

Correcting for artificial heat in coupled sea ice perturbation experiments

Luke Fraser-Leach, Paul Kushner, and Alexandre Audette

July 12, 2023

Keywords

Sea ice, climate models, polar amplification

Abstract

A common approach to assessing how polar amplification affects lower latitude climate is to perform coupled ocean-atmosphere experiments in which sea ice is perturbed to a future state. A recent critique by M. England and others uses a simple 1-dimensional energy balance model (EBM) to show that sea ice perturbation experiments add artificial heat to the climate system. We explore this effect in a broader range of models and suggest a technique to correct for the artificial heat post-hoc. Our technique successfully corrects for artificial heat in the EBM and a possible generalization of this approach is developed to correct for artificial heat in an albedo modification experiment in a comprehensive earth system model. However, this technique can not be directly generalized to sea ice perturbation methodologies that employ a “ghost flux” seen only by the sea ice model. Applying the correction to the comprehensive albedo modification experiment, we find stronger artificial warming than in the EBM. Failing to account for the artificial heat also leads to overestimation of the climate response to sea ice loss, and can suggest false or artificially strong “tugs-of-war” between low latitude warming and sea ice loss over some fields, for example Arctic surface temperature and zonal wind.

22 1 Introduction

23 Arctic amplification and sea ice loss are robustly observed features of recent climate change (Stroeve
24 et al., 2012; Sumata et al., 2023), and are expected to continue. In addition to local impacts, Arctic
25 amplification has consequences for lower latitude climate (Cohen et al., 2014; Screen et al., 2018;
26 Shaw & Smith, 2022). Coupled climate model simulations in which the interactive sea ice model is
27 constrained to a target state (e.g. corresponding to a given radiative forcing or a level of global mean
28 warming) in the absence of greenhouse gas (GHG) forcing have been central to understanding the
29 consequences of sea ice loss and Arctic amplification (Deser et al., 2015; Sun et al., 2020). Multiple
30 approaches exist to constraining sea ice in a coupled model, including adding a “ghost flux” seen
31 only by the sea ice model in grid cells where sea ice melt is desired (Deser et al., 2015), nudging
32 the sea ice concentration to a target state at every timestep (Smith et al., 2017), and reducing the
33 albedo of sea ice to melt it (Blackport & Kushner, 2016). We refer to methods like these, which
34 constrain an interactive sea ice model to a state which is not in equilibrium with the climate, as
35 *sea ice perturbation methods*. Other techniques which do not constrain the interactive sea ice model
36 have been used to study the effect of sea ice loss in coupled models (e.g. Dai et al., 2019). These
37 are not the focus of this study.

38 England et al. (2022) criticize sea ice perturbation methods categorically, arguing that they all
39 induce artificial effects unrelated to sea ice loss. To make this argument, the authors use the one
40 dimensional energy balance model (EBM) introduced by Wagner and Eisenman (2015). The EBM

$$\frac{\partial E}{\partial t} = aS - (A + BT) + D\nabla^2 T + F_b, \quad (1)$$

41 determines the evolution of upper ocean enthalpy E , which represents upper ocean heat content
42 for temperatures above freezing and sea ice latent heat content for temperatures below freezing.
43 In equation (1), $a(x, T)$ is the albedo (which depends on $x = \sin\theta$ where θ is latitude and
44 temperature T), S is the incoming shortwave flux, $A + BT$ is the outgoing longwave flux, D is the
45 diffusion coefficient for the diffusive parameterization of meridional heat transport by dynamics,
46 and F_b is the constant heat flux from the deep ocean into the mixed layer. See section 2 for further
47 details on the model.

48 In the annual mean (denoted $\bar{\cdot}$) equilibrium, equation (1) becomes

$$0 = \overline{aS} - (A + B\overline{T}) + D\nabla^2\overline{T} + F_b. \quad (2)$$

49 If a spatially and temporally constant forcing F_{ghg} representing an increase in atmospheric GHG
50 concentration is applied, the response (represented by δ symbols) is determined by

$$B\delta\overline{T}_{ghg} - D\nabla^2\delta\overline{T}_{ghg} = \delta\overline{aS}_{ghg} + F_{ghg}. \quad (3)$$

51 The main argument of England et al. (2022) is that by equation (3), the true annual mean temper-
52 ature response to a given amount of sea ice loss in this EBM is the response required to balance the
53 increase in absorbed shortwave due to the sea ice albedo feedback, given by $B\delta\overline{T} - D\nabla^2\delta\overline{T} = \delta\overline{aS}$.
54 They then implement three sea ice perturbation methods in the EBM, and show that the warming
55 in those simulations exceeds the true warming.

56 Insight into the England et al. (2022) argument can be gained by taking the global mean (denoted
57 $\langle\cdot\rangle$) of (3), and using $\delta\langle\overline{aS}\rangle \approx (\partial\langle\overline{aS}\rangle/\partial\langle\overline{T}\rangle)\delta\langle\overline{T}\rangle > 0$ for a given spatial pattern of forcing (here the
58 spatially constant F_{ghg}), where the partial derivative represents the expected increase of coalbedo
59 with temperature. In this case

$$B\delta\langle\overline{T}\rangle_{ghg} = \delta\langle\overline{aS}\rangle_{ghg} + F_{ghg} \approx (\partial\langle\overline{aS}\rangle/\partial\langle\overline{T}\rangle)\delta\langle\overline{T}\rangle + F_{ghg}. \quad (4)$$

60 It is easily shown (see the SI) that for a stable equilibrium solution to (2), it is required that

$$B > \partial\langle\overline{aS}\rangle/\partial\langle\overline{T}\rangle. \quad (5)$$

61 In a sea ice perturbation simulation, F_{ghg} is zero. The inequality (5) therefore implies that without
62 some other heat flux, the only solution to (4) is $\delta\langle\overline{T}\rangle = 0$, which corresponds to no change in sea
63 ice. To obtain a nonzero change in the sea ice state, there must be an additional forcing term on
64 the right hand side of equation (4). From the perspective of annual mean energy balance, the role
65 of any sea ice perturbation method is to add this additional heat flux, which we call F_{pert} . The
66 annual mean global mean temperature response in a sea ice perturbation simulation, $\delta\langle\overline{T}\rangle_{pert}$, is

67 therefore the response to sea ice loss plus the additional heat flux,

$$B\delta\langle\bar{T}\rangle_{pert} = \delta\langle\bar{aS}\rangle_{ghg} + \delta\langle\bar{F}_{pert}\rangle, \quad (6)$$

68 where $\delta\langle\bar{aS}\rangle_{ghg}$ is the change in absorbed shortwave from the GHG simulation. $\delta\langle\bar{T}\rangle_{pert}$ therefore
69 exceeds the true annual mean global mean warming due to sea ice loss in this model, which would
70 be $\delta\langle\bar{aS}\rangle/B$, by $\langle\bar{F}_{pert}\rangle/B$. As such, all sea ice perturbation methods introduce artificial warming,
71 because they add an artificial heat flux in order to perturb sea ice in a climate stable to sea ice
72 perturbations.

