline{aS}\rangle_{ghg}$  is the change in absorbed shortwave from the GHG simulation.  $\delta\langle\overline{T}\rangle_{pert}$  therefore  
 69 exceeds the true annual mean global mean warming due to sea ice loss in this model, which would  
 70 be  $\delta\langle\overline{aS}\rangle/B$ , by  $\langle\overline{F_{pert}}\rangle/B$ . As such, all sea ice perturbation methods introduce artificial warming,  
 71 because they add an artificial heat flux in order to perturb sea ice in a climate stable to sea ice  
 72 perturbations.

73 The artificial warming effect in the EBM is illustrated in [figure 1](#). The left column shows the  
 74 radiative forcing, temperature response, and sea ice thickness response to the shortwave forcing from  
 75 the sea ice albedo feedback alone (SPECIFIED\_ALBEDO). This is the true annual mean effect of  
 76 sea ice loss in this model (see [section 2](#)). Importantly, the shortwave forcing due to a given loss of sea  
 77 ice does not achieve that same sea ice loss, again because the EBM’s equilibrium climate is stable to  
 78 perturbations in sea ice ([5](#)). The right column shows the ghost flux method implemented in the EBM  
 79 (GHOST\_FLUX). The sea ice is successfully constrained to the target state in GHOST\_FLUX, but  
 80 to achieve this an artificial heat flux has been added, and this introduces its own artificial warming.

81 In this study, we attempt to correct for the effects of artificial heat in the EBM and in coupled  
 82 model simulations via post processing using two-parameter scaling (Blackport & Kushner, [2017](#)).  
 83 This is an effort to determine what value can be recovered from the commonly employed sea ice  
 84 perturbation framework. The simulations and techniques used are outlined in [section 2](#). We present  
 85 our two-parameter pattern scaling technique for accounting for the additional heat and assess its  
 86 validity in the EBM in [section 3](#). In [section 4](#), we use the pattern scaling technique to assess the  
 87 primary effects of the additional heat in comprehensive model simulations. We summarize our  
 88 conclusions in [section 5](#).

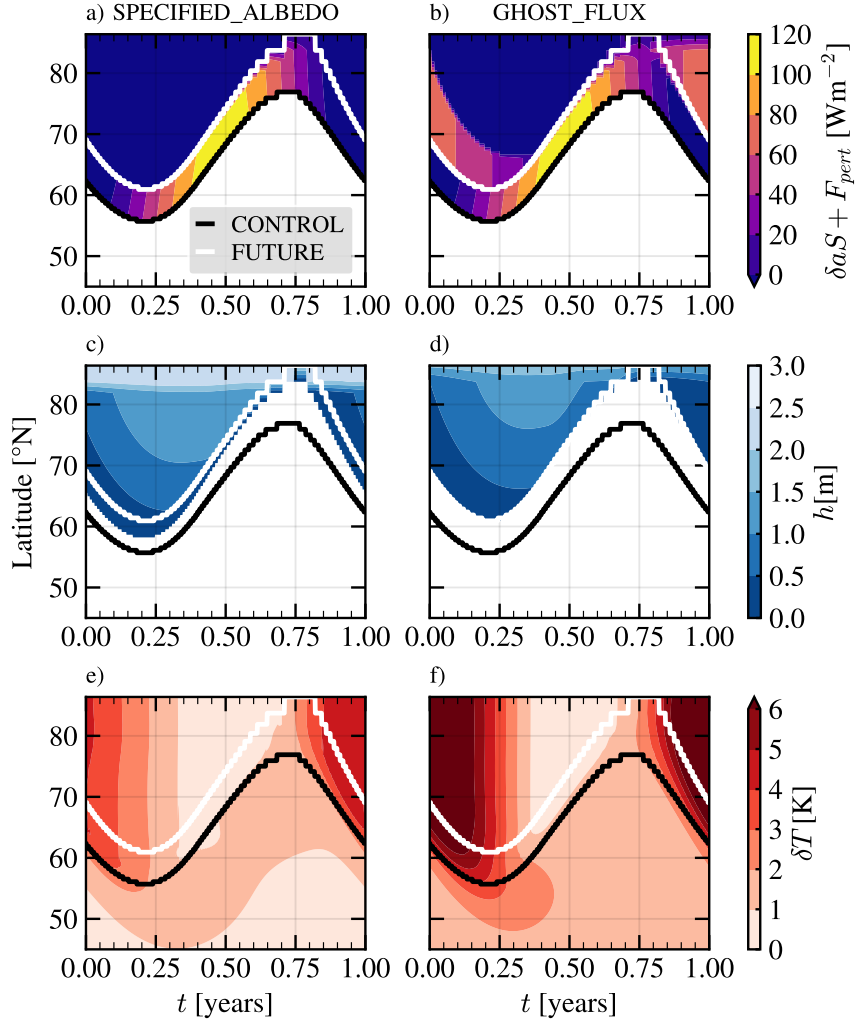


Figure 1: Left column: change in (a) sum of absorbed shortwave and additional heat flux, (c) temperature, and (e) sea ice thickness in the GHOST\_FLUX simulation in the dry EBM. Right column: same as left column but for the SPECIFIED\_ALBEDO simulation. The white (black) line displays the ice edge in CONTROL (FUTURE).

## 2 Methods

### 2.1 EBM simulations

The EBM is described comprehensively in Wagner and Eisenman (2015). Its state is determined by the surface enthalpy  $E$ , which is a convenient way of representing surface temperature  $T$  and sea ice thickness  $h$  in a single variable.

$$E = \begin{cases} T/c_w, & E \geq 0 \\ h/L_f, & E < 0 \end{cases} \quad (7)$$

Here,  $c_w$  is the specific heat capacity of the ocean,  $L_f$  is the latent heat of freezing, and  $T = 0$  is the freezing temperature of the mixed layer. The surface temperature is determined by

$$T = \begin{cases} E/c_w, & E > 0 & \text{(open water)} \\ 0, & E < 0 \text{ and } T_0 > 0 & \text{(melting)} \\ T_0, & E < 0 \text{ and } T_0 < 0 & \text{(freezing),} \end{cases} \quad (8)$$

where  $T_0$  is the surface temperature required for zero heat flux into the surface when sea ice is present (Wagner & Eisenman, 2015). We use the numerical implementation presented by Wagner and Eisenman (2015), in which the diffusive heat transport takes place in a “ghost” layer whose temperature is relaxed to the temperature of the main layer. This implementation is modified to include a global rather than hemispheric domain.

