Predicting infrasound transmission loss using deep learning

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(Dated: December 16, 2021)

Modelling the spatial distribution of infrasound attenuation (or transmission loss, TL) is key to understanding and interpreting microbarometer data and observations. Such predictions enable the reliable assessment of infrasound source characteristics such as ground pressure levels associated with earthquakes, man-made or volcanic explosion properties, and ocean-generated microbarom wavefields. However, the computational cost inherent in full-waveform modelling tools, such as Parabolic Equation (PE) codes, often prevents the exploration of a large parameter space, i.e., variations in wind models, source frequency, and source location, when deriving reliable estimates of source or atmospheric properties – in particular for real-time and near-real-time applications. Therefore, many studies rely on analytical regression-based heuristic TL equations that neglect complex vertical wind variations and the range-dependent variation in the atmospheric properties. This introduces significant uncertainties in the predicted TL. In the current contribution, we propose a deep learning approach trained on a large set of simulated wavefields generated using PE simulations and realistic atmospheric winds to predict infrasound ground-level amplitudes up to 1000 km from a ground-based source. Realistic range dependent atmospheric winds are constructed by combining ERA5, NRLMSISE-00, and HWM-14 atmospheric models, and small-scale gravity-wave perturbations computed using the Gardner model. Given a set of wind profiles as input, our new modelling framework provides a fast (0.05 s runtime) and reliable ($\sim$ 5 dB error on average, compared to PE simulations) estimate of the infrasound TL.

1. INTRODUCTION

Surface and subsurface sources (e.g., explosions, microbaroms, earthquakes) excite low-frequency acoustic waves, i.e., infrasound, that can travel large distances in the Earth's atmosphere. The refraction and reflection of infrasound waves back to the surface due to vertical and horizontal gradients of atmospheric winds and temperatures enable their detection at ground arrays. Because infrasound waves carry information about the source, they have traditionally been used to retrieve location and yield estimates of nuclear explosions (*Evers and Haak*, 2010). Recently, the detection and modelling of infrasound phases have also enabled the inversion of critical seismic source and subsurface parameters such as focal mechanism (*Shani-Kadmiel et al.*, 2021), focal depth (*Averbuch et al.*, 2020; *Lai et al.*, 2021), ground motions (*Hernandez et al.*, 2018), or seismic velocity structures (*Brissaud et al.*, 2021).

Accurately predicting the spatial distribution of infrasound attenuation, i.e., Transmission Loss (TL), is key to build robust estimates of source and subsurface characteristics. Parabolic Equations (PE) (*Waxler et al.*, 2021) or finite difference codes (*de Groot-Hedlin*, 2008; *Brissaud et al.*, 2016) are typically used to compute accurate estimates of acoustic amplitudes in realistic wind structures. However, owing to the prohibitive computational cost of full-waveform numerical modelling tools, most infrasound studies rely on empirical equations to relate infrasound amplitudes to source parameters. Widely-used regression equations include models to estimate the explosion yield from peak infrasound amplitudes (e.g., *Golden et al.*, 2012) and empirical equations relating pressure at the source and observed infrasound amplitudes (*Le Pichon et al.*, 2012). In particular, the construction of empirical equations ignores or greatly over-simplify atmospheric wind structures. For instance, in *Le Pichon et al.* (2012), the authors assume a single range-independent Gaussian stratospheric duct to optimize their regression model. Yet, vertical and horizontal wind gradients at various altitudes can drastically affect the TL at the ground (*de Groot-Hedlin et al.*, 2010).

Empirical models rely on over-simplistic representations of the wind structures because the mapping between source frequency, atmospheric specifications, and TL is highly nonlinear and poorly constrained. In order to bridge the gap between computationally expensive numerical models and over-simplistic empirical equations, supervised Machine-Learning (ML) models trained over synthetic or recorded datasets can offer an accurate and inexpensive alternative to existing modelling tools (*Michalopoulou et al.*, 2021). Several authors have employed ML models to predict TL: *Pettit and Wilson* (2020) built a Physics-Informed Neural Network (PINN) trained over synthetic PE simulation results to predict attenuation maps (along range and altitude) in the atmospheric boundary layer. PINN consist in updating the cost function to include physics-based constraints. This model provides an inexpensive alternative to existing modelling tools but shows low accuracy as it is difficult adjusting the weights of the physics-informed parameters in the objective function. Additionally, atmospheric specifications are encoded using only wind profiles, and this approach was not adapted to long-range propagation. *Hart et al.* (2021) used a fully connected neural network to predict two-dimensional (2D) attenuation in a turbulent atmosphere from a set of predefined input parameters describing the turbulent field. This model shows a relatively low error (< 7 dB) but relies on over-simplified wind models with a set of 13 inputs to describe the velocity field which are not representative of long-range propagation.

Relating wind structures to TLs is key to accurately reproduce full-waveform simulations. Instead of using pre-defined parameters to describe the wind velocity field, Convolutional-

Neural Networks (CNN, *Krizhevsky et al.* (2012)) provide an excellent solution to identify patterns of interest within input wind models. Such patterns are extracted using a set of filters described by a number of coefficients that are optimized during the ML training process. Such network is typically followed by a set of fully-connected network to relate the encoded information by the CNN and the output. In this contribution we propose a new ML model trained over synthetic PE simulations to build ground TL in realistic range-dependent wind models that both shows a low computational cost compared to existing modelling tools, and high accuracy over long-range propagation.

2. BUILDING A TRANSMISSION-LOSS DATASET

Building a synthetic TL dataset requires a modelling tool and a set of atmospheric models. Similar to *Le Pichon et al.* (2012), we generate TL profiles using the open-source (PE) solver ePape, provided by the US National Center for Physical Acoustics (NCPA, *Waxler et al.*, 2021). To provide realistic bounds for the atmospheric models, we collect 524 slices of 1000 km up to 80 km altitude from ERA5 re-analysis models, discretized over 137 altitude levels (*ECMWF*, 2018) with a horizontal resolution of 1 degree. The spatial step of 1 degree is picked as a trade-off between the resolution to capture ERA5 spatial variability and the computational time to both download atmospheric models and run simulations. Since ERA5 models are limited to around 80 km altitude, we use two empirical models to retrieve atmospheric properties up to 120 km altitude: HWM-14 to obtain zonal and meridional winds (*Drob et al.*, 2015), and NRLMSISE-00 to retrieve temperatures (*Picone et al.*, 2002). ERA5 and HWM-14/NRLMSISE-00 atmospheric models are stitched together using a cubic interpolation between over the altitude range of 75 to 85 km. Because atmospheric properties vary with latitude, longitude, and time of the year, ERA5 profiles are uniformly sampled between latitudes -40 to 70 degrees, longitudes -150 to 165 degrees, and between years 2010 to 2020 (see Fig. 1a).