73 The artificial warming effect in the EBM is illustrated in [figure 1](#). The left column shows the
74 radiative forcing, temperature response, and sea ice thickness response to the shortwave forcing from
75 the sea ice albedo feedback alone (SPECIFIED_ALBEDO). This is the true annual mean effect of
76 sea ice loss in this model (see [section 2](#)). Importantly, the shortwave forcing due to a given loss of sea
77 ice does not achieve that same sea ice loss, again because the EBM’s equilibrium climate is stable to
78 perturbations in sea ice ([5](#)). The right column shows the ghost flux method implemented in the EBM
79 (GHOST_FLUX). The sea ice is successfully constrained to the target state in GHOST_FLUX, but
80 to achieve this an artificial heat flux has been added, and this introduces its own artificial warming.

81 In this study, we attempt to correct for the effects of artificial heat in the EBM and in coupled
82 model simulations via post processing using two-parameter scaling (Blackport & Kushner, [2017](#)).
83 This is an effort to determine what value can be recovered from the commonly employed sea ice
84 perturbation framework. The simulations and techniques used are outlined in [section 2](#). We present
85 our two-parameter pattern scaling technique for accounting for the additional heat and assess its
86 validity in the EBM in [section 3](#). In [section 4](#), we use the pattern scaling technique to assess the
87 primary effects of the additional heat in comprehensive model simulations. We summarize our
88 conclusions in [section 5](#).

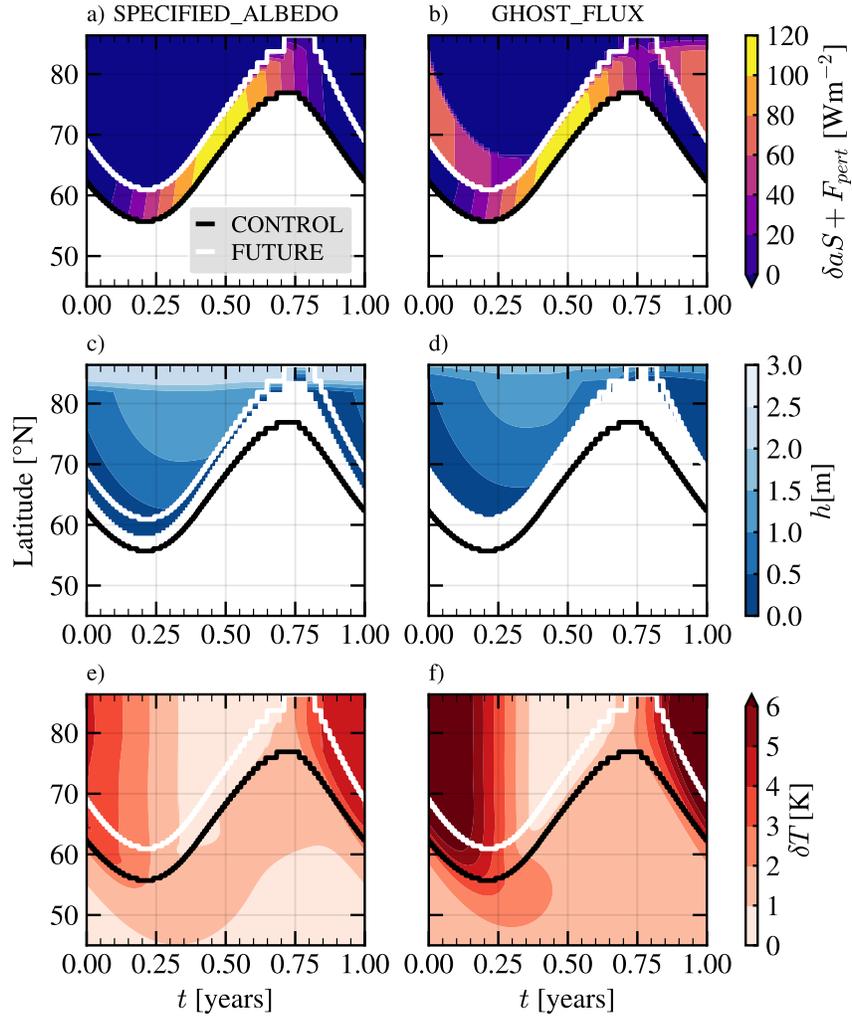


Figure 1: Left column: change in (a) sum of absorbed shortwave and additional heat flux, (c) temperature, and (e) sea ice thickness in the GHOST_FLUX simulation in the dry EBm. Right column: same as left column but for the SPECIFIED_ALBEDO simulation. The white (black) line displays the ice edge in CONTROL (FUTURE).

89 2 Methods

90 2.1 EBM simulations

91 The EBM is described comprehensively in Wagner and Eisenman (2015). Its state is determined
92 by the surface enthalpy E , which is a convenient way of representing surface temperature T and
93 sea ice thickness h in a single variable.

$$E = \begin{cases} T/c_w, & E \geq 0 \\ h/L_f, & E < 0 \end{cases} \quad (7)$$

94 Here, c_w is the specific heat capacity of the ocean, L_f is the latent heat of freezing, and $T = 0$ is
95 the freezing temperature of the mixed layer. The surface temperature is determined by

$$T = \begin{cases} E/c_w, & E > 0 & \text{(open water)} \\ 0, & E < 0 \text{ and } T_0 > 0 & \text{(melting)} \\ T_0, & E < 0 \text{ and } T_0 < 0 & \text{(freezing),} \end{cases} \quad (8)$$

96 where T_0 is the surface temperature required for zero heat flux into the surface when sea ice is
97 present (Wagner & Eisenman, 2015). We use the numerical implementation presented by Wagner
98 and Eisenman (2015), in which the diffusive heat transport takes place in a “ghost” layer whose
99 temperature is relaxed to the temperature of the main layer. This implementation is modified to
100 include a global rather than hemispheric domain.

101 Following England et al. (2022), we run simulations in the EBM called CONTROL, FUTURE,
102 and SPECIFIED_ALBEDO. These and the other EBM simulations described below are run for 100
103 years, with data from the last year used as output. CONTROL is simply the EBM run in the default
104 configuration with no forcing. In FUTURE, a forcing $F_{ghg} = 3.1 \text{ W m}^{-2}$ is imposed to represent
105 a doubling of CO_2 . In SPECIFIED_ALBEDO, $F_{ghg} = 0.0 \text{ W m}^{-2}$ but the coalbedo $a(x)$ is fixed
106 to be identical to the equilibrium $a(x)$ from FUTURE, regardless of the model’s current sea ice
107 state (England et al., 2022). The annual mean temperature change in SPECIFIED_ALBEDO is the
108 model’s response to the change in absorbed shortwave $\delta(aS)$ from FUTURE. Following the interpre-
109 tation of equation (3) in England et al. (2022), we refer to the warming in SPECIFIED_ALBEDO

110 as the “true” SIL-induced warming.

111 The simple representation of sea ice in the EBM allows for an implementation of sea ice per-
112 turbation methods. England et al. (2022) run three such simulations: NUDGING, GHOST_FLUX,
113 and ALBEDO_ANNUAL (renamed DARK_ICE in this study). We reproduce these simulations (fig-
114 ure 3, solid curves), a full description of which can be found in England et al. (2022). In NUDGING,
115 the sea ice thickness is nudged to the target state with a timescale of 2.5 days. In GHOST_FLUX, a
116 heat flux which varies sinusoidally between 5 W m^{-2} in summer and 65 W m^{-2} in winter is applied
117 to any ice-covered grid cell that is either ice-free or has very thin ice ($E < -5 \text{ W m}^{-2}$) at the
118 same time in FUTURE. In DARK_ICE, the coalbedo of sea ice is increased from 0.4 to 0.48, which
119 was found to roughly reproduce the annual mean change in sea ice area from FUTURE. All EBM
120 simulations are summarized in table 1.

