



# Automatic error-term separation approach in InSAR time-series analysis and application to Arima-Takatsuki fault zone, western Japan

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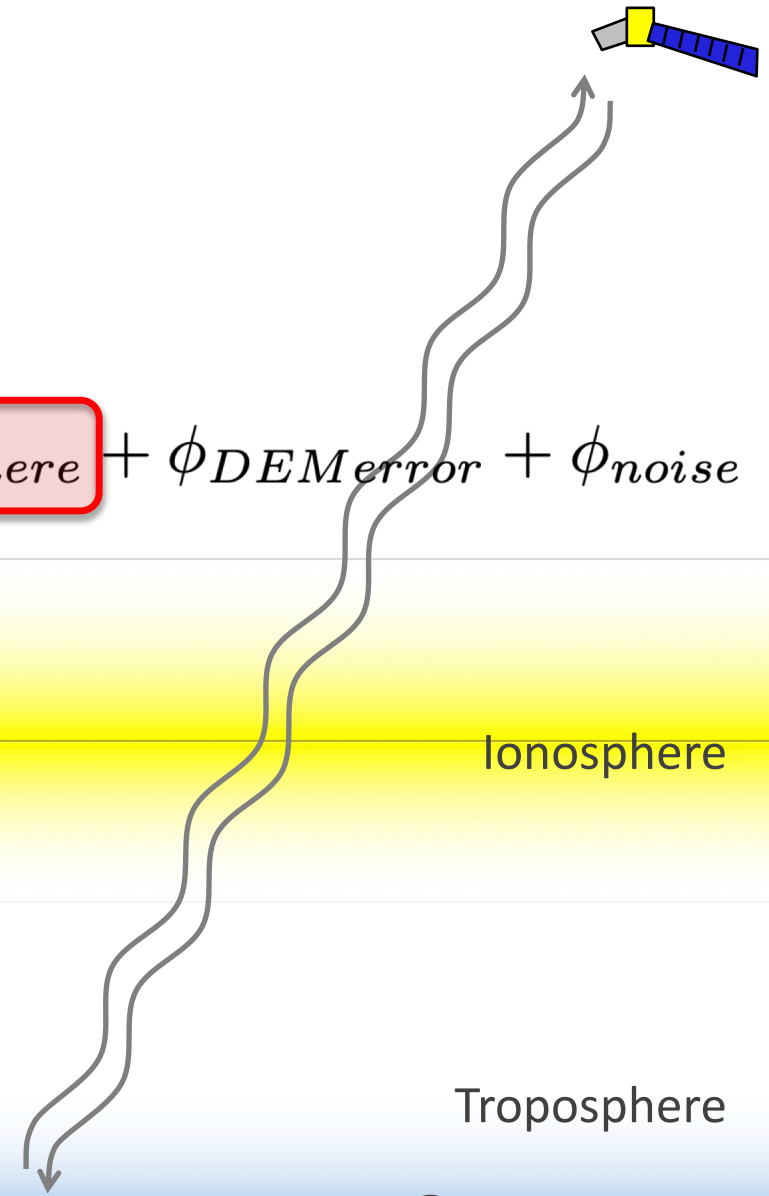
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# “Noise” terms in InSAR

Observed phase of an interferogram:

$$\phi_{\text{observation}} = \phi_{\text{deformation}} + \phi_{\text{offset}} + \phi_{\text{orbit}} + \phi_{\text{ionosphere}} + \phi_{\text{troposphere}} + \phi_{\text{DEMerror}} + \phi_{\text{noise}}$$