ERA5 models lack resolution to capture fine-scale wind and temperature fluctuations owing to, e.g., gravity-wave breaking above the troposphere (*Chunchuzov et al.*, 2015; *Chunchuzov and Kulichkov*, 2019). To account for unresolved wind perturbations at higher altitudes, infrasound studies typically consider the Gardner model to add gravity-wave perturbations to the original wind profiles (*Gardner et al.*, 1993). Therefore, we account for small-scale perturbations by considering four Gardner realizations for each atmospheric slice (see green stage in Fig. 2a). Similar to *Norris and Gibson* (2002), we generate Gardner perturbations by considering four altitude levels 84, 70, 45, and 21 km, at which we sample standard deviations uniformly within the range of, respectively, 1–25, 1–18, 1–10, and 1–5 m/s. Finally, because the direction of propagation within an atmospheric slice, i.e., upwind or downwind propagation, greatly alters the TLs at the ground, we augment our dataset of atmospheric models by running simulations in both scenarios by changing the sign of the projected winds (see yellow stage in Fig. 2a). Our final dataset includes 20960 simulations.

The distribution of effective velocity ratios $\overline{c}_{\text{eff}}$ computed from our final atmospheric model dataset for three different altitude regimes, shown in Fig. 1b, is close to a Gaussian distribution, centred around $\overline{c}_{\text{eff}} = 1$. This indicates that our dataset includes models with and without strong high-altitude ducts. The distribution of tropospheric effective velocity ratios is centred at lower values than for higher-altitude layers. This owes to the small number of occurrences of tropospheric wave ducts in our dataset. In contrast to large vertical variations of wind velocities, most ERA5 models show small (< 15 m/s) lateral variations of

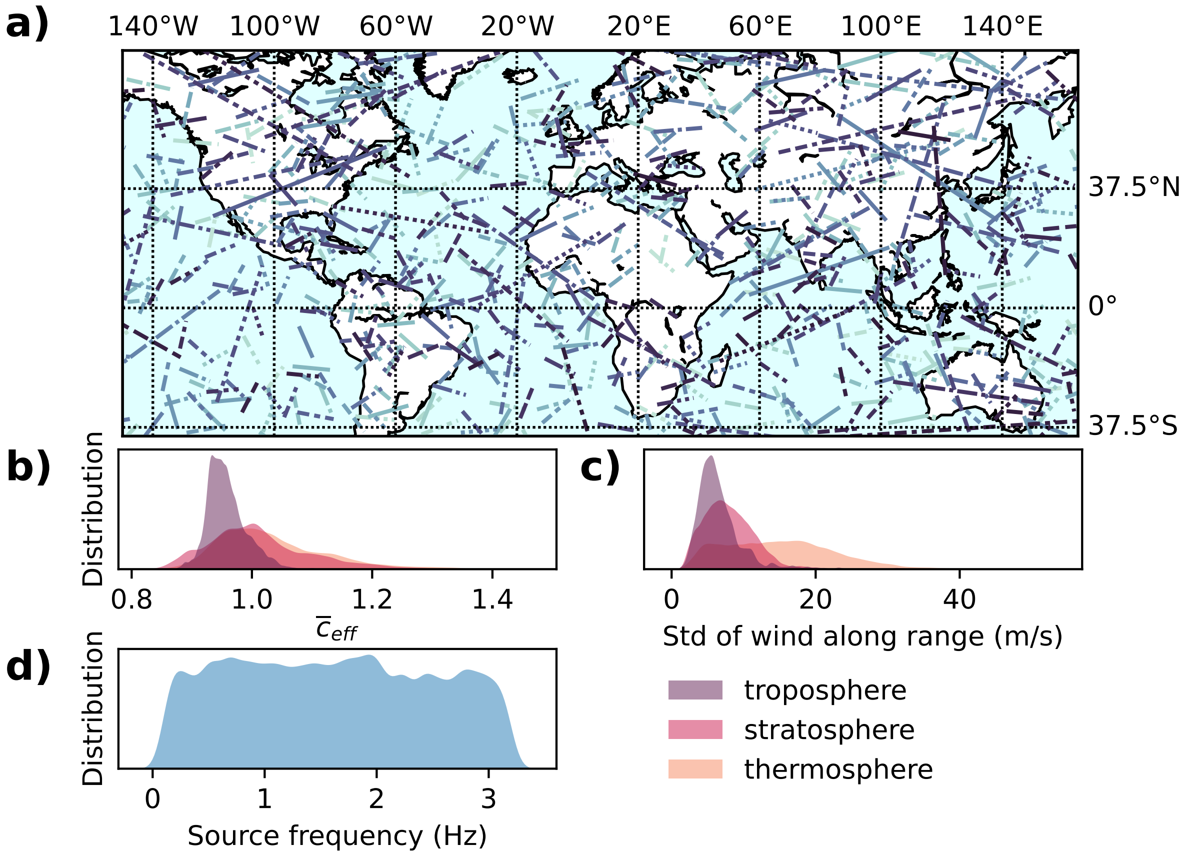

Figure 1. Atmospheric model dataset. (a) distribution of 1000 km long atmospheric slices extracted from the ERA5 dataset. (b) Distribution of effective velocity ratio $\overline{c}_{\text{eff}}$ between the ground and various atmospheric layers: troposphere (purple) between 5 and 20 km altitude, troposphere (purple) between 20 and 50 km altitude, and thermosphere (purple) between 50 and 100 km altitude. (c) Distribution of standard deviations of wind velocities along range for various atmospheric layers. (d) Distribution of input source frequencies used in PE simulations to build our TL dataset.

wind velocities. The largest lateral wind variations occur above the stratosphere since winds at these high altitudes are generally the strongest on Earth (*Blanc et al.*, 2018).

TL profiles are then computed for a surface sources over 1000 km using 7 Padé coefficients and the Sutherland-Bass attenuation model (*Sutherland and Bass*, 2004) using NCPA's ePape PE simulator (*Waxler et al.*, 2021). Signals from sources of interest (earthquakes, volcanoes, large explosions) typically show dominant frequencies below 5 Hz. Therefore, similar to *Le Pichon et al.* (2012), we sample 5 source frequencies from a uniform distribution between 0.1 to 3.2 Hz for each atmospheric slice (see Fig. 1d and Fig. 2a). PE assumes slow lateral variations in the atmospheric properties over the scale of one wavelength. To ensure smoothly varying atmospheric properties, we must only consider models that do not include lateral variations over the scale of the largest wavelength considered, which means $\lambda \approx 3.5$ km at 0.1 Hz. Because we are using a 100 km horizontal sampling, interpolation of atmospheric properties within the NCPA software will generate smooth-enough models to fulfil the PE assumptions.

