

1 **Intercomparison of the Performance of Four Data Assimilation Schemes in a Limited-Area**
2 **Model on Forecasts of an Extreme Rainfall Event over the Himalayas**

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27 **Highlights**

- 28 • The performance of four data assimilation systems are compared for a heavy rainfall event
- 29 • Non-cycled nested 4DVAR experiments outperformed the other experiments for rainfall
30 forecasts
- 31 • Early merging of weather systems produced enhanced precipitation in EnKF experiments

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Abstract

27 This study compares the performance of four data assimilation (DA) systems: Ensemble
28 Adjustment Kalman Filter (EAKF), Variational (3DVAR/4DVAR), and Hybrid ensemble-
29 3DVAR (HYBRID) in the Weather Research and Forecast (WRF) model. A heavy rainfall event
30 that produced notorious floods in the Uttarakhand over the Himalayan region is considered.
31 Observations are assimilated at every 6 h interval and all the conventional observations including
32 cloud tracked-wind from the satellite are used. The forecast initialized from the analysis of four
33 DA systems at different lead times is evaluated. A non-cycled nested assimilation strategy that
34 provides advantages of increased resolution in the DA system is tested. The results indicate that
35 4DVAR experiments produce more skillful forecasts for wind while both 4DVAR and EAKF
36 experiments show improvement for upper tropospheric temperature forecasts as compared to the
37 other experiments. The evaluation of rainfall forecast depicts that the 4DVAR DA system has
38 outperformed the other DA systems when the effect of high-resolution assimilation is mimicked
39 in the system using the nested assimilation strategy. Further analysis of the event indicates that
40 an early merging of the southward protruding trough with the westward-moving monsoon
41 depression has resulted in stronger southeastward flow in EAKF and HYBRID experiments,
42 which is suggested as a potential reason for enhanced precipitation over the Uttarakhand in both
43 the experiments.

44 **Keywords: Data Assimilation, Heavy Rainfall Event, WRF**

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48 **1. Introduction**

49 Data Assimilation (DA) methods are employed to improve the accuracy of initial conditions
50 in a numerical weather prediction (NWP) model. Operational NWP models use variational
51 (e.g, Parrish and Derber 1992, Kleist et al. 2009; Lorenc et al. 2000) and ensemble-based
52 (e.g, Houtekamer and Mitchell 2005) DA algorithms to initialize the model forecasts. Three
53 dimensional variational (3DVAR) approach estimates the minimum variance through
54 iterative minimization of the cost function (Barker et al. 2004), while four-dimensional
55 variational (4DVAR) scheme adds a time dimension in the variational framework through a
56 linearized model and its adjoint (e.g., Rabier et al. 2000). One of the crucial factors that can
57 influence the performance of a DA system is the prescription of background error covariance
58 (BEC) matrix. The 3DVAR uses a time-invariant, climatological BEC, while the 4DVAR
59 incorporates the time evolving flow-dependent information in the DA system, implicitly. On
60 the other hand, the ensemble Kalman filter (EnKF) DA system follows probabilistic
61 approach for assimilating observations with the model forecast that uses anisotropic,
62 inhomogeneous flow-dependent BEC (Evensen 1994; Houtekamer and Mitchell 2001). The
63 BEC in an EnKF DA system is estimated from the ensemble of nonlinear model forecasts,
64 which carries the information about the “errors of the day”. The strategy of incorporating the
65 ensemble estimated flow-dependent BEC in the variational framework is popularly known as
66 Hybrid ensemble – variational DA system (“HYBRID”) (e.g; Hamill and Snyder 2000;
67 Wang et al. 2008; Campbell et al. 2010). Compared to standalone ensemble-based DA
68 system, HYBRID is computationally less expensive as it improves the state of the system
69 with relatively smaller ensemble size. The effectiveness of HYBRID in improving the NWP

70 forecasts are well documented (e.g., Buehner 2005; Kleist and Ide 2015; Kutty and Wang
71 2015; Kutty et al. 2018; Gogoi et al. 2020).

72 Previous studies have performed systematic intercomparison of the performance of DA
73 systems in various NWP models. For instance, Whitaker et al. (2008) has shown that the
74 analysis and forecast from EnKF are superior to that of 3DVAR in the operational global
75 models of National Center for Environmental Prediction (NCEP) and Environmental Canada
76 (Houtekamer and Mitchell 2005). Buehner et al. (2010) and Miyoshi et al. (2010) have
77 shown that the performance of EnKF is comparable to that of 4DVAR in the operational
78 models of Canadian and Japan Meteorological Agency (JMA). Wang et al. (2013) compared
79 the performance of 3DVAR, EnKF and HYBRID DA system in the NCEP GFS and found
80 that HYBRID produced more skillful forecast than EnKF and 3DVAR DA system. Zhang et
81 al. (2011) has found similar results in the limited area regional models when the compared
82 the performance of 3DVAR, 4DVAR and EnKF DA systems. Schwartz et al. (2013)
83 suggested that the precipitation forecast initialized from HYBRID is better than from the
84 standalone EnKF and 3DVAR. Chu et al. (2013) found that the performance of 4DVAR
85 experiments is comparable to that of high-resolution 3DVAR experiments, which indicates
86 that high resolution model forecasts are as important as the DA system for the precipitation
87 forecasts. Despite the aforementioned studies, a comprehensive understanding of the
88 performance of DA systems in the heavy rainfall events that involves multiscale dynamical
89 interactions is elusive.

90 Extreme precipitation and flood episodes are quite frequent over Himalayan region and such
91 high impact weather events are observed and studied extensively (e.g., Priya et al. 2015;
92 Singh and Kumar 1997; Joshi and Kumar 2006; Joseph et al. 2015; Ranalkar et al. 2016;

93 Krishnamurti et al. 2017). Studies such as Rasmussen and Houze (2012) has shown that the
94 extreme precipitation episodes over the Western Himalayas are multiscale in nature. During
95 June 14 -17 of the year 2013, the Indian state, Uttarakhand experienced heavy rainfall and
96 disastrous flooding thereafter. The event caused thousands of fatalities and extensive
97 damages to the life and properties of the adjoining villages. In a study conducted by Vellore
98 et al. (2016), it is found that extreme precipitation events over the Western Himalayas are
99 often associated with southward penetrating large-scale westerly flow. Houze et al. (2017)
100 suggested that the storm event is multiscale in nature and the presence of southward extended
101 midlevel trough has provided a conducive environment for the development of the storm.
102 Studies performed on the Uttarakhand heavy rainfall event using National Center for
103 Medium Range Weather Forecasting (NCMRWF) Unified Model (NCUM) indicate
104 improved performance in precipitation forecast when 4DVAR DA system is employed (Dube
105 et al. 2014).

106 This study evaluates the performance of 3DVAR, 4DVAR, EAKF and HYBRID DA systems
107 in Weather Research and Forecast (WRF) model for the extreme rainfall event over the
108 Uttarakhand during 14 to 18 June 2013. Though the assimilation is performed on a coarser
109 resolution domain, a non-cycled nested assimilation strategy is adopted to provide
110 advantages of increased resolution in a computationally efficient manner (e.g., Cavallo et al.
111 2013; Torn 2010). This paper is organized as follows. Section 2 provides the experimental
112 design. Section 3 describes major results and Section 4 and 5 provide discussion and
113 conclusion of the paper, respectively.

