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**Three-Dimensional Dynamic Rupture Simulations on Partially-Creeping Strike-Slip Faults**

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**Key Points:**

- Patches of aseismic creep can be barriers to rupture, depending on their positions and dimensions.
- Rupture can propagate around creeping zones only if there is a wide enough locked area to maintain directivity and rupture energy.
- Rate-strengthening friction in creeping zones depletes the energy of the rupture front until it stops.

21 **Abstract**

22 Partially creeping faults exhibit complex behavior in terms of which parts of the fault slip  
23 seismically versus aseismically. The specific geometry of creeping versus locked fault patches  
24 may pose constraints on rupture lengths on partially-creeping faults. We use the 3D finite  
25 element method to conduct dynamic rupture simulations on simplified partially-creeping strike-  
26 slip faults, to determine whether coseismic rupture can propagate into creeping regions, and  
27 how the presence and distribution of creeping regions affects the ability of rupture to  
28 propagate across the whole fault. We implement rate-state friction, in which locked zones are  
29 represented by rate-weakening behavior and creeping zones are assigned rate-strengthening  
30 properties. We model two simplified geometries: a locked patch at the base of a creeping fault  
31 and a creeping patch at the surface of a locked fault. In the case of a locked patch within a  
32 creeping fault, rupture does not propagate far past the edges of the locked patch, regardless of  
33 its radius. The case of a creeping patch within a locked fault is more complicated. The width of  
34 the locked areas around the creeping patch determine whether rupture is able to propagate  
35 around the creeping patch. Although rupture is always able to propagate at least a small  
36 distance into the creeping patch, if the width of the locked zone between the edge of the  
37 creeping patch and the end of the fault is too narrow, rupture stops. This simplified parameter  
38 study may be useful for understanding first-order behaviors of real-world partially-creeping  
39 strike-slip faults.

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## 44 1 Introduction

45 Partially-creeping faults are faults which sustain both non-episodic, measurable surface  
46 creep, and large-scale dynamic rupture. Partial creep defines the base and the top of the  
47 seismogenic zone in subduction zones (e.g. *Shibazaki and Shimamoto* [2007], *McCaffrey et al.*  
48 [2008]), but it also occurs on strike-slip faults around the world, most famously in the northern  
49 San Andreas Fault system in California (e.g. *Schulz et al.* [1982]; *Lienkaemper et al.* [2014];  
50 *Murray et al.* [2014]). Variations in creep may be spatial, with patches of creep within a locked  
51 fault or vice versa, as is the case with the Hayward Fault in the San Francisco Bay Area (e.g.  
52 *Lienkaemper et al.* [1991]) or the San Andreas Fault near Parkfield (e.g. *Harris and Segall* [1987],  
53 *Waldhauser et al.* [2004]). They may also be temporal, where patches that seem to creep  
54 interseismically rupture coseismically, as in the 2011 Tohoku, Japan earthquake (e.g. *Kodaira et*  
55 *al.* [2012]); or faults which appeared fully locked creep following a rupture, as in the 2014 South  
56 Napa, California earthquake (e.g. *Lienkaemper et al.* [2016]; *Floyd et al.* [2016]) or following an  
57 earthquake on another fault, as with the Garlock Fault following the 2019 Ridgecrest, California  
58 earthquake (e.g. *Barnhart et al.* [2019]; *Bilham and Castillo* [2020]).

59 The observation that locked and creeping patches may exist on the same fault, and that  
60 the same patches of fault may creep or rupture at different points in the earthquake cycle,  
61 poses important questions for fault dynamics. There is the matter of how rupture negotiates  
62 the frictional and stress complexity that comes with a partially-creeping fault releasing stress  
63 interseismically, of how that behavior controls the endpoints of such ruptures, and of how  
64 rupture lengths and positions may or may not change over multiple seismic cycles. Here, we use  
65 dynamic rupture modeling to focus on the issue of how variation in creeping/locking properties  
66 along a strike-slip fault affects rupture behavior in a single earthquake.

67 Dynamic rupture models are frequently used in parameter studies on the effects of  
68 complex fault geometry and stress state on rupture behavior and termination (e.g. *Harris and*  
69 *Day* [1993]; *Kame et al.* [2003]; *Oglesby* [2008]; *Lozos et al.* [2011]; *Harris et al.* [2018]; *Wang et*  
70 *al.* [2020]). Dynamic modeling has also been used to investigate how varying individual  
71 frictional and weakening parameters affects rupture behavior (e.g. *Nielsen et al.* [2000]; *Kaneko*  
72 *et al.* [2008]; *Ryan and Oglesby* [2014]; *Lozos et al.* [2014]).