Following England et al. (2022), we run simulations in the EBM called CONTROL, FUTURE, and SPECIFIED\_ALBEDO. These and the other EBM simulations described below are run for 100 years, with data from the last year used as output. CONTROL is simply the EBM run in the default configuration with no forcing. In FUTURE, a forcing  $F_{ghg} = 3.1 \text{ W m}^{-2}$  is imposed to represent a doubling of  $\text{CO}_2$ . In SPECIFIED\_ALBEDO,  $F_{ghg} = 0.0 \text{ W m}^{-2}$  but the coalbedo  $a(x)$  is fixed to be identical to the equilibrium  $a(x)$  from FUTURE, regardless of the model’s current sea ice state (England et al., 2022). The annual mean temperature change in SPECIFIED\_ALBEDO is the model’s response to the change in absorbed shortwave  $\delta(aS)$  from FUTURE. Following the interpretation of equation (3) in England et al. (2022), we refer to the warming in SPECIFIED\_ALBEDO

as the “true” SIL-induced warming.

The simple representation of sea ice in the EBM allows for an implementation of sea ice perturbation methods. England et al. (2022) run three such simulations: NUDGING, GHOST\_FLUX, and ALBEDO\_ANNUAL (renamed DARK\_ICE in this study). We reproduce these simulations (figure 3, solid curves), a full description of which can be found in England et al. (2022). In NUDGING, the sea ice thickness is nudged to the target state with a timescale of 2.5 days. In GHOST\_FLUX, a heat flux which varies sinusoidally between  $5 \text{ W m}^{-2}$  in summer and  $65 \text{ W m}^{-2}$  in winter is applied to any ice-covered grid cell that is either ice-free or has very thin ice ( $E < -5 \text{ W m}^{-2}$ ) at the same time in FUTURE. In DARK\_ICE, the albedo of sea ice is increased from 0.4 to 0.48, which was found to roughly reproduce the annual mean change in sea ice area from FUTURE. All EBM simulations are summarized in table 1.

## 2.2 Moist EBM

One important process missing in the EBM of Wagner and Eisenman (2015) is the latent heat transported poleward by water vapor, which accounts for about half the atmospheric poleward heat transport in models and is itself a source of Arctic amplification (Feldl & Merlis, 2021). Latent heat transport can be easily be added to the EBM by changing the meridional heat transport term to diffuse moist static energy (MSE) instead of dry static energy. Following (Feldl & Merlis, 2021), we use  $s = T + c_p^{-1} H L_v q(T)$  as the MSE in units of temperature. Here  $c_p$  is the specific heat capacity of dry air at constant pressure,  $H = 0.8$  is the constant relative humidity,  $L_v$  is the latent heat of vaporization of water, and  $q(T)$  is the saturation pressure of water vapor, determined by the Clausius-Clapeyron equation. We hereafter refer to the EBM with dry static energy diffusion as the “dry EBM” and the EBM with MSE diffusion as the “moist EBM”. Parameter values for the dry EBM are identical to those in Table 1 of Wagner and Eisenman (2015). Parameter values for the moist EBM are identical to those used in Feldl and Merlis (2021), which are nearly identical to the dry EBM values except that (1)  $D$  is  $0.3 \text{ W m}^{-2} \text{ K}^{-1}$  (vs.  $0.6 \text{ W m}^{-2} \text{ K}^{-1}$  in the dry EBM), (2) the ocean mixed layer heat capacity is  $7.8 \text{ W yr m}^{-2} \text{ K}^{-1}$  (vs.  $9.8 \text{ W yr m}^{-2} \text{ K}^{-1}$  in the dry EBM), and (3) in DARK\_ICE the albedo of sea ice is increased from 0.4 to 0.52 (vs. 0.4 to 0.48 in the dry EBM). The diffusivity  $D$  is halved in the moist EBM to maintain similar total poleward energy transport across the two EBMs, because including diffusion of latent heat EBM roughly doubles the

total poleward heat transport if  $D$  is held constant. Note that the mixed layer heat capacity does not affect the global mean properties of the EBM. The coalbedo in DARK\_ICE in each of the EBMs is the value required to match the annual mean sea ice extent in FUTURE in the corresponding EBM.

### 2.3 Comprehensive model simulations

In addition to the EBM, we study the additional heat issue in two sets of comprehensive model experiments: an albedo modification experiment in the Community Earth System Model version 1 (CESM1) with the Community Atmospheric Model version 5 (CAM5), and a hybrid nudging experiment in CESM1 with the Whole Atmosphere Community Climate Model version 4 (WACCM4). A complete description of CESM1 is given in Hurrell et al. (2013) and references therein. The comprehensive simulations are summarized in table 1.

The modified albedo experiments are described in Hay (2020). Three simulations are branched from the CESM large ensemble with historical forcing at year 2000: a year 2000 control run in which all forcings are kept constant (Control), a doubled  $\text{CO}_2$  run in which the concentration of  $\text{CO}_2$  is abruptly set to 560 ppm ( $2\times\text{CO}_2$ ), and a simulation in which all forcings are constant but the albedo of snow on sea ice and bare sea ice are reduced in the northern hemisphere giving similar annual mean sea ice extent to that in  $2\times\text{CO}_2$  (“Low Albedo” in this study, referred to as “Arctic strong” in an Hay (2020)). All three simulations are run for 500 years after they are branched. We use time means over years 200 to 500 in all of the analysis presented here.

We also analyze the time slice WACCM4 hybrid nudging experiments presented in Audette and Kushner (2022), whose configurations and names follow the polar amplification model inter-comparison project (PAMIP) protocol (Smith et al., 2019). In particular, our analysis is based on a control year 2000 simulation (pa-pdSIC); a simulation in which  $\text{CO}_2$  concentration is doubled relative to 2000 and Arctic sea ice is nudged to a state corresponding to a  $2^\circ\text{C}$  warming scenario (pa-futArcSIC- $2\times\text{CO}_2$ ); and a sea ice perturbation simulation in which  $\text{CO}_2$  concentration is set to its year 2000 concentration but Arctic sea ice is nudged to the  $2^\circ\text{C}$  warming state (pa-futArcSIC). All simulations are run for 100 years, of which we use the last 40 for analysis.

Table 1: Summary of simulations used in this study.