114 **2. Experimental design**

115 The Advanced Weather Research and Forecast (ARW-WRF) of version 3.8.1 is used to
116 investigate the performance of the DA systems. The WRF is a non-hydrostatic, fully
117 compressible model with advanced parameterization schemes. This study employs Unified
118 Noah Land Surface Model for surface parameterization, Rapid Radiative Transfer Model for
119 longwave radiation calculation, Dudhia scheme for shortwave radiation calculation, WRF
120 single-moment five-class for microphysics scheme, and Yonsei State University (YSU)
121 scheme for planetary boundary layer parameterization. Simulations are performed in 27 km,
122 9 km, and 3 km resolution using two-way interactive nest with the assimilations performed
123 on the outer domain. There are 36 non-uniformly spaced vertical levels with the model top at
124 50 hPa. The initial and lateral boundary conditions are generated from National Center for
125 Environmental Prediction (NCEP) Global Forecast System (GFS) data available at $0.5^{\circ} \times 0.5^{\circ}$
126 resolution. Observations available from the Global Telecommunication System (GTS) are
127 assimilated in ± 3 h interval assuming that all the observations are valid at the analysis time.
128 The observations from various platforms are ingested including surface synoptic observation
129 (SYNOP), buoys (BUOY), ships (SHIP), Radiosonde (RAOB), aircraft routine weather
130 report (METAR), and wind reports from satellites (GEOAMV). Observation errors are
131 obtained from the NCEP statistics and are assumed to be uncorrelated.

132 The 3DVAR, 4DVAR and HYBRID DA systems available in the WRF Data Assimilation
133 system (WRFDA) are used in this study. The details regarding formulation and
134 implementation of 3DVAR and 4DVAR is described in Barker et al. (2004) and Huang et al.
135 (2009), respectively. The HYBRID DA system in WRFDA software uses extended control
136 variable approach to incorporate ensemble covariance in 3DVAR cost function (Wang et al.
137 2008). Here, Ensemble Adjustment Kalman Filter (EAKF) from the Data Assimilation

138 Research Testbed (DART; Anderson 2001) is used to update the background ensembles in
139 HYBRID DA system and also for the standalone EnKF DA system. Covariance localization
140 and inflation is applied to maintain sufficient ensemble spread and avoid spurious
141 correlations in the EAKF DA system. Gaspari and Cohn (1999) localization function has
142 been used to control the effect of observations with half-widths of approximately 950 km in
143 EAKF system. Initial inflation of 1.02 is applied to inflate the deviations from the ensemble
144 mean using the adaptive inflation scheme (Anderson 2009) with a standard deviation of 0.6
145 and damping of 0.9.

146 The initial set of ensemble members are generated by adding randomly sampled
147 perturbations to the initial conditions on 12 UTC 14 June 2013. The perturbations are the
148 random draws from the distribution of the default background error covariance (“cv3”
149 option) available in WRFDA system. The ensembles are then integrated forward in time for
150 12 hours to achieve model balance. The ensemble mean obtained at 00 UTC 15 June 2013 is
151 used as the first guess for all the DA systems. Assimilation is then performed from 00 UTC
152 15 to 00 UTC 16 June 2013 every 6 h interval before the initializing the 48 h free forecast
153 from the analysis at 00 UTC 16 June 2013.

154 *2.1 Non-cycled nested assimilation*

155 As indicated in the previous section, four sets of non-cycled nested assimilation experiments
156 (Torn 2010) are performed for all the DA systems used in this study *viz.* 3DVAR-N, EAKF-
157 N, HYBRID-N, and 4DVAR-N to provide advantages of increased resolution in a
158 computationally efficient manner. The DA cycling is performed at 27 km horizontal grid
159 spacing, which is too coarser to resolve the convective aspects of precipitation patterns of the

160 event. To overcome this limitation, a non-cycled nested assimilation strategy is designed as
161 follows. After completing the first analysis cycle at 27 km resolution, it is integrated forward
162 in time to the next assimilation step using a two-interactive nested domain at 27 km, 9km,
163 and 3 km horizontal grid spacing. It is to be noted that the innermost 3 km domain is centered
164 on the Uttarakhand region. Once the forecast step is completed all the higher resolution runs
165 are discarded and the assimilation is performed on the coarser resolution parent domain.
166 Since the nesting strategy is two-way interactive, the outer domain will get benefitted from
167 the high resolution innermost domain.

168 **3. Results**

169 *3.1 Domain-wide comparison*

170 The analyses from 3DVAR, 4DVAR, HYBRID and EAKF experiments are validated using
171 root mean square (RMS) fit with respect to Radiosonde observations. The results from this
172 section need to be treated with caution since assimilated observations are used for the
173 verification of the analyses. Therefore, the RMS fit of analysis to observations are not
174 depicting the analysis error, rather it shows how much each DA method draws its analysis
175 closer to the observations. Figure 1 represents domain averaged vertical profiles of RMS fit
176 of analysis to radiosonde observations for the mass and the wind variables for 3DVAR,
177 EAKF, HYBRID and 4DVAR experiments. The analysis from EAKF fits more closely to the
178 wind observations than 3DVAR, 4DVAR and HYBRID analyses. Compared to 3DVAR and
179 4DVAR, the analysis from HYBRID depicts a better fit to the wind observations. However,
180 the analysis from the 3DVAR DA system depict a better fit to the temperature observations
181 while for mixing ratio the EAKF analysis shows closer association to the observations. The

182 prescription of background and observational error covariance plays an important role in
183 determining the fit of analysis to observation. Since the specification of the observational
184 error and the background are the same, the differences in RMS fit are due to differences in
185 the background error covariance. Wang et al. (2013) has shown that the analysis fits better to
186 the observations when the correlations scales (background error variances) are smaller
187 (larger), and therefore, RMS fit may not reflect on the accuracy of forecasts generated from
188 the analysis.

189 The root mean square error (RMSE) of horizontal wind components, temperature, and mixing
190 ratio forecasts are validated with respect to radiosonde observations. The domain-averaged
191 vertical profiles of RMSE at 24 h forecast lead time is shown in Figure 2. For wind, 4DVAR
192 experiments produce more skillful forecasts as compared to the other experiments. The
193 4DVAR and EAKF experiments show improvements in the upper tropospheric temperature
194 forecasts, and EAKF shows larger error near 800 hPa as compared to other experiments.
195 Figure 3 illustrates the domain averaged RMSE for the four DA experiments at 48 h forecast
196 lead time. Apparently, 4DVAR shows larger improvement in the meridional wind above
197 about 500 hPa and below 300 hPa. Unlike the results from 24 h forecast lead time, EAKF
198 experiment depicts larger error near the tropopause as compared to the other experiments, for
199 zonal wind. As far as mixing ratio is concerned, EAKF and HYBRID experiments produce
200 more skillful forecasts than 3DVAR and 4DVAR experiments over lower troposphere.