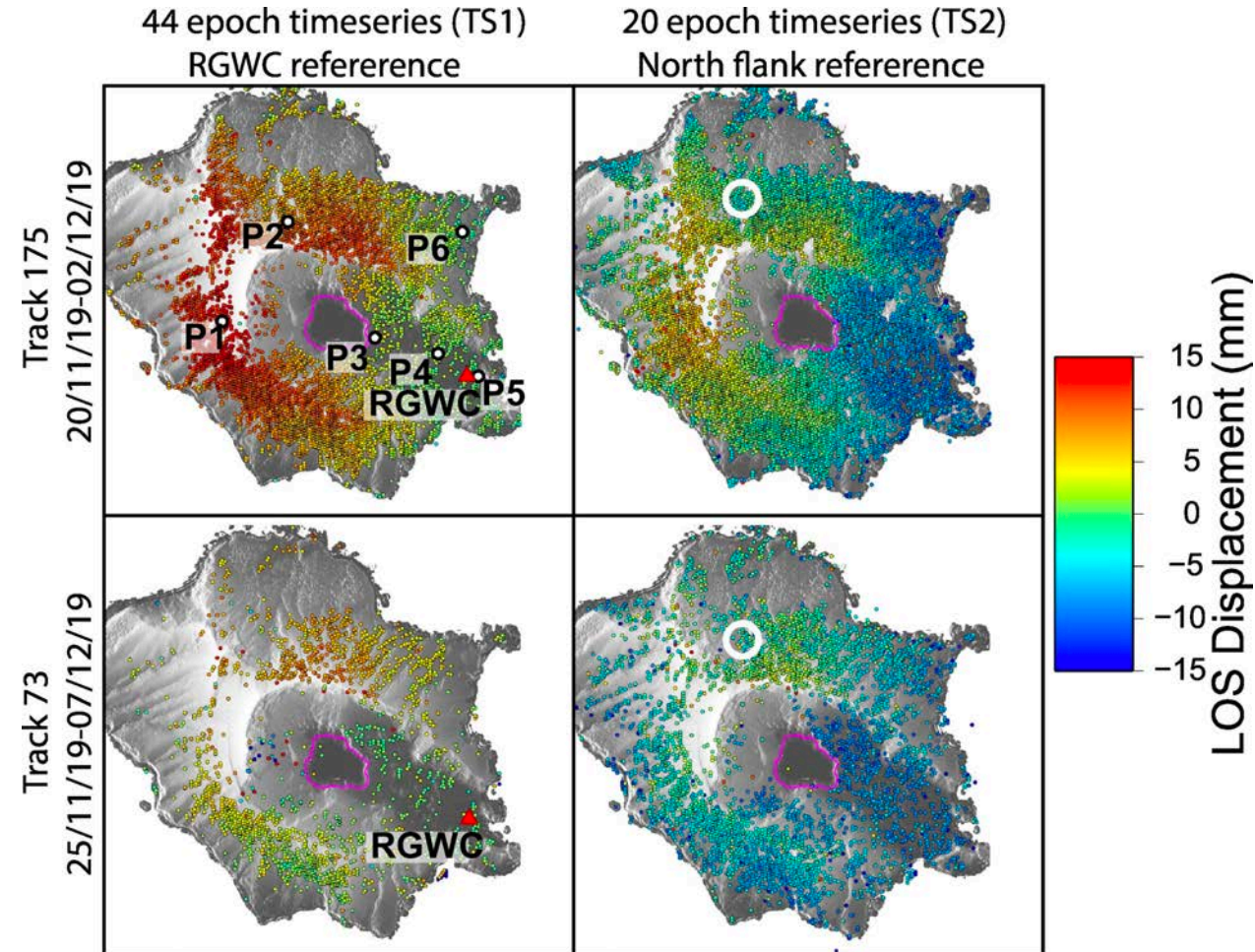
can often be problematic





# Problem of reference location selection in InSAR time-series analysis

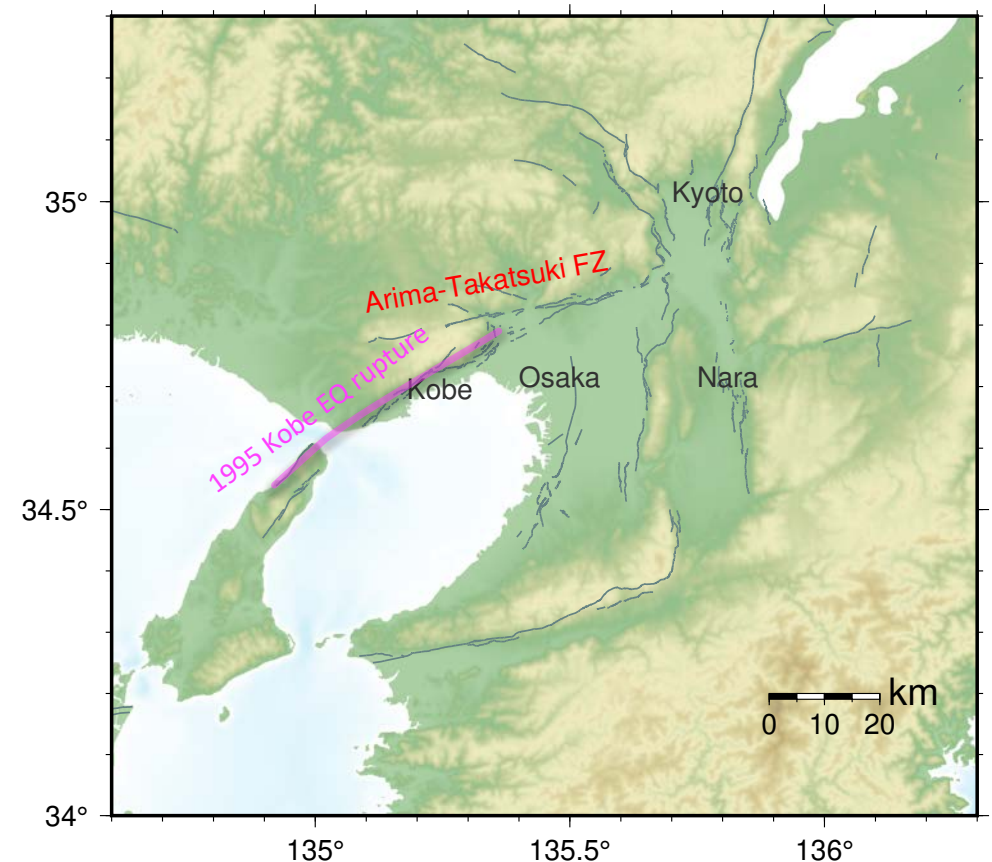
Problematic if the reference point was actually moving and/or the location was affected by atmospheric noise.



Hamling and Kilgour (2021)

# Purpose

- By adopting **De-Noising while solving for Time-Series (DeNTiS)** approach, this study derives InSAR displacement time-series while automatically minimizing other noise components
- Apply the DeNTiS algorithm on Osaka plain area, in which Arima-Takatsuki Fault Zone (ATFZ) is located.
- About ATFZ:
  - Located north of the 1995 Kobe earthquake (M7.2) rupture fault
  - Right-lateral
  - Ruptured in 1596 (M~7.5, slip ~ 3m)



# DeNTiS Algorithm

Essence: Small-baseline analysis, solve for velocity time-series and noise components (coefficients of linear functions) with regularization.

(Based on Fukushima et al., 2019, EPS, doi: 10.1186/s40623-019-1096-5)

For the  $i$ -th interferogram,  $m$ -th time step, and  $k$ -th pixel:

## Observation Equations

$$d_{i,k} = d_{i,k}^{deform} + d_{i,k}^{error}$$

$$d_{i,k}^{deform} = \mathbf{g}_i \mathbf{v}_k$$

Topography ↓

$$d_{i,k}^{error} = \underline{a_i + b_i x_k + c_i y_k + \dots + f_i h_k}$$

↑ Can be any order of polynomials

+

## Regularization Equations

$$\sum_m (v_{m,k} \Delta t_{m,k}) = \bar{v}_k \sum_m (\Delta t_{m,k})$$

$$\sum_m v_{m,k} = 0$$

↑ Const. velocity  
(NSBAS, LiCSBAS)

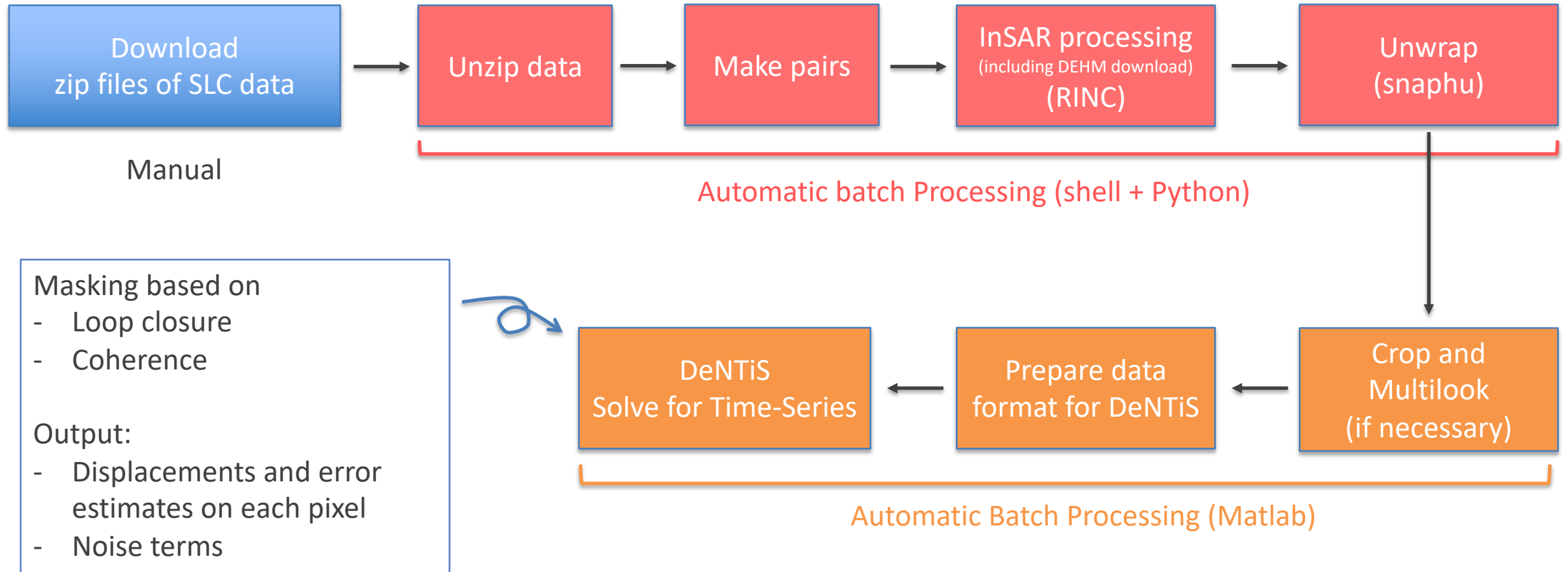
↑ Min. cumulative velocity (only 1<sup>st</sup> step)

※ Weights of these regularization are made small enough

1<sup>st</sup> step: Estimate the noise terms from subsampled points

2<sup>nd</sup> step: px-by-px inversion on denoised ifgs.

