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## Abstract

Stochastic precipitation generators (SPGs) are often used to produce synthetic precipitation series for water resource management. Typically, an SPG assumes a stationary climate. We present an hourly precipitation generation algorithm for non-stationary conditions informed by the Global Climate Model (GCM) forecasted average monthly temperature (AMT). The physical basis for precipitation formation is considered explicitly in the design of the algorithm using hourly Pressure Change Events (PCE) to define the relationship between hourly precipitation and AMT. The algorithm consists of a multi-variable Markov Chain and a moving window driven by time, temperature, and pressure change. We demonstrate the methodology by generating a 100-year, continuous, synthetic hourly precipitation time series using GCM AMT projections for the Northeast US. When compared with historical observations, the synthetic results suggest that future precipitation in this region will be more variable, with more frequent mild events and fewer but intensified extremes, especially in warm seasons. The synthetic time series suggests that there will be less precipitation in the summers, while winters will be wetter, consistent with other research on climate change projections for the northeast US. This SPG provides physically plausible weather ensembles for water resource studies involving climate change.

**Keywords:** Stochastic process, rainfall generator, GCM temperature, hourly precipitation, pressure change, extreme precipitation, climate change

This paper has 27 acronyms listed after the main text and sited before the references.

## Introduction

The anthropogenic use of fossil fuels releases greenhouse gases (GHGs) into the atmosphere, contributing to global warming [Solomon *et al.*, 2007; US EPA (*Environmental Protection Agency*), 2010; VijayaVenkataRaman *et al.*, 2012]. Global Climate Models (GCMs) suggest that increased GHG emissions could alter precipitation patterns, with associated impacts on the reliability and performance of water resource infrastructure. These impacts could be particularly acute in urban settings, where even small changes in the intensity and duration of precipitation can result in pronounced changes in runoff due to the proliferation of impervious surfaces [Betts *et al.*, 2007; Hamlet and Lettenmaier, 1999; Huntington, 2003; Labat *et al.*, 2004]. Changes in precipitation patterns can also alter urban flood risks [Pfister *et al.*, 2004; Schreider *et al.*, 2000], change the volume and frequency of combined sewer overflows (CSOs) [Nie *et al.*, 2009; Semadeni-Davies *et al.*, 2008], and impact the performance of the billion dollars green infrastructure (GI) programs implemented in an increasing number

of North American cities [Gill *et al.*, 2007].

Global warming is very likely to increase precipitation potential due both to acceleration of evaporation, and an increase in the air holding capacity of the atmosphere, [Solomon *et al.*, 2007; K. E. Trenberth, 2011]. In theory, a one-degree Celsius change in air temperature can bring about a 7% increase in the air’s moisture-holding capacity. The Clausius–Clapeyron (CC) relationship extends this increase in the air holding capacity to the global scale under climate change [Sun *et al.*, 2007; Kevin E Trenberth and Shea, 2005]. The actual relationship between temperature and air holding capacity has been investigated using measured climatic data at monthly [King *et al.*, 2014; Kevin E Trenberth and Shea, 2005], daily [Sun *et al.*, 2007; Westra *et al.*, 2013a] and sub-daily [Geert Lenderink and van Meijgaard, 2008; G. Lenderink and van Meijgaard, 2010] time scales. Researchers have also investigated how changes in air temperature alter mean [Allen and Ingram, 2002; K. E. Trenberth, 2011], and extreme [Groisman *et al.*, 2005; Kunkel *et al.*, 2013; Meehl *et al.*, 2005; Meehl *et al.*, 2012; Shaw *et al.*, 2011] precipitation amounts, as well as event durations [Panthou *et al.*, 2014; Wasko *et al.*, 2015a].

At relatively coarse temporal (e.g., decadal, annual, or seasonal) and spatial (e.g., continental, regional) scales, GCMs can be used to investigate how different emission scenarios might alter precipitation patterns. Precipitation is, however, the GCM output with the greatest bias relative to observations [Johnson and Sharma, 2009; Kendon *et al.*, 2008]. The use of GCM outputs in predicting precipitation at finer temporal (e.g., daily, hourly, sub-hourly) and spatial scales (e.g., local and mesoscale) is generally considered inappropriate, in large part due to the inability of GCMs to accurately simulate precipitation intensity and resolve localized weather patterns.

At finer temporal and spatial scales, GCM outputs can be dynamically down-scaled into regional climate models (RCMs) and/or incorporated into stochastic precipitation generators (SPG) [Fowler *et al.*, 2007; Wilks, 2010] in different ways. SPGs have been used to incorporate precipitation uncertainty and variability into the evaluation of flood risks [Haberlandt *et al.*, 2008], the reliability of rainwater harvesting systems [Basinger *et al.*, 2010], and the effectiveness of other water resource decisions [Shamir *et al.*, 2015]. In stationary applications, a variety of techniques can be employed to generate multiple Markovian sequences of precipitation, e.g., ensembles [Wilks and Wilby, 1999]. Parametric methods utilize statistical distributions of wet-day rain volumes [Stern and Coe, 1984; Wilks, 1998], precipitation arrival time, intensity, and duration [Rodríguez-Iturbe *et al.*, 1987; 1988; Wasko and Sharma, 2017; Wasko *et al.*, 2015b], and other rain event characteristics [Heneker *et al.*, 2001]. Non-parametric methods, by contrast, create synthetic sequences by strategically sampling historical precipitation [Basinger *et al.*, 2010; Lall and Sharma, 1996; Lall *et al.*, 1996; Sharma and Lall, 1999], for example within a moving window to preserve seasonality [Balaji Rajagopalan *et al.*, 1996].

In many applications, especially those requiring fine temporal precipitation

quantities (e.g., urban stormwater planning), the direct use of GCM-forecasted precipitation in SPGs is not appropriate since GCMs poorly reproduce precipitation event intensity [Johnson and Sharma, 2009; 2012], especially during extreme events [Kim *et al.*, 2020]. However, GCM forecasts of future annual, seasonal, or monthly precipitation amounts are routinely compared to historical precipitation to generate delta change factors (at annual, monthly, or seasonal scales) that can be used to modify historical event characteristics. Maimone *et al.* [2019], for example, developed an SPG to stochastically generate future sequences of hourly precipitation for 2080~2100 by inflating historical rainfall amounts by factors derived from an analysis of multiple GCM predictions of annual and seasonal precipitation for Philadelphia.

Whether they are parametric or nonparametric, and regardless of whether they are being used to create ensembles of historical or future precipitation, SPG sampling procedures typically make a static assumption regarding the physical processes causing the formation of precipitation. Such assumptions can be defended under a stationary climate, but as the atmosphere warms drivers of precipitation could change. Although the accuracy of precipitation forecasts under climate change could be improved by considering the fundamental physical mechanisms of precipitation formation, dynamic simulation of convection processes remains challenging [Westra *et al.*, 2013b].

Precipitation is caused when moist air rises, cools, condenses, and coalesces into droplets that can fall under the right conditions. [Evans and Westra, 2012; Westra *et al.*, 2013b] The dynamic relationship between precipitation, temperature, and pressure were generalized by Ahrens *et al.* [2012] who showed that air pressure at the ground surface is consistently reduced as air is lifted. At small (e.g., local and/or mesoscale) spatial scales, Horst *et al.* [1976] found that surface pressure dropped due to the formation of convective clouds. Ahrens *et al.* [2012] and Visser *et al.* [2020] presented temperature changes associated with the onset of an extreme precipitation event in the Australian tropics. These processes vary even at sub-daily time scales [Evans and Westra, 2012] with “no a priori reason” to assume consistency in a future climate [Westra *et al.*, 2013b]. In Yu *et al.* [2018], we suggest the use of pressure changes as potential predictors of future non-stationary precipitation formation.

In this paper, we present a non-parametric SPG for non-stationary future precipitation. The SPG generates dynamic sequences of hourly precipitation using GCM predictions of future Average Monthly Temperature (AMT). The algorithm is based on the meteorological relationships between precipitation and temperature involving pressure changes, as originally introduced by Yu *et al.* [2018]. One of the purposes of this study is to demonstrate that using pressure changes, SPG algorithms can be used to preserve the physical causality of precipitation in a non-stationary generator.