201 *3.2 Rainfall*

202 The geographical distribution of 24 h accumulated precipitation from TRMM satellite for day
203 1 and day 2 valid at 00 UTC June 17, 2013 and 00 UTC June 18, 2013, respectively, is shown
204 in Figure 4. The TRMM satellite observation indicates that the rainfall is mostly over the

205 Uttarakhand state and the eastern parts of Himachal Pradesh for the first day while the
206 precipitation bands are found to be shifted southeastward on the second day. Figure 5 shows
207 24 h accumulated precipitation for day 1 and day 2 simulated by 3DVAR, EAKF, HYBRID,
208 and 4DVAR experiments. The EAKF and HYBRID experiments indicate that the rainfall is
209 widely distributed over the Uttarakhand, and the northern regions of Himachal Pradesh. More
210 specifically, two prominent precipitation maxima can be seen in EAKF experiment for day 1;
211 one over the Uttarakhand and another one over the Himachal Pradesh (Figure 5c). The
212 4DVAR experiment simulated precipitation bands with a lower intensity and the precipitation
213 maxima are located much south of the Uttarakhand state. For day 2, all the experiments
214 except 4DVAR depict a southeastward shift of precipitation patterns as observed in TRMM
215 satellite observations. Additionally, EAKF and HYBRID experiments overestimate the
216 precipitation intensity, while 4DVAR run shows weak rainfall patterns as compared to the
217 other experiments.

218 Figure 6 indicates that the position and intensity errors have reduced in all the experiments
219 that adopted the non-cycled nested assimilation strategy, in general, and the largest
220 improvement in day 2 precipitation forecast is observed for 4DVAR experiments (Figure 6f).
221 It is worth noting that for non-cycled nested assimilation experiments, the intensity errors
222 have considerably reduced in EAKF and HYBRID experiment as compared to the
223 experiments without nesting. In the non-cycled nested assimilation, the spatial extent of
224 precipitation in EAKF is larger than other experiments, and HYBRID run shows enhanced
225 precipitation to the north of Uttarakhand.

226 To evaluate the precipitation forecasts quantitatively, verification statistics based on
227 contingency table such as Equitable Threat Score (ETS), and Bias scores are employed. The

228 ETS value of 1 indicates perfect rainfall forecast by the experiments. The Bias score indicates
229 the tendency of model to underpredict (when Bias score is less than 1) or overpredict an event
230 (when Bias score is greater than 1). Figure 7 illustrates that among all the DA cycling
231 experiments, 4DVAR-N shows the highest skill score for precipitation forecast for all the
232 rainfall thresholds for both day 1 and day 2. For non-cycled nested assimilation experiments,
233 rainfall forecast skill for day 1 has improved substantially in HYBRID-N experiment as
234 compared to its corresponding non-nested assimilation experiment. The EAKF experiments
235 have overestimated day1 and day 2 rainfall forecasts, however with a reduced intensity
236 estimation error for day 1 precipitation in EAKF-N experiment. Barring that, using the non-
237 cycled nested assimilation strategy is found to be not very effective in EAKF experiments. On
238 the other hand, 3DVAR-N experiment shows higher skill scores at lower thresholds as
239 compared to 3DVAR. Overall, the results indicate that convection-permitting resolution is
240 inevitable for the accurate precipitation forecast and the 4DVAR DA system has
241 outperformed other DA systems when the effect of high-resolution assimilation is mimicked
242 in the system using the nested assimilation strategy.

243 **4. Discussion**

244 The primary synoptic scale factor that is associated with the devastating rainfall over the
245 Uttarakhand during June 2013 is the southward extending midlevel trough that eventually
246 merged with westward migrating monsoon low. The accuracy in the precipitation placement
247 and intensity forecast depends on the accuracy in the depiction of synoptic-scale flow pattern
248 in the DA analysis and forecast. Figure 8 shows the geopotential heights at 850 hPa in the
249 analysis valid at 00 UTC of 16 June 2013 of 3DVAR, EAKF, HYBRID, and 4DVAR, which
250 indicates that position of the trough simulated in each experiments are distinctly different.

251 This could be the potential reason for the observed variations in the position and intensity of
252 precipitation forecast over the Uttarakhand. To understand how the variations in the analysis
253 reflected in the forecast, the evolution of geopotential height at 850 hPa level in the forecasts
254 initialized from each of the analysis is shown in Figure 9. While EAKF and HYBRID
255 experiments depicted an early merging of southward protruding trough with the westward
256 moving monsoon depression, the forecast from 4DVAR analysis indicates that the merging
257 weather system occurred by June 17. The merging of weather systems and northward shift in
258 the position of trough created a strong southwesterly flow over the Uttarakhand by 16 June
259 2013 in the EAKF experiment, which is proposed as the reason for enhanced precipitation in
260 EAKF run during the first 24 h model forecast (Figure 5c). The enhanced magnitude and
261 northward shift in the position of trough in EAKF experiment during the later hours of
262 forecast can be attributed as the reason for stronger precipitation band. Figure 10 shows the
263 vertical cross-section plot of specific humidity overlaid with the wind vectors during 18 UTC
264 of 16 June 2013. Vertical extension of moisture column is more pronounced in EAKF and
265 3DVAR run as compared to 4DVAR experiment. Furthermore, EAKF indicates stronger
266 vertical updraft along Himalayan escarpment as compared to other experiments, which could
267 be due to the proximity of the trough over the Uttarakhand region.

268 **5. Conclusion**

270 The performance of four DA systems viz. 3DVAR, EAKF, HYBRID, and 4DVAR in
271 Weather Research and Forecast (WRF) model during a heavy rainfall event over the
272 Himalayas is compared. The accuracy of forecast initialized from the four DA systems at
273 different lead times is examined. A non-cycled nested assimilation strategy that provides

274 advantages of increased resolution in a computationally efficient manner in a DA system is
275 tested.

276 Results indicate that the analysis from EAKF fits more closely to the wind observations than
277 3DVAR, 4DVAR and HYBRID analyses. Compared to 3DVAR and 4DVAR, the analysis
278 from HYBRID depicts a better fit to the wind observations. For 24 h wind forecasts, the
279 4DVAR experiments are found to be more skillful as compared to the other experiments
280 while for upper tropospheric temperature forecasts, both 4DVAR and EAKF experiments
281 outperforms other experiments. For 48 h forecasts, 4DVAR shows larger improvements in
282 the meridional wind and unlike the results from 24 h forecast lead time, EAKF experiment
283 depicts larger error near the tropopause as compared to the other experiments. The forecasts
284 initialized from EAKF and HYBRID DA systems produce more skillful forecasts for mixing
285 ratio than that from 3DVAR and 4DVAR over lower troposphere. The EAKF experiments
286 overestimates rainfall intensity, while the 4DVAR experiments underestimates the
287 precipitation in both forecast days. The spatial patterns of precipitation and quantitative skill
288 scores indicate that the non-cycled nested assimilation strategy has significantly improved
289 the forecast skill scores, especially for 4DVAR experiments. Further analysis indicates that
290 an early merging of southward protruding trough with the westward moving monsoon
291 depression has resulted in stronger southeastward flow in EAKF and HYBRID experiments,
292 which is suggested as a potential reason for enhanced precipitation over the Uttarakhand in
293 both the experiments.