# Analysis Flow





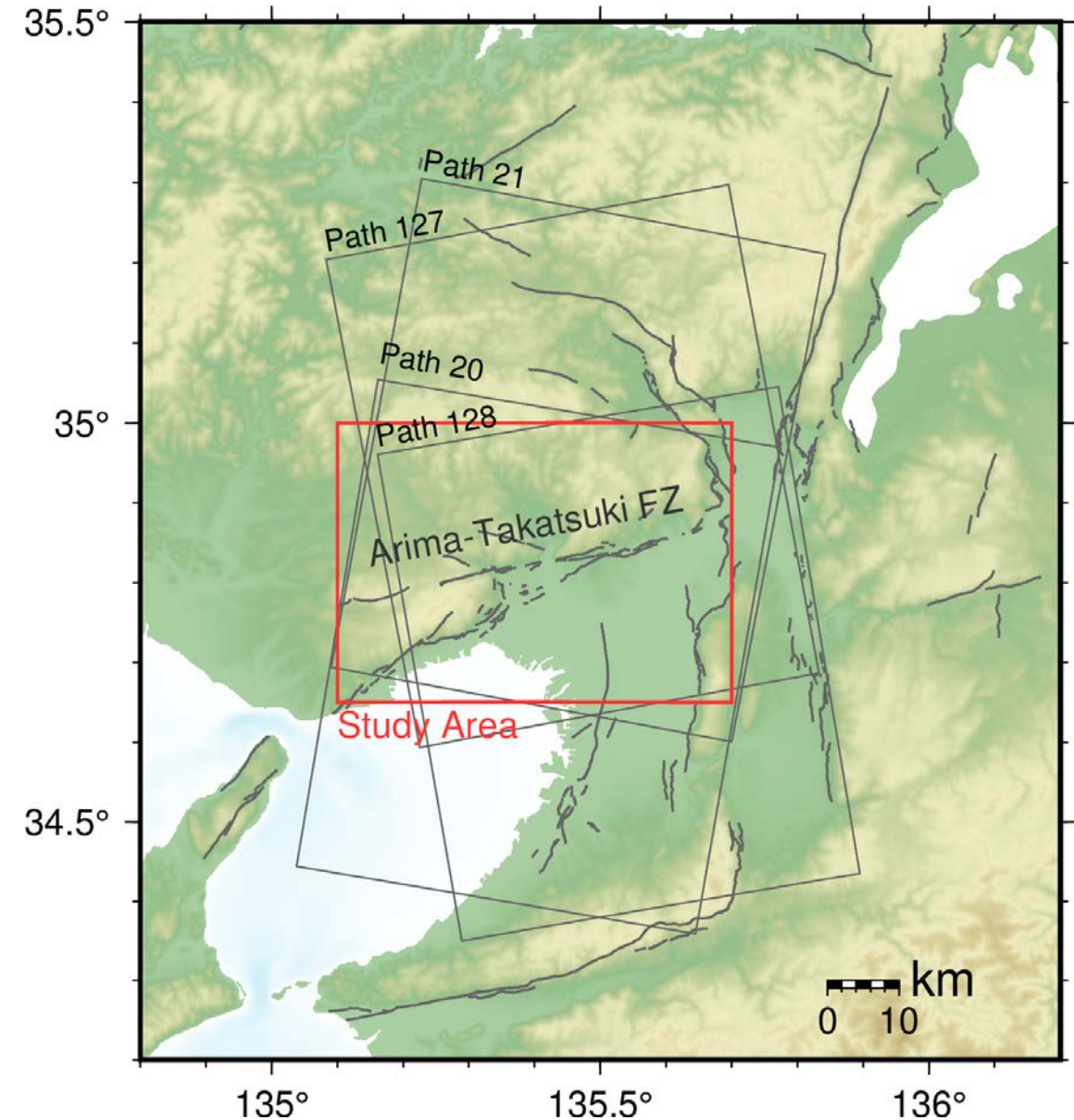
# Data

ALOS-2, Ultra-Fine-Beam Mode (SM1)

Acquired betw. Aug 2014 – Mar 2021

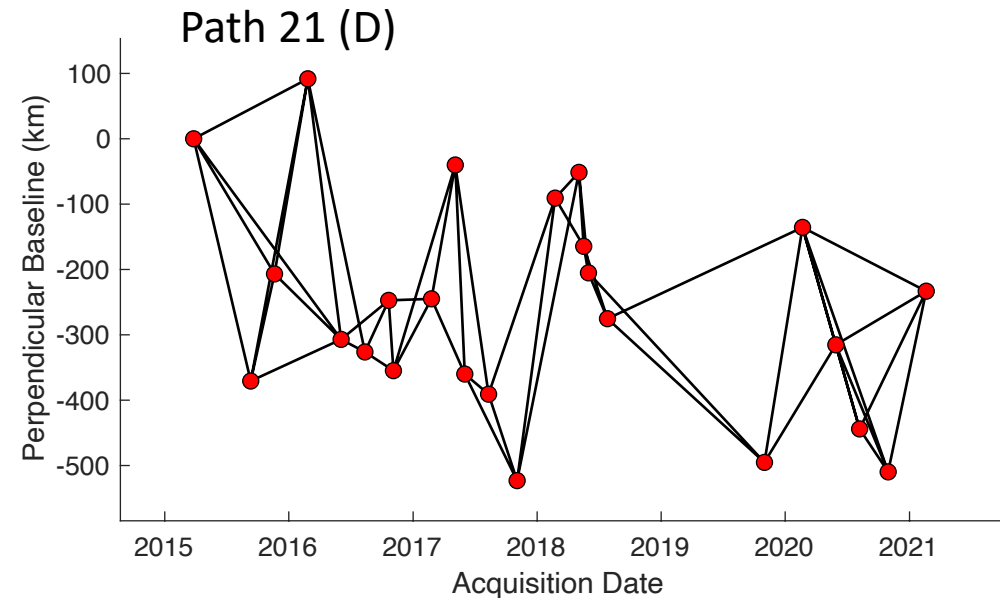
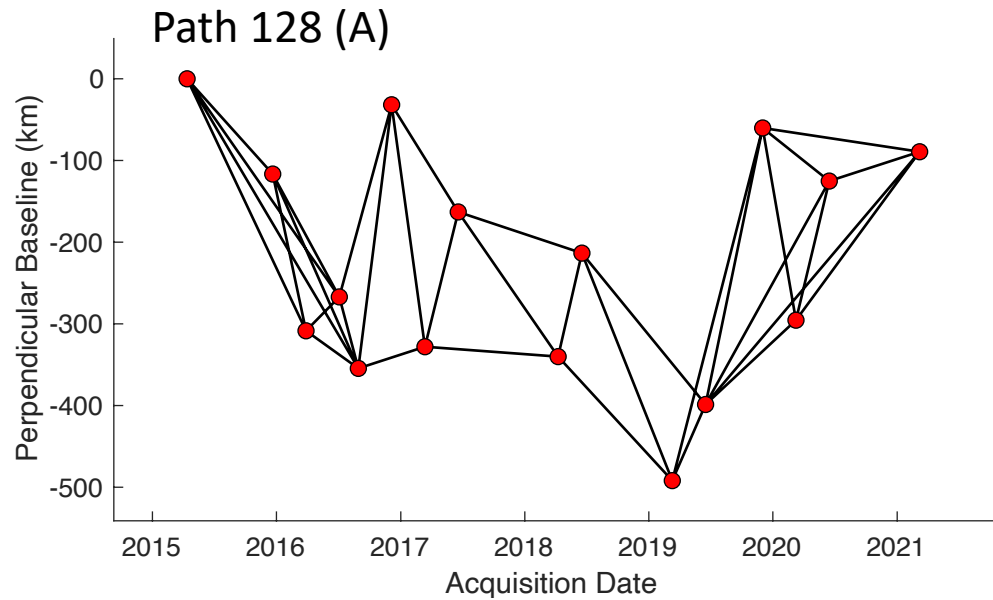
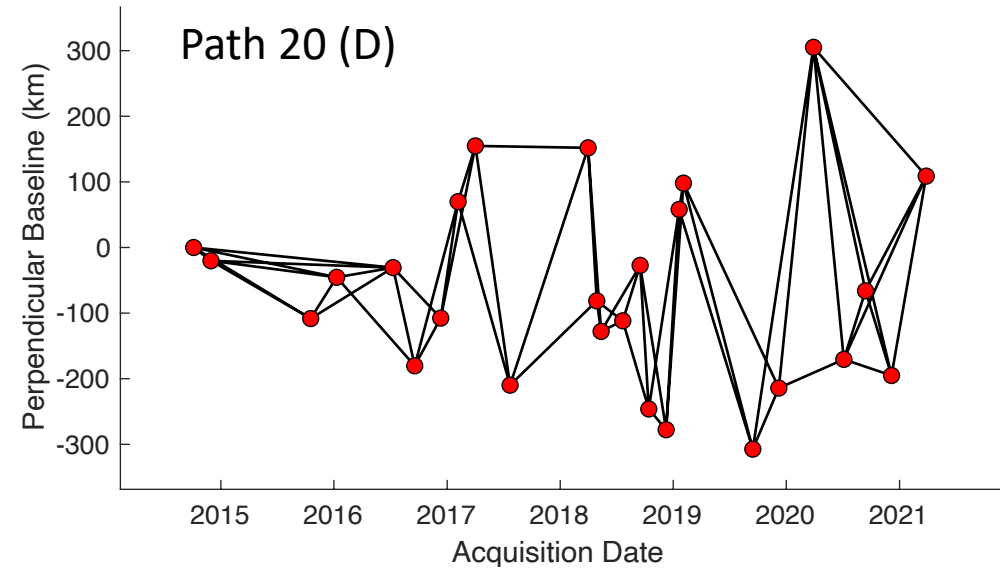
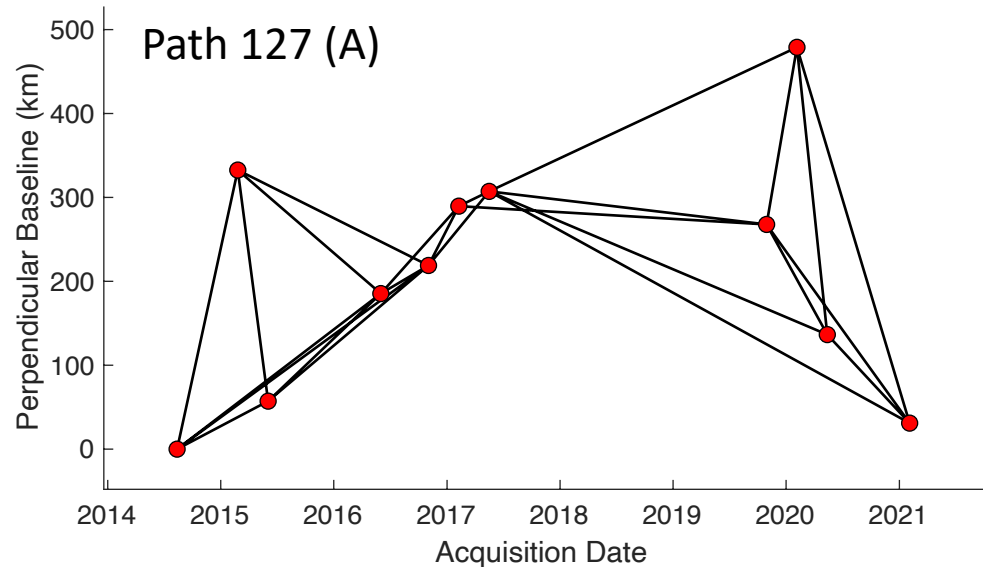
Data sets of four paths:

| Path | Orbit | Incidence Angle (deg) | Number of Images | Number of Interferograms |
|------|-------|-----------------------|------------------|--------------------------|
| 20   | D     | 42.9                  | 26               | 55                       |
| 21   | D     | 32.4                  | 24               | 51                       |
| 127  | A     | 32.4                  | 11               | 25                       |
| 128  | A     | 42.9                  | 16               | 35                       |



# Baselines

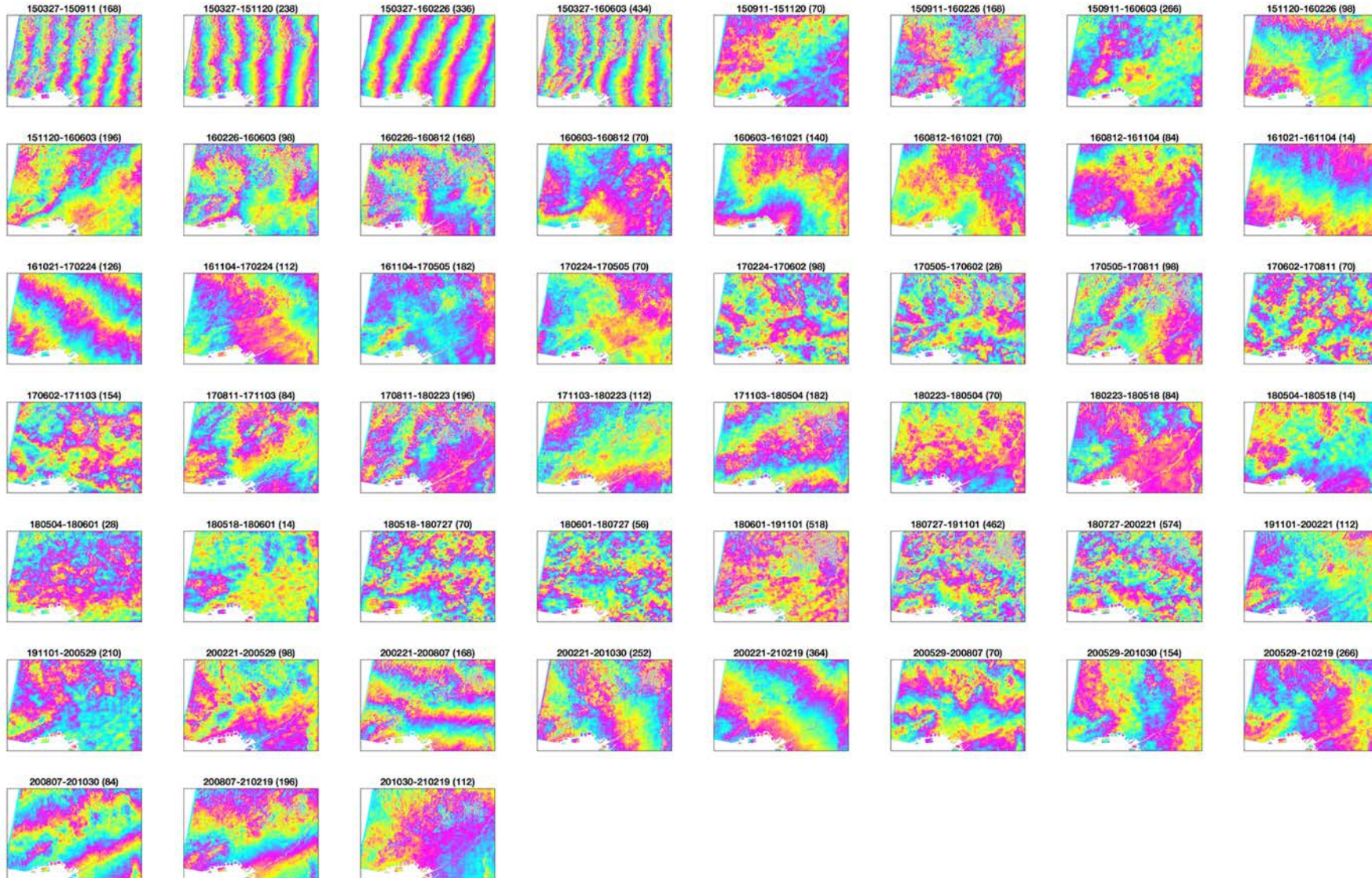
3 or 4 ifgs per acquisition





# Original interferograms

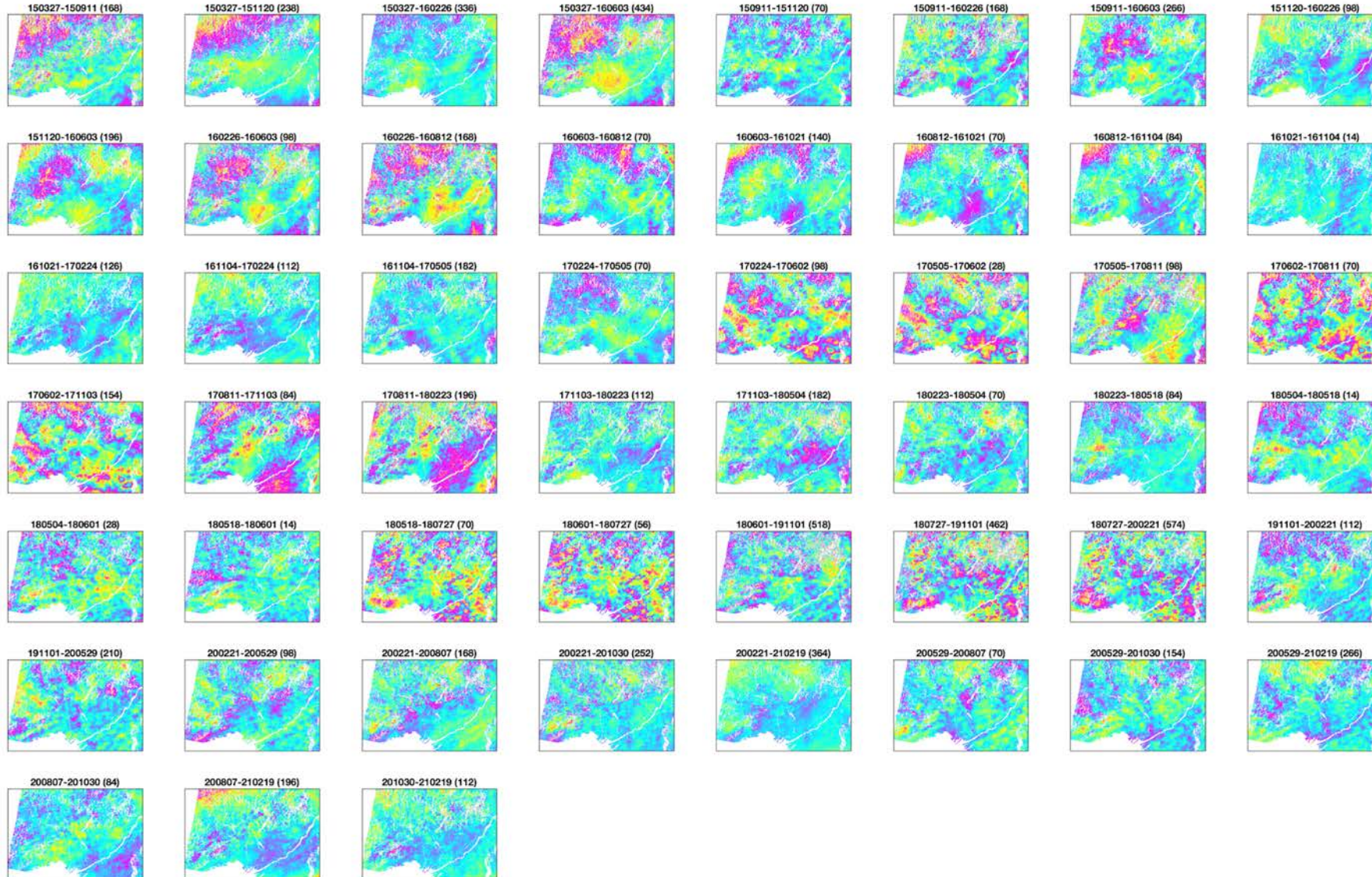
Path 21 (descending)  
Rewrapped to [0, 5cm]