121 2.2 Moist EBM

122 One important process missing in the EBM of Wagner and Eisenman (2015) is the latent heat
123 transported poleward by water vapor, which accounts for about half the atmospheric poleward heat
124 transport in models and is itself a source of Arctic amplification (Feldl & Merlis, 2021). Latent heat
125 transport can be easily be added to the EBM by changing the meridional heat transport term to
126 diffuse moist static energy (MSE) instead of dry static energy. Following (Feldl & Merlis, 2021), we
127 use $s = T + c_p^{-1}HL_vq(T)$ as the MSE in units of temperature. Here c_p is the specific heat capacity
128 of dry air at constant pressure, $H = 0.8$ is the constant relative humidity, L_v is the latent heat
129 of vaporization of water, and $q(T)$ is the saturation pressure of water vapor, determined by the
130 Clausius-Clapeyron equation. We hereafter refer to the EBM with dry static energy diffusion as the
131 “dry EBM” and the EBM with MSE diffusion as the “moist EBM”. Parameter values for the dry
132 EBM are identical to those in Table 1 of Wagner and Eisenman (2015). Parameter values for the
133 moist EBM are identical to those used in Feldl and Merlis (2021), which are nearly identical to the
134 dry EBM values except that (1) D is $0.3 \text{ W m}^{-2} \text{ K}^{-1}$ (vs. $0.6 \text{ W m}^{-2} \text{ K}^{-1}$ in the dry EBM), (2)
135 the ocean mixed layer heat capacity is $7.8 \text{ W yr m}^{-2} \text{ K}^{-1}$ (vs. $9.8 \text{ W yr m}^{-2} \text{ K}^{-1}$ in the dry EBM),
136 and (3) in DARK_ICE the coalbedo of sea ice is increased from 0.4 to 0.52 (vs. 0.4 to 0.48 in the
137 dry EBM). The diffusivity D is halved in the moist EBM to maintain similar total poleward energy
138 transport across the two EBMs, because including diffusion of latent heat EBM roughly doubles the

139 total poleward heat transport if D is held constant. Note that the mixed layer heat capacity does
140 not affect the global mean properties of the EBM. The coalbedo in DARK_ICE in each of the EBMs
141 is the value required to match the annual mean sea ice extent in FUTURE in the corresponding
142 EBM.

143 **2.3 Comprehensive model simulations**

144 In addition to the EBM, we study the additional heat issue in two sets of comprehensive model
145 experiments: an albedo modification experiment in the Community Earth System Model version 1
146 (CESM1) with the Community Atmospheric Model version 5 (CAM5), and a hybrid nudging exper-
147 iment in CESM1 with the Whole Atmosphere Community Climate Model version 4 (WACCM4).
148 A complete description of CESM1 is given in Hurrell et al. (2013) and references therein. The
149 comprehensive simulations are summarized in table 1.

150 The modified albedo experiments are described in Hay (2020). Three simulations are branched
151 from the CESM large ensemble with historical forcing at year 2000: a year 2000 control run in
152 which all forcings are kept constant (Control), a doubled CO_2 run in which the concentration of
153 CO_2 is abruptly set to 560 ppm ($2\times\text{CO}_2$), and a simulation in which all forcings are constant but
154 the albedo of snow on sea ice and bare sea ice are reduced in the northern hemisphere giving similar
155 annual mean sea ice extent to that in $2\times\text{CO}_2$ (“Low Albedo” in this study, referred to as “Actic,
156 strong” in an Hay (2020)). All three simulations are run for 500 years after they are branched. We
157 use time means over years 200 to 500 in all of the analysis presented here.

158 We also analyze the time slice WACCM4 hybrid nudging experiments presented in Audette
159 and Kushner (2022), whose configurations and names follow the polar amplification model inter-
160 comparison project (PAMIP) protocol (Smith et al., 2019). In particular, our analysis is based on
161 a control year 2000 simulation (pa-pdSIC); a simulation in which CO_2 concentration is doubled
162 relative to 2000 and Arctic sea ice is nudged to a state corresponding to a 2 °C warming scenario
163 (pa-futArcSIC- $2\times\text{CO}_2$); and a sea ice perturbation simulation in which CO_2 concentration is set to
164 its year 2000 concentration but Arctic sea ice is nudged to the 2 °C warming state (pa-futArcSIC).
165 All simulations are run for 100 years, of which we use the last 40 for analysis.

Table 1: Summary of simulations used in this study.

Experiment name	GHG forcing	Arctic sea ice forcing
<i>EBM simulations</i>		
CONTROL	$F_{ghg} = 0.0 \text{ W m}^{-2}$	None
FUTURE	$F_{ghg} = 3.1 \text{ W m}^{-2}$	None
SPECIFIED_ALBEDO	$F_{ghg} = 0.0 \text{ W m}^{-2}$	Coalbedo field $a(x)$ fixed to output coalbedo field from FUTURE
DARK_ICE	$F_{ghg} = 0.0 \text{ W m}^{-2}$	Coalbedo of sea ice increased from $a_i = 0.4$ to 0.48 (dry EBM) or 0.52 (moist EBM)
GHOST_FLUX	$F_{ghg} = 0.0 \text{ W m}^{-2}$	$35 + 30 \cos(2\pi t) \text{ W m}^{-2}$ applied to ice-covered grid cells that are ice-free in FUTURE
NUDGING	$F_{ghg} = 0.0 \text{ W m}^{-2}$	E relaxed to 2 W yr m^{-2} with a timescale of 2.5 days in ice-covered grid cells that are ice-free in FUTURE
<i>CESM-CAM simulations</i>		
Control	$[\text{CO}_2] = 280 \text{ ppm}$	None
$2 \times \text{CO}_2$	$[\text{CO}_2] = 560 \text{ ppm}$	None
Low Albedo	$[\text{CO}_2] = 280 \text{ ppm}$	Albedo of snow on sea ice and bare sea ice reduced (Hay, 2020)
<i>CESM-WACCM simulations</i>		
pa-pdSIC	$[\text{CO}_2] = 285 \text{ ppm}$	Hybrid nudging to present day sea ice (Audette & Kushner, 2022)
pa-futArcSIC- $2 \times \text{CO}_2$	$[\text{CO}_2] = 569 \text{ ppm}$	Hybrid nudging to sea ice corresponding to $2 \text{ }^\circ\text{C}$ warming (Audette & Kushner, 2022)
pa-futArcSIC	$[\text{CO}_2] = 285 \text{ ppm}$	Hybrid nudging to sea ice corresponding to $2 \text{ }^\circ\text{C}$ warming (Audette & Kushner, 2022)

166 2.4 Pattern scaling

167 Our method of accounting for the additional heat flux is based upon the two-parameter pattern
168 scaling technique developed by Blackport and Kushner (2017). Traditional pattern scaling hypothe-
169 sizes that the climate response to GHG forcing scales linearly with global mean surface temperature
170 (Tebaldi & Arblaster, 2014). Two-parameter pattern scaling extends this hypothesis to allow for
171 independent patterns that scale with global mean surface temperature and with sea ice area. Specif-
172 ically, two-parameter pattern scaling decomposes the response δZ to a GHG or sea ice forcing as

$$\delta Z = \left. \frac{\partial Z}{\partial T_l} \right|_I \delta T_l + \left. \frac{\partial Z}{\partial I} \right|_{T_l} \delta I, \quad (9)$$

