Moulin density impacts the effect of subglacial hydrology on ice dynamics

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Key Points:

- The density of moulins changes the impact of subglacial water drainage on ice dynamics.
- Localised water inputs to the subglacial hydrological system helps with the stability of the system.

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Abstract

The current increase in temperature over Greenland and other glaciated regions allows for more surface melt, which poses the question of the impact of this extra amount of meltwater on ice dynamics. As subglacial hydrology models evolve they are now easier to apply to realistic scenarios to quantify the effect of an increase in melt on the dynamics of glaciers. However, a number of processes linking the surface melt to the water pressure at the base of glaciers are still overlooked in models due to a lack of knowledge or an excess of complexity. Here, we apply a subglacial hydrology model coupled to an ice dynamics model to a synthetic geometry to investigate the impact of moulins distribution on the dynamics of the glacier. Our results show that a sparser distribution of moulins leads to the faster development of the efficient drainage system and greatly slows down the glacier.

Plain Language Summary

As climate warms, a larger amount of meltwater is produced at the surface of ice sheets and glaciers. Most of this water makes its way through cracks and other passageways of the ice to end up at the interface between the glacier itself and the underlying rock. Once at the base of the glacier this water acts as a lubricant and as its pressure increase it has the potential to speed-up the overlying ice. The relationship between ice velocity and water amount is however not straightforward as the drainage system at the base of the glacier can reconfigure and potentially has a large impact on water pressure. Due to this complex interactions, numerical models of subglacial drainage system are needed to get a better idea of the effect of an increase in meltwater production on ice dynamics. Using such a model in a conceptual set-up, we show that reducing the number of injection points into the subglacial drainage system in models can lead to a substantial deceleration of the glacier above.

1 Introduction

Since the first measurement of the impact of meltwater on the dynamics of glaciers in Greenland by Zwally et al. (2002) the question of the long term impact of an increase of Greenland surface melt on its dynamics has been debated within the community. Further observations (e.g., Sole et al., 2013; Meierbachtol et al., 2013; Doyle et al., 2014; Tedstone et al., 2015) have revealed a complex interaction between the amount of runoff at the ice surface and the observed accelerations or lack thereof. A large part of the complexity of the system resides in the way the subglacial water drainage system operates, with the capacity to enhance its efficiency when the water volume injected into the system increases (e.g., Chandler et al., 2013; Andrews et al., 2014). These complex interactions lead to a decoupling between the volume of available runoff water and the subglacial water pressure that drives glacier sliding (Bartholomew et al., 2010; Schoof, 2010; Fitzpatrick et al., 2013; Sole et al., 2013; van de Wal et al., 2015). The complexity of this system warrants the use of fully coupled subglacial hydrology ice dynamics models to evaluate if the increase of meltwater production will have a notable effect on ice dynamics as the temperatures continue to rise (M. Hoffman & Price, 2014; Stevens et al., 2018; Davison et al., 2019).

Important efforts have been made to improve the representation of the subglacial hydrological drainage system in models This lead to the development of a new generation of multi component models able to compute the water pressure at the base of glaciers (e.g. Pimentel et al., 2010; Werder et al., 2013; de Fleurian et al., 2014; M. J. Hoffman et al., 2018). These models have recently been coupled to ice dynamics models in order to investigate the meltwater lubrication feedback on various timescales (Gagliardini & Werder, 2018; de Fleurian et al., 2022), Given the complexity of the system these studies have focused on synthetic designs to isolate the effect of a specific component of the

system. Here, we continue on this trend and investigate the impact of the water supply distribution on the subglacial water pressure and its impact on ice dynamics. This question have been under the scope of different studies so far (A. Banwell et al., 2016; Scholzen et al., 2021) but those studies focused on the effect on subglacial water pressure without taking the final step of assessing the effect on ice dynamics.

The distribution intensity and timing of meltwater input to the subglacial drainage system is controlled by the intensity of the surface melt and the efficiency of the supraglacial and intraglacial drainage systems. Models are emerging to represent these components (e.g. A. F. Banwell et al., 2012; Clason et al., 2015; Yang et al., 2022) but the complexity of each subsystem means that there is still no simulations that can introduce in a realistic manner all the component of the system. This is a drawback for the modelling of subglacial water pressure as the intensity of water input at the base of glaciers has a large impact on the development of an efficient subglacial drainage system (Colgan et al., 2011; Bartholomew et al., 2012; Tedesco et al., 2013; de Fleurian et al., 2022) and hence on the subglacial water pressure. A recent study by Yang et al. (2020) showed that changing the supraglacial drainage model that was feeding into the subglacial drainage system did not yield large changes in pressure on timescales longer than a day. Mejia et al. (2022) drew similar conclusion after monitoring supraglacial drainage catchment with different characteristics showing again that a change in the supraglacial drainage can lead to lags in subglacial water peak pressure on the order of a few hours. Here we focus on longer timescales and investigate the impact of a changes in the distribution of meltwater input into the subglacial drainage system on a yearly timescale.