# Denoised interferograms

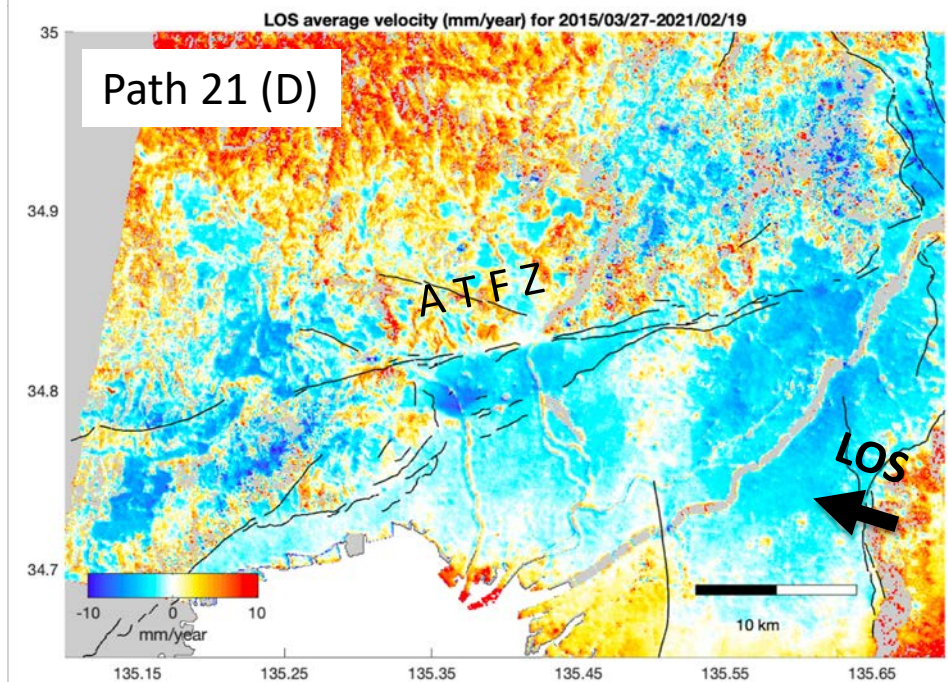
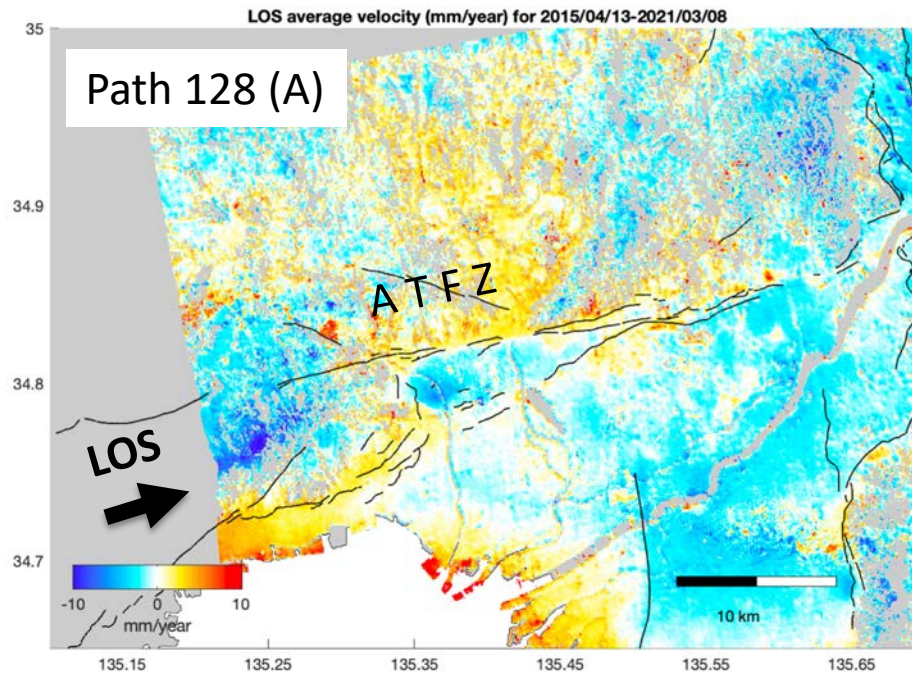
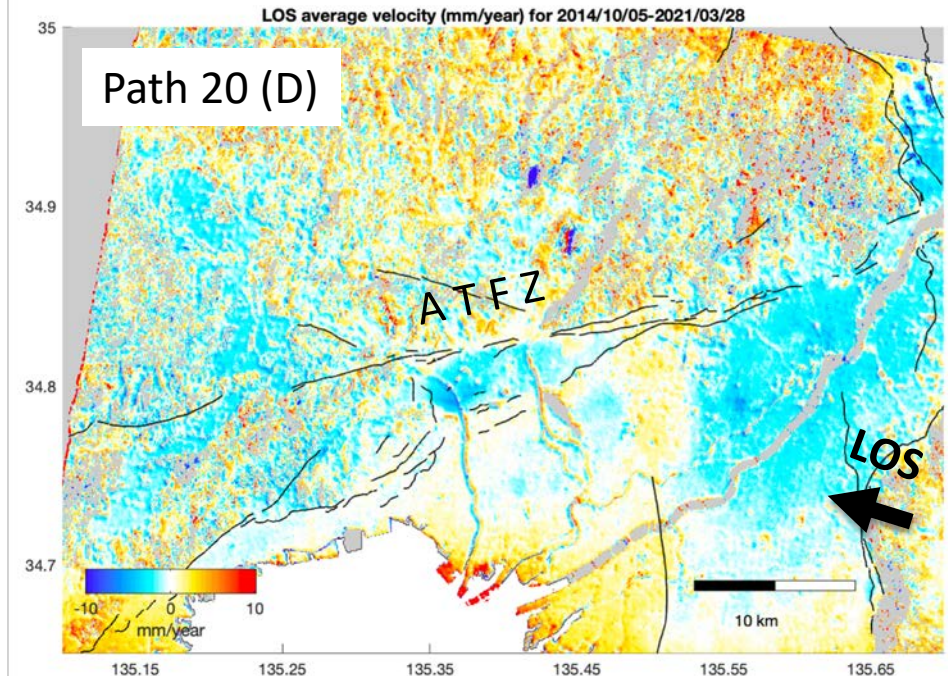
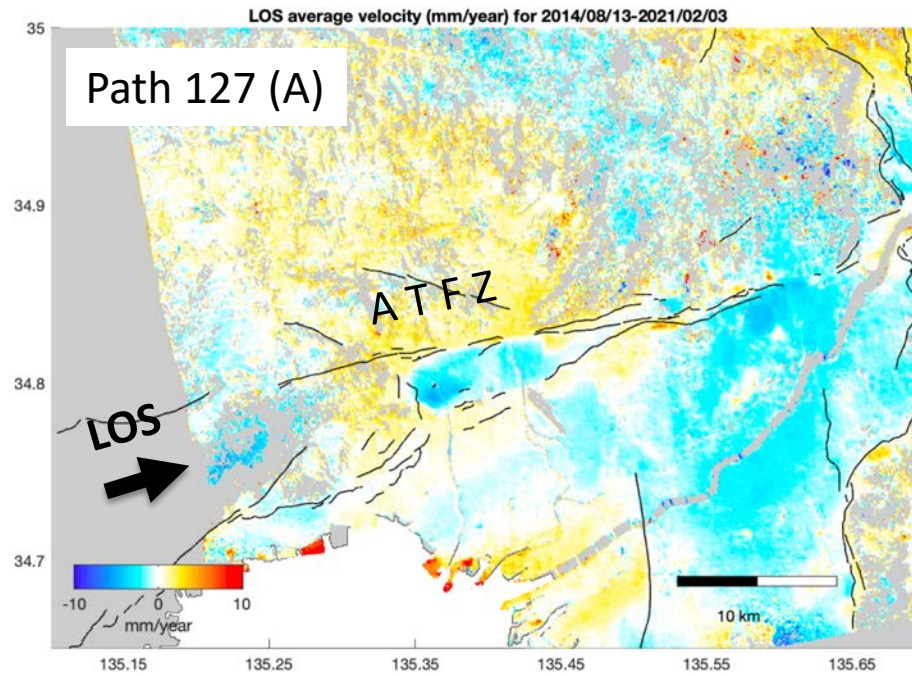
Path 21 (descending)  
Rewrapped to [0, 5cm]