294 The present study is an initial effort to broaden our understanding on the performance of data
295 assimilation system during an extreme rainfall event that occurred over Himalayas. The data
296 assimilation cycling is performed in relatively coarser resolution. The skill of data

297 assimilations systems will improve significantly, when high-resolution background and
298 observations such as that from radar are used. More systematic comparisons during such
299 weather events are required for understanding the fundamental differences that are significant
300 for the performance of data assimilation systems. Future studies in this direction are
301 warranted.

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305 Data assimilation is performed using observations derived from NCEP ADP Global Upper Air
306 and Surface Weather Observations archived in the <https://rda.ucar.edu> at
307 <https://doi.org/10.5065/Z83F-N512>.

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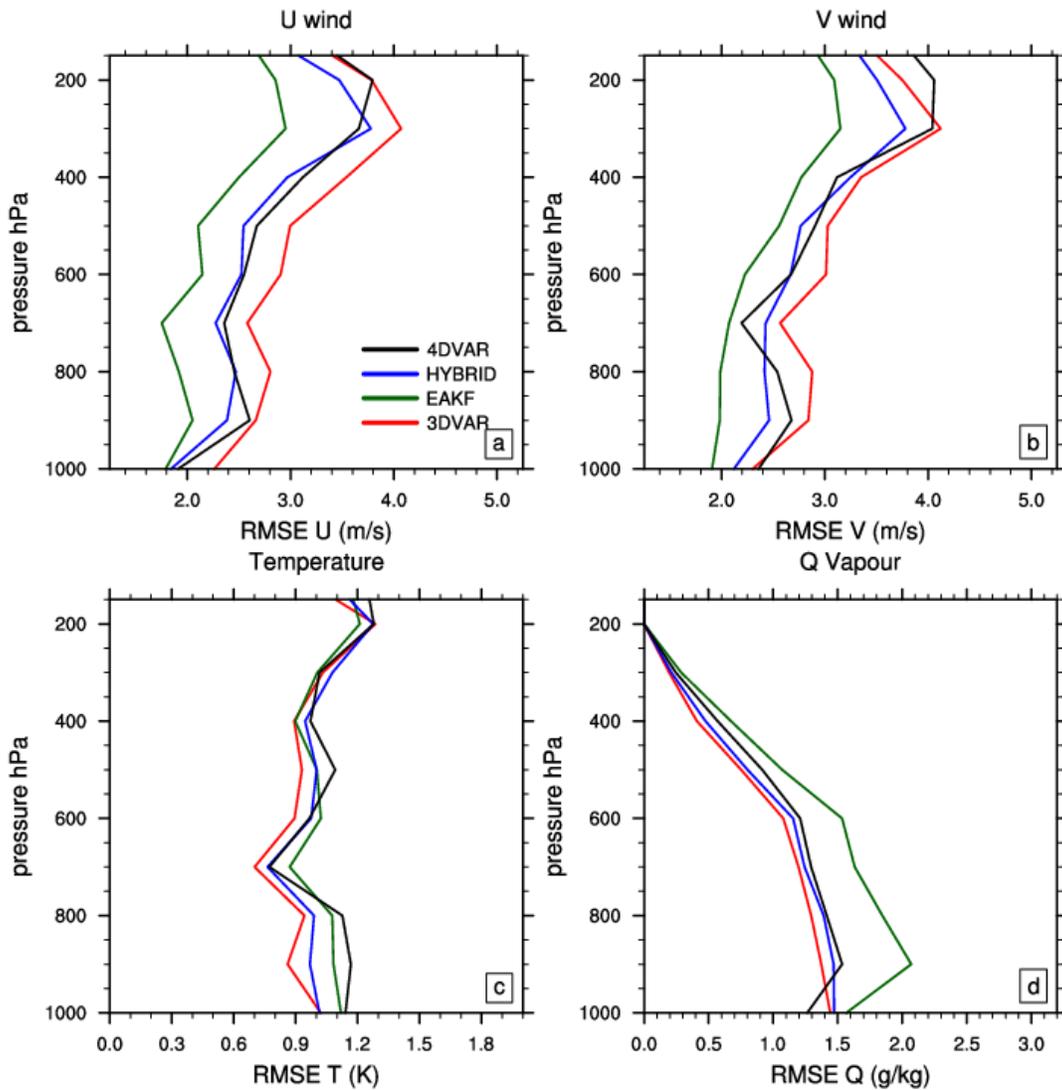
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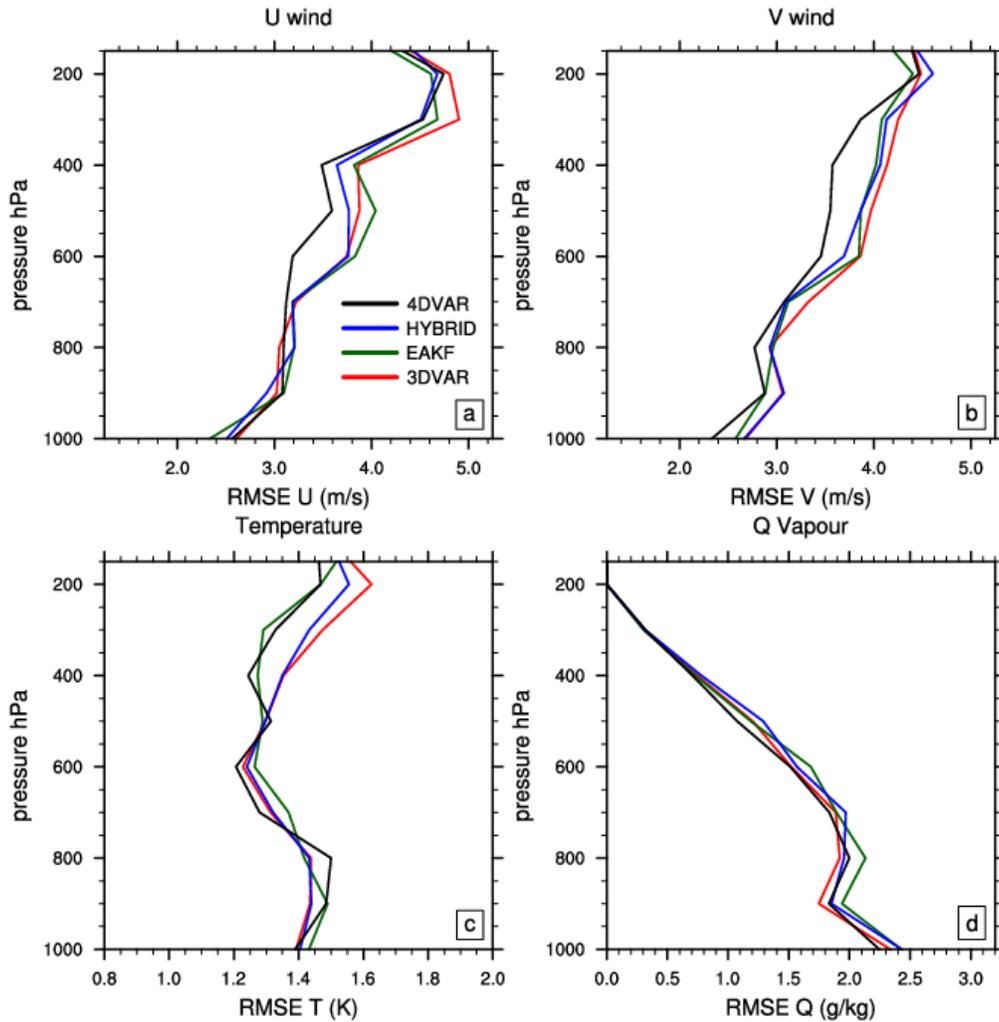
416 **Figures:**