173 where $\partial Z/\partial T_l|_I$ and $\partial Z/\partial I|_{T_l}$ are the space and time-dependent “sensitivities” to low latitude
174 temperature T_l and sea ice area I , respectively, and the δ symbols represent changes in those
175 variables between a forced simulation and the control simulation. Throughout this work, I is
176 defined as annual mean sea ice area north of 70 °N and T_l is defined as the annual mean of the
177 0-40 °N mean radiative surface temperature in the comprehensive models, or annual mean of the
178 0-40 °N mean T in the EBM. The sensitivities are calculated by assuming the responses in a sea
179 ice perturbation experiment and a GHG forcing experiment can each be written as (9) and solving
180 for the two sensitivities given δZ , δT_l , and δI in the two simulations. This assumption is supported
181 by the observation that responses to sea ice loss and GHG forcing imposed in isolation in sea ice
182 perturbation experiments add relatively linearly to the response in a total GHG forcing experiment
183 (McCusker et al., 2017). In Figures 2, 4, and 5, the sensitivities are multiplied by their associated
184 scaling variables to compare the contributions from each effect. We refer to such fields as “partial
185 responses”.

186 3 Correcting for the additional heat

187 The artificial warming effect suggests that sea ice perturbation experiments have been misinter-
188 preted. Effects that were previously identified as responses to sea ice loss are really responses to sea
189 ice loss plus the additional heat flux, F_{pert} . In the EBM, the temperature response to the artificial
190 forcing is of similar magnitude to the response to sea ice loss alone. It would therefore be useful

191 if there were a way of quantifying the response to the artificial forcing, to allow the true effect of
 192 sea ice loss to be identified. In this section, we assess whether the effect of artificial heat can be
 193 accounted for using two-parameter scaling.

194 3.1 New scaling parameters

195 The solid curves in [figure 2](#) show the partial responses to sea ice loss (SIL) and low latitude warming
 196 (LLW) calculated using EBM simulations. The top row shows the partial responses derived from
 197 SPECIFIED_ALBEDO, which represent the true partial responses in this model in the absence of
 198 F_{pert} . In [figure 2a](#), the partial response to LLW is spatially constant, corresponding to the LLW
 199 that scales with the spatially constant F_{ghg} . The partial response to SIL accounts for all the spatial
 200 structure in the total warming, a result of the fact that albedo changes are the only source of Arctic
 201 amplification in this model, as per equation (3). All changes in the meridional temperature gradient
 202 are therefore attributable to SIL ([figure 2b](#)).

203 The solid curves in the second row of [figure 2](#) show the partial responses to LLW and SIL
 204 identified using DARK_ICE instead of SPECIFIED_ALBEDO. These differ from the true partial
 205 responses because the temperature response in DARK_ICE includes artificial warming due to F_{pert}
 206 in addition to the true warming caused by SIL itself. Because of the artificial warming at high
 207 latitudes, all polar warming is attributed to SIL, with the partial response to LLW showing polar
 208 *cooling*. These features are made clear by taking the global mean of the sensitivities (derived in the
 209 SI),

$$\begin{aligned} \frac{\partial \langle \bar{T} \rangle}{\partial T_l} &\approx \frac{B^{-1} (F_{ghg} - \langle F_{pert} \rangle)}{\delta T_{l,F}} \\ \frac{\partial \langle \bar{T} \rangle}{\partial I} &\approx \frac{B^{-1} (\delta \langle \bar{a}S \rangle + \langle F_{pert} \rangle)}{\delta I}. \end{aligned} \quad (10)$$

210 The warming induced by the perturbation flux, $\langle F_{pert} \rangle / B$, is attributed to sea ice loss. This arti-
 211 ficially increases $\partial \langle \bar{T} \rangle / \partial I$ and artificially decreases $\partial \langle \bar{T} \rangle / \partial T_l$. Locally, the effect is greatest at the
 212 pole, where F_{pert} is greatest, as seen in [figure 2c](#).

213 This suggests that we should replace the scaling parameter I with a variable that accounts for
 214 both SIL and the artificial heat flux. In the EBM, a good candidate is the total ice-related radiative
 215 forcing, $F_{ice} = \delta aS + F_{pert}$. We also replace T_l (which is meant to capture the direct response to
 216 GHG forcing) by F_{ghg} , the direct GHG forcing itself. The annual mean global mean sensitivities to