Experiment name	GHG forcing	Arctic sea ice forcing
<i>EBM simulations</i>		
CONTROL	$F_{ghg} = 0.0 \text{ W m}^{-2}$	None
FUTURE	$F_{ghg} = 3.1 \text{ W m}^{-2}$	None
SPECIFIED_ALBEDO	$F_{ghg} = 0.0 \text{ W m}^{-2}$	Coalbedo field $a(x)$ fixed to output coalbedo field from FUTURE
DARK_ICE	$F_{ghg} = 0.0 \text{ W m}^{-2}$	Coalbedo of sea ice increased from $a_i = 0.4$ to 0.48 (dry EBM) or 0.52 (moist EBM)
GHOST_FLUX	$F_{ghg} = 0.0 \text{ W m}^{-2}$	$35 + 30 \cos(2\pi t) \text{ W m}^{-2}$ applied to ice-covered grid cells that are ice-free in FUTURE
NUDGING	$F_{ghg} = 0.0 \text{ W m}^{-2}$	$E$ relaxed to $2 \text{ W yr m}^{-2}$ with a timescale of 2.5 days in ice-covered grid cells that are ice-free in FUTURE
<i>CESM-CAM simulations</i>		
Control	$[\text{CO}_2] = 280 \text{ ppm}$	None
$2 \times \text{CO}_2$	$[\text{CO}_2] = 560 \text{ ppm}$	None
Low Albedo	$[\text{CO}_2] = 280 \text{ ppm}$	Albedo of snow on sea ice and bare sea ice reduced (Hay, 2020)
<i>CESM-WACCM simulations</i>		
pa-pdSIC	$[\text{CO}_2] = 285 \text{ ppm}$	Hybrid nudging to present day sea ice (Audette & Kushner, 2022)
pa-futArcSIC- $2 \times \text{CO}_2$	$[\text{CO}_2] = 569 \text{ ppm}$	Hybrid nudging to sea ice corresponding to $2^\circ \text{C}$ warming (Audette & Kushner, 2022)
pa-futArcSIC	$[\text{CO}_2] = 285 \text{ ppm}$	Hybrid nudging to sea ice corresponding to $2^\circ \text{C}$ warming (Audette & Kushner, 2022)

## 2.4 Pattern scaling

Our method of accounting for the additional heat flux is based upon the two-parameter pattern scaling technique developed by Blackport and Kushner (2017). Traditional pattern scaling hypothesizes that the climate response to GHG forcing scales linearly with global mean surface temperature (Tebaldi & Arblaster, 2014). Two-parameter pattern scaling extends this hypothesis to allow for independent patterns that scale with global mean surface temperature and with sea ice area. Specifically, two-parameter pattern scaling decomposes the response  $\delta Z$  to a GHG or sea ice forcing as

$$\delta Z = \left. \frac{\partial Z}{\partial T_l} \right|_I \delta T_l + \left. \frac{\partial Z}{\partial I} \right|_{T_l} \delta I, \quad (9)$$

where  $\partial Z / \partial T_l|_I$  and  $\partial Z / \partial I|_{T_l}$  are the space and time-dependent “sensitivities” to low latitude temperature  $T_l$  and sea ice area  $I$ , respectively, and the  $\delta$  symbols represent changes in those variables between a forced simulation and the control simulation. Throughout this work,  $I$  is defined as annual mean sea ice area north of 70 °N and  $T_l$  is defined as the annual mean of the 0-40 °N mean radiative surface temperature in the comprehensive models, or annual mean of the 0-40 °N mean  $T$  in the EBM. The sensitivities are calculated by assuming the responses in a sea ice perturbation experiment and a GHG forcing experiment can each be written as (9) and solving for the two sensitivities given  $\delta Z$ ,  $\delta T_l$ , and  $\delta I$  in the two simulations. This assumption is supported by the observation that responses to sea ice loss and GHG forcing imposed in isolation in sea ice perturbation experiments add relatively linearly to the response in a total GHG forcing experiment (McCusker et al., 2017). In Figures 2, 4, and 5, the sensitivities are multiplied by their associated scaling variables to compare the contributions from each effect. We refer to such fields as “partial responses”.

## 3 Correcting for the additional heat

The artificial warming effect suggests that sea ice perturbation experiments have been misinterpreted. Effects that were previously identified as responses to sea ice loss are really responses to sea ice loss plus the additional heat flux,  $F_{pert}$ . In the EBM, the temperature response to the artificial forcing is of similar magnitude to the response to sea ice loss alone. It would therefore be useful

191 if there were a way of quantifying the response to the artificial forcing, to allow the true effect of  
 192 sea ice loss to be identified. In this section, we assess whether the effect of artificial heat can be  
 193 accounted for using two-parameter scaling.

### 194 3.1 New scaling parameters

195 The solid curves in [figure 2](#) show the partial responses to sea ice loss (SIL) and low latitude warming  
 196 (LLW) calculated using EBM simulations. The top row shows the partial responses derived from  
 197 SPECIFIED\_ALBEDO, which represent the true partial responses in this model in the absence of  
 198  $F_{pert}$ . In [figure 2a](#), the partial response to LLW is spatially constant, corresponding to the LLW  
 199 that scales with the spatially constant  $F_{ghg}$ . The partial response to SIL accounts for all the spatial  
 200 structure in the total warming, a result of the fact that albedo changes are the only source of Arctic  
 201 amplification in this model, as per equation (3). All changes in the meridional temperature gradient  
 202 are therefore attributable to SIL ([figure 2b](#)).

203 The solid curves in the second row of [figure 2](#) show the partial responses to LLW and SIL  
 204 identified using DARK\_ICE instead of SPECIFIED\_ALBEDO. These differ from the true partial  
 205 responses because the temperature response in DARK\_ICE includes artificial warming due to  $F_{pert}$   
 206 in addition to the true warming caused by SIL itself. Because of the artificial warming at high  
 207 latitudes, all polar warming is attributed to SIL, with the partial response to LLW showing polar  
 208 *cooling*. These features are made clear by taking the global mean of the sensitivities (derived in the  
 209 SI),

$$\begin{aligned}\frac{\partial \langle \bar{T} \rangle}{\partial T_l} &\approx \frac{B^{-1} (F_{ghg} - \langle \bar{F}_{pert} \rangle)}{\delta T_{l,F}} \\ \frac{\partial \langle \bar{T} \rangle}{\partial I} &\approx \frac{B^{-1} (\delta \langle \bar{a} S \rangle + \langle \bar{F}_{pert} \rangle)}{\delta I}.\end{aligned}\tag{10}$$

210 The warming induced by the perturbation flux,  $\langle \bar{F}_{pert} \rangle / B$ , is attributed to sea ice loss. This arti-  
 211 ficially increases  $\partial \langle \bar{T} \rangle / \partial I$  and artificially decreases  $\partial \langle \bar{T} \rangle / \partial T_l$ . Locally, the effect is greatest at the  
 212 pole, where  $F_{pert}$  is greatest, as seen in [figure 2c](#).