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418 **Figure 1:** Domain averaged profiles of Root Mean Square (RMS) fit of analysis to Radiosonde
419 observations for (a) Zonal wind (b) Meridional wind (c) Temperature, (d) Mixing ratio. Red,
420 green, blue and black are for 3DVAR, EAKF, HYBRID, and 4DVAR experiments, respectively

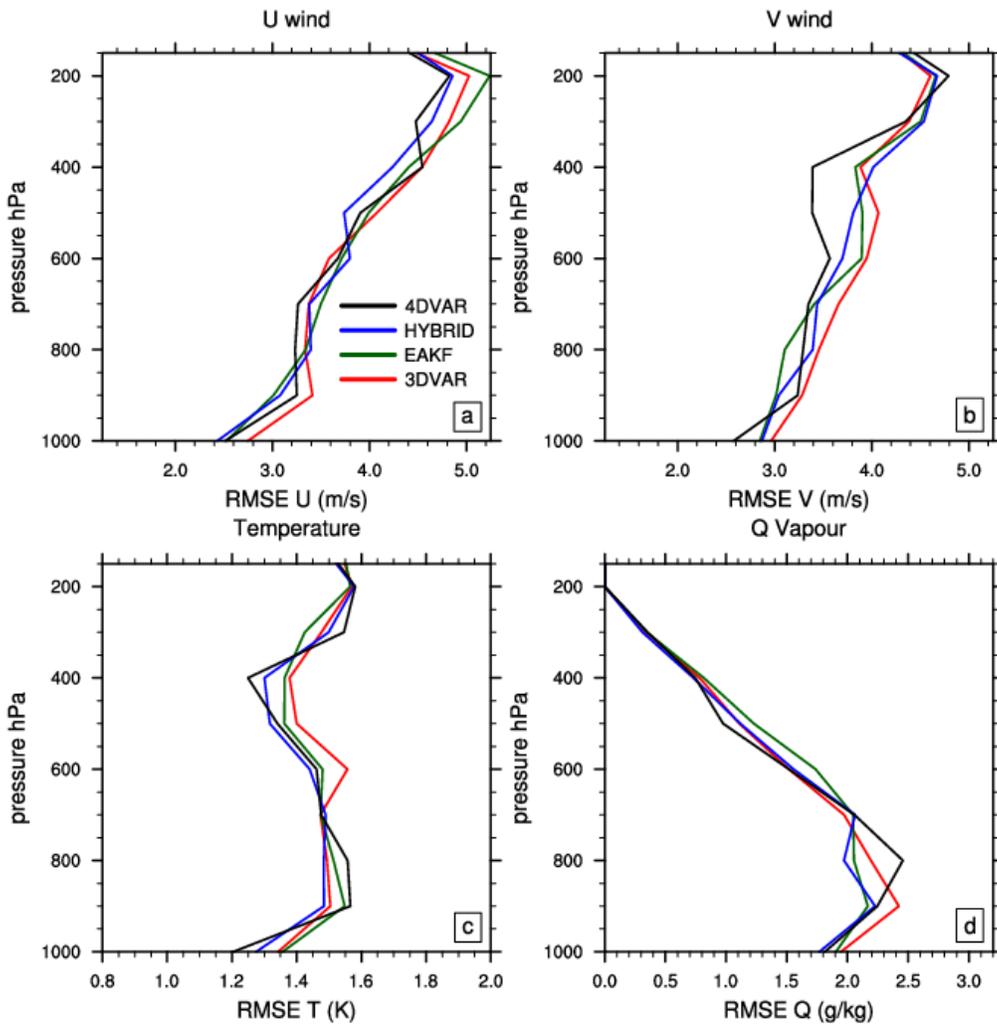
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424 **Figure 2:** Vertical profiles of RMSE with respect to Radiosonde observations for 24 h forecasts
 425 for (a) Zonal wind (b) Meridional wind (c) Temperature, (d) Mixing ratio. Red, green, blue and
 426 black are for 3DVAR, EAKF, HYBRID, and 4DVAR experiments, respectively