2 Methods

2.1 Model Description

In order to investigate the influence of moulins density on the effective pressure and velocity evolution of glaciers we carry out coupled ice dynamic, subglacial hydrology simulations within the Ice-sheet and Sea-level System Model (ISSM, Larour et al., 2012). Within ISSM we use the Double Continuum (DoCo) approximation for the hydrology model as described in de Fleurian et al. (2014, 2016). The ice flow is then resolved with a Shallow Shelf Approximation (SSA, Morland & Zainuddin, 1987; MacAyeal, 1989) and the coupling is achieved through a friction law in which the effective pressure (N), defined as the difference between the water pressure at the bed and the ice overlying pressure, is a key parameter. We elected to use a non-linear friction law described by Schoof (2005) and Gagliardini et al. (2007) which ties sliding velocities ($\vec{u_b}$) and basal shear stress ($\vec{\tau_b}$):

$$\vec{\tau_b} + \frac{CN|\vec{u_b}|^{(1/n-1)}}{(|\vec{u_b}| + C^n N^n A_s)^{(1/n)}}\vec{u_b} = 0, \tag{1}$$

where C is Iken's bound (Iken, 1981) which sets the maximum value taken by $\vec{\tau_b}/N$ while A_s is the sliding parameter without cavitation and n is the rheological exponent in Glen's flow law (Glen, 1958) taken here as ($n = 3$).

As for most of the model set-up, the subglacial hydrology model version and parameters used in the present study are exactly the same as the one described in de Fleurian et al. (2022). As in de Fleurian et al. (2022) the model is initialised with a parabolic function which resembles a west Greenland land terminating glacier surface elevation. The glacier is initially 150 km long and 20 km wide with a flat bedrock at an elevation z_b =465 m The surface elevation (z) then follows:

$$z_s(x, y) = 4.5 \times \sqrt{x + 4000} + 186 \tag{2}$$

The geometry is then relaxed within the coupled model framework to achieve a pseudo steady-state geometry.

Table 1. Catchment area characteristics for every simulation, the area taken into account for the average catchment area is the area that experiences melt at anytime during the year. The number of moulins corresponds to the number of catchment areas as there is a single moulin per catchment area.

Simulation name	number of moulins	Average catchment area	smallest catchment area
Uniform	844	0.7 km^2	0.1 km^2
Fine	467	1.4 km^2	0.3 km^2
Mid	99	6.5 km^2	1.2 km^2
Coarse	50	13 km^2	2.1 km^2

2.2 Meltwater Forcing

The surface mass balance is applied through an idealised method following Hewitt (2013), where the surface temperature is described at a reference elevation through the length of the melt season (Δ_m), a positive degree day (r_m) at the reference elevations, the day of the year when the melt season starts (t_{spr}) and the duration that the temperature takes to reach its maximum value (Δ_t in days). The reference temperature (T_{ref}) then reads :

$$T_{ref}(t) = \frac{r_m}{\Delta_m} \times \left(\frac{1}{2} \tanh\left(\frac{t - t_{spr}}{\Delta_t} \right) - \frac{1}{2} \tanh\left(\frac{t - (t_{spr} + \Delta_m}{\Delta_t} \right) \right) \tag{3}$$

From that temperature, the runoff (r) at the surface of our synthetic geometry is computed through a lapse rate (r_s) and a given degree day factor (ddf):

$$r(s,t) = \max\{0, T_{ref}(t) \times (z_s - 465) \times r_s\} \times ddf \tag{4}$$

