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Supporting Information for

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**Shear-Enhanced Electrical Conductivity of Synthetic Quartz-Graphite Gouges:
Implications for Electromagnetic Observations in Carbonaceous Shear Zones**

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16 **Introduction**

17 The supporting information includes analytical data on the starting materials and
18 experimental data details, as well as information on data processing, fitting, and data
19 comparison.

20 **Text S1. Experimental data processing**

21 Due to slight assembly misalignment, the rotatory corundum cylinder often fluctuated at
22 each frictional revolution. Thus, all frictional curves were smoothed using the moving-average
23 method, which takes an average of data points with the window width corresponding to one
24 revolution (Figure S2a, for more smoothing details see Yao et al., 2013). In addition, to
25 investigate the frictional properties in the early stage, all mechanical data before the steady
26 state were not smoothed. For LHV1372, three hold tests occurred in the slip displacements of
27 0.53, 1.97, and 2.97 m (black arrows in Figure S2a), with no noticeable changes in the
28 mechanical and electrical behaviors.

29 Figure S2b shows the smoothed frictional coefficient data (μ , linear scale) and the raw
30 electrical conductivity data (σ , log scale) plotted against slip displacement (D) for a 5 wt.% Gr-
31 bearing specimen at 2.0 MPa (LHV1372). As the slip displacement increased to 0.57 m, μ
32 rapidly increased to a peak value at first and then slightly decreased. Finally, a steady state was
33 achieved, *i.e.*, μ remained stable within ± 0.1 m until the eventual 3.21 m displacement (violet-
34 shaded area). In contrast, σ grew logarithmically after the slip displacement of 0.23 m,
35 increasing by eight orders of magnitude. Then, σ maintained until the end a conduction-
36 steady-state within one order of magnitude variation from 0.79 m (red-shaded area).

37 To explain the mechanical–electrical properties of the specimens, we identified several
38 critical parameters on all experimental curves. Taking the LHV1372 experiment as an example,
39 (1) steady-state frictional coefficient (μ_{ss}) and steady-state electrical conductivity (σ_{ss}) were
40 respectively obtained from the arithmetically average value of μ in steady-state and the
41 logarithmically average value of σ in steady-state; (2) D when μ achieved μ_{ss} ($D_{\mu_{ss}}$) and σ
42 achieved σ_{ss} ($D_{\sigma_{ss}}$). Occasionally, the determination of $D_{\mu_{ss}}$, and thus μ_{ss} , suffered from the large
43 fluctuations in the friction curves, in which case, we gained insight from the evolution of
44 gouge layer thickness, which always showed exponential compaction in the displacement
45 range of $D_{\mu_{ss}}$ (pentagrams in Figure S3) and was expected to roughly share the characteristic
46 displacement as that for friction (Marone, 1998); (3) interestingly, the σ curve showed large
47 jumps from the initial level (σ_0) at short displacements, even before reaching the peak friction.
48 Accordingly, we marked this displacement as $D_{\sigma_{chr}}$, defined by more than two orders of
49 magnitude σ -increase for $\sigma_0 < 0.01$ S/m and by a factor of 1.5 for $\sigma_0 > 0.01$ S/m.

50 Each set of μ (linear scale) and σ (log scale) curves of all experiments, as a function of slip
51 displacement, are listed in Figures S4–S6. Due to technique bias for recorded data, all
52 experimental data were managed with a translational correction; all initial friction coefficients
53 were corrected to 0 and all frictional slips were corrected to start in 10^{-4} m. As the offsets were
54 very small (< 0.001 for μ and 10^{-8} – 10^{-6} m for D), we believe this correction did not affect our
55 experimental results. The corresponding critical parameters for each experiment (*i.e.*, μ_{ss} , $D_{\mu_{ss}}$,
56 σ_{ss} , $D_{\sigma_{chr}}$, and $D_{\sigma_{ss}}$) were located on the experimental curves of the aforementioned figures.
57 Moreover, several specimens performed erratic frictional behaviors, *i.e.*, LHV2051, LHV2052,
58 LHV2057, and LHV2429, due to (1) Qz particles leakage, (2) a part of the Teflon[®] components
59 was cut in the slip surface, and (3) frictional resistance existed between PMMA (transparent
60 vessel) and clamping. Therefore, these frictional curves (blue dashed lines in Figures S4–S6)
61 were not shown in Figures 2–3 and were not applied to fit the equation in the discussion.
62

63 **Text S2. Fitting details and experimental data comparison**

64 Figures S7a and S7b show the μ_{ss} and the σ_{ss} plotted against X_{Gr} at 2 and 5 MPa for all
65 specimens, respectively. A similar trend can be seen in the relationship between μ_{ss}/σ_{ss} and X_{Gr}