The paper is structured as follows. First, we describe the data sources used and the relationship between hourly precipitation and AMT. Next, the stochastic precipitation generation algorithm is introduced, followed by a validation of the

model outputs using pooled gauge data across the Northeast US as a test case.

## Data Sources and Collection

The study focuses on the northeastern coastal United States: a coastal region extending from Philadelphia to Boston characterized by mostly flat terrain (See Figure 9 Appendix). Throughout this region, the vertical lifting of air is typically associated with frontal precipitation rather than orographic lifting. Over 50 years of high-quality, hourly measurements of temperature, precipitation, and sea-level air pressure were obtained from the National Climate Data Center (NCDC), (formerly the National Center for Environmental Information) at stations located at the international airports in New York City (NYC) (station ID: 72503014732 for 1973~2018 & 99999914732 for 1948~1973), Philadelphia (PHL) (station ID: 72408013739 for 1973~2018 & 99999913739 for 1941~1973) and Boston (BOS) (station ID: 72509014739 for 1943~2018). (See Figure 9 in Appendix) Since topographic relief and climatic conditions vary little across the region, data from all three cities were pooled into one data set. This pooling also increased the overall sample size for all events, especially the extreme events that are more likely to detect with observations from multiple gauges distributed spatially across the region [Hayhoe *et al.*, 2008; Hayhoe *et al.*, 2007; Hoerling *et al.*, 2016; Tebaldi *et al.*, 2006]

Projections of future changes to AMT were obtained from the NASA Goddard Institute for Space Studies, Center for Climate Systems Research at Columbia University in New York City. Because this research was initiated prior to the release of the Coupled Model Intercomparison Project 5 (CMIP5) and the most recent CMIP6, neither the Representative Concentration Pathways (RCPs) of CMIP5, nor the Shared Socioeconomic Pathways (SSCs) of CMIP6 are referenced explicitly. Instead, the MIROC GCM [Hasumi and Emori, 2008] was selected for this analysis because its higher relative predicted increases in temperature would yield a more pronounced effect on the generated precipitation series. AMT projections under the A2 emission scenario- “a very heterogeneous world, ” [Nakicenovic *et al.*, 2000], were used due to the regional scale of this study.

Following the procedure described in Yu *et al.* [2018], the continuous hourly pressure time series were discretized into individual Pressure Change Events (PCEs) associated with fronts or other precipitation-causing systems. During the definition of PCEs, daily fluctuations in atmospheric pressure were minimized by defining the pressure change as the difference between two pressure readings separated from each other by 24 hours, as shown in Equation 1:

$$P_t = P_t - P_{t-24} \text{ Equation (1)}$$

where  $P_t$  is the pressure reading at hour  $t$ , and  $P_t$  is the pressure change relative to 24 hours prior. PCEs were categorized as either Increasing (InPCEs) or Decreasing (DePCEs) based on the computed direction of the pressure change.

Two important features defining the magnitude of each PCE are the duration and the Cumulative Event Pressure Change (CEPC). In the stochastic process described in the next section, these two features will be used as the conditions for selecting the subsequent PCE. The CEPC for each PCE is defined per Equation 2:

$$\text{CEPC} = \sum_{t=0}^d P_t \quad \text{Equation (2)}$$

where  $P_t$  is the 24-hour pressure change relative to hour  $t$  in a PCE defined in Equation. 1,  $d$  is the duration of the PCE. The intensity, duration, and alternating of DePCEs and InPCEs correspond to the strength and speed of the precipitation causing meteorological systems as they move past the recording gauges.

## Methodology

### Algorithm Design

*Yu et al.* [2018] used PCEs to describe the relationship between AMT and specific precipitation characteristics, including the Probability of Precipitation (POP) and the event Precipitation Depth (PD). PCEs, and especially DePCEs, were shown to be associated with the vertical lifting of air, and associated condensation, coalescence, and precipitation. The analysis also showed that the frequency of PCEs can be represented as a function of AMT, suggesting that a synthetic series of future PCEs can be derived from future AMT projections.

The model uses non-parametric methods to simulate precipitation, making it portable to other regions [*Basinger et al.*, 2010]. The algorithm samples historical PCEs from specific AMT ranges (indexed to GCM outputs) occurring within moving time windows. Since the characteristics of PCEs (e.g., type and magnitude), their associated precipitation characteristics (e.g., POP and PD), and AMT are statistically and physically related [*Yu et al.*, 2018], a synthetic precipitation series can be generated by concatenating precipitation event characteristics associated with specific sequences of PCEs. (Additional analysis regarding the relationship between POP and PCE is presented in the Appendix).

Figures 1 and 2 provide more detail on the procedure used to sample an individual PCE based on temperature and time. The overall stochastic algorithm is represented in Equations 3 and 4, where  $\text{PCE}_1$  is selected from a group of candidate PCEs,  $\{\text{PCE}\}$ , that could begin at the time  $t_0$  based on the GCM-projected AMT for  $t_0$ , ( $\text{AMT}_0$ ), and the size of the moving window,  $\text{Win}$ . Specifically, the set  $\{\text{PCE}\}$  is selected based on Equation 3.

$$\{\text{PCE}\} = f(t_0, \text{AMT}_0, \text{Win}) \quad \text{Equation (3)}$$

$\text{PCE}_1$ , the new successive PCE, is selected from within  $\{\text{PCE}\}$  but is conditioned on the preceding PCE,  $\text{PCE}_0$ , in the sequence per Equation 4

$$\text{PCE}_1 = f(\text{PCE}_0, \{\text{PCE}\}) \quad \text{Equation (4)}$$

The moving window has been used to simulate temporally stationary precipitation by other researchers using different length, such as 60 days by [Sharma and Lall, 1999] or 90 days by [B. Rajagopalan and Lall, 1999]. The decision to use a shorter window (e.g., 30 days) was made in this study to better represent seasonality. The seasonal window is further narrowed using temperature, such that only PCEs corresponding to a particular time of year and temperature is selected, creating stability to the algorithm. The 6°C window was selected because seasonal shifts of POP for both DePCE and InPCE were detectable in this range [Yu *et al.*, 2018]. For example, in Figure 2, a day in March with AMT of 9°C can be used to select the subsequent PCE. The horizontally and vertically shaded bars, both centered at this data point, graphically depict the 30-day, and the 6°C, windows, respectively. The intersection of these two shaded bars defines the set  $\{PCE\}$ , described by Equation 3.

Steps 2 & 3 of Figure 1 can be denoted by Equation 4, where the new PCE will be sampled from  $\{PCE\}$  based on the condition of the previous one,  $PCE_0$ . In step 2, the PCEs of the same type of  $PCE_0$  are excluded, ensuring that InPCEs are always followed by DePCEs and vice versa. In Step 3, a K Nearest Neighbor (KNN) approach [Lall and Sharma, 1996] is employed to select one PCE out of the remaining PCEs from Step 2 to append to the synthetic series after  $PCE_0$ . In this study, “nearest neighbors” are selected from  $\{PCE\}$  based on the magnitude of  $PCE_0$ , defined by the Euclidian distance of the standard scores of CEPC and event duration (Additional details provided in the Appendix 10.2). Specifically, the candidate PCE in  $\{PCE\}$  whose predecessor’s magnitude is closest to the magnitude of  $PCE_0$  will be chosen as the subsequent one to continue the generation.

After the selection of  $PCE_1$ , the time of interest is advanced from  $t_0$  to  $t_1$  by the duration of  $PCE_1$  (Equation 5). Next,  $t_1$  is used to update the projected AMT,  $AMT_1$  in Equation 6. For example, if  $t_0$  is 2054-1-31 10:00 and the duration of  $PCE_1$  is 25 hours, then  $t_1$  will be 2054-2-1 11:00.  $AMT_1$  will be the AMT projected for Feb 2054.

$$t_1 = t_0 + \text{duration of } PCE_1 \text{ Equation (5)}$$

$$AMT_1 = f(t_1) \text{ Equation (6)}$$

After completing the stochastic process, the corresponding precipitation series of each synthetic PCE is concatenated to form the final hourly synthetic precipitation series.

