

# Recommendations for the Formulation of Grazing in Marine Biogeochemical and Ecosystem Models

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## Key Points:

- We provide a review of the derivation of the functional response equations, unified across all common response types and parameter schemes.
- Zooplankton grazing parameter values vary by 3 to 4 orders of magnitude with inconsistent allometric relationships, both in models and experiments.
- The apparent mean functional response, averaged across sufficient sub-grid scale heterogeneity, begins to resemble the shape and parameter sensitivity of a type III Michaelis-Menten response even when a local type II disk response is prescribed.
- We recommend a type II disk response in smaller scale, finer resolution models but a type III Michaelis-Menten response in larger scale, coarser resolution models.
- We recommend considering a wide range of  $K_{1/2}$  values, particularly low ones.

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## Abstract

For nearly a century, the functional response curves, which describe how predation rates vary with prey density, have been a mainstay of ecological modelling. While originally derived to describe terrestrial interactions, they have been adopted to characterize aquatic systems in marine biogeochemical, size-spectrum, and population models. However, marine ecological modellers disagree over the qualitative shape of the curve (e.g. Type II vs. III), whether its parameters should be mechanistically or empirically defined (e.g. disk vs. Michaelis-Menten scheme), and the most representative value of those parameters. As a case study, we focus on marine biogeochemical models, providing a comprehensive theoretical, empirical, and numerical road-map for interpreting, formulating, and parameterizing the functional response when used to prescribe zooplankton specific grazing rates on a single prey source. After providing a detailed derivation of each of the canonical functional response types explicitly for aquatic systems, we review the literature describing their parameterization. Empirical estimates of each parameter vary by over three orders of magnitude across 10 orders of magnitude in zooplankton size. However, the strength and direction of the allometric relationship between each parameter and size differs depending on the range of sizes being considered. In models, which must represent the mean state of different functional groups, size spectra or in many cases the entire ocean's zooplankton population, the range of parameter values is smaller, but still varies by two to three orders of magnitude. Next, we conduct a suite of 0-D NPZ simulations to isolate the sensitivity of phytoplankton population size and stability to the grazing formulation. We find that the disk parameterizations scheme is much less sensitive to its parameterization than the Michaelis-Menten scheme, and quantify the range of parameters over which the Type II response, long known to have destabilizing properties, introduces dynamic instabilities. Finally, we use a simple theoretical model to show how the mean apparent functional response, averaged across sufficient sub-grid scale heterogeneity diverges from the local response. Collectively, we recommend using a type II disk response for models with smaller scales and finer resolutions but suggest that a type III Michaelis-Menten response may do a better job of capturing the complexity of all processes being averaged across in larger scale and coarser resolution modal, not just local consumption and capture rates. While we focus specifically on the grazing formulation in marine biogeochemical models, we believe these recommendations are robust across a much broader range of ecosystem models.

## 1 Introduction

In the late 1950s, Buzz Holling began studying the predation of sawfly cocoons by small mammals (Holling, 1959a) to better understand how predation rates varied with prey density, a relationship coined a decade earlier as the functional response (Solomon, 1949). Holling observed that individual predators consumed more prey at higher prey densities, but found that this relationship was not necessarily linear or consistent across species. Over the course of three seminal papers, Holling went on to develop a theoretical framework to describe how different assumptions about the rates at which predators captured and consumed their prey could explain observed nonlinearities and variability in the shape of functional response curve (Holling, 1959a, 1959b, 1965). Using this mechanistic approach, Holling derived three qualitatively distinct response types to describe differences in predator-prey interactions and their associated rates. In the ensuing decades, these equations have been further generalized (Real, 1977, 1979) and cemented into the bedrock of ecological modelling (Beardsell et al., 2021; Denny, 2014).

Although the functional response was originally developed for terrestrial applications (Holling, 1959a), the equations are also common in marine ecological modelling (Evans & Parslow, 1985; Fasham, 1995; Franks, Wroblewski, & Flierl, 1986). In the ocean, the functional response equations are now routinely used to link trophic dynamics in marine biogeochemical (Law et al., 2017; Moore, Lindsay, Doney, Long, & Misumi, 2013),

76 size spectrum (Heneghan et al., 2020), and population models (Alver, Broch, Melle, Bagøien,  
77 & Slagstad, 2016). They are used to simulate both the rate at which heterotrophic zoo-  
78 plankton graze on autotrophic phytoplankton (Evans & Parslow, 1985; Franks et al., 1986)  
79 as well as the transfer of mass and energy further up the food chain in ecosystem (Buten-  
80 schön et al., 2016) and fisheries models (Maury, 2010; Tittensor et al., 2018, 2021).

81 However, there remains a great deal of uncertainty surrounding the formulation of  
82 the functional response. For example, trade offs between the ecological veracity and nu-  
83 merical stability of different response types (Gismervik, 2005; A. Morozov, 2010; A. Mo-  
84 rozov, Arashkevich, Reigstad, & Falk-Petersen, 2008) have led to disagreement over which  
85 is best suited for rapidly growing, easily excitable, microbial systems common in marine  
86 ecology (Fasham, 1995; Flynn & Mitra, 2016; Gentleman & Neuheimer, 2008). Even amongst  
87 mathematically identical curves, there is not a consensus on how to define their param-  
88 eters, no less prescribe them. While some modellers opt for a parameter scheme that mir-  
89 rors the Michaelis–Menten (Michaelis & Menten, 1913) and Monod (Monod, 1949) equa-  
90 tions developed to describe enzyme kinetics and bacterial growth rates (Aumont & Bopp,  
91 2006; Dutkiewicz et al., 2015; Moore et al., 2013; Vichi, Pinardi, & Masina, 2007), oth-  
92 ers use a parameter scheme that mirrors the disk equation (Holling, 1959b, 1965) devel-  
93 oped by Holling to describe terrestrial interactions (Fasham, 1995; Laws, Falkowski, Smith,  
94 Ducklow, & McCarthy, 2000; Oke et al., 2013; Schartau & Oschlies, 2003b). While the  
95 parameters used in the Michaelis–Menten scheme are overtly empirical, those used in the  
96 disk scheme are theoretically mechanistic. Disagreement over which parameter set to use  
97 can confuse inter-model comparisons and influence the parameter space considered in  
98 optimization schemes, especially if there are not robust observations to bound them.

99 Here, we focus on the formulation of grazing in marine biogeochemical models, which  
100 are a critical component of coupled climate models (Eyring et al., 2016; Flato et al., 2013;  
101 Taylor, Stouffer, & Meehl, 2012) and often used to drive fisheries models (Maury, 2010;  
102 Tittensor et al., 2018, 2021), but are increasingly under constrained and over parame-  
103 terized (Doney, 1999; Mearns, 1995; Schartau et al., 2017; Ward, Friedrichs, Anderson,  
104 & Oschlies, 2010). Accurately representing grazing is critical to both climate and fish-  
105 eries models, as it mediates the biological transport of carbon fixed via net primary pro-  
106 duction (Behrenfeld, Doney, Lima, Boss, & Siegel, 2013; Laufkötter et al., 2015) and trans-  
107 ported to higher trophic levels via secondary production (Brander, 2007; Scherrer et al.,  
108 2020). Still, despite the growing recognition that biogeochemical models are highly sen-  
109 sitive to the grazing formulation (Adjou, Bendtsen, & Richardson, 2012; Anderson, Gen-  
110 tleman, & Sinha, 2010; Chenillat, Rivière, & Ohman, 2021; Fasham, 1995; Flynn & Mi-  
111 tra, 2016; Fussmann & Blasius, 2005; Gentleman & Neuheimer, 2008; Gross, Ebenhöf,  
112 & Feudel, 2004), it remains challenging to constrain global zooplankton dynamics us-  
113 ing a limited number of simplified equations, state variables, and parameters. Most bio-  
114 geochemical models represent only 1-2 zooplankton functional groups, but parameters  
115 inferred empirically vary largely across zooplankton species, size and age (Hansen, Bjørn-  
116 sen, 1997; Hirst & Bunker, 2003). Allometric models can vary parameters across  
117 size class, but measured allometric relationships are not always robust (Hansen et al.,  
118 1997). Even once parameters are chosen, global simulations cannot be easily validated  
119 because we lack the required spatial resolution in observed distributions of zooplankton  
120 biomass and their associated grazing parameters (but see (Moriarty, Buitenhuis, Le Quéré,  
121 & Gosselin, 2013; Moriarty & O’Brien, 2012)). Moreover, the equations modellers must  
122 parameterize are empirical and theoretical oversimplifications and may not be adequate  
123 to represent the mean-state of diverse communities grazing in fundamentally different  
124 ways distributed heterogeneously across a patchy ocean.

125 Depending on the model, zooplankton diets range from a single generic phytoplankton  
126 to a complex portfolio of multiple phytoplankton, smaller zooplankton, and detri-  
127 tus. When multiple prey is available, the distribution of grazing across them is deter-  
128 mined by one of many multiple-prey response functions, which can take into account both

129 the relative distribution of prey options and their intrinsic desirability (Fasham, Duck-  
 130 low, & McKelvie, 1990). These equations, which are typically extensions of the single-  
 131 prey response functions, have been reviewed in detail by Gentleman, Leising, Frost, Strom,  
 132 and Murray (2003). Here, we focus on the single-prey response functions, which are a  
 133 prerequisite for understanding the multiple-prey response functions and often describe  
 134 their implied behavior when only one prey option is available. While many modern mod-  
 135 els use a multiple-prey response Aumont, Ethé, Tagliabue, Bopp, and Gehlen (2015); Stock  
 136 et al. (2020); Totterdell (2019); Yool et al. (2021), zooplankton grazing with a single-prey  
 137 response remains common in state-of-the-art many CMIP6-class global climate models  
 138 (Christian et al., 2021; Hajima et al., 2020; Law et al., 2017; Long et al., 2021; Tjipu-  
 139 tra et al., 2020)

140 By combining theory, empirical data, and numerical models, we consolidate a com-  
 141 prehensive guide to how the single-prey functional response is employed in marine eco-  
 142 logical models to represent grazing. We begin by presenting a unified review of how each  
 143 functional response and its associated parameter schemes are derived, providing detailed  
 144 insights into how they relate to each other and first principles (**Section 2**). Next we re-  
 145 view the mathematical influence of different grazing formulations on population stabil-  
 146 ity (**Section 3**) and survey the literature to assess the range of parameter values that  
 147 have been estimated empirically and used prescriptively in models (**Section 4**). Then  
 148 we conduct a suite of simulations to isolate the sensitivity of phytoplankton population  
 149 size and stability to the parameterization of the functional response using four different  
 150 combinations of response type (i.e. II vs. III) and parameter scheme (i.e. disk vs. Michaelis-  
 151 Menten) (**Section 5**). Finally, we use a simple theoretical model to examine the influ-  
 152 ence of sub-grid scale heterogeneity on the shape of the functional response (**Section**  
 153 **6**). We conclude with a set recommendations for the formulation of grazing based on the  
 154 evidence presented (**Section 7**). These recommendations are tailored to the single-prey  
 155 representation of grazing in marine biogeochemical models, but are broadly applicable  
 156 to much wider usage of the functional response across marine and terrestrial applications.

## 157 2 Derivation of the grazing formulation

158 The rate at which prey is grazed by zooplankton is generally expressed as the graz-  
 159 ing rate ( $G$ ) in units of prey concentration lost per unit time (e.g.  $\frac{mmolC}{m^3d}$ ). Here, we gen-  
 160 erally refer to prey as phytoplankton, but all results are relevant to grazing on any generic  
 161 single prey (e.g. bacteria, detritus, or carnivory on other zooplankton). The grazing rate  
 162 is equal to the product of the ambient zooplankton concentration,  $[Z]$ , and the zooplank-  
 163 ton specific grazing rate ( $g$ ), often referred to as the ingestion rate (Franks et al., 1986;  
 164 Gentleman & Neuheimer, 2008), which describes the concentration of phytoplankton grazed  
 165 per unit zooplankton per unit time, reducing to units of one over time (e.g.  $1/d$ ), such  
 166 that

$$G = g[Z] \tag{1}$$

167 To account for the intuitive fact that grazing is less successful when phytoplank-  
 168 ton are scarce, the zooplankton specific grazing rate,  $g$ , must vary with the ambient phy-  
 169 toplankton concentration,  $[P]$ , particularly when  $[P]$  is low. The mathematical formula  
 170 that describes these relationships is known as the functional response.

171 Buzz Holling originally derived the functional response by assuming there was a  
 172 fixed time interval,  $T$ , over which predator and prey were exposed (e.g. same location,  
 173 same time, predator is awake), and that predators were assumed to exclusively be cap-  
 174 turing (e.g. searching, encountering, hunting, attacking) ( $T_{cap}$ ) or consuming (e.g. killing,  
 175 handling, processing, eating, digesting) prey ( $T_{con}$ ) during this interval (Holling, 1959a),  
 176 such that

$$T = T_{cap} + T_{con}. \quad (2)$$

177 The canonical type I, II, and III functional responses (**Fig. 1a**) were consequently  
 178 derived (**Fig. 1b**) from different assumptions (**Fig. 1c**) about the efficiency of the cap-  
 179 ture and consumption processes, the associated total time needed to capture and con-  
 180 sume a given amount of prey, and how those rates and times vary with prey density (see  
 181 **Table 1** for a catalogue of terms). However, prey density was originally expressed in dis-  
 182 crete units of prey over a given circular area (or disk). Here, we instead provide a deriva-  
 183 tion of the type I (**Section 2.2**), II (**Section 2.3**), and III (**Section 2.4**) responses ex-  
 184 plicitly for aquatic systems, with example units of carbon biomass per meter cubed ( $mmolC/m^3$ )  
 185 for phytoplankton and zooplankton concentrations and days ( $d$ ) for time. Further, we  
 186 show how each functional response can be described by two sets of parameters: the disk  
 187 scheme in which the consumption and capture processes are explicitly prescribed and  
 188 mechanistically defined, and the Michaelis-Menten scheme, in which the maximum graz-  
 189 ing rate and half saturation concentration of the curve are explicitly prescribed and em-  
 190 pirically defined. Note, many of these equations have been derived in various forms and  
 191 various contexts before (Aksnes & EGGE, 1991; Caperon, 1967). Here, we present them  
 192 together, specifically in the context of zooplankton grazing, with careful attention to how  
 193 they relate theoretically and mathematically to each other and first principles.

194 For each derivation, consider some concentration of phytoplankton,  $[P_G]$  ( $mmolC/m^3$ ),  
 195 that is grazed (i.e. captured and consumed) by the ambient zooplankton population,  $[Z]$   
 196 ( $mmolC/m^3$ ), over the fixed grazing (or exposure) interval,  $T$  ( $d$ ), at a grazing rate of  
 197  $G = \frac{[P_G]}{T}$  and a zooplankton specific (i.e. considering the amount of predator present)  
 198 grazing rate of  $g = \frac{[P_G]}{[Z]T}$ . To derive each functional response type,  $g([P])$ , we must solve  
 199 for  $g$  ( $1/d$ ) in terms of the ambient phytoplankton population,  $[P]$  ( $mmolC/m^3$ ), con-  
 200 sidering their respective assumptions regarding capture and consumption rates.

## 201 2.1 Type 0 response

202 A type 0 functional response is described by a straight horizontal line in which a  
 203 zooplankton specific grazing rate is invariant to the ambient phytoplankton population  
 204 ( $g([P]) = constant$ , **Fig. 1**; magenta). A type 0 response is not ecologically realistic  
 205 for any species, nor does it appear in any models, but for pedagogical purposes assumes  
 206 that the capture process is unaffected by prey scarcity and that the consumption pro-  
 207 cess is negligible.

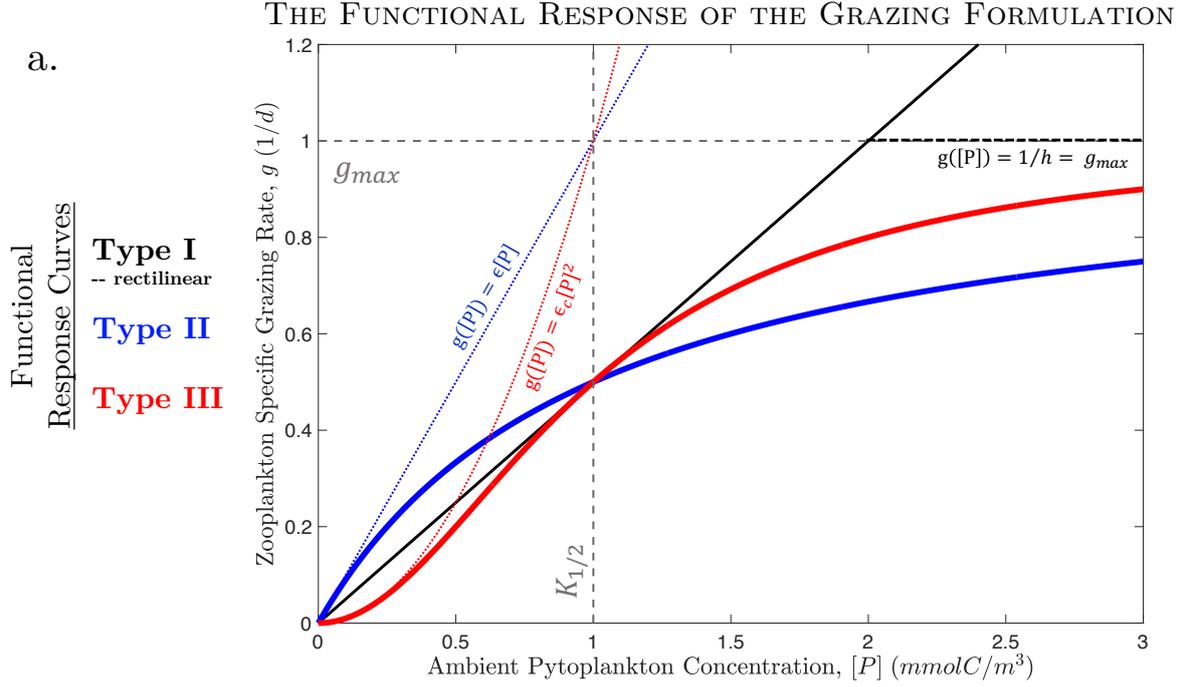
## 208 2.2 Type I response

209 A type I functional response is described by a straight line (Holling, 1959b), in which  
 210 the zooplankton specific grazing rate ( $g([P])$ ) increases linearly with the ambient phy-  
 211 toplankton concentration (**See Fig. 1**; black). Ecologically, a type I response assumes  
 212 that zooplankton capture prey faster when it is more abundant and that the time needed  
 213 to consume it is negligible compared with the time needed to capture it ( $T_{cap} \gg T_{con}$ ).  
 214 Accordingly, zooplankton can spend all of their time capturing prey, such that

$$T = T_{cap}. \quad (3)$$

215 The time,  $T_{cap}$  ( $d$ ), that it takes to capture some concentration of phytoplankton,  
 216  $[P_{Cap}]$  ( $mmolC/m^3$ ), can be related to the capture rate,  $C$  ( $\frac{mmolC/m^3}{d}$ ), or the concen-  
 217 tration of phytoplankton captured per unit time, by the equation

$$T_{cap} = \frac{[P_{Cap}]}{C}, \quad (4)$$



b.

	<b>Type I</b>	<b>Type II</b>	<b>Type III</b>
Capture Rate	$E = \epsilon[P]$	$E = \epsilon[P]$	$E = \epsilon[P] = \epsilon_c[P]^2$
Theoretical Assumptions	<b>Zooplankton</b> capture prey easier (faster) when there is more.	<b>Zooplankton</b> capture prey easier (faster) when there is more.	<b>Zooplankton</b> learn to be more efficient hunters when exposed to more prey.
Consumption Time	$h = 0$	$h = 1/g_{max}$	$h = 1/g_{max}$
Theoretical Assumptions	<b>Zooplankton</b> take no time consuming prey and spend all their time capturing.	<b>Zooplankton</b> spend a fixed amount of time consuming each phytoplankton.	<b>Zooplankton</b> spend a fixed amount of time consuming each phytoplankton.
Mass Balance of Time (for derivation)	$T = \frac{[P_G]}{\epsilon[P][Z]} + 0$	$T = \frac{[P_G]}{\epsilon_c[P][Z]} + \frac{h[P_G]}{[Z]}$	$T = \frac{[P_G]}{\epsilon_c[P]^2[Z]} + \frac{h[P_G]}{[Z]}$
<b>Disk Formulation</b>	$g = \epsilon[P]; \quad [P] < \frac{g_{max}}{\epsilon}$ $g = g_{max}; \quad [P] > \frac{g_{max}}{\epsilon}$	$g = \frac{g_{max}\epsilon[P]}{g_{max} + \epsilon[P]}$	$g = \frac{g_{max}\epsilon_c[P]^2}{g_{max} + \epsilon_c[P]^2}$
<b>Michaelis-Menten Formulation</b>	$g = \frac{g_{max}}{2K_{1/2}} [P]; \quad [P] < 2K_{1/2}$ $g = g_{max}; \quad [P] > 2K_{1/2}$	$g = \frac{g_{max}[P]}{K_{1/2} + [P]}$	$g = \frac{g_{max}[P]^2}{K_{1/2}^2 + [P]^2}$
Parameter Relationship	$\epsilon = g_{max}/2K_{1/2}$	$\epsilon = g_{max}/K_{1/2}$	$\epsilon_c = g_{max}/K_{1/2}^2$

**Figure 1.** The functional response of the grazing formulation. **a)** The zooplankton specific grazing rate (or ingestion rate) as a function of prey density, known as the the functional response curve is plotted for a type I, II, and III response, along with **b)** a description their associated attributes, assumptions, and formulations. Each response type is parameterized such that the maximum specific grazing rate,  $g_{max}$ , and the half saturation concentration,  $K_{1/2}$  are equal to one. Note, this requires different parameters for the disk parameter scheme. Dashed lines in **a)** show what each response reduces to a low and high prey densities.