73 In the specific context of dynamic rupture on a partially-creeping strike-slip fault, we  
74 are only aware of dynamic rupture modeling studies related to specific real-world faults. *Lozos*  
75 *et al.* [2015] conducted models of ruptures on the partially-creeping Bartlett Springs fault in  
76 northern California, and found that reduced shear stress due to creep prevented coseismic  
77 rupture from propagating through the entire fault. *Stephenson and Lapusta* [2018] modeled  
78 ruptures across the creeping section of the San Andreas Fault in central California, and found  
79 that rupture could only propagate through if strong dynamic weakening was imposed. *Harris et*  
80 *al.* [2019] modeled ruptures across the Calaveras-Hayward-Rodgers Creek fault network in the  
81 San Francisco Bay Area, and found that creeping patches prevented rupture from propagating  
82 through the entire system of faults regardless of nucleation location. *Lozos and Funning*  
83 [submitted to this issue] modeled the Hayward Fault alone, and also found that frictional and  
84 stress contrasts associated with creep kept rupture confined to locked patches. The only  
85 partially-creeping fault parameter studies of which we are aware are on subduction zones (e.g.  
86 *Noda and Lapusta* [2013]), which have considerably different kinematics from strike-slip faults.

87 In the present study, we conduct a series of dynamic rupture models for two different  
 88 simplified cases of a vertical, planar, partially-creeping strike-slip fault: one in which a patch of  
 89 surface creep is embedded near the surface in a predominantly locked fault, and one in which a  
 90 locked patch is embedded at the base of a predominantly creeping fault.

## 93 2 Methods

94 We use FaultMod [Barall, 2009], a 3D finite element code which has performed  
 95 consistently in the Southern California Earthquake Center's dynamic rupture code verification  
 96 exercise [Harris et al., 2009; Harris et al., 2018], to conduct dynamic rupture models of partially-  
 97 creeping planar strike-slip faults embedded in a homogeneous fully elastic half space. These  
 98 models represent a single coseismic rupture, and do not incorporate the physics of the process  
 99 of aseismic creep; we model only the effects of creeping zones (i.e., zones of rate-strengthening  
 100 friction) on coseismic rupture propagation.

102 Table 1. Physical and Computational Parameters

Shear stress	75 MPa
Normal stress	120 MPa
a (rate weakening)	0.008
a (rate strengthening)	0.016 (strong), 0.014 (weak), 0.012 (neutral)
b	0.012
$f_0$	0.6
$V_0$	$1 \times 10^{-6}$ m/s
$D_c$	0.02015 m
$\psi_{init}$	0.135524
P wave velocity	6000 m/s
S wave velocity	3464 m/s
Density	2670 kg/m <sup>3</sup>
Element size	200 m
Nucleation radius	3000 m
Nucleation shear stress	100 MPa

103 We implement rate-state friction, specifically a modified Dieterich-Ruina aging law  
 104 [Dieterich, 1978; Ruina, 1983]:  $\tau = a\sigma_d \text{arcsinh}[(V/2V_0)\exp((f_0+\psi)/a)]$ , where state variable  $\psi$  is  
 105 defined as  $d\psi/dt = -(bV_0/L)(\exp(-\psi_{ss}/b) - \exp(-\psi/b))$ ,  $\psi_{ss}$  is the state variable at steady state,  $V$  is  
 106 the slip rate,  $V_0$  is a reference velocity,  $f_0$  is a reference friction coefficient,  $\tau$  is shear stress,  $\sigma_d$  is  
 107 time-dependent normal stress, and  $a$  and  $b$  are dimensionless direct effect parameters. It is the  
 108 difference between  $a$  and  $b$  that controls the overall frictional behavior of the fault. If  $b-a$   
 109 is positive, the steady-state friction on the fault weakens as the slip rate increases, allowing for  
 110 normal dynamic rupture, while a negative  $b-a$  means that the fault strengthens with increased  
 111 slip rate, thus promoting aseismic creep and disfavoring coseismic rupture. If  $b-a$  is zero, the  
 112 fault is rate-neutral, meaning that it neither actively weakens with increasing slip rate, nor  
 113 actively resists slip.

115 Laboratory friction experiments on rocks collected from creeping fault zones (e.g.  
116 *Moore and Rymer* [2007]; *Moore et al.* [2018]) show that these rocks exhibit rate-strengthening  
117 behavior. As such, there are a number of modeling studies on aseismic slip processes such as  
118 afterslip and creep events which implement rate-strengthening friction on creeping faults (e.g.  
119 *Barbot et al.* [2009], *Kaneko et al.* [2013], *Wei et al.* [2015]). We therefore follow this example  
120 and parameterize the creeping sections of our model faults with rate-strengthening friction,  
121 while the locked sections of the fault have rate-weakening properties. We use three different  
122 creep parameterizations: one with stronger rate-strengthening properties, which should be  
123 more resistant to coseismic rupture; one with weaker rate-strengthening; and one case with  
124 rate-neutral properties. In all of our models, we force nucleation within the rate-weakening  
125 zones by raising the shear stress above the yield stress and forcing rupture to propagate over a  
126 fixed radius that is larger than the critical patch size needed for self-sustaining rupture  
127 propagation. We use the same parameters as in the friction law comparison parameter study of  
128 *Ryan and Oglesby* [2014]. We list our physical and computational parameters in Table 1.