This setup for the mass balance computation uses the parameters of the reference simulation in de Fleurian et al. (2022) with Δ_t=141 days, a maximum temperature at the reference elevation (r_m/Δ_m) of 5.85 °C and Δ_t=10 days. The major difference here is that the injection in the subglacial hydrology model is slightly different. Our reference simulation (*Uniform* in Table 1) uses the set-up that was previously described where every model node is an injection point in the subglacial hydrology model. However we also use some setup where a smaller number of injection point is used. For simplicity we will further call those injection points moulins even if we do not try to actually model the supraglacial and intraglacial components of the drainage system, implying a direct transfer of surface melt to the base of the glacier at each moulin. The procedure to define those moulins is as follow. First, a given number of nodes are drawn randomly within the nodes of the model that fall within the region that experiences runoff at any time during the year. From this initial draw, we define a Voronoi diagram in which each polygon associated to a given model node represents one drainage basin at the surface of the ice. The moulin for each of those basins is then placed on the lowest elevation node contained in the catchment. From there on, the runoff is integrated over the whole catchment area and the given water discharge is then injected at the location of the moulin through a vertical shaft into the subglacial hydrology model. This procedure insures that for all the simulations the same volume of water is injected in the subglacial drainage system and only the location of the injection changes. Table 1 gives an overview of the different simulations with a few statistics on the catchment areas and number of moulins.

2.3 Ensemble Design

The experiments of de Fleurian et al. (2022) showed that the model presented a physical instability that needed to perform an ensemble of simulations in order to inves-

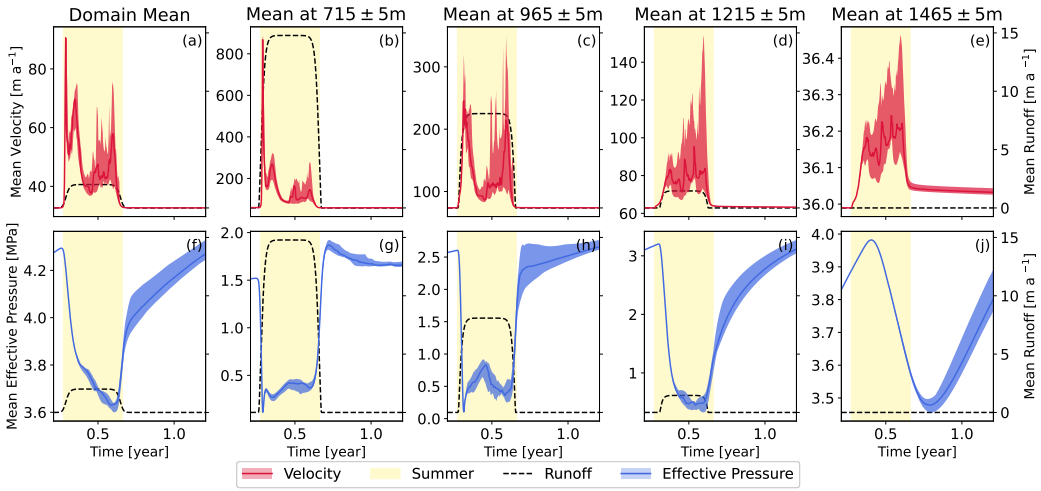

Figure 1. Evolution of velocities (a to e) and effective pressures (f to j) presented as a mean value for the whole domain (a and f) or a given elevation band (b-e and g-j) for the *Uniform* ensemble. The red line and shading show the mean ensemble and spread of the velocity respectively. In the same way, the blue colour represents the effective pressure while the dashed black line is the runoff presented on the right axis. Note that the runoff axis is the same for every plot but that this is not true for the velocity and effective pressure axes. The yellow shading represents the summer period from day 100 to 241.

tigate the impact of the different forcings. Here we expect those instability to be similar for the simulations with a large number of moulins (*Uniform* and *Fine* in Table 1), to cope with this issue we will again perform a ensemble of simulations with this time only 20 members per ensembles. We use the same method as was used in de Fleurian et al. (2022) to produce the ensemble with all parameters of the simulations identical but the starting time which is delayed by one extra second for every simulation.

3 Results

We take as a reference the *Uniform* simulation in which each model node is an injection point for the subglacial drainage system. In this case, the models counts 844 moulins that are active at one time or an other during the simulation. That translates to a mean drainage basin area of 0.7 km^2 (Table 1). The results of this ensemble of simulations are presented in Figure 1 where we show the evolution of the surface velocity and effective pressure as a mean value over the whole domain and at given altitudes.