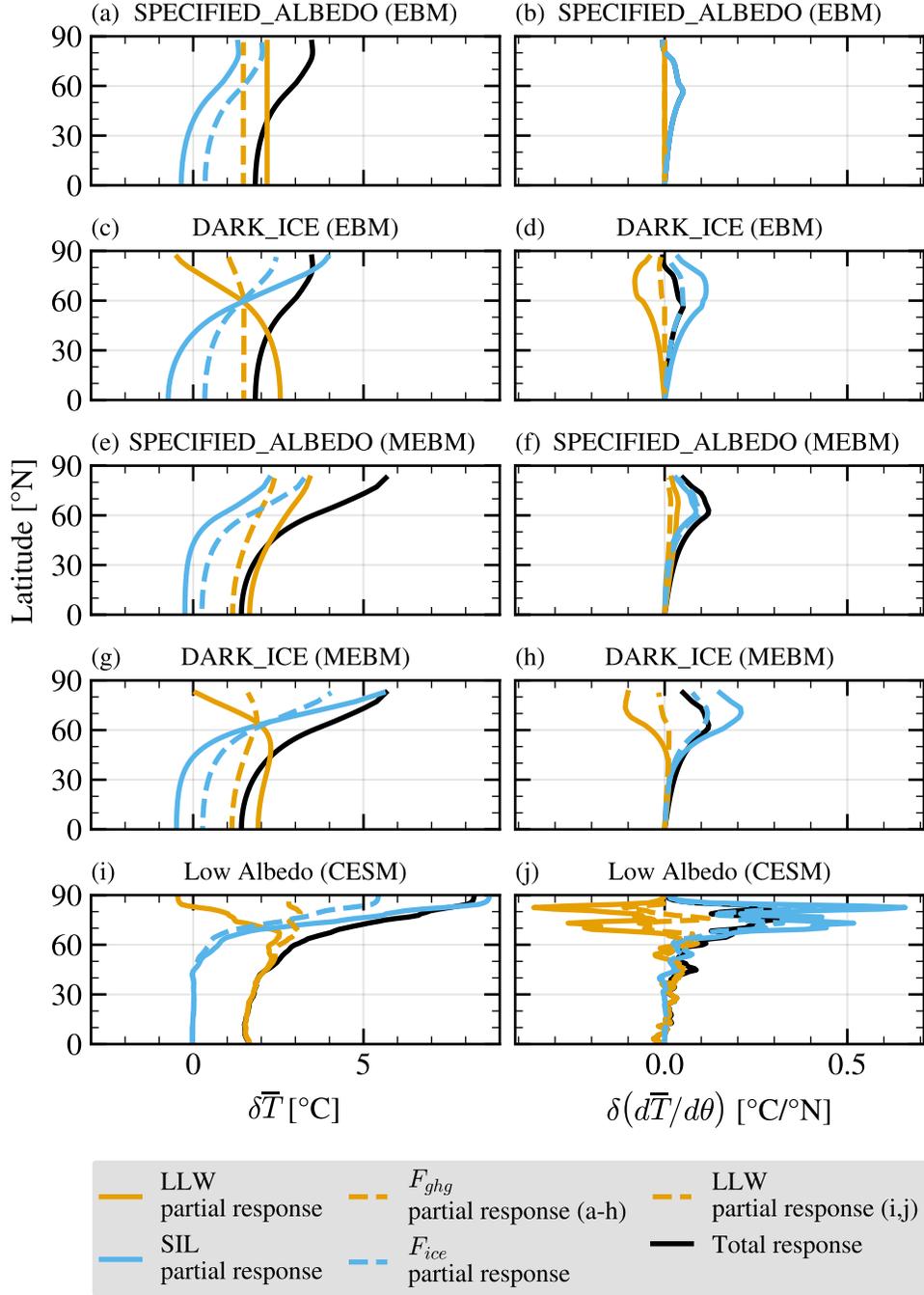


Figure 2: Black: Annual mean of response of surface temperature (left column) and its meridional gradient (right column) in the dry EBM (a-d), the moist EBM (e-h), and the CESM Low Albedo perturbation (i,j) experiments. In (a-h) colored curves show the decomposition of the response into partial responses using two pattern scaling approaches: solid blue and gold show the decomposition into LLW and SIL effects, and dashed blue and gold show the decomposition into F_{ghg} and F_{ice} effects. In (i,j), solid curves show the decomposition into LLW and SIL effects, and the dashed curves show the decomposition into LLW and F_{ice} effects.

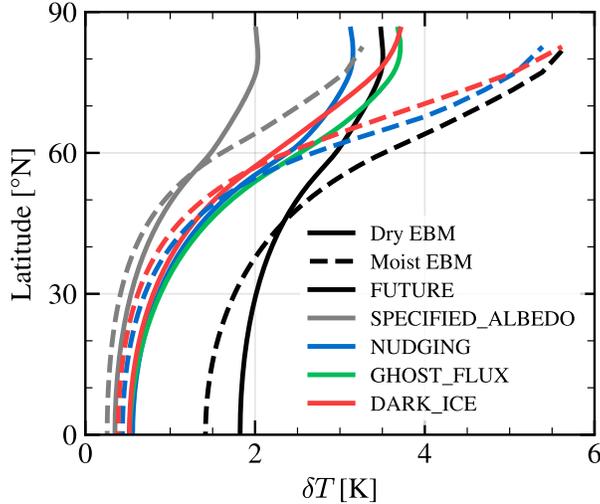


Figure 3: Annual mean temperature change in the dry (solid) and moist (dashed) EBMs in the FUTURE (black), SPECIFIED_ALBEDO (grey), and sea ice perturbation (coloured) simulations.

217 these new parameters (also shown in the SI) are

$$\begin{aligned}
 \frac{\partial \langle \bar{T} \rangle}{\partial F_{ghg}} &= \frac{B^{-1} F_{ghg}}{F_{ghg}} = \frac{1}{B} \\
 \frac{\partial \langle \bar{T} \rangle}{\partial F_{ice}} &= \frac{B^{-1} (F_{pert} + \delta a S)}{F_{pert} + \delta a S} = \frac{1}{B}.
 \end{aligned}
 \tag{11}$$

218 Both global mean temperature sensitivities are equal to B^{-1} , as expected for the global mean
 219 temperature response to any radiative forcing in the EBM.

220 The partial responses to F_{ghg} and F_{ice} are shown as dashed lines in [figure 2](#). In the dry EBM, the
 221 partial responses to these new variables in DARK_ICE (second row) are closer to the true partial
 222 responses in the EBM (top row). Notably, the partial response to F_{ghg} is nearly latitudinally
 223 constant ([figure 2c](#)), and the partial response to F_{ice} accounts for nearly all of the latitudinal
 224 structure in the total response. Accounting for F_{pert} does not change the partial responses from
 225 SPECIFIED_ALBEDO in any meaningful way: the new partial responses are simply constant offsets
 226 of the original partial responses. This is not related to accounting for F_{pert} , but a consequence of
 227 using F_{ghg} instead of T_l .

228 3.2 Moist effects in the EBM

229 As discussed in [section 2](#), an important process missing in the EBM is that of latent heat transport
230 by water vapor. We implement the DARK_ICE and SPECIFIED_ALBEDO simulations in the
231 moist EBM. The annual mean warming in the moist EBM simulations is shown in [figure 3](#). The
232 key result of England et al. (2022) is essentially unchanged in the moist EBM: the warming in the
233 sea ice perturbation simulations is a factor of 1.5-2 greater than the true warming due to sea ice
234 loss alone. All simulations show more polar amplification in the moist EBM than in the dry EBM,
235 because MSE transport is an additional mechanism for polar amplification (Flannery, 1984).

236 The third row of [figure 2](#) shows the true temperature partial responses in the moist EBM. The
237 partial response to SIL is similar across the dry and moist EBMs. There is an interesting difference
238 in the LLW partial response across the models: because MSE transport increases under global
239 warming, the partial response to LLW shows polar amplification in the moist EBM ([figure 2e](#)).
240 Thus, both SIL and LLW contribute to polar amplification in the moist EBM.

241 The partial responses from the DARK_ICE simulation in the moist EBM are shown in the fourth
242 row of [figure 2](#). As in the dry EBM, before the additional heat is accounted for SIL takes credit for
243 all the polar warming, which requires the partial response to LLW to be small or negative at high
244 latitudes ([figure 2h](#)) and gives a large cancellation in the meridional gradients of the two partial
245 responses ([figure 2i](#)). Dashed curves again show partial responses to F_{ghg} and F_{ice} , which account
246 for the additional heat as in the dry EBM (11). These partial responses closely resemble the true
247 ones. Most importantly, the cancellation in the meridional gradients has disappeared. In principle,
248 both partial responses should show some polar amplification, such that the polar amplification in the
249 total response is partially attributable to both F_{ghg} and F_{ice} ([figure 2f](#)). The DARK_ICE-derived
250 partial response to F_{ghg} does have a small positive gradient up to 65°N, but the gradient is negative
251 at high latitudes. This negative gradient, which is also present in the dry EBM ([figure 2d](#)) is likely
252 due to the fact that the albedo method induces the most artificial warming ([figure 3](#)) to achieve the
253 target sea ice state. The NUDGING simulation, which does not induce as much warming, yields
254 partial responses which more closely resemble the true partial responses (Figure S2).

255 3.3 Comprehensive model

256 In CESM, we define F_{ice} to be the change in net all-sky top of atmosphere (TOA) shortwave north
257 of 70 °N. As in DARK_ICE, the artificial heat flux in Low Albedo is equal to the incoming shortwave
258 that is absorbed at the surface because of the artificial reduction in sea ice albedo. F_{ice} therefore
259 includes two sea ice related contributions: (1) a change in absorbed shortwave due to newly exposed
260 ocean, and (2) a change in absorbed shortwave because the remaining sea ice is artificially darker.
261 We keep low latitude temperature (T_l or LLW) as the other scaling parameter, as there is not an
262 easily calculated analogue to F_{ghg} in the comprehensive model. The EBM results are not sensitive
263 to the use of LLW or F_{ghg} as the scaling parameter complementary to F_{ice} (Figure S2).