213 This suggests that we should replace the scaling parameter  $I$  with a variable that accounts for  
 214 both SIL and the artificial heat flux. In the EBM, a good candidate is the total ice-related radiative  
 215 forcing,  $F_{ice} = \delta a S + F_{pert}$ . We also replace  $T_l$  (which is meant to capture the direct response to  
 216 GHG forcing) by  $F_{ghg}$ , the direct GHG forcing itself. The annual mean global mean sensitivities to

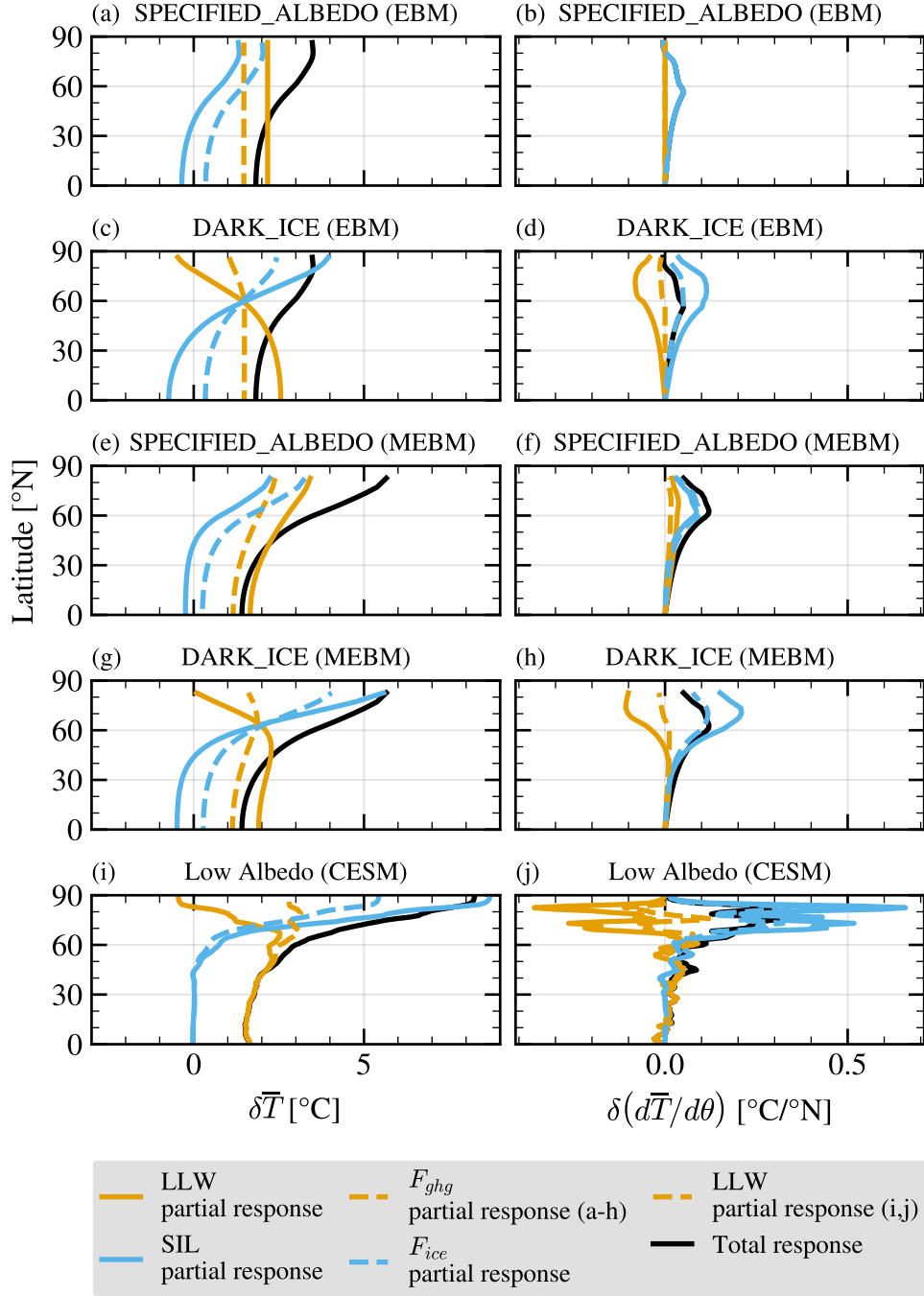


Figure 2: Black: Annual mean of response of surface temperature (left column) and its meridional gradient (right column) in the dry EBM (a-d), the moist EBM (e-h), and the CESM Low Albedo perturbation (i,j) experiments. In (a-h) colored curves show the decomposition of the response into partial responses using two pattern scaling approaches: solid blue and gold show the decomposition into LLW and SIL effects, and dashed blue and gold show the decomposition into  $F_{ghg}$  and  $F_{ice}$  effects. In (i,j), solid curves show the decomposition into LLW and SIL effects, and the dashed curves show the decomposition into LLW and  $F_{ice}$  effects.