The mean velocity over the domain (Figure 1a) presents a typical pattern for a glacier with a marked and short-lived spring speed-up event followed by a second acceleration event before the velocities drop down to a lower level. At the end of the melt season we see a large spread in the evolution of the velocities with some of the ensemble members showing a strong re-acceleration while other tend to stay at a more reasonable summer velocity level. The velocity patterns are driven by the evolution of the effective pressure, as shown on Figure 1f the initial speed up is related to a sharp drop in effective pressure at the beginning of the melt season. Then the activation of the efficient drainage system leads to a gentler slope in the decrease of the effective pressure which in turn allows the velocity to slow down to their summer level. Finally at the end of the season, the end of the melt leads to a fast increase of the effective pressure which is mediated by the pace at which the efficient drainage system collapses and explains why some mem-

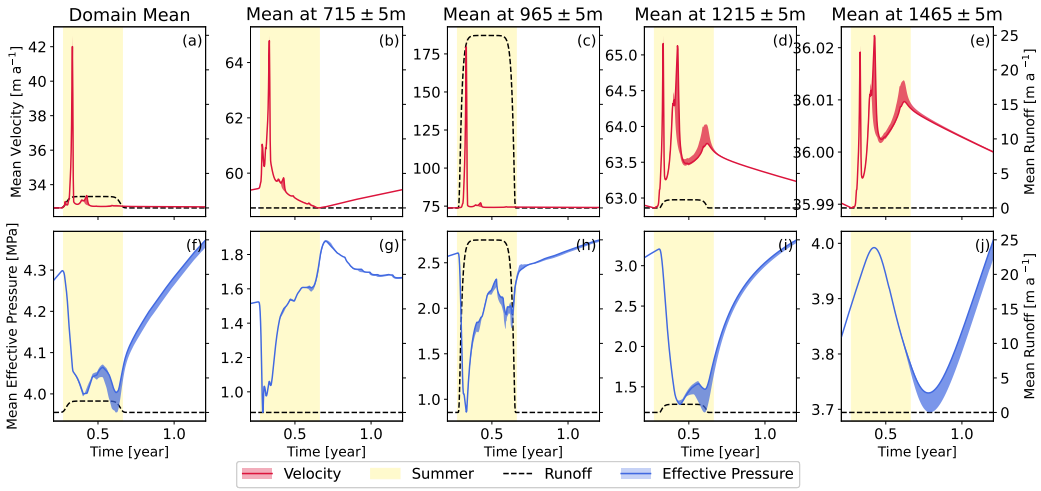

Figure 2. Same as Figure 1 but for the *Coarse* ensemble. Note that the runoff is null at 715 m as there is no moulins in this elevation band

bers have a strong end of summer acceleration while other don't. The velocity and effective pressure pattern is quite different depending on the altitude that we consider. At low elevations (bellow 1000m, Figures 1b-c and 1g-h) the velocity and effective pressure evolution are very similar to the one described for the whole domain with a slight difference in the fact that the effective pressure rebounds to slightly higher values once the efficient drainage system is activated. At higher elevation but below the no melt zone (Figures 1d and i) the most obvious change is the absence of a spring speed-up event. At this elevation, the velocity evolution is characterised by a gradual increase in velocities from the beginning of the melt season all the way to its end. This acceleration is driven by a decrease in effective pressure that first drops at the beginning of the melt season and then levels out but without the rebound that was observed at lower elevations. Above the melt region (Figures 1e and j) the velocity pattern is similar as described above but with a much smaller amplitude (note the changes in y-axis range in Figure 1). Here the small amplitude of the velocity changes, the decoupling with the effective pressure evolution, and the absence of meltwater input points towards a velocity change that is due to the downstream evolution of velocities.

Changing the number of moulins that are used to inject water into the subglacial drainage system as a large impact on the model results. Figure 2 shows the result for the *Coarse* simulation with only 50 moulins which translates to a mean catchment area of 13 km^2 (Table 1).

The first obvious difference with Figure 1 is the drastically smaller amplitude of the velocity changes for the simulation with a lower number of moulins. An other clear result is the diminution in the spread of the computed velocities with the ensemble with only 50 moulins showing almost no spread between its members (Figure 2). The reduction of the number of moulins as presented on the *Coarse* simulation (Figure 2) leads to the disappearance of the end of summer acceleration at all elevations. The velocity response of the *Coarse* simulation is entirely explained by the changes in the evolution of the effective pressure during the melt season. While the evolution at higher altitudes is quite comparable for the *Uniform* (Figure 1i-j) and *Coarse* (Figure 2i-j) simulations the patterns are quite different at lower elevations. Closer to the glacier front, the effective pressure of the *Coarse* simulations (Figure 2g-h) show an earlier rebound of the pressures towards a higher summer value after the initial drop than the one in the *Uniform*