66 in the range of 2–5 MPa normal stress. Therefore, we concentrated all experimental data of 2
67 and 5 MPa for data fitting to explore the X_{Gr} dependency of μ_{ss} and σ_{ss} , respectively. Although
68 μ_{ss} at 5 MPa was slightly higher than that at 2 MPa, we believe it does not affect our
69 conclusions. In addition, we allowed the parameters μ_{ss} , σ_{ss} , and X_{Gr} for each specimen to vary
70 within an optimization range during the fitting process. These ranges include the variabilities
71 in the standard deviation of all experimental data and the uncertainties in adapting the X_{Gr}
72 (within $\pm 0.4\%$). Because a small quantity of Qz particles was inevitably extruded into the gaps
73 between the outer electrode loop and rotary cylinder during the frictional slip, the mechanical
74 data became oscillatory during the frictional slip, especially for the specimens with low to
75 intermediate Gr contents (< 10 wt.%) (Figures 2–3). As a result, the μ_{ss} values of the low- X_{Gr}
76 mixtures were higher and more scattered than those of Oohashi et al. (2013) (0.53–0.85,
77 orange regime in Figure S7a). Therefore, μ_{Qz} (0.73) was taken to be the mean value of μ_{ss} for the
78 low- X_{Gr} specimens (< 13.6 vol.%).

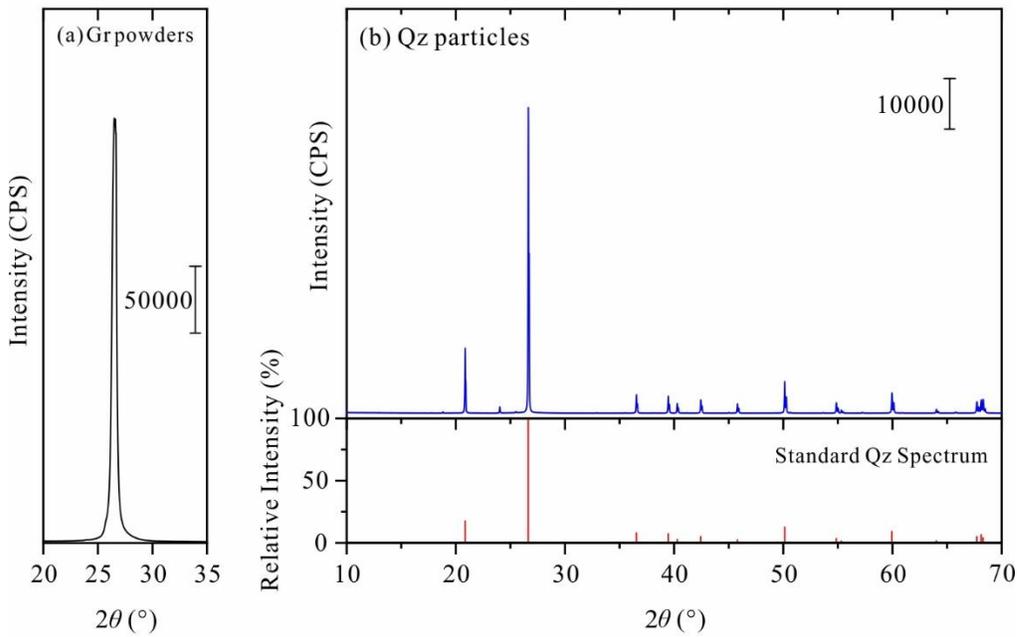
79 All fitted parameters of Equation 2 and Equation 3 in this study are shown in Table 3 and
80 Table 4, respectively. The friction of pure Gr flakes was consistent with that in Oohashi et al.
81 (2013)'s results (0.08–0.16). Our X_{cw} -value (22.3 vol.%) and S -value (8.97) were higher than
82 Oohashi et al. (2013)'s values ($X_{cw} = 11.8$ – 12.8 vol.%, $S = 1.56$ – 1.82 , for a range of slip rate 0.2–
83 56 mm/s), indicating higher critical value but more rapid weakening. Meanwhile, our critical Gr
84 volume fraction for a dramatic decrease of the frictional coefficient (~ 13.6 vol.%) (grey dashed
85 lines in Figure S7a) was higher than that observed by Oohashi et al. (2013) (~ 5 vol.%). It might
86 be related to the difference in the grain size of Qz particles used in the experiment, i.e., the Qz
87 grain size of their experimental specimens (< 200 μm) was approximately an order of
88 magnitude greater than ours (12.2 μm). Gouges with larger Qz particles tend to have a smaller
89 specific surface area, which requires a smaller amount of Gr to attain an *ad-hoc* microstructure
90 that leads to lubrication of the gouge. This is also supported by a recent study (Chen, 2022). It
91 implies that the grain size of strong Qz particles is also a pivotal character in determining the
92 frictional stability of Gr-bearing gouges.