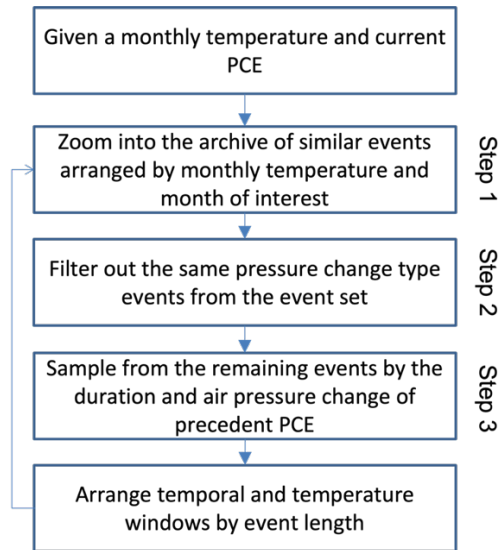


Figure 1. Flow chart of the synthetic precipitation generation algorithm

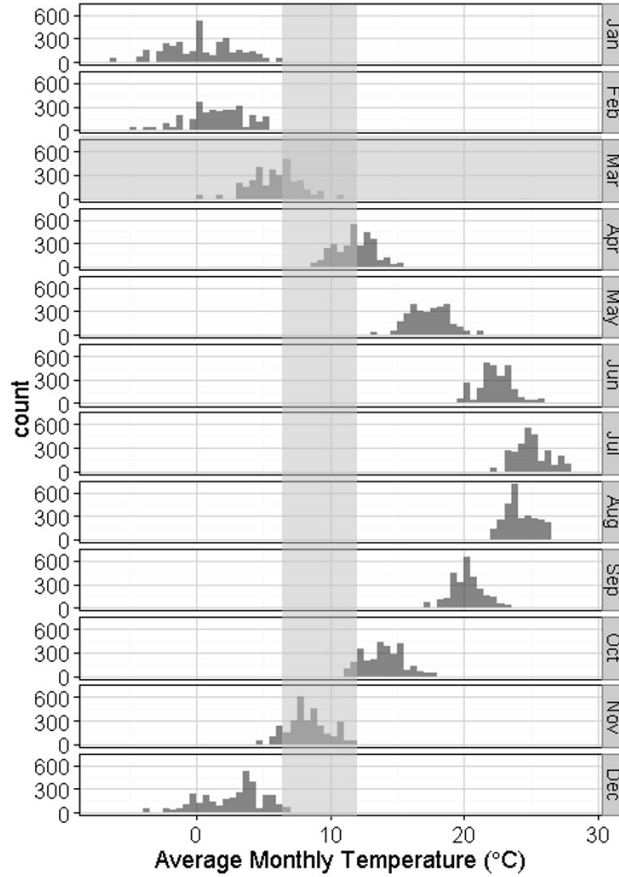


Figure 2. Sample of a two-dimensional moving window, a day in March with 9°C AMT is the time of interest. The horizontal shadow area is the 30-day moving window. The vertical shadow area is the 6°C wide temperature window, centered on 9°C. The PCEs in the intersection are the candidates for sampling the next one.

## Two-step Validation Approach

To validate the approach, the algorithm was used to generate synthetic sequences of precipitation for both historic (e.g., 1975-2012) and future (e.g., 2035-2099) periods. One hundred realizations of precipitation for each of these time periods were generated. The historic simulations were generated using observed AMT, while the future simulations used the climate change AMT projected by Center for Climate Systems Research at Columbia University. To simplify the discussion, the time series of historic precipitation is referred to as the “Observed” series, the modeled time series of the historic period is referred to as the



“Reanalysis” series, and the modeled time series of the future period is referred to as the “Forecasted” series.

The validation process involves two steps. In step 1 (described in Section 4.1), the Reanalysis series is compared to the pooled precipitation observations described above, demonstrating the algorithm’s ability to replicate the physical link between precipitation occurrence and temperature. The goal is to demonstrate the model’s ability to bracket trends displayed in the historical data. This comparison will first depict the relationship between PD and the magnitude of pressure change (e.g., CEPC). Next, it will show the impact of temperature (e.g., AMT) and the dependence of different seasonal PD percentiles on temperature (e.g., AMT). The analysis of PD distributions in all the plots are displayed in contours while the trends of PD are lined up by Loess regression curves ([*Cleveland et al.*, 1992]) are generated to display trends in these relationships.

In Step 2 of the validation process (described in Section 4.2), the forecasted series are qualitatively compared to precipitation forecasts made for this period by *Hayhoe et al.* [2007]. Box plots of seasonal and annual PD for 2035–2069 and for 2070–2099 are developed for comparison with box plots for the same future time slices generated by *Hayhoe et al.* [2007]. This same plot is used to discuss the implications of climate change on future precipitation, specifically through a comparison of the Reanalysis series to the Forecasted series. A further breakdown of the shifts of distributions and trends of seasonal precipitation of the reanalysis series is presented against pressure change (e.g., CEPC) and temperature (e.g., AMT).

## Results

### Validation Step 1: Comparison of all series

We note that because the Reanalysis series includes 100 replicates of the historic period, it more clearly presents the characteristics of PCE than the pooled observations. To reflect the relationship between precipitation and temperature, the results are presented for each of the three series.

The relationships between PD and CEPC embedded in all time periods are shown in Figure 3, with nearly identical trends evident in all series. Because all dry PCEs lie on the horizontal axis (e.g., PD = 0 mm), the contours reflect the density distribution of only the wet-weather PCEs. The contours show a nearly identical distribution of PCEs over all three series. On the horizontal axis, 0 hPa separates DePCEs (to the left) and InPCEs (to the right). This point on the horizontal axis also corresponds to a point of inflection in the PD trend line. The steeper slope of the PD trend line indicates that precipitation is more sensitive to DePCEs than to InPCEs. Among DePCEs, PD increases with increasing (negative) CEPC. Among InPCEs, PD decreases with increasing (positive) CEPC. These differences are not surprising because increasing pressure tends to be associated with increased atmospheric stability, indicating less

convection, condensation, coalescence, and precipitation. Slight discrepancies in the trend lines are apparent at the left and right extremities. The differences between the Reanalysis trend and the Observed trend at the extreme DePCEs and InPCEs are likely due to the larger sample size of the synthetic series. The impact of climate change is evident through the higher trend line for the Forecasted series at the extreme InPCEs. An analysis of the associated POP is provided in the Appendix.

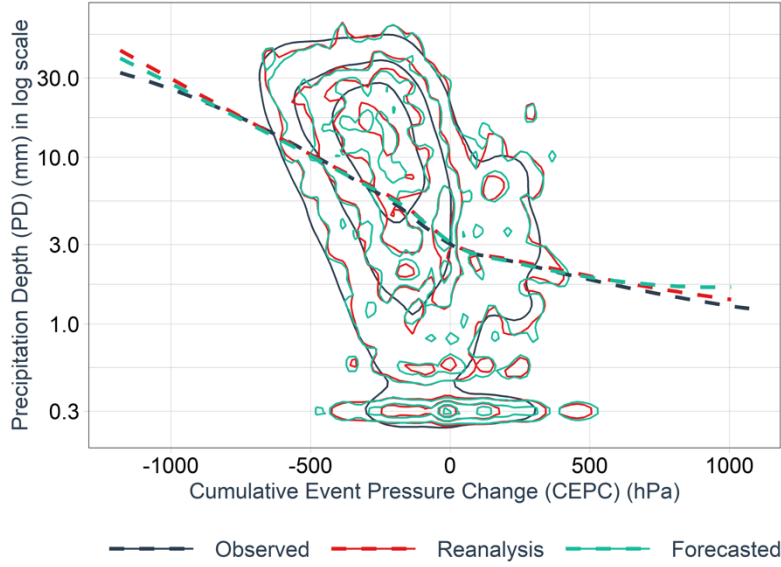


Figure 4. The relationship between Precipitation Depth (PD) and Cumulative Event Pressure Change (CEPC) of all Pressure Change Events (PCEs) for the comparisons of Observed, Reanalysis (for validation), and Forecasted (for showing climate change impacts). Since contours indicate the distribution of PCEs qualitatively, their corresponding values are not shown. Loess regression curves in-dash are shown for each dataset to denote the trend of PD against CEPC.