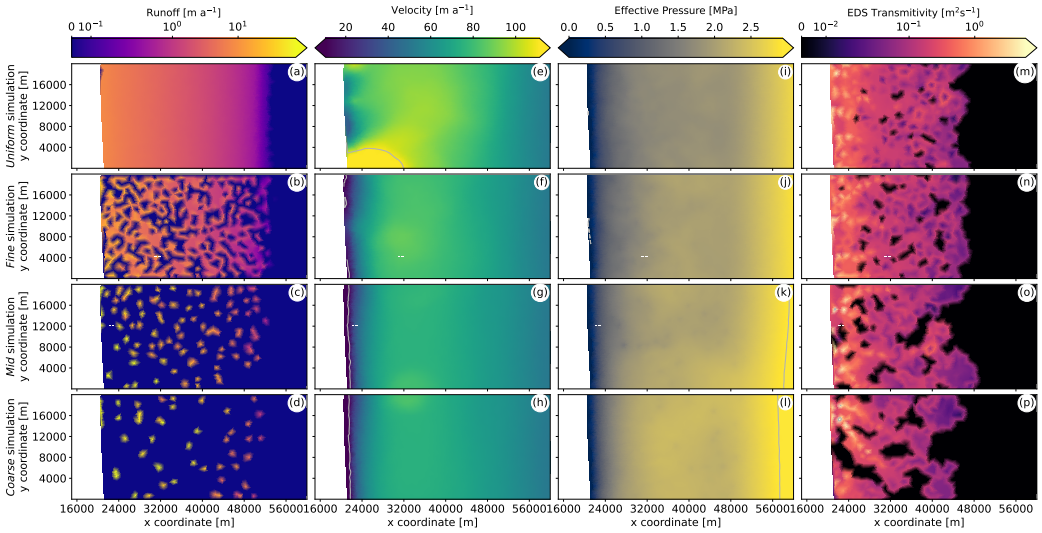

Figure 3. Annual mean values of Runoff (a-d), Velocity (e-h), Effective Pressure (i-l) and efficient drainage system (EDS) Transmitivity (m-p) for the different simulations (*Uniform, Fine, Mid, Coarse*). The ice flow is from right to left and we only show here the lower region of the glacier which experiences melt. The grey lines show the boundaries out of which the colorbar is saturated. We present here the values for a single member of the ensemble and all other ensemble members show a similar pattern.

ensemble (Figure 1g-h). It is this difference in effective pressure that explains why the end of summer acceleration events are mostly absent from the simulations with a smaller number of moulins.

A map view of the mean annual value of the different variables of the model give a better insight into the sources of the differences that are observed in the effective pressure and velocity evolution. Figure 3 presents map views of the region of the glacier where the runoff takes place leaving out the uppermost region of the glacier where the differences due to a change in recharge distribution are less pronounced.

Figure 3 compares the mean annual runoff, velocity, effective pressure and efficient drainage system transmitivity for a given member of the four ensembles from *Uniform* at the top to *Coarse* at the bottom. Note here that as the number of moulins reduces, the intensity of the recharge at each of those points increase as the moulins are draining a larger area of the glacier and so funnelling a larger amount of water toward the ice base (see Table 1 for statistics on catchment area). In term of velocities Figures 3(e-h) show the large difference that appears between the simulation fed by every node or the ones that receive water through a decreasing number of moulins that was already shown on Figures 1 and 2. The observation of the temporal evolution of velocities are confirmed by the mean annual values with notably faster velocities if the water input is spread over a larger number of moulins. The upstream shift of the maximum velocity region which was noticeable on the temporal evolution is also very clear here with only the *Uniform* simulation that presents its fastest velocity towards the front of the glacier while the simulation with a lower number of moulins have their maximum velocities roughly 12km upstream from the front. This is driven by the effective pressure presented on Figures 3(i-l) where we observe higher effective pressure with a lower number of moulins but also a more grainy pattern for the effective pressure which is driven by the coarser water input. Those fields are explained by the way in which the efficient drainage system devel-

ops, on Figures 3(m-p) we show the mean transmitivity of the efficient drainage system which describes its efficiency. We see for the *Uniform* simulation a smooth transmitivity pattern for the efficient drainage system with a decrease from high efficiency at the front to lower efficiency at the top of the ablation zone. As the number of moulins is reduced the efficient drainage system shows a more localised pattern where the regions of the efficient drainage system that are active are also more efficient than they were when a large area of the bedrock was occupied by the efficient drainage system.