93 The σ values of pure Qz particles (1.1×10^{-10} S/m– 2.7×10^{-10} S/m) and of pure Gr flakes ($\sim 10^3$
94 S/m) were stable and were close to previous static compaction experimental data under 0.1–
95 300 MPa (Chen et al., 2017). The fitting of the σ_{ss} - X_{Gr} curve yielded an r -value of 3.36, which is
96 slightly higher than that obtained from static compaction of Qz-Gr mixtures, 2.53 (Chen et al.,
97 2017), and lower than that of Gr-bearing olivine aggregates under high pressure and
98 temperature conditions, ~ 10 (Wang et al., 2013). Interestingly, the α -value was 1.29, much
99 lower than that of the above-mentioned studies (3.39 and 10–20). We propose the following
100 explanation for such difference: From the percolation theory, the conductivity of a mixture
101 increases substantially once thin disk-shaped Gr grains are interconnected at edges (Gueguen
102 & Dienes, 1989). The α -values can be converted to the ratio of the average diameter (c) to the
103 thickness (w) for the Gr disks ($c/w = \alpha/(\pi/4)$) (Wang et al., 2013). In this study, our c/w value
104 (1.67) is inconsistent with the geometry of the traditional conductive structure of
105 interconnected grain-boundary carbon films ($c/w > 10$) (Duba & Shankland, 1982; Frost et al.,
106 1989; Mareschal et al., 1992). Because the direction of the conductive pathway in the SLZ in
107 this experiment was parallel to the direction of the Gr disks, the c/w defined by the α from
108 Equation 3 was not the average diameter-thickness ratio of the Gr disks, but rather the major
109 axis-minor axis ratio of the Gr disks. Therefore, the c/w ratio reflects the geometry of the actual
110 conductive channel.

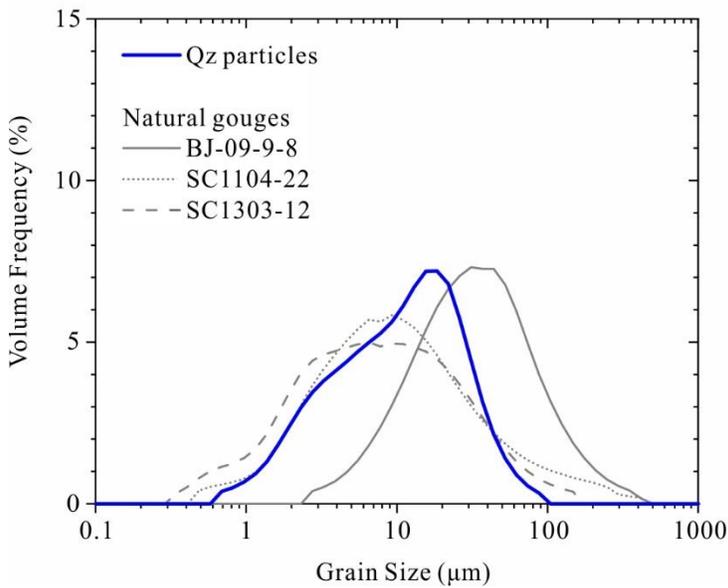
111 The percolation threshold value (X_c) was determined based on our experimental results:
112 The σ_{ss} of the specimen with 4 wt.% Gr was very high (10^3 S/m), while the σ_{ss} of the specimen
113 with 3 wt.% Gr maintained a low value ($\sim 10^{-11}$ S/m) throughout most of the slip displacement

114 range and only slightly increased at the end ($> 10^8$ S/m) (Figure 2d), suggesting that some of
115 the Gr flakes can locally develop connected fabric. Therefore, we roughly determined the Gr
116 weight fraction of 3 wt.% (corresponding to a volume fraction of 3.4 vol.%) as the percolation
117 threshold value (X_c) of the relationship between σ_{ss} and X_{Gr} . In this study, the X_c is a fixed value.
118 However, compared with the X_c under static compaction (Figure 3b), normal stress and shear
119 strain significantly influence it. We interpreted the abrupt enhancement of the electrical
120 conductivity as due to the fabric of "GCCs", i.e., the Gr-interconnectivity has something to do
121 with the geometry (i.e., aspect ratio) of the Gr flakes over the surface area of individual Qz
122 particles in the shear zone. Normal stress or static compaction can reduce the porosity of Qz
123 particles and increase the interconnectivity of Gr flakes. In contrast, shear deformation can
124 enhance the aspect ratio of Gr flakes, which leads to higher interconnectivity of grain-
125 boundary Gr flakes and lower percolation threshold of the mixture compared with static
126 compaction (decrease from 6.0 to 3.4 vol.% in Figure 8).
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(a)-(b) XRD Analysis