By introducing AMT and precipitation quantity as additional dimensions to the validation process, the distribution of PD can be further decomposed, as shown in Figure 4. Most precipitation events are categorized as mild PD (e.g., 0~20mm) and, as a result, the distribution of PD is stable in the upper plot of Figure 4. Enhanced ensembles in the Reanalysis series provide a clearer transition from 5 mm and 10 mm than in the Observed.

For moderate events that have a smaller sample size, (e.g., PD = 20~60mm) differences in the Observed and Reanalysis series distributions are more obvious. The contours of 35 mm retreat from the middle of the plot in the Reanalysis compared to the Observed. Only an isolated area located at 20 °C and -300 hPa is denoted as >35mm. Under the impacts of climate change in the Forecasted, the 35 mm contour retreats even further while the isolated peak area expanded

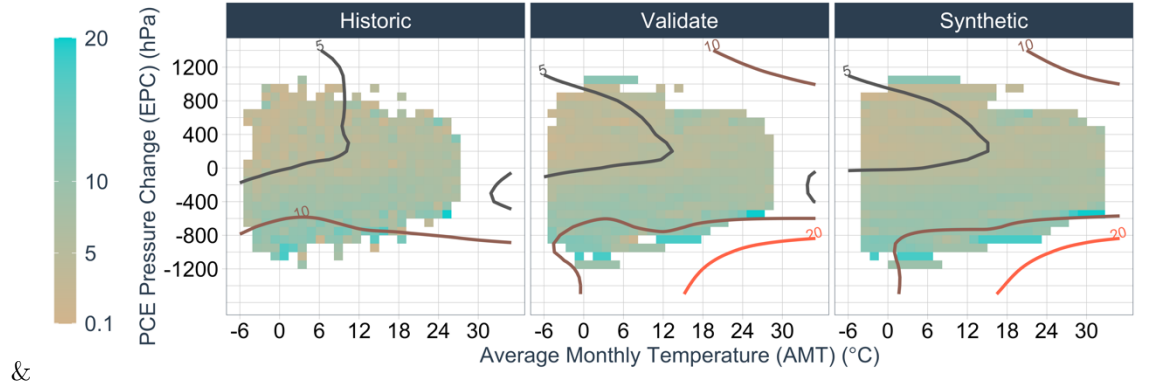
toward low temperature and low CEPC.

Extreme events (e.g., PD > 60mm) presented in the Observed series are too few and too scattered to discuss. In the Reanalysis series, the high DePCEs (low end of the tiled area) for all AMTs have PD > 100 mm. Impacts of climate change are evident in the Forecasted series as the region of PD > 100mm extends to high AMTs. This observation is consistent with the projections of more extreme precipitation under climate change that have been made by many other researchers [Betts *et al.*, 2007; Hamlet and Lettenmaier, 1999; Huntington, 2003; Labat *et al.*, 2004], to be discussed further in the next section.

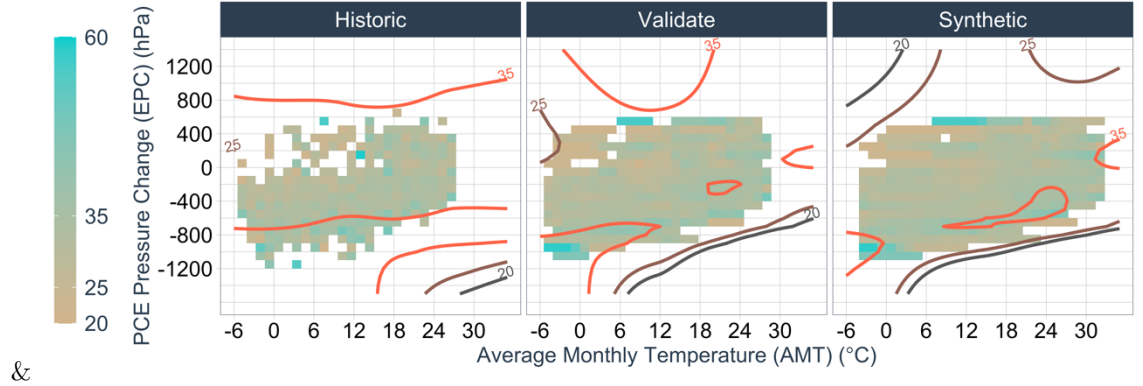
As reflected in Figure 4, most of the high wet InPCEs (high end of the tiled area) are of mild PD and occur more frequently in low AMT. With the spreading occurrence region toward warm AMT in the Forecasted for all categories, extreme wet InPCEs will have higher PD under the climate change which agrees with the discrepancy of trend lines observed at the right end in Figure 3.

@ >p(- 2) \* >p(- 2) \* @

#### 1. Mild Precipitation



#### 1. Intensive precipitation



### 1. Extreme Precipitation

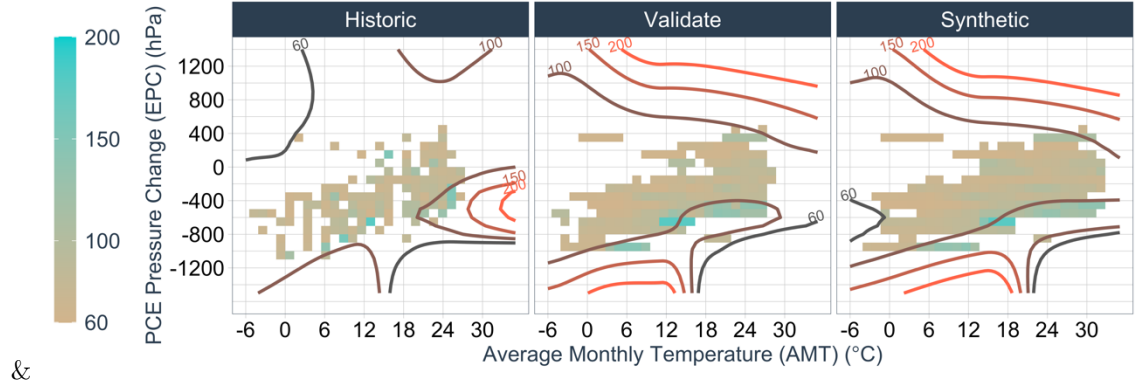


Figure . Relationship of Precipitation Depth (PD) against Cumulative Event Pressure Change (CEPC) and Average Monthly Temperature (AMT) in different ranges of PD. The color area represents the average PD of rainy Pressure Change Events (PCEs) corresponding to different combinations of CEPC and AMT. Contours and labels indicate the local regressions of PD vs. CEPC & AMT generated by the locfit function in R. (A: mild precipitation with PD between 0 and 20 mm, B: moderate precipitation with PD between 20 and 60 mm, C: extreme precipitation with PD > 60 mm)

Additional insights of the dependence between PD and temperature can be derived from PD percentiles separated by type of PCEs (Figure 5). While the PD of DePCE is similar across all temperatures, the PD of InPCE generally increases with temperature, especially between 25<sup>th</sup> and 99<sup>th</sup> percentiles. This relationship could be related to the type of precipitations in different seasons. During winter, most weather mechanisms are systematic and the movement of the precipitation region is geographically related to DePCE. Once the shifting to InPCE, precipitation will end quickly causing PD of InPCE much lower

than that of DePCE. But in Summer, there are many localized convections that a rainy system generated in a DePCE of small geographic scale has a big chance to move into a large scale InPCE area remaining a big portion of PD. Specifically, DePCE is the small center forming precipitation while InPCE is the surrounding contributor of air and humidity. To balance a DePCE, air must move downward in the surrounding region, creating an InPCE. However, the precipitation formation cloud is dynamically developed and moves. Given the tributary InPCE area is usually much larger than what can be represented by the point-sourced data collected at ground-based stations, precipitation was more difficult to be observed for InPCEs than for DePCEs, especially in local systems in summer. In addition to PD, the variance of PD percentiles of InPCE expands as the temperature gets warm, indicating that such possibility may get higher at extreme PD. The relationship between POP with seasonality and for different PCE types is explored in Appendix.