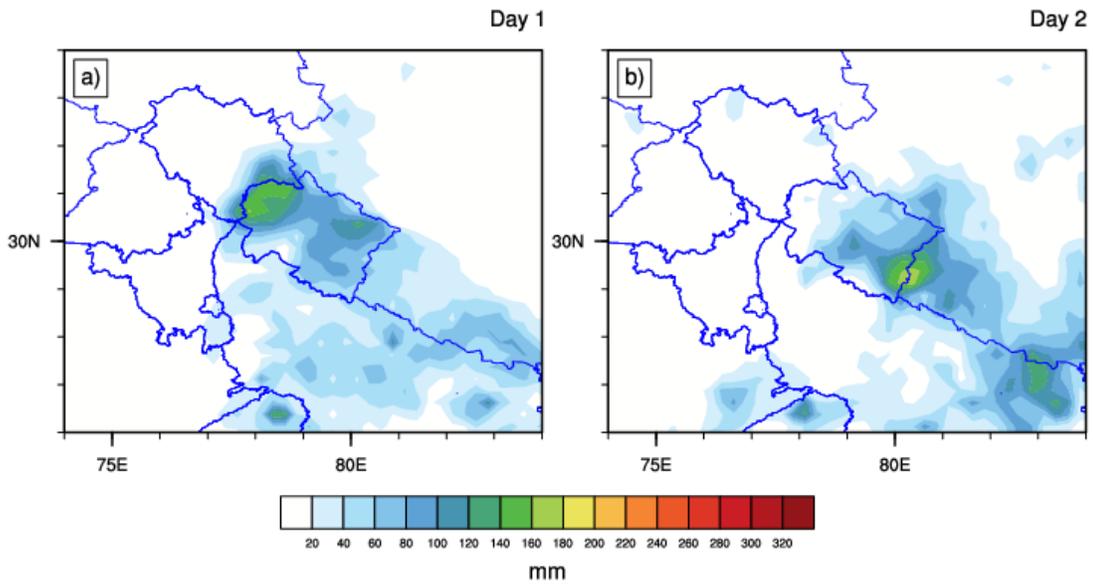
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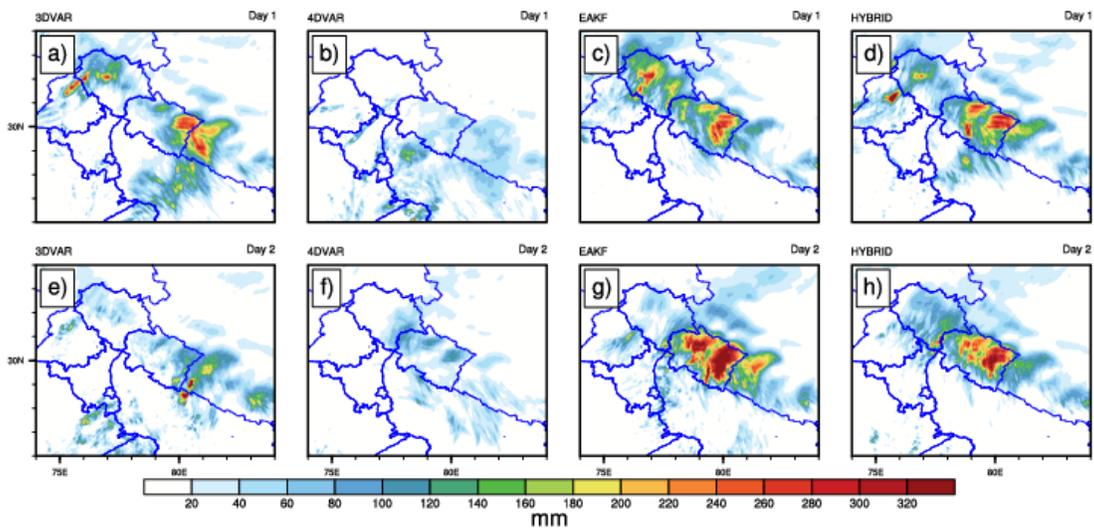
Figure 3: Same as in Figure 2, but for 48 h forecast



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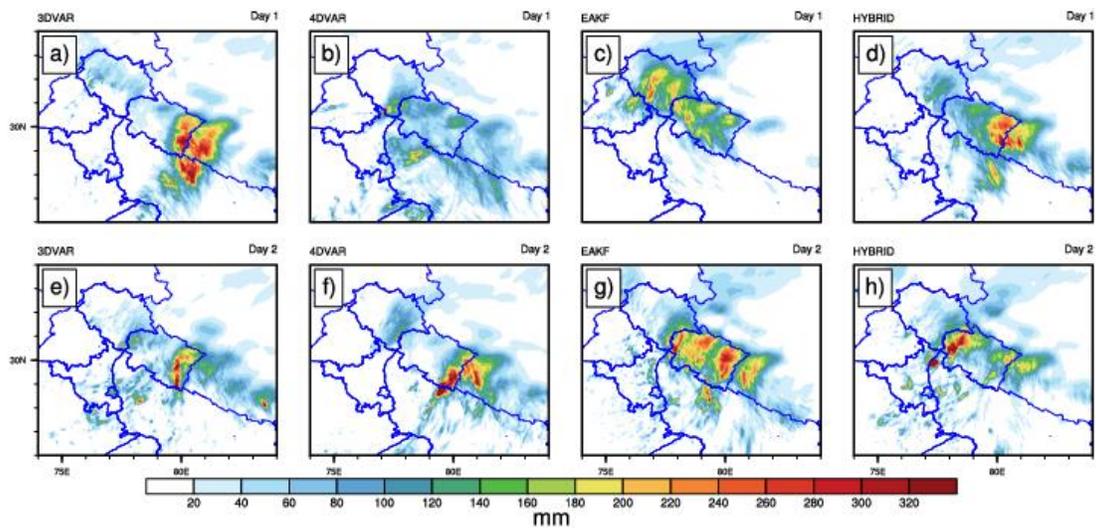
432 **Figure 4:** Geographical distribution of 24 h accumulated precipitation from TRMM satellite
 433 observations valid at (a) 00 UTC June 17, 2013 and (b) 00 UTC June 18, 2013.

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436 **Figure 5:** Geographical distribution of 24 h accumulated precipitation valid at (top panel: a-d) 00
 437 UTC June 17, 2013 and (bottom panel: e-h) 00 UTC June 18, 2013, respectively, for (a,e)
 438 3DVAR (b,f) 4DVAR (c,g) EAKF (d,h) HYBRID experiments.



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440 **Figure 6:** Same as in Figure 5, but for non-cycled nested assimilation experiments