129 We show the geometry for our models of a creeping patch embedded within a locked  
130 fault in Figure 1. We place a semi-circular rate-strengthening patch at the top center of the  
131 fault, as a representation of a fault with measurable surface creep, similar to the Green Valley  
132 Fault and one interpretation of the Bartlett Springs Fault [*Lienkaemper et al.*, 2014]. In the  
133 primary set of models, we test creeping patch radii of 4, 6, 8, 10, and 12 km, while keeping the  
134 other fault dimensions fixed, and keeping the nucleation at 3 km from the left edge of the fault  
135 and 8 km from the base of the fault. In order to test for horizontal directivity effects, we also  
136 conducted a set of models in which we extended the length of the fault as we increased the  
137 radius of the creeping patch, thus keeping the nucleation point at the same distance from the  
138 edge of the creeping patch in all cases. Similarly, we tested for vertical directivity effects by  
139 conducting a set of models in which we increased the depth of the fault as we increased the  
140 radius of the creeping patch, and varied the nucleation point such that the distance between it  
141 and the edge of the creeping patch was the same in all cases.

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Figure 1.



Figure 1. Cartoon of fault geometry, for models with a rate-strengthening patch embedded within an otherwise rate-weakening fault. Dotted lines indicate dimensions that we varied within our exploration of parameter space.

159 Figure 2 shows the geometry of our models of a locked patch embedded within a  
160 creeping fault. In these models, we place a semi-circular rate-weakening patch at the base of  
161 the fault, also to represent a fault with measurable surface creep, similar to the Hayward Fault  
162 [Schmidt *et al.*, 2005; Funning *et al.*, 2009] and another interpretation of the Bartlett Springs  
163 Fault [Murray *et al.*, 2014]. As in the previous set of models, we tested locked patch radii of 4,  
164 6, 8, 10, and 12 km, while keeping the other fault dimensions constant. Our forced nucleation in  
165 these models is at the center of the locked patch. Because rupture directivity in these cases is  
166 controlled by the size of the locked patch, we did not conduct models with variable fault length  
167 or basal depth in this creep/locking configuration.

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Figure 2.

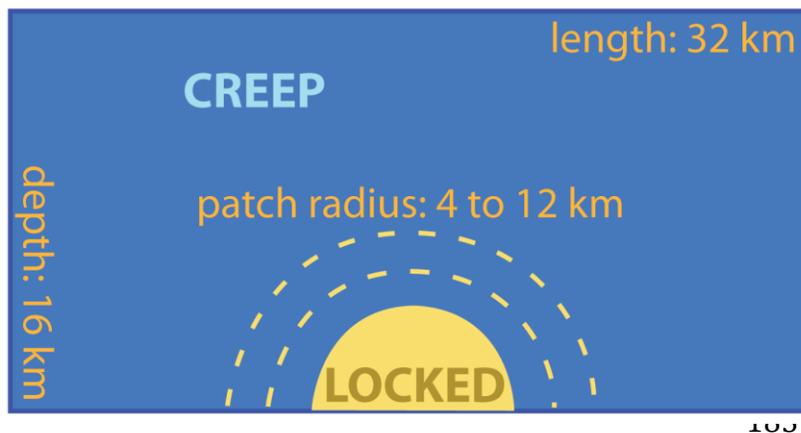


Figure 2. Cartoon of fault geometry, for models of a rate-weakening patch in an otherwise rate-strengthening fault. The radius of the locked patch is the only variable dimension here; the fault length and depth are fixed.

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### 3 Results

#### 3.1 Creeping Patch Within a Locked Fault

188 In the set of models in which we keep the fault dimensions constant but vary the radius  
189 of the creeping patch, we find that the radius of the creeping patch controls both the ability of  
190 dynamic rupture to propagate across the entire length of the fault, and the ability of the  
191 creeping patch to sustain coseismic slip. Figure 3 shows the maximum horizontal slip rate  
192 sustained across the fault in these models, using the stronger rate-strengthening properties for  
193 the creeping patches. We do not show vertical slip rate because we set these models up to  
194 produce strike-slip motion, and any dip-slip movement is negligibly small compared to the  
195 horizontal motion. We find that, if the radius of the creeping patch is half, or less than half of  
196 the seismogenic thickness of the fault, rupture is able to propagate past the creeping patch,  
197 along the full strike of the fault. In these cases, the primary rupture through the locked part of  
198 the fault progresses along strike and wraps around the creeping patch, after which point slower  
199 slip propagates inward into the creeping patch. For radii of 4 and 6 km, the entire creeping  
200 patch sustains some coseismic slip, but slip does not reach the center of the patch in the  
201 models with an 8 km or greater patch radius. In models with a patch radius of greater than half  
202 the seismogenic thickness of the fault (10 and 12 km), rupture stops within the narrow locked  
203 zone between the edge of the creeping patch and the base of the fault. In these models, the

204 left edge of the creeping patch, closer to the forced nucleation point, sustains some slow  
205 coseismic slip, but this does not progress as far into the creeping patch as in the models where  
206 dynamic rupture is able to wrap around the patch and then propagate inward.

207 Using weaker rate-strengthening properties for the creeping patches does not have a  
208 first order effect on rupture's ability to propagate across the entire fault (see supplemental  
209 figures S1), though it does allow for the creeping patches to sustain more coseismic slip and  
210 higher slip rates than in the models with stronger rate-strengthening properties. Using rate-  
211 neutral properties for the creeping patches (supplemental figure S2) allows rupture to  
212 propagate through or around creeping patches with radii up to 10 km, rather than 8 km, but the  
213 12 km radius case still stops rupture before it reaches the other end of the fault.