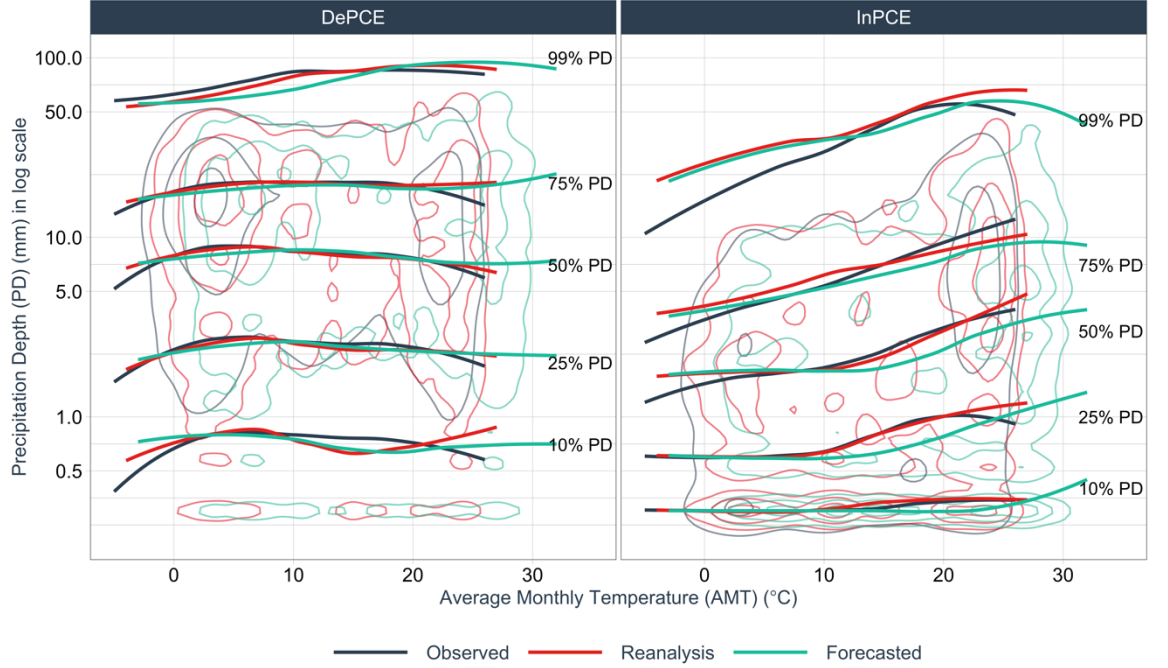


Figure 1. Dependence of Pressure Change Event (PCE) type and Precipitation Depth (PD) on Average Monthly Temperature (AMT). The contours represent the distributions of PCE in different datasets. Again, since contours indicate the distribution of PCEs qualitatively, their corresponding values are not shown. The percentiles of PD illustrate its trend and variances against AMT.

## Validation Step 2: Comparison of the Forecasted Series to forecasts made by others

In this section, the SPG algorithm results will be qualitatively compared to other research. After researching nine coupled atmosphere–ocean general circulation models (AOGCMs) under different emission scenarios, *Hayhoe et al.* [2007] projected a consistent change of precipitation under global warming across the northeast US, with the magnitudes positively correlated to GHG emissions. As shown in Figure 6A, under the A2 emissions scenario, annual temperature and precipitation across the northeast US are projected to increase by about 2.5°C and 6%, respectively in 2035~2064, and by about 4.5°C and 8% in 2070~2099, respectively. The greatest percent increase in precipitation is expected to occur in winter.

Figure 6B presents a seasonal comparison of temperature and precipitation change between the Observed and the Forecasted datasets for the two time slices considered in Hayhoe et al [2007]. AMT projections show a gradual increase of about 2°C by 2069 and 5°C by 2099 on average, annually as well as for both Summer and Winter. The modeled change in precipitation reflects a shift that partially aligns with the projections by *Hayhoe et al.* [2007]. While annual increases are small and hard to differentiate, Winter precipitation will increase more both before and after the 2069 breakpoint than *Hayhoe et al.* [2007]. Summer precipitation will decrease by about 5% in the two future time slices. These findings qualitatively agree with the projections by *Hayhoe et al.* [2007], validating the results.

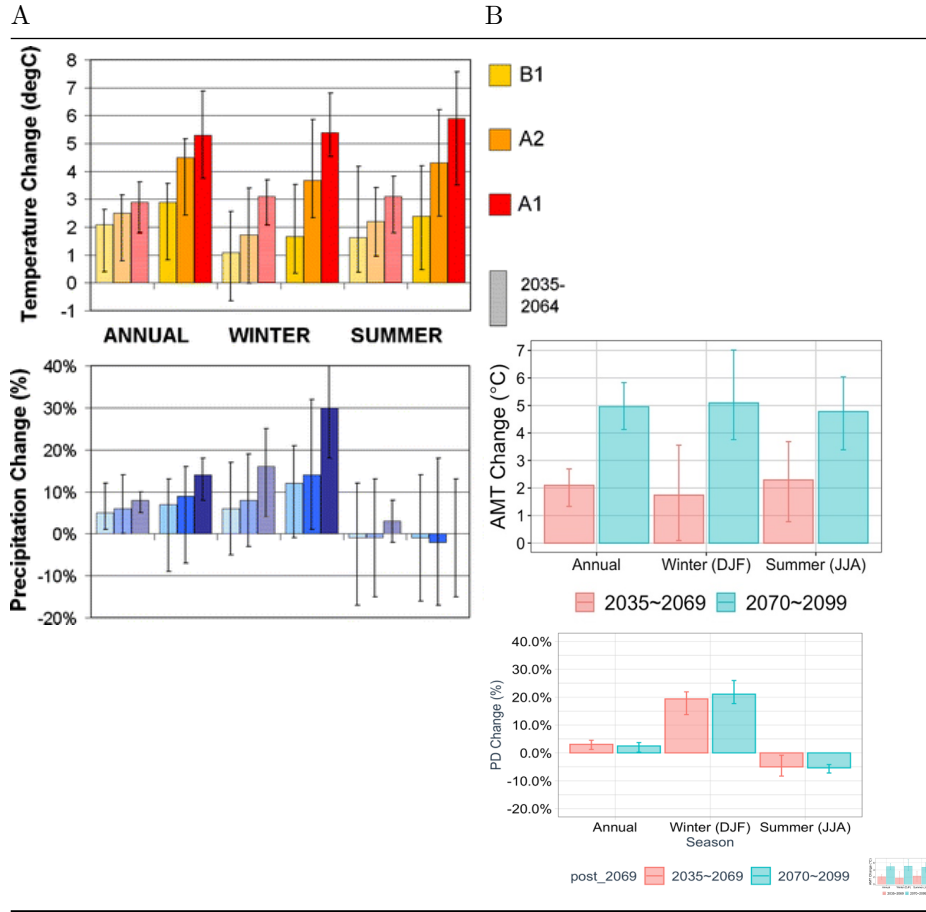


Figure . Comparison of temperature and precipitation projections in NE US in A2 emissions (A from [Hayhoe et al., 2007], B from the Observed and the Forecasted datasets)

Figure 7 provides a closer examination of the seasonal trends of PD relative to CEPC & AMT and reveals more information about precipitation changes under climate change by focusing on three time periods, the observed period, 2035~2069, and 2070~2099. According to Yu *et al.* [2018], maximum PCE frequencies occur at 0°C. This observation suggests that global warming may promote atmospheric stability, producing more PCEs for small CEPCs. This phenomenon can be observed from the upward trend of PCE distributions from the observed period to 2035~2069 and to 2070~2099 in Figure 7, especially in winter, spring, and fall. For summer, although the upward trend is not pronounced, the portion of PCE distributions (solid lines) < 10 mm (dashed lines) shrinks from the observed period to 2035~2069 and to 2070~2099, indicating that small PD will be less frequent in the climate change impact. This could

be due to the reason that the convection system in summer is much more intensive than in other seasons and can deplete the amplified moisture-holding in warmer air under the CC relationship. However, the portion of the rainy PCEs in Summer (labeled under the marginal density plot) out of all rainy PCEs indicates that the chance of Summer precipitation will slightly decrease from 24.7% to 24.6%. Thus, even though intensive PD would be favored under warm AMT, the overall Summer PD may not increase, agreeing with Figure 6. In Winter, the portion of rainy PCE in Winter will increase from 26.1% to 26.7% in 2035~2069 and to 27.3% in 2070~2099. Consequently, an increase in Winter PD would occur as Figure 6 shows.