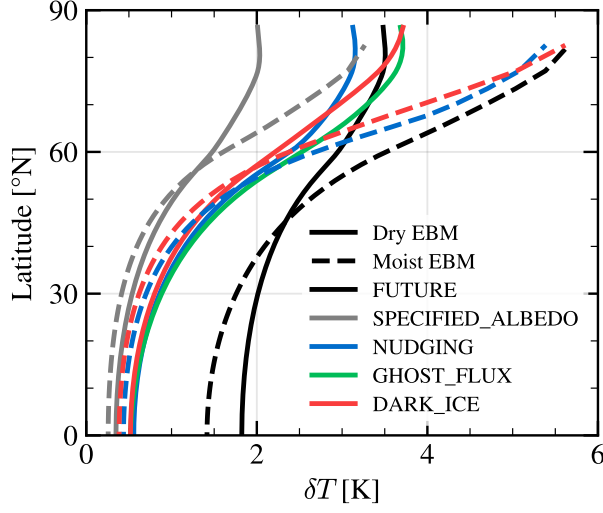


Figure 3: Annual mean temperature change in the dry (solid) and moist (dashed) EBM in the FUTURE (black), SPECIFIED\_ALBEDO (grey), and sea ice perturbation (coloured) simulations.

these new parameters (also shown in the SI) are

$$\begin{aligned} \frac{\partial \langle \bar{T} \rangle}{\partial F_{ghg}} &= \frac{B^{-1} F_{ghg}}{F_{ghg}} = \frac{1}{B} \\ \frac{\partial \langle \bar{T} \rangle}{\partial F_{ice}} &= \frac{B^{-1} (F_{pert} + \delta a S)}{F_{pert} + \delta a S} = \frac{1}{B}. \end{aligned} \quad (11)$$

Both global mean temperature sensitivities are equal to  $B^{-1}$ , as expected for the global mean temperature response to any radiative forcing in the EBM.

The partial responses to  $F_{ghg}$  and  $F_{ice}$  are shown as dashed lines in figure 2. In the dry EBM, the partial responses to these new variables in DARK ICE (second row) are closer to the true partial responses in the EBM (top row). Notably, the partial response to  $F_{ghg}$  is nearly latitudinally constant (figure 2c), and the partial response to  $F_{ice}$  accounts for nearly all of the latitudinal structure in the total response. Accounting for  $F_{pert}$  does not change the partial responses from SPECIFIED\_ALBEDO in any meaningful way: the new partial responses are simply constant offsets of the original partial responses. This is not related to accounting for  $F_{pert}$ , but a consequence of using  $F_{ghg}$  instead of  $T_l$ .

### 3.2 Moist effects in the EBM

As discussed in [section 2](#), an important process missing in the EBM is that of latent heat transport by water vapor. We implement the DARK\_ICE and SPECIFIED\_ALBEDO simulations in the moist EBM. The annual mean warming in the moist EBM simulations is shown in [figure 3](#). The key result of England et al. (2022) is essentially unchanged in the moist EBM: the warming in the sea ice perturbation simulations is a factor of 1.5-2 greater than the true warming due to sea ice loss alone. All simulations show more polar amplification in the moist EBM than in the dry EBM, because MSE transport is an additional mechanism for polar amplification (Flannery, 1984).

The third row of [figure 2](#) shows the true temperature partial responses in the moist EBM. The partial response to SIL is similar across the dry and moist EBMs. There is an interesting difference in the LLW partial response across the models: because MSE transport increases under global warming, the partial response to LLW shows polar amplification in the moist EBM ([figure 2e](#)). Thus, both SIL and LLW contribute to polar amplification in the moist EBM.

The partial responses from the DARK\_ICE simulation in the moist EBM are shown in the fourth row of [figure 2](#). As in the dry EBM, before the additional heat is accounted for SIL takes credit for all the polar warming, which requires the partial response to LLW to be small or negative at high latitudes ([figure 2h](#)) and gives a large cancellation in the meridional gradients of the two partial responses ([figure 2i](#)). Dashed curves again show partial responses to  $F_{ghg}$  and  $F_{ice}$ , which account for the additional heat as in the dry EBM (11). These partial responses closely resemble the true ones. Most importantly, the cancellation in the meridional gradients has disappeared. In principle, both partial responses should show some polar amplification, such that the polar amplification in the total response is partially attributable to both  $F_{ghg}$  and  $F_{ice}$  ([figure 2f](#)). The DARK\_ICE-derived partial response to  $F_{ghg}$  does have a small positive gradient up to 65°N, but the gradient is negative at high latitudes. This negative gradient, which is also present in the dry EBM ([figure 2d](#)) is likely due to the fact that the albedo method induces the most artificial warming ([figure 3](#)) to achieve the target sea ice state. The NUDGING simulation, which does not induce as much warming, yields partial responses which more closely resemble the true partial responses (Figure S2).

### 3.3 Comprehensive model

In CESM, we define  $F_{ice}$  to be the change in net all-sky top of atmosphere (TOA) shortwave north of 70 °N. As in DARK\_ICE, the artificial heat flux in Low Albedo is equal to the incoming shortwave that is absorbed at the surface because of the artificial reduction in sea ice albedo.  $F_{ice}$  therefore includes two sea ice related contributions: (1) a change in absorbed shortwave due to newly exposed ocean, and (2) a change in absorbed shortwave because the remaining sea ice is artificially darker. We keep low latitude temperature ( $T_l$  or LLW) as the other scaling parameter, as there is not an easily calculated analogue to  $F_{ghg}$  in the comprehensive model. The EBM results are not sensitive to the use of LLW or  $F_{ghg}$  as the scaling parameter complementary to  $F_{ice}$  (Figure S2).

The partial surface temperature responses from the CESM simulations are shown in the bottom row of [figure 2](#). They tell a similar story to the partial temperature responses in the moist EBM. Before the additional heat is accounted for, all the Arctic warming is attributed to SIL ([figure 2i](#), solid curves). The partial response to SIL therefore has a high degree of Arctic amplification, which requires tropical amplification (and in fact Arctic cooling) in the partial response to LLW. Once the additional heat is accounted for, both LLW and SIL contribute to Arctic warming and Arctic amplification ([figure 2i](#), dashed curves).

We do not have an analogue to the SPECIFIED\_ALBEDO simulation in CESM - designing such a simulation is not the purpose of this work. Therefore, we cannot diagnose the true effect of SIL in CESM. However, the similarity of the partial responses in CESM and the moist EBM suggests that similar effects determine the partial responses in both models. Namely, it appears that in CESM the partial responses to LLW and SIL contain the same artificial effects as they do in the moist EBM. Further, using  $F_{ice}$  rather than  $I$  as a pattern scaling parameter seems to properly account for the artificial effects in CESM, as it does in the moist EBM.

We also attempted to use pattern scaling with  $F_{ice}$  to account for the artificial heat flux in the WACCM hybrid nudging simulations, to less success. In the hybrid nudging method,  $F_{pert}$  is equal to the ghost flux applied to the bottom of the sea ice plus the latent heat flux implicit in removing thinnest category ice (Audette & Kushner, [2022](#)). Because both of these fluxes are “ghost” fluxes, seen only by the sea ice model itself, it is not sensible to add them on equal footing to the change in TOA shortwave. Simply taking  $F_{ice} = F_{pert} + S\delta a_{Arctic}$  as a scaling variable therefore gives

unphysical partial responses. More work would be required to determine a scaling variable that captures the correct physics in simulations that employ ghost fluxes. An in-depth discussion can be found in the SI.