PE neglect nonlinear terms and cross winds. Nonlinearities affect primarily the amplitude and frequency content of thermospheric phases for large-amplitude pressure sources (*Sabatini et al.*, 2019). Therefore, uncertainties on the predicted amplitudes must be accounted for when investigating high-yield surface sources. When large-amplitude sources are considered, PE simulations will severally overpredict the amplitude of refracted phases at the ground. While cross winds have a significant impact on the apparent backazimuth observed from refracted phases at stations located at large distances from the source, their influence on infrasound amplitudes is insignificant (*Hernandez et al.*, 2018; *Shani-Kadmiel et al.*, 2021).

3. DESIGNING A TRANSMISSION-LOSS MODEL

Parabolic equations correspond to a mapping between 2D vertical range-dependent vertical profiles (temperature, winds, and pressure), frequency, and ground transmission loss profiles under the effective-velocity approximation (*Waxler et al.*, 2021). Our goal is to find an alternative nonlinear map between PE inputs and outputs using a neural network in order to reduce the computational cost. Variations of TL with range for a given source frequency between different atmospheric models are primarily controlled by lateral and vertical wind variations. To reduce the complexity of our ML architecture, we simplify the TL-prediction problem by assuming that there exists an additional nonlinear mapping between frequency, 2D wind variations and TL that approximates the PE solution.

Because local wind variations can explain the of infrasound rays back to the surface (*Chunchuzov et al.*, 2015), we use a Convolutional Neural Network (CNN) to encode the nonlinear relationship between local wind patterns, represented as 2D images, and TL profiles. Since the relationship between frequency and TL for complex wind structures is poorly constrained, we approximate this undefined mapping by using fully-connected layers, which are the most generic neural network architectures. The final architecture (Fig. 2b) consists of two layers of 2D convolutions using 5×5 kernels followed by Batch normalization and Average Pooling. The encoded winds are then concatenated with the source frequency input, and three fully-connected layers. Average pooling consists of taking the average of the output of each convolution which is employed to both reduce the dimensionality and learn translation invariance over the input representation. Batch normalization (*Ioffe and Szegedy*, 2015) re-centers and re-scale the input of each layer over each mini-batch during the training process. Normalizing batches reduces the variations of distributions in inputs at each layer, speeds up training, and produces more reliable models. Both Batch normalization and Average Pooling layers are used to make the ML model more robust to new data. The last fully connected layer being the output layer that represents the normalized TL profile between 0 to 1000 km. All weights are initialized using a uniform Glorot initializer (*Glorot and Bengio*, 2010).

To facilitate the recognition of patterns in input data, winds are vertically downscaled and horizontally upscaled from a 10×1000 2D image, i.e., 10 profiles discretized over 1000 points along the altitude, to a 50×40 2D images. To limit the range of input and output values, input profiles and outputs TLs are then normalized by removing the mean and scaled to unit variance. Both mean and variance are computed over the training dataset only. The output layer corresponds to the normalized TL profile linearly interpolated it over 500 points within the range 0 to 1000 km. We train the neural network using an Adam optimizer (*Kingma and Ba*, 2015) with a starting learning rate of 10^{-4}. ReLu activation functions are used throughout the network expect for the output layer where we do use any activation function. The ML architecture is implemented in Python using the TensorFlow library (*Abadi et al.*,