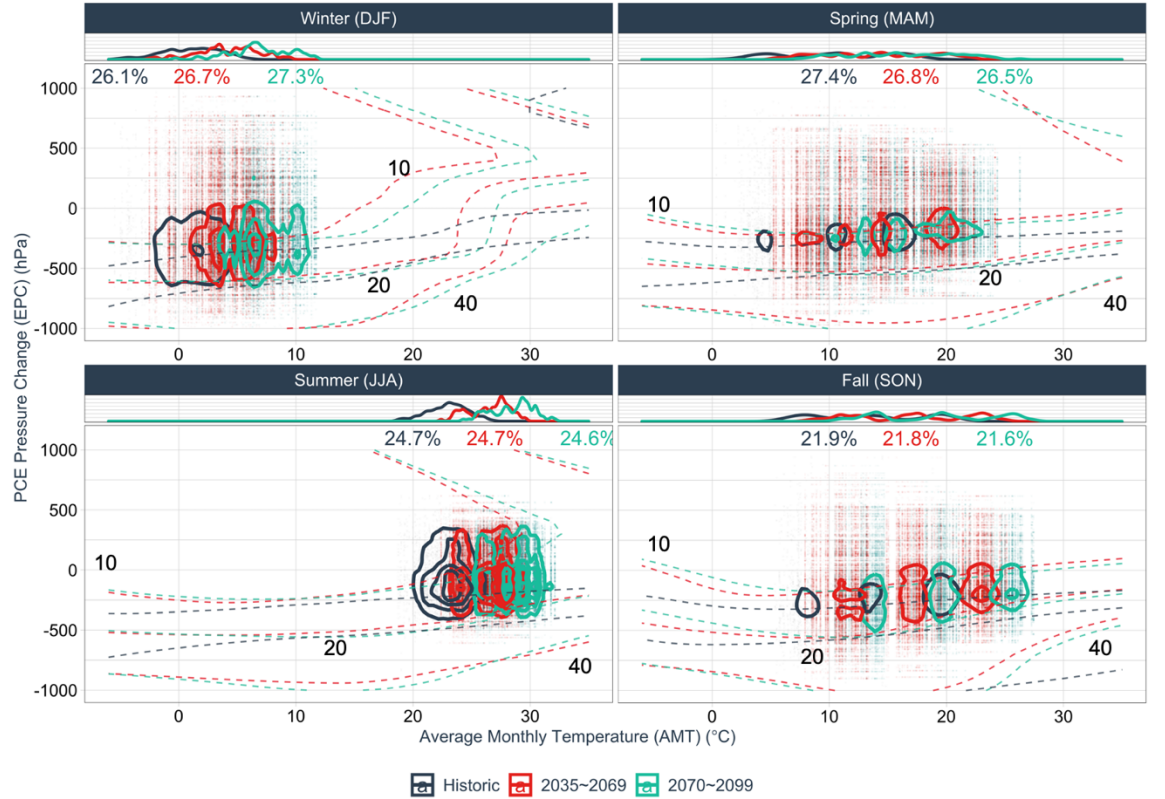


Figure . Seasonal average Precipitation Depth (PD) change vs. Cumulative Event Pressure Change (CEPC) & Average Monthly Temperature (AMT) in the Observed dataset and different projection periods. Solid contours represent the main distribution of Pressure Change Events (PCEs), while the dotted lines show the distribution of PD. Again, since contours indicate the distribution of PCEs qualitatively, their corresponding values are not shown. Dotted contours and labels in black are in millimeters indicating the local regression of PD vs. CEPC & AMT generated by the locfit function in R. The percentage numbers below the marginal density plots show the portion of PCEs of each season in a



year for different datasets.

## Key findings

The foundations of this algorithm are the relationships between precipitation and AMT using PCE characteristics as a media for interpreting the precipitation mechanism. With the logic that precipitation is subject to its PCE characteristics while the PCE occurrence is determined by temperature (AMT  $\rightarrow$  PCE

Precipitation), synthetic future precipitation time series were created using AMT as a primary input for generating PCE sequence under climate change. It is crucial that the algorithm has a sound physical basis because 1) the physical construct should not vary significantly as the climate changes and 2) empirical models may not be valid or accurate when extrapolated beyond observed datasets.

Many researchers have endeavored to describe the dependency of precipitation on temperature, such as prior and post temperature change to an extreme precipitation event in a tropical area [Visser *et al.*, 2020]. As atmospheric instability favors precipitation formation, high CEPC is an indicator for vertical air movement, condensation, and precipitation, and as such is representative of the CC relationship. Therefore, the extreme events (e.g., summer convections, Winter blizzards) with intensive precipitation formation mechanisms have the capability to deplete the precipitable moisture. The trend is apparent in InPCE as indicated by PD driven percentiles shown in Figure 5. As intensive and rainy InPCE are typically contributory to intensive DePCE, the CC relationship is an accurate representation of these conditions.

Figure 5 reveals that the PCE type plays an important role. Condensation is favored during DePCEs the intensity of which indicates the forces extracting moisture from the air. This could be a possible explanation for the stable distribution of PD over the temperature in Figure 5. At the same time, strong air convection requires the intake of air from surrounding regions that are much larger than the rainy zone itself. In other words, a high-intensity DePCE is balanced by a high-intensity wide-spreading InPCE. Thus, precipitation during InPCEs usually occurs when the observation site is originally outside of the core DePCE area but located on the path of the rainy zone movement. Consequently, not all available moistures can be condensed, and this condition is even capped by the moisture-holding capacity represented by the shift up of PD distribution for InPCE in Figure 5. The analysis also shows that during InPCEs, PD increases above 12°C in Figure 5, likely corresponding with the increased frequency of thunderstorms and other severe air convection beginning in Spring, and agreeing with condensed Summer PD contours in Figure 7.

The dissimilarities observed in intensive CEPC PD in Figure 3 suggest that extreme PD is likely to become more intensive in the future as the temperature warms. Given that Summer DePCEs is likely to skew toward non-high inten-

sity events (see Figure 7), intensive DePCEs ( -2000hPa ~ -300hPa) that cause extreme precipitation is likely to occur less frequently. Accounting for warming, the remaining extreme precipitation associated with intensive DePCEs would be benefited from the CC relationship and result in more severe precipitation stress in the future.

## Limitations and future efforts

One of the main purposes of this study was to demonstrate the physical soundness of PCE as a media to associate precipitation and temperature. Thus, the study did not include many climate models to obtain a robust sample size for analysis and the analysis was neither conducted statistically. We believe the physical phenomenon represented by PCE will be generally found in any climate model, but MIROC, the extreme condition, could embody it more pronouncedly than other mild models.

Although the results qualitatively agree with other research, the current algorithm resamples observed events without altering their volumes or temporal patterns whose changes are expected under global warming [*Fadhel et al.*, 2018; *Wasko and Sharma*, 2015]. Although better extrapolation of future precipitation can be made, introducing scaling parameters, however, may bring bias to the demonstration of this algorithm. Being conservative in this study to prove the physical soundness of PCE as the first step, our future work will focus on how to tune the model or scaling for extrapolation.

In addition, the hourly time step was not fine enough to reflect the temporal pattern of a precipitation event, especially in summer convections. To solve this issue, possible improvements could be 1) using new data in more granular temporal scales to embody the patterns of extreme weather events, 2) investigating the nexus of temperature, humidity, and pressure in triggering and producing precipitation, and 3) quantifying the scaling impact of climate change on the volume and temporal patterns of PCEs, which is the driven force of moisture extraction. In the contrast to precipitation, the above improvements can also be applied to drought since InPCE is very likely an important indicator of NO rain. More importantly, PCE brings the light to preserve the physical concepts that hold regardless of locations, time, and weather conditions while generating synthetic series. Once weather conditions can be classified properly by including PCE with other weather variables, all PCEs observed in the world can be polled to support the current non-parametric algorithm for any location at any time with any projected climate change temperature in the same physical system with significantly enhanced sample size.