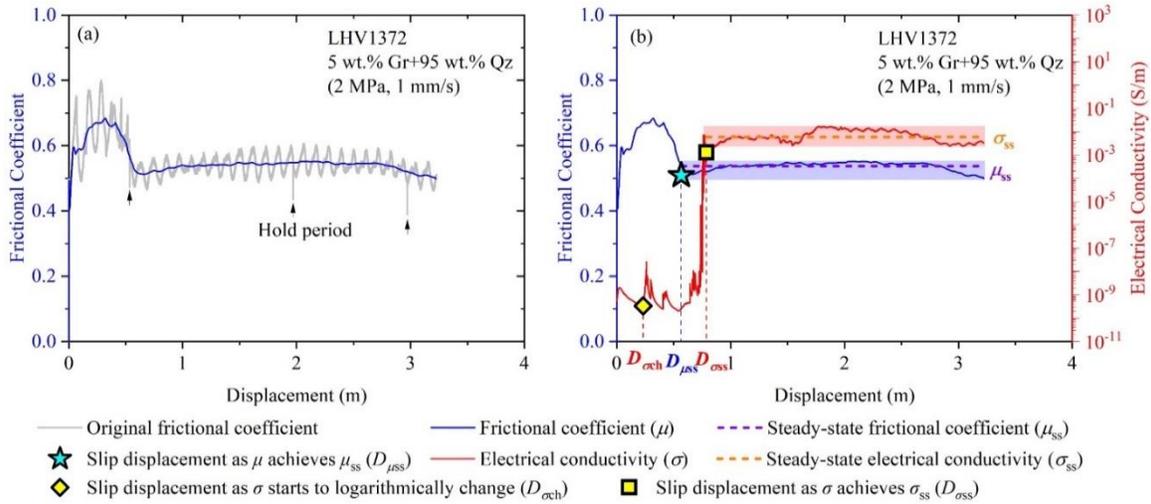


(c) Grain Size Analysis



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129 **Figure S1.** Analytical data of the starting materials used for the experiments. (a) X-ray
130 diffraction spectrum of Gr and (b) Qz particles compared with the standard Qz spectrum. (c)
131 Particle size distribution of the Qz particles (blue line). Grey lines represent natural gouges
132 collected from the coseismic slip zone of the Yingxiu–Beichuan fault zone in Sichuan province,
133 China P.R. (Chen et al., 2017).