4 Discussion

Our experiments show that the distribution of injection points to the subglacial drainage system leads to substantial changes in both the geometry of the efficient drainage system and its overall impact on ice velocity.

This conclusion is in line with the study Scholzen et al. (2021) that showed that a more localised water input into the subglacial drainage system leads to a faster development of the efficient subglacial drainage system. It is however quite different from the results presented by A. Banwell et al. (2016) who found that a higher moulin density causes an earlier onset of channelization and overall more widespread efficient drainage system. We argue that the differences here are mostly due to the change in timing in their recharge scenario but also on the definition of the efficient drainage. A. Banwell et al. (2016) consider any channel that opens as an efficient drainage system, but looking at their Figure 4 we see that their simulations present the same patterns as ours with a lower moulin density leading to less widespread efficient drainage system but with a higher efficiency. This leads to a more efficient drainage of the inefficient drainage system and higher effective pressures which in turns causes slower ice flow than in experiments with a more homogeneous water recharge.

In our model, the specific localisation of water input induces a more stable configuration of the subglacial drainage system. This is due to the fact that the moulins act as anchor points for the subglacial drainage system to develop. This contrasts with the more random development of the efficient drainage system for simulations with a more uniform input which lead to large spread of effective pressure within a given model ensemble (see *Uniform* ensemble and simulations from (de Fleurian et al., 2022).

The observed response can be compared to the results of our preceding study comparing the intensity vs. length of the melt season (de Fleurian et al., 2022). There, a more intense melt season was driving a slower ice flow as it allowed the faster development of the efficient drainage system and as such an overall higher effective pressure. That compares well with the results that we show here, were a lower number of moulins lead to a more intense and localised water input. This triggers a faster development of the efficient drainage system at these locations which help to raise the effective pressure on the whole domain and such lead to a slower glacier.

The change in the distribution of the water sources also shows an upstream shift in the maximum velocity values. This is well illustrated in Figures 3(e-h) but also comparing the velocities on Figures 1, S1, S2, and 2 where we see an upstream migration of the fastest velocities. The pattern of the lower density moulin simulations are more coherent with the velocity patterns that have been observed in Greenland (Fitzpatrick et al., 2013; Sole et al., 2013). This change is driven by the concentration of subglacial water in a small number of pathways at the front of the glacier. The large efficiency of the drainage system close to the front leads to a quick rebound of the effective pressure at the beginning of summer towards a high effective pressure. This, in turns, reduces the intensity of the spring speed-up for the simulations with a low moulin density (*Mid* and *Coarse*. The recurrence of late summer acceleration is also reduced when the water input is achieved through a network of moulins rather than a uniform input. Again that

is due to the localisation of the water input which leads to more localised and efficient subglacial drainage system. Those well developed system tend to be active longer through the season and avoids the low effective pressure that was observed with more widespread water input.

5 Conclusions

On a synthetic geometry and with an idealised meltwater forcing, we show that a change in the distribution of the meltwater input to the basal drainage system as a large impact on the velocity of the overlying glacier. Our experiments show that as the number of moulins diminishes, and the intensity of the recharge at these points increases, the velocity at the surface of the glacier greatly decreases. We associate this decrease in velocity to a faster, and more localised development of the efficient drainage system in our model with a higher efficiency of this system. The more localised water input into the subglacial hydrology model also leads in this particular model to a better physical stability of the model due to the "anchoring" effect of the more localised input which constrains the location of the efficient drainage system. The results of this study show the importance of moving away from uniform water input into subglacial hydrology models. This poses the question of what is the real distribution of moulins and warrants more studies to allow a better characterisation of the supraglacial drainage system that would be usable for subglacial hydrology models.

Open Research Section

The Ice-sheet and Sea-level System Model is freely available at `https://issm.jpl.nasa.gov/` this specific study uses the development branch of the code at the revision number 27528 last updated on January 19 2023. The model set-up, outputs and post treating scripts corresponding to this study are available on zenodo (doi to come). The figures in this manuscript were generated with the script in the archive above and with Matplotlib v3.5 (Hunter, 2007).

Acknowledgments
This work is part of the SWItchDyn project funded by the Research Council of Norway (NFR-287206). Computing was performed on the resources provided by UNINETT Sigma2 – the National Infrastructure for High Performance Computing and Data Storage in Norway (NN9635K and NS9635K).

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