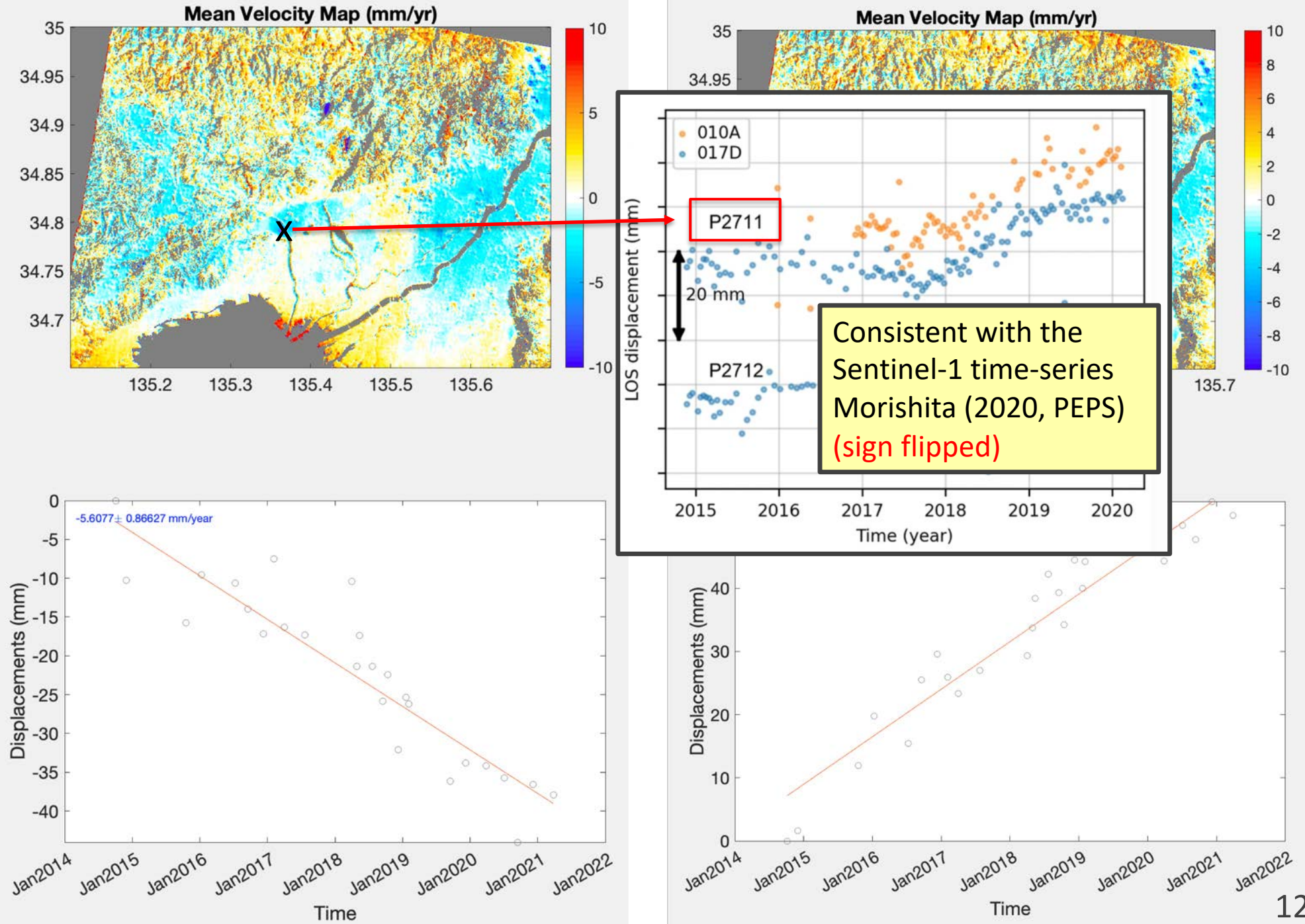
# Mean Velocity

Red: away from satellite  
Blue: toward satellite



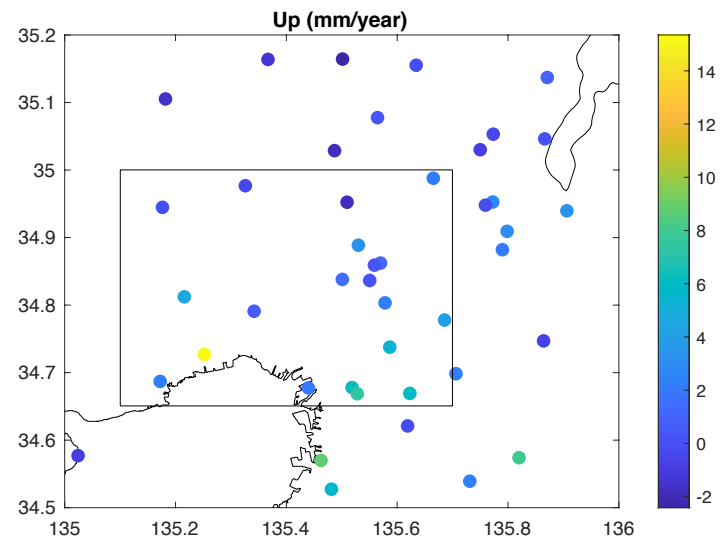
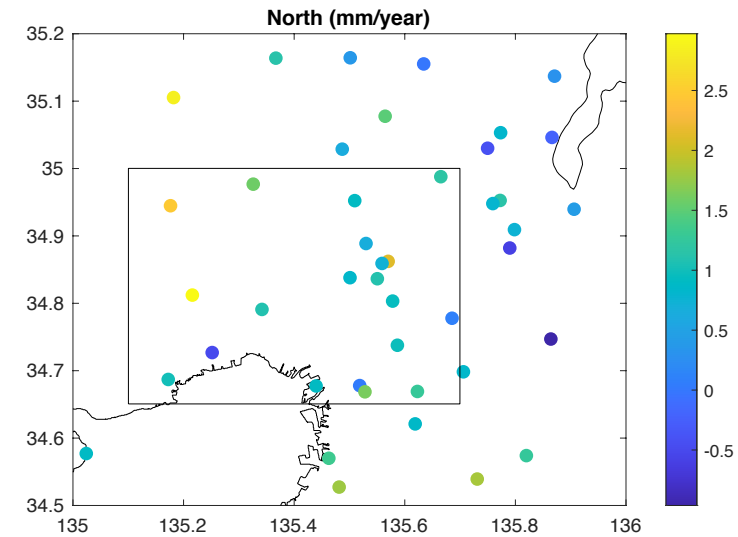
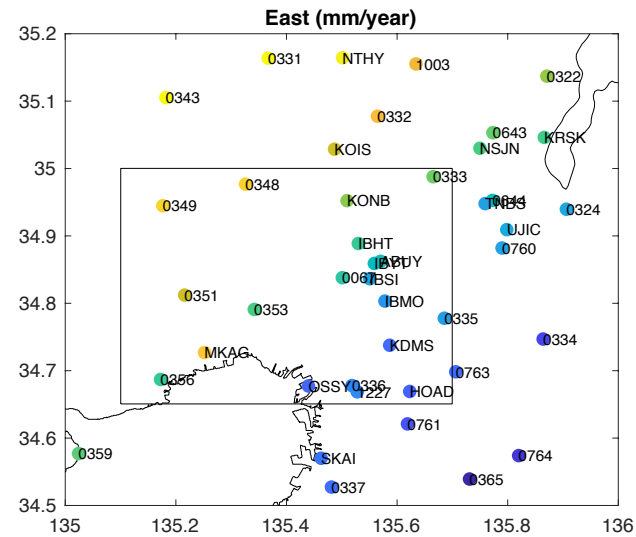