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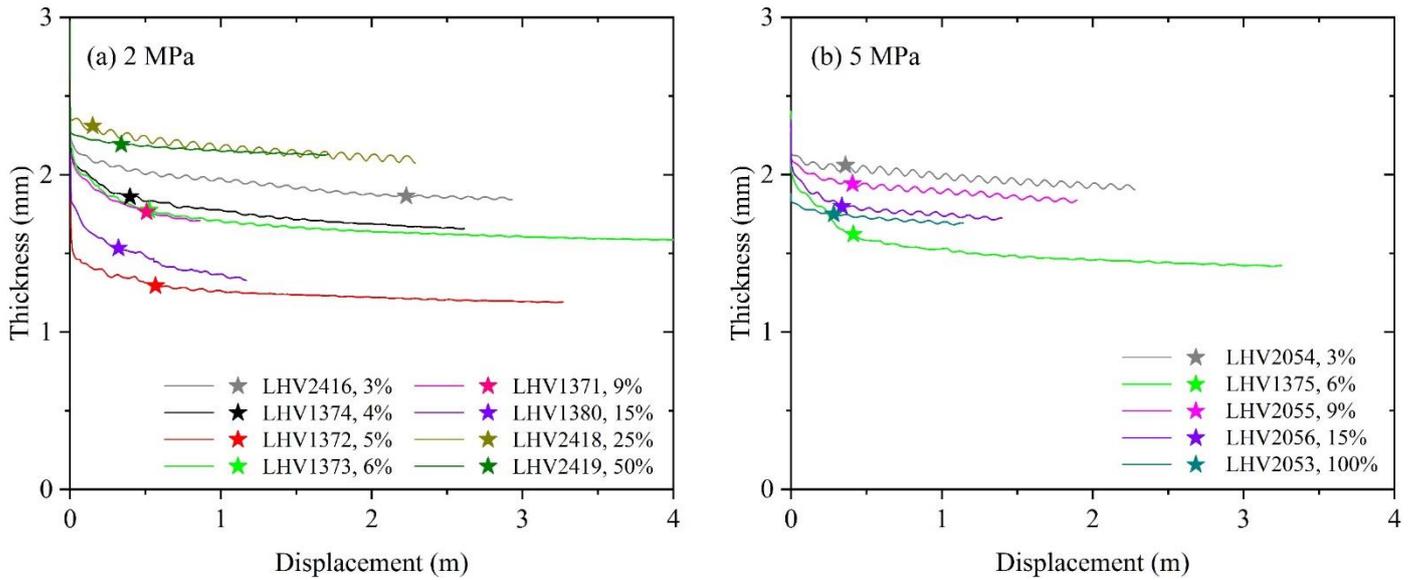
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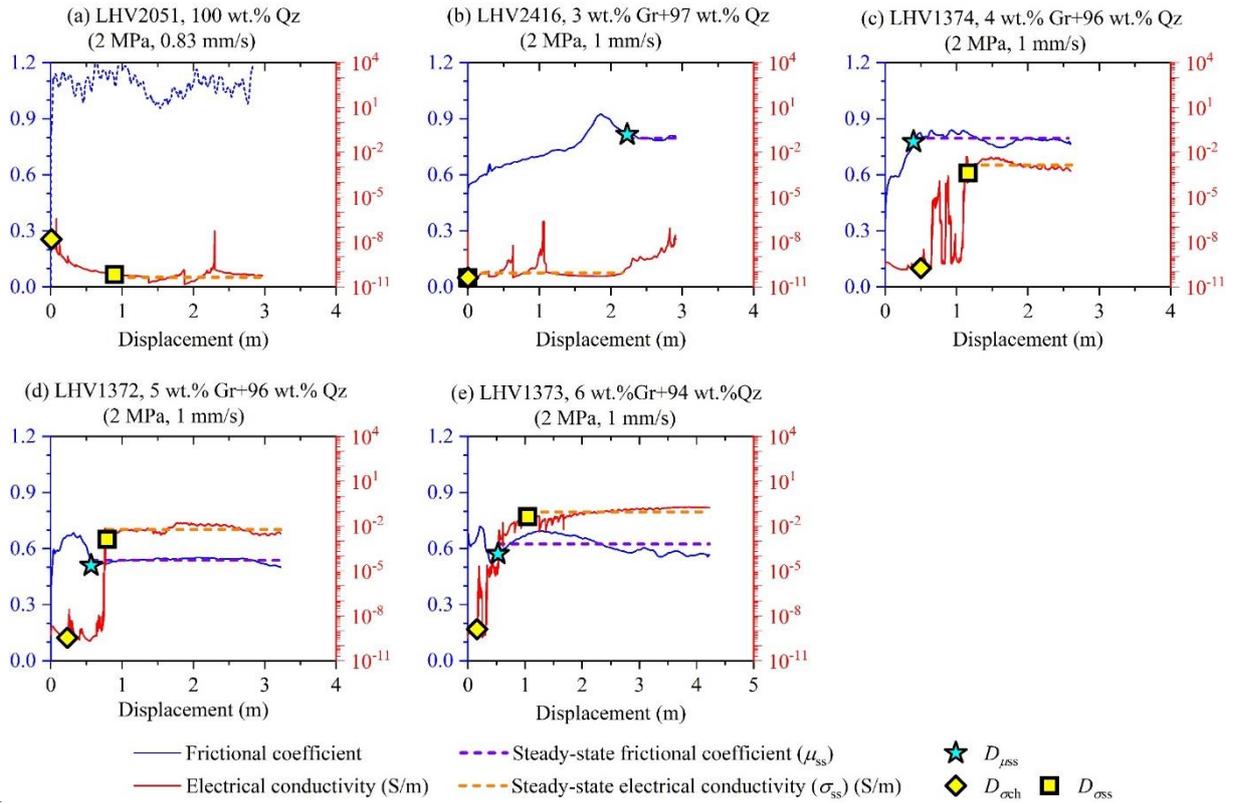
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Figure S2. Experimental data curves of 5 wt.% Gr-bearing specimen (LHV1372) at 2 MPa and 1 mm/s as a function of slip displacement. This figure illustrates mechanical data smoothing and the obtained critical parameters. (a) Original (light grey line) vs smoothed (blue line) friction data. The experimental data in the hold period ($v_e < 0.6$ mm/s) are pointed by black arrows, and they were removed in smoothed processing. (b) Evolution of smoothed frictional coefficient (μ , blue line) on a linear scale and electrical conductivity (σ , red line) on a log scale. The dashed violet line, dashed orange line, blue pentagram symbol, yellow diamond symbol, and yellow square symbol located on the curve indicate μ_{ss} , σ_{ss} , $D_{\mu_{ss}}$, D_{och} , and $D_{\sigma_{ss}}$, respectively.



