

A Machine Learning Augmented Data Assimilation Method for High-Resolution Observations

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Key Points:

- Machine learning augmented data assimilation of high-resolution observations improves the analysis in a nonlinear dynamical model.
- Explainable Artificial Intelligence identifies system covariances to guide neural network training for analysis state reproduction.
- Short-term forecasts from the analysis generated by the machine learning augmented data assimilation are more accurate and more reliable.

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Abstract

The accuracy of initial conditions is an important driver of the forecast skill of numerical weather prediction models. Increases in the quantity of available measurements, in particular high-resolution remote sensing observational data products from satellites, are valuable inputs for improving those initial condition estimates. However, the data assimilation methods used for integrating observations into forecast models are computationally expensive. This makes incorporating dense observations into operational forecast systems challenging, and it is often prohibitively time-consuming. As a result, large quantities of data are discarded and not used for state initialization. We demonstrate, using the Lorenz-96 system for testing, that a simple machine learning method can be trained to assimilate high-resolution data. Using it to do so improves both initial conditions and forecast accuracy. Compared to using the Ensemble Kalman Filter with high-resolution observations ignored, our augmented method has an average root-mean-squared error reduced by 15%. Ensemble forecasts using initial conditions generated by the augmented method are more accurate and reliable at up to 10 days of forecast lead time.

Plain Language Summary

Weather forecasts are highly sensitive to the estimate of the current state of the atmosphere, known as initial conditions. The atmosphere is chaotic, meaning that small errors in this estimate can grow quickly as the forecast model predicts events further into the future. The satellite era has contributed to large improvements in weather forecasts by providing additional data that allow for more accurate estimates of initial conditions. However, current methods for generating initial conditions are computationally time-consuming, and as a result, large fractions of available measurements are not used for this purpose. In a proof-of-concept study using a simplified representation of the atmosphere for testing, we train a machine learning method to replicate the results of a traditional method. Once trained, machine learning models are usually very fast. Applying the trained model exclusively to measurements that would otherwise be too time-consuming to use produces better initial conditions and more accurate forecasts.

1 Introduction

The accuracy of operational weather forecast models is highly dependent on the quality of the initial conditions provided to the model (Bauer et al., 2015). To correct drift and maintain the robustness of forecasts, model initial conditions are regularly updated based on measurements (Bannister, 2017; Edwards et al., 2015). These measurements include both in-situ data, such as weather station measurements, and remotely sensed data (Zhang & Tian, 2021; Choi et al., 2017). Observations are noisy and may not be aligned with the model grid or state variables; the task of identifying optimal initial conditions consistent with all available information is therefore challenging and computationally expensive. Data assimilation (DA) methods are employed to do this. With the proliferation of high-resolution datasets, often at resolutions higher than that of the forecast models, otherwise useful data is regularly ignored and not assimilated into operational models due to time or computational constraints (Eyre et al., 2022; Kumar et al., 2022). Assimilation of a subset of available satellite data has improved forecasts, making it likely that leveraging currently unused data could generate further improvements (Eyre et al., 2022).

DA techniques can be generally categorized as variational methods or sequential methods (Bannister, 2017; Edwards et al., 2015). Variational methods use numerical optimization, finding the initial condition that minimizes an error metric or cost function. Sequential methods nowadays are some variant of the Ensemble Kalman Filter (EnKF), in which a set of model realizations are simulated to quantify covariance structures before assimilating observations (Evensen, 2003; Hoteit et al., 2018). Both methods require running multiple simulations of the full forecast model, a step that is computationally expensive and time-

63 consuming. To capture the information of a high-resolution measurement, the model itself
64 must at least match the resolution of the measurement – further increasing the cost of this
65 step as model run time scales with resolution. In addition to the necessity of using a higher
66 resolution model (run multiple times), the physics of smaller scale dynamics create more
67 complex correlation structures, and a larger ensemble size is required to actually improve
68 the forecast (Miyoshi et al., 2015).

69 An additional cost associated with assimilating high-resolution observations is the ob-
70 servation operator. Both variational and sequential methods assess the error of a model
71 forecast for a given initial condition in observation space. This requires, for each obser-
72 vation, explicitly mapping between forecast model space and observation space. For some
73 observations, this is straightforward. For others, particularly for remotely sensed data such
74 as high-resolution satellite measurements, this calculation itself is a physics-based model
75 that can be a computational bottleneck (Eyre et al., 2022). In some operational models,
76 the trade-off between the speed and accuracy of these observation operators is already an
77 important avenue of research for improving the performance of their DA systems even before
78 currently unusable high-resolution data is considered (Shahabadi & Buehner, 2021). The
79 observation operator calculation must be performed for each data point and so also scales
80 with the number of discrete observations, again increasing its cost.

81 When possible, assimilation of these remotely sensed observations can and has improved
82 forecasts, especially since in-situ observations of large portions of the atmosphere and surface
83 are sparse (Bannister, 2017). Efforts to incorporate satellite and other remotely sensed
84 observations into assimilation systems have been effective at improving model initialization
85 and forecast accuracy (Shahabadi & Buehner, 2021). However, as a result of the expense
86 associated with assimilation much of the potential of these high-resolution measurements for
87 improving state initialization in forecast models has not been realized. Currently employed
88 DA methods are simply not efficient enough to sufficiently quickly ingest this data to be
89 useful in an operational setting. Machine Learning (ML) methods may provide a potential
90 solution.

91 ML techniques have been increasingly used in earth science applications, including
92 DA (Sonnewald et al., 2021; Abarbanel et al., 2018; Bonavita et al., 2021; Penny et al.,
93 2022). They are appealing for this particular problem mostly due to their speed. While
94 the training process is often expensive, once trained ML methods are very fast compared
95 to weather forecast models. Since many of the bottlenecks in traditional DA methods are
96 related to computational efficiency, as described above, much of the effort in employing
97 ML to improve DA has been targeted at the most computationally expensive parts of the
98 process.

99 One obvious place to look is at the model simulations themselves. Attempts to use deep
100 learning, in which neural networks comprised of many layers are used to capture complex
101 structures, have proven successful. The basic approach is to train the ML model on the
102 output of a traditional physics-based model (Kim et al., 2019; Pathak et al., 2017). The
103 result is more computationally efficient but at the cost of accuracy. In the context of DA, it
104 has been demonstrated that model surrogates can be successfully trained iteratively using
105 DA state estimates (Brajard et al., 2020; Gottwald & Reich, 2021).

106 Extending this approach beyond demonstrating that ML can capture the dynamics
107 of complex and chaotic systems, augmented approaches that use model surrogates only to
108 represent scales unresolved by the physical model (Brajard et al., 2021) have shown that
109 the integration of ML as a model surrogate can generate improvements over traditional
110 DA methods. Other work has demonstrated the utility of using ML model surrogates to
111 increase the ensemble size beyond what would be otherwise practical (Yang & Grooms,
112 2021; Wu et al., 2021). Related to the issue of unresolved scale and model resolution, ML
113 has been employed to successfully generate parameterizations used to capture unresolved

114 physics, making the generation of the tangent linear models needed in many variational DA
115 methods more efficient (Hatfield et al., 2021).

116 The observation operator, which can be another computational bottleneck, has also
117 been targeted using ML (Jung et al., 2010; J. Liang et al., 2023; Wang et al., 2022; Geer,
118 2021; X. Liang et al., 2022; Stegmann et al., 2022). Other efforts have used ML methods to
119 identify regions of tropical cyclone activity to target high-resolution modeling in a subdo-
120 main (Lee et al., 2019), to perform bias correction of model forecasts before they are fed into
121 the assimilation algorithm (Arcucci et al., 2021; Chen et al., 2022), and apply time-varying
122 localization to the covariance structure of the system (Lacerda et al., 2021).