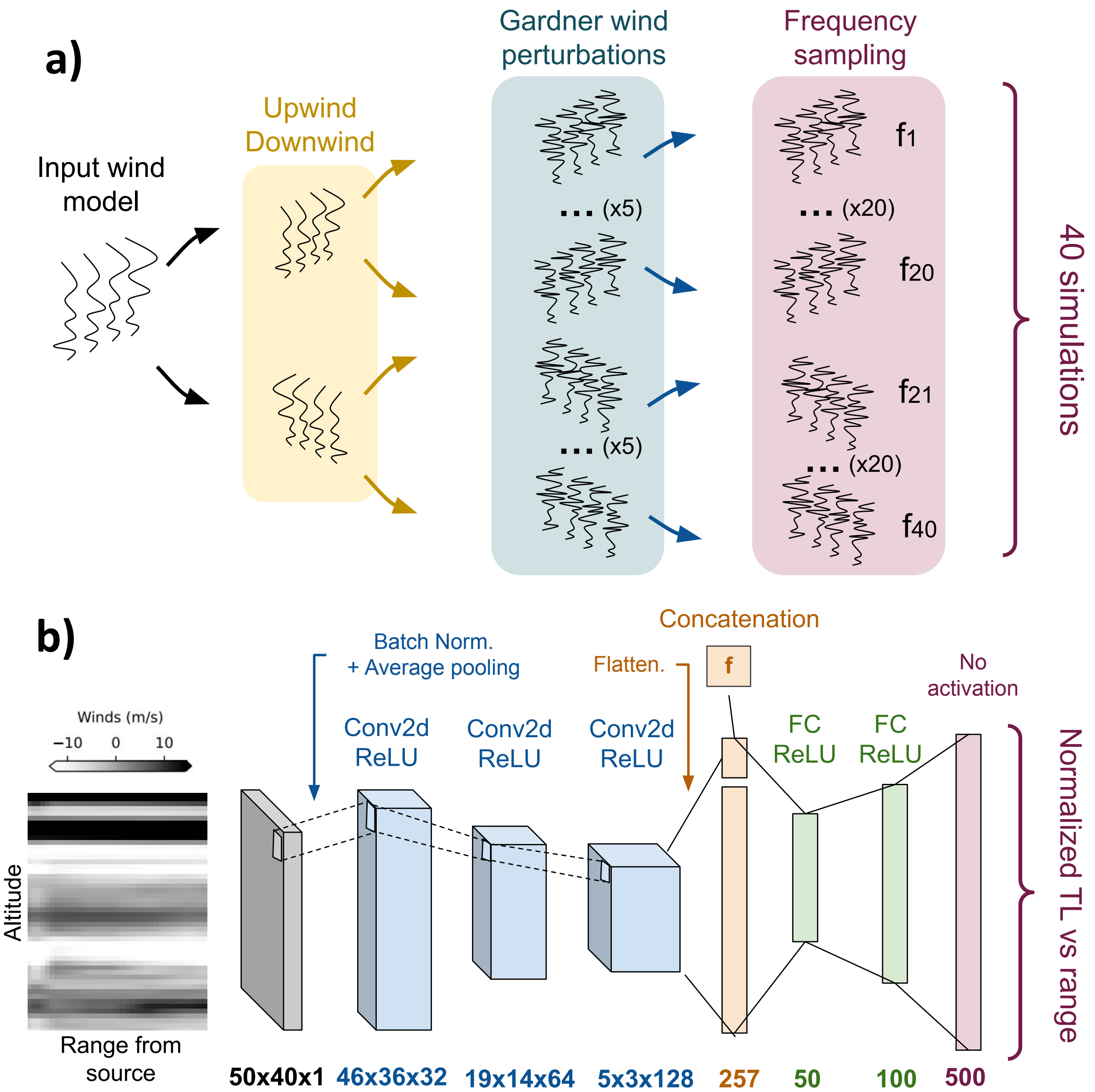

Figure 2. Dataset creation and ML architecture. (a) Procedure to augment our atmospheric model dataset. First upwind and downwind scenarios are considered for each wind slice. The difference between upwind and downwind scenarios corresponds simply to flipping the sign of the projected winds onto the slice. Then, 5 random set of Gardner perturbations are generated for both upwind and downwind scenarios. Finally, 4 input frequencies are considered for each perturbed wind model. A total of 40 wind models are generated for each atmospheric slice extracted from the ERA5 dataset. (b) Cartoon depicting a deep learning network workflow for TL predictions. We use 2D representation of wind amplitudes (grey) with size 50 × 40 as inputs for our ML model. In the first stage (blue) we use three Convolutional Neural Networks (CNN) to encode the wind information as a vector of size 256. In the second stage (orange), we concatenate this wind encoding with the input source frequency. In the third stage (green), we build a mapping between input frequency and encoded wind representation using two Fully-Connected (FC) layers to finally produce a normalized TL vs range of size 500 (red). This normalized TL can be transformed back to dB by using the scaling transformer used for pre-processing the data.

2015). More details about architecture optimization are provided in Appendix A.

4. VALIDATION OF MACHINE-LEARNING PREDICTIONS

To optimize our ML model, we split our full dataset between 85% training data and 15% validation data. Strong correlations in TL are expected between PE simulations using wind models corresponding to perturbed versions of the same original unperturbed wind model along a given atmospheric slice. Therefore, before training, all simulations corresponding to the same original atmospheric slice (see the first stage in Fig. 2a) are added to same set (either training or validation) to make our model more robust to new data. To facilitate convergence, we adaptatively update the learning rate when the Root Mean-Square-Error (RMSE) does not decrease over the course of 3 epochs, i.e., training steps. To avoid over-fitting the training data, we use early stopping if the MSE does not decrease over the course of 12 epochs. Finally, to speed up the training process, we use mini-batches of size 32.

Our ML model converges within 80 epochs with a validation RMSE (over normalized TL profiles) twice larger than the training RMSE (see Fig. 3a). Once trained, the ML model has a computational cost of around 0.05 s (Dell T5610 Intel Xeon E5-2630 v2 2.6 GHz 6 CPUs 64GB RAM on CentOS 7) for all input frequencies while PE simulation cost increases significantly with frequency up to 100 s at 3.2 Hz (see Fig. 3b), which is 2000 times larger than the cost for a ML prediction at the same frequency. In Figs 3c and 3d, we show that the RMSE of our ML model follows a bell-shaped distribution centred between 5 to 9 dB with both variations in distance from the source and source frequency. This distribution of errors indicates that our ML implementation is stable for the range of frequencies and distances considered in our dataset. Larger errors tend to occur for high frequencies (> 2 Hz) and close to the source (< 200 km). Higher frequencies are more sensitive to small-scale wind variations which leads to more complex distributions of TL with range. This added complexity in high-frequency TLs leads to larger errors in ML predictions. Most TL variations occur within 200 km from the source with the presence of the first acoustic shadow zone and first stratospheric return which explains the larger errors observed close to the source.

We observe in Figs 3e and 3f that ML predictions match well the average variations of TL with range from the source. In particular, the ML model captures accurately the TL gain associated with the different stratospheric returns and the TL asymptotic behaviour at large distances from the source. However, the ML model does not fully reproduce high-frequency TL variations, which correspond to small-scale changes in effective wind velocities. The ML model therefore provides a low-passed solution of the true TL profile. Our model is unable to learn all small-scale perturbations in the wind models primarily due to the lack of training data. Yet, small-scale wind perturbations are generally unresolved in currently available atmospheric models. Therefore, these high-frequency TL perturbations fall within the uncertainty range associated with available atmospheric model resolutions. Along with ML predictions, we can determine an estimate of the ML uncertainty u by computing the median TL error vs range in a given frequency range $\mathbf{f}$, as the median TL error vs range from the source over the testing dataset such that $u(r, \mathbf{f}) = \text{median}\{|\text{PE}(r, f) - \text{ML}(r, f)|\}$, where r is the range, f is the frequency, PE is the TL predicted using Parabolic Equations, and ML is the TL predicted using Machine Learning. The frequency dependence of the uncertainty curves u (see frequency dependence of the errors in Fig 3c) is accounted for by computing the errors in five frequency ranges $\mathbf{f}$ equally distributed between 0.1 to 3.2 Hz. We observe that errors between our ML predictions and the PE simulations fall within the ML uncertainty