264 The partial surface temperature responses from the CESM simulations are shown in the bottom
265 row of [figure 2](#). They tell a similar story to the partial temperature responses in the moist EBM.
266 Before the additional heat is accounted for, all the Arctic warming is attributed to SIL ([figure 2i](#),
267 solid curves). The partial response to SIL therefore has a high degree of Arctic amplification, which
268 requires tropical amplification (and in fact Arctic cooling) in the partial response to LLW. Once
269 the additional heat is accounted for, both LLW and SIL contribute to Arctic warming and Arctic
270 amplification ([figure 2i](#), dashed curves).

271 We do not have an analogue to the SPECIFIED_ALBEDO simulation in CESM - designing such
272 a simulation is not the purpose of this work. Therefore, we cannot diagnose the true effect of SIL in
273 CESM. However, the similarity of the partial responses in CESM and the moist EBM suggests that
274 similar effects determine the partial responses in both models. Namely, it appears that in CESM
275 the partial responses to LLW and SIL contain the same artificial effects as they do in the moist
276 EBM. Further, using F_{ice} rather than I as a pattern scaling parameter seems to properly account
277 for the artificial effects in CESM, as it does in the moist EBM.

278 We also attempted to use pattern scaling with F_{ice} to account for the artificial heat flux in the
279 WACCM hybrid nudging simulations, to less success. In the hybrid nudging method, F_{pert} is equal
280 to the ghost flux applied to the bottom of the sea ice plus the latent heat flux implicit in removing
281 thinnest category ice (Audette & Kushner, [2022](#)). Because both of these fluxes are “ghost” fluxes,
282 seen only by the sea ice model itself, it is not sensible to add them on equal footing to the change
283 in TOA shortwave. Simply taking $F_{ice} = F_{pert} + S\delta a_{Arctic}$ as a scaling variable therefore gives

284 unphysical partial responses. More work would be required to determine a scaling variable that
285 captures the correct physics in simulations that employ ghost fluxes. An in-depth discussion can be
286 found in the SI.

287 4 Primary effects of the artificial heat

288 The most striking effect in [figure 2](#) is that too much Arctic amplification is attributed to SIL when
289 the artificial heat is not accounted for. This feature is robust across all models. Sea ice perturbation
290 experiments therefore imply a false “tug of war” (negative feedback from sea ice loss) between SIL
291 and LLW over the meridional temperature gradient. Once the artificial heat is properly accounted
292 for, the tug of war disappears, and both LLW and F_{ice} contribute to Arctic amplification. In
293 the CESM Low Albedo simulations, this false tug of war is confined below 750 hPa ([figure 4d](#)
294 compared to [figure 4b](#)). In the moist EBM, the Arctic amplification that scales with LLW is due to
295 increased poleward transport of latent heat under global warming. In CESM, such LLW-induced
296 Arctic amplification could be due to any number of Arctic amplification-producing feedbacks that
297 do not scale with SIL, including but not limited to the lapse rate feedback, the Planck feedback,
298 and increased latent heat transport.

299 Attributing too much Arctic amplification to SIL may similarly overestimate the role of SIL
300 in any dynamical response related to Arctic amplification. Especially suspect is the zonal wind
301 response. SIL is thought to induce a weakening on the poleward flank of the midlatitude jet and a
302 strengthening on its equatorward flank, with the weakening outweighing the strengthening (Screen
303 et al., [2018](#)). This feature is seen in the zonal wind partial response to SIL derived from the CESM
304 Low Albedo simulations ([figure 5b](#)). When the perturbation flux is accounted for, the partial
305 response retains its spatial structure but decreases in magnitude by about 50%. This is interesting,
306 considering that ocean coupling is thought to increase the strength of the zonal wind response to SIL
307 (Deser et al., [2015](#)). Our results suggest that at least part of the strengthening is due to the fact that
308 the zonal wind responds to two forcings (SIL and F_{pert}) in coupled sea ice perturbation simulations
309 compared to only one (SIL) in atmospheric general circulation model simulations. Additionally,
310 past analyses of sea ice perturbation simulations have found that the zonal wind partial response
311 to LLW tends to shift the jet poleward, opposing the partial response to SIL and leading to a small

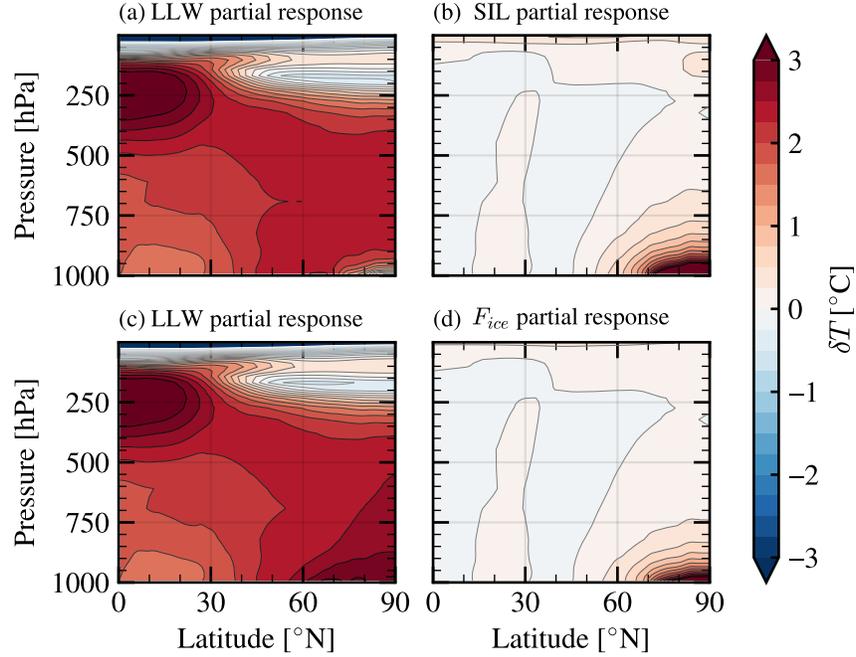


Figure 4: The annual mean zonal mean air temperature response in the $2\times\text{CO}_2$ experiment decomposed into partial responses using two pattern scaling approaches. (a,b) show the decomposition into LLW and SIL effects, and (c,d) show the decomposition into LLW and F_{ice} effects.

312 net response (Blackport & Kushner, 2017; Hay et al., 2022). As such, it has been suggested that
 313 there is a tug-of-war over the midlatitude zonal wind between LLW and SIL. Figure 5 demonstrates
 314 that failing to account for the artificial heat exaggerates such tugs-of-war in pattern scaling partial
 315 responses, suggesting a need to reinterpret this effect in previous experiments.