Variable	Notation	Conceptual Units	Reduced Units	Relevant Relationships	Description
Phytoplankton concentrations	$[P], [P_G], [P_{Cap}], [P_{Con}]$	$[P]$	$\frac{mmolC}{m^3}$	$[P_G] = GT = g[Z]T$ $[P_G] = [P_{Cap}] = [P_{Con}]$	Concentration of ambient, grazed (i.e. captured and consumed), captured, and consumed phytoplankton over the exposure period, respectively
Zooplankton concentration	$[Z]$	$[Z]$	$\frac{mmolC}{m^3}$	-	Concentration of Zooplankton biomass
Functional response	$g([P])$	$\frac{[P]}{[Z]time}$	$\frac{1}{d}$	$g([P]) = \epsilon[P]$ (I) $= \frac{g_{max}}{2K_{1/2}}[P]$ (I-Rect) $g([P]) = \frac{g_{max}\epsilon[P]}{g_{max} + \epsilon[P]}$ (II) $= \frac{g_{max}[P]}{K_{1/2} + [P]}$ $g([P]) = g_{max}(1 - e^{-\lambda[P]})$ (II-IV) $g([P]) = \frac{g_{max}\epsilon_c[P]^2}{g_{max} + \epsilon_c[P]^2}$ (III) $= \frac{g_{max}[P]^2}{K_{1/2}^2 + [P]^2}$	Functional description of how the zooplankton specific grazing rate varies with the phytoplankton concentration
Half saturation concentration	$K_{1/2}$	$[P]$	$\frac{mmolC}{m^3}$	$K_{1/2} = \frac{g_{max}}{2\epsilon}$ (II-R) $K_{1/2} = \frac{g_{max}}{\epsilon}$ (II) $K_{1/2} = \frac{\epsilon}{-\ln(0.5)}$ (II-IV) $K_{1/2} = \sqrt{\frac{g_{max}}{\epsilon_c}}$ (III)	Phytoplankton concentration where $g = \frac{g_{max}}{2}$
Maximum grazing rate	$g_{max}$	$\frac{[P]}{[Z]time}$	$\frac{1}{d}$	$g_{max} = \frac{1}{h}$	Rate of phytoplankton consumption per unit zooplankton when food is replete
Grazing rate	$G$	$\frac{[P]}{time}$	$\frac{mmolC}{m^3d}$	$G = \frac{[P_G]}{T}$ $G = g[Z]$	Rate at which phytoplankton are grazed by the zooplankton population
Phytoplankton specific grazing loss rate	$l$	$\frac{[P]}{[P]time}$	$\frac{1}{d}$	$l = \frac{G}{[P]}$	Phytoplankton specific rate at which phytoplankton are lost to grazing
Zooplankton specific grazing rate (i.e. ingestion rate)	$g$	$\frac{[P]}{[Z]time}$	$\frac{1}{d}$	$g = \frac{G}{[Z]}$	Zooplankton specific rate at which phytoplankton are grazed. The way in which $g$ varies with $[P]$ is the functional response
Clearance rate	$Cl$	$\frac{[P]}{[P][Z]time}$	$\frac{m^3}{mmolCd}$	$Cl = \frac{G}{[P][Z]}$ $Cl = \frac{g}{[P]}$	Phytoplankton specific rate at which phytoplankton are grazed per unit zooplankton
Exposure period	$T$	$time$	$d$	$T = T_{cap} + T_{con}$	Fixed period over which zooplankton and phytoplankton are exposed
Capture period	$T_{cap}$	$time$	$d$	$T_{cap} = \frac{[P_G]}{[Z]\epsilon[P]}$	Time spent capturing phytoplankton
Consumption period	$T_{con}$	$time$	$d$	$T_{con} = 0$ (I) $T_{con} = \frac{h[P_G]}{[Z]}$ (II,III)	Time spent consuming phytoplankton
Capture rate	$C$	$\frac{[P]}{time}$	$\frac{mmolC}{m^3d}$	$C = \frac{[P_{cap}]}{T_{cap}}$ $C = E[Z]$ (II) $C = \epsilon_c[Z]^2$ (III)	Rate at which phytoplankton are captured by the zooplankton population
Zooplankton specific capture rate	$E$	$\frac{[P]}{[Z]time}$	$\frac{1}{d}$	$E = \frac{C}{[Z]}$ $E = \epsilon[P]$	Specific rate at which phytoplankton are captured per unit zooplankton
Prey capture efficiency	$\epsilon$	$\frac{[P]}{[P][Z]time}$	$\frac{m^3}{mmolCd}$	$\epsilon = \epsilon_c[P]$ (III) $\epsilon = \lambda g_{max}$ (II-IV)	Rate at which the zooplankton specific capture rate increases with the ambient phytoplankton concentration
Prey capture efficiency coefficient	$\epsilon_c$	$\frac{[P]}{[P]^2[Z]time}$	$\frac{m^6}{mmolC^2d}$	-	Rate at which the prey capture efficiency increases with the ambient phytoplankton concentration
Consumption time	$h$	$\frac{[Z]time}{[P]}$	$d$	-	Time it takes for one unit of zooplankton to eat one unit of phytoplankton
Consumption rate	$\frac{1}{h}$	$\frac{[P]}{[Z]time}$	$\frac{1}{d}$	-	Rate of phytoplankton consumption per unit zooplankton
Ivlev parameter	$\lambda$	$\frac{1}{[P]}$	$\frac{m^3}{mmolCd}$	-	Used to parameterize Ivlev equation which is qualitatively similar to a type II

**Table 1.** List of terms relevant to the derivation, parameterization and context of the functional response. Conceptual units distinguish between phytoplankton and zooplankton concentration and are not reduced.

218 The capture rate can then be decomposed into the product of the ambient zooplank-  
 219 ton concentration,  $[Z]$  ( $mmolC/m^3$ ), and the zooplankton specific capture rate,  $E$  ( $1/d$ ),  
 220 which describes the concentration of phytoplankton captured per unit zooplankton per  
 221 unit time, such that

$$C = E[Z]. \quad (5)$$

222 Depending on the zooplankton in question, the zooplankton specific capture rate,  
 223  $E$  ( $1/d$ ), can represent a passive encounter rate (e.g. filter feeding) or an active search  
 224 and attack rate (e.g. hunting), but does not include the time required to consume phy-  
 225 toplankton once captured. Either way,  $E$  ( $1/d$ ) is assumed to increase linearly with the  
 226 ambient phytoplankton concentration,  $[P]$  ( $mmolC/m^3$ ), to account for the fact that zoo-  
 227 plankton are stochastically more likely to encounter and capture phytoplankton at higher  
 228 ambient phytoplankton concentrations. The rate (per unit phytoplankton) at which the  
 229 zooplankton specific capture rate increases with the ambient phytoplankton concentra-  
 230 tion can be considered the prey capture efficiency,  $\epsilon$  ( $\frac{1}{(mmolC/m^3)d}$ ), such that

$$E = \epsilon[P]. \quad (6)$$

231 The prey capture efficiency can be thought of as the fraction of the ambient phytoplank-  
 232 ton concentration captured per unit zooplankton per unit time, in which units of  $\frac{(mmolC/m^3)}{(mmolC/m^3)^2d}$   
 233 reduce to  $\frac{1}{(mmolC/m^3)d}$ , and reflects the efficiency with zooplankton can capture the prey  
 234 they are exposed to. Note that the prey capture efficiency is variously referred to as the  
 235 prey capture rate (Schartau & Oschlies, 2003b), attack rate (Gentleman & Neuheimer,  
 236 2008), affinity, and maximum clearance rate. It is also qualitatively similar to the search  
 237 area defined by Holling (1959b), but not identical for concentration-based rates.

238 Substituting **eqs. 5 & 6** into **eq. 4** yields,

$$T_{cap} = \frac{[P_{Cap}]}{\epsilon[P][Z]}. \quad (7)$$

239 Next, we can substitute  $T_{cap}$  for  $T$  because of our assumption that no time is needed  
 240 for zooplankton to consume phytoplankton (i.e.  $T_{con} = 0$ ), and substitute  $[P_{Cap}]$  for  
 241  $[P_G]$  because the entire concentration of phytoplankton lost to grazing,  $[P_G]$ , must first  
 242 be captured,  $[P_{Cap}]$ . Finally, we solve for the rate at which phytoplankton are grazed  
 243 by the zooplankton population ( $G = gZ = \frac{[P_G]}{T}$ ) as a function of  $[P]$ ,

$$G([P]) = \frac{[P_G]}{T} = \epsilon[P][Z], \quad (8)$$

244 and divide by  $[Z]$  to yield the zooplankton specific grazing rate,  $g$  ( $1/d$ ), as a function  
 245 of the ambient phytoplankton concentration  $[P]$ , such that,

$$g([P]) = \frac{[P_G]}{T[Z]} = \epsilon[P]. \quad (9)$$

246 With **eq. 9** we have arrived at the type I functional response, wherein  $g([P])$  in-  
 247 creases linearly with the ambient phytoplankton concentration,  $[P]$ , at a rate described  
 248 by the prey capture efficiency,  $\epsilon$ . This type of response is akin to a food-limited system  
 249 in which it takes much longer to find and capture prey than it takes to consume it, and  
 250 is analogous to the classic Lotka-Volterra equations (Lotka, 1910; Volterra, 1927) used  
 251 to describe simple predator-prey dynamics. Note that here the grazing rate is identical

252 to the capture rate ( $G = C$ ) and the zooplankton specific grazing rate is identical to  
 253 the zooplankton specific capture rate ( $g = E = \epsilon[P]$ ). This is because the entire graz-  
 254 ing process is assumed to be described by the capture process; however, this is not the  
 255 case for higher order functional responses, in which zooplankton are assumed to spend  
 256 a non-trivial amount of time consuming phytoplankton in addition to capturing them.

257 A standard type I response may be characteristic of passive filter feeders (Jeschke,  
 258 Kopp, & Tollrian, 2004), but can overestimate the zooplankton specific grazing rate of  
 259 mesozooplankton such as copepods (Gentleman & Neuheimer, 2008) by over an order  
 260 of magnitude compared to observations (Frost, 1972; Hansen et al., 1997) because it does  
 261 not account for predator satiation at high prey densities. To account for predator sati-  
 262 ation, the type I response can be extended to a rectilinear response (Chen, Laws, Liu,  
 263 & Huang, 2014; Frost, 1972; Hansen, Bjørnsen, & Hansen, 2014; Mayzaud, Tirelli, Bernard,  
 264 & Roche-Mayzaud, 1998), in which  $g([P])$  reaches some maximum rate,  $g_{max}$  ( $d^{-1}$ ) such  
 265 that

$$\begin{aligned} g([P]) &= \epsilon[P] & \text{if } [P] < \frac{g_{max}}{\epsilon} \\ g([P]) &= g_{max} & \text{if } [P] > \frac{g_{max}}{\epsilon}, \end{aligned} \quad (10)$$

266 where  $\frac{g_{max}}{\epsilon}$  ( $\frac{mmolC}{m^3}$ ) describes the prey concentration required to reach the maximum  
 267 zooplankton specific grazing rate,  $g_{max}$ , for a given prey capture efficiency,  $\epsilon$ .

268 Solving for  $[P]$  when  $g([P]) = \frac{g_{max}}{2}$  returns the half saturation concentration,  $K_{1/2} =$   
 269  $\frac{g_{max}}{2\epsilon}$ . Note that parameterizing **eq. 10** with  $K_{1/2}$  allows one to explicitly define the lo-  
 270 cation of satiation using a single variable (as opposed to  $\frac{g_{max}}{2\epsilon}$ ); however, changing  $K_{1/2}$   
 271 with a fixed  $g_{max}$  necessarily alters the slope of the response,  $\epsilon$ , and therefor implicitly  
 272 alters assumptions about the prey capture efficiency.

### 273 2.3 Type II response

274 A type II functional response assumes a more gradual transition to satiation by em-  
 275 ploying a rectangular hyperbola with downward concavity (Holling, 1959b), in which the  
 276 zooplankton specific grazing rate ( $g([P])$ ) saturates towards a maximum asymptote at  
 277 high phytoplankton concentrations (**See Fig. 1**; blue). Ecologically, a type II response  
 278 assumes that zooplankton capture prey faster when it is more abundant and that a fixed,  
 279 non-trivial, amount of time is needed to consume it ( $T_{con} > 0$ ), allowing for gradual  
 280 predator satiation as the prey density increases and more time is needed to consume all  
 281 of it (Jeschke et al., 2004). Note, all assumptions about the capture process and zooplank-  
 282 ton specific capture rate ( $E = \epsilon[P]$ ) from the type I response are held.

283 The time it takes to consume the captured phytoplankton is parameterized by the  
 284 consumption time,  $h$  ( $d$ ), also commonly referred to as the handling time (Holling, 1959b,  
 285 1965), which is assumed to be equal to the fixed amount of time it takes for one unit of  
 286 zooplankton to eat one unit of phytoplankton. The total time,  $T_{con}$  ( $d$ ), needed for con-  
 287 sumption of the entire captured phytoplankton concentration,  $[P_{Cap}]$  ( $mmolC/m^3$ ), by  
 288 the ambient zooplankton concentration,  $[Z]$  ( $mmolC/m^3$ ), can then be expressed as the  
 289 consumption time,  $h$ , multiplied by the ratio of the concentration of phytoplankton cap-  
 290 tured relative to the ambient concentration of zooplankton capturing them ( $\frac{[P_{Cap}]}{[Z]}$ ), such  
 291 that

$$T_{con} = \frac{h[P_{Cap}]}{[Z]}. \quad (11)$$

292 Remembering that all phytoplankton grazed must first be captured (i.e.  $[P_G] = [P_{Cap}]$ )  
 293 and substituting  $T_{cap}$  and  $T_{con}$  into **eq. 2** yields

$$T = T_{cap} + T_{con} = \frac{[P_G]}{\epsilon[P][Z]} + \frac{h[P_G]}{[Z]}. \quad (12)$$

294 Solving for the concentration of phytoplankton lost to grazing,  $[P_G]$ , yields the aquatic  
 295 analogue to familiar disk equation, originally derived by Holling (1959b) for terrestrial  
 296 predation on a planar disk,

$$[P_G] = \frac{\epsilon[P][Z]T}{1 + \epsilon h[P]}, \quad (13)$$

297 where dividing by  $T$  returns the grazing rate,

$$G = \frac{[P_G]}{T} = \frac{\epsilon[P][Z]}{1 + \epsilon h[P]}, \quad (14)$$

298 and dividing again by  $Z$  returns the zooplankton specific grazing rate, which is equiv-  
 299 alent to the type II functional response,

$$g([P]) = \frac{[P_G]}{[Z]T} = \frac{\epsilon[P]}{1 + \epsilon h[P]}. \quad (15)$$

300 Note that by factoring out  $\epsilon[P]$  from the denominator and rearranging **eq. 15** as

$$g([P]) = \frac{1}{\frac{1}{\epsilon[P]} + h}, \quad (16)$$

301 it becomes clear that when food is limiting the type II disk equation reduces to a type  
 302 I linear Lotka-Volterra functional response with a slope equal to the prey capture efficiency  
 303 (**Fig. 1a**; dashed blue line). If the consumption rate ( $\frac{1}{h}$ ) is much faster than the zoo-  
 304 plankton specific capture rate ( $E = \epsilon[P]$ ), such that  $\frac{1}{h} \gg \epsilon[P]$  or equivalently  $h \ll$   
 305  $\frac{1}{\epsilon[P]}$ , then **eqs. 15 & 16** reduce to  $g([P]) = \epsilon[P]$  (i.e. **eq. 9**). This occurs when the  
 306 consumption time,  $h$ , is very fast (i.e. type I, **Section 2.1.1**), or the phytoplankton con-  
 307 centration,  $[P]$ , is very low (i.e. a food-limited system). The slope of the

308 Alternatively, we see that **eqs. 15 & 16** saturate towards  $g([P]) = 1/h$  when the  
 309 consumption rate ( $\frac{1}{h}$ ) is much slower than the zooplankton specific capture rate ( $E =$   
 310  $\epsilon[P]$ ), such that  $\frac{1}{h} \ll \epsilon[P]$  or equivalently  $h \gg \frac{1}{\epsilon[P]}$  (**Fig. 1a**; dashed black line).  
 311 This is typical of a food replete system (high  $[P]$ ), where more food is captured as soon  
 312 as the previous prey item has been consumed. The maximum grazing rate,  $g_{max}$  ( $1/d$ ),  
 313 can now be defined by the consumption rate, or one over the consumption time, such  
 314 that  $g_{max} = \frac{1}{h}$ . Note, however,  $g_{max}$  is approached slowly in a type II response, and  
 315  $g([P])$  is still only 80% of  $g_{max}$  even when  $[P] > 4K_{1/2}$ .

316 The disk equation (**eq. 13**) can be simplified by substituting the parameter  $g_{max} =$   
 317  $\frac{1}{h}$  into **eq. 15** and multiplying by  $\frac{g_{max}}{g_{max}}$  to arrive at

$$\begin{aligned} & \text{Type II (disk)} \\ g([P]) &= \frac{g_{max}\epsilon[P]}{g_{max} + \epsilon[P]} \end{aligned} \quad (17)$$

318 Henceforth, this will be referred to as the disk parameter scheme. Note, the formulation  
 319 of the disk equation used here differs from the traditional form (**eq. 14**) because we re-  
 320 placed the handling time with its reciprocal ( $g_{max}$ )

321 Finally, **eq. 17** can be rewritten as the familiar Michaelis–Menten equation origi-  
 322 nally derived for enzyme kinetics (Michaelis & Menten, 1913) (or Monod equation de-  
 323 rived for bacterial growth (Monod, 1949)) by defining the half-saturation concentration,  
 324  $K_{1/2}$  ( $mmolC/m^3$ ), in terms of parameters  $g_{max}$  and  $\epsilon$ . Setting  $g([P]) = \frac{g_{max}}{2}$  and solv-  
 325 ing for  $[P]$ , we find,

$$[P] = K_{1/2} = \frac{g_{max}}{\epsilon}. \quad (18)$$

326 Substituting  $\epsilon = \frac{g_{max}}{K_{1/2}}$  into **eq. 17** and rearranging yields the familiar form,

### Type II (Michaelis–Menten)

$$g([P]) = \frac{g_{max}[P]}{K_{1/2} + [P]}. \quad (19)$$

327 Henceforth, this will be referred to as the Michaelis–Menten parameter scheme. Note,  
 328 that in the Michaelis–Menten formulation  $g([P])$  still reduces to  $g_{max}$ , or  $\frac{1}{h}$ , when  $[P] \gg$   
 329  $K_{1/2}$  and to  $\frac{g_{max}}{K_{1/2}}$ , or (**eq. 18**), when  $[P] \ll K_{1/2}$ .

330 **Eq. 19** is mathematically identical to **eq. 17**. That is, for all parameter sets  $\{g_{max}, \epsilon\}$ ,  
 331 there exists a parameter set  $\{g_{max}, K_{1/2}\}$  that can identically describe  $g([P])$ . As with  
 332 the type I response (**eq. 10**), the difference is that  $\{g_{max}, \epsilon\}$  are ecologically indepen-  
 333 dent, while  $\{g_{max}, K_{1/2}\}$  more directly define the shape of the curve. For example, in-  
 334 creasing  $g_{max}$  in **eq. 17** does not affect the prey capture efficiency,  $\epsilon$ , but it does increase  
 335 the half-saturation concentration. This makes sense ecologically, as it should require a  
 336 higher phytoplankton concentration for a faster consumption time (i.e. higher  $g_{max}$ ) to  
 337 become limiting, given a constant prey capture efficiency. On the other hand, increas-  
 338 ing  $g_{max}$  in **eq. 19** does not change the location of  $K_{1/2}$ , but implicitly assumes that  
 339 the prey capture efficiency,  $\epsilon$ , increases in order to maintain a constant  $K_{1/2}$ .

340 Note, another common formulation that is qualitatively similar to the type II re-  
 341 sponse is the Ivlev equation (Ivlev, 1961), where

$$g([P]) = g_{max}(1 - e^{-\lambda[P]}) \quad (20)$$

342 (Anderson et al., 2010; C. A. Edwards, Batchelder, & Powell, 2000; Franks & Chen, 2001;  
 343 Shigemitsu et al., 2012). However, the Ivlev formulation is strictly empirical and can-  
 344 not be derived mechanistically, but is qualitatively similar to the type II response (**See**  
 345 **Fig. 1a**; cyan). All else being equal, the Ivlev equation will yield slower grazing rates  
 346 below the half saturation concentration and faster grazing rates above the half satura-  
 347 tion concentration. As noted elsewhere (Aldebert & Stouffer, 2018; Anderson et al., 2010;  
 348 Gentleman et al., 2003), the half saturation point and prey capture efficiency can be re-  
 349 lated to the Ivlev parameter,  $\lambda$  ( $\frac{1}{mmolC/m^3}$ ), as

$$K_{1/2} = \frac{-\ln(.5)}{\lambda} \quad (21)$$

$$\epsilon = \lambda g_{max}$$

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## 2.4 Type III response

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A type III functional response is described by a sigmoidal curve (Jeschke et al., 2004), in which the zooplankton specific grazing rate ( $g([P])$ ) increases quadratically at low phytoplankton concentrations and approaches saturation much faster at high ones (**Fig. 1**; red). Ecologically, a type III response further assumes that the prey capture efficiency,  $\epsilon$  ( $\frac{1}{(\text{mmolC}/\text{m}^3)d}$ ), increases with prey density. That is, the zooplankton specific capture rate,  $E = \epsilon[P]$ , does not just increase due to a stochastic increase in the likelihood of encountering phytoplankton as the ambient phytoplankton concentration increases, but zooplankton additionally become more efficient grazers as well, capturing an increasing fraction of the ambient phytoplankton concentration. Consequently, specific grazing rates increases quadratically at low  $[P]$  and approach saturation much faster than at high  $[P]$

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Mathematically, this change in behavior can be represented by assuming the prey capture efficiency,  $\epsilon$  ( $\frac{1}{(\text{mmolC}/\text{m}^3)d}$ ), is a function of the ambient phytoplankton concentration,  $[P]$ . In a type III response this function is assumed to be linearly proportional to some prey capture efficiency coefficient,  $\epsilon_c$  ( $\frac{1}{(\text{mmolC}/\text{m}^3)^2d}$ ), such that,

$$\epsilon = \epsilon_c[P], \quad (22)$$

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and

$$E = \epsilon_c[P]^2. \quad (23)$$

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By assuming that the prey capture efficiency,  $\epsilon$ , increases linearly with the phytoplankton concentration at a rate described by the prey capture efficiency coefficient,  $\epsilon_c$ , we are in turn assuming that the zooplankton specific grazing rate,  $E$ , increases quadratically with the phytoplankton population (i.e.  $E = \epsilon_c[P]^2$ ). Note that higher order functional responses can be achieved by modifying the relationship between the prey capture efficiency and the phytoplankton concentration (e.g.  $\epsilon = \epsilon_c[P]^2$ ).