# Examples of time-series (Path 20)





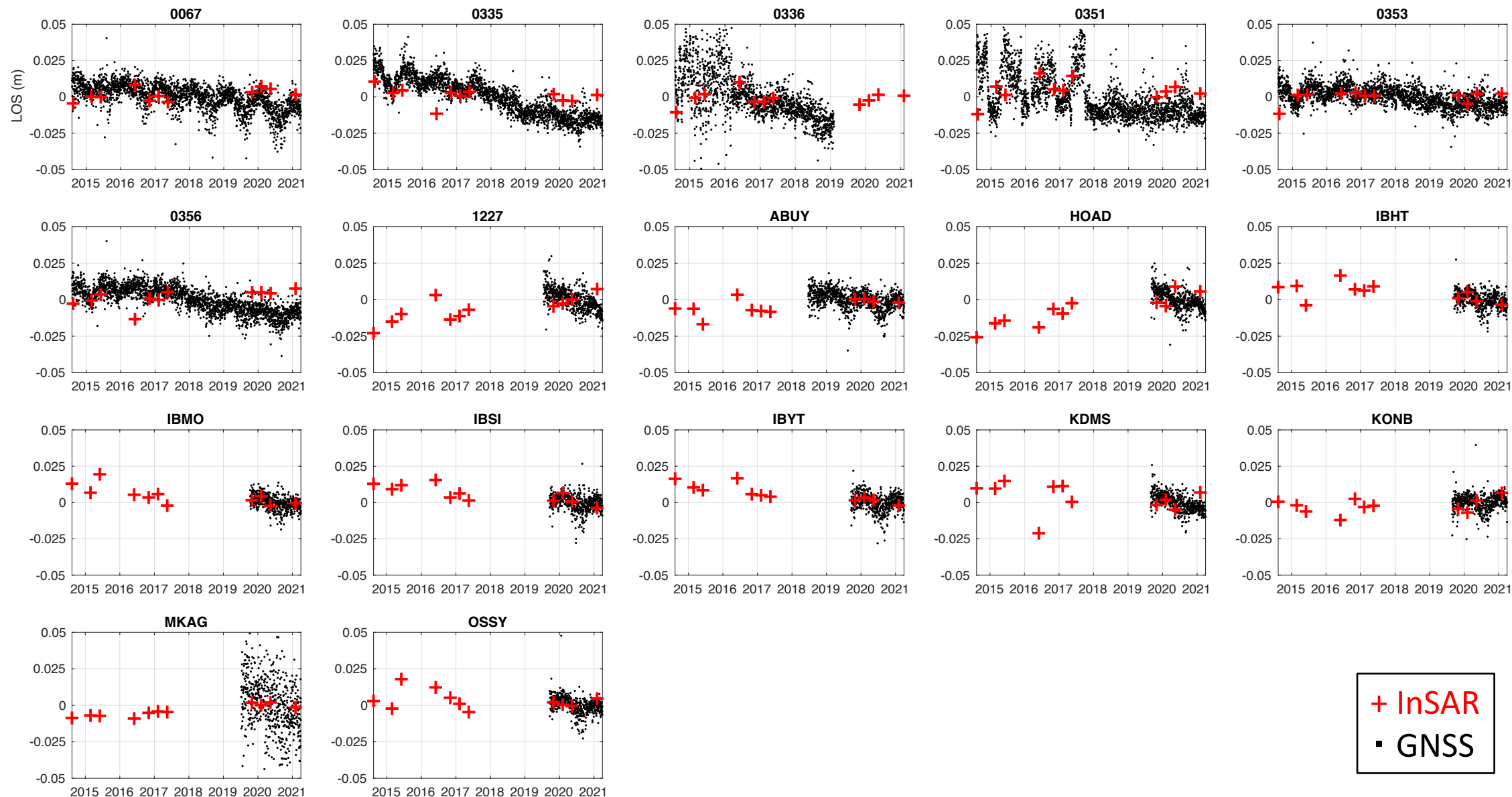
# Comparison with GNSS time-series



Data courtesy of GSI, T. Nishimura, and K. Miyahara

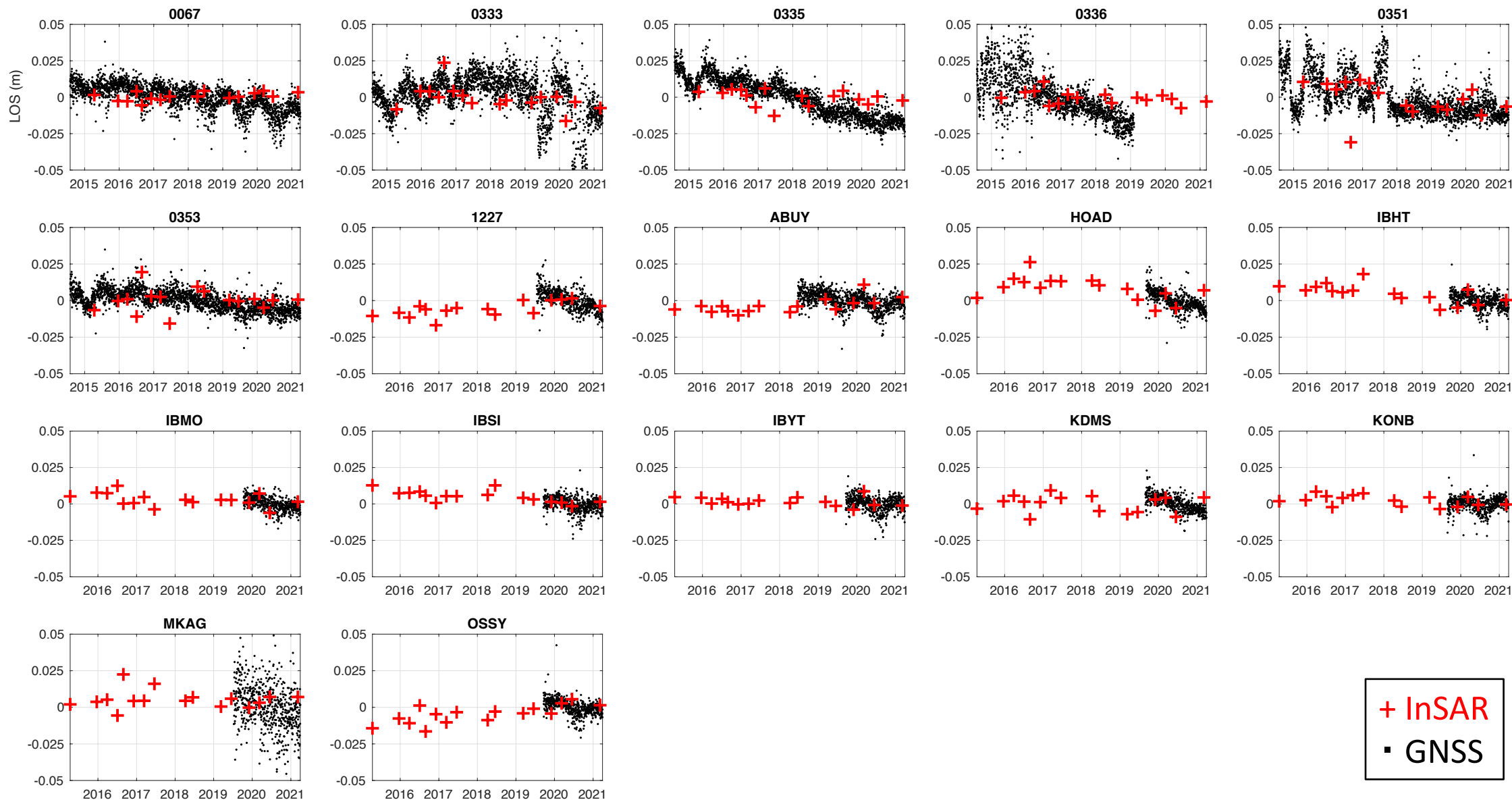
# Comparison with GNSS time-series (Path 127)