123 In contrast, relatively limited efforts have been directed toward using ML to perform
124 the assimilation step directly. Rather than using ML to replace pieces of the DA process,
125 we propose an augmented DA method in which a ML model is trained offline to assimilate
126 high-resolution measurements. Convolutional neural networks (CNN) are particularly good
127 candidates for assimilating spatial data and learning the spatial correlation structure of the
128 system of interest, as their design and main demonstrated use cases rely on their ability to
129 identify spatial patterns (Dong et al., 2021; Mallat, 2016).

130 In a real-world scenario, computational resource bottlenecks require some high-resolution
131 observations to be either thinned before being assimilated or discarded entirely. As a proof-
132 of-concept demonstration for our proposed method, we use a synthetic system with observa-
133 tions available at regular time intervals. The observations are alternatively high-resolution
134 or low-resolution. Low-resolution observations are always assimilated using the EnKF, and
135 in the augmented method, high-resolution observations are assimilated using the trained
136 CNN.

137 This study will explore these two hypotheses:

- 138 1. A shallow CNN can be successfully trained to reproduce the analysis of the EnKF
139 offline
- 140 2. When used online to assimilate otherwise ignored high-resolution data, with the tradi-
141 tional EnKF used for low-resolution data, assimilation performance will be improved

142 with the chaotic Lorenz-96 model as the test system. Yet the relevance is broader with
143 applications in weather and climate predictions. Section 2 describes the Lorenz-96 modeling
144 system, the machine learning augmentation of EnKF framework and the explainable AI
145 methodology. Section 3 presents the results from the experiments and analyses performed.
146 Section 4 summarizes the results and discussion and section 5 concludes.

147 2 Methods

148 2.1 Lorenz-96 System

149 The Lorenz-96 system is described by a set of N discrete differential equations, designed
150 to mimic some behaviors of the atmosphere (Lorenz, 2005). It is commonly used for testing
151 data assimilation methods. It is defined as a 1-D analog of an atmospheric state variable at
152 discrete points evenly spaced in the zonal direction, with its dynamics governed by:

$$\frac{dx_i}{dt} = (x_{i+1} - x_{i-2})x_{i-2} - x_i + F \quad (1)$$

153 for $i \in [1, N]$ and F a constant forcing term. The system is cyclically symmetric with grid
154 point $i = N + 1$ equal to grid point $i = 1$. We use $F = 8$, a value for which the system is
155 known to be chaotic, and $N = 40$, a typical value for testing DA methods.

156 To generate a reference trajectory for our experiments, we numerically integrated Equa-
157 tion 1 forward. A 5th order Runge-Kutta method was used, with a variable time step to

158 control error assuming 4th-order accuracy (Dormand & Prince, 1980), as implemented in
 159 the SciPy package (Virtanen et al., 2020). The maximum allowable relative error was set
 160 to 0.001 and the maximum allowable absolute error to 10^{-6} . The system is in an unstable
 161 equilibrium when all variables are equal to F ; initial conditions were set by perturbing one
 162 of the variables to a value of 8.01. The system was integrated out to $t = 2000$ and output
 163 was generated at time intervals of $\Delta t = 0.05$ generating data for a 40 variable vector at
 164 40,000 time steps, or 800,000 data points representing the true time evolution of the system.
 165 Synthetic observations were generated by adding normally distributed random noise with
 166 a standard deviation equal to 30% of the standard deviation of the reference state. This
 167 level of observation noise is consistent with other work done using the Lorenz-96 system for
 168 testing DA methods. (Hatfield et al., 2018; Brajard et al., 2020; Hoteit et al., 2008).

169 2.2 The Ensemble Kalman Filter

170 Data assimilation is used to combine model forecasts and observations and solves the
 171 filtering problem. Formally, the filtering problem is to generate a minimum-variance esti-
 172 mate of a state vector, \vec{x} , conditional on a noisy forecast and a noisy observation. The state
 173 vector evolves in time with model dynamics represented by a forward operator M . The time
 174 evolution of the system is defined iteratively; the system states at times t_i and t_{i+1} , \vec{x}_i and
 175 \vec{x}_{i+1} are related via:

$$M(\vec{x}_i) = \vec{x}_{i+1} + \vec{\mu} \quad (2)$$

176 where μ is the assumed model forecast error. Observations y_i at time t_i are related to the
 177 state vector via an observation operator, H :

$$y_i = H(\vec{x}_i) + \vec{\nu} \quad (3)$$

178 where ν is the assumed observation error.

179 The solution to the filtering problem is referred to as the analysis. When forecast and
 180 observation errors are unbiased, normally distributed, and independent, and the forecast
 181 model and observation operator are both linear, the Kalman filter (KF) provides the closed-
 182 form optimal solution of the filtering problem (Kalman, 1960).

183 In earth system applications, the system's time evolution and thus the forecast models
 184 are often non-linear. The Ensemble Kalman filter (EnKF) is an extension of the KF that
 185 accommodates nonlinear models at the cost of being an approximate, rather than exact,
 186 solution to the filtering problem by using an ensemble of model forecasts (Evensen, 2003).
 187 The EnKF analysis equation is:

$$X^a = X^f + CH^T(HCH^T + R)^{-1}(Y - HX^f). \quad (4)$$

188 Here, X^a is a matrix whose column vectors are analysis ensemble members. X^f is
 189 a matrix whose column vectors are individual forecasts. C is the sample covariance of
 190 the ensemble forecast, X^f , used as an approximate representation of the true covariance/
 191 R is the observation error covariance matrix, and Y is a matrix whose columns are the
 192 observation vector y_i . To ensure that the covariance does not systematically underrepresent
 193 the true error, random Gaussian noise with covariance R is added to the observation matrix
 194 Y (Evensen, 2003).

195 The EnKF assumes normality for the forecast and observation errors, $\vec{\mu}$ and $\vec{\nu}$, although
 196 has been demonstrated to be somewhat robust to non-Gaussian distributions (Reichle et al.,
 197 2002). Also relevant for earth system models in which the state space is very large, the EnKF
 198 can be effective even when the number of ensemble members is much smaller than the size
 199 of the state space. This is in contrast to more exact methods such as particle filters, which

Run Name	Observation Error StDev (fraction)	Ensemble Size	Inflation Factor	Localization Distance
Base	0.3	100	1	5
s1	0.4	100	1	5
s2	0.2	100	1	5
s3	0.3	33	1	5
s4	0.3	1000	1	5
s5	0.3	100	1.01	5
s6	0.3	100	1.05	5
s7	0.3	100	1.1	5
s8	0.3	100	1	3
s9	0.3	100	1	7

Table 1. Sensitivity settings for the EnKF runs. Observation error is presented as observation noise standard deviation as a fraction of total system standard deviation.

often exhibit stability problems in such situations (Farchi & Bocquet, 2018; Hoteit et al., 2008).

The EnKF is known to be vulnerable to issues associated with the fact that it approximates a PDF with samples represented by a finite number of ensemble members. These issues include spurious correlations as well as a covariance collapse, in which the ensemble becomes sharply clustered at a point in state space far away from the true state. To address this localization is often used, a technique that has been shown to improve performance by reducing the impact of spurious correlations of the system state at distant grid points (Evensen, 2003). For this application we used a step function to localize the covariance, setting any covariance between variables greater than five grid points apart equal to zero.

Covariance inflation, in which all covariance values are multiplied by a factor greater than 1 before computing equation 4, is another technique used for improving the stability and performance of the EnKF. Our base settings did not include covariance inflation as our initial experiments did not show significant improvements employing it. Both approaches can improve performance in some circumstances by preventing covariance collapse (Evensen, 2003). However, since both address issues created by the finite size of the ensemble, they become less necessary with larger ensemble sizes and must be tuned (Miyoshi et al., 2015). As such they are appropriate parameters to vary in our sensitivity analysis in order to identify optimal values.