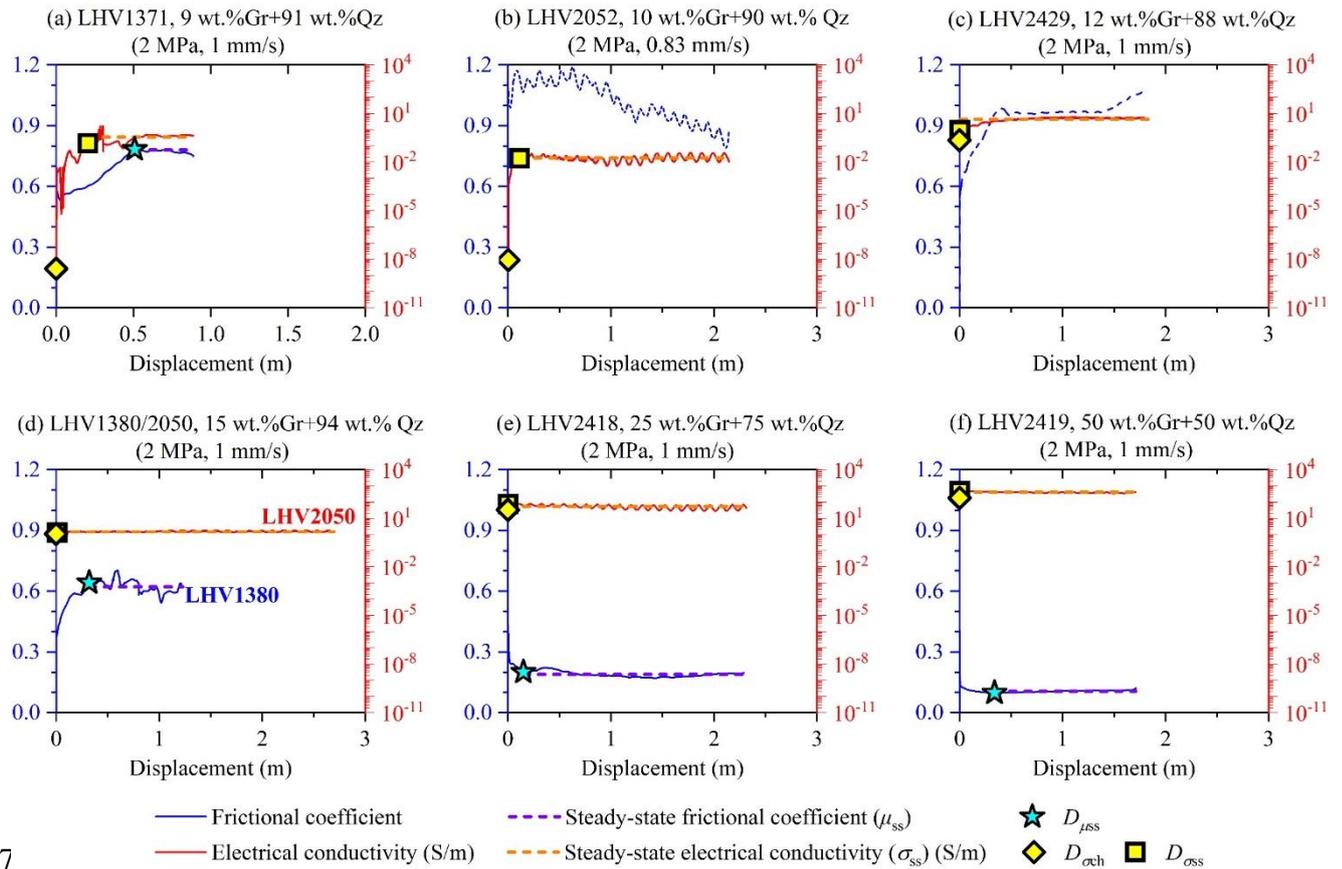
144 **Figure S3.** Evolution of thickness as a function of slip displacement during a progressive
 145 fault slip. This figure shows results for all experiments performed at a normal stress of (a) 2
 146 MPa and (b) 5 MPa. The pentagram symbols identify the critical points of thickness
 147 evolution, *i.e.*, transformed from the exponential decreases to the linear reductions, which
 148 are expected to have similar characteristic displacement as that for friction. The numerical
 149 percentages of the legends indicate the Gr weight percentages of experimental
 150 specimens.