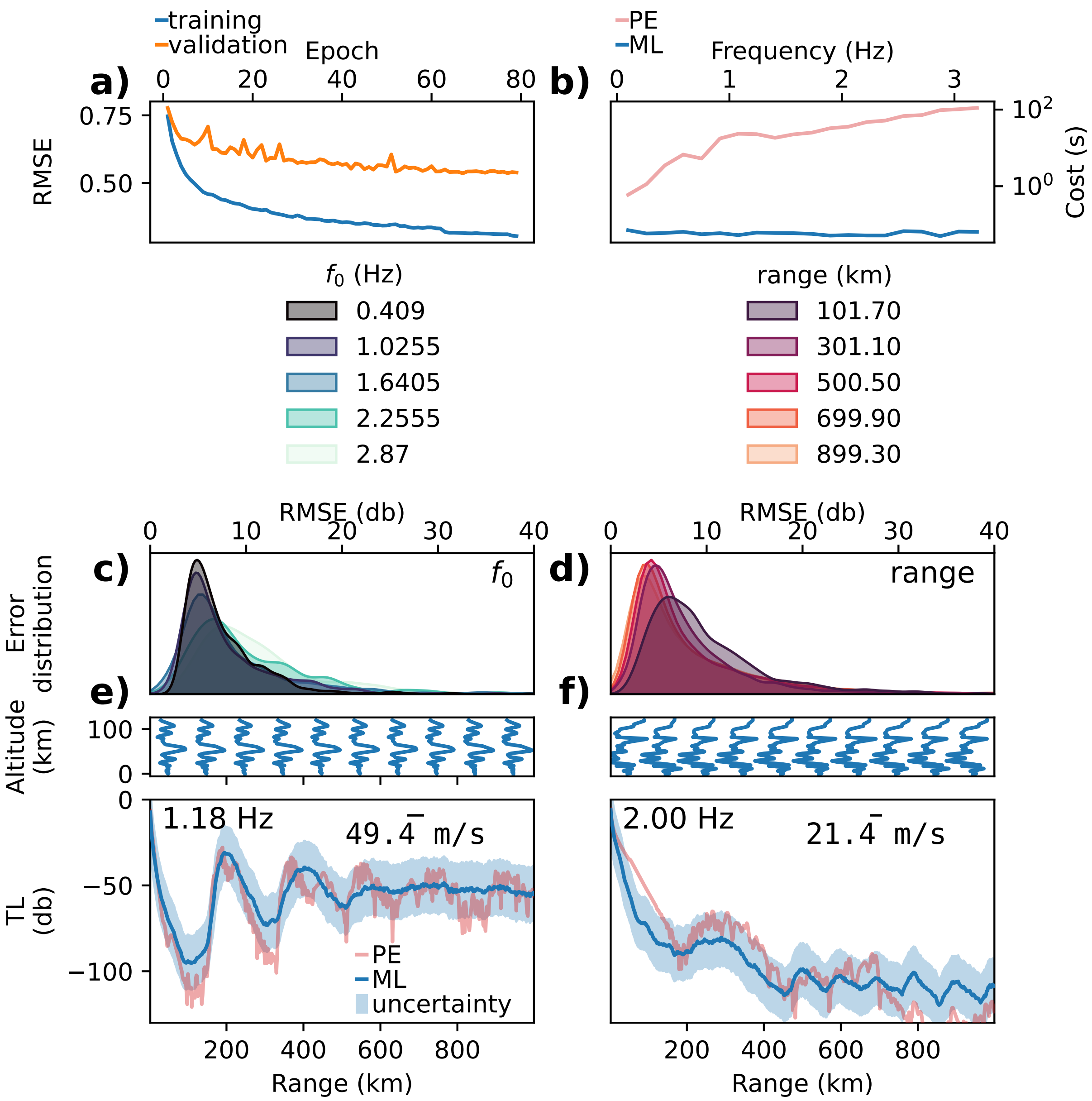

Figure 3. Training and validation of the ML model. (a) Evolution of Root-Mean Square Errors (RMSE) with training epoch. (b) Computational cost of PE simulations (red) and ML predictions (blue) vs input source frequencies. (c) Distribution of RMSE over the testing dataset for various input frequencies. (d) Distribution of RMSE over the testing dataset for various ranges from the source. (e,f) bottom, TL predicted by PE simulations (red) and ML model (blue) along with the ML uncertainty (light blue) for an (e) upwind and (f) downwind wind scenario. (e,f) top, corresponding wind models used for ML predictions. The ML uncertainty u is computed, in a given frequency range $\mathbf{f}$, as the median TL error vs range from the source over the testing dataset such that $u(r, \mathbf{f}) = \text{median}\{|\text{PE}(r, f) - \text{ML}(r, f)|\}$, where r is the range, f is the frequency, PE is the TL predicted using Parabolic Equations, and ML is the TL predicted using Machine Learning.

range (blue shaded region in Figs 3e and 3f). As suggested by the distributions showed in Figs 3c and 3d, the uncertainty range remains stable with variations in frequency and range from the source.

Transfer Learning (TrLe) is typically used to improve the performances of CNNs over small datasets. Here, TrLe consists of using a CNN network pre-trained over a large dataset of 2D images for a different task (e.g., multi-class classification of real images from a dataset such as ImageNet *Deng et al.* (2009)) to initialize our wind encoding stage. This technique assumes that there are some invariances between our wind-encoding problem and traditional image-segmentation problems. We tested TrLe by replacing our CNN encoding stage (blue in Fig. 2b) by both a VGG16 (*Simonyan and Zisserman*, 2015) or a ResNet50 (*He et al.*, 2016) network and trained our network using their pre-trained weights and removing pooling layers. However, TrLe's performances were worse (RMSE 9) than with the model presented in Fig. 2b owing to the significant differences between both the set of images used for training in VGG16 or ResNet50 and our wind inputs and the problem of image detection vs TL prediction. .

5. ANALYTICAL VS ML PREDICTIONS OF GROUND TLS

Stratospheric winds are one of the dominant factors to explain the refraction of acoustic waves at large distances from the source (*de Groot-Hedlin et al.*, 2010). A widely used empirical regression equation, introduced in *Le Pichon et al.* (2012), referred in the rest of the paper as LP12, has provided estimates of TL over large distances from a variety of surface sources (*Hernandez et al.*, 2018; *Vorobeva et al.*, 2020; *De Carlo et al.*, 2021). However, the original model was optimized over a set of idealized synthetic and range-independent models where the main feature was a stratospheric duct of various strength, modelled using a Gaussian wind profile centered at 50 km altitude added to the U.S. Standard Atmosphere.

Estimates of LP12 uncertainties over idealized range-independent profiles (*Tailpied et al.*, 2021) show low errors compared to PE simulations ($<$ 10 dB) when strong winds are ducting the signal in the stratosphere. However, in the case of upwind propagation, the accuracy decreases significantly, especially at high frequencies where the errors can be up to 70 dB. Yet, uncertainties introduced by this empirical model for realistic range-dependent wind models are still mostly unconstrained. Comparisons with our PE simulation dataset offer the opportunity to investigate the uncertainties associated with highly heterogeneous wind models for both LP12 and our ML model.