We use the EnKF here for two purposes: to generate training data for a CNN and as a benchmark to evaluate the performance of our augmented method. After assimilating the synthetic observations with the EnKF using settings described above, at all 40,000 time steps, the following data are available: the true model state, the model forecast, the synthetic observation, and the EnKF analysis. Other combinations of settings were also used to assess sensitivity. These are outlined in Table 1. Observation error is specified as the standard deviation of the added noise used to generate the synthetic observations, as a fraction of the system standard deviation.

2.3 CNN Architecture and Training

The machine learning model consists of a convolutional neural network with two hidden layers. Its architecture is shown in Figure 1. The input layer has two channels: the model ensemble forecast mean and the difference between the forecast mean and the observation (the innovation). A CNN is defined by the following parameters for each layer: the filter size, the number of feature maps, and the activation function (Alzubaidi et al., 2021). We use a filter size of 3 for all convolutions. The weights of each convolutional filter are independent of space and are applied uniformly across the domain. 5 feature maps are used in both hidden

235 layers, with each feature map assigned different filter weights and a constant bias weight.
 236 The ReLU activation function is used for both hidden layers and no activation function is
 237 applied to the output, which is then a linear weighted sum of the activation values in the
 238 second hidden layer.

239 Output from a convolution has a smaller dimension than its input, since locations on
 240 the edge of the domain don't have a neighboring point on one side. In image recognition
 241 and other similar tasks, zero-padding is used to address this issue by artificially adding
 242 zeros to the input on the edges of the domain. Here, with a cyclically symmetric system,
 243 zero-padding is not an appropriate solution. Instead, we implemented cyclic padding such
 244 that the neighboring spatial nodes for $i = 1$ are $i = N$ and $i = 2$. Similarly, the neighboring
 245 spatial nodes for $i = N$ are $i = 1$ and $i = N - 1$. Applying three convolutions with a filter
 246 size of three will reduce the domain size by 6. The data from spatial locations $i = [1, 3]$
 247 were concatenated to the end of the spatial domain, and the data from spatial locations
 248 $i = [N - 2, N]$ were concatenated to the beginning of the spatial domain. This maintains
 249 the cyclic nature of the Lorenz-96 system and ensures that the size of the CNN output
 250 matches the dimensions of the system. The size of the input to the neural network is 46×2 .
 251 Its output, the analysis, is 40×1 . The model has 131 trainable weights.

252 The training data is comprised of the first half of the EnKF analysis states, for times
 253 $t = 0$ to 1,000 covering 20,000 individual time steps. The dataset from the best-performing
 254 EnKF sensitivity run settings described in Table 1 was used for training. A stochastic
 255 gradient descent optimizer (Sutskever et al., 2013) was used to train the model, using 20
 256 training epochs and 100 batches per epoch.

257 **2.4 Augmented Method and Experimental Setup**

258 The augmented method is designed to be applicable to a scenario in which high-
 259 resolution observations are available but not assimilated (Figure 2). To create an analog
 260 of this scenario with the Lorenz-96 system, we created a set of low-resolution observations
 261 at every other time step ($\Delta t = 0.1$) for the second half of the time series ($t = 1000.05$ to
 262 $t = 2000$) by randomly selecting 25% of the variables to measure. The EnKF using base
 263 settings was then used to assimilate these observations. This run is the baseline against
 264 which the augmented method will be compared. This method will subsequently be referred
 265 to as “EnKF SparseObs”, with the method used to generate the training data in which
 266 100% of variables were measured at every time step referred to as “EnKF AllObs”.

267 The augmented method uses the EnKF to assimilate low-resolution observations. On
 268 alternating time steps, a “high-resolution” observation is available that includes observa-
 269 tions of 100% of the variables. For EnKF SparseObs these observations are assumed to
 270 be prohibitively computationally expensive to assimilate and are therefore ignored. The
 271 forecast continues on to the next time step where a low-resolution observation is available
 272 and assimilated by the EnKF. In the augmented method, the CNN is used to assimilate the
 273 high-resolution observations that cannot be assimilated by the EnKF.

274 The CNN takes the ensemble forecast mean and the observation as input and returns
 275 a single analysis as output. At this stage, an ensemble must be re-created to generate
 276 an ensemble forecast for the next time step (where the EnKF will be applied to the low-
 277 resolution observation). To be consistent with the analysis generated by the CNN, the new
 278 ensemble mean must be equal to the vector analysis produced by the CNN. We create such
 279 an ensemble by computing the vector difference between the CNN analysis value and the
 280 ensemble forecast mean, $\vec{\delta} = \vec{x}_{mean}^f - \vec{x}_{cnn}^a$. To generate the new initial ensemble, $\vec{\delta}$ is
 281 subtracted from each member of the ensemble forecast. The new ensemble mean then by
 282 definition is equal to the vector analysis generated by the CNN with the same spread as the
 283 ensemble forecast.

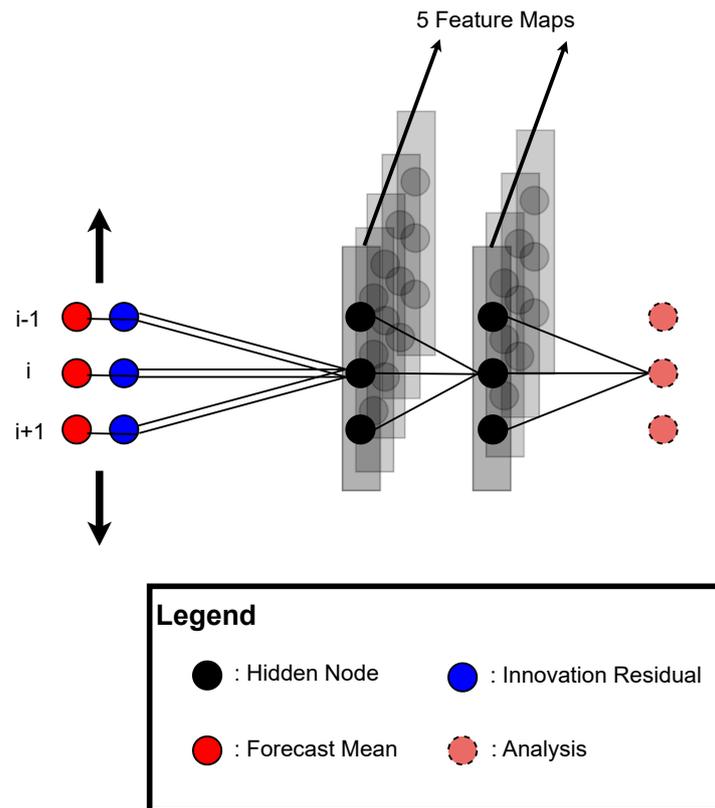


Figure 1. Architecture of the CNN trained to emulate the EnKF analysis step with observations of all variables. Forecast mean and observations are provided in separate collocated input channels. Two hidden convolutional layers each contain 5 feature maps, with different filter weights. Analysis mean is generated as output.