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Figure 3.

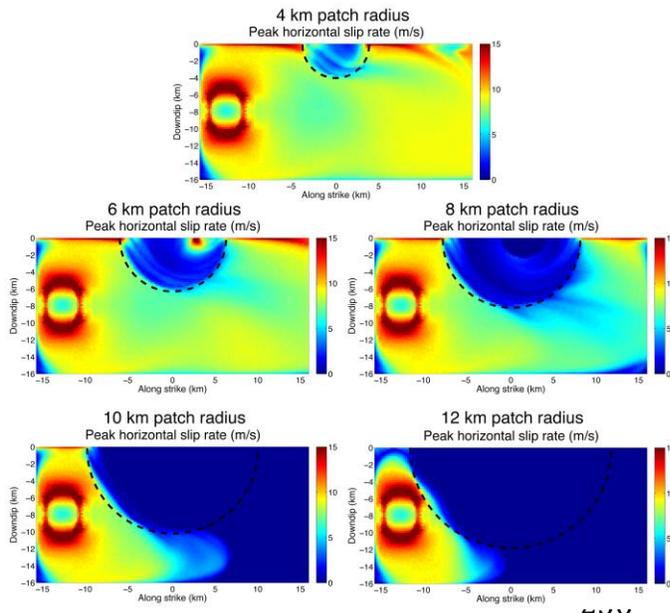


Figure 3. Plots of maximum horizontal slip rate for models of a rate-strengthening/creeping patch within an otherwise rate-weakening/locked fault. The dashed black line marks the edge of the creeping patch. The ring of high slip rate to the left of the fault represents the forced nucleation zone. Dynamic rupture progresses through the creeping patch in the 4 km radius model, whereas it wraps around the creeping patch and then propagates bilaterally inward in the 6 and 8 km radius models. The zone of high slip rate within the creeping patch in the 6 km radius model represents the coalescence of the rupture fronts propagating inward from either side. If the creeping patch is greater than 8 km in radius, it prevents the rupture from propagating to the other end of the fault.

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Next we investigate the maximum slip rate for the set of models in which we extend the length of the fault by the same amount as we increase the radius of the creeping patch, thereby ensuring that the rupture front is able to build up the same amount of directivity before reaching the edge of the creeping patch, regardless of the patch radius. We show these results in in Figure 4. This additional energy due to directivity did not affect the ability of rupture to propagate across the entire fault. Creeping patch radii of greater than half the seismogenic thickness of the fault still arrested rupture propagation. The primary effect of extending the length of the fault was increased extent and amount of coseismic slip within the creeping patches.

248 Figure 4.

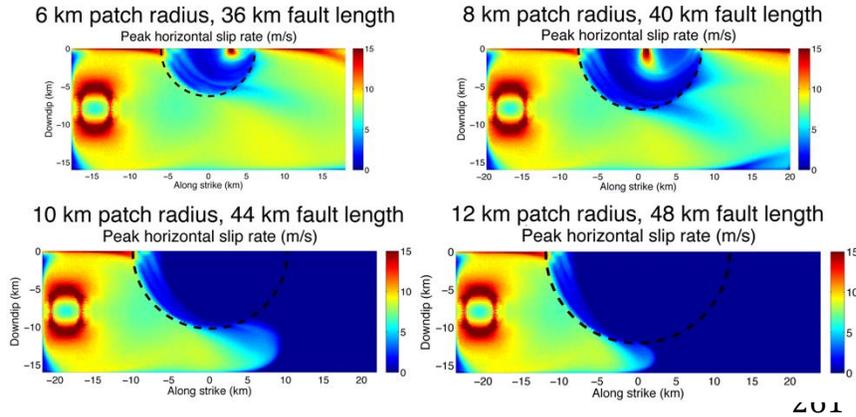


Figure 4. Plots of maximum horizontal slip rate for models of a rate-strengthening/creeping patch within an otherwise rate-weakening/locked fault, with the length of the fault scaled by the radius of the creeping patch. The ring of high slip rate to the left of the fault represents the forced nucleation zone. The dashed black line marks the edge of the creeping patch. Increasing the

262 length of the fault has no first-order effect on rupture's ability to propagate along strike (compare to Figure 3), but  
 263 the larger directivity effect that results from rupture propagating a larger distance before reaching the creeping  
 264 patch allows for more coseismic slip within the creeping patch. The areas of particularly high slip rate within the  
 265 creeping patch in the 6 and 8 km radius models represent the coalescence of two rupture fronts propagating  
 266 inward from either side of the patch.  
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268 The models in which we increased the depth of the fault as we increased the radius of  
 269 the creeping patch are shown in Figure 5. Keeping the distance between the base of the  
 270 creeping patch and the base of the fault fixed allowed rupture to propagate through the full  
 271 strike of the fault in all cases. However, rupture was unable to propagate all the way to the  
 272 surface of the fault in the models with the largest patch radii. Increasing the basal depth of the  
 273 fault also has little effect on the ability of the creeping patch to sustain coseismic slip.  
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Figure 5.