## Summary and conclusion

A nonparametric stochastic algorithm for generating non-stationary hourly precipitation was developed. The semi-physical link between hourly precipitation and Average Monthly Temperature (AMT) was built using Pressure Change Event (PCE). Moving windows on both temperature and time were used to identify PCE and associated historical hourly rainfall observations that could be used to simulate future changing conditions. A multi-variate bootstrapping method was employed to reflect the covariance of Cumulative Event Pressure Change (CEPC) and PCE duration in a simulation process. This process is a very important finding that provides a sophisticated solution to build the relationship between Global Climate Model (GCM) temperature projections on a coarser temporal scale and climate characteristics on a finer scale.

After applying GCM AMT projections for the US Northeast until 2099, this algorithm was used to generate synthetic PCE ensembles and associated precipitation series qualitatively agreeing with the projections obtained by other researchers in terms of seasonal precipitation and extreme precipitation. Precipitation Depth (PD) was found to be highly correlated to PCE. The PCEs can be used to link temperature and precipitation dynamics, presenting a more physically plausible concept, in contrast to pure statistical assumptions used by most existing models.

Overall, the analysis suggests that:

- Increasing Pressure Change Event (InPCE) PD increases with AMT more significantly than with Decreasing Pressure Change Event (DePCE) which could be due to the point sourced data in this study
- In the NE US, more frequent mild and lighter precipitation events are likely to occur in the future during all seasons
- Overall, Summer precipitation is likely to be reduced, while Summer extreme events are likely to become more frequent under climate change
- Winter precipitation is likely to increase

Moreover, because PCEs are more strongly related to precipitation formation than coarser temporal scale temperature (e.g., monthly), this algorithm may represent a reliable method for downscaling precipitation from GCM AMT projections, which are more trustworthy than GCM precipitation projections on their own. Despite being non-parametrically structured, PCE could also be further explored as a means of integrating physically plausible synthetic future events into time series generated, even through parametric procedures.

In conclusion, this paper demonstrates a means of generating long, continuous, synthetic precipitation series scaled-down from GCM AMT projections. These series could then be used for a variety of climate change model applications, such

as hydrologic and hydraulic modeling, water resource modeling and agriculture applications, etc.

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## Acronyms and References

A glossary of acronyms

Acronyms	Description
AMT	Average Monthly Temperature
AOGCM	atmosphere-ocean general circulation models
BOS	Boston
CC	Clausius-Clapeyron
CMIP5	Coupled Model Intercomparison Project 5
CSO	Combined Sewer Overflow
DePCE	Decreasing Pressure Change Event
CEPC	Cumulative Event Pressure Change for a single pressure change event
GCM	Global Climate Model
GHG	Greenhouse Gas
GI	Green Infrastructure
Observed	The dataset of historical observations
InPCE	Increasing Pressure Change Event
KNN	K Nearest Neighbor
NCDC	National Climate Data Center
NCEI	National Center for Environmental Information
NYC	New York City
PCE	Pressure Change Event
PD	Precipitation Depth during a PCE
PHL	Philadelphia
POP	Probability of Precipitation
RCM	Regional Climate Model
RCP	Representative Concentration Pathway
SPG	Stochastic Precipitation Generator

Acronyms	Description
Forecasted	The dataset of 100 synthetic replications of climate projection of 2035~2099
Reanalysis	The dataset of 100 synthetic replications of 1975~2012
Win	The size of the moving window including both time and AMT dimensions

<https://books.google.com/books?id=qrcRAQAAIAAJ>

<https://books.google.com/books?id=PhjmnQEACAAJ>

<https://books.google.com/books?id=jvnQiFG3dPkC>

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## Appendix

### Geographic scope

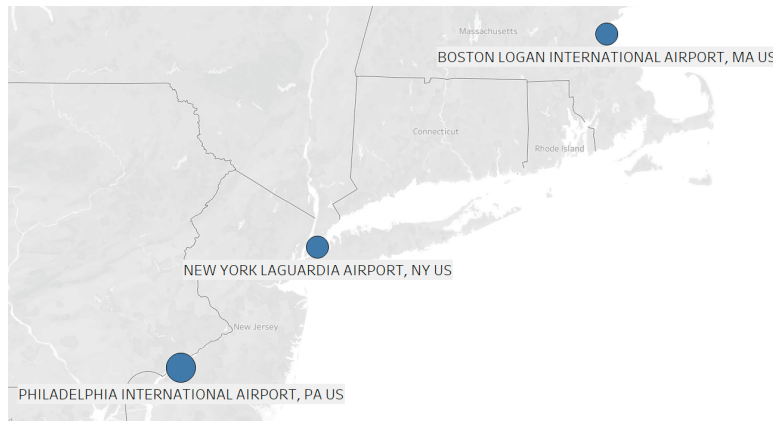


Figure . Locations of weather stations in the research area (size of circles indicates the length of available data) New York City (NYC) (station ID: 72503014732 for 1973~2018 & 99999914732 for 1948~1973), Philadelphia (PHL) (station ID: 72408013739 for 1973~2018 & 99999913739 for 1941~1973) and Boston (BOS) (station ID: 72509014739 for 1943~2018) from NOAA NCEI

### Dependence of precipitation on PCE characteristics

The CEPC magnitude and PCE duration are used in the KNN analysis because of their relationships to the stability of air masses. Since a collision of air mass is usually accompanied by pressure change, the PCE duration is considered a general indicator of the horizontal stability of the air mass over the weather station (i.e., a short PCE indicates a stable air system). Within an air mass, vertical stability is negatively associated with CEPC magnitude. For example, the smaller the CEPC, either DePCE or InPCE, the more vertically stable

the air mass, and vice versa. Precipitation is more likely to form in vertically unstable air masses [Ackerman and Knox, 2007; Ackerman and Knox, 2015], especially DePCE.

For illustration, Figure 9 graphically depicts the relationship between CEPC and PCE duration of all historical PCEs. The contours indicate that precipitation is more likely to occur during DePCE, favored by both intensity and duration.

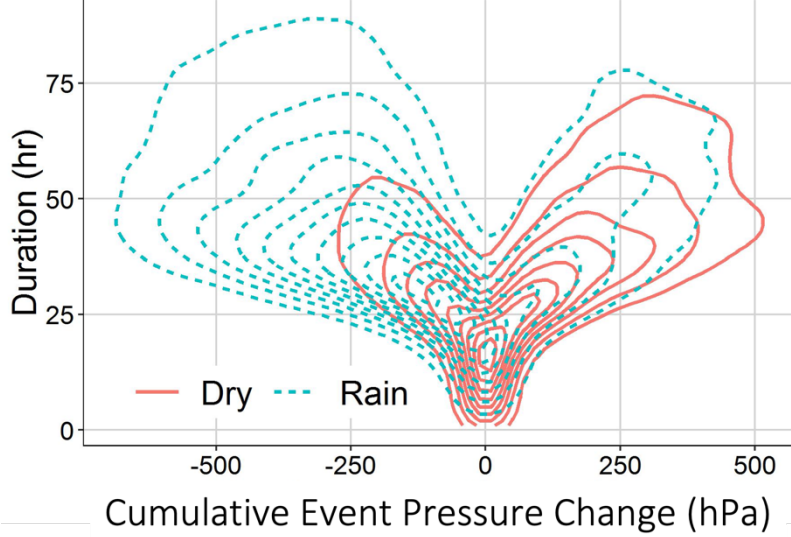


Figure 9. Precipitation dependence on both Pressure Change Event (PCE) duration and Cumulative Event Pressure Change (CEPC) (Red: dry PCE, Blue: wet PCE)

To consider both CEPC and duration of the stochastic process, the magnitude of a PCE is defined by Equation 7.

$$M_{\text{PCE}} = \sqrt{(d_z)^2 + (\text{CEPC}_z)^2} \text{ Equation 7}$$

Where  $M_{\text{PCE}}$  is the magnitude of a PCE; subscript  $z$  denotes the  $z$  score of the corresponding dataset;  $d_z$  and  $\text{CEPC}_z$  are the  $z$  scores of the duration and CEPC of the PCE, respectively. The conversion of the  $z$  score help obtain equal weighting for the two features in determining the magnitude of a PCE.