## 4 Primary effects of the artificial heat

The most striking effect in [figure 2](#) is that too much Arctic amplification is attributed to SIL when the artificial heat is not accounted for. This feature is robust across all models. Sea ice perturbation experiments therefore imply a false “tug of war” (negative feedback from sea ice loss) between SIL and LLW over the meridional temperature gradient. Once the artificial heat is properly accounted for, the tug of war disappears, and both LLW and  $F_{ice}$  contribute to Arctic amplification. In the CESM Low Albedo simulations, this false tug of war is confined below 750 hPa ([figure 4d](#) compared to [figure 4b](#)). In the moist EBM, the Arctic amplification that scales with LLW is due to increased poleward transport of latent heat under global warming. In CESM, such LLW-induced Arctic amplification could be due to any number of Arctic amplification-producing feedbacks that do not scale with SIL, including but not limited to the lapse rate feedback, the Planck feedback, and increased latent heat transport.

Attributing too much Arctic amplification to SIL may similarly overestimate the role of SIL in any dynamical response related to Arctic amplification. Especially suspect is the zonal wind response. SIL is thought to induce a weakening on the poleward flank of the midlatitude jet and a strengthening on its equatorward flank, with the weakening outweighing the strengthening (Screen et al., 2018). This feature is seen in the zonal wind partial response to SIL derived from the CESM Low Albedo simulations ([figure 5b](#)). When the perturbation flux is accounted for, the partial response retains its spatial structure but decreases in magnitude by about 50%. This is interesting, considering that ocean coupling is thought to increase the strength of the zonal wind response to SIL (Deser et al., 2015). Our results suggest that at least part of the strengthening is due to the fact that the zonal wind responds to two forcings (SIL and  $F_{pert}$ ) in coupled sea ice perturbation simulations compared to only one (SIL) in atmospheric general circulation model simulations. Additionally, past analyses of sea ice perturbation simulations have found that the zonal wind partial response to LLW tends to shift the jet poleward, opposing the partial response to SIL and leading to a small

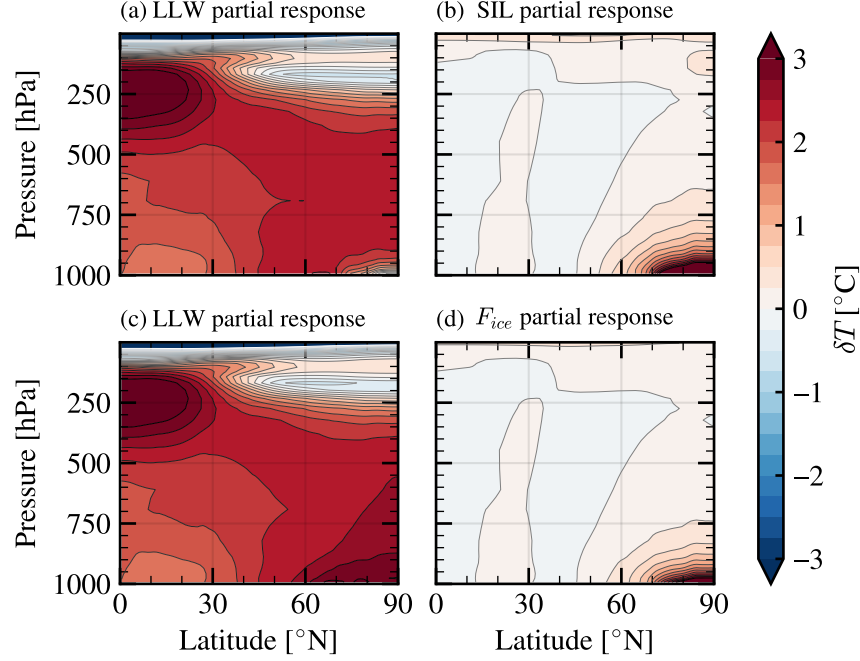


Figure 4: The annual mean zonal mean air temperature response in the 2 $\times$ CO<sub>2</sub> experiment decomposed into partial responses using two pattern scaling approaches. (a,b) show the decomposition into LLW and SIL effects, and (c,d) show the decomposition into LLW and  $F_{ice}$  effects.

312 net response (Blackport & Kushner, 2017; Hay et al., 2022). As such, it has been suggested that  
 313 there is a tug-of-war over the midlatitude zonal wind between LLW and SIL. Figure 5 demonstrates  
 314 that failing to account for the artificial heat exaggerates such tugs-of-war in pattern scaling partial  
 315 responses, suggesting a need to reinterpret this effect in previous experiments.

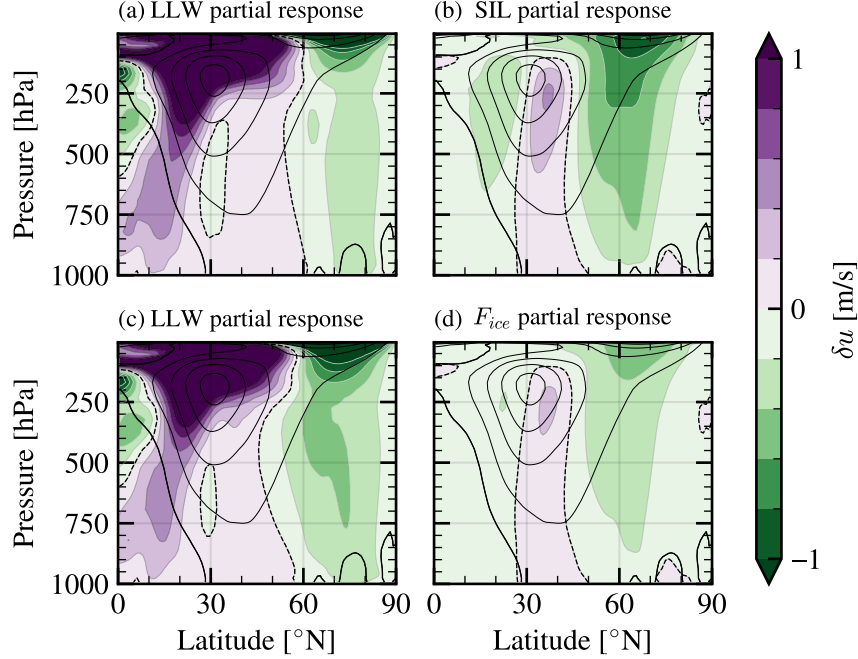


Figure 5: As in [figure 4](#), but for DJF zonal wind.