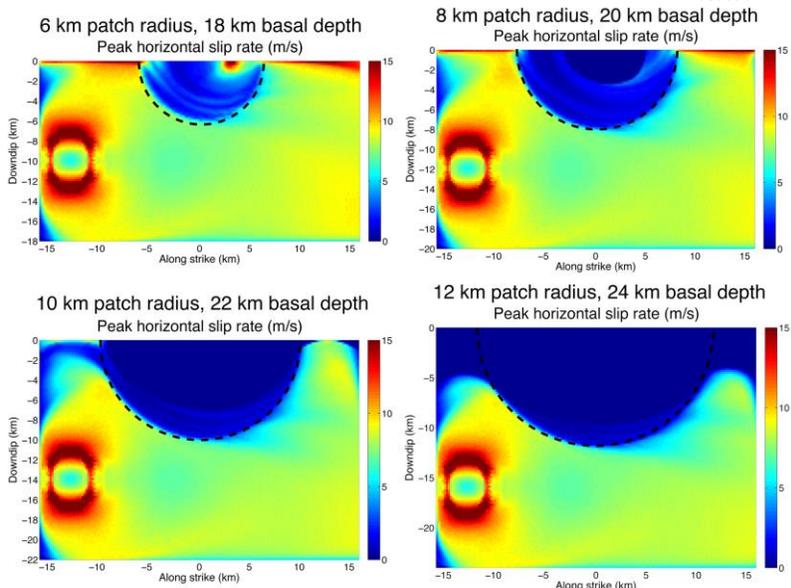


Figure 5. Plots of maximum horizontal slip rate for models of a rate-strengthening/creeping patch within an otherwise rate-weakening/locked fault, with the basal depth of the fault scaled by the radius of the creeping patch. The dashed black line marks the edge of the creeping patch. The ring of high slip rate to the left of the fault represents the forced nucleation zone. In all cases, rupture propagates along the full extent of the fault strike, but larger creeping patches prevent surface rupture. As in the set of models with a constant 16 km basal depth, smaller creeping patches sustain higher slip rates.

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### 3.2 Locked Patch Within a Creeping Fault

The radius of a locked patch within a predominantly creeping fault has very little effect on the overall rupture behavior other than to increase the size of the slipping region. In all of these models (see Figure 6), rupture propagated to the edges of the locked patch, then died out within 1 km of the interface between the locked patch and the creeping zone. Even in the model with a 4 km locked patch radius, in which the radius of the forced nucleation zone was larger than the radius of the locked patch and dynamic rupture was forced into the rate-strengthening zone, rupture still stopped within 1 km of the edge of the forced nucleation zone. Implementing a weaker rate-strengthening effect (supplementary figure S3) for the creeping parts of the fault slightly increased how far coseismic slip was able to propagate into the creeping zone before coming to a halt, but this effect was not significant enough to allow full dynamic rupture through a rate-strengthening zone. For the most part, implementing rate-neutral friction in the creeping zones (supplementary figure S4) follows this pattern, with slightly more slip slightly further outside the locked patch. However, the 12 km radius case does have full rupture of the fault, since the area of creeping fault between the top of the locked patch and the free surface is small enough that waves from the rupture in the locked patch are able to interact with the free surface, producing high slip rates there (e.g. *Kaneko and Lapusta [2010], Hu et al. [2019]*). Despite this effect at the surface, slip rates remain low between the top of the fault and the free surface.

Figure 6.

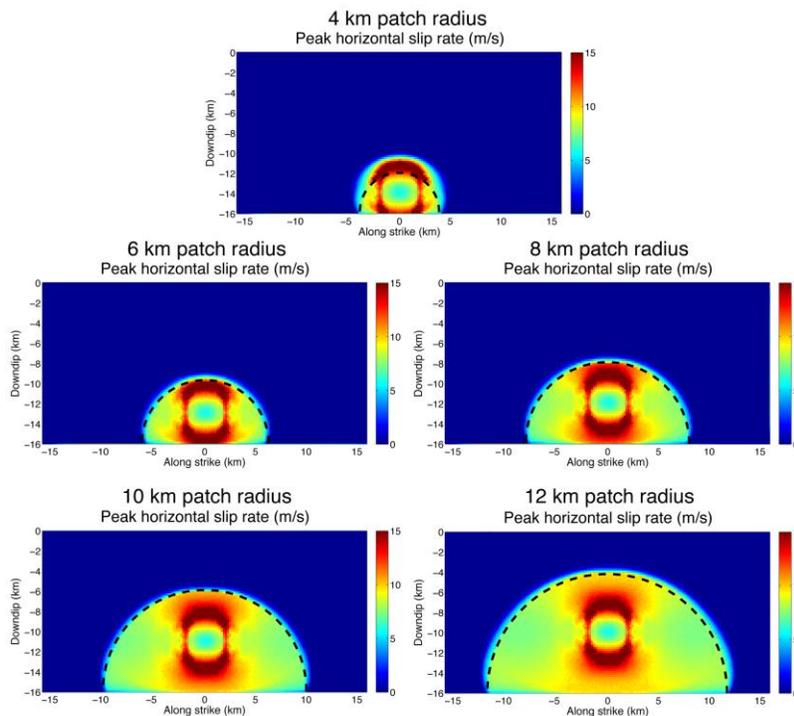


Figure 6. Plots of maximum horizontal slip rate for models of a locked/rate-weakening patch within an otherwise creeping/rate-strengthening fault. The dashed black line indicates the edge of the locked patch. The ring of highest slip rate in the center of the locked patch represents the forced nucleation zone. Note that regardless of the size of the locked patch, rupture does not propagate more than 1 km beyond the edge of the patch into the creeping zone – which is consistent with past work on high-strength asperities in low-stress faults (e.g. *Day [1982]*). In addition, in the 4 km patch radius model, the size of the forced nucleation zone is larger than the size of the locked patch, but even forced propagation into the creeping part of the fault does not result in self-sustaining rupture outside of the forced nucleation zone.