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Following the same derivation as **Section 2.3**, but now using **eq. 23** instead of **eq. 6** to define the specific capture rate, yields the disk parameterization of the type III functional response,

### Type III (disk)

$$g([P]) = \frac{g_{max}\epsilon_c[P]^2}{g_{max} + \epsilon_c[P]^2}. \quad (24)$$

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As for the type II response,  $g([P])$  reduces to the zooplankton specific capture rate ( $E = \epsilon_c[P]^2$ ) at low phytoplankton densities (**Fig. 1a**; dashed red line) and saturates towards the consumption rate ( $1/h$ ) at high phytoplankton densities (**Fig. 1a**; dashed black line). Now, however, because the zooplankton specific capture rate,  $E$ , is described by a quadratic function of  $[P]$ , the functional response,  $g(P)$ , is sigmoidal in shape (**Fig. 1a**).

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The prey capture efficiency,  $\epsilon$ , in **eq. 17** has been replaced with the prey capture efficiency coefficient,  $\epsilon_c$ , in **eq. 24**, which describes how  $\epsilon$  varies with  $[P]$ . Units of  $\epsilon_c$  are non-intuitive, but can be considered as the fraction of the phytoplankton population captured per unit zooplankton, per unit phytoplankton, per unit time, which reduces to  $\frac{1}{(\text{mmolC}/\text{m}^3)^2d}$ .

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Finally, following identical logic to the type II response, **eq. 24** can be transformed to the Michaelis–Menten function by setting  $g([P])$  equal to  $\frac{g_{max}}{2}$ , solving for  $[P]$  to find  $K_{1/2}$ , and substituting the ensuing value of  $K_{1/2}$  into **eq. 24**. The result is the Michaelis–Menten parameterization of the type III functional response,

**Type III (Michaelis–Menten)**

$$g([P]) = \frac{g_{max}[P]^2}{K_{1/2}^2 + [P]^2}, \quad (25)$$

388 where,

$$K_{1/2} = \sqrt{\frac{g_{max}}{\epsilon_c}}. \quad (26)$$

389 Note that the Michaelis-Menten parameter scheme employs the same parameters in each  
 390 response type ( $K_{1,2}, g_{max}$ ), while the disk scheme requires a slightly different paramete-  
 391 ter set in a type II ( $\epsilon, g_{max}$ ) and III ( $\epsilon_c, g_{max}$ ) response.

392 Finally, note that where we refer to the disk and Michaelis–Menten parameteriza-  
 393 tion of the type III response, throughout the literature they are often referred to as the  
 394 ‘Sigmoidal Type III’ and ‘Holling Type III’ response, respectively. We use the former  
 395 nomenclature to clarify that both functions are sigmoidal in shape and because it allows  
 396 us to refer to the parameter scheme generically without specifying the response type. This  
 397 is semantically useful for comparisons between parameter scheme but not response type  
 398 which occur throughout the manuscript.

**3 Stability of the grazing formulation**

399  
 400 A suite of past studies have shown that the shape of these theoretical relationships,  
 401 when embedded into models and integrated forward in time, influences the dynamical  
 402 stability of the system, and in turn the propensity for phytoplankton extinction (Adjou  
 403 et al., 2012; Dunn & Hovel, 2020; J. Steele, 1974) and excitation (i.e. blooms) (Hernández-  
 404 García & López, 2004; Malchow, Hilker, Sarkar, & Brauer, 2005; Truscott & Brindley,  
 405 1994; Truscott, Brindley, Brindley, & Gray, 1994). In particular, (Gentleman & Neuheimer,  
 406 2008) have shown how the stabilizing influence of the grazing formulation is determined  
 407 by the sign of the first derivative of the clearance rate ( $\frac{dCl}{d[P]}$ ). The clearance rate ( $Cl$ )  
 408 is equal to the the functional response ( $g([P])$ ) normalized by the ambient phytoplank-  
 409 ton concentration (i.e.  $Cl = g([P])/[P]$ ). This is equivalent to the phytoplankton spe-  
 410 cific loss rate to grazing per unit zooplankton (see **Table 1**) or in other words, the vol-  
 411 ume of water completely cleared of phytoplankton per unit time, per unit zooplankton  
 412 (Gentleman & Neuheimer, 2008). Ecologically, higher clearance rates imply individual  
 413 zooplankton are either spending less time consuming their prey or more efficiently cap-  
 414 turing it.

415 Gentleman and Neuheimer (2008) showed how clearance rates vary with prey den-  
 416 sity in different functional response types (see **Fig. 2** there-in). In a type I functional  
 417 response clearance rates are constant because it is assumed that the prey capture effi-  
 418 ciency ( $\epsilon$ ) is constant and the consumption time is negligible (thus constant). In a type  
 419 II response clearance rates decrease with increasing prey density because the consump-  
 420 tion rate is no longer assumed negligible, meaning the more zooplankton graze, the more  
 421 time they need to consume their food, leaving less time to capture it. In a type III re-  
 422 sponse clearance rates first increase, then decrease with prey density based on the bal-  
 423 ance between increasing consumption time and increasing prey capture efficiency.

424 The stabilizing influence of the functional response is negative, or destabilizing, when  
 425 clearance rates decrease with increasing prey density ( $\frac{dCl}{d[P]} < 0$ ). In turn, growing (de-  
 426 caying) phytoplankton populations are subject to decreasing (increasing) per capita graz-  
 427 ing pressure, creating a destabilizing feedback that amplifies changes in phytoplankton  
 428 growth (decay) and increases the likelihood of excitation (extinction). This occurs when

429 the functional response has downward concavity, such that a type II response has a desta-  
 430 bilizing influence at all prey densities, while a type III response has a destabilizing in-  
 431 fluence only above  $K_{1/2}$  (Gentleman & Neuheimer, 2008). The stabilizing influence of  
 432 the functional response is positive, or stabilizing when clearance rates increase with in-  
 433 creasing prey density ( $\frac{dCl}{d[P]} < 0$ ). In turn, growing (decaying) phytoplankton popula-  
 434 tions are subject to increasing (decreasing) per capita grazing pressure, creating a sta-  
 435 bilizing feedback that buffers changes in phytoplankton growth (decay) and decreases  
 436 the likelihood of excitation (extinction). This occurs when the functional response has  
 437 upward concavity, such that a type III response has stabilizing influence below  $K_{1/2}$  (Gen-  
 438 tleman & Neuheimer, 2008). A type I response, in which clearance rates are constant  
 439 ( $\frac{dCl}{d[P]} = 0$ ), has no first order influence on stability.

440 The parameterization of the functional response can influence stability in two ways.  
 441 First, increasing  $g_{max}$  or decreasing  $K_{1/2}$  both increase the curvature of the response,  
 442 which directly increases its stabilizing or destabilizing influence. Thus, a type II response  
 443 with a higher  $g_{max}$  or lower  $K_{1/2}$  is more destabilizing at all prey densities. However,  
 444 a type III response is more destabilizing above  $K_{1/2}$  but more stabilizing below  $K_{1/2}$ .  
 445 This is illustrated clearly in Figure 5 of Gentleman and Neuheimer (2008), which tracks  
 446 the first derivative of clearance rates ( $\frac{dCl}{d[P]}$ ). Second, the parameterization of the func-  
 447 tional response can influence stability indirectly by applying stronger or weaker grazing  
 448 pressure which in turn drives the size of the phytoplankton population and thus the po-  
 449 sition on the curve at which  $\frac{dCl}{d[P]}$  is considered. For example, if using a type III response  
 450 with a lower  $K_{1/2}$ , the functional response will have a more destabilizing influence on  
 451 all phytoplankton populations above  $K_{1/2}$ , but faster grazing rates associated with the  
 452 lower  $K_{1/2}$  value make it more difficult for population levels to exceed  $K_{1/2}$ , such that  
 453 the overall outcome may be increasing the stabilizing influence of the response. Note,  
 454 in a disk scheme,  $K_{1/2}$  is not parameterized directly and its location varies with both  
 455 parameters.

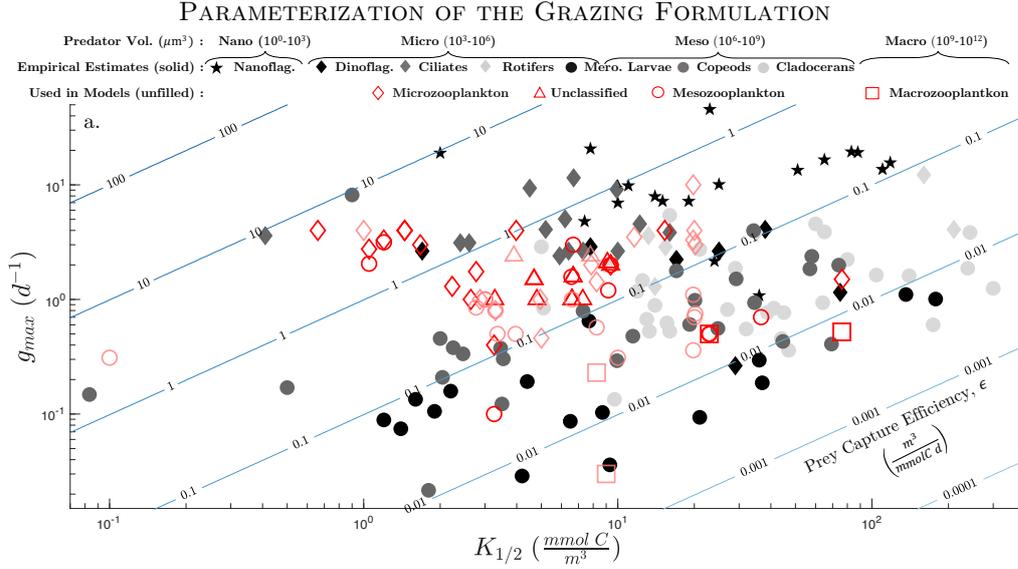
#### 456 4 Parameters of the grazing formulation

457 Constrained by computational resources, biogeochemical models are limited in the  
 458 number of zooplankton functional groups they can include, making it difficult to select  
 459 parameters that accurately represent the mean state of natural variability across the di-  
 460 verse zooplankton they are trying to simulate. We combine data from two extensive re-  
 461 views by Hansen et al. (1997); Hirst and Bunker (2003) to show how the values of 119  
 462 empirically estimated sets of grazing parameters vary largely across zooplankton size and  
 463 species (**Fig. 2**; filled markers; **Fig. 3a-c**). We then compare them to the values used  
 464 in 40 modelling studies consisting of over 70 unique grazing formulations (**Table 2**; **Fig.**  
 465 **2**; empty markers; **Fig. 3d-f**). Of the 40 models surveyed, 28 include only one zooplank-  
 466 ton group, meaning they must represent the mean behavior of all global zooplankton with  
 467 a single set of parameters. Those that include multiple zooplankton have the flexibility  
 468 to imply different traits for different functional groups by selecting different parameters.  
 469 However, functional group resolution is still very limited, with only one model includ-  
 470 ing more than three (Stock, Powell, & Levin, 2008). To determine if the values used in  
 471 models are ecologically realistic approximations of the mean state, it is essential to un-  
 472 derstand how empirical estimates vary and how models attempt to either capture or av-  
 473 erage out this variability.

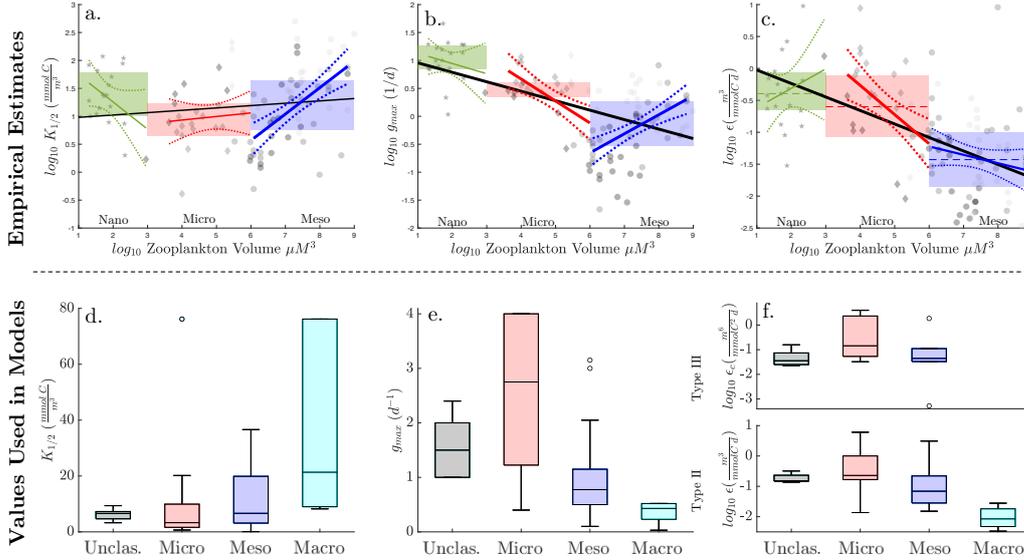
474 The most common partitioning of zooplankton functional groups in models is al-  
 475 lometric, or by size. Accordingly, we have binned all observed and modelled zooplank-  
 476 ton as ‘nano-’, ‘micro-’, ‘meso-’, or ‘macrozooplankton’. For the empirical studies, zoo-  
 477 plankton are categorized by their reported body volume, with nanozooplankton defined  
 478 as  $< 10^3 \mu m^3$  ( $\sim$  nanoflagellates), microzooplankton defined as  $10^3 - 10^6 \mu m^3$  ( $\sim$  di-  
 479 noflagellates, rotifers and ciliates), mesozooplankton defined as  $10^6 - 10^9 \mu m^3$  ( $\sim$  cope-  
 480 pods, meroplankton larvae and cladocerans) and macrozooplankton as  $> 10^9 \mu m^3$  (none

481 reported). In the models the same size classes are assigned based on the relative prey  
 482 portfolio or other specified descriptions of each zooplankton functional group. For ex-  
 483 ample, in a model with 2 zooplankton functional groups nominally called ‘small’ and ‘large’  
 484 and prescribed to preferentially graze on small phytoplankton and diatoms, we would  
 485 categorize these as ‘micro’ and ‘meso’, respectively. The ‘nano-’ and ‘macro-’ designa-  
 486 tions were only given when more than two zooplankton were included or they were clas-  
 487 sified explicitly as such in the study. Models with one generic, unspecified zooplankton  
 488 were left unclassified.

489 For consistent comparison between models and empirical studies, we converted all  
 490 units to  $mmolC/m^3$  for prey density and  $1/d$  for rates. In Hirst and Bunker (2003)  $K_{1/2}$   
 491 was reported in chlorophyll units and converted with a C:Chl ratio of 50:1 (Anderson  
 492 et al., 2010). In Hansen et al. (1997)  $K_{1/2}$  was reported in ppm, and converted with a  
 493 carbon density of  $0.12 gC/cm^3$ . Note, no explicit conversion factor was given for prey  
 494 carbon density by Hansen et al. (1997); however,  $0.12 gC/cm^3$  was explicitly assumed  
 495 for zooplankton and is consistent with the range of carbon densities in phytoplankton  
 496 (Menden-Deuer & Lessard, 2000). Different conversion factors would shift the absolute  
 497 values of  $K_{1/2}$  reported here, but not the size of their range or strength of their correla-  
 498 tions with size. In modelling studies that used a currency other than carbon, units were  
 499 converted assuming a fixed Redfield ratio of 106:16:1, unless otherwise stated in the study.  
 500 Finally, eqs. 18 & 26 were used to convert between Michaelis-Menten and disk param-  
 501 eters and eq. 21 was used to determine the initial slope (i.e.  $\epsilon$ ) and half saturation con-  
 502 centration (i.e.  $K_{1/2}$ ) of Ivlev responses. Note, the maximum clearance rates reported  
 503 in Hansen et al. (1997) are synonymous with  $\epsilon$  once units have been converted.



**Figure 2.** The parameters of the grazing formulation. **a)** Empirical estimates of parameters for >60 zooplankton species (Hansen et al., 1997; Hirst & Bunker, 2003) are plotted with filled markers. Parameters for different zooplankton functional groups from 40 modelling studies (Table 2) are plotted with red empty markers. Light red markers denote formulations with a multiple-prey response and parameters refer to the implied single-prey response when grazing exclusively on their most preferred prey. Contours for the corresponding prey capture efficiency (assuming type-II response) are overlaid.



**Figure 3.** Allometric Relationships. **a-c**) Empirical estimates of all grazing parameters are plotted against zooplankton size and subdivided into size classes. Marker shapes are consistent with species in **Fig. 2**. The interquartile range (IQR) is overlaid for each size class along with a log-linear regression and 95% confidence intervals. A log-linear regression is shown for the complete data set as well (black). Statistically significant correlations have thicker line widths and detailed statistical information is provided in **Table 3a**. **d-f**) Distributions for each grazing parameter within each size class are shown for the model values. Note, macro- and nanozooplankton are not included for empirical and model plots, respectively, because less than two of each were surveyed. Additionally,  $\epsilon_c$  is not shown for the empirical values because all empirical estimates were fit to a type II response. Note, similar figures to **a-c** first appeared in (Hansen et al., 1997). Ours differ in that they are converted to units more familiar to modellers, additionally include the Hirst and Bunker (2003) data set, and provide statistical information on three distinct size classes.

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#### 4.1 Empirical estimates

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The grazing parameters for a myriad of different zooplankton have been estimated empirically via laboratory incubation and dilution experiments. In these studies, specific grazing rates were measured at different prey concentrations and then fit to a type II response function. Together, reviews by Hansen et al. (1997) and Hirst and Bunker (2003) describe 119 empirical estimates of over 20 functional groups, derived from data on over 200 species. Looking across all surveyed zooplankton, the values of each grazing parameter vary by over three orders of magnitude, with  $K_{1/2}$  ranging from .08-499  $mmolC/m^3$ ,  $g_{max}$  ranging from 0.02-45.6  $d^{-1}$ , and  $\epsilon$  ranging from .003-9.5  $\frac{m^3}{mmolCd}$  (**Fig. 2**). While some of this variability can be explained statistically by the large variability in zooplankton size ( $10-10^9 \mu m^3$ ), the strength of the allometric relationship differs with both the parameter in question and whether you are considering all samples or just a subset within a certain size class (**Fig. 3; Table 3**).

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Consistent with Hansen et al. (1997), when considering the entire, combined data set there is a statistically significant allometric relationship between zooplankton size and both  $g_{max}$  (**Fig. 3b**; black regression) and  $\epsilon$  (**Fig. 3c**; black regression). This decrease in the parameters that describe consumption and capture rates, respectively, is consis-

521 tent with the conventional wisdom that grazing rates decrease with predator size (Moloney  
 522 & Field, 1989; Peters & Downing, 1984; Saiz & Calbet, 2007; Wirtz, 2013). However,  
 523 as in Hansen et al. (1997),  $K_{1/2}$  values from the combined data set do not exhibit a sta-  
 524 tistically significant allometric relationship (**Fig. 3a**; black regression), contradicting the  
 525 notion that  $K_{1/2}$  should increase with increasing predator size (Ray et al., 2011). This  
 526 can be explained because  $K_{1/2}$  is not an independent, physiological parameter, but rather  
 527 a mathematical description of the curve, relating the other two parameters that mech-  
 528 anistically describe consumption (i.e.  $g_{max}$ ) and capture (i.e.  $\epsilon$ ) rates (see **Section 2**).  
 529 While all parameters are estimated here empirically, only  $\epsilon$  and  $g_{max}$  reflect independent  
 530 trait-based differences in grazing behaviour. Therefor, if  $g_{max}$  and  $\epsilon$  both decrease with  
 531 zooplankton size, grazing rates will decrease at low and high concentrations such that  
 532 the half-saturation concentration may increase, decrease, or remain largely unaltered,  
 533 depending of the relative changes. The net effect when considered across all zooplank-  
 534 ton sizes is a flat and statistically insignificant (**Table 3a**).

535 Similarly, when grouped into discrete size classes, the mean, median and interquar-  
 536 tile range (IQR) of  $g_{max}$  and  $\epsilon$  decrease monotonically from nanozooplankton (**Fig. 3**;  
 537 **green**) to microzooplankton (red) to mesozooplankton (blue), while those of  $K_{1/2}$  do  
 538 not (**Table 3b**). Instead the median value of  $K_{1/2}$  decreases from 23  $mmolC/m^3$  in nanoo-  
 539 zooplankton to 8.9  $mmolC/m^3$  in microzooplankton but then increases to 18.1  $mmolC/m^3$   
 540 in mesozooplankton. Of the three parameters, binning by size class does the best job of  
 541 explaining variability in distributions of  $g_{max}$ , which has the smallest coefficient of vari-  
 542 ability (i.e.  $std/mean$ ) of all parameters in all size classes. Moreover, using a two sam-  
 543 ple t-test at the 95% confidence level,  $g_{max}$  is the only parameter in which the mean value  
 544 in adjoining size classes are statistically different from one another. For  $\epsilon$ , only nano- and  
 545 mesozooplankton have statistically different means, although the difference between micro-  
 546 and mesozooplankton is nearly significant ( $p=0.1$ ) and may become so if the binning bounds  
 547 were adjusted. For  $K_{1/2}$ , the range of values in each size class varies by over two order  
 548 of magnitude and largely overlaps. In turn, there is no statistically significant difference  
 549 between the mean  $K_{1/2}$  value within any two size classes, even nano- and microzooplank-  
 550 ton which differ by  $\sim 6$  orders of magnitude in volume. Together, empirical estimates  
 551 of  $g_{max}$  appear better constrained by size class than  $K_{1/2}$ , or even  $\epsilon$ , suggesting that con-  
 552 sumption rates are better correlated than capture rates with zooplankton size class.