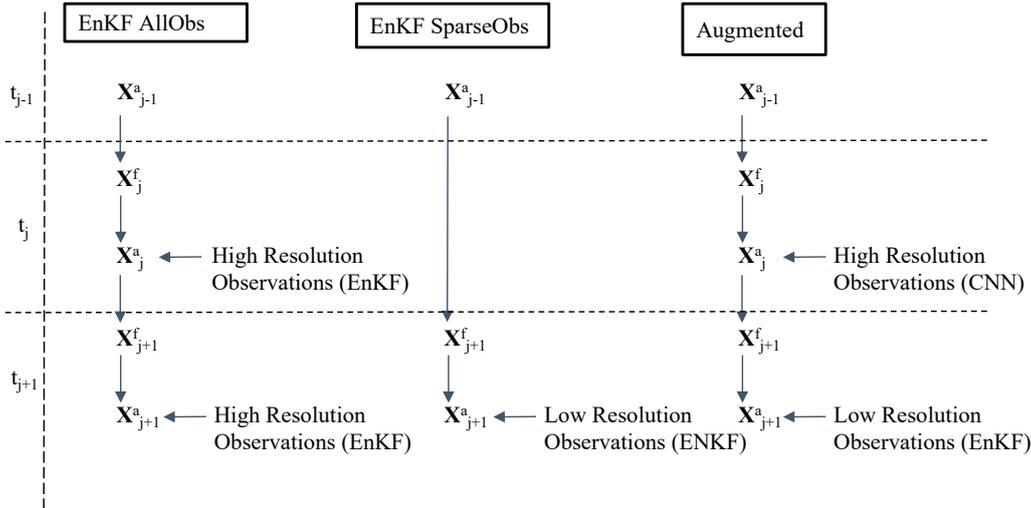


Figure 2. Flow chart of the experimental setup and augmented method. EnKF AllObs is provided with full observations at every time step. EnKF SparseObs is provided with observations 25% of the variables at every other time step. The augmented method is identical to EnKF SparseObs but is additionally provided with observations of 100% of the variables on alternating time steps and uses the trained CNN to assimilate these.

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2.5 Explainable AI

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Machine learning models are fast to run and accurate when sufficient training data are available. In many earth system science applications, the computational efficiency of traditional tools is a significant bottleneck and available training data is voluminous. These models have a major drawback, however: models are a black box and it is therefore often not clear how they are generating their predictions (Gevaert, 2022). Using testing and validation datasets can provide some level of confidence in the models by demonstrating their level of accuracy on data not used for training. If they are to be deployed in something like an operational weather forecast system, however, such demonstrations may not provide a sufficient level of confidence. Out-of-sample input data cannot be guaranteed never to occur, and no guarantees can be made about the behavior of the machine learning model when presented with such data.

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A variety of tools are available to make otherwise opaque data-driven models more transparent, collectively referred to as Explainable AI (XAI) methods (Linardatos et al., 2021). Shapely Additive Explanations, or SHAP, is one such tool. SHAP quantifies the impact of a specific input variable on the output generated by a model. The method is model-agnostic and is equally applicable to a simple linear regression model or a deep neural network with millions of trainable parameters. Full details and a formal definition can be found in Lundberg and Lee (2017). Heuristically, a SHAP value is the anomaly in an output variable attributable to the anomaly in an input variable. It provides a way of apportioning the deviation from the mean in the output to each input variable. This information can increase confidence that the trained model is reliable as well as provide insights into the structure of the underlying system.

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We apply it here to analyze how the trained CNN generates analyses from forecasts and innovations. In a DA context, the behavior of the CNN should be predictable and consistent with our understanding of the dynamics of the Lorenz-96 system; it should not, for example, heavily weight forecasts from highly spatially distant nodes. Evaluating the

Run Name	Observation Error (StDev fraction)	Ensemble Size	Inflation Factor	Localization Distance	RMSE (% of Observation StDev)
Base	0.3	100	1	5	20.3059
s1	0.2	100	1	5	20.1084
s2	0.4	100	1	5	20.6152
s3	0.3	33	1	5	29.5916
s4	0.3	1000	1	5	19.6315
s5	0.3	100	1.01	5	20.3089
s6	0.3	100	1.05	5	20.3404
s7	0.3	100	1.1	5	20.4216
s8	0.3	100	1	3	22.6087
s9	0.3	100	1	7	19.4958

Table 2. EnKF-only sensitivity results. RMSE is presented as a fraction of the observation standard deviation to allow for comparison between different observation error settings.

311 CNN in this way can provide confidence in its ability to perform well when presented with
312 new data.

313 **3 Results**

314 **3.1 Sensitivity and Training**

315 The results of the base run and 9 sensitivity runs using the EnKF are outlined in Table
316 2. These runs are intended to identify optimal settings for generating training data, with the
317 EnKF assimilating all observations at every time step (i.e. the high-resolution observation at
318 every time step). The performance for each run is evaluated as the mean analysis root-mean-
319 squared error (RMSE) divided by the standard deviation of the observation error. For all
320 10 cases, the EnKF analysis has a lower error than the observation error, as expected, with
321 all runs achieving better than 24% on this metric. As the EnKF approximates the optimal
322 solution by using the first two moments of the forecast ensemble to represent a normal
323 distribution, errors caused by the finite size of the ensemble are expected to decrease with
324 ensemble size. This is evident in our results, which show larger ensemble sizes producing
325 lower errors.

326 Localization and covariance inflation can improve EnKF performance by mitigating
327 errors related to finite ensemble size but can be detrimental for larger ensemble sizes as
328 such errors become less important. We expect the performance to be dependent on local-
329 ization and inflation settings but it is not clear a priori which values will be optimal. The
330 best-performing combination of settings was run s9 with localization of 7 grid spaces and
331 covariance inflation factor of 1 (i.e. no inflation). These are the EnKF settings used for
332 training the CNN and used in the augmented method.

333 The results from the training process are shown in Figure 3. The training targets were
334 the EnKF analyses produced using observations of all variables as described in section 2.3.
335 CNN error can be considered in terms of how well CNN output matches the EnKF analyses
336 as well as its deviation from the true state. The RMSE with respect to these training targets
337 is shown across 20 training iterations. Additionally, the error with respect to true states in
338 the second half of the time series, i.e. the set not used for training, is included for validation.
339 Over-fitting would be indicated by an increase in validation error even as the training error
340 remained flat or decreased. This is not evident here, demonstrating that our trained CNN
341 is not overfitting and produces reliable predictions when presented with data from outside
342 its training set (Ying, 2019).

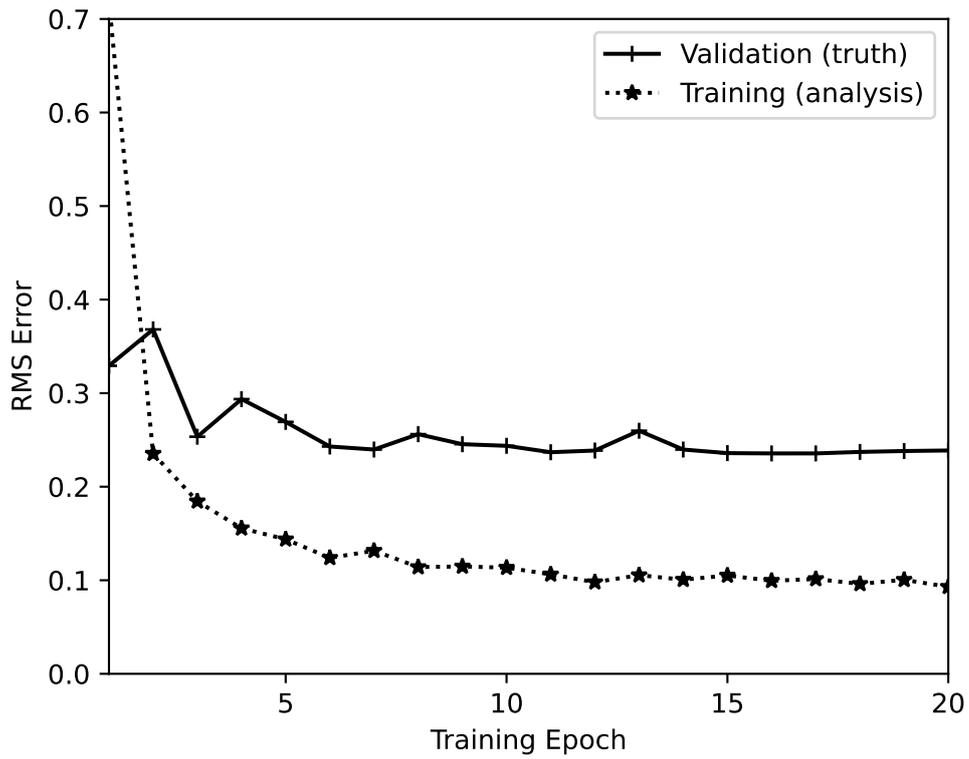


Figure 3. Root mean squared error of the CNN through training epochs, with the error shown based on both training targets (dashed line) and validation error (solid line). Training error is with respect to EnKF analysis, validation error is with respect to truth.