A typical approach to investigate the influence of stratospheric winds on refracted infrasound is to represent the variations of TLs with variations in stratospheric effective velocity ratios, i.e., stratospheric wind strength, and range from the source for different frequencies (*Le Pichon et al.*, 2012). Yet, in contrast to the dataset used for the optimization of LP12, effective velocity ratios in our dataset are not equally distributed since we use the atmospheric model products and not idealized profiles. To provide meaningful comparisons with LP12, we build uniformly-spaced 2D TL maps by performing a linear interpolation of the ML- and PE-predicted TLs between $0.8 \leq \overline{c}_{\text{eff, 40–50 km}} \leq 1.2$, where $\overline{c}_{\text{eff, 40–50 km}}$ is the effective velocity ratio between 40 to 50 km altitude. Linearly-interpolated TL maps are shown in Fig. 4. Comparison between Figs 4a and 4b as well as between Figs 4e and 4f shows that the PE-based TL is well-reproduced by ML over the range of frequencies considered. As mentioned earlier, our ML model tends to smooth out the rapid oscillations in TL predicted by PE simulations. Yet, average errors shown in Figs 4d and 4h are stable around 5 dB for

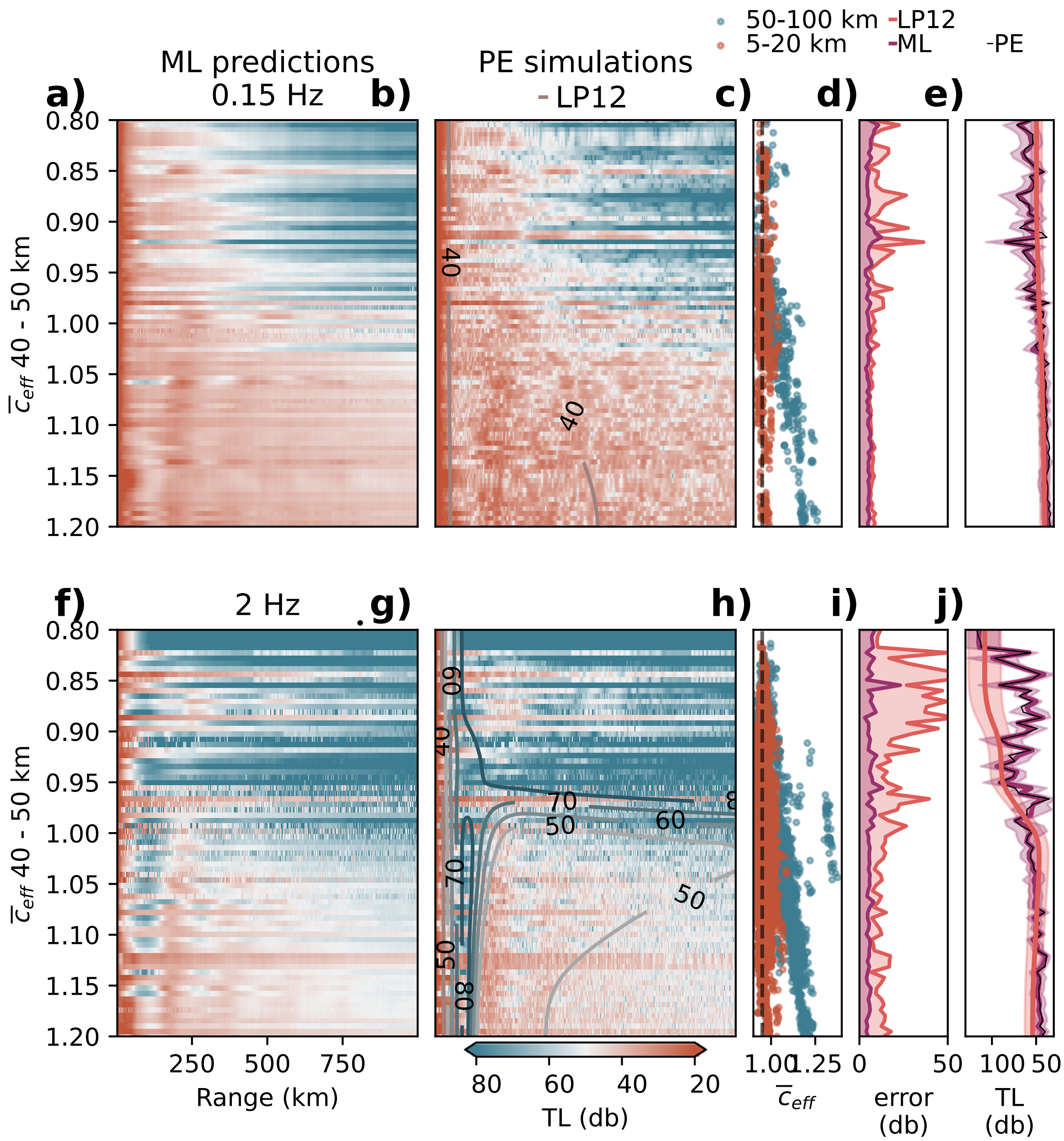

Figure 4. Comparisons of TL maps produced by PE, ML, and LP12 models. (a,b) and (f,g) TL maps vs range and effective velocity ratio $\overline{c}_{\text{eff}}$ between $40-50$ km altitude for a source frequency at 0.15 Hz (a,b) and at 2 Hz (f,g) as predicted by (a,f) the ML model, (b,g) PE simulations, and (b,f isocontours) Le Pichon model. (c,h) effective velocity ratios $\overline{c}_{\text{eff}}$ for the troposphere ($5-20$ km altitude, red) and mesosphere-thermosphere ($50-100$ km altitude, blue) at (c) 0.15 Hz (h) and 2 Hz. (d,i) RMSE in dB between the interpolated TL maps from the PE simulations and the ML model (purple) and Le Pichon model (LP12, red) at (d) 0.15 Hz and (i) 2 Hz. (e,j) Median TL in dB vs $\overline{c}_{\text{eff, 40–50 km}}$ computed from the interpolated TL maps from the PE (black), the ML (purple), and LP12 (red) models at (e) 0.15 Hz and (j) 2 Hz.

all values of $\bar{c}_{\text{eff, 40–50 km}}$.

We also observe that LP12, represented as isocontours in Figs 4b and 4f, is able to capture the main features of the TL maps, namely the first acoustic shadow zone and first stratospheric return within 250 km from the source, and the high attenuation for low stratospheric effective velocity ratios ($\bar{c}_{\text{eff, 40–50 km}} < 1$). The good agreement between numerical simulations and LP12 (Figs 4c and 4h) confirms that average TLs are most sensitive to stratospheric winds when a strong duct is present. This is also shown in Figs 4e and 4j where we observe that the high-$\bar{c}_{\text{eff, 40–50 km}}$ trends of the median TLs are well captured by LP12. However, Figs 4e and 4j show that errors between the empirical model and PE simulations increase significantly for low stratospheric effective velocity ratios ($\bar{c}_{\text{eff, 40–50 km}} < 1$).