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#### 347 **4 Discussion**

348 We find that the dimensions of the creeping parts of a fault relative to the locked parts  
349 have a strong effect on the overall rupture behavior and extent. In particular, our results  
350 suggest there must be a critical width of locked fault through which full dynamic rupture can  
351 propagate around a creeping zone. If the narrowest dimension of the locked zone is between  
352 the base of the fault and the furthest down-dip edge of the creeping patch, as in the 10 and 12  
353 km radius cases in Figure 3, along-strike rupture may be halted. Similarly, if the narrowest  
354 dimension is between the end of the fault and the nearest along-strike edge of the creeping  
355 patch, as in the 12 km radius case in Figure 5, rupture may be prevented from reaching the  
356 surface of the fault. This is very similar to studies of dynamic rupture propagating around high-  
357 stress or geometrical asperities in locked strike-slip faults (e.g. *Day [1982], Das and Kostrov*  
358 *[1983]*); this presents the possibility of treating creeping patches as generalized barriers in  
359 hazard assessments.

360 That said, in the specific context of rate-strengthening creeping patches, this barrier  
361 effect is a result of how the energy budget of a rupture front is divided. A rupture propagating  
362 along a homogeneous rate-weakening fault builds up energy ahead of the rupture front in the  
363 direction of rupture, and can expend most of that energy on seismic radiation and increasing its  
364 propagation speed, rather than on fracture energy or friction. Creeping patches with smaller  
365 radii do not pose much of an interruption to directivity and to this buildup of energy, which is  
366 why fracturing and slipping into the rate-strengthening patch do not use so much of the energy  
367 budget such that none is left for propagation and radiation. However, a creeping patch with a  
368 large radius alters the energy balance both by requiring more energy to go into fracturing  
369 through the creeping area, and by decreasing the area of fault that is building up more energy  
370 ahead of the rupture front. Thus, the rupture becomes less energetic overall, and is spending  
371 more of the remaining energy on fracture and less on propagation and radiation, which  
372 ultimately leads to the rupture dying out in the narrow locked zone and not propagating as far  
373 into the creeping patch.

374 We illustrate this effect in Figure 7. There is not currently a rate-state friction-specific  
375 equation for energy budget, but *Ryan and Oglesby [2014]* show that, at coseismic rupture  
376 speeds, rate-state friction and slip-weakening friction behave nearly identically. Therefore, we  
377 adapt our data to the slip-weakening friction formulation of *Kanamori and Rivera [2006]*. The  
378 total energy available for rupture propagation is given as  $E_{t0} = \frac{1}{2}(\tau_1 - \tau_2)DA$ , where  $\tau_1$  is initial  
379 shear stress,  $\tau_2$  is final shear stress,  $D$  is fault displacement, and  $A$  is fault area. The fracture  
380 energy in the rupture front is given as  $E_g = (\tau_p - \tau_1)D_c A / 2$ , where  $\tau_p$  is the yield stress,  $\tau_1$  is the  
381 initial shear stress,  $D_c$  is the critical slip-weakening distance, and  $A$  is the fault area. In adapting  
382 these theoretical formulas to plot model results, we use the slip-weakening friction distances  
383 and coefficients from *Ryan and Oglesby [2014]* that correspond to the rate-state parameters in  
384 this study. We set  $\tau_0$  to be the initial pre-rupture shear stress at each node on the fault,  $\tau_1$  as the  
385 yield stress at each node, and  $\tau_2$  as the final shear stress at each node after the fault has fully  
386 weakened.  $D$  is the total displacement at each fault node; if  $D$  is larger than the critical  
387 weakening parameter  $D_c$ , we set  $D = D_c$ . Since we calculate these parameters at each fault  
388 node, we use the area of one on-fault element for the parameter  $A$ .

389            These formulas represent the energy budget of an entire fault for an entire earthquake,  
 390 so it is not rigorously correct to use them to indicate the energy budget for individual time-  
 391 steps at many finite points on the fault. However, they still provide a general qualitative insight  
 392 into the relative partitioning of energy during fault rupture, given that we are trying to illustrate  
 393 a first-order effect. Figure 7 clearly shows that the total available rupture energy ( $E_{to}$ ) drops  
 394 significantly as the rupture front reaches the creeping patch, while fracture energy ( $E_g$ ) rises, as  
 395 does the ratio of  $E_g$  to  $E_{to}$ .

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 397 Figure 7.