553 However, these trait-based correlations become more complex when looking at vari-  
 554 ability within a given size class, rather than across them (**Fig. 3a-c**; **Table 3a**). Nanoo-  
 555 zooplankton are the most poorly constrained by size. When considered in isolation there  
 556 is no statistically significant relationship between any of their empirically derived graz-  
 557 ing parameters and size (**Fig. 3a-c**; **green**). Microzooplankton, on the other hand, are  
 558 the best constrained by size. Both  $g_{max}$  (**Fig. 3b**; **red**) and  $\epsilon$  (**Fig. 3c**; **red**) exhibit  
 559 a robust, statistically significant, inverse relationship with size, with a higher coefficient  
 560 of determination ( $r^2$ ) than in any other size class. In turn, the correlation between  $K_{1/2}$   
 561 and size is flat and statistically insignificant (**Fig. 3b**; **red**). This is consistent with de-  
 562 creasing capture and consumption rates that combine to lower mean grazing rates but  
 563 not systematically modify  $K_{1/2}$ . Mesozooplankton traits are also fairly well constrained  
 564 by size, but in a qualitatively different way. When exclusively considering mesozooplan-  
 565 kton (**Fig. 3a-c**; **blue**),  $K_{1/2}$  and  $g_{max}$  both exhibit a statistically significant positive  
 566 relationship with size, while the relationship with  $\epsilon$  is flatter and statistically insignif-  
 567 icant. This suggests that consumption rates in mesozooplankton actually increase with  
 568 size while capture rates are invariant, leading to an apparent increase in the  $K_{1/2}$  (see  
 569 **eq. 18**). Critically though, this increase in  $K_{1/2}$  is associated with faster, not slower,  
 570 grazing on average.

571 From a modelling perspective, the most common partitioning in models with mul-  
 572 tiple zooplankton is into two micro- and mesozooplankton groups (**Table 2**). Nanoo-  
 573 zooplankton on the other hand only appear in one surveyed (**Table 2**). When considering

574 exclusively empirical variability in micro- and mesozooplankton, ignoring nanozooplankton,  
 575 there is a statistically significant correlation with size for all three parameters. Sim-  
 576 ilar to when considering all zooplankton,  $g_{max}$  and  $\epsilon$  both decrease with size; however,  
 577 with nanozooplankton removed, the decline in  $g_{max}$  is flatter and less significant (i.e. lower  
 578 p-value) while the decline in  $\epsilon$  is steeper and more significant (**Table 3a**). In turn, there  
 579 is now also a statistically significant increase in  $K_{1/2}$  with size. Additionally, if only con-  
 580 sidering the IQR of  $K_{1/2}$ , there is statistically significant difference in the means value  
 581 in micro- and mesozooplankton.

582 Accordingly, in biogeochemical models using two discrete zooplankton state vari-  
 583 ables to simulate the mean state of micro- and mesozooplankton, it appears the meso-  
 584 zooplankton class should have slower consumption (i.e.  $g_{max}$ ) and capture rates (i.e.  $\epsilon$ )  
 585 than microzooplankton. Further, the empirically observed increase in  $K_{1/2}$  means that  
 586 the decrease in  $\epsilon$  should be disproportionately larger than that of  $g_{max}$ . However, in dif-  
 587 ferent model configurations one may wish to vary different parameters in different ways,  
 588 depending on the range and resolution of what you are simulating. For example, a size-  
 589 spectrum model of exclusively microzooplankton may wish to decrease both capture and  
 590 consumption rates with size, whereas a size spectrum model of exclusively mesozooplan-  
 591 tkon may wish to increase consumption rates with size and leave capture rates constant.

592 Finally, it is important to note that the way in which these trait-based correlations  
 593 can be prescribed depends on the parameter scheme. For example, to increase consump-  
 594 tion rates without increasing capture rates in a Michaelis-Menten scheme one must in-  
 595 crease  $g_{max}$  and  $K_{1/2}$  or else otherwise increase  $\epsilon$  implicitly as well. This would inad-  
 596 vertently overestimate grazing rates at low prey densities. However, to increase consump-  
 597 tion and capture rates in a Michaelis-Menten scheme one must still increase  $g_{max}$  but  
 598 the change in  $K_{1/2}$  depends on the intended relative difference in the two properties. In  
 599 any scenario all parameters should be computed and considered explicitly to confirm the  
 600 correct behavior is being implied at low and high prey densities.

## 601 4.2 Values used in models

602 Over 70 independent grazing formulations from 40 modelling studies were surveyed  
 603 (**Table 2**, **Fig. 2**; empty markers) to gauge the range of commonly prescribed param-  
 604 eter values and see if they vary in a manner that is consistent with the natural variabil-  
 605 ity measured empirically (**Sec. 4.1**). A large sampling of prominent modelling studies,  
 606 from canonical 0-dimensional theoretical work (Evans & Parslow, 1985; Franks et al., 1986),  
 607 through slightly more sophisticated NPZD models (Fasham, 1995; Fasham et al., 1990),  
 608 to state-of-the-art CMIP6 climate models (Aumont et al., 2015; Christian et al., 2021;  
 609 Hajima et al., 2020; Law et al., 2017; Long et al., 2021; Stock et al., 2020; Tjiputra et  
 610 al., 2020; Totterdell, 2019; Yool et al., 2021) were included. Surveyed models were as-  
 611 sessed to determine if their selection of parameter values is representative of the mean  
 612 state of empirically estimated values and if variability their-in is consistent with the ob-  
 613 served allometric variability (**Fig. 3d-f**; **Table 3c**) or varies with other aspects of the  
 614 grazing formulation (**Table 3d**).

615 Of the 40 models surveyed, 26 include a zooplankton group that grazes with a single-  
 616 prey response, including 5 of 9 IPCC CMIP6 climate models. This amounts to 40 of the  
 617 70 unique grazing formulations. The others graze on multiple prey (**Table 2**; grey rows  
 618 & **Figure 3**; light red markers) and use a  $K_{1/2}$  parameter that is fundamentally differ-  
 619 ent from that of the single-prey response Gentleman et al. (2003). In multiple-prey re-  
 620 sponse functions,  $K_{1/2}$  refers to the half saturation 'concentration' of the total, preference-  
 621 weighted prey pool, which is not a one-to-one function of the prey distribution. In **Ta-**  
 622 **ble 2** we report this value in parenthesis, but focus our analysis on the implied  $K_{1/2}$  for  
 623 the single-prey response for each zooplankton group when grazing exclusively on their  
 624 most preferred prey. Gentleman et al. (2003) describe in detail how this value can be cal-

Reference	Dimensions (# Z, P tracers)	Location	Zooplankton Functional Group	Grazing Formulation (Single Prey Response)			
				Resp. Type	Parameter Scheme	$K_{1/2}$ ( $mmolC/m^3$ )	$g_{max}$ ( $1/d$ )
Wroblewski (1977)	2 (1P1Z) <sup>N</sup>	coastal upwelling	macro	II	Ivlev	76.18	.52
Evans and Parslow (1985)	0 (1P1Z) <sup>N</sup>	N. Atlantic	-	II <sup>th</sup>	M-M	7.28	
Franks et al. (1986)	0 (1P1Z) <sup>N</sup>	-	meso	II	Ivlev	2.25-45.7	0.16-1.5
Fasham et al. (1990)	0 (1P1Z) <sup>N</sup>	Bermuda	meso	II	M-M	6.6 (6.6)	1
Frost (1993)	1 (1P1Z) <sup>C</sup>	Station P	micro	II <sup>th</sup>	M-M	2.23	1.01-1.6
Truscott and Brindley (1994)	0 (1P1Z) <sup>N</sup>	coastal (red tide)	meso	III	M-M	36.6	0.7
Fasham (1995)	0 (1P1Z) <sup>N</sup>	Station P	-	II	disk	6.6	1
Franks and Chen (1996)	2 (1P1Z) <sup>N</sup>	Georges Bank	meso	II	Ivlev	22.9	.5
Franks and Walstad (1997)	2 (1P1Z) <sup>N</sup>	-	meso	II	Ivlev	22.9	.5
Denman and Peña (1999)	1 (1P1Z) <sup>N</sup>	Station P	micro	III	M-M	2.64	1
Edwards et al. (2000)	2 (1P1Z) <sup>N</sup>	coastal upwelling	micro macro	II II	Ivlev Ivlev	15.3 22.9	4 0.5
Franks and Chen (2001)	3 (1P1Z) <sup>N</sup>	Georges Bank	meso	II	Ivlev	22.9	.5
Denman and Peña (2002)	1 (1P2Z) <sup>N</sup>	Station P	micro meso	III III	M-M M-M	4.96 (4.96) 3.96 (3.96)	1 0.5
Leising et al. (2003)	0 (1P1Z) <sup>N</sup>	HNLC equatorial Pacific	micro micro micro micro	II II <sup>th</sup> II III	M-M M-M M-M M-M	0.66 1.45 3.98 1.45	4 4 4 4
Newberger et al. (2003)	0 (1P1Z) <sup>N</sup>	coastal upwelling	micro	II	Ivlev	76.18	1.5
Spitz et al. (2003)	2 (1P1Z) <sup>N</sup>		macro	II	Ivlev	76.18	0.52
Schartau and Oschlies (2003b)	3 (1P1Z) <sup>N</sup>	N. Atlantic	-	III	disk	6.67	1.58
Aumont and Bopp (2006) (PISCES)	3 (2P2Z) <sup>C</sup>	global	micro meso	II II	M-M M-M	20 (20) 20 (20)	4 0.7
Gentleman and Neuheimer (2008)	0 (1P1Z) <sup>N</sup>	-	-	III, II, II, II <sup>th</sup>	M-M, M-M Ivlev, M-M	4.68	1.5
Stock et al. (2008)	0 (3P4Z) <sup>N</sup>	Low, Mid, High Productivity	nano(100 $\mu$ m) micro(1e4 $\mu$ m) meso(1e6 $\mu$ m) macro(1e8 $\mu$ m)	II II II II	M-M M-M M-M M-M	20 (20) 20 (20) 20 (20) 20 (20)	10 3.3 1.1 0.6
Sinha et al. (2010) (PLANKTOM5.2)	3 (3P2Z) <sup>C</sup>	global	micro meso	II II	M-M M-M	11.6 (15) 0.1 (0.26)	3.5 0.31
T. Anderson et al. (2010)	3 (3P2Z) <sup>C</sup>	global	micro meso	I, II, II, III	M-M, M-M, Ivlev, M-M	1 (1) 3 (3)	4 1
Adjou et al. (2012)	0 (2P1Z) <sup>N</sup>	Station P	-	II, III	M-M, disk	6.6	1
Kriest et al. (2012)	3 (1P1Z) <sup>P</sup>	global	-	III	M-M	9.38	2
Shigemitsu et al. (2012) (MEM)	1 (2P3Z) <sup>N</sup>	N. Pacific	micro meso	II <sup>th</sup> II <sup>th</sup>	Ivlev Ivlev	3.38 3.28	.4 0.1, 0.4
Dunne et al. (2013) (TOPAZ)	3 (1P0Z)	global	allometric	-	-	-	0.19
Tjiputra et al. (2013) (NORESM1)	3 (1P1Z) <sup>P</sup>	global	-	II	M-M	4.8	1
Hauck et al. (2013) (REcoM2)	3 (2P1Z) <sup>N</sup>	global	<i>micro</i> <i>meso</i>	III III	M-M M-M	3.9 (3.9) 7.8 (3.9)	2.4 2.4
Moore et al. (2013) (BEC)	3 (3P1Z) <sup>C</sup>	global	<i>micro</i> <i>meso</i>	III III	M-M M-M	1.05 1.05	2.05 2.75
Oke et al. (2013) (WOMBAT)	3 (1P1Z) <sup>N</sup>	global	-	III	disk	9.1	2.1
Dutkiewicz et al. (2015) (Darwin)	3 (8P2Z) <sup>P</sup>	global	micro meso	III III	M-M M-M	2.86 (2.86) 3.01 (2.86)	1 1
Le Quéré et al. (2016) (PlankTOM10)	3 (6P3Z) <sup>C</sup>	global	micro meso macro	II II II	M-M M-M M-M	5 (10) 10 (10) 9 (9)	0.46 0.31 0.03
Law et al. (2017) (WOMBAT)	3 (1P1Z) <sup>N</sup>	global	-	III	disk	6.57	1.58
Totterdell (2019) (diat-HadOCC)	3 (2P1Z) <sup>N</sup>	global	<i>micro</i> <i>meso</i>	II II	M-M M-M	3.3 (3.3) 3.3 (3.3)	0.8 0.8
Stock et al. (2020, 2014) (COBALTv2, COBALT)	3 (3P3Z) <sup>N</sup>	global	micro meso macro	II II II	M-M M-M M-M	8.28 (8.28) 8.28 (8.28) 8.28 (8.28)	1.42 0.57 0.23
Christian et al. (2021) (CANOE)	3 (2P2Z) <sup>C</sup>	global	micro meso	II II	Ivlev Ivlev	2.77 2.77 (2.77)	1.75 0.85
Yool et al. (2021, 2013) (MEDUSA2.0)	3 (2P2Z) <sup>N</sup>	global	micro meso	III III	M-M M-M	7.65 (5.3) 3.36 (1.88)	2 0.5
Long et al. (2021) (MARBL)	3 (3P1Z) <sup>C</sup>	global	<i>micro</i> <i>meso</i>	II II	M-M M-M	1.2 1.2	3.3 3.15
Hajima et al. (2020) (MIROC)	3 (2P1Z) <sup>N</sup>	global	<i>micro</i> <i>meso</i>	II II	disk disk	9.36 9.36	2 2
Aumont et al. (2015) (PISCESv2)	3 (2P2Z) <sup>C</sup>	global	micro meso	II II	M-M M-M	20 (20) 20 (20)	3 0.75
Tjiputra et al. (2020) (NORESM2)	3 (1P1Z) <sup>P</sup>	global	-	II	M-M	9.76	1.2

**Table 2.** The parameterization of the grazing formulation in biogeochemical models. The model currency (C,N, or P) is noted in the superscript in column 1 and units of  $K_{1/2}$  are converted to carbon where required using a Redfield ratio of 106:16:1 (C:N:P) if not noted in the study. The  $K_{1/2}$  relationship algebraically relates the mathematical half saturation concentration ( $g(P) = g_{max}/2$ ) to the parameters specified in the model when not parameterized explicitly. Different zooplankton size classes are given separate rows. Values from a given study separated by commas indicate different simulations. Models with a multiple prey response are highlighted in grey and the reported  $K_{1/2}$  values refer to the implied single-prey response when grazing exclusively on their most preferred prey. In parentheses is the  $K_{1/2}$  prescribed for bulk ingestion on the total preference weighted prey field. Models with one zooplankton tracer that grazes separately on two phytoplankton groups with two distinct single-prey responses (i.e. specific grazing rates on one prey group are not effected by the concentration of the other) are considered to have a single-prey response and two implicit zooplankton groups. Implicit functional groups are italicized.

**a) Empirical Estimates: Trait-based Correlation with Size**

Size Class	$K_{1/2}$			$g_{max}$			$\epsilon$		
	p	$r^2$	b	p	$r^2$	b	p	$r^2$	b
All Sizes n=119	0.12	0.02	0.04	$10^{-11}$	0.31	-0.17	$10^{-13}$	0.37	-0.21
Nano. & Micro. n = 49	0.06	0.07	-0.10	$10^{-7}$	0.44	-0.24	0.01	0.12	-0.13
Micro & Meso. n=94	$10^{-4}$	0.13	0.17	0.01	0.06	-0.11	$10^{-8}$	0.29	-0.27
Nanozooplankton n=19	0.1	0.15	-0.47	0.41	0.04	-0.18	0.35	0.05	0.30
Microzooplankton n=30	0.68	.008	0.06	$10^{-4}$	0.33	-0.39	$10^{-3}$	0.29	-0.046
Mesozooplankton n=64	$10^{-6}$	0.29	0.47	$10^{-5}$	0.23	0.34	0.18	0.03	-0.13

**b) Empirical Estimates: Sample Statistics by Size Class**

Size Class	$K_{1/2}$ (mmolC/m <sup>3</sup> )				$g_{max}$ (1/d)				$\epsilon$ (m <sup>3</sup> /mmolC/d)			
	mean	med.	range	IQR	mean	med.	range	IQR	mean	med.	range	IQR
All zooplankton n=119	40	16	$8.3e^{-2}$ 500	6.4 43	3.7	1.6	$2.1e^{-2}$ 46	0.46 3.8	0.49	$8.4e^{-2}$	$3.4e^{-3}$ 9.5	$2.1e^{-2}$ 0.27
Nanozooplankton n=19	37	23	1.7 120	10 62	13	10	1.1 46	7.0 19	1.1	0.40	$3.0e^{-2}$ 9.5	0.22 0.85
Microzooplankton n=30	25	8.9	0.41 210	4.5 17	3.6	3.0	0.11 12	2.2 4.1	0.71	0.25	$9.1e^{-3}$ 8.8	$9.0e^{-2}$ 0.78
Mesozooplankton n=64	45	18	$8.0e^{-2}$ 500	5.8 45	1.3	0.77	$2.0e^{-2}$ 8.2	0.29 1.8	0.24	$4.0e^{-2}$	$3.4e^{-3}$ 9.1	$1.0e^{-2}$ 0.10

**c) Values Used in Models: Sample Statistics by Size Class**

Size Class	$K_{1/2}$ (mmolC/m <sup>3</sup> )				$g_{max}$ (1/d)				$\epsilon$ (m <sup>3</sup> /mmolC/d) *				$\epsilon_c$ (m <sup>3</sup> /mmolC <sup>2</sup> /d) **			
	mean	med.	range	IQR	mean	med.	range	IQR	mean	med.	range	IQR	mean	med.	range	IQR
All Zoo. (n=70,47*,23**)	11	6.6	0.1 76	3.3 11.6	1.7	1.1	$3.0e^{-2}$ 10	0.7 2.4	0.56	0.15	$3.3e^{-3}$ 6.1	$3.2e^{-2}$ 0.32	0.50	0.04	$5.0e^{-4}$ 4	$3.3e^{-2}$ 0.14
Uncat. (n=14,5*,9**)	6.3	6.6	3.3 9.4	4.7 7.3	1.5	1.5	1.0 2.4	1.0 2.0	0.19	0.15	0.14 0.32	0.15 0.24	$5.6e^{-2}$	$3.5e^{-2}$	$2.3e^{-4}$ 0.16	$2.5e^{-4}$ 4
Nanozoo. (n=1,1*,0**)	20	20	-	-	10	10	-	-	0.51	0.51	-	-	-	-	-	-
Microzoo. (n=25,18*,7**)	9.1	3.3	0.66 76	1.6 9.9	2.4	2.8	0.40 4.0	1.2 4.0	0.96	0.23	$1.4e^{-2}$ 6.1	0.17 1.0	1.2	0.14	4.0 4.0	$6.1e^{-2}$ 2.3
Mesozoo. (n=24,17*,7**)	10	6.6	0.10 37	3.1 20	1.0	0.78	0.10 3.2	0.5 1.2	0.44	$6.9e^{-2}$	$1.5e^{-2}$ 3.1	$2.9e^{-2}$ 0.22	0.31	$4.4e^{-2}$	$5.0e^{-4}$ 1.9	$3.3e^{-2}$ 0.11
Macrozoo. (n=6,6*,0**)	35	21	8.3 76	9 76	0.37	0.43	$3.0e^{-2}$ 0.52	0.23 0.52	$1.2e^{-2}$	$9.9e^{-3}$	$3.3e^{-3}$ $2.8e^{-2}$	$4.7e^{-3}$ $1.8e^{-2}$	-	-	-	-

**d) Values Used in Models: Sample Statistics by Grazing Formulation**

Grazing Formulation	$K_{1/2}$ (mmolC/m <sup>3</sup> )				$g_{max}$ (1/d)				$\epsilon$ (m <sup>3</sup> /mmolC/d) *				$\epsilon_c$ (m <sup>3</sup> /mmolC <sup>2</sup> /d) **			
	mean	med.	range	IQR	mean	med.	range	IQR	mean	med.	range	IQR	mean	med.	range	IQR
Type III (n=23,0*,23**)	6.0	4.0	1.0 37	3.0 6.7	1.7	1.6	0.5 4.0	1 2.1	-	-	-	-	0.50	$4.4e^{-2}$	$5.0e^{-4}$ 4	$3.3e^{-2}$ 0.14
Type II (Ivlev) (n=35,35*,0**)	8.9	7.3	0.1 20	3.5 11	1.9	1.2	$3.0e^{-2}$ 10	0.8 3.1	0.72	0.20	$3.3e^{-3}$ 6.1	0.10 0.49	-	-	-	-
Ivlev (n=12,12*,0**)	29	23	2.7 76	3.3 50	0.97	0.51	0.1 4.0	0.5 1.2	$8.5e^{-2}$	$1.5e^{-2}$	$4.7e^{-3}$ 0.44	$1.4e^{-2}$ 0.13	-	-	-	-
Michaelis-Menten (n=49,32*,17**)	7.8	5.0	0.10 37	12.8 9.2	1.9	1.2	$3.0e^{-2}$ 10	0.79 3.0	0.77	0.19	$3.3e^{-3}$ 6.1	$8.0e^{-2}$ 0.54	0.66	0.11	$5.0e^{-4}$ 4.0	$3.8e^{-2}$ 0.58
disk (n=9,3*,6**)	7.1	6.6	3.2 9.4	6.6 9.2	1.5	1.6	1.0 2.1	1.0 2.0	0.19	0.21	0.15 0.21	0.17 0.21	0.04	$3.6e^{-2}$	$2.3e^{-2}$ $9.3e^{-2}$	$2.5e^{-2}$ $3.6e^{-2}$
Single Prey (n=40,27*,13**)	13	6.6	0.66 76	2.7 9.8	1.8	1.5	0.1 4.0	1.0 2.4	0.75	0.18	$4.7e^{-3}$ 6.1	$1.6e^{-2}$ 0.55	0.52	$3.6e^{-2}$	$5.0e^{-4}$ 2.5	$2.5e^{-2}$ 0.57
Multiple Prey (n=30,20*,10**)	9.3	7.8	0.1 20	3.3 20	1.6	1.0	$3.0e^{-2}$ 10	0.5 2.4	0.29	0.15	$3.3e^{-3}$ 3.1	$3.6e^{-2}$ 0.23	0.5	$7.0e^{-2}$	$3.3e^{-2}$ 3.1	$3.6e^{-2}$ 0.23

**Table 3.** Statistics from empirically estimated and modelled grazing parameters. **a)** The p-value (p), coefficient of determination ( $r^2$ ), and slope (b) are displayed for a linear regression fit between the  $\log_{10}$  of zooplankton size ( $\mu\text{m}^3$ ) and the  $\log_{10}$  of  $K_{1/2}$ ,  $g_{max}$ , and  $\epsilon$ . Data included in each model is limited to the size class(es) specified in the left column. Statistically significant relationship ( $p < 0.05$ ) are highlighted in blue for positive correlations ( $b > 0$ ) and red for negative correlations ( $b < 0$ ). **b,c,d)** Sample statistics are shown for **b)** empirical values sorted by size classes and **c,d)** model values sorted by size class and other attributes of the grazing formulation. The IQR refers to the Inter-quartile range (i.e. middle 50%). Statistics for  $\epsilon$  do not include any type III responses and statistics for  $\epsilon_c$  do not include any type II or Ivlev response.  $\epsilon_c$  is not shown for the empirical data as a type II response was always assumed.