LP12 systematically underpredicts the TL for low effective velocity ratios at high frequencies (Fig. 4j), which is consistent with a previous assessment of the empirical model (*Tailpied et al.*, 2021). This owes to the presence of wind ducts outside the stratosphere that are not accounted for in the empirical model (see Figs 4c and 4g). This is especially true at high frequencies (*Chunchuzov et al.*, 2015) and close to the source where small wind variations can make acoustic energy return to the ground (*Chunchuzov et al.*, 2015). Tropospheric ducted arrivals generally show strong acoustic amplitudes at ground arrays and can represent up to 20% of the energy radiated from the source (*Drob et al.*, 2003). Accounting for tropospheric ducting is therefore critical for accurate attenuation assessments in the range of distances from the source (< 1000 km) considered here. However, these ducts generally exist only up to a range of ~ 750 km and do not affect longer-range propagation at a global scale. Note in Figs 4c and 4g that there is a bias in our dataset with the presence of thermospheric ducts only when large stratospheric ducts are present for $\bar{c}_{\text{eff, 40–50 km}} > 1$. This bias represents the inherent correlations present in combined ERA5-NRLMSISE-00 models. Therefore, considering scenarios with low thermospheric winds and strong stratospheric winds might lead to a decrease in ML prediction accuracy.

6. CONCLUSIONS AND DISCUSSION

In this contribution we have proposed an ML-based approach to rapidly (~ 0.05 s runtime) and reliably (~ 5 db dB error on average, compared to PE simulations) predict estimates of ground TL from surface sources up to 1000 km. The trained ML model takes as input a range-dependent atmospheric specification and a wave frequency to generate a TL estimate. Errors compared to full PE simulations remain low for increasing source frequency at close range of the source. Our ML model can reproduce complex TL where guided tropospheric waves and multiple stratospheric returns are present. Comparisons with the regression equation introduced in *Le Pichon et al.* (2012) indicate that considering only the influence of stratospheric winds between 40 and 50 km altitude enables one to reproduce the main features of the variations of TL with effective velocity ratio (LP12's errors remain below 10 dB at low frequency for $c_{\text{eff}} > 1$). However, by neglecting the impact of tropospheric and high-altitude winds, LP12 can lead to significant errors (RMSE ~ 50 dB) while the ML model is able to capture accurately the TL for highly heterogeneous wind structures.

Several techniques could be used to further improve the accuracy of our ML model. Running additional simulations will increase the size of the training dataset which will reduce the RMSE but will not affect the computational cost of ML predictions once trained. Building on *Raissi et al.* (2019); *Pettit and Wilson* (2020), physical constraints imposed by the PEs and its boundary conditions could be integrated into the cost function to facilitate the convergence of our ML model. Because we trained our algorithm over atmospheric models extracted only from the ERA5 and the NRLMSISE-00/HWM-14 climatological models, biases might be present in the structure of the input wind fields used for training due to the specific system of equations solved to produce ERA5 models. Acquiring atmospheric models from additional sources (e.g., MERRA dataset as presented in *Kumar et al.* (2015)), could make the ML model more robust to arbitrary wind models. In addition to atmospheric models, small-scale gravity-wave models could be enhanced by considering more realistic range-dependent perturbations (*Drob et al.*, 2013; *Lalande and Waxler*, 2016).

Our ML model was trained over a set of simulations generated by a PE modelling tool (*Waxler et al.*, 2021) which has strong assumptions about infrasound propagation (see Section 2). In particular, PE simulations ignore the influence of cross winds which have a strong impact on the acoustic wavefronts at large distances from the source. ML predictions are expected to be significantly improved if the synthetic dataset were generated using a more accurate modelling tool such as Finite-Differences (FD, *Brissaud et al.* (2016); *Sabatini et al.* (2019)) or Spectral Element Methods (SEM, *Brissaud et al.* (2017); *Martire et al.* (2021)) solving the full linearized Navier-Stokes equations. However, the computational cost associated with such method is much greater than for PE simulations and generating a large synthetic dataset would require extensive computational resources. This cost could be somewhat alleviated since, by resolving the full three-dimensional wavefield, multiple TLs could be extracted from one FD or SEM simulation by considering different azimuths from the source. Once trained over computationally expensive FD or SEM simulations, we can anticipate the cost of one ML simulation to be on the same order than presented here (< 0.1 s) which makes ML even more attractive than when trained over PE simulations. In addition to the absence of cross-winds, PE simulations ignore topography which causes a significant scattering of acoustic energy (*Drob et al.*, 2003). As FD or SEM tools can incorporate topography, an encoded representation of topographic variations (e.g., one-dimensional CNN) could be concatenated to the frequency and encoded winds to provide more accurate predictions.

This work paves the way for the monitoring and characterization of infrasound sources. Recent studies (*Vorobeva et al.*, 2020; *De Carlo et al.*, 2021) have shown that infrasound generated by colliding ocean waves, called microbaroms, may provide important constraints on stratospheric winds. To validate their theoretical model connecting ocean sources and observations, these studies rely on the empirical model presented in *Le Pichon et al.* (2012). Extending the current ML model to longer ranges (> 1000 km) would be is useful in, e.g., global acoustic event analysis, but would also allow an enhanced modelling of microbarom amplitudes, hence also facilitating the development of global infrasound-based near-realtime atmospheric model diagnostics. Crosswinds are not taken into account in PE simulations which would introduce strong uncertainties at greater ranges. The localization of infrasound sources is generally performed using only the arrival times and backazimuth observed at ground arrays and neglects amplitude (e.g., *Blom et al.* (2018)). The absence of amplitude inputs in the optimization process owes to the high computational cost of full-waveform modelling approaches. The inexpensive ML model introduced here could enable the exploration of variations of relative amplitudes between stations with the choice of source location.

Finally, because ML models provide an analytical relationship between input wind models and ground TLs, our ML tool could be used to investigate the sensitivity of infrasound amplitudes with variations in wind models. Sensitivity kernels could be built using explanatory techniques such as Layer-wise Relevance Propagation (*Bach et al.*, 2015) which propagates the ML predictions backwards in the neural network to determine what part of the input data, i.e., wind model, was used to build a given output, i.e., TL. The construction of wind sensitivity kernels could then be employed to further constrain wind structures in infrasound-based wind inversions (*Vera Rodriguez et al.*, 2020). While we restricted our model to absolute TL predictions, i.e., predictions of the norm of the complex TL, both real and imaginary parts of the TL could be independently predicted. Predicting complex TL would enable one to reconstruct the full infrasound time series from any source time function input (e.g., *Arrowsmith et al.* (2012)).