Run Name	Observation Error (StDev fraction)	Ensemble Size	Inflation Factor	Localization Distance	Augmented RMSE	SparseObs RMSE
Base	0.3	100	1	5	0.750	0.877
s1	0.2	100	1	5	n/a	n/a
s2	0.4	100	1	5	n/a	n/a
s3	0.3	33	1	5	0.782	1.453
s4	0.3	1000	1	5	0.7371	0.8243
s5	0.3	100	1.01	5	0.751	0.883
s6	0.3	100	1.05	5	0.754	0.876
s7	0.3	100	1.1	5	0.759	0.882
s8	0.3	100	1	3	0.873	0.989
s9	0.3	100	1	7	0.728	0.899

Table 3. Sensitivity results for the augmented and EnKF SparseObs methods. RMSE for both is presented as a fraction of the observation error standard deviation. For all runs, the augmented method outperforms EnKF SparseObs.

343 Another check on the trained CNN is to compare its RMSE on the validation dataset
344 to the observation error. To generate an improvement in the state estimate the CNN must
345 perform better than observations alone. Using EnKF AllObs forecasts and residuals, the
346 final validation RMSE with respect to the true state in Figure 3 is 23% of the observation
347 standard deviation.

348 The sensitivity of the augmented method to different settings was tested. These results
349 are shown in Table 3. For all runs, the CNN trained on results using the s9 run settings
350 was used. The s1 and s2 run settings were not tested; the CNN was trained on data with
351 the observation error specified by s9 settings and the s1 and s2 settings are therefore not
352 applicable for the augmented method. For those cases that are applicable, the augmented
353 method performance was compared to the EnKF assimilating only the low-resolution obser-
354 vations (EnKF SparseObs). For all sensitivity settings, the augmented method outperforms
355 EnKF SparseObs (Table 3).

356 3.2 Performance Comparison

357 Having shown that the trained CNN does not over-fit and that its error is 23% of
358 observation error, we can now assess the performance of the augmented method using this
359 CNN. In addition to the augmented method and EnKF SparseObs, the performance of
360 EnKF AllObs assimilating observations of all variables at every time step is included for
361 comparison. The analysis RMSE for all three methods is shown in Figure 4. Time is shown
362 as earth-years with 1 model time unit is equivalent to 5 real days (Lorenz, 2005). EnKF
363 AllObs performs best with an average RMSE of 0.22. Considering only the density and
364 frequency of assimilated observations, this comparative overperformance is unsurprising
365 as EnKF AllObs assimilates more data than the other methods. More interestingly, the
366 augmented method performs better than EnKF SparseObs, with an average RMSE of 0.75
367 compared to 0.88, representing an improvement of 14.5%.

368 The other thing to note is the variability of errors between methods. The time series on
369 the left is smoothed, and in this rolling average the augmented method consistently outper-
370 forms sparse obs at nearly all time steps. The histogram on the right shows the distribution
371 of errors at all time steps for EnKF AllObs, EnKF SparseObs, and the augmented method.
372 There is substantial overlap in the distribution of errors; using unsmoothed data, the aug-
373 mented method outperforms in 30% of coincident time steps. The EnKF SparseObs errors
374 have a notably fatter tail in the histogram, however. These spikes are periods where the

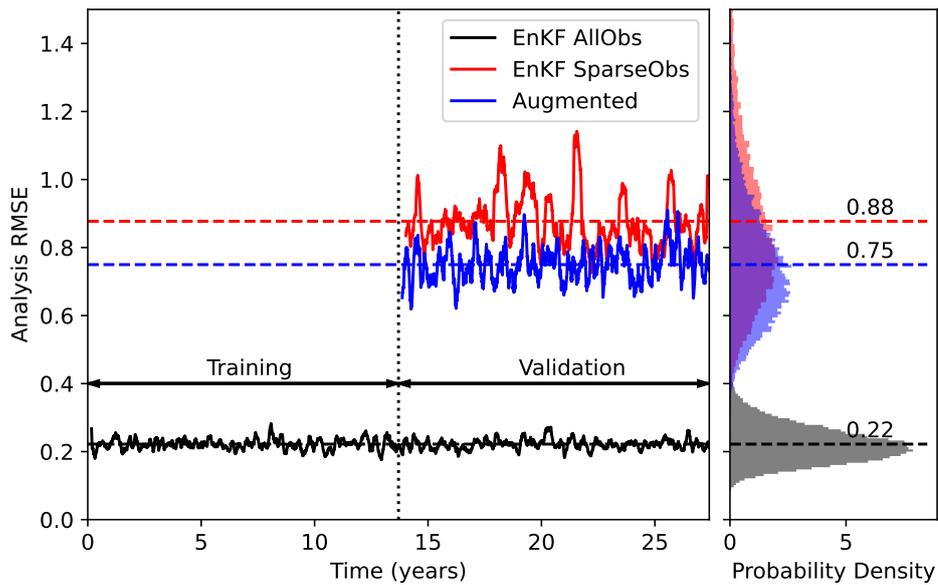


Figure 4. A time series (left) and histogram (right) of the RMSE of the EnKF AllObs, EnKF SparseObs, and augmented methods. The mean error for each method is represented by a horizontal dashed line. The first half of the time series includes only results for EnKF AllObs, which is used for training the CNN. The second half of the time series includes EnKF SparseObs and augmented as well, with both initialized using the last analysis produced by the EnKF AllObs. The time series data is smoothed with a moving window of 60 days for readability. On the right, a histogram of the distribution of RMSE for all three methods is shown using the same axis as the time series plot. This plot uses unsmoothed data and as a result, the tails extend beyond the range of time series traces.