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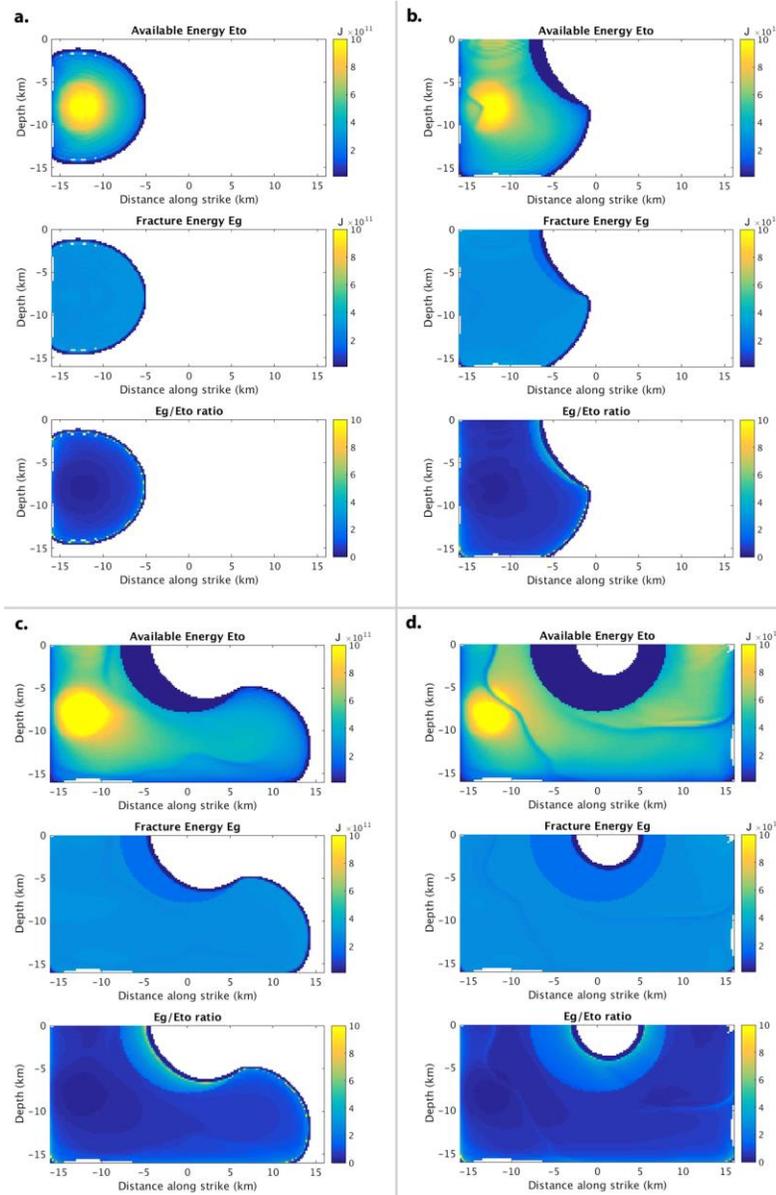


Figure 7. Snapshots of a rough estimate of the energy budget as rupture progresses, for the 8 km creep radius case.  $E_{to}$  is the available energy for rupture, and  $E_g$  is the fracture energy in the rupture front, based on equations from *Kanamori and Rivera [2006]*. We plot energy budget in parts of the fault which are slipping at faster than 1 mm/s. The rupture front itself is most clearly visible in the  $E_g/E_{to}$  ratio plots, where there is a sharp contrast between dark blue and yellow/orange.

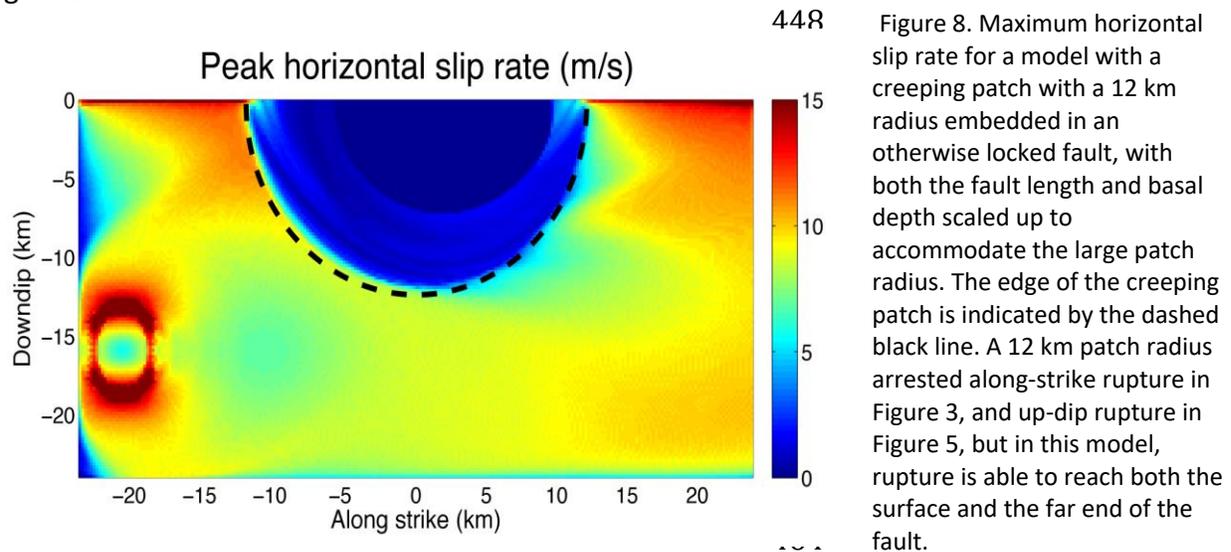
a. The rupture so far has been entirely in the locked zone.  $E_g$  and  $E_{to}$  are comparable.  
 b. The rupture front encounters the creeping patch. Both  $E_{to}$  and  $E_g$  drop, but  $E_g$  is now higher than  $E_{to}$ . The ratio goes up.  
 c. Rupture progresses faster through the locked zone than the creeping patch.  $E_{to}$  and  $E_g$  are still comparable in the rate-weakening zones. Both are still lower in the creeping patch, but the  $E_g/E_{to}$  ratio remains high.  
 d. The locked zones of the fault have completely ruptured, and slow rupture continues into the unfavorable creeping patch. The total energy remains low, but the  $E_g/E_{to}$  ratio remains high.