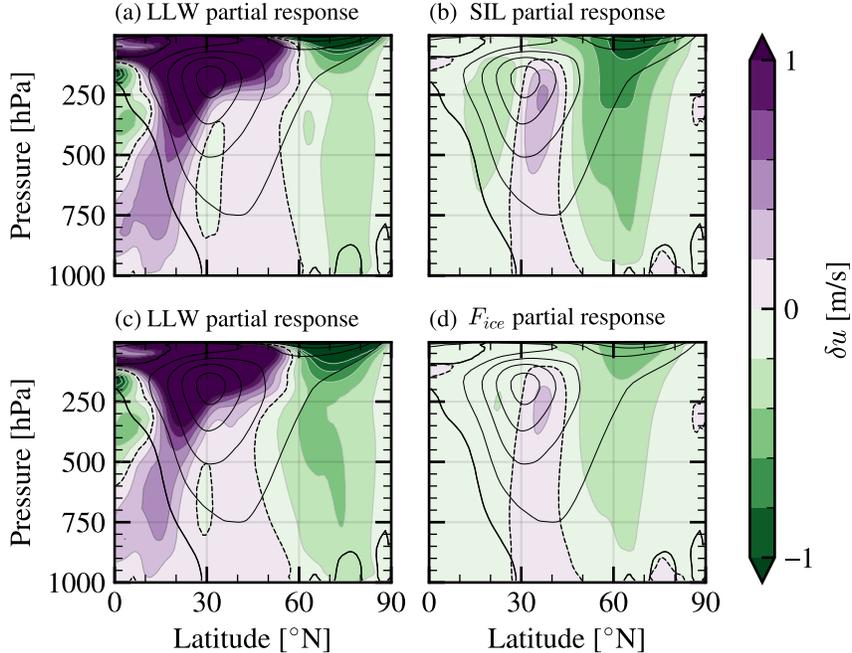


Figure 5: As in figure 4, but for DJF zonal wind.

5 Conclusions

This study follows up on the finding that sea ice perturbation simulations induce spurious polar warming (England et al., 2022). We have confirmed this finding in a broader range of models, and explored its implications.

First, we have shown that perturbing a thermodynamic sea ice model necessarily induces artificial warming. In order to perturb sea ice, it is necessary to supply it some artificial heat flux F_{pert} . By energy balance, this requires an artificial increase in outgoing longwave radiation and therefore artificial warming. Artificial warming is therefore present in any simulation in which a thermodynamic sea ice model is constrained to a state that is out of equilibrium with the climate. Most common approaches to imposing sea ice loss in coupled models have this property and therefore induce artificial heat, including all sea ice perturbation methods as defined this study. Our results suggest that the effects of artificial heat are just as strong (if not stronger) in coupled in models as in the EBM used in England et al. (2022).

Second, we have found that the artificial effects of F_{pert} can be accounted for by using two-parameter scaling. In past studies the two scaling parameters used have been tropical sea surface temperature and Arctic sea ice area. This gives an artificially large partial response to SIL because

332 the response in the sea ice perturbation simulation, which is due to SIL and the artificial heat flux,
333 is attributed entirely to SIL (equation (10)). Scaling by a different parameter, F_{ice} , that accounts
334 for both SIL and F_{pert} corrects this unphysical behaviour, recovering the true partial responses in
335 the EBM (equation (11)). Evaluating the pattern scaling partial responses to SIL and to F_{ice} in
336 an albedo modification simulation in a comprehensive earth system model, we find very similar
337 results to what we found in the EBM. This suggests that artificial warming is of similar strength in
338 comprehensive model simulation as in the EBM, and that scaling by F_{ice} successfully accounts for
339 the artificial effects in this simulation.

340 Third, we have used the new scaling parameters to diagnose the effect of the artificial heat in an
341 EBM with and without latent heat transport, and in a comprehensive model. Accounting for the
342 artificial heat reveals a general misinterpretation of perturbation simulations common to all models
343 in this study. Taken at face value, sea ice perturbation simulations overestimate the role of sea ice
344 loss in climate changes, because responses to the artificial heat flux are attributed to SIL itself. This
345 misattribution is evident in the surface temperature response in the EBM simulations of England
346 et al. (2022): the perturbation simulations overestimate the true annual mean surface warming by a
347 factor of 1.5-2. We have shown that the same overestimation is present in a comprehensive model,
348 and that it is not limited to surface temperature.

349 Overestimation of the role of sea ice loss by perturbation simulations suggests that some past
350 conclusions should be questioned. For example, it has been found that ocean coupling increases the
351 temperature and zonal wind responses to sea ice loss (Deser et al., 2015). Our results suggest that at
352 least part of the stronger response in coupled simulations is due to the artificial heat flux applied by
353 perturbation methods in coupled models. There is no artificial heat flux in sea ice loss simulations
354 in atmosphere-only models, because SIL is imposed as a boundary condition. Also worthy of some
355 question are responses over which there is a “tug-of-war” between SIL and LLW (Screen et al.,
356 2018). The artificially large response to SIL in perturbation simulations implies an artificially
357 diminished and potentially opposing role for LLW, if the responses to LLW and SIL sum linearly
358 to the total climate response. In all simulations analyzed in this study, accounting for the artificial
359 heat flux eliminates a tug-of-war over Arctic surface warming and Arctic amplification. Once the
360 artificial heat is accounted for, both SIL and LLW contribute to Arctic surface warming and Arctic
361 amplification. Similarly, accounting for the artificial heat reduces the magnitude of the zonal wind

362 partial response to SIL by about 50% in the comprehensive model, reducing its opposition to LLW.
363 The tug-of-war paradigm is still likely a useful one, as evidence for opposing effects of Arctic surface
364 warming and tropical warming transcends sea ice perturbation simulations (Barnes & Polvani, 2015).
365 But our results suggest that the artificial heat added by sea ice perturbation methods exaggerates
366 cancellations in the responses to SIL and LLW, and in some cases even introduces false cancellations.

367 Applying a similar pattern scaling technique to simulations where F_{pert} is a “ghost flux”, seen
368 only by the sea ice model, would require more work. In such simulations it is likely not sensible to
369 add F_{pert} directly to the change in TOA shortwave, because the latter is a term in the TOA energy
370 balance, while the former is applied only to the sea ice model and therefore only indirectly affects
371 the TOA energy balance.

372 We finish by noting that whether to consider the warming caused by F_{pert} as “artificial” is in
373 part a philosophical question. As made clear by Figure 1, artificial warming is required for the
374 climate to be consistent with the sea ice state. As such, it could be argued that the warming caused
375 by F_{pert} is not artificial, but physically associated with sea ice loss. However, the F_{pert} -caused
376 warming is necessary to *produce* sea ice loss; it is not a *response* to sea ice loss. Therefore, we
377 find it more natural to attribute F_{pert} -caused warming to CO₂. In this interpretation, the warming
378 induced by F_{pert} is indeed artificial in sea ice perturbation experiments, which have no CO₂ forcing.

379 Data and code availability

380 Code for running the EBM is available at <https://github.com/lukefl/ebm-icy-moist-seasonal>. Rel-
381 evant output from the CESM-CAM albedo modification and CESM-WACCM hybrid nudging sim-
382 ulations is available at <https://borealisdata.ca/dataverse/lf1>.

383 Acknowledgements

384 We thank Stephanie Hay for providing simulation output for this study. We acknowledge the
385 support of the NSERC Discovery Grant program.