AUTHOR CONTRIBUTIONS

Quentin Brissaud (QB) and Sven Peter Näsholm (SPN) initiated this work and elaborated the plan for the study. QB performed the wave propagation simulations and implemented the ML training and validation. Antoine Turquet (AT) implemented the Garder's model in Python. Alexis Le Pichon (ALP) generated the TL profiles using LP12 model (*Le Pichon et al.*, 2012) which are presented in Fig. 4. QB created the figures and visualizations, which were further elaborated in collaboration with all co-authors. QB wrote the initial manuscript draft and all co-authors contributed in review, revisions, and editing previous to submission.

ACKNOWLEDGMENTS

The authors would like to thank Alexander Binder, Associate Professor at the Department of Informatics, University of Oslo, for insightful discussion in the implementation and optimization of Convolutional Neural Networks and transfer learning. The authors are also grateful to Claus Hetzer, Research and Development Engineer at University of Mississippi, for providing details about the theoretical background behind the Parabolic Equations modelling software ePape.

This work was mainly funded from a NORSAR institute grant. It was also supported by the project *Middle Atmosphere Dynamics: Exploiting Infrasound Using a Multidisciplinary Approach at High Latitudes* (MADEIRA), funded by the Research Council of Norway basic research programme FRIPRO/FRINATEK under Contract No. 274377. This study was facilitated by previous research performed within the framework of the ARISE and ARISE2 projects (*Blanc et al.*, 2018, 2019), funded by the European Commission FP7 and Horizon 2020 programmes (Grant Nos. 284387 and 653980)

DATA AVAILABILITY STATEMENT

The ERA5 operational data were accessed from the ECMWF MARS archive using the Climate Data Store API (*ECMWF*, 2018), which is accessible to ECMWF Member and Co-operating States. We are grateful to the National Center for Physical Acoustics (NCPA) at the University of Mississippi for making the Parabolic Equation modelling tool ePape publicly available through GitHub at *Waxler et al.* (2021). The TensorFlow library for Python can be downloaded from the TensorFlow repository (`https://doi.org/10.5281/zenodo.4724125`). The ML model Python implementation, and the corresponding PE TL profiles will be released upon publication on a GitHub repository.

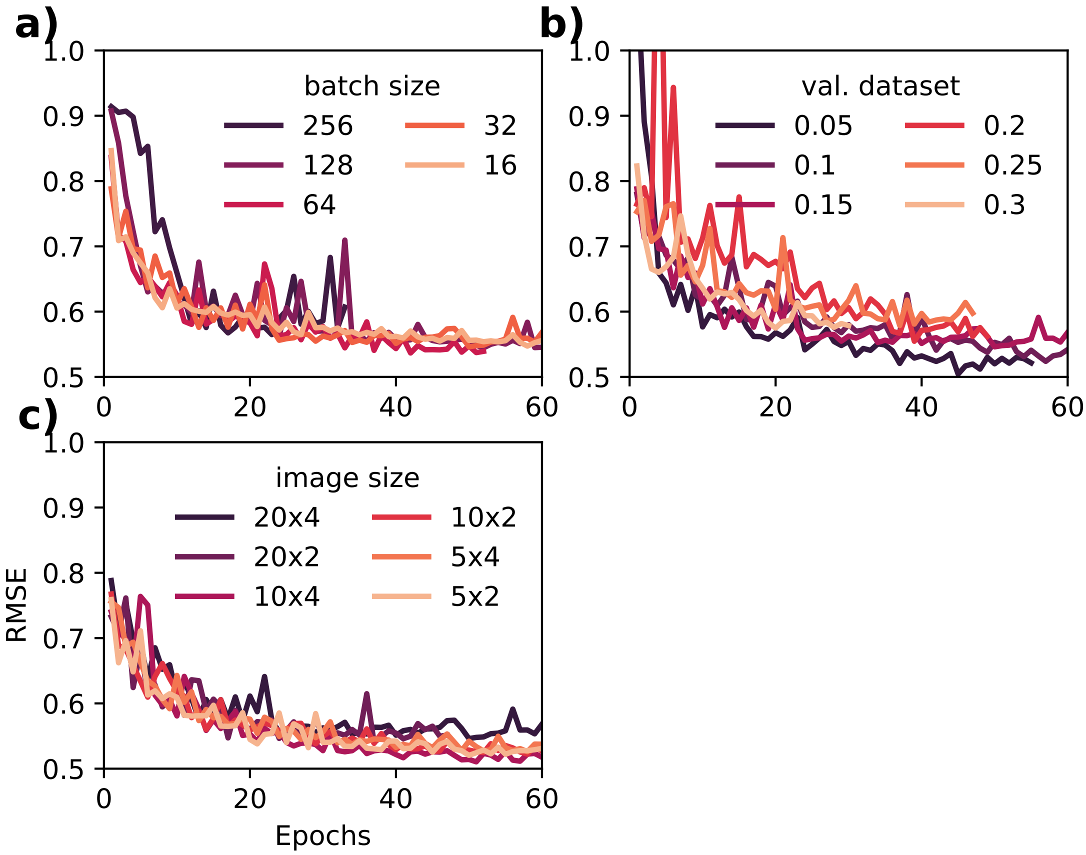

Figure 5. Optimization of training and input hyperparameters. RMSE vs epochs during training for variations in (a) batch size, (b) validation dataset size, and (c) input image size from a baseline model with: batch size 32, 15% validation dataset size, and 20×4 input size.

Appendix A: Hyper-parameter optimization

The ML model is described by a set of hyper-parameters that must be optimized in order to obtain the best regression performance. First, we optimized the ML architecture, i.e., the number of CNN and dense layers as well as number of CNN filters, using a Bayesian optimization with Gaussian Processes as implemented in the scikit-optimize Python library (*Head et al.*, 2021). In addition to architecture optimizations, we investigated the variations in RMSE with the choice of training parameters (batch size and validation dataset size) as well as inputs image size. Such variations are shown in Fig. 5. There are generally negligible error differences between each model. As a trade-off between training time and error we choose batches of size 32, a dataset of size 20%, and input images of size 20×4.

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