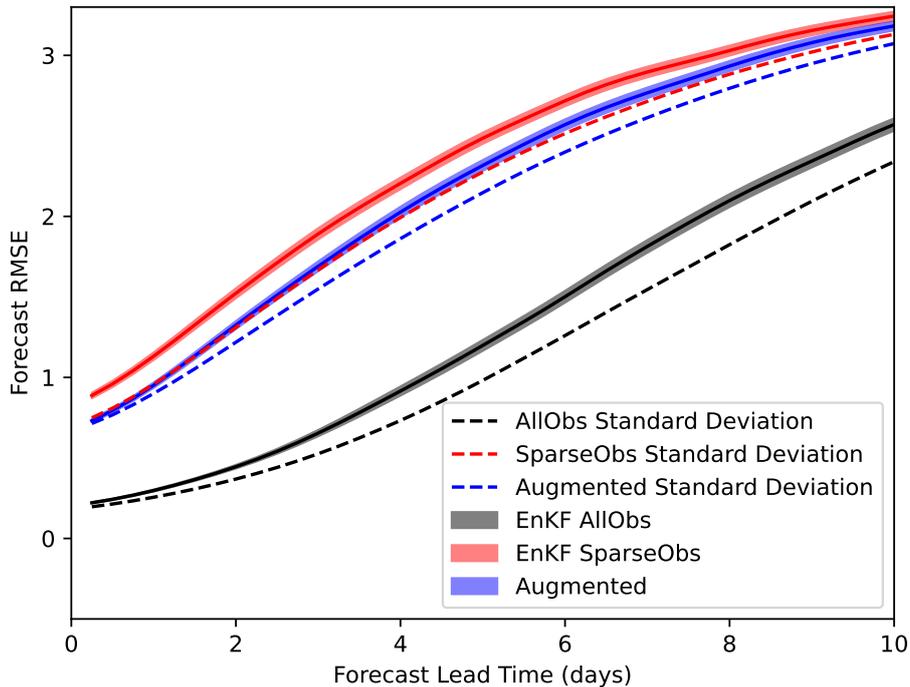


Figure 5. The forecast accuracy out to 10 days using initial conditions produced by the augmented method as well as the EnKF (sparse and all obs). 95% confidence intervals are included for all three methods based on the RMSE standard deviation across 1,000 randomly selected initial conditions. The mean ensemble standard deviations are also shown as dashed lines.

375 state estimate diverged from reality, generating instabilities in the EnKF that resulted in
 376 large errors.

377 Despite having a similar error distribution to EnKF SparseObs, the augmented method
 378 does not have the same fat tail. It is better at maintaining the state estimate in the vicinity
 379 of the true state, preventing instabilities and periodic spikes in the analysis error. This
 380 accounts for the consistent over-performance in the smoothed time series. The improved
 381 stability is an important factor in evaluating the relative performance and suggests that the
 382 augmented method is more reliable in excess of what would be otherwise assessed based on
 383 the fact that it only outperforms EnKF SparseObs in 30% of time steps. The improved
 384 stability and reduced mean RMSE are clear benefits of exploiting all available data in
 385 assimilation using an efficient but possibly sub-optimal technique (the CNN) compared to
 386 ignoring a subset of observations.

387 Another way of assessing the performance of the three methods is to generate forecasts
 388 using their analyses as initial conditions. Forecast skill over time can then be compared.
 389 These results are shown in Figure 5. The mean error of ensemble forecasts from a sample
 390 of initial conditions is plotted out to 10 days of lead time. As with the results in Figure 4,
 391 EnKF AllObs performs best, generating better forecasts for all lead times. The augmented
 392 method again outperforms EnKF SparseObs. Out to 5 days of forecast lead time, the RMSE
 393 of forecasts generated using initial conditions from the augmented method is statistically

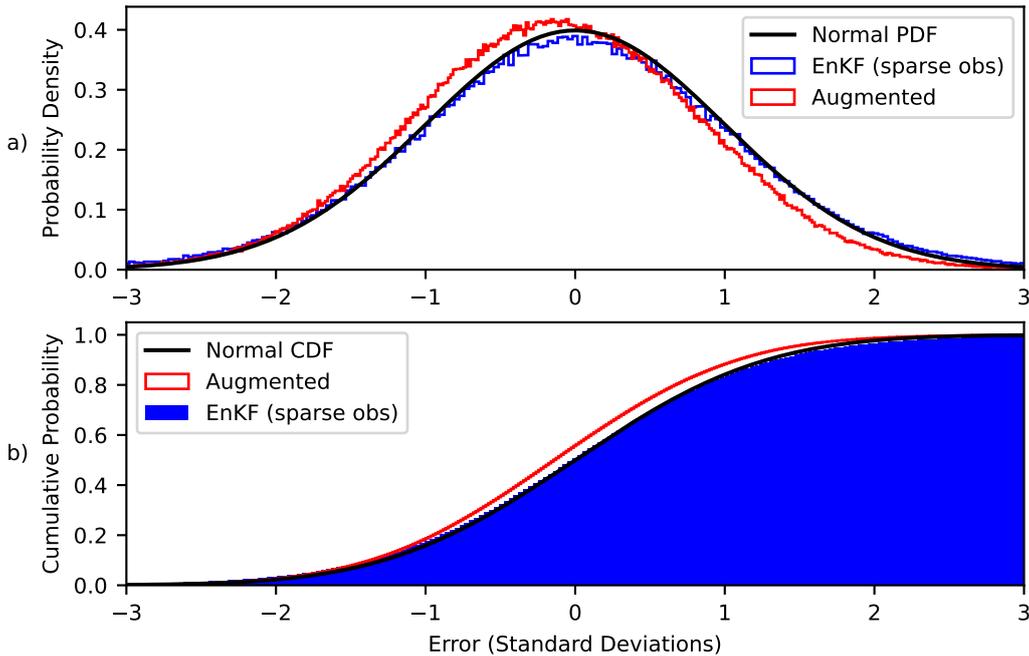


Figure 6. The distribution of augmented (red) and EnKF SparseObs (blue) analysis errors normalized by ensemble standard deviation as probability density plots (a) and cumulative probability plots (b). A reference unit normal distribution is also included in both plots in black.

394 significantly better at the $p < 0.05$ level. Graphically, this is immediately evident as the 95%
 395 confidence interval bands do not initially overlap.

396 Figure 5 also shows another metric for evaluating the reliability of the ensemble fore-
 397 casts. By definition, when errors are unbiased the standard deviation of the error and the
 398 RMSE are equivalent. If the ensemble spread is reflective of the true error, then the actual
 399 RMSE should equal the ensemble standard deviation (Leutbecher & Palmer, 2008; Gneit-
 400 ing & Katzfuss, 2014). If the ensemble is overprecise with estimated errors smaller than
 401 actual, it is said to be underdispersive. If the ensemble is under-precise, with its spread
 402 overestimating actual errors and precision, it is said to be overdispersive.

403 Here, the ensemble standard deviation for all three methods is generally less than
 404 the RMSE indicating underdispersive ensemble forecasts that do not adequately represent
 405 the true forecast error. For the first day, however, the standard deviation of the augmented
 406 analysis error is within the 95% confidence interval of its RMSE. Beyond this, the augmented
 407 method is underdispersive but less so than EnKF SparseObs with the difference between
 408 its RMS and standard deviation smaller for several more days. This is another indication
 409 of the improved reliability of the augmented method compared to EnKF SparseObs. In
 410 addition to avoiding large spikes in RMSE shown in Figure 4, ensemble forecasts using the
 411 augmented method analyses as initial conditions produce both more accurate forecasts as
 412 well as uncertainty estimates that more closely match the true statistics of forecast errors.

413 For a more detailed examination of the reliability of ensemble state estimates, we exam-
 414 ine the distribution of actual vs. expected analysis errors. These results (as opposed to the
 415 distributions of RMSE) can indicate if forecasts are biased or otherwise not well distributed.