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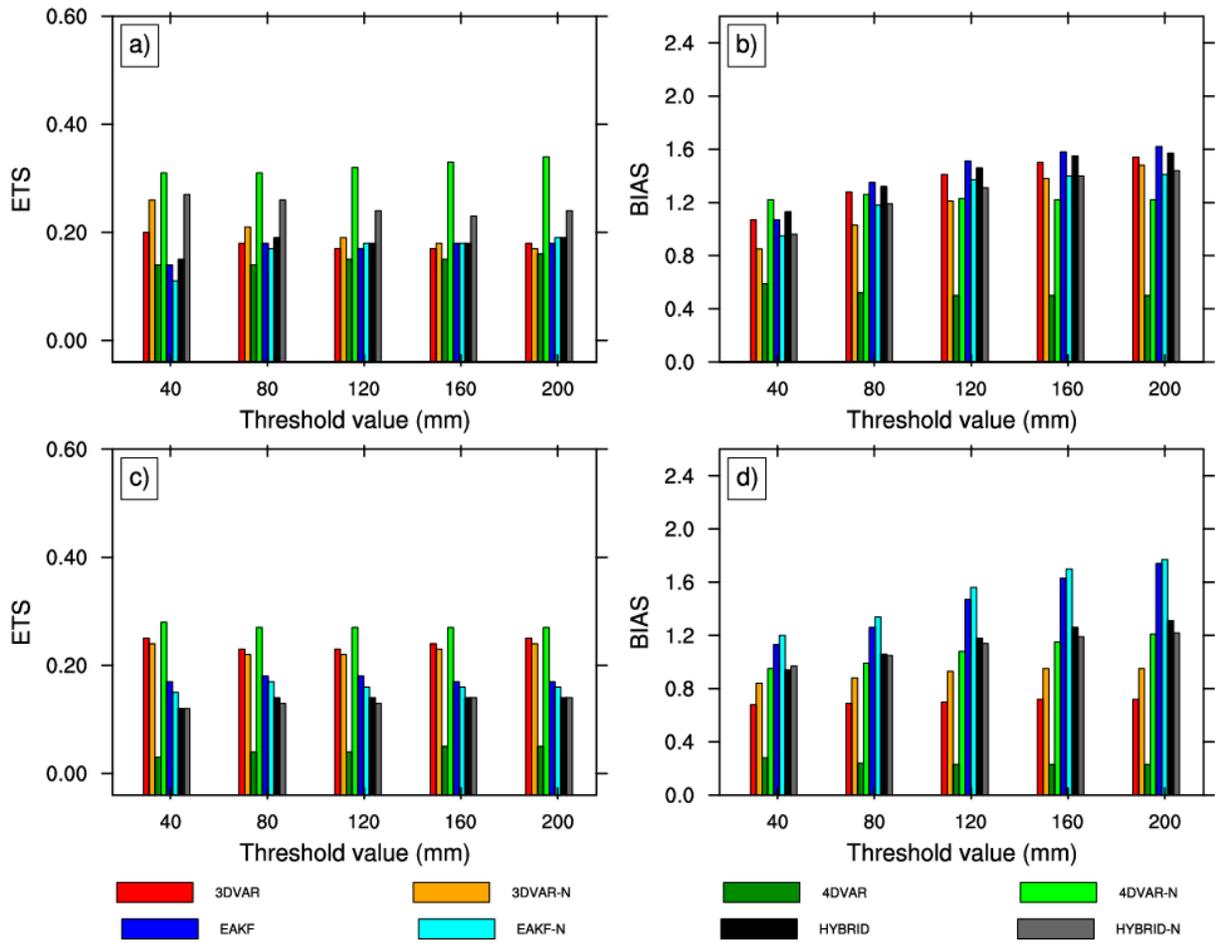
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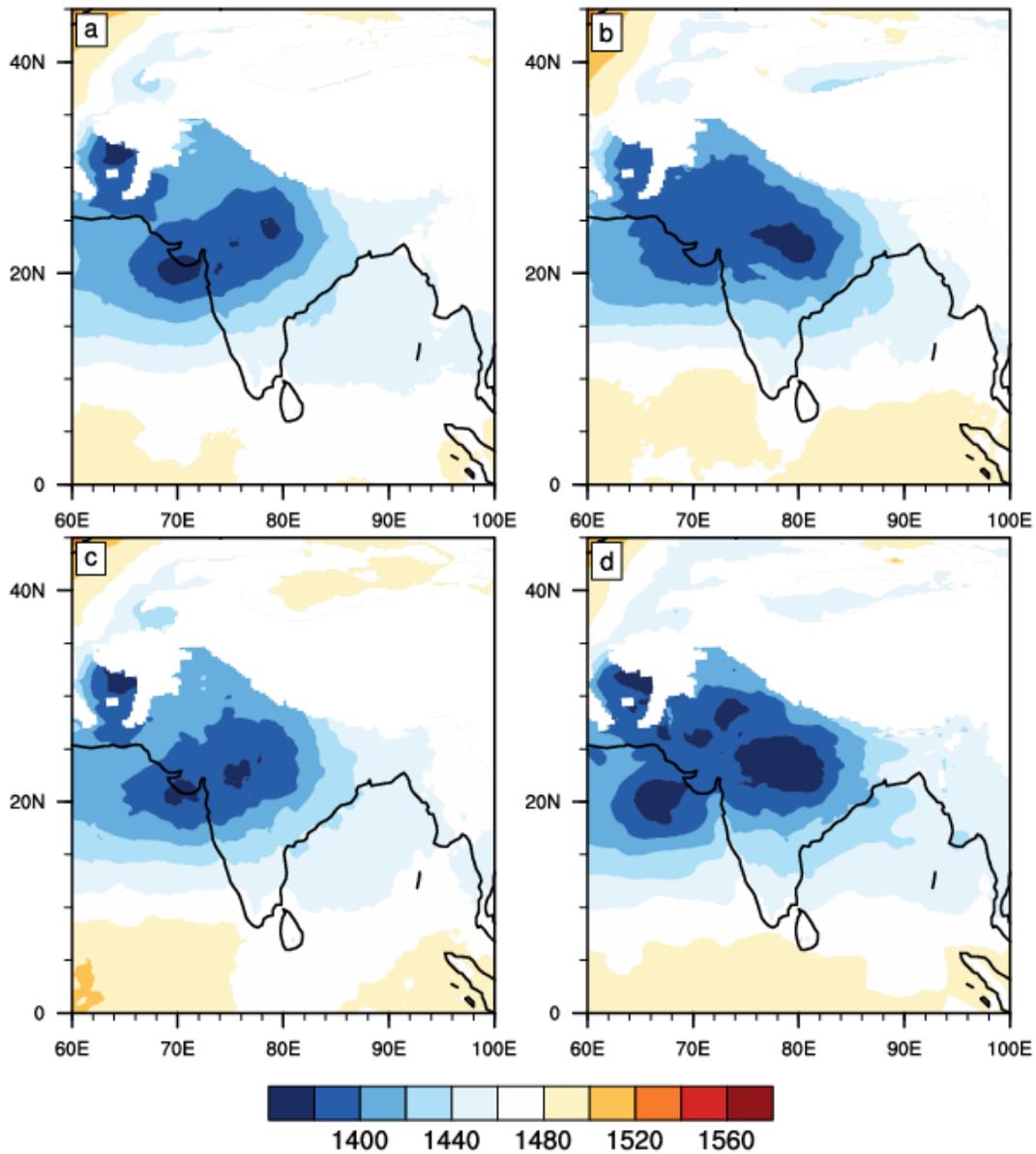
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448 **Figure 7:** The ETS and Bias Scores for rainfall forecasts valid at (top panel: a, b) 00 UTC June
 449 17, 2013 and (bottom panel: c, d) 00 UTC June 18, 2013. Red, green, blue, black, orange, light
 450 green, cyan, and grey are for 3DVAR, 4DVAR, EAKF, HYBRID, 3DVAR-N, 4DVAR-N,
 451 EAKF-N, HYBRID-N experiments, respectively