625 culated algebraically from the reduced multiple-prey response based on both innate prey  
 626 preferences (i.e. constants) and assumptions about whether preferences can vary with  
 627 the relative distribution of prey (i.e. switching vs. no switches) (Fasham et al., 1990).  
 628 Although the apparent  $K_{1/2}$  for a given prey item will increase in the presence on other  
 629 prey options, we consider the implied  $K_{1/2}$  for the single-prey response as it is informa-  
 630 tive as to how modellers assume zooplankton behave in optimal conditions, grazing on  
 631 exclusively on their preferred prey.

632 Overall, the full range of grazing parameters used in models varies largely (**Fig.**  
 633 **2; empty red markers**).  $K_{1/2}$  and  $g_{max}$  both vary by over two orders of magnitude,  
 634 from 0.1-76  $mmol\ C/m^3$  and 0.03-10  $1/d$ , respectively. When converted into a disk pa-  
 635 rameter scheme the range is even larger, with  $\epsilon$  in type II (and Ivlev) response functions  
 636 spanning more than 3 orders of magnitude, from  $3.3*10^{-3}$ - $6.1\ \frac{m^3}{mmolCd}$ , and  $\epsilon_c$  in type  
 637 III response functions spanning nearly 4 orders of magnitude, from  $5.2*10^{-4}$ - $4\ \frac{m^6}{mmol^2Cd}$ .  
 638 Considering that these values are used to represent the mean state of many zooplank-  
 639 ton, they might be expected vary substantially less than the empirical estimates, which  
 640 should be expected to span a large range of natural variability. However, the range of  
 641 model values for each parameter exceeds the interquartile range of empirical estimates  
 642 (**Table 3b,c**), suggesting that some models may be using unreasonably high or low pa-  
 643 rameter values. This is especially true for model values of  $\epsilon$ , which exceed the interquar-  
 644 tile range of empirical estimates by an order of magnitude in both directions. Moreover,  
 645 the mean of model and empirical distributions are not statistically similar ( $p>0.05$ ; 2-  
 646 sample t-test) for any parameter. However, this comparison may be biased by intended  
 647 differences in the zooplankton functional groups being modelled.

648 Breaking down the model values by size class gives a better indication of how rep-  
 649 resentative models are of empirically estimated values (**Fig. 3d-f; Table 3b,c**). Focus-  
 650 ing on microzooplankton and mesozooplankton, the most commonly simulated size classes,  
 651 the range of  $K_{1/2}$ ,  $g_{max}$ , and  $\epsilon$  for both size classes falls within the range, but beyond  
 652 the interquartile range, of their respective empirical estimates. However, relative differ-  
 653 ences between the two size classes are generally consistent with the observations. Sta-  
 654 tistically, modelled consumption ( $g_{max}$ ; **Fig. 3e**) and capture ( $\epsilon$ ,  $\epsilon_c$ ; **Fig. 3f**) rates both  
 655 decline with zooplankton size and do so in a manner that increases  $K_{1/2}$  (**Fig. 3d**).

656 In particular, variability in  $g_{max}$  across the two size classes is well aligned with the  
 657 observations (**Fig. 3b,e; Table 3b,c**). The median value (and interquartile range) of  
 658  $g_{max}$  decreases from 2.75 (1.2-4) in microzooplankton to 0.78 (0.5-1.15) in mesozooplank-  
 659 ton models, compared to from 3.0 (2.2-4) to 0.77 (0.3-1.8) in the empirically measured  
 660 values. Moreover, there is no statistical difference between the mean of the model and  
 661 empirical distributions of  $g_{max}$  in either simulated size class. Unsurprisingly, both sets  
 662 of model and empirical values reported here are consistent with values of 2-4  $1/d$  and  
 663 1  $1/d$ , respectively, reported elsewhere throughout the literature (C. A. Edwards et al.,  
 664 2000; Gismervik, 2005; Lancelot et al., 2005; Leising, Gentleman, & Frost, 2003; Strom  
 665 & Morello, 1998).

666 However, allometric variability in capture rates, either prescribed directly by  $\epsilon$  (**Fig.**  
 667 **3c,f**) and  $\epsilon_c$  or indirectly by  $K_{1/2}$  (**Fig. 3a,d**), is less consistent with the observations.  
 668 The median value (and IQR) of  $\epsilon$  decreases from 0.27 (.17-1.79) to 0.14 (.04-.37) in mod-  
 669 els, compared to from 0.25 (.09-0.78) to .04 (.01-.09) in the empirically measured val-  
 670 ues. This smaller drop in  $\epsilon$  between size classes in the models is consistent with a smaller  
 671 increase in  $K_{1/2}$  than observed. The median value (and IQR) of  $K_{1/2}$  increases from 3.3  
 672 (1.6-9.9) to 6.6 (3-9.9) in models, compared to from 8.9 (4.5-17) to 18 (5.8-45) in the em-  
 673 pirically measured values (**Table 3b,c**). In turn, the relative decrease mesozooplank-  
 674 ton grazing at low prey concentrations (where capture rates dominate) may be under-  
 675 estimated in the models. This is likely happening because most models which include  
 676 micro- and mesozooplankton use a Michaelis-Menten parameter scheme and vary  $g_{max}$   
 677 between size classes but not  $K_{1/2}$  (**Table 2**). While this is consistent with the allomet-

678 ric relationships measured across the full range of zooplankton, it may not be when fo-  
 679 cusing explicitly on difference between micro- and mesozooplankton (**Sec 4.1; Table**  
 680 **3a**). In turn, models that vary both  $g_{max}$  and  $K_{1/2}$  (e.g. Anderson et al. (2010)) may  
 681 be more realistic than those that fix  $K_{1/2}$  across size.

682 While the clearest source of variability between model values is justifiably allomet-  
 683 ric, we additionally check for differences associated with attributes of the grazing for-  
 684 mulation (**Table 3d**). The only statistically significant difference related to the grazing  
 685 formulation was between capture rates prescribed in Ivlev response types compared to  
 686 those in Holling type III, or even type II, responses. The mean  $K_{1/2}$  used in zooplank-  
 687 ton simulated with an Ivlev response was nearly 5x larger ( $29 \text{ mmolC}/\text{m}^3$ ) than that  
 688 used in a type III response (6.0), and over 3x larger than that used in a qualitatively sim-  
 689 ilar type II response (8.0). Although a disproportionate number of zooplankton simu-  
 690 lated with a Ivlev response are described as macrozooplankton (50%), mean  $K_{1/2}$  val-  
 691 ues for micro- (24) and mesozooplankton (15) simulated with an Ivlev response are also  
 692 much higher than the average value used in non-Ivlev type II response functions (7.8 &  
 693 9.6, respectively). This suggests that  $K_{1/2}$  may be systematically overestimated in Ivlev  
 694 responses, perhaps because the Ivlev parameter is further abstracted from any mecha-  
 695 nistically meaningful value or intuitive characteristic of the curve. Finally, there was no  
 696 statistically significant difference between the mean of any parameter value when compar-  
 697 ing those used in Michaelis-Menten versus disk parameter schemes or when compar-  
 698 ing single-prey response types with the implied single prey response from multi-prey re-  
 699 sponse types.

## 700 5 Sensitivity of the grazing formulation

701 To isolate the sensitivity of phytoplankton population dynamics to the functional  
 702 response and its parameterization, we extend the sensitivity analysis conducted by Gen-  
 703 tleman and Neuheimer (2008). We use an identical, idealized, 0-dimensional Nutrient-  
 704 Phytoplankton-Zooplankton (NPZ) box model to that of Gentleman and Neuheimer (2008),  
 705 and earlier Franks et al. (1986). This model assumes that phytoplankton (P) grow via  
 706 uptake of external inorganic nutrients (N) and are lost to zooplankton (Z) grazing and  
 707 mortality. Nutrients are returned to the inorganic pool via phytoplankton mortality, zoo-  
 708 plankton mortality and sloppy grazing. Phytoplankton growth follows nutrient limited  
 709 Michaelis-Menten kinetics Michaelis and Menten (1913) and both phytoplankton and zoo-  
 710 plankton mortality terms are linear. Mass transfer between N, P and Z pools is described  
 711 by,

$$\begin{aligned}
 \frac{dN}{dt} &= (1 - \alpha)g([P])Z - \mu_{max} \frac{N}{K_N + N}P + m_pP + m_zZ, \\
 \frac{dP}{dt} &= \mu_{max} \frac{N}{K_N + N}P - g([P])Z - m_pP, \\
 \frac{dZ}{dt} &= \alpha g([P])Z - m_zZ,
 \end{aligned}
 \tag{27}$$

712 where  $\alpha$  is the grazing efficiency,  $\mu_{max}$  is the phytoplankton maximum specific growth  
 713 rate,  $K_N$  is the nutrient uptake half saturation constant,  $m_p$  is the phytoplankton mor-  
 714 tality rate,  $m_z$  is the phytoplankton mortality rate, and  $g([P])$  is the grazing formu-  
 715 lation (i.e. **eq. 17, 18, 24, or 25**). The model is not forced with seasonality in light, mix-  
 716 ing or other environmental conditions, such that  $\mu_{max}$  is constant and phytoplankton  
 717 growth is determined only by nutrient availability. Non-grazing parameters and initial  
 718 conditions (**Table 4b**) are identical to Gentleman and Neuheimer (2008), but converted  
 719 to carbon units using a stoichiometric ratio of C:N = 106:16.

a. The Grazing Formulation					b. Other Parameters and Initial Conditions			
	Response Type	Parameter Scheme	Parameters	Sensitivity Range		Parameter	Value	Sensitivity Range
$g(P)$	II	disk	$\epsilon$ $g_{max}$	$0.01 - 10 \frac{m^3}{mmolCd}$ $0.1 - 45 d^{-1}$	$\alpha$	Grazing efficiency	0.7	0.35, 1.0
	III	disk	$\epsilon_c$ $g_{max}$	$0.01 - 10 \frac{m^6}{mmolC^2d}$ $0.1 - 45 d^{-1}$	$\mu_{max}$	Phytoplankton maximum specific growth rate	$2 d^{-1}$	$1, 4 d^{-1}$
	II	Michaelis-Menten	$K_{1/2}$ $g_{max}$	$100 - 0.1 \frac{mmolC}{m^3}$ $0.1 - 45 d^{-1}$	$m_P$	Phytoplankton mortality rate	$0.1 d^{-1}$	.05, $0.2 d^{-1}$
	III	Michaelis-Menten	$K_{1/2}$ $g_{max}$	$100 - 0.1 \frac{mmolC}{m^3}$ $0.1 - 45 d^{-1}$	$m_Z$	Zooplankton mortality rate	$0.2 d^{-1}$	0.1, $0.4 d^{-1}$
					$K_N$	Nutrient uptake half-saturation constant	$6.6 \frac{mmolC}{m^3}$	3.3, 13.2 $\frac{mmolCl}{m^3}$
					$N_0$	Nutrient density initial condition	$10.6 \frac{mmolC}{m^3}$	5.3, 21.2 $\frac{mmolC}{m^3}$
					$P_0$	Phytoplankton density initial condition	$1.3 \frac{mmolC}{m^3}$	0.65, 2.6 $\frac{mmolC}{m^3}$
					$Z_0$	Zooplankton density initial condition	$1.3 \frac{mmolC}{m^3}$	0.65, 2.6 $\frac{mmolC}{m^3}$

**Table 4.** List of **a.** grazing formulations and **b.** other parameters and initial conditions used for the NPZ (eq. 27) sensitivity analysis in **Section 5.**

720 Gentleman and Neuheimer (2008) used this model to assess the change in dynamical stability when switching between a type II and III response or doubling/halving  $K_{1/2}$  and  $g_{max}$ . In addition to testing both response types, we go on to test both parameter schemes (disk, Michaelis-Menten) and a much larger range of grazing parameters. This allows for the comparison of gradients across the parameter space between four different grazing formulations (i.e. Type II-disk, Type III-disk, Type II-Michaelis-Menten, Type III-Michaelis-Menten; see **Table 4a**). Within each grazing formulation we consider a range of log-spaced values spanning nearly 3 orders of magnitude for both parameters (**Table 4a**). These ranges are all within the range of what has been estimated empirically (**Fig. 2**; **Table 3b**). Note, corresponding grid cells in each panel of **Figs. 5 & 6** do not correspond to identical functional response curves; identical parameter values used in different response types or parameter schemes will yield differently shaped curves and thus different dynamics. Instead, when comparing panels, we consider differences in gradients across the parameter space.

734 All 784 combinations of parameters values for each functional response (i.e. 3136 total tests) were integrated using a non-stiff ordinary differential equation solver (Matlab's ode45) for 5 years, after which the system has either reached steady state, quasi state-state (repeating limit cycles), or numerical instability. Integrating any further did not meaningfully change our results. We analyse the final year of each integration, which was long enough to capture limit cycles which a had a period of anywhere from weeks to months. We then assess how the choice of response type, parameter scheme, and parameter values influences prescribed grazing rates (**Section 5.1**) and in turn drives the size (**Section 5.2**) and stability (**Section 5.3**) of the phytoplankton population. The sensitivity of our results to non-grazing parameters and initial conditions is also examined (**Table 4b**; **Section 5.4**).

### 745 5.1 Sensitivity of grazing rates

746 Modellers can prescribe faster grazing rates by increasing  $\epsilon$ ,  $\epsilon_c$ , and/or  $g_{max}$  in a disk parameter scheme, or decreasing  $K_{1/2}$  and/or increasing  $g_{max}$  in a Michaelis-Menten parameter scheme. Note that while  $\epsilon$  and  $g_{max}$  modify the curve in the same direction when using a disk formulation,  $K_{1/2}$  and  $g_{max}$  modify it in opposite directions when using a Michaelis-Menten formulation, meaning that modellers must ensure parameter changes do not inadvertently cancel out if modifying both in the same direction. Moreover, the sensitivity of the shape of the curve and associated grazing rates to these parameters varies with the parameter scheme, response type, and the prey density (or location on the curve)

754 in question. To illustrate this, we have provided a schematic showing how proportional  
 755 changes in different parameters modify the curve in different ways at low and high  $[P]$   
 756 values (**Fig. 4**). We then quantify these changes by computing the mean grazing rates  
 757 prescribed at low and high  $[P]$  values for all curves defined across the entire parameter  
 758 space (**Fig. 5**).

759 When using a disk scheme (**Fig. 4**, green), regardless of response type, grazing rates  
 760 are determined almost entirely by prey capture rates when food is scarce (Low  $[P]$ ; **Fig.**  
 761 **4**, middle row) and by consumption rates when food is replete (High  $[P]$ ; **Fig. 4**, bot-  
 762 tom row). This is self-evident if one understands the underlying theory, but not neces-  
 763 sarily obvious from the terms ‘attack’ or ‘capture rate’ to non-experts. In turn,  $g_{max}$  has  
 764 almost no bearing on the shape of the curve at low  $[P]$  (**Fig. 4f, h**) and  $\epsilon$  (or  $\epsilon_c$ ) has  
 765 little influence on the shape of the curve at high  $[P]$ ; (**Fig. 4i, k**). Moving from a type  
 766 II (**Fig. 4**, left side) to III (**Fig. 4**, right side) response switches the description of prey  
 767 capture rates from a linear to quadratic function of  $[P]$  (see **Section 2**), which decreases  
 768 the sensitivity of grazing rates to  $\epsilon_c$  (relative to  $\epsilon$ ), especially at low  $[P]$  (**Fig. e, g**).

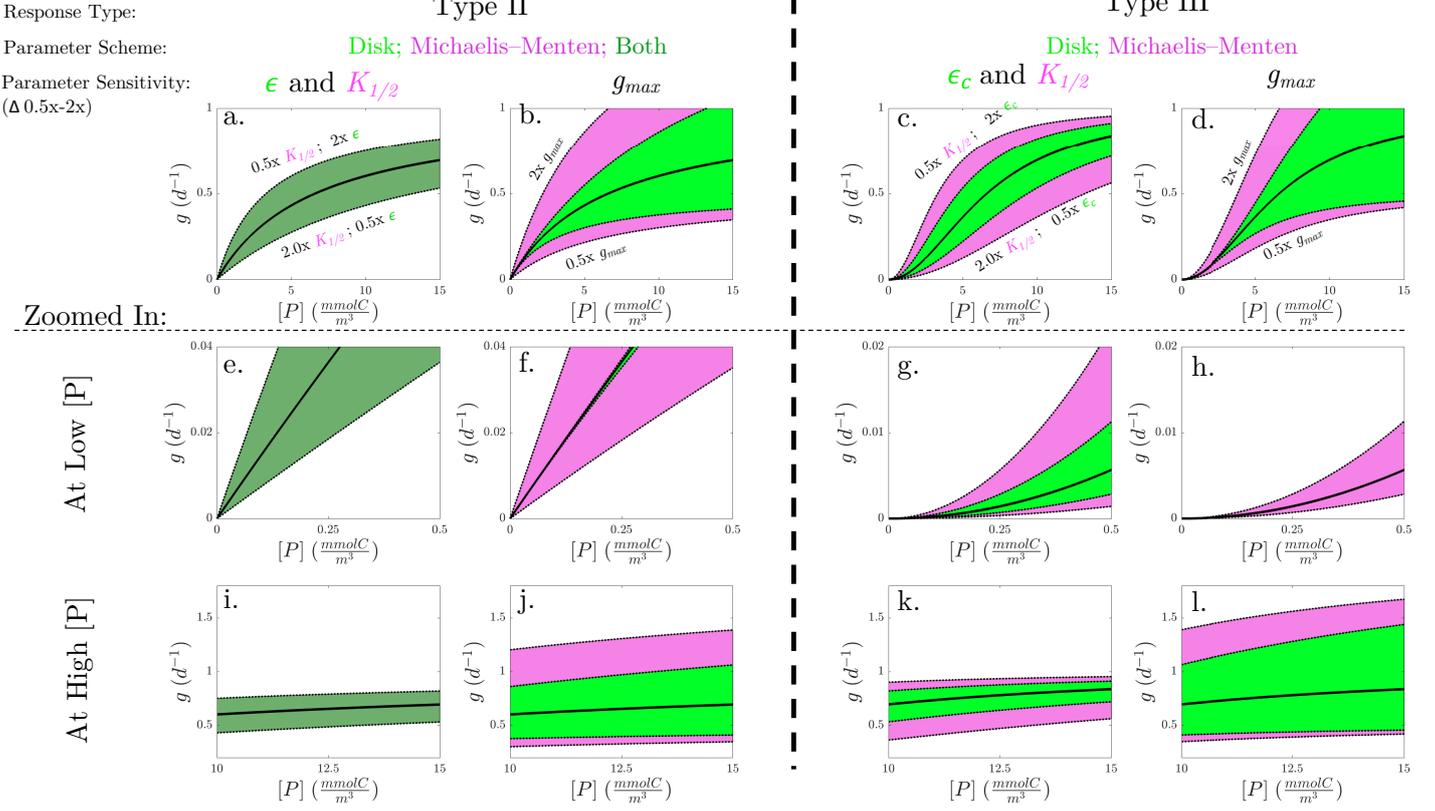
769 When using a Michaelis-Menten parameter scheme (**Fig. 4**, magenta), grazing rates  
 770 are proportionally, but inversely, affected by changes in  $K_{1/2}$  compared to  $\epsilon$  in a disk scheme  
 771 (**Fig. 4a, e, i**), leading to the dark green overlapping curves in the left-most panel of  
 772 **Fig. 4**. This occurs because,  $K_{1/2}$  is equal to  $\frac{g_{max}}{\epsilon}$ , or equivalently  $\frac{1}{\epsilon h}$  (see **Sec. 2.3**),  
 773 and  $g_{max}$  (and its reciprocal,  $h$ ) are held constant. However, in a type III response, graz-  
 774 ing rates are substantially more sensitive to  $K_{1/2}$  than  $\epsilon_c$ , (**Fig. 4c, g, k**), particularly  
 775 at low prey densities (**Fig. 4g**). Moreover, in both a type II and III response, the Michaelis-  
 776 Menten scheme is dramatically more sensitive to  $g_{max}$  at low prey densities (**Fig. 4f,**  
 777 **h**). This is because faster (slower) prey capture rates (and thus a larger prey capture ef-  
 778 ficiency,  $\epsilon$ ) are implicitly required for the curve to saturate at a faster (slower) grazing  
 779 rate with the same half saturation concentration.

780 Computing the mean grazing rate across low ( $0-0.5 \frac{mmolC}{m^3}$ ) and high ( $10-15 \frac{mmolC}{m^3}$ )  
 781 phytoplankton concentrations ( $[P]$ ) for all grazing formulations considered in our sensi-  
 782 tivity analysis (**Table 4**) confirms these trends (**Fig. 5**). In a type II disk formulation,  
 783 grazing rates at low  $[P]$  are almost entirely unaffected by  $g_{max}$ , especially when  $\epsilon$  is low  
 784 (**Fig. 5a**), whereas grazing rates at high  $[P]$  are almost entirely driven by  $g_{max}$ , espe-  
 785 cially when  $\epsilon$  is large (**Fig. 5b**). Introducing the concavity of a Type III response in-  
 786 creases this disparity. In turn, the mean grazing pressure at low  $[P]$  increases with  $\epsilon_c$  but  
 787 is effectively invariant across 3 orders of magnitude change in  $g_{max}$  (**Fig. 5c**). Alterna-  
 788 tively, mean grazing rates at high  $[P]$  are almost entirely described by  $g_{max}$  unless  $\epsilon_c$  is  
 789 so low that our definition of ‘high  $[P]$ ’ no longer falls above the half saturation point of  
 790 the curve (**Fig. 5d**).