151

152 **Figure S4.** Frictional coefficient-electrical conductivity vs slip displacement for dry Gr-Qz
 153 mixtures at 2 MPa and 0.83–1.00 mm/s. The Gr fractions of mixtures include (a) 0 wt.%, (b) 3
 154 wt.%, (c) 4 wt.%, (d) 5 wt.%, and (e) 6 wt.%. The erratic frictional behavior of LHV2051 in (a)
 155 is shown in a blue dashed line. Legends are identical to those in Figure S2.

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158

159 **Figure S5.** Frictional coefficient-electrical conductivity plotted against slip displacement

160 for dry Gr–Qz mixtures at 2 MPa and 0.83–1.00 mm/s. The Gr fractions of mixtures include

161 (a) 9 wt.%, (b) 10 wt.%, (c) 12 wt.%, (d) 15 wt.%, (e) 25 wt.% and (f) 50 wt.%. The erratic

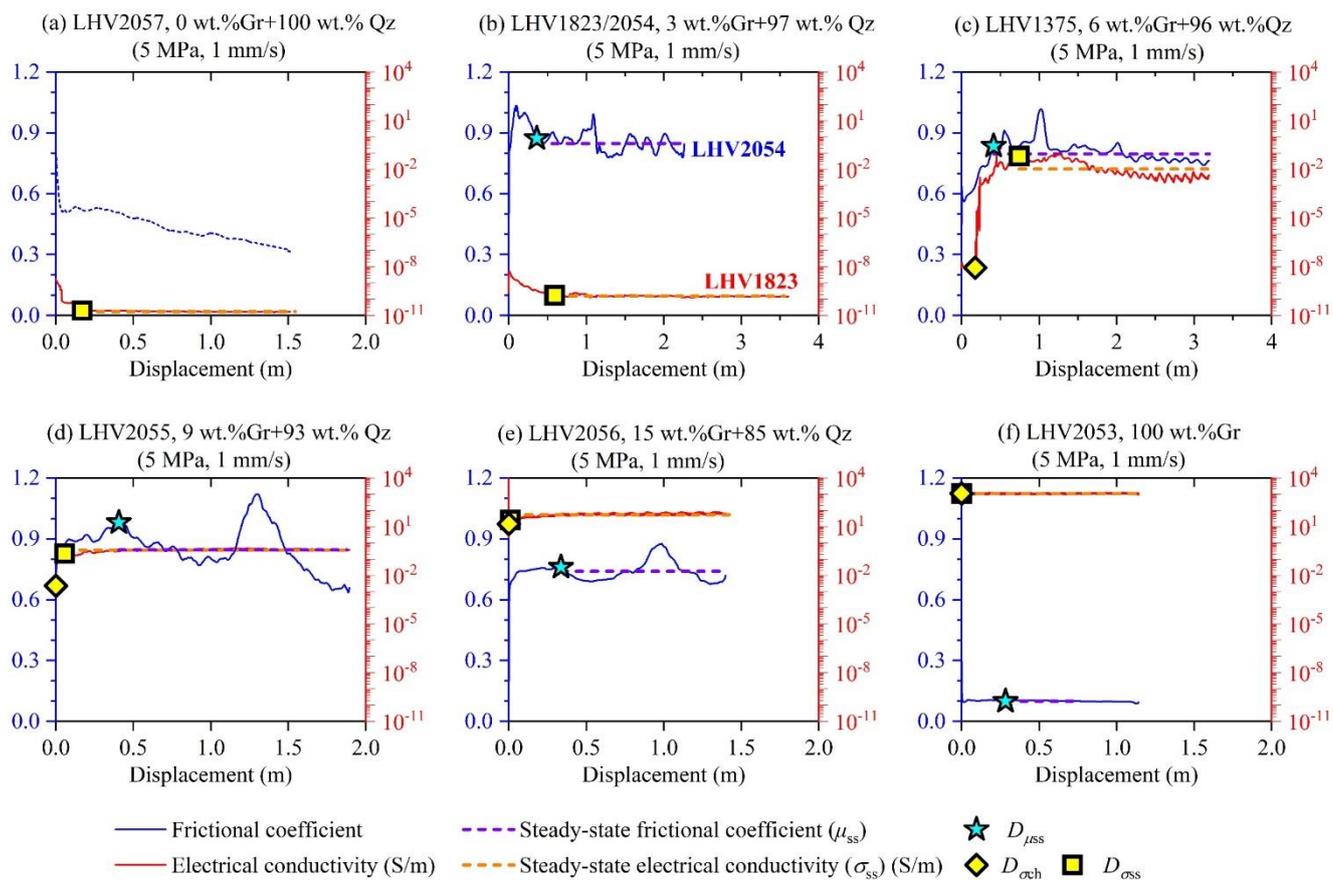
162 frictional behavior of LHV2052 and LHV2429 in panels b and c are shown in a blue dashed