RMS = 10.8 mm



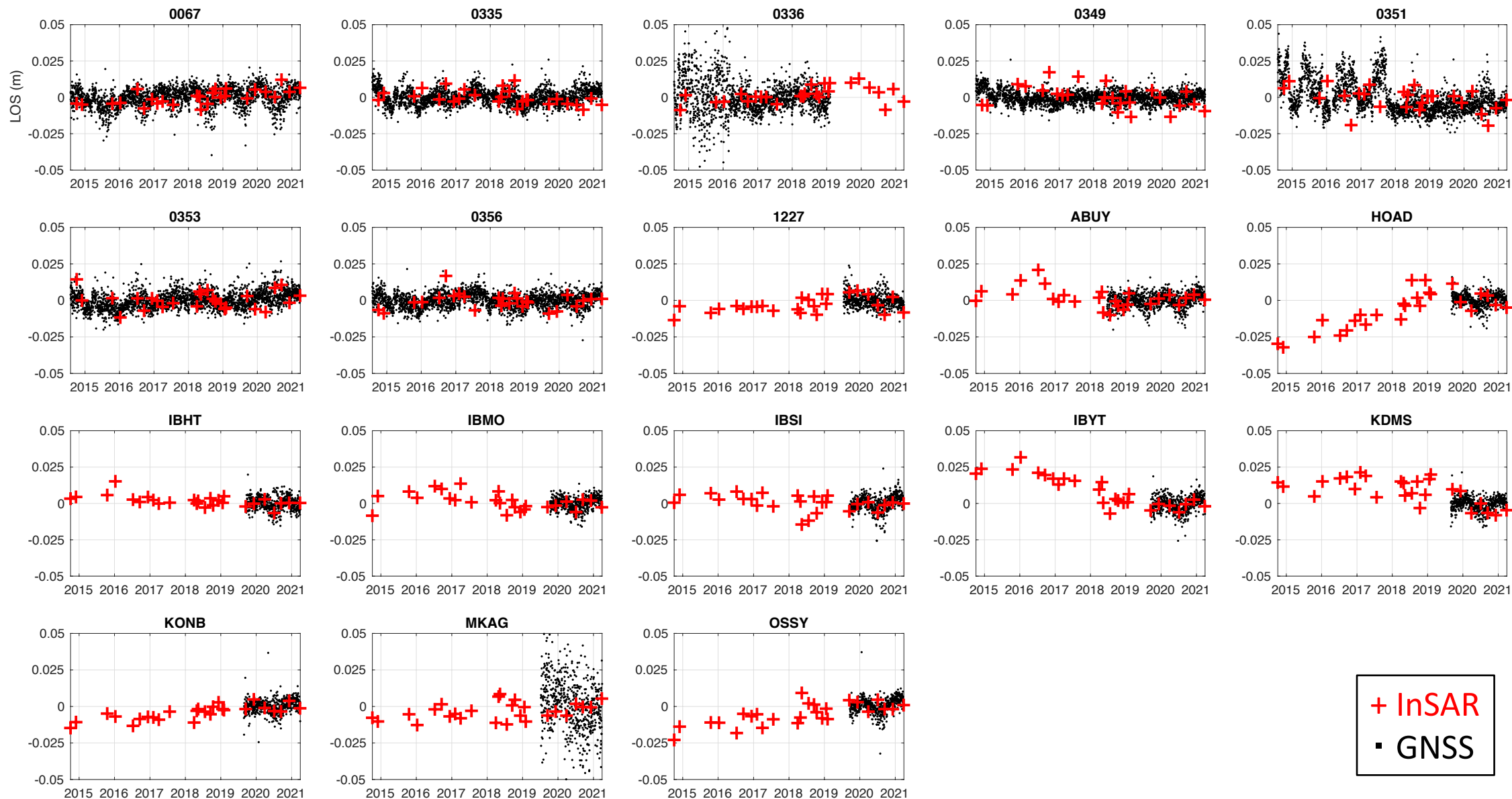
# Comparison with GNSS time-series (Path 128)

RMS = 10.3 mm



# Comparison with GNSS time-series (Path 20)

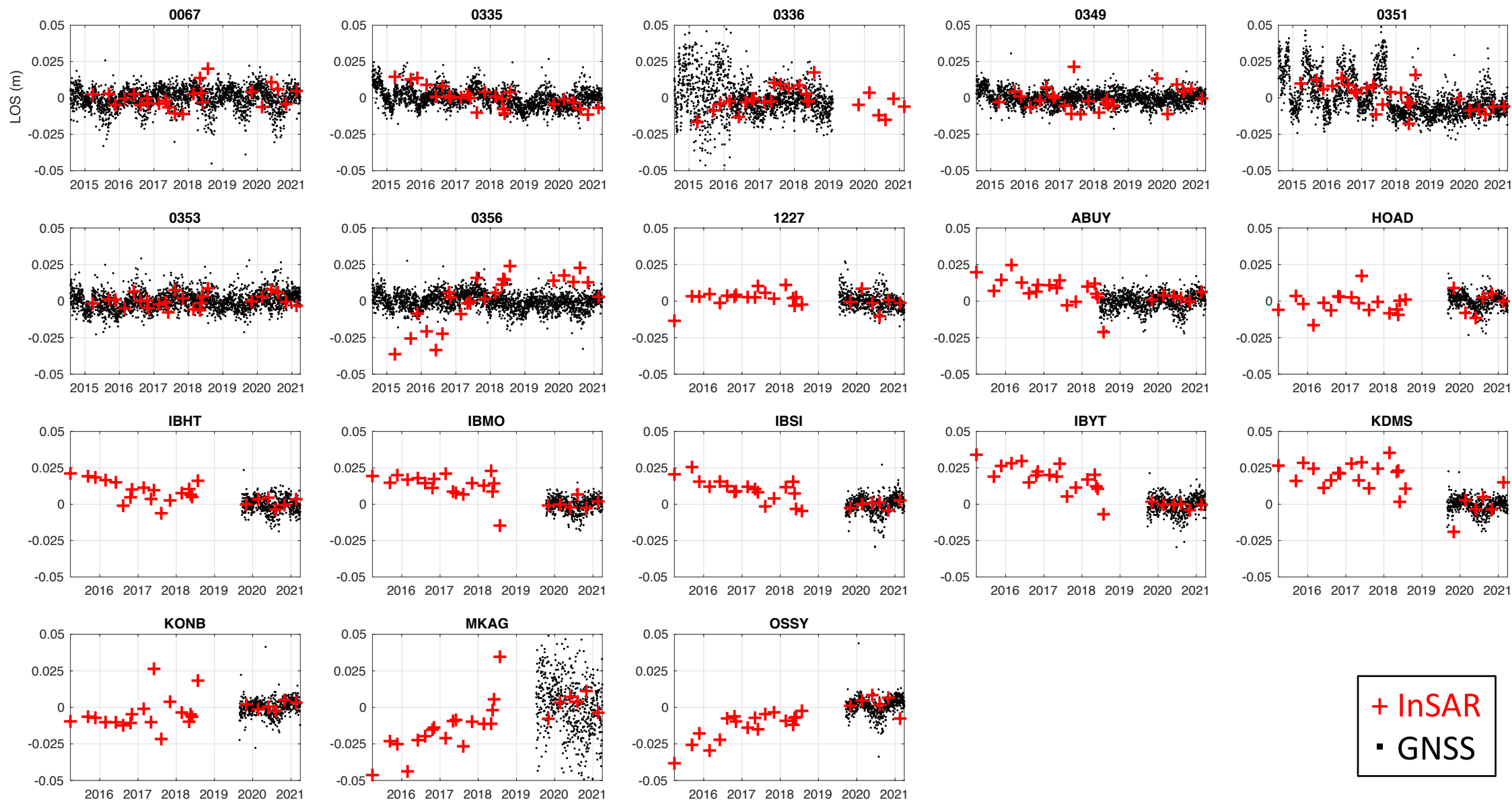
RMS = 7.5 mm





# Comparison with GNSS time-series (Path 21)

RMS = 10.0 mm



# Summary

- De-Noising while solving for Time-Series (DeNTiS) algorithm is developed (formulation written in Fukushima et al. (2019, Earth Planets and Space).
- By applying DeNTiS on ALOS-2 data, the displacement time-series and the mean velocity map around the Arima-Takatsuki Fault Zone were obtained.
- Results consistent with those using Sentinel-1 data (much denser temporal sampling) were obtained, showing the effectiveness of the approach.

Please contact [fukushima@irides.tohoku.ac.jp](mailto:fukushima@irides.tohoku.ac.jp) if you want to try the codes.

# Acknowledgements

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