## 5 Conclusions

This study follows up on the finding that sea ice perturbation simulations induce spurious polar warming (England et al., 2022). We have confirmed this finding in a broader range of models, and explored its implications.

First, we have shown that perturbing a thermodynamic sea ice model necessarily induces artificial warming. In order to perturb sea ice, it is necessary to supply it some artificial heat flux  $F_{pert}$ . By energy balance, this requires an artificial increase in outgoing longwave radiation and therefore artificial warming. Artificial warming is therefore present in any simulation in which a thermodynamic sea ice model is constrained to a state that is out of equilibrium with the climate. Most common approaches to imposing sea ice loss in coupled models have this property and therefore induce artificial heat, including all sea ice perturbation methods as defined this study. Our results suggest that the effects of artificial heat are just as strong (if not stronger) in coupled in models as in the EBM used in England et al. (2022).

Second, we have found that the artificial effects of  $F_{pert}$  can be accounted for by using two-parameter scaling. In past studies the two scaling parameters used have been tropical sea surface temperature and Arctic sea ice area. This gives an artificially large partial response to SIL because

the response in the sea ice perturbation simulation, which is due to SIL and the artificial heat flux, is attributed entirely to SIL (equation (10)). Scaling by a different parameter,  $F_{ice}$ , that accounts for both SIL and  $F_{pert}$  corrects this unphysical behaviour, recovering the true partial responses in the EBM (equation (11)). Evaluating the pattern scaling partial responses to SIL and to  $F_{ice}$  in an albedo modification simulation in a comprehensive earth system model, we find very similar results to what we found in the EBM. This suggests that artificial warming is of similar strength in comprehensive model simulation as in the EBM, and that scaling by  $F_{ice}$  successfully accounts for the artificial effects in this simulation.

Third, we have used the new scaling parameters to diagnose the effect of the artificial heat in an EBM with and without latent heat transport, and in a comprehensive model. Accounting for the artificial heat reveals a general misinterpretation of perturbation simulations common to all models in this study. Taken at face value, sea ice perturbation simulations overestimate the role of sea ice loss in climate changes, because responses to the artificial heat flux are attributed to SIL itself. This misattribution is evident in the surface temperature response in the EBM simulations of England et al. (2022): the perturbation simulations overestimate the true annual mean surface warming by a factor of 1.5-2. We have shown that the same overestimation is present in a comprehensive model, and that it is not limited to surface temperature.

Overestimation of the role of sea ice loss by perturbation simulations suggests that some past conclusions should be questioned. For example, it has been found that ocean coupling increases the temperature and zonal wind responses to sea ice loss (Deser et al., 2015). Our results suggest that at least part of the stronger response in coupled simulations is due to the artificial heat flux applied by perturbation methods in coupled models. There is no artificial heat flux in sea ice loss simulations in atmosphere-only models, because SIL is imposed as a boundary condition. Also worthy of some question are responses over which there is a “tug-of-war” between SIL and LLW (Screen et al., 2018). The artificially large response to SIL in perturbation simulations implies an artificially diminished and potentially opposing role for LLW, if the responses to LLW and SIL sum linearly to the total climate response. In all simulations analyzed in this study, accounting for the artificial heat flux eliminates a tug-of-war over Arctic surface warming and Arctic amplification. Once the artificial heat is accounted for, both SIL and LLW contribute to Arctic surface warming and Arctic amplification. Similarly, accounting for the artificial heat reduces the magnitude of the zonal wind

partial response to SIL by about 50% in the comprehensive model, reducing its opposition to LLW. The tug-of-war paradigm is still likely a useful one, as evidence for opposing effects of Arctic surface warming and tropical warming transcends sea ice perturbation simulations (Barnes & Polvani, 2015). But our results suggest that the artificial heat added by sea ice perturbation methods exaggerates cancellations in the responses to SIL and LLW, and in some cases even introduces false cancellations.

Applying a similar pattern scaling technique to simulations where  $F_{pert}$  is a “ghost flux”, seen only by the sea ice model, would require more work. In such simulations it is likely not sensible to add  $F_{pert}$  directly to the change in TOA shortwave, because the latter is a term in the TOA energy balance, while the former is applied only to the sea ice model and therefore only indirectly affects the TOA energy balance.

We finish by noting that whether to consider the warming caused by  $F_{pert}$  as “artificial” is in part a philosophical question. As made clear by Figure 1, artificial warming is required for the climate to be consistent with the sea ice state. As such, it could be argued that the warming caused by  $F_{pert}$  is not artificial, but physically associated with sea ice loss. However, the  $F_{pert}$ -caused warming is necessary to *produce* sea ice loss; it is not a *response* to sea ice loss. Therefore, we find it more natural to attribute  $F_{pert}$ -caused warming to CO<sub>2</sub>. In this interpretation, the warming induced by  $F_{pert}$  is indeed artificial in sea ice perturbation experiments, which have no CO<sub>2</sub> forcing.

## Data and code availability

Code for running the EBM is available at <https://github.com/lukefl/ebm-icy-moist-seasonal>. Relevant output from the CESM-CAM albedo modification and CESM-WACCM hybrid nudging simulations is available at <https://borealisdata.ca/dataverse/lfl>.