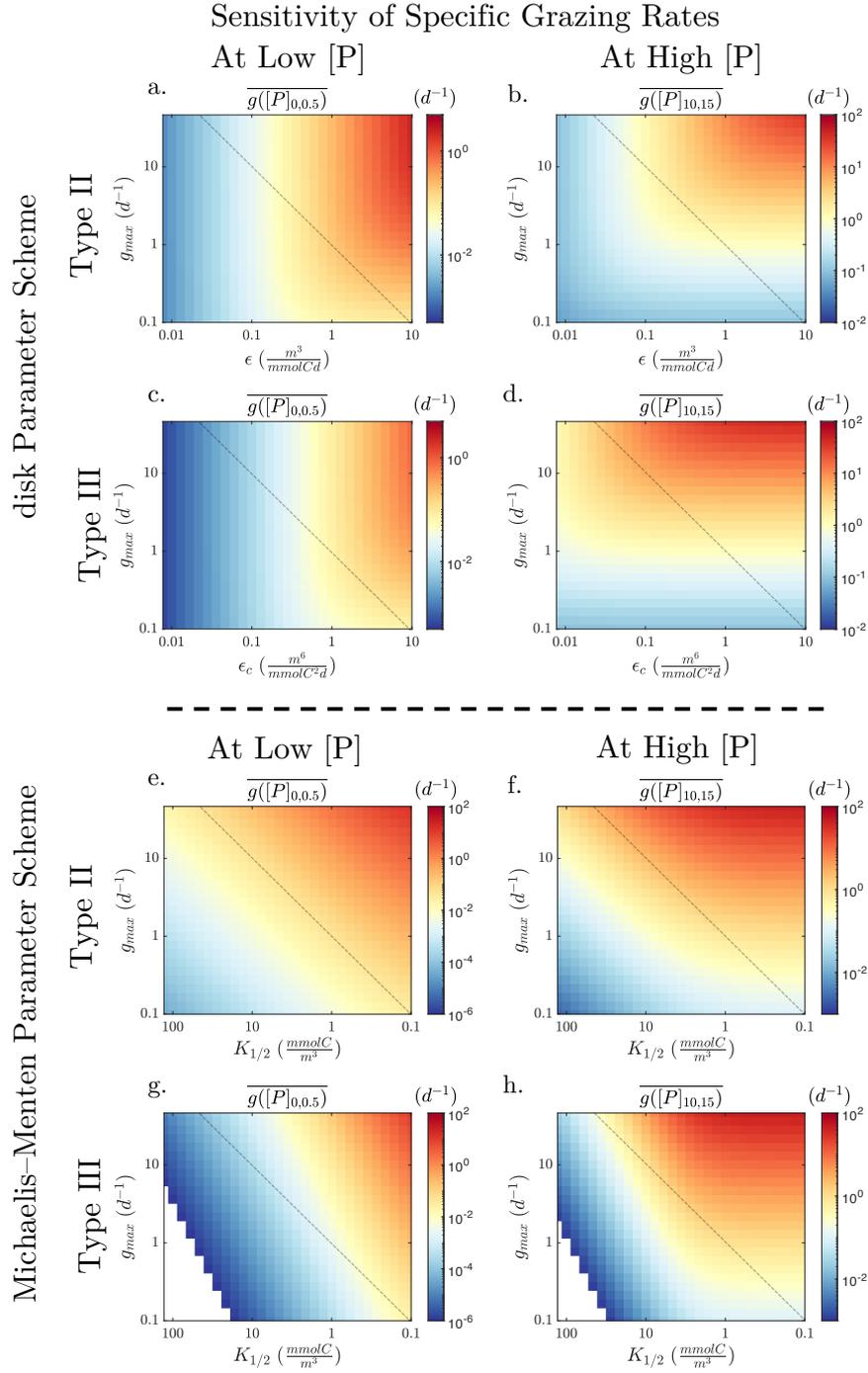
791 Using a Michaelis-Menten scheme increases the sensitivity of grazing rates to both  
 792 parameters (**Fig. 5e-h**), such that  $g_{max}$  has much more influence at low  $[P]$  (**Fig. 5e,**  
 793 **g**) and  $K_{1/2}$  has more influence at high  $[P]$  (**Fig. 5f, h**). However, in a type III response,  
 794 grazing rates are still more sensitive to  $K_{1/2}$  than  $g_{max}$  at low  $[P]$  (**Fig. 5g**) and more  
 795 sensitive to  $g_{max}$  than  $K_{1/2}$  at high  $[P]$  (**Fig. 5h**). Increased parameter sensitivity in  
 796 the Michaelis-Menten scheme means that a greater variety of curve shapes and associ-  
 797 ated grazing rates can be described with an equivalent range of parameter values, albeit  
 798 with lower resolution. This means that there should be more variability in model out-  
 799 put derived from equivalent changes in Michaelis-Menten versus disk parameters.

800 In other words, in a Michaelis-Menten scheme a smaller range of parameters can  
 801 test the same range of curves, but many intermediate options will be skipped.

SCHMATIC OF THE FUNCTIONAL RESPONSE CURVE

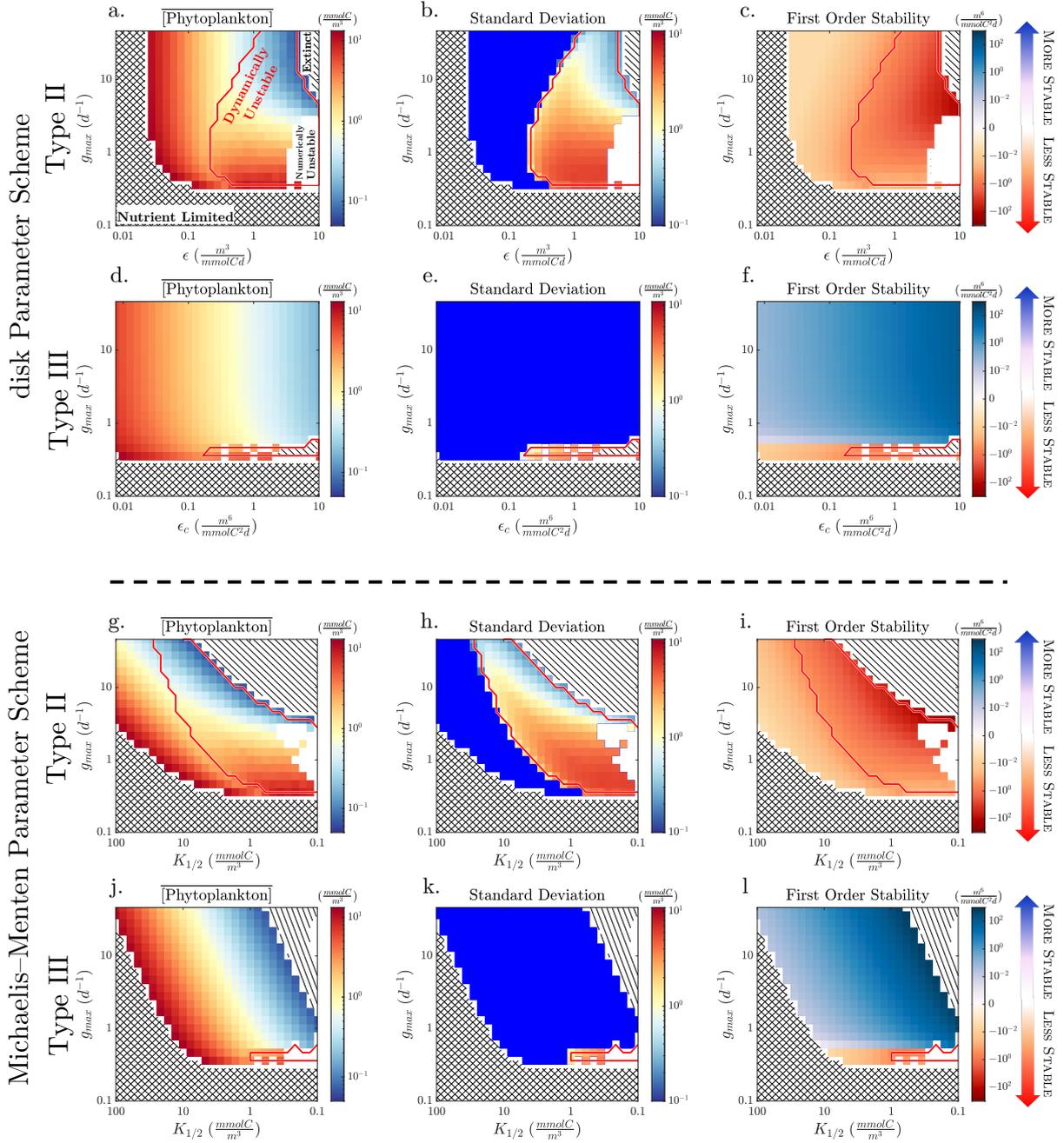


**Figure 4.** Schematic of the functional response curve. A type II (a,b) and III (c,d) response curve is plotted in black with colored windows depicting how the curve varies with proportional changes to its parameters. Initial parameters were chosen such that the disk and Michaelis-Menten parameter schemes yield mathematical identical curves ( $g_{max} = 1$ ,  $K_{1/2} = 6.625$ ). Colored windows show how the curve varies when its parameters are individually halved (0.5x) or doubled (2x) within a disk (green) or Michaelis-Menten (magenta) parameter scheme. The shaded region depicts the range of curves encompassing a 0.5x-2x change in the associated parameter. Close ups of the same curves are shown below for (e-h) low and (i-l) high phytoplankton concentrations. Annotations in Row 1 show which curves correspond to which parameter modification. Note, the dark green shading in (a,e & i) indicates a complete overlap in the variability window for both parameter schemes.



**Figure 5.** Sensitivity of specific grazing rates. Variability in the mean zooplankton specific grazing rate averaged across (a, c, e, g) low ( $[P] < 0.5 \frac{\text{mmolC}}{\text{m}^3}$ ) and (b, d, f, h) high ( $10 < [P] < 15 \frac{\text{mmolC}}{\text{m}^3}$ ) phytoplankton concentrations ( $[P]$ ) is shown as a function of the parameters of the functional response curve using a (a, b, e, f) Type II and (c, d, g, h) Type III response type as well as a (a-d) disk and (e-h) Michaelis-Menten parameter scheme. The range of low and high  $[P]$  correspond to the zoomed in panels of the schematic in Fig. 4. A dashed log 1-1 line is included to assess the relative parameter sensitivity.

## Sensitivity of Phytoplankton Population Dynamics



**Figure 6.** Sensitivity of phytoplankton population dynamics. Variability in the (a, d, g, j) mean annual phytoplankton concentration, (b, e, h, k) standard deviation, and (c, f, i, l) First Order Stability of the solution are plotted against the parameterization of the functional response curve using a (a-c, g-j) Type II and (d-f, j-l) Type III response type as well as a (a-f) disk and (g-l) Michaelis-Menten parameter scheme. Parameter schemes that yield complete nutrient utilization or phytoplankton extinction are hatched out with cross or single lines, respectively. Dynamically unstable regions are bounded with a red contour while dynamically stable solutions have a near-zero standard deviation and appear blue in b, e, h, k. Numerically unstable regions are plotted in white. Note, the dynamics and stability of the disk and Michaelis-Menten parameter schemes are identical when their parameters overlap (i.e.  $\epsilon = g_{max}/K_{1/2}$  or  $\epsilon_c = g_{max}/K_{1/2}^2$ )

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## 5.2 Sensitivity of phytoplankton population size

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The mean size of the phytoplankton population,  $\overline{[P]}$ , (**Fig. 6**, left column) is largely driven by the shape of the functional response at low phytoplankton concentrations and unaffected by what the curve looks like once it begins to saturate at high phytoplankton concentrations. For example,  $\overline{[P]}$  is 14% lower in type II than analogously parameterized type III responses (i.e. same  $K_{1/2}$  and  $g_{max}$ ), despite the fact that a type II response takes much longer to reach maximum grazing rates (i.e. saturation), and prescribes slower grazing at all prey concentrations above  $K_{1/2}$ . This disparity increases to 58% when only considering stable solutions that have neither gone extinct nor reached complete nutrient limitation (see **Section 5.3**). This occurs because  $\overline{[P]}$  dynamics are more sensitive to grazing when prey  $[P]$  is low and a type II response imposes faster grazing than its type III analogue below  $K_{1/2}$ .

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The out-sized importance of the grazing rates at low  $[P]$  is even more noticeable in the type III response. Considering all dynamically stable,  $\overline{[P]}$  has a much stronger correlation with mean grazing rates at low  $[P]$  ( $r^2 = 0.97$ ) than high  $[P]$  ( $r^2 = -0.53$ ). Accordingly, the sensitivity of  $\overline{[P]}$  to the grazing formulation qualitatively mirrors the sensitivity of mean grazing rates at low  $[P]$  to the grazing formulation (**Fig. 5, 6**, left columns). Ecologically, this implies that the size of phytoplankton populations is limited by zooplankton capture rates, which dominate when prey is scarce, not consumption rates, which dominate when prey is replete and the zooplankton population is more likely to be larger and capable of exerting strong grazing pressure, regardless of the speed of zooplankton specific grazing rates.

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In turn,  $\overline{[P]}$  is most sensitive to the parameterization of the response curve when the response type and parameter scheme allow for those parameters to most efficiently describe the bottom of the response curve. This means  $\overline{[P]}$  is less sensitive to the parameterization of the functional response in a disk than Michaelis-Menten parameter scheme. For example, phytoplankton in a type III disk scheme only experienced extinction or complete nutrient utilization in 20% of the tested parameter space (**Fig. 6d**), compared to 40% when using a type III Michaelis-Menten scheme (**Fig. 6j**). The size of the intermediate solution space will vary with other parameter choices and the size of the nutrient pool; however, the fact remains that a smaller range of parameters is needed to span from extinction to complete nutrient utilization in a Michaelis-Menten than disk scheme. Similarly, when using a type III response,  $\overline{[P]}$  is more sensitive to  $K_{1/2}$  and  $\epsilon_c$  than  $g_{max}$  in both parameter schemes because they more directly define the shape of the response curve when prey is scarce (**Fig. 4g, h**). Together, the value  $g_{max}$  has almost no influence on the size of the phytoplankton population in a type III disk scheme.

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## 5.3 Sensitivity of phytoplankton population stability

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In the simplified NPZ model, with no seasonal forcing, phytoplankton populations tend to quickly reach a seasonally invariant steady state. However, if the destabilizing influence of the functional response is large enough, dynamically unstable oscillations (i.e. limit cycles) in the phytoplankton population can emerge. The magnitude of the destabilizing (or stabilizing) influence of the grazing formulation is determined by both the curvature the functional response as well as the prognostic feedback of grazing on the phytoplankton population, which determines it's the position on the curve. We approximate the magnitude of this stabilizing influence with the First Order Stability (**Fig. 6c, f, i, l**), defined as the first derivative of clearance rates (see **Sec. 3**) calculated at the mean phytoplankton concentration in year 5 of the solution. Larger negative values, for example, mean that the grazing formulation has a more destabilizing influence on the mean phytoplankton population, but does not necessarily determine if the system is dynamically unstable, as other stabilizing processes could dominate. To determine if the system is dynamically unstable, we look to see if oscillations emerge. The strength of these

853 oscillations is approximated by the standard deviation of the phytoplankton population  
 854 (**Fig. 6b, e, h, k**). The system is deemed stable if it reached roughly steady state by  
 855 year five of the integration and exhibits a near-0 standard deviation (plotted in blue).  
 856 The system is deemed dynamically unstable if the standard deviation in year 5 is greater  
 857 than 0.5% of the total nutrient pool. The system is further deemed numerically unsta-  
 858 ble if the solution cannot be reached using a non-stiff integration technique.

859 The phytoplankton population remains dynamically stable, with a near zero stand-  
 860 ard deviation (**Fig. 6b, e, h, k**, blue shading), when First Order Stability is positive  
 861 or slightly negative (**Fig. 6c, f, i, l**). However, the phytoplankton population begins to  
 862 oscillate, exhibiting much larger standard deviations, once First Order Stability becomes  
 863 sufficiently negative. It is possible for a dynamically stable solution with negative First  
 864 Order Stability to emerge if other stabilizing factors dominate the destabilizing influenc-  
 865 ing of the grazing formulation. First Order Stability, as defined here, is only a measure  
 866 of the stabilizing (or destabilizing) influence of the grazing formulation and other factors  
 867 can provide a stabilizing feedback on the phytoplankton population. In this model,  
 868 these factors include nutrient limitation and the size of the zooplankton population, which  
 869 both increasingly dampen phytoplankton population growth as phytoplankton biomass  
 870 accumulates, even if specific grazing rates decline. In more complicated NPZ models other  
 871 factors, including more complex closure schemes such as quadratic zooplankton mortal-  
 872 ity, can provide stability as well (A. M. Edwards & Yool, 2000; J. H. Steele & Hender-  
 873 son, 1992). Conversely, in this simple model oscillations never occur when First Order  
 874 Stability is positive, even when initial conditions are varied by 0.5-2x (**Table 4b**). How-  
 875 ever, it is possible that in longer simulations of more complex models with other desta-  
 876 bilizing factors, they may.

877 When using a type II response (**Fig. 6**; rows 1 & 3), First Order Stability is al-  
 878 ways negative and the phytoplankton population in 53% of tested solutions was either  
 879 dynamically unstable (37.5%, red contour), numerically unstable (5.5%, white), or ex-  
 880 tinct (10%, diagonal hash). Increasing  $g_{max}$  and decreasing  $K_{1/2}$  both decrease stabil-  
 881 ity; however, when using a Michaelis-Menten parameter scheme, the First Order Stabili-  
 882 ty is, on average,  $\sim 5$  times more sensitive to changes in  $K_{1/2}$  than  $g_{max}$  due to its greater  
 883 influence on the curvature of the functional response. In a disk scheme, however, First  
 884 Order Stability is only 0.25 times more sensitive to  $\epsilon$  than  $g_{max}$ , because both param-  
 885 eters influence the location of  $K_{1/2}$ . Because the stability of the population is much more  
 886 sensitive to  $g_{max}$  than the size of the population, relatively small changes in  $g_{max}$  could  
 887 trigger sudden instabilities with little warning.

888 When using a type III response (**Fig. 6**; rows 2 & 4), First Order Stability is rarely  
 889 negative. Only 5.5% of tested solutions were dynamically (1.7%) or numerically (3.8%)  
 890 unstable and less than 4% led to phytoplankton extinction. First Order Stability becomes  
 891 increasingly stable with increasing  $g_{max}$  and decreasing  $K_{1/2}$  because increasing graz-  
 892 ing pressure drives  $[P]$  below  $K_{1/2}$  where the upward concavity of the response curve pro-  
 893 vides stability and protects against extinction. This holds even though decreasing  $K_{1/2}$   
 894 simultaneously lowers the threshold for instability. There is only negative First Order  
 895 Stability and oscillations in the phytoplankton population when both  $K_{1/2}$  and  $g_{max}$  are  
 896 very low. This occurs because as the  $g_{max}$  approaches the zooplankton mortality rate,  
 897 zooplankton net population growth slows, decoupling  $[P]$  and  $[Z]$  and allowing  $[P]$  to es-  
 898 cape grazing pressure and exceed a low  $K_{1/2}$  value.

#### 899 5.4 Influence of other parameters

900 The sensitivity of phytoplankton population size to the grazing formulation does  
 901 not appear to be qualitatively influenced by the selection of other non-grazing param-  
 902 eters or initial conditions (see **Table 4b**); however, these choices do influence the size  
 903 of the stable solution space. Nutrient limitation is described by a type II Michaelis-Menten

904 curve and thus has similar, but qualitatively opposite, stabilizing properties to the graz-  
 905 ing formulation. The difference is that the saturation of nutrient uptake provides a neg-  
 906 ative, rather than positive, feedback on phytoplankton population growth. In turn, in-  
 907 creasing the maximum phytoplankton specific division rates ( $\mu_{max}$ ) or decreasing the  
 908 half saturation concentration for nutrient uptake ( $K_N$ ) both increase the stability of the  
 909 system and reduce the number of unstable solutions. On the other hand, our results agree  
 910 with previous work that limiting zooplankton population growth by either increasing zoo-  
 911 plankton mortality ( $m_Z$ ) or reducing grazing efficiency ( $\alpha$ ) can increase the destabiliz-  
 912 ing influence of a type II (or Ivlev) response (Edwards et al., 2000a, b, GN08) (C. Ed-  
 913 wards, Powell, & Batchelder, 2000; C. A. Edwards et al., 2000; Gentleman & Neuheimer,  
 914 2008). We go on to show that this can even occur in a type III response if  $m_Z > \alpha g_{max}$   
 915 (**Fig. 6e,k**), thereby decoupling specific grazing rates from bulk grazing pressure (i.e.  
 916  $g[Z]$ ). Reallocating the initial distribution of nutrients between the  $[N]$ ,  $[P]$ , and  $[Z]$  pools  
 917 had little influence on stability. However, as similiarly shown by Franks and Chen (1996,  
 918 2001) increasing the total nutrient pool increases the number of unstable solutions by  
 919 diminishing the stabilizing influence of nutrient limitation.

## 920 6 Sensitivity to sub-grid scale heterogeneity

921 Mechanistic derivations (**Sec. 2**) and empirical approximations (**Sec. 4**) of the func-  
 922 tional response are based on well-mixed solutions. Therefor, the shape and sensitivity  
 923 of the functional response is predicated on the assumption that a homogeneously dis-  
 924 tributed zooplankton population is grazing on a homogeneously distributed phytoplank-  
 925 ton population. However, the ocean is notoriously patchy, with global plankton distri-  
 926 butions highly heterogeneous at scales well below the typical resolution of even eddy-  
 927 resolving ocean models (Ohman, 1990; Raymont, 2014). Phytoplankton and zooplank-  
 928 ton populations are often log-normally distributed (J. Campbell, 1995; Druon et al., 2019),  
 929 such that an increase in the mean plankton concentration is associated with a dispro-  
 930 proportionate increase in smaller areas of high productivity, surrounded by large swaths of  
 931 lower productivity. In turn, the functional response used in global, or even coarse regional  
 932 models, is likely implicitly being averaged over a great deal of sub-grid scale heterogene-  
 933 ity.