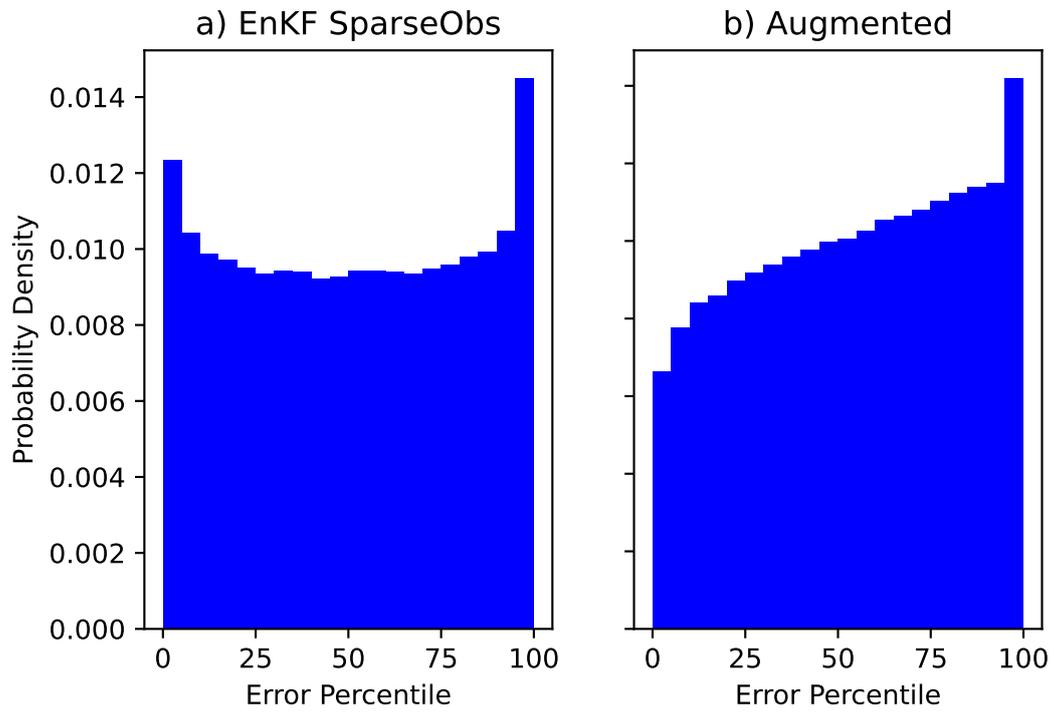


Figure 7. Rank histograms of the observations with respect to the ensemble of analyses for EnKF SparseObs (left) and augmented (right) methods. The percentile in which an observation falls is on the x-axis, with the normalized frequency on y-axis.

416 If errors are assumed to be Gaussian, then if scaled by the ensemble standard deviation the
 417 error distribution should follow a unit normal with a mean of zero. Conversely, if the er-
 418 rors are not well represented by a normal distribution, or the ensemble standard deviations
 419 don't reflect the true analysis error statistics, the scaled distribution will diverge from the
 420 reference unit normal. This comparison is shown in Figure 6.

421 Figure 6a suggests that the augmented method has a slight bias with its PDF shifted
 422 left compared with the reference unit normal. It also suggests that EnKF SparseObs is
 423 slightly underdispersive, with its peak lower and its tails higher than the reference unit
 424 normal PDF. These features are also apparent in Figure 6b, which displays the same data
 425 but as a CDF instead. For negative errors, EnKF SparseObs is higher than the reference
 426 distribution; for positive errors, it is lower. Consistent with the results presented in Figure
 427 5, despite its bias the augmented method better represents the true statistics of its error
 428 than EnKF SparseObs, with a standard deviation of 0.96 compared to 1.18, while a perfectly
 429 dispersive ensemble would have a standard deviation of 1.

430 Rank histograms are an alternative way of visualizing the dispersion of ensemble fore-
 431 casts or analyses (Hatfield et al., 2018; Candille & Talagrand, 2005; Weigel, 2011; Hamill,
 432 2001). For each forecast (or analysis), the percentile of the true value within the ensemble is
 433 calculated. When the distribution of the percentile values is plotted, a uniform distribution
 434 indicates a well-dispersed forecast. Errors of a given size occur as frequently as would be
 435 expected if the ensemble spread represents the true error statistics. A U shape is under-
 436 dispersive, with errors outside the range of the ensemble over-represented. A tilt indicates
 437 a biased ensemble forecast, with positive errors more or less likely to occur than negative
 438 errors.

439 Figure 7 includes rank histograms for both methods. It is more visually apparent
 440 here that the EnKF SparseObs produces underdispersive state estimates. Small and large
 441 percentile frequencies are clearly larger than frequencies at or around the 50th percentile.
 442 Conversely, while the dispersion of the augmented method state estimates is not as visually
 443 clear, the bias evident in Figure 6 is also visible here. The augmented method produces
 444 more accurate state estimates and more stability but with a slight bias compared with EnKF
 445 SparseObs.

446 3.3 Explainable AI: SHAP Values

447 We now return to the behavior the CNN in producing state estimates from forecasts and
 448 innovations. In an operational setting, allowing black-box operators to produce new initial
 449 conditions is not tenable. There must be some confidence that the system won't generate
 450 unrealistic results when presented with out-of-sample data, and some understanding of how
 451 it is producing its state estimates. Here we use SHAP values to estimate the impact of input
 452 variables on the outputs generated by the CNN (Figure 8).

453 Figure 8a shows the mean absolute SHAP values in decreasing order. The largest con-
 454 tributors to the state estimate of a variable are the forecast and the innovation of that
 455 variable. This is an excellent first sanity check on the CNN. In estimating a state vari-
 456 able, it weights the forecast and observation of that variable more heavily than forecasts or
 457 observations of nearby variables.

458 Figure 8b, identical to Figure 8a but with the first input variable not shown, suggests
 459 that the next two most heavily weighted inputs for generating a state estimate are the
 460 forecasts at 1 and 3 spatial lags, followed by observations and forecasts at 2 spatial lags.
 461 The long-term spatial correlation structure of the Lorenz-96 system is important to note
 462 at this point. Since the system is symmetric, without loss of generality we can consider
 463 the dynamics and correlation between locations only in terms of absolute spatial lag. The
 464 dynamics of a state variable are nonlinearly dependent on the state variables at spatial lags
 465 of 1 and 2 as described in Equation 1.