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## References

- Audette, A., & Kushner, P. J. (2022). Simple hybrid sea ice nudging method for improving control over partitioning of sea ice concentration and thickness. *Journal of Advances in Modeling Earth Systems*, 14(12). <https://doi.org/10.1029/2022MS003180>
- Barnes, E. A., & Polvani, L. M. (2015). CMIP5 projections of arctic amplification, of the north american/north atlantic circulation, and of their relationship. *Journal of Climate*, 28(13). <https://doi.org/10.1175/JCLI-D-14-00589.1>
- Blackport, R., & Kushner, P. J. (2016). The transient and equilibrium climate response to rapid summertime sea ice loss in CCSM4. *Journal of Climate*, 29(2). <https://doi.org/10.1175/JCLI-D-15-0284.1>
- Blackport, R., & Kushner, P. J. (2017). Isolating the atmospheric circulation response to arctic sea ice loss in the coupled climate system. *Journal of Climate*, 30(6). <https://doi.org/10.1175/JCLI-D-16-0257.1>
- Cohen, J., Screen, J. A., Furtado, J. C., Barlow, M., Whittleston, D., Coumou, D., Francis, J., Dethloff, K., Entekhabi, D., Overland, J., & Jones, J. (2014). Recent arctic amplification and extreme mid-latitude weather. *Nature Geoscience*, 7(9). <https://doi.org/10.1038/ngeo2234>
- Dai, A., Luo, D., Song, M., & Liu, J. (2019). Arctic amplification is caused by sea-ice loss under increasing CO<sub>2</sub>. *Nature Communications*, 10(1). <https://doi.org/10.1038/s41467-018-07954-9>
- Deser, C., Tomas, R. A., & Sun, L. (2015). The role of ocean–atmosphere coupling in the zonal-mean atmospheric response to arctic sea ice loss. *Journal of Climate*, 28(6). <https://doi.org/10.1175/JCLI-D-14-00325.1>
- England, M. R., Eisenman, I., & Wagner, T. J. W. (2022). Spurious climate impacts in coupled sea ice loss simulations. *Journal of Climate*, 35(22). <https://doi.org/10.1175/JCLI-D-21-0647.1>
- Feldl, N., & Merlis, T. M. (2021). Polar amplification in idealized climates: The role of ice, moisture, and seasons. *Geophysical Research Letters*, 48(17). <https://doi.org/10.1029/2021GL094130>
- Flannery, B. P. (1984). Energy balance models incorporating transport of thermal and latent energy. *Journal of the Atmospheric Sciences*, 41(3). [https://doi.org/10.1175/1520-0469\(1984\)041<0414:EBMITO>2.0.CO;2](https://doi.org/10.1175/1520-0469(1984)041<0414:EBMITO>2.0.CO;2)

- Hay, S. (2020). *Pattern scaling methods for understanding the response to polar sea ice loss in coupled earth system models* (Doctoral dissertation). University of Toronto (Canada). Canada. Retrieved August 16, 2022, from <https://www.proquest.com/docview/2466731873/abstract/DD83F44E6C2B45D2PQ/1>
- Hay, S., Kushner, P. J., Blackport, R., McCusker, K. E., Oudar, T., Sun, L., England, M., Deser, C., Screen, J. A., & Polvani, L. M. (2022). Separating the influences of low-latitude warming and sea ice loss on northern hemisphere climate change. *Journal of Climate*, 35(8). <https://doi.org/10.1175/JCLI-D-21-0180.1>
- Hurrell, J. W., Holland, M. M., Gent, P. R., Ghan, S., Kay, J. E., Kushner, P. J., Lamarque, J.-F., Large, W. G., Lawrence, D., Lindsay, K., Lipscomb, W. H., Long, M. C., Mahowald, N., Marsh, D. R., Neale, R. B., Rasch, P., Vavrus, S., Vertenstein, M., Bader, D., . . . Marshall, S. (2013). The community earth system model: A framework for collaborative research. *Bulletin of the American Meteorological Society*, 94(9). <https://doi.org/10.1175/BAMS-D-12-00121.1>
- McCusker, K. E., Kushner, P. J., Fyfe, J. C., Sigmond, M., Kharin, V. V., & Bitz, C. M. (2017). Remarkable separability of circulation response to arctic sea ice loss and greenhouse gas forcing. *Geophysical Research Letters*, 44(15). <https://doi.org/10.1002/2017GL074327>
- Screen, J. A., Deser, C., Smith, D. M., Zhang, X., Blackport, R., Kushner, P. J., Oudar, T., McCusker, K. E., & Sun, L. (2018). Consistency and discrepancy in the atmospheric response to arctic sea-ice loss across climate models. *Nature Geoscience*, 11(3). <https://doi.org/10.1038/s41561-018-0059-y>
- Shaw, T. A., & Smith, Z. (2022). The midlatitude response to polar sea ice loss: Idealized slab-ocean aquaplanet experiments with thermodynamic sea ice. *Journal of Climate*, 35(8). <https://doi.org/10.1175/JCLI-D-21-0508.1>
- Smith, D. M., Dunstone, N. J., Scaife, A. A., Fiedler, E. K., Copsey, D., & Hardiman, S. C. (2017). Atmospheric response to arctic and antarctic sea ice: The importance of ocean–atmosphere coupling and the background state. *Journal of Climate*, 30(12). <https://doi.org/10.1175/JCLI-D-16-0564.1>
- Smith, D. M., Screen, J. A., Deser, C., Cohen, J., Fyfe, J. C., García-Serrano, J., Jung, T., Kattsov, V., Matei, D., Msadek, R., Peings, Y., Sigmond, M., Ukita, J., Yoon, J.-H., & Zhang,

- X. (2019). The polar amplification model intercomparison project (PAMIP) contribution to CMIP6: Investigating the causes and consequences of polar amplification. *Geoscientific Model Development*, 12(3). <https://doi.org/10.5194/gmd-12-1139-2019>
- Stroeve, J. C., Serreze, M. C., Holland, M. M., Kay, J. E., Malanik, J., & Barrett, A. P. (2012). The arctic's rapidly shrinking sea ice cover: A research synthesis. *Climatic Change*, 110(3). <https://doi.org/10.1007/s10584-011-0101-1>
- Sumata, H., de Steur, L., Divine, D. V., Granskog, M. A., & Gerland, S. (2023). Regime shift in arctic ocean sea ice thickness. *Nature*, 615(7952). <https://doi.org/10.1038/s41586-022-05686-x>
- Sun, L., Deser, C., Tomas, R. A., & Alexander, M. (2020). Global coupled climate response to polar sea ice loss: Evaluating the effectiveness of different ice-constraining approaches. *Geophysical Research Letters*, 47(3). <https://doi.org/10.1029/2019GL085788>
- Tebaldi, C., & Arblaster, J. M. (2014). Pattern scaling: Its strengths and limitations, and an update on the latest model simulations. *Climatic Change*, 122(3). <https://doi.org/10.1007/s10584-013-1032-9>
- Wagner, T. J. W., & Eisenman, I. (2015). How climate model complexity influences sea ice stability. *Journal of Climate*, 28(10). <https://doi.org/10.1175/JCLI-D-14-00654.1>