163 line. The friction-conductivity data of the 15 wt.% Gr-bearing specimens were obtained

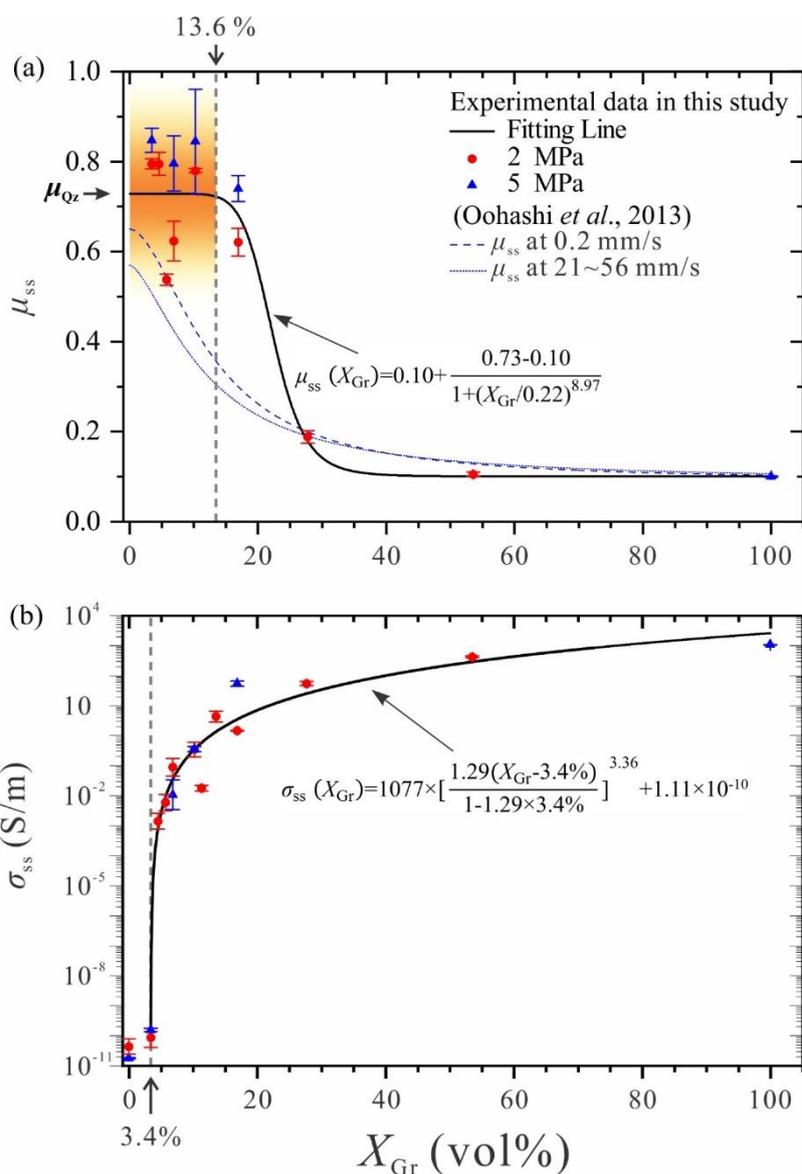
164 from two experiments, *i.e.*, LHV1380 and LHV 2050. Legends are identical to those in Figure

165 S2.

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167 **Figure S6.** Frictional coefficient–electrical conductivity plotted against slip displacement
168 for dry Gr–Qz mixtures at 5 MPa and 1 mm/s. The Gr fractions of mixtures include (a) 0
169 wt.%, (b) 3 wt.%, (c) 6 wt.%, (d) 9 wt.%, (e) 15 wt.% and (f) 100 wt.%. The erratic frictional
170 behavior of LHV2057 in (a) is shown in a blue dashed line. The friction–conductivity data of
171 the 3 wt.% Gr-bearing specimen was obtained from two experiments, *i.e.*, LHV1823 and
172 LHV 2054. Legends are identical to those in Figure S2.



173

174 **Figure S7.** Effect of X_{Gr} on (a) μ_{ss} and (b) σ_{ss} of the Gr–Qz mixtures at 2 (red circular symbols)
 175 and 5 MPa (blue triangular symbols). Error bars indicate the variabilities in the standard
 176 deviation of all experimental data. Black solid curves in panels a and b display the fit to
 177 each data set with Equation 1 and Equation 2, respectively. The μ_{ss} – X_{Gr} relationship of Qz–Gr
 178 mixtures at 0.2 and 21–56 mm/s under similar environmental conditions proposed by
 179 Oohashi et al. (2013) were drawn by blue dashed and dotted lines, respectively. An orange
 180 area identifies the potential distributed range of μ_{Qz} .

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