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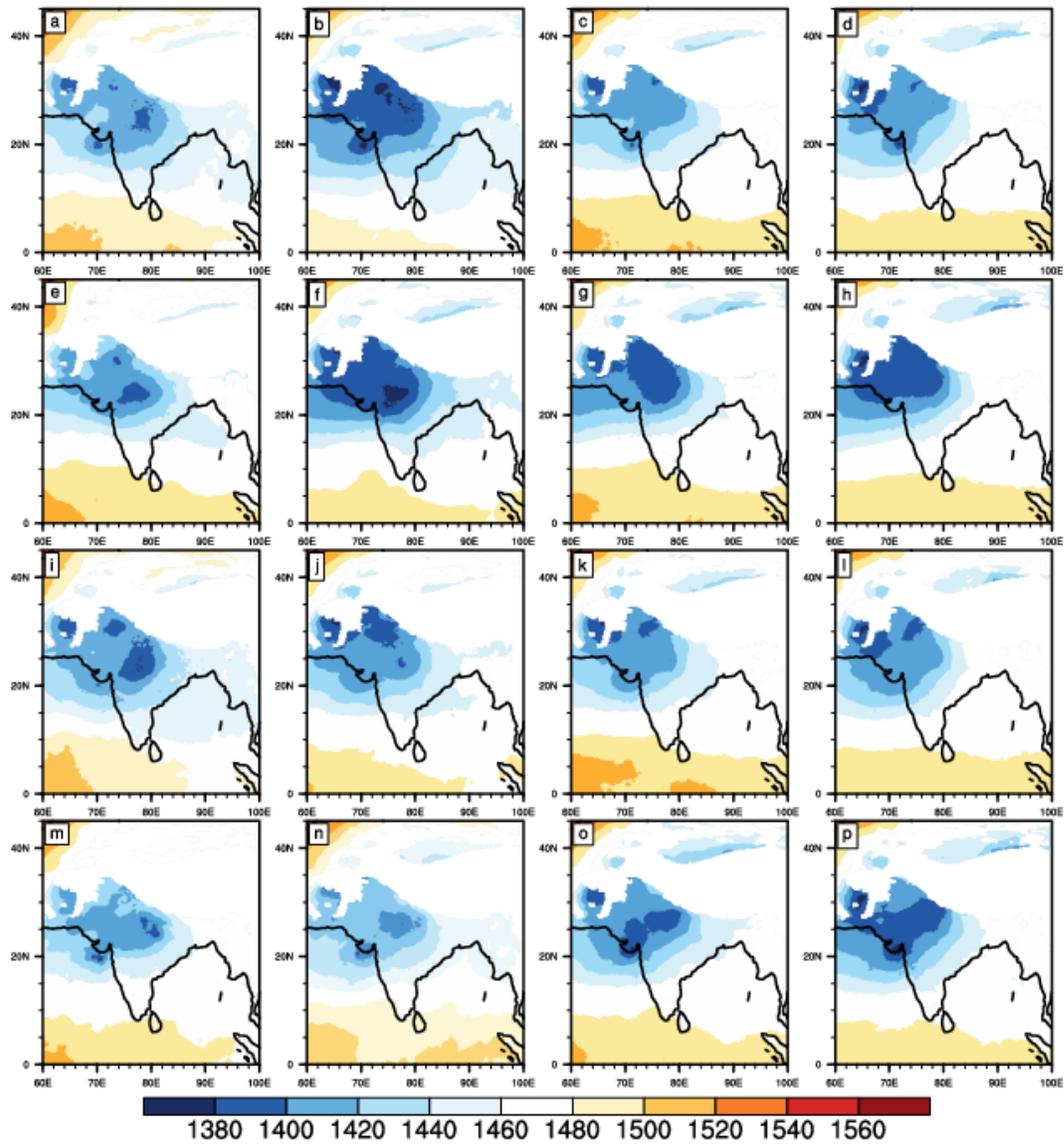


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455 **Figure 8:** Spatial distribution of geopotential height at 850 hPa from the analysis of (a) 3DVAR
 456 (b) EAKF (c) HYBRID (d) 4DVAR valid at 00 UTC of 16 June 2013

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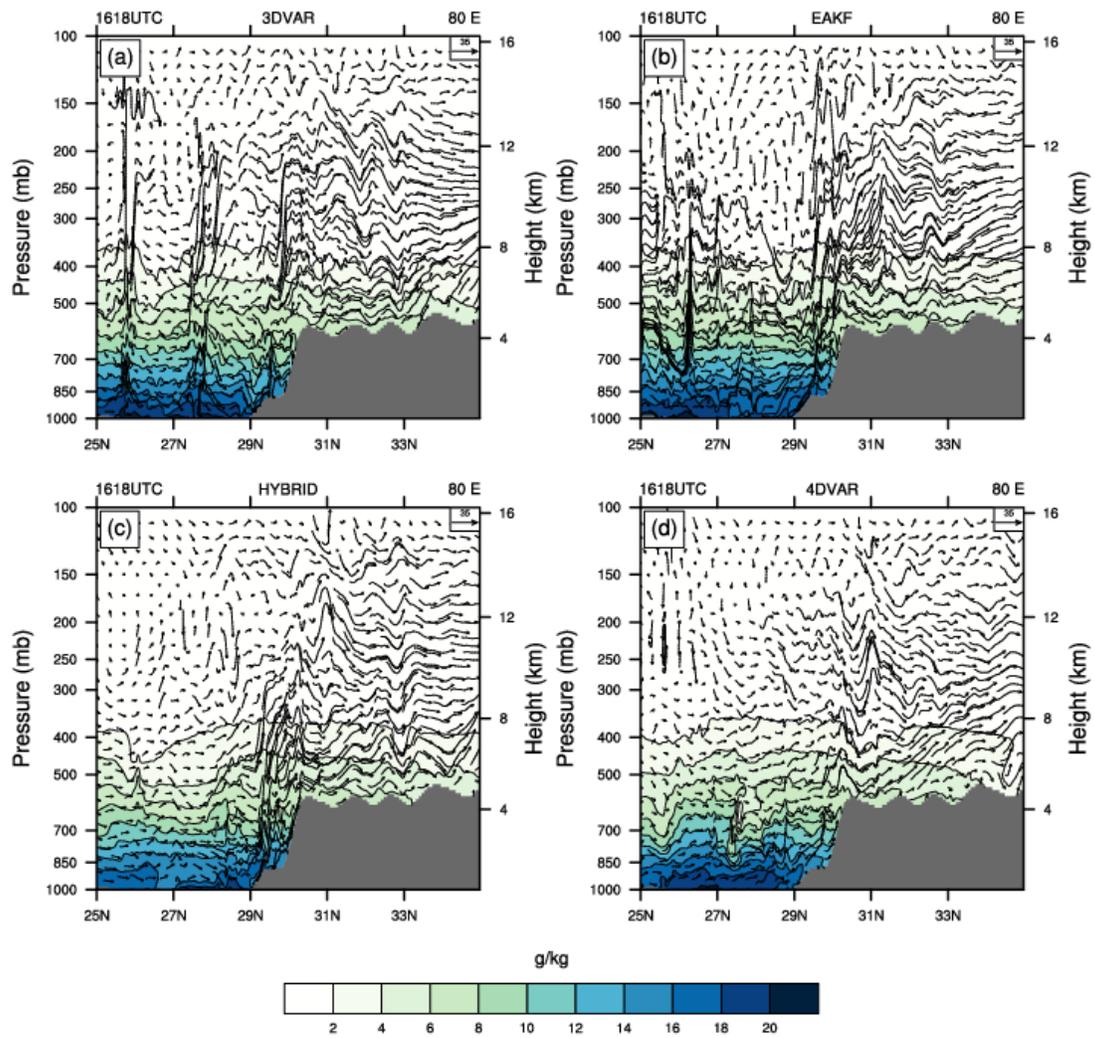
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460 **Figure 9:** Time evolution of geopotential height at 850 hPa forecasts for (first row: a-d) 3DVAR
 461 (second row: e-h) EAKF (third row: i-l) HYBRID (fourth row: m-p) 4DVAR experiments at 0 h,
 462 6h, 12h, and 18 h forecast.

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467 **Figure 10:** Vertical cross section of mixing ratio (shaded) overlaid with the wind vectors for (a)
 468 3DVAR (b) EAKF (c) HYBRID (d) 4DVAR experiments valid at 18 UTC of 16 June 2013.

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