934 Ideally, coarse models should strive to prescribe how mean specific grazing rates,  
 935  $\bar{g}$ , averaged across the a grid-cell, vary with the grid-cell mean phytoplankton popula-  
 936 tion,  $\overline{[P]}$ . However, this apparent mean functional response ( $\overline{g([P])}$ ) can differ substan-  
 937 tially from the local response of individual zooplankton ( $g([P])$ ) when averaged across suf-  
 938 ficient sub-grid scale heterogeneity. For example, A. Y. Morozov and Arashkevich (2010)  
 939 have shown the emergence of upward concavity in  $\overline{g([P])}$  when averaged across a 1-D wa-  
 940 ter column model, even though  $g([P])$  was prescribed with a type II response. We fur-  
 941 ther generalize these results by examining a simple non-dimensional system (or grid cell)  
 942 composed of just two regimes: one fraction of high productivity water, and one fraction  
 943 with low productivity water. Our results show how in the simplest case, averaging over  
 944 the two regimes fundamentally changes the shape of the apparent mean functional re-  
 945 sponse. We show how averaging across the two patches can increase apparent mean cap-  
 946 ture rates, induce upward concavity at low  $\overline{[P]}$ , and increase the sensitivity of mean spe-  
 947 cific grazing rates to local consumption rates.

948 We assume a generic model grid cell is divided into two regimes, one fraction with  
 949 high productivity eutrophic water ( $f_{eu}$ ) and one fraction with low productivity oligotrophic  
 950 water,  $f_{ol}$  ( $f_{eu} + f_{ol} = 1$ ). All zooplankton are assumed to graze according to the same  
 951 local functional response,  $g([P])$ , but the sub-grid scale distributions of phytoplankton  
 952 ( $[P]_{eu}$ ,  $[P]_{ol}$ ) and zooplankton ( $[Z]_{eu}$ ,  $[Z]_{ol}$ ) biomass are assumed to be heterogeneous  
 953 and allowed to vary in time. The phytoplankton population is assumed to grow expo-  
 954 nentially with a different growth rate in each region ( $\mu_{ol}$ ,  $\mu_{eu}$ ). Following A. Y. Moro-  
 955 zov and Arashkevich (2010), the concentration of zooplankton biomass in either region

956 is assumed to be proportional to the distribution of phytoplankton. The concentration  
 957 of phytoplankton and zooplankton in either fraction of the grid cell ( $R = eu, ol$ ) can  
 958 then be computed at a given time as

$$[P]_R = [P]_{R,t=0}(1 + \mu_R)^t \quad (28)$$

$$[Z]_R = \theta \frac{[P]_R}{[P]}, \quad (29)$$

959 where  $[P]_{R,t=0}$  is the initial concentration and  $\theta$  is the proportionality constant for zoo-  
 960 plankton biomass. Finally, the apparent grid cell mean specific grazing rate,  $\bar{g}$ , and phy-  
 961 toplankton concentration,  $\overline{[P]}$  can be calculated as,

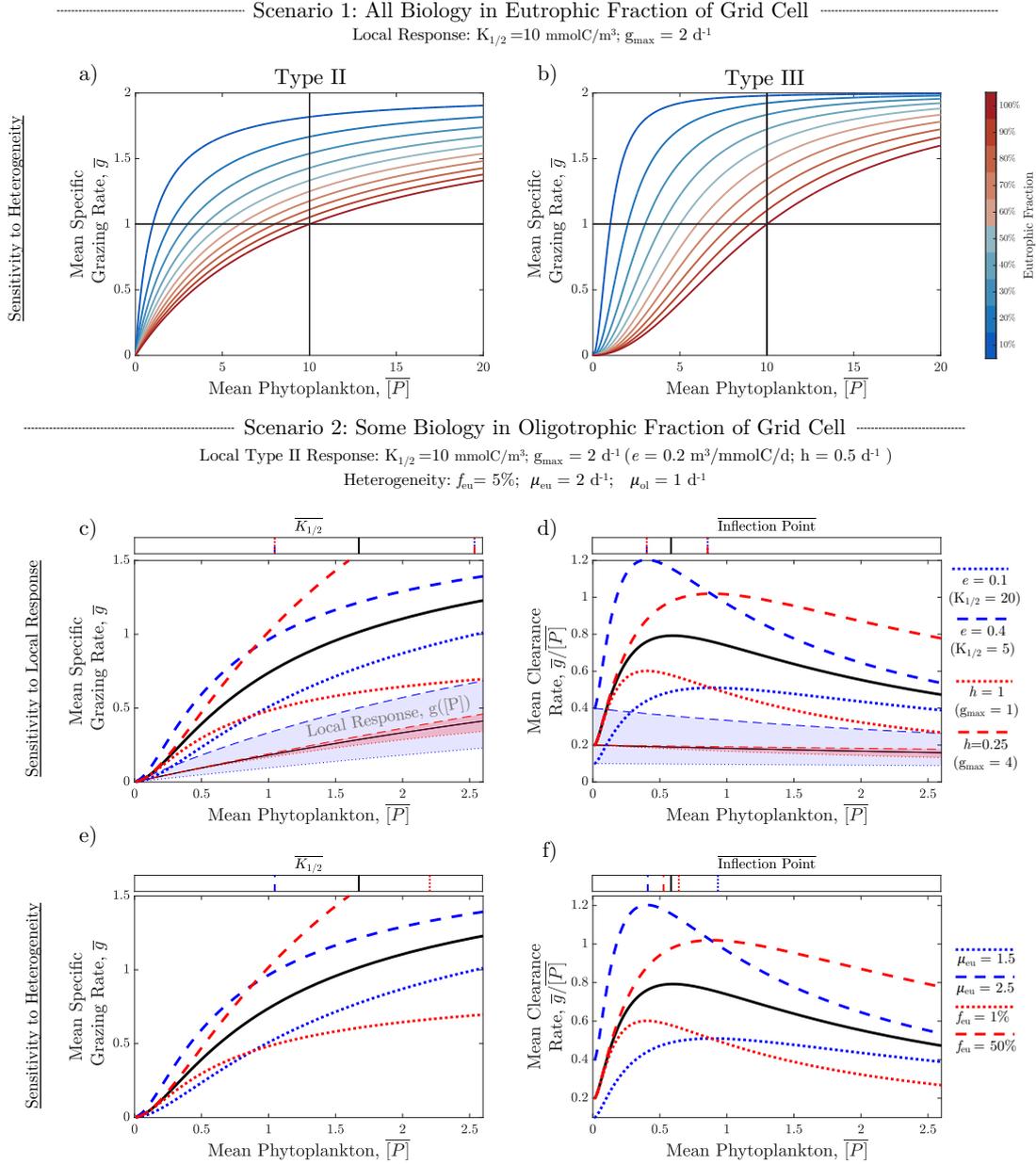
$$\overline{[P]} = (f_{eu}[P]_{eu} + f_{ol}[P]_{ol})/1 \quad (30)$$

$$\bar{g} = g([P]_{eu}) \frac{[Z]_{eu} f_{eu}}{Z_{tot}} + g([P]_{ol}) \frac{[Z]_{ol} f_{ol}}{Z_{tot}}, \quad (31)$$

962 where 1 is the area of the grid cell in nominal units and  $Z_{tot}$  is the sum of all zooplank-  
 963 ton in the grid cell (i.e.  $Z_{tot} = [Z]_{eu} * [f]_{eu} + [Z]_{ol} * [f]_{ol}$ ). Note that  $\theta$  cancels out in **eq.**  
 964 **31**. The spatially-averaged, apparent mean functional response,  $\bar{g}(\overline{[P]})$ , can then be ex-  
 965 amined by plotting all values of  $\overline{[P]}$  against  $\bar{g}$  (**Fig. 7**).

966 We consider two scenarios. In the first scenario (**Fig. 7a, b**), all biology is assumed  
 967 to be consolidated in the eutrophic fraction of the grid cell (i.e.  $[P]_{ol,t=0}$ ,  $\mu_{ol}$ ,  $[P]_{ol}$  and  
 968  $[Z]_{ol}$  all equal 0). In this scenario it does not matter what the initial concentration or  
 969 growth rate of phytoplankton in the euphotic region is because the relative distribution  
 970 is constant (i.e.  $[P]_{eu} f_{eu} / [P]_{Tot} = 1$ ) and the grid-cell mean specific grazing rate,  $\bar{g}$ ,  
 971 reduces to the local response,  $g([P]_{eu})$ . However,  $\overline{[P]}$  is less than  $[P]_{eu}$  as it is diluted  
 972 by the oligotrophic fraction. We consider a local type II (**Fig. 7a**) and type III (**Fig.**  
 973 **7b**) response. In both cases, the qualitative shape of  $\bar{g}(\overline{[P]})$  is consistent with the local  
 974 response; however, there is a decrease the half saturation concentration of  $\bar{g}(\overline{[P]})$  which  
 975 is proportional to the size of euphotic fraction of the grid cell, such that  $\overline{K}_{1/2} = f_{eu} K_{1/2}$ .  
 976 This occurs because all zooplankton are actually grazing on a phytoplankton concentra-  
 977 tion ( $[P]_{eu}$ ) that is  $1/f_{eu}$  larger than the grid cell mean. In turn, as biological produc-  
 978 tivity is consolidated into a smaller fraction of the grid cell the apparent capture rate  
 979 appears to increase (i.e. the initial slope of the curve steepens). However, this occurs not  
 980 because local capture rates increase, but because zooplankton are grazing at saturation  
 981 in a smaller area.

982 In the second scenario (**Fig. 7c-f**) we assume that all water contains at least some  
 983 biomass, but that phytoplankton population growth is faster in the eutrophic fraction.  
 984 Here, phytoplankton biomass begins uniformly distributed with an initial concentration  
 985 of  $0.01 \text{ mmolC}/\text{m}^3$ , then grows exponentially at a rate of  $2 \text{ d}^{-1}$  in the eutrophic frac-  
 986 tion and  $1 \text{ d}^{-1}$  in the oligotrophic fraction. Zooplankton biomass is still assumed pro-  
 987 portional to phytoplankton. The eutrophic fraction of the grid cell is now assumed to  
 988 be 5% and the local grazing response is a Type II disk response with  $K_{1/2} = 10$  and  
 989  $g_{max} = 2$ . We find that even though all zooplankton graze locally with a type II re-  
 990 sponse (**Fig. 7c; thin black line**),  $\bar{g}(\overline{[P]})$  exhibits upward concavity at low  $\overline{[P]}$  (**Fig.**  
 991 **7c; solid black line**), akin to a type III response. This is even clearer when looking at  
 992 mean clearance rates ( $\bar{g}/\overline{[P]}$ ). Unlike local clearance rates (**Fig. 7d; thin black line**)  
 993 which decreases monotonically, mean clearance rates (**Fig. 7d; solid black line**) ini-  
 994 tially increase, providing the same stabilizing influence as the type III response (**Sec.**



**Figure 7.** Influence of sub-grid scale heterogeneity. The spatially-averaged, apparent mean functional response is plotted for several simple examples of sub-grid scale heterogeneity. **a,b)** shows what happens if **a)** type II or **b)** III local functional response is used but biological activity is consolidated in some fraction (see colorbar) of the grid cell, with nothing in the remaining fraction. Note, the darkest red line ( $f_{eu}=1$ ) is equivalent to the local response. **c-f)** show what happens to **c,e)** the mean functional response and **d,f)** mean clearance rates (solid black lines) when the same local type II response is used but some phyto- and zooplankton growth is permitted in the oligotrophic fraction of the grid cell, but at a slower rate. Red and blue lines show the sensitivity of the mean functional response to changes in **c,d)** the local response parameters and **e,f)** degree of sub-grid scale heterogeneity. The sensitivity of the local response is shaded in the background of **c & d**. Above each subplot the location of the mean response’s half saturation concentration and inflection point is noted with the corresponding line style.

995 **3**). Note, however,  $\overline{g([P])}$  is a fundamentally different mathematical curve than the stan-  
 996 dard type III response. Its apparent mean half saturation constant ( $\overline{K_{1/2}} = 1.7$ ) is sub-  
 997 stantially lower than that of the local response ( $K_{1/2} = 10$ ) and unlike the standard type  
 998 III response,  $\overline{K_{1/2}}$  is no longer the location of the inflection point of the curve (i.e. transi-  
 999 tion from upward to downward concavity) which occurs before  $\overline{K_{1/2}}$  in  $\overline{g([P])}$  (**Fig. 7b,c**)

1000 Still, it is significant that the mean of many individual type II responses can yield  
 1001 the upward concavity associated with a type III response when averaged across hetero-  
 1002 geneously distributed plankton populations. The reason for this is that phytoplankton  
 1003 growth is associated with a shift in the relative distribution of zooplankton into the eu-  
 1004 trophic region where they can graze faster. Therefore as the mean grid cell phytoplank-  
 1005 ton concentration increases, the mean specific grazing rate will increase multiplicatively  
 1006 with an increasing proportion of zooplankton grazing at increasingly fast specific rates,  
 1007 leading to an exponential increase at low  $[P]$ . Note, that there was no upward concav-  
 1008 ity in Scenario 1, despite sub-grid scale heterogeneity. This is because the proportion of  
 1009 zooplankton grazing in the eutrophic region did not increase with  $[P]$ . Therefore, for up-  
 1010 ward concavity to exist in the mean state, we must assume that zooplankton are more  
 1011 likely to aggregate where there is more prey, either because they are growing faster lo-  
 1012 cally or because they are actively migrating. This is ecologically and numerically impor-  
 1013 tant because it can provide dynamical stability and refuge for low phytoplankton con-  
 1014 centrations without invoking any associated change in the assumptions about the for-  
 1015 aging behavior of individual zooplankton.

1016 The exact shape of  $\overline{g([P])}$  is a function the local response (**Fig. 7c,d**) and the evo-  
 1017 lution of sub-grid scale plankton distributions (**Fig. 7e,f**). Alterations to the local cap-  
 1018 ture rate (**Fig. 7c,d**; blue lines) and consumption time (red lines) show how modifica-  
 1019 tions to the local response (thin lines; shaded area) do not directly translate to the mean  
 1020 response (thick lines). As with the local response, increasing (decreasing) capture rates  
 1021 ( $\epsilon$ ) or decreasing consumption times ( $h$ ) both decrease the half saturation concentration,  
 1022  $\overline{K_{1/2}}$ , of the mean response. However,  $\overline{g([P])}$  is much more sensitive to changes in the  
 1023 consumption time compared to the local response. For the most part,  $\overline{g}$  is more sensi-  
 1024 tive to changes in  $h$  (thick red lines) than  $\epsilon$  (thick blue lines) at low  $[P]$ , despite hardly  
 1025 any change to  $g$  at low  $[P]$  (thin, shaded lines). This is possible because even at low  $[P]$ ,  
 1026 heterogeneously distributed zooplankton are predominately grazing at or near satura-  
 1027 tion in small patches, where consumption, not capture, rates drive grazing.

1028 Altering the distribution of plankton (**Fig. 7e,f**), either by increasing population  
 1029 growth rates in the eutrophic fraction (blue lines) or by changing the size of the eutrophic  
 1030 fraction (red lines) also has a pronounced effect on the shape of  $\overline{g([P])}$ . Increasing (de-  
 1031 creasing)  $\mu_{eu}$  has a qualitatively similar effect to decreasing (increasing)  $K_{1/2}$  because  
 1032 it increases the disparity between eutrophic and oligotrophic plankton populations. Re-  
 1033 ducing sub-grid scale heterogeneity by increasing (decreasing) the size of  $f_{eu}$  lowers the  
 1034 inflection point and decreases (increases) the extent of upward concavity. At  $f_{eu} = 50\%$ ,  
 1035  $\overline{g([P])}$  begins to qualitatively resemble  $g([P])$ , but  $\overline{K_{1/2}}$  is still 45% lower than  $K_{1/2}$ . Even  
 1036 when we reduced heterogeneity to 20% of the grid cell growing just 10% faster,  $\overline{g([P])}$   
 1037 still exhibited increase clearance rates at very low  $[P]$ . Together, it is clear that the shape  
 1038 of  $\overline{g([P])}$  is can dramatically diverge from  $g([P])$  but the degree to which it does is very  
 1039 sensitive to the degree of sub-grid scale heterogeneity.

1040 Considering that the evolution of natural plankton distributions is much more com-  
 1041 plex than modelled here, a more sophisticated analysis is required to understand which  
 1042 curve best begin approaches representing their mean state. However, provided there is  
 1043 sufficient heterogeneity, when compared to the local response, it appears that  $\overline{g([P])}$  should  
 1044 have faster capture rates, be more sensitive to consumption rates at low  $[P]$ , and exhibit  
 1045 a larger degree of upward concavity at low  $[P]$ .

## 1046 7 Recommendations for modellers

### 1047 7.1 Functional Response Choice for Single-Prey Grazing

1048 Biogeochemical models are largely split in their use of a type II (or Ivlev) or type  
 1049 III functional response (**Table 3**). Of all 70 surveyed grazing formulations, 23 use a type  
 1050 III and 35 use a type II (12 used an Ivlev). Of those that graze with a single-prey re-  
 1051 sponse the split is 13, 16, and 14 for type III, II and Ivlev, respectively. Mathematically,  
 1052 when parameterized with analogous parameters (i.e. the same  $K_{1/2}$  and  $g_{max}$ ), a type  
 1053 II response is more likely to exert stronger grazing pressure (**Sec. 5.2**) and produce dy-  
 1054 namically unstable solutions (**Sec. 3, 5.3**) due to its downward concavity at low prey  
 1055 concentrations. Ecologically, the most realistic option likely depends on the model con-  
 1056 figuration and the system being simulated.

1057 Models that use a type III response typically benefit from its stabilizing proper-  
 1058 ties (Gentleman & Neuheimer, 2008). For example, many models require a type III re-  
 1059 sponse to produce realistic blooms rather than unstable oscillations (Hernández-García  
 1060 & López, 2004; Malchow et al., 2005; A. Morozov, 2010; Truscott & Brindley, 1994; Tr-  
 1061 uscott et al., 1994). This is because the stabilizing properties of a type III response pre-  
 1062 vent the extinction of a very small wintertime phytoplankton seed population, while starv-  
 1063 ing the zooplankton population, subsequently permitting a bloom at the onset of rapid  
 1064 changes in bottom-up growth conditions during spring stratification (Behrenfeld et al.,  
 1065 2013; Evans & Parslow, 1985).

1066 However, stability in it's own right is not a sufficient justification to use a type III  
 1067 response. Natural systems have been observed to exhibit dynamical instabilities (Mc-  
 1068 Cauley & Murdoch, 1987) and even when they do not, there are many plausible stabi-  
 1069 lizing factors that could dominate unstable predator-prey dynamics to dampen limit cy-  
 1070 cles and stabilize the system (C. A. Edwards et al., 2000; Gentleman & Neuheimer, 2008).  
 1071 For example, only half the parameter combinations tested here actually produced a dy-  
 1072 namically unstable solution when using a type II response (**Fig. 6a,g**). This was because  
 1073 the destabilizing influence of the predator-prey dynamics (i.e. the First Order Stability;  
 1074 **Fig. 6c,i**) was weak enough to be dominated by the stabilizing influence of nutrient lim-  
 1075 itation, which buffers changes in the phytoplankton population by decreasing (increas-  
 1076 ing) division rates when the population is large (small). Similarly, other factors such as  
 1077 quadratic zooplankton mortality can create a negative feedback loop which stabilizes pop-  
 1078 ulation dynamics despite the destabilizing influence of the grazing formulation. Select-  
 1079 ing a response type that does not represent the true destabilizing (or stabilizing) influ-  
 1080 ence of natural predator-prey dynamics could lead parameter optimization schemes to  
 1081 underestimating (or overestimating) the influence other stabilizing processes. Thus, the  
 1082 stabilizing influence of a type III response is only preferable if it is ecologically represen-  
 1083 tative of the predator-prey dynamics it seeks to represent.

1084 Ecologically, there is disagreement on whether a type II (Hansen et al., 1997; Hirst  
 1085 & Bunker, 2003; Jeschke et al., 2004) or type III (Chow-Fraser & Sprules, 1992; Frost,  
 1086 1975; Gismervik & Andersen, 1997; Sarnelle & Wilson, 2008) response is more appro-  
 1087 priate to represent the grazing behavior of individual zooplankton. Laboratory dilution  
 1088 experiments are often better fit empirically by a type II response (Hansen et al., 1997;  
 1089 Hirst & Bunker, 2003), while a type III response is typically justified by more complex  
 1090 behavior, such as changes in prey refuge, (Wang, Morrison, Singh, & Weiss, 2009), preda-  
 1091 tor learning (Holling, 1965; van Leeuwen, Jansen, & Bright, 2007), predator effort, (Gis-  
 1092 mervik, 2005), or prey switching (Gentleman et al., 2003; Oaten & Murdoch, 1975; Uye,  
 1093 1986). Unfortunately, this behavior is difficult to replicate in a lab (Leising et al., 2003)  
 1094 and large-scale field experiments are challenging and rare.

1095 However, despite uncertainty in the true behavior of individual zooplankton in their  
 1096 natural environment, it is possible that a type III response is more representative of their

mean state, even if individuals are assumed to exhibit a sub-grid scale type II response (Sec. 6). If plankton are assumed to be heterogeneously distributed and the relative distribution of the zooplankton population is assumed to co-vary with the phytoplankton population, then the mean grazing rate should generally exhibit some degree of upward concavity (Fig. 6c,e) and exert an associated stabilizing influence on mean population dynamics (Fig. 6d, f). A. Morozov (2010) found similar upward concavity in the mean dynamics of vertically distributed plankton and argued for the emergence a Holling type III response. However, it should be clarified that while the mean behavior of heterogeneous systems likely does exhibit some upward concavity, the function is not exactly sigmoidal in shape and is mathematically distinct from a type III disk response. Importantly, the mean response becomes destabilizing (i.e. downwardly concave) well before the half-saturation concentration of the local response (Fig. 6a,b) and varies with the degree of sub-grid scale heterogeneity (Fig. 6c,d).

In turn, the most ecologically justifiable response type may depend on the resolution of the model in question. For high resolution, small scale models, or those representing system known to be well-mixed, a type II response is likely the most appropriate. Even though laboratory incubations are unlikely to translate directly to zooplankton feeding behavior in the open ocean (Dutkiewicz et al., 2015), there are not sufficient observations individual zooplankton grazing with type III dynamics to justify ignoring the many empirical estimates of a type II response (Hansen et al., 1997; Hirst & Bunker, 2003). However, a type III response may be a more ecologically realistic representation of the mean state of many zooplankton grazing locally with a type II response on a highly heterogeneous phytoplankton population. Therefore, for coarse resolution, large scale models (e.g. global earth systems models) a type III response may be more appropriate.