References

- Audette, A., & Kushner, P. J. (2022). Simple hybrid sea ice nudging method for improving control over partitioning of sea ice concentration and thickness. *Journal of Advances in Modeling Earth Systems*, 14(12). <https://doi.org/10.1029/2022MS003180>
- Barnes, E. A., & Polvani, L. M. (2015). CMIP5 projections of arctic amplification, of the north american/north atlantic circulation, and of their relationship. *Journal of Climate*, 28(13). <https://doi.org/10.1175/JCLI-D-14-00589.1>
- Blackport, R., & Kushner, P. J. (2016). The transient and equilibrium climate response to rapid summertime sea ice loss in CCSM4. *Journal of Climate*, 29(2). <https://doi.org/10.1175/JCLI-D-15-0284.1>
- Blackport, R., & Kushner, P. J. (2017). Isolating the atmospheric circulation response to arctic sea ice loss in the coupled climate system. *Journal of Climate*, 30(6). <https://doi.org/10.1175/JCLI-D-16-0257.1>
- Cohen, J., Screen, J. A., Furtado, J. C., Barlow, M., Whittleston, D., Coumou, D., Francis, J., Dethloff, K., Entekhabi, D., Overland, J., & Jones, J. (2014). Recent arctic amplification and extreme mid-latitude weather. *Nature Geoscience*, 7(9). <https://doi.org/10.1038/ngeo2234>
- Dai, A., Luo, D., Song, M., & Liu, J. (2019). Arctic amplification is caused by sea-ice loss under increasing CO₂. *Nature Communications*, 10(1). <https://doi.org/10.1038/s41467-018-07954-9>
- Deser, C., Tomas, R. A., & Sun, L. (2015). The role of ocean–atmosphere coupling in the zonal-mean atmospheric response to arctic sea ice loss. *Journal of Climate*, 28(6). <https://doi.org/10.1175/JCLI-D-14-00325.1>
- England, M. R., Eisenman, I., & Wagner, T. J. W. (2022). Spurious climate impacts in coupled sea ice loss simulations. *Journal of Climate*, 35(22). <https://doi.org/10.1175/JCLI-D-21-0647.1>
- Feldl, N., & Merlis, T. M. (2021). Polar amplification in idealized climates: The role of ice, moisture, and seasons. *Geophysical Research Letters*, 48(17). <https://doi.org/10.1029/2021GL094130>
- Flannery, B. P. (1984). Energy balance models incorporating transport of thermal and latent energy. *Journal of the Atmospheric Sciences*, 41(3). [https://doi.org/10.1175/1520-0469\(1984\)041<0414:EBMITO>2.0.CO;2](https://doi.org/10.1175/1520-0469(1984)041<0414:EBMITO>2.0.CO;2)

415 Hay, S. (2020). *Pattern scaling methods for understanding the response to polar sea ice loss in coupled*
416 *earth system models* (Doctoral dissertation). University of Toronto (Canada). Canada. Re-
417 trieved August 16, 2022, from [https://www.proquest.com/docview/2466731873/abstract/
418 DD83F44E6C2B45D2PQ/1](https://www.proquest.com/docview/2466731873/abstract/DD83F44E6C2B45D2PQ/1)

419 Hay, S., Kushner, P. J., Blackport, R., McCusker, K. E., Oudar, T., Sun, L., England, M., Deser,
420 C., Screen, J. A., & Polvani, L. M. (2022). Separating the influences of low-latitude warming
421 and sea ice loss on northern hemisphere climate change. *Journal of Climate*, *35*(8). [https:
422 //doi.org/10.1175/JCLI-D-21-0180.1](https://doi.org/10.1175/JCLI-D-21-0180.1)

423 Hurrell, J. W., Holland, M. M., Gent, P. R., Ghan, S., Kay, J. E., Kushner, P. J., Lamarque, J.-F.,
424 Large, W. G., Lawrence, D., Lindsay, K., Lipscomb, W. H., Long, M. C., Mahowald, N.,
425 Marsh, D. R., Neale, R. B., Rasch, P., Vavrus, S., Vertenstein, M., Bader, D., . . . Marshall,
426 S. (2013). The community earth system model: A framework for collaborative research.
427 *Bulletin of the American Meteorological Society*, *94*(9). [https://doi.org/10.1175/BAMS-D-
12-00121.1](https://doi.org/10.1175/BAMS-D-
428 12-00121.1)

429 McCusker, K. E., Kushner, P. J., Fyfe, J. C., Sigmond, M., Kharin, V. V., & Bitz, C. M. (2017).
430 Remarkable separability of circulation response to arctic sea ice loss and greenhouse gas
431 forcing. *Geophysical Research Letters*, *44*(15). <https://doi.org/10.1002/2017GL074327>

432 Screen, J. A., Deser, C., Smith, D. M., Zhang, X., Blackport, R., Kushner, P. J., Oudar, T., Mc-
433 Cusker, K. E., & Sun, L. (2018). Consistency and discrepancy in the atmospheric response
434 to arctic sea-ice loss across climate models. *Nature Geoscience*, *11*(3). [https://doi.org/10.
1038/s41561-018-0059-y](https://doi.org/10.
435 1038/s41561-018-0059-y)

436 Shaw, T. A., & Smith, Z. (2022). The midlatitude response to polar sea ice loss: Idealized slab-
437 ocean aquaplanet experiments with thermodynamic sea ice. *Journal of Climate*, *35*(8). [https:
//doi.org/10.1175/JCLI-D-21-0508.1](https:
438 //doi.org/10.1175/JCLI-D-21-0508.1)

439 Smith, D. M., Dunstone, N. J., Scaife, A. A., Fiedler, E. K., Copsey, D., & Hardiman, S. C. (2017).
440 Atmospheric response to arctic and antarctic sea ice: The importance of ocean–atmosphere
441 coupling and the background state. *Journal of Climate*, *30*(12). [https://doi.org/10.1175/
JCLI-D-16-0564.1](https://doi.org/10.1175/
442 JCLI-D-16-0564.1)

443 Smith, D. M., Screen, J. A., Deser, C., Cohen, J., Fyfe, J. C., García-Serrano, J., Jung, T., Kattsov,
444 V., Matei, D., Msadek, R., Peings, Y., Sigmond, M., Ukita, J., Yoon, J.-H., & Zhang,

- 445 X. (2019). The polar amplification model intercomparison project (PAMIP) contribution
446 to CMIP6: Investigating the causes and consequences of polar amplification. *Geoscientific*
447 *Model Development*, 12(3). <https://doi.org/10.5194/gmd-12-1139-2019>
- 448 Stroeve, J. C., Serreze, M. C., Holland, M. M., Kay, J. E., Malanik, J., & Barrett, A. P. (2012).
449 The arctic's rapidly shrinking sea ice cover: A research synthesis. *Climatic Change*, 110(3).
450 <https://doi.org/10.1007/s10584-011-0101-1>
- 451 Sumata, H., de Steur, L., Divine, D. V., Granskog, M. A., & Gerland, S. (2023). Regime shift in arctic
452 ocean sea ice thickness. *Nature*, 615(7952). <https://doi.org/10.1038/s41586-022-05686-x>
- 453 Sun, L., Deser, C., Tomas, R. A., & Alexander, M. (2020). Global coupled climate response to polar
454 sea ice loss: Evaluating the effectiveness of different ice-constraining approaches. *Geophysical*
455 *Research Letters*, 47(3). <https://doi.org/10.1029/2019GL085788>
- 456 Tebaldi, C., & Arblaster, J. M. (2014). Pattern scaling: Its strengths and limitations, and an update
457 on the latest model simulations. *Climatic Change*, 122(3). [https://doi.org/10.1007/s10584-](https://doi.org/10.1007/s10584-013-1032-9)
458 [013-1032-9](https://doi.org/10.1007/s10584-013-1032-9)
- 459 Wagner, T. J. W., & Eisenman, I. (2015). How climate model complexity influences sea ice stability.
460 *Journal of Climate*, 28(10). <https://doi.org/10.1175/JCLI-D-14-00654.1>