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438 As a test of this energy budget imbalance and critical width effect, we conducted a  
439 model in which a creeping patch with a 12 km radius is embedded in a fault that is as long as  
440 the 12 km radius case in Figure 3 and as deep as the 12 km radius case in Figure 5, thus  
441 eliminating any major narrowing of the locked zone. In this model, the results of which are  
442 shown in Figure 8, rupture propagated from end to end of the fault, and from base to surface.  
443 Because it propagated through a much larger locked area than in the other models, this rupture  
444 front was able to build up enough energy that it was able to propagate much further into the  
445 creeping patch than in any of our other models.  
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447 Figure 8.



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467 The balance of the energy budget is also why the cases in which the rate-weakening part  
468 of the fault is completely surrounded by rate-strengthening all result in rupture stopping within  
469 a short distance of the edge of the locked patch. In these cases, the available energy for rupture  
470 still decreases when rupture reaches the rate-strengthening zone, but here, the rate-  
471 strengthening zone is most of the fault. While the fracture energy initially does rise relative to  
472 the rupture energy, the lack of ongoing rupture in a rate-weakening zone elsewhere on the  
473 fault, and therefore the lack of energy accumulation ahead of the rupture front, decreases the  
474 total energy in the system, and the rupture front is not able to sustain the level of fracture  
475 energy necessary to break into the creeping patch. In these cases, rupture halts far more  
476 quickly when it reaches the creeping zone than it does in the cases with a creeping patch  
477 surrounded by a locked fault.  
478

## 479 5 Conclusions

481 We find that the presence of a creeping patch within a locked fault, and vice versa, can  
482 have a controlling effect on the ability of rupture to propagate through the entire fault. In  
483 particular, the down-dip width between the bottom of the creeping zone and the base of the  
484 fault is the controlling factor. If the locked zone at depth is too narrow, then the overall energy

485 budget of the rupture decreases, and more of the remaining energy is spent on fracture as  
486 opposed to propagation and radiation, which can lead to arrest of the rupture front. In the case  
487 of a locked patch within a creeping fault, this reduction and re-balancing of the energy budget  
488 is almost instantaneous when rupture reaches the edge of the locked patch, which results in  
489 near immediate cessation of rupture propagation. We also find that some coseismic slip  
490 through a creeping zone is possible in cases where the rupture front is not forced to narrow  
491 much around the creeping zone, though the amount of slip is less than in locked areas, and the  
492 associated slip rate is slower (except in the small area where inward-propagating rupture fronts  
493 meet, as shown in figures 3, 4, and 5).

494 Although our models are extremely simple when compared to a real-world fault, and  
495 although they do not account for the difference in interseismic stress and strain accumulation  
496 on a creeping zone as opposed to a locked one (which would further reduce the ability of  
497 rupture to propagate into the creeping zones, e.g. *Lozos and Funning* [submitted to this issue]),  
498 they still provide indications as to possible rupture extents. In a case where the locked patches  
499 are surrounded entirely by creep, dynamic rupture is likely to be confined to those locked  
500 patches, which means an end-to-end dynamic rupture of the entire fault is unlikely, and that  
501 observed surface displacement is more likely to be postseismic than coseismic. Our case-  
502 specific simulations of Hayward Fault ruptures show these same behaviors even within a more  
503 complex model setup [*Lozos and Funning*, submitted to this issue]. However, if the creeping  
504 patches of a given fault are small and surrounded by locked zones, they may be able to sustain  
505 coseismic slip, and possibly even produce a pulse of seismic radiation. Our models highlight the  
506 importance of knowing the geometry of the creeping and locked parts of a partially-creeping  
507 fault in assessing potential rupture lengths and amounts of coseismic surface displacement. We  
508 emphasize that any dynamic rupture models on specific real-world partially-creeping faults  
509 should incorporate this complexity with as much detail as possible.

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#### 521 **Acknowledgments, Samples, and Data**

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526 We did not directly use any external datasets, nor did we collect or generate new data in this  
527 modeling study.

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