### K Nearest Neighbor (KNN) parameter selection

In Step 3 of the algorithm (Figure 1), the measure to determine the “nearest neighbors” is calculated by the Euclidian distance integrating both CEPC and PCE duration after scaling on the whole population. The value  $k$  is defined in the following equation suggested by *Lall and Sharma* [1996] on Page 684.

$$k = \sqrt{n}$$

where  $n$  is the number of PCE in  $\{\text{PCE}\}$

## Relationship between POP and CEPC

In Figure 10, as the magnitude of CEPC increases, the POP of DePCE climbs from 15% to 100% within  $0 \sim -800$  hPa, while InPCE POP increases only from 15% to about 50% within  $0 \sim 1000$  hPa. Given the limited sample size of extreme InPCE ( $n = 79$  when  $\text{CEPC} > 820$  hPa in historical data), less confidence is associated with the POP beyond 820 hPa. For  $\text{CEPC} < -1000$ , there are 5 historical PCE observed in BOS between 1944 and 1946 without precipitation. But all of them have a sudden air pressure drop about 100 hPa within 1 hour, which lead to a heavy bias. Although these events are excluded in the analysis in our model, we treat the POP in this range as 100% regardless of the decreasing trend lines. Thus, falling pressure appears to be a better indicator of precipitation than increasing pressure.

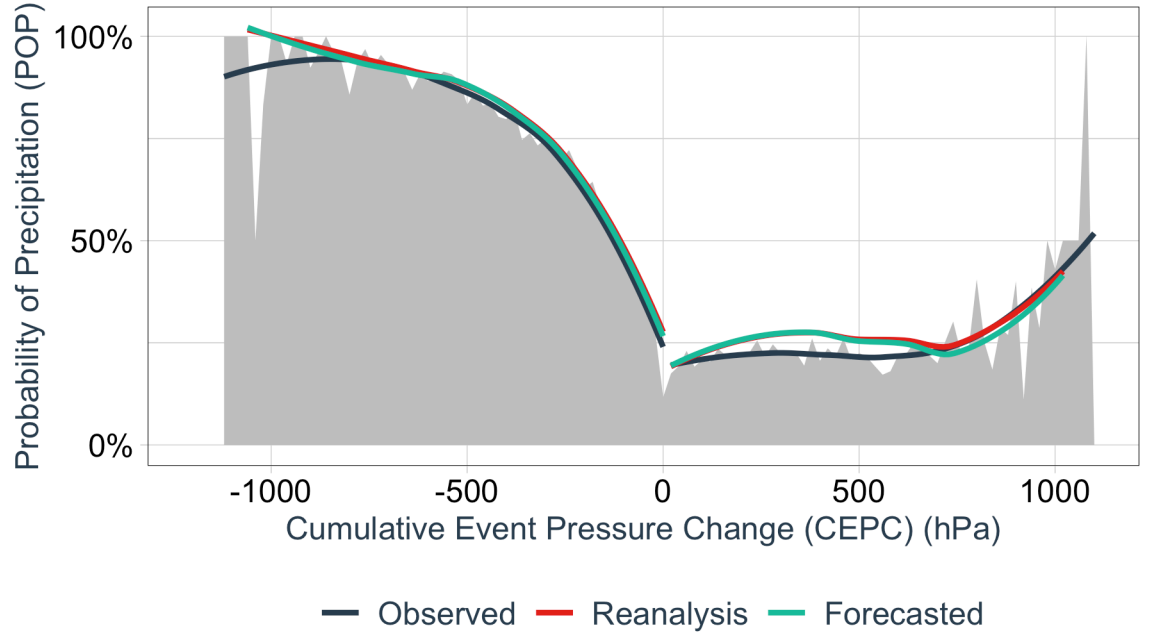


Figure . Dependence of Probability of Precipitation (POP) on Cumulative Event Pressure Change (CEPC). The grey area represents the Observed data. All datasets are fitted by loess regression in different colors separated by two types of Pressure Change Event (PCE) at  $\text{CEPC} = 0$  hPa.

In Figure 11, the POP in Spring for DePCE historically oscillates between 50%

to 70% with a low end at around 19°C. Despite the decrease beyond 15°C, its synthetic trend bears a similar general level. As for InPCE, POP remains around 25% for both the Observed and the Forecasted. The Forecasted POP trend on AMT spans a larger range than the Observed with a similar pattern after 5°C. This situation could also be found similar in Summer and Fall for both PCE types. Despite similar patterns, the Winter POP of both PCE types historically increases after 6°C while the Forecasted series remain stable. This indicates that the rain likelihood would be lowered for warm Winters in the future in this region. Focusing on the low variation parts in the middle-temperature range of all seasons, the POPs for both PCE types generally match between the Observed and the Forecasted.

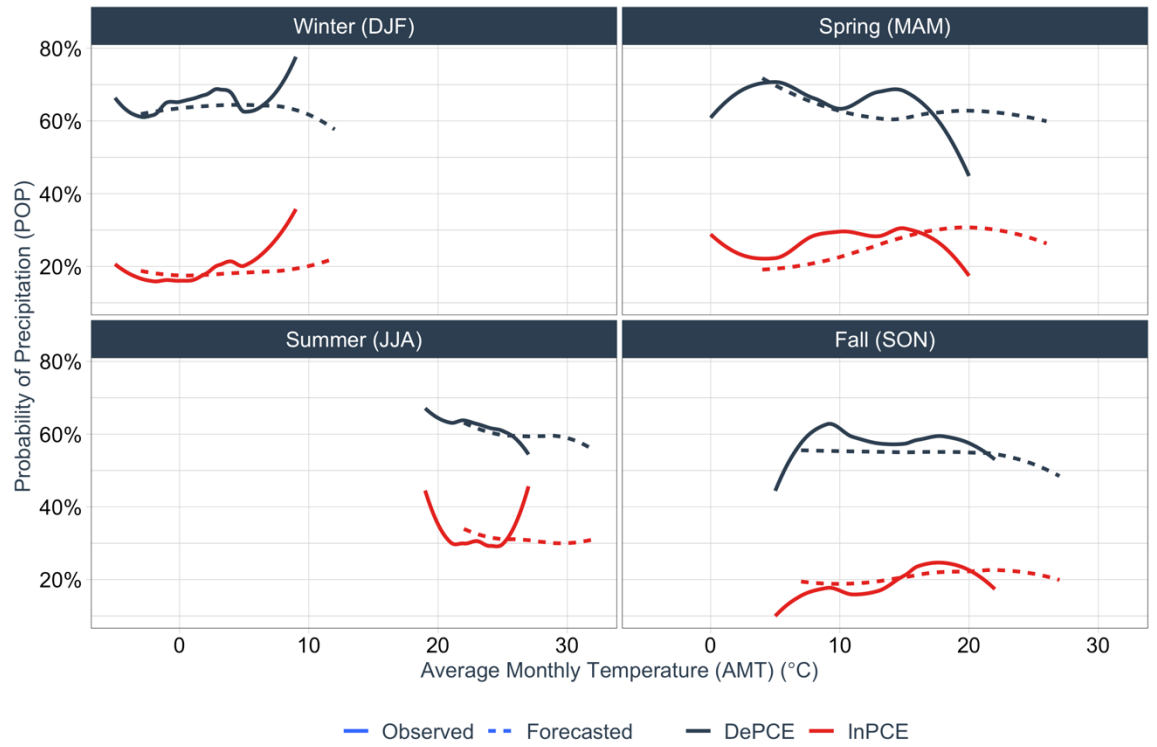


Figure 11. Seasonal dependence of Probability of Precipitation (POP) on Average Monthly Temperature (AMT). The average POP for each AMT from the Observed and the Forecasted datasets is differentiated by solid lines and dotted lines. Pressure Change Event (PCE) types are colored differently.