## 7.2 Parameter Scheme for Single-Prey Grazing

Throughout the literature, the type II and type III functional response appear in two distinct, but mathematically equivalent, forms (Table 2): the disk parameter scheme (eq. 17, 24) (Adjou et al., 2012; Fasham, 1995; Law et al., 2017; Oke et al., 2013; Schartau & Oschlies, 2003b) and the Michaelis–Menten parameter scheme (eq. 19, 25) (Aumont & Bopp, 2006; Dutkiewicz et al., 2015; Hauck et al., 2013; Le Quéré et al., 2016; Moore et al., 2013; Stock, Dunne, & John, 2014; Totterdell, 2019; Vichi et al., 2007). Both parameter schemes can describe identical response curves given the right parameterization, but use different information to do so. The disk scheme uses ecologically significant quantities to mechanistically determine how grazing rates vary in well-mixed systems. On the other hand, the Michaelis–Menten scheme is an empirical description of the shape of the curve, with no theoretical basis, per say. This distinction would be irrelevant if we had robust knowledge of the real parameters or infinite computational power to sample them all in multivariate parameter optimization schemes. Unfortunately, observations span several orders of magnitude (Section 4) and computational limitations exist (Matear, 1995; Neelin, Bracco, Luo, McWilliams, & Meyerson, 2010), meaning that modellers must pick a limited subset of parameters to test and the parameter scheme they choose may influence this choice.

The disk scheme has a strong theoretical basis and allows modellers to directly prescribe biologically meaningful quantities. In general, this is the simplest way to reduce confusion amongst biologist and modellers and ensure that trait-based relationships are correctly parameterized between functional groups (see Sec. 4). However, the theoretical integrity of the disk response is limited to well-mixed systems and does not necessarily represent the mean state of a patchy ocean, which coarse global models must implicitly average over. In Section 6, we demonstrated how the apparent mean functional response,  $\overline{g([P])}$ , can differ significantly from the local response,  $g([P])$  (Fig. 7). When  $\overline{g([P])}$  is plotted empirically by explicitly averaging across sub-grid scale heterogeneity, it is clear that the characteristics of the mean response diverge from the theoretical ba-

1149 sis of the disk parameters, even as they describe how zooplankton graze locally. For ex-  
 1150 ample, decreasing local zooplankton consumption times ( $h = 1/g_{max}$ ) can substantially  
 1151 increase the grid cell mean grazing rate at low  $\overline{[P]}$ , without meaningfully influencing how  
 1152 zooplankton graze locally on low  $[P]$ , where grazing rates remain dominated by capture  
 1153 rates (**Fig. 7c**). This is possible because a disproportionate amount of zooplankton are  
 1154 grazing at a prey density closer to saturation than the mean phytoplankton concentra-  
 1155 tion, which is diluted by large swaths of oligotrophic water, would suggest. Therefor, when  
 1156 modelling the mean state of a sufficiently heterogeneous region the most ecologically jus-  
 1157 tifiable functional response is necessarily empirical, as it must capture the local grazing  
 1158 dynamics as governed by the disk parameters as well as the evolving sub-grid scale dis-  
 1159 tribution of zooplankton and phytoplankton.

1160 This distinction is important to allow parameter search algorithms to best select  
 1161 for the most ecologically representative parameter values. For example, if running a ge-  
 1162 netic parameter optimization algorithm in a low mean biomass biome, then a mutation  
 1163 to the  $g_{max}$  gene (i.e. parameter) will not significantly influence the fitness of the solu-  
 1164 tion (and thus not be selected for or against) when using a disk scheme. This is the de-  
 1165 sired, theoretically correct, outcome if the system you are modelling is believed to be well-  
 1166 mixed, because grazing rates (and thus phytoplankton dynamics) should be limited by  
 1167 capture rates, not consumption times, when food is scarce. However, if the system is as-  
 1168 summed to have a sufficient degree of sub-grid scale heterogeneity, with zooplankton dis-  
 1169 proportionately consolidated in small patches where they can graze closer to saturation,  
 1170 then  $g_{max}$  should influence population dynamics and thus the fitness of the solution. There-  
 1171 for, the parameters of  $\overline{g([P])}$  should reflect not just assumptions regarding local consump-  
 1172 tion and capture rates, but also assumptions about the sub-grid scale distribution of biomass.  
 1173 In this way, the Michaelis–Menten parameter scheme may offer an advantage, as it is al-  
 1174 ready empirical in nature. For instance, changes to  $g_{max}$  in a Michaelis–Menten scheme  
 1175 have a significantly heightened influence on grazing rates (relative to a disk scheme) at  
 1176 low prey concentrations. This would allow for a genetic search algorithm to better se-  
 1177 lect for the true  $g_{max}$  which best describes  $\overline{g([P])}$ . Critically though, this  $g_{max}$  param-  
 1178 eter should not be understood as the reciprocal of the consumption time (as in a disk  
 1179 scheme) but as an empirical reflection of the combined effect of the local disk paramet-  
 1180 ers and sub-grid scale heterogeneity.

1181 Another advantage of the Michaelis–Menten scheme is that population dynamics  
 1182 are more sensitive to proportional changes in its parameters, compared to the disk pa-  
 1183 rameters, particularly for a type III response (**Section 5.2**). This is predominately be-  
 1184 cause  $\epsilon_c$  implicitly varies with the square of  $K_{1/2}$  in a Michaelis-Menten scheme ( $\epsilon_c =$   
 1185  $\frac{g_{max}}{K_{1/2}^2}$ ). In turn, the disk scheme is less sensitive to its parameterization, meaning it re-  
 1186 quires a larger range of parameters to be tested to cover the same range of solutions. For  
 1187 example, a conservative range of observed  $\epsilon_c$  values, from .0001-1  $\frac{m^6}{mmolC^2d}$ , can be span  
 1188 with  $K_{1/2}$   $\frac{mmolC}{m^3}$  values from 1-100 at a fixed  $g_{max}$  (see contours on **Fig. 2**). The trade  
 1189 off is increased precision in the disk scheme; however, the overwhelming lack of consen-  
 1190 sus on what these parameters actually are (**Section 4**), especially for the mean state of  
 1191 the entire ocean (Moriarty et al., 2013; Moriarty & O’Brien, 2012), suggests that it is  
 1192 more valuable to consider a wider, but lower resolution, set of parameters to avoid in-  
 1193 advertently constraining the parameter space, rather than trying to narrow in on an im-  
 1194 possibly exact value. For example, the parameter search used by Schartau and Oschlies  
 1195 (2003a), who use a disk scheme to represent the mean state of relatively coarse grid cells,  
 1196 chose both parameter values at the boundary of their search space, suggesting a wider  
 1197 range might have found a better solution. Practically speaking, this problem could be  
 1198 addressed by careful conversion. Modellers using a disk scheme could sub sample a wider  
 1199 set of coarser resolution  $\epsilon_c$  values in optimization search schemes; however, modellers must  
 1200 select a search range for dozens, if not hundreds, of parameters, and are less likely to mis-  
 1201 takenly constrain the parameter space if using a Michaelis-Menten scheme, which has  
 1202 a narrower range of realistic parameters and much more intuitive units.

1203 Together, the mechanistic and empirical nature of the disk and Michaelis-Menten  
 1204 parameter schemes should be used intentionally to modeller’s advantage, depending on  
 1205 whether they are trying to mechanistically represent the behavior of zooplankton in a  
 1206 well-mixed system or empirically represent the mean state of grazing at the mean phy-  
 1207 toplankton concentration of a patchy grid cell. Thus a disk scheme should be used in smaller  
 1208 scale, higher resolution models, in which the biological attributes of zooplankton are rel-  
 1209 atively well understood. This allows know, measured values, of  $\epsilon$  and  $h$  to be directly  
 1210 prescribed and reduces the chance of inadvertently mis-parameterizing their relationship  
 1211 in a Michaelis–Menten scheme. However, a Michaelis–Menten scheme may be more ap-  
 1212 propriate to represent the mean state of a patchy ocean in lower resolution, larger scale  
 1213 models, in which the true parameter values are not well know. This affords the empir-  
 1214 ical flexibility to account for differences in the system as a whole, not just the local dy-  
 1215 namics, which may allow parameter search algorithms to better select for the true ap-  
 1216 parent mean response, which is a necessarily empirical relationship averaging over the  
 1217 effects of many distinct processes, including consumption rates, capture rates, zooplank-  
 1218 ton migration, sub-mesoscale nutrient enhancement, and more.

### 1219 7.3 Parameter Search Range for Single-Prey Grazing

1220 Given the uncertainty in empirically estimated parameter values, it is necessary to  
 1221 select what range of parameters to test in optimization routines. Although there is a high  
 1222 degree of variability in both all parameter values (**Fig. 3; Table 3**), there is more un-  
 1223 certainty in the correct value of  $K_{1/2}$ , or associated attack rates in a disk scheme. Com-  
 1224 pared to  $K_{1/2}$ , the value of  $g_{max}$  is better constrained by size (**Sec. 4.1**), more consis-  
 1225 tent between models and observations (**Sec. 4.2**), and less influential on driving phy-  
 1226 toplankton population dynamics (**Section 5.2**). In turn, parameter search schemes should  
 1227 favor testing on a larger range of  $K_{1/2}$  values than  $g_{max}$  values when resource limited.  
 1228 However, it is reasonable to ask how large a range is appropriate, lest implicitly impos-  
 1229 ing ecologically unrealistic prey capture rates or selecting values of fringe functional groups  
 1230 to represent the mean state. However, there are insufficient empirical, ecological, and math-  
 1231 ematical arguments to heavily restrict the range of grazing parameters, and  $K_{1/2}$  val-  
 1232 ues as low as  $0.1 \left(\frac{mmolC}{m^3}\right)$  and as high as  $100 \left(\frac{mmolC}{m^3}\right)$  should be considered.

1233 Empirically, reported estimates of  $K_{1/2}$  and  $g_{max}$  fit to a type II response function  
 1234 by Hansen et al. (1997); Hirst and Bunker (2003) combine to yield a range of  $\epsilon$  that spans  
 1235 4 orders of magnitude, from .003 to  $10 \frac{m^3}{mmolC \cdot d}$  (**Section 3.1; Fig. 2**). Moreover, if a  
 1236 type III response had been assumed,  $K_{1/2}$  estimates would remain similar while the range  
 1237 of  $\epsilon_c$  would increase to nearly 7 orders of magnitude, from .00001 to  $21 \frac{m^6}{mmolC^2 \cdot d}$ , or roughly  
 1238 1 order of magnitude slower and 3 orders of magnitude faster than the range tested in  
 1239 the parameter optimization search of Schartau and Oschlies (2003a) ( $0.00056 < \epsilon_c <$   
 1240  $.0364$ ). At the species level, the range of plausible  $K_{1/2}$  values appears largely uncon-  
 1241 strained by empirical estimates of  $\epsilon_c$ .

1242 Ecologically, we simply do not have a firm understanding of how myriad complex  
 1243 interactions combine across innumerable zooplankton species and evolve over time to yield  
 1244 a reasonable approximation of the mean state. For instance, juvenile zooplankton have  
 1245 different metabolic rates (Clerc, Aumont, & Bopp, 2021) and graze with  $K_{1/2}$  an order  
 1246 of magnitude smaller than adults (Hirst & Bunker, 2003; Richardson & Verheye, 1998),  
 1247 suggesting the apparent  $K_{1/2}$  of the community could be substantially lower during spawn-  
 1248 ing events. On the other hand, filter feeders, such as salps and larvaceans, that are typ-  
 1249 ically common in low chlorophyll waters, have a much smaller  $K_{1/2}$  than euphausiids and  
 1250 copepods that graze in high chlorophyll waters (Hansen et al., 1997; Hirst & Bunker, 2003).  
 1251 If species with slower  $K_{1/2}$  values dominate in more productive ecosystems, such that  
 1252  $K_{1/2}$  increases with chlorophyll (Chen et al., 2014), that would effectively raise the ap-  
 1253 parent global mean  $K_{1/2}$  value. In turn, the community-wide  $K_{1/2}$  value probably varies  
 1254 spatially and temporally depending on the zooplankton community present and whether

1255 it is dominated by juveniles or adults, such that the mean state of a population with shift-  
 1256 ing age and species distributions could have an apparent  $K_{1/2}$  value much different than  
 1257 any individual within.

1258 Mathematically, it is not just the ecosystem complexity that is poorly resolved in  
 1259 models, but also its spatial heterogeneity. If the phytoplankton density the average zoo-  
 1260 plankton experiences is larger than the grid cell mean, which is averaged across many  
 1261 square kilometers of implicitly less productive water (J. Campbell, 1995; Druon et al.,  
 1262 2019) then the  $K_{1/2}$  value of the mean response will appear much lower than that which  
 1263 the zooplankton are actually grazing at (**Fig. 7a, b**). This further increases the range  
 1264 of possible  $K_{1/2}$  values below even the fastest prey capture rates inferred from dilution  
 1265 experiments with homogeneous phytoplankton concentrations.

1266 Although the full range of empirically observed  $K_{1/2}$  values ( $0.1\text{-}71\text{ mmolC/m}^3$ )  
 1267 is likely larger than the range of plausible values to represent the mean state, this only  
 1268 applies to the mean value of individuals in well-mixed incubation experiments. Uncer-  
 1269 tain ecological complexities and spatial heterogeneity both work to expand the range of  
 1270  $K_{1/2}$  values that plausibly could represent the mean state of myriad dynamics across a  
 1271 patchy ocean. We thus recommend testing a broad range of  $K_{1/2}$  values, particularly on  
 1272 the lower end, in parameter optimization routines.

#### 1273 **7.4 Recommendations for future models**

1274 Biogeochemical models are evolving to include an increasingly complex representa-  
 1275 tion of phytoplankton, including dozens of functional groups (Follows & Dutkiewicz, 2011),  
 1276 variable composition Smith et al. (2015), and the flexibility to adapt to changing envi-  
 1277 ronments (Anugerahanti, Kerimoglu, & Smith, 2021). With these changes must come  
 1278 similar advances in the representation of zooplankton and zooplankton grazing. Notably,  
 1279 it is essential that the mean parameterization of the zooplankton field be able to respond  
 1280 to the evolving phytoplankton field to reflect that different zooplankton eat different things  
 1281 and do so at different rates. Already, many modern models include multiple zooplank-  
 1282 ton functional groups (Le Quéré et al., 2016; Stock et al., 2020) and multiple-prey graz-  
 1283 ing response (Aumont et al., 2015; Yool et al., 2021). Moving forward, it is important  
 1284 to consider how insights into the single-prey response extend to more complex grazing  
 1285 schemes.

1286 One concern is that the Michaelis-Menten form of the multi-prey response is over  
 1287 parameterized, requiring an extra parameter to describe the same equation as the cor-  
 1288 responding disk form (Gentleman et al., 2003). In turn, the parameterization of the im-  
 1289 plied single-prey response cannot be prescribed directly, but becomes a function of prey  
 1290 preference and the preference weighted  $K_{1/2}$  used for bulk ingestion. If not careful, this  
 1291 could confuse the interpretation of parameter values and lead modellers to prescribe un-  
 1292 intended single-prey dynamics that may imply inappropriate relationships between func-  
 1293 tional groups. Despite recommendations to parameterize the attributes of the multi-prey  
 1294 response directly with a disk scheme (Gentleman et al., 2003), 29 of 30 multi-prey graz-  
 1295 ing formulations surveyed here used a Michaelis-Menten scheme, and none used a disk  
 1296 (**Table 2**). To help assess if this has influenced their parameterization, we compared the  
 1297 implied single-prey response of micro- and meso-zooplankton grazing on their most preferred  
 1298 prey and compared them to those directly parameterized in single-prey formula-  
 1299 tions. In multi-prey formulations the median implied single-prey  $K_{1/2}$  value decreases  
 1300 from 7.7 in microzooplankton to 4.0 in mesozooplankton. This is qualitatively inconsis-  
 1301 tent with the observed relationship (**Table 3**) as well as single-prey formulations in which  
 1302 the median  $K_{1/2}$  value increases from 2.4 in microzooplankton to 9.1 in mesozooplank-  
 1303 ton. This suggests the models using a Michaelis-Menten multi-prey response may be im-  
 1304 plying unintended allometric relationships between functional groups grazing in their op-

1305 timal conditions and highlights that modeller's who select a Michaelis-Menten multi-prey  
1306 response must carefully consider the implied relationships between parameter values.

1307 Finally, future work is needed to better assess the shape of the apparent mean func-  
1308 tional response, both in-situ and in models. Higher resolution general circulation mod-  
1309 els are known to modify local biogeochemical distribution via their representation of nu-  
1310 trient transport (Harrison, Long, Lovenduski, & Moore, 2018). While it is intractable  
1311 to estimate the apparent mean functional response exactly, it would be useful to better  
1312 understand its attributes with deliberate experiments designed to empirically average  
1313 across high resolution biogeochemical models into coarser grid-cells representative of stan-  
1314 dard global earth systems models. This may help constrain the functional response curve  
1315 and range of parameter values beyond what has been observed for individual well-mixed  
1316 zooplankton towards a better understanding of how to represent unresolved process across  
1317 the entire system which could influence sub-grid scale heterogeneity.

## 1318 7.5 Implications for other models

1319 We focus on grazing in marine biogeochemical models, but these recommendations  
1320 apply to a much broader range of marine and terrestrial ecological models. Most mod-  
1321 els in marine and terrestrial systems that involve predator-prey interactions use type I,  
1322 type II or type III functional responses. We found that when trying to implicitly rep-  
1323 resent sub-grid scale heterogeneity, a type III (**Section 6.1**) Michaelis-Menten response  
1324 (**Section 6.2**) parameterized with a lower than-expected  $K_{1/2}$  value (**Section 6.3**) may  
1325 be a more ecologically realistic way to describe the mean state of patchy predator and  
1326 prey populations, even if individual interactions are best described by a type II disk re-  
1327 sponse, parameterized with higher  $K_{1/2}$  values. In the ocean, this would apply to most  
1328 higher trophic levels simulated in size spectrum (Blanchard, Heneghan, Everett, Trebilco,  
1329 & Richardson, 2017; Heneghan et al., 2020), population (Alver et al., 2016), ecosystem  
1330 (Audzijonyte et al., 2019; Butenschön et al., 2016) and fisheries models (Maury, 2010;  
1331 Tittensor et al., 2018, 2021). Fish, for instance aggregate in schools and feed on sparse,  
1332 but consolidated, patches of prey. These distribution are in turn reflected in global fish-  
1333 ing effort (Kroodsma et al., 2018). On land, plants and animals are also patchy in time  
1334 and space, with high prey concentration rare. Most abundance data for marine and ter-  
1335 restrial species are overdispersed and/or have an excess of zeros, implying there is a long  
1336 tail to the right of low abundances (H. Campbell, 2021). The mean state of any of these  
1337 systems, is likely best represented by a low- $K_{1/2}$ , type III, Michael-Menten response; how-  
1338 ever, the range of possible  $K_{1/2}$  considered should increase with the number of unique  
1339 species, interactions, and stages of life history being averaged into individual pools.

1340 On the other hand, well understood interactions in well mixed systems, may be bet-  
1341 ter represented by a type II disk response, provided there is a low amount of implicit av-  
1342 eraging at the species and spatial level. At the species level, this may include models of  
1343 simple systems with fewer species, such as lakes or polar regions rather than rain forests  
1344 or coral reefs, or models of more complex systems, but with many explicitly resolved preda-  
1345 tor groups. At the spatial level, this may include the oligotrophic gyres in the ocean and  
1346 grasslands or boreal forests on the land. Still, modellers should consider how much im-  
1347 plicit averaging is baked into their model and consider if it warrants a more empirical  
1348 approach before choosing a mechanistic framework (disk) or response type (II) better  
1349 suited for homogeneously distributed systems.

## 1350 8 Conclusions

1351 In marine biogeochemical and ecological modelling, the transfer of carbon and nu-  
1352 trients between trophic groups, particularly from phytoplankton to zooplankton via graz-  
1353 ing, is typically represented with one of two functional response curves. However, we find  
1354 that there is little consensus across biogeochemical models regarding: **I**) which response

1355 type to use (II vs. III); **II**) whether to describe that curve with mechanistic (disk scheme)  
 1356 or empirical parameters (Michaelis-Menten scheme); and **III**) what parameter values to  
 1357 use.

1358 We examine the single-prey formulation of the functional response in systematic  
 1359 detail to provide theoretical clarity, assess the agreement between observed parameters  
 1360 and those used in models, examine the sensitivity of the response to its parameteriza-  
 1361 tion, and explore how the shape of the curve changes when averaged explicitly over sub-  
 1362 grid scale heterogeneity. Collectively, we recommend using a type II disk response in mod-  
 1363 els with smaller scales, finer resolution, and or well understood ecological interactions.  
 1364 However, we suggest that a type III Michaelis-Menten response may be more appropri-  
 1365 ate for models with larger scales, coarser resolution, and more complex ecological and  
 1366 physical processes implicitly being averaged across. In both scenarios, a large range of  
 1367 parameter values should be tested in parameter optimization schemes as the interquar-  
 1368 tile range of empirically observed values spans roughly an order of magnitude for all pa-  
 1369 rameters, and the full range spans 3-4. Moreover, averaging across sub-grid scale het-  
 1370 erogeneity could lead to  $K_{1/2}$  values well below the mean of empirically estimated val-  
 1371 ues obtained from experiments in well-mixed solutions. These recommendations are specif-  
 1372 ically tailored to the single-prey grazing formulation in marine biogeochemical models,  
 1373 but also apply to any effort to describe the mean state of multiple interactions across  
 1374 a large grid cell with populations assumed to have heterogeneous sub-grid cell distribu-  
 1375 tions.

## 1376 Data Access

1377 All code required to run all four NPZ models and compute the relevant diagnos-  
 1378 tics from **Section 5** (PO\_Rohr\_NPZ\_Models.m) and run the theoretical experiments on  
 1379 sub-grid scale heterogeneity from **Section 6** (PO\_Rohr\_Subgrid\_Heterogeneity.m) is hosted  
 1380 on the CSIRO data portal and can be found at *DOI PENDING*. Please contact tyler.rohr@csiro.au  
 1381 for any further data access inquiries.

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