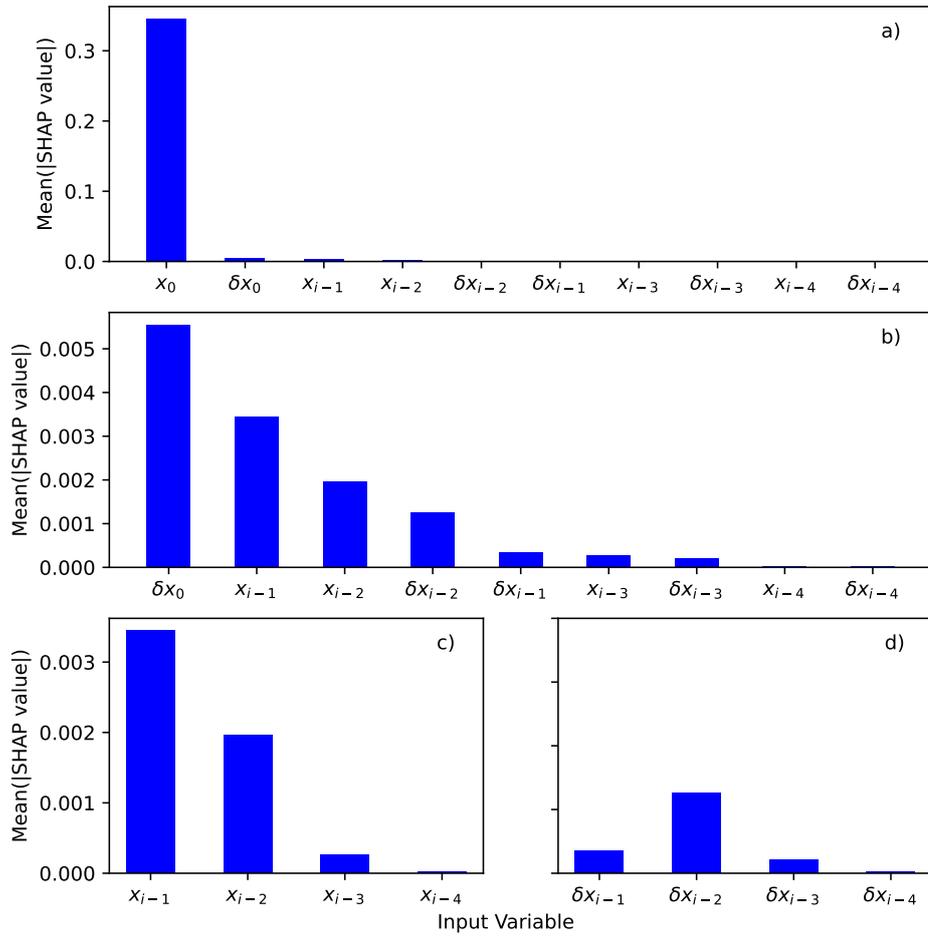


Figure 8. Estimated mean absolute SHAP values at a given location for the forecast(x) and innovation (δx) at spatial lags of 0 to 4. In panel a), input variables are sorted from largest to smallest mean absolute SHAP value. In panel b), panel a) is replicated without the first value (the analysis at a spatial lag of zero). Panel c) includes SHAP values for the forecast at spatial lags of 1-4, and panel d) for innovations at spatial lags of 1-4.

466 This dependence defines the temporal derivative. In non-differential terms, considering
 467 the variable values rather than rates of change, the correlation extends further than two grid
 468 points. At spatial lags of 1-4, the long-term absolute correlation coefficients are 0.05, 0.33,
 469 0.11, and 0.03. Variables at a distance of 2 and 3 grid points removed from one another
 470 are more highly correlated than immediately adjacent variables one grid point removed
 471 (Lorenz, 2005). It is also important to note that the convolutional layers will tend to
 472 create a binomial distribution here: larger lags have fewer paths of influence. This means
 473 that we should expect the SHAP results at increasing spatial lags to be a combination of a
 474 binomial distribution and the Lorenz-96 correlations. Figure 8c demonstrates monotonically
 475 decreasing SHAP values with increasing spatial lag consistent with the binomial influence
 476 of the CNN. Figure 8d shows a peak SHAP value at a spatial lag of 2, consistent with the
 477 correlation structure of Lorenz-96. In both cases, at a spatial lag of 4 the SHAP value is
 478 essentially zero. This is another important check on the results: the structure of the CNN
 479 means that the impact of data 4 spatial lags away cannot impact the output. The fact that
 480 the SHAP results reflect the known behavior of the CNN at a lag of 4 provides confidence
 481 that the other SHAP values have meaning.

482 4 Discussion

483 The results of using the augmented method outlined above are encouraging, and clearly
 484 show that it outperforms a traditional approach using only the EnKF. However, considering
 485 the training process of the CNN makes some limitations apparent. First: the network is
 486 trained using only the ensemble mean, rather than the entire ensemble, as input. As a result,
 487 it can only learn the covariance structure to the extent that the covariance is dependent on
 488 location in the state space. Other factors, most obviously the time since the last observation
 489 and analysis, will impact forecast uncertainty. The trained CNN cannot include such factors.

490 Even within the confines of the experiment we have set up, the limitations of the
 491 training data have an impact on performance. When employed online in the augmented
 492 method the CNN is provided as input a forecast initialized by assimilating only 25% of
 493 the variables. In comparison, all variables are observed in the EnKF configuration used to
 494 generate training data. In the online setting, therefore, the initial condition error will be
 495 larger and the forecast precision lower than in the training set. In the experimental setup,
 496 the augmented method has an RMS of 0.74, nearly three times worse than the RMSE when
 497 it is simply applied to forecasts from the validation time period generated offline. This
 498 partly reflects the fact that the augmented method is simply assimilating less data. On a
 499 time-averaged basis, it is observing 62.5% of the observations assimilated in the training
 500 set, but that does not fully explain the 3-fold increase in RMSE. The remaining decrease
 501 in accuracy is attributable to the smaller forecast errors in the training data compared to
 502 forecast errors in the online setting.

503 While the reduced performance of the CNN applied to an online setting as opposed
 504 to input data generated offline is unavoidable to some extent, future opportunities for im-
 505 provement may be found by allowing the CNN to better approximate forecast accuracy.
 506 Providing additional input to the network, such as ensemble standard deviation at the last
 507 time step combined with time since observations were last assimilated, is one option. Our
 508 results here provide no indication either way whether a neural network would be able to
 509 learn effectively from other input data, or how complex the network would have to be, but
 510 it is a potential avenue of further exploration.

511 The results from the SHAP analysis provide additional insights into the possible ex-
 512 tensions of the approach. Localization is widely used to improve the performance of many
 513 assimilation systems. The SHAP values demonstrate that the trained CNN has applied
 514 localization to the forecast. The CNN also has learned the long-term correlation structure
 515 (teleconnections) of the system, applying a localization structure to the innovations con-
 516 sistent with that of the Lorenz-96 system. These are both reasons to think it is plausible

517 that in future extensions convolutional layers may be able to generate spatial estimates
518 that blend forecasts and observations in a way that is both reliable and skillfully reflects
519 underlying system behavior and dynamics.

520 **5 Conclusion**

521 This study demonstrated a proof-of-concept augmented assimilation methodology in
522 which machine learning was used to directly assimilate high-resolution observations for po-
523 tential improvement of the performance of an assimilation scheme. Significant quantities
524 of observational data, particularly from remote-sensing platforms, go unused in operational
525 forecast models due to the computational cost and time required for incorporating them
526 into the model. The potential viability of training a machine learning model offline to as-
527 similate this data could have a significant impact – improved state initialization has real
528 and notable impacts on forecast quality, and the ability to use the vast amounts of newly
529 available observational data products to that end is of clear benefit.

530 As a demonstration of the potential feasibility of such an approach, we trained a 2-layer
531 convolutional neural network to replicate the results generated by the Ensemble Kalman
532 Filter on synthetic observations. Using the EnKF on low-resolution observations and the
533 trained CNN on the high-resolution observations outperformed an EnKF assimilating only
534 low-resolution data. More specifically, in an experimental setting using the Lorenz-96 model,
535 the analyses generated by the augmented method have a mean RMSE 14.5% lower than using
536 the EnKF on only low-resolution observations. Forecasts using analyses generated by the
537 augmented method as initial conditions produce lower RMSE up to a forecast lead time
538 of 10 days. Ensemble forecasts using initial conditions from the augmented method were
539 also found to be less underdispersive, with ensemble standard deviations that more closely
540 reflect true forecast error.

541 Additionally, using an explainable AI method, we demonstrate that the trained CNN ef-
542 fectively both applies localization as well as learns the correlation structure (teleconnections)
543 of the underlying system via training. Distant observations do not impact its estimates. The
544 natural tendency of convolutional layers to exploit local spatial correlations in this way is
545 encouraging for potential extensions to more realistic applications. It also generates confi-
546 dence that such a method would both be reliable and generate physically realistic results
547 when presented with new data.

548 Further studies are needed to demonstrate the ability of this approach to work in more
549 complex systems and at scale. Testing using a quasigeostrophic model and more realistic
550 observational data would be a logical next step. The demonstrated feasibility of the general
551 approach in this proof-of-concept study will hopefully encourage additional efforts to address
552 the large quantity of data that is currently unusable in an operational forecast setting using
553 machine learning approaches.

554 **6 Open Research**

555 Code for generating the data used in this study as well as code for generating the
556 plots in this paper (and the processed data used in the plots) can be accessed at [https://](https://github.com/climprocpred/machine_learning_DA_part_1)
557 github.com/climprocpred/machine_learning_DA_part_1.

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