A New Method to Invert for Interseismic Deep Slip Along Closely Spaced Faults using Surface Velocities and Subsurface Stressing-Rate Tensors

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Key Points:

- Joint inversions of velocity and stressing-rate data can better estimate slip rates along complex faults than individual inversions.

- Inverting data at multiple depths can better estimate fault locking depth than inverting data at a single depth.

- Application of the new method requires estimates of crustal deviatoric stressing-rate tensors with magnitude.

Abstract

Inversions of interseismic geodetic surface velocities often cannot uniquely resolve the three-dimensional slip-rate distribution along closely spaced faults. Microseismic focal mechanisms reveal stress information at depth and may provide additional constraints for inversions that estimate slip rates. Here, we present a new inverse approach that utilizes both surface velocities and subsurface stressing-rate tensors to constrain interseismic slip rates and activity of closely spaced faults. We assess the ability of the inverse approach to recover slip rate distributions from stressing-rate tensors and surface velocities generated by two forward models: 1) a single strike-slip fault model and 2) a complex southern San Andreas fault system (SAFS) model. The single fault model inversions reveal that a sparse array of regularly spaced stressing-rate tensors can recover the forward model slip distribution better than surface velocity inversions alone. Because focal mechanism inversions currently provide normalized deviatoric stress tensors, we perform inversions for slip rate using full, deviatoric or normalized deviatoric forward-model-generated stressing-rate tensors to assess the impact of removing stress magnitude from the constraining data. All the inversions, except for those that use normalized deviatoric stressing-rate tensors, recover the forward model slip-rate distribution well, even for the SAFS model. Jointly inverting stressing rate and velocity data best recovers the forward model slip-rate distribution and may improve estimates of interseismic deep slip rates in regions of complex faulting, such as the southern SAFS; however, successful inversions of crustal data will require methods to estimate stressing-rate magnitudes.

1 Introduction

During interseismic periods, elastic strain accumulation around isolated locked faults produces a broad zone of geodetically measurable velocity gradients that may be more than 30 km wide for faults with locking depths greater than 10 km (e.g., Savage and Burford, 1973). In regions with multiple closely spaced (i.e., < 30 km) and branching faults that have locking depths greater than 10 km, such as the southern San Andreas fault system (SAFS) through the San Gorgonio Pass region (Figure 1), the geodetic velocity signatures of individual faults can overlap one another (e.g., McGill et al., 2015). As a result, inversions of geodetic velocity data alone often cannot uniquely resolve the slip rate distribution on these closely spaced faults (e.g., Spinler et al., 2010). Inversions of geodetic data for slip rates continue to improve with the

49 increasing availability of geodetic surface velocity estimates (e.g., d'Alessio et al., 2005; Evans

50 et al., 2012; Guns et al., 2021; Wang et al., 2021). However, jointly inverting geodetic data with

51 an independent dataset, such as stress information, could provide more robust slip rate

52 distribution estimates. Previous studies have inverted stress orientations inferred from surface

53 cracks for coseismic slip (John P. Loveless et al., 2016) and regional stress orientations to

54 estimate long-term slip rates (e.g., Becker et al., 2005). Stress states derived from focal

55 mechanisms of microseismicity during the period between large ground rupturing earthquakes,

56 which have not yet been used within inversions, may reflect local stress conditions and provide

57 valuable information about deep interseismic slip rates on closely spaced faults because, unlike

58 surface velocities, the microseismicity occurs at depth, closer to the deep portions of faults that

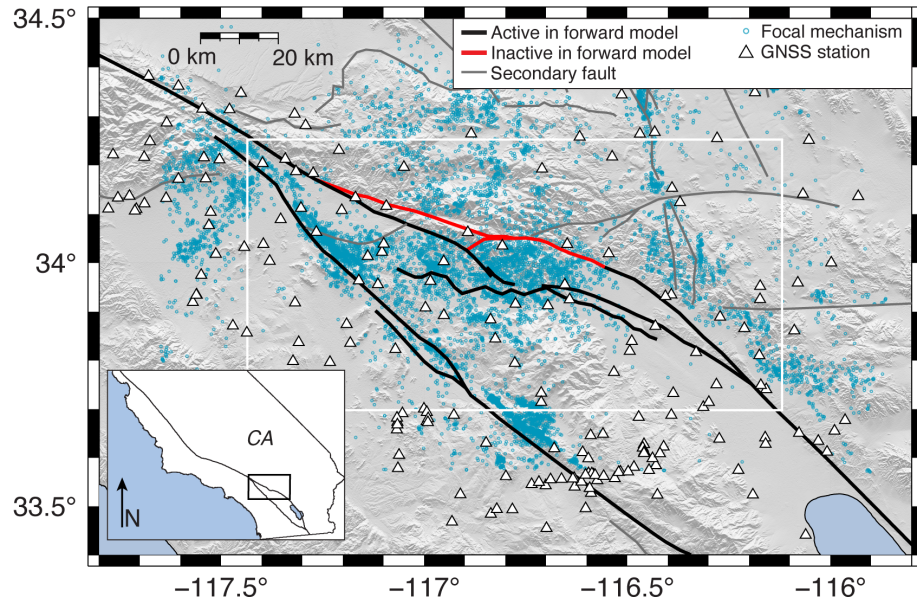59 slip during interseismic periods.

Figure 1. Map of the San Gorgonio Pass region with the modeled fault surface traces for the region of interest. Black fault traces indicate active faults in all complex forward models. Red traces indicate faults that are inactive in all forward models. Gray traces indicate the secondary faults that are active in the long-term forward models only. Blue open circles show microseismicity from the declustered catalog. White triangles show GNSS stations that we use. White box shows the area we use to calculate the inverse model misfits.

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61   Here, we present and assess a new inverse approach that utilizes both surface velocities

62 and subsurface stressing-rate tensors to estimate three-dimensional fault slip-rate distributions

63 (Figure 2). We perform joint and individual inversions of forward model-generated surface

64 velocities and stressing-rate tensors to assess the potential of using stressing-rate tensors to infer

interseismic slip rates (Figure 2). Using a simple fault model consisting of a single, planar strike-slip fault (Figure 3A), we determine the spacing of stressing-rate tensors that minimizes the inverse model misfit to the forward model applied slip rate distribution. To assess how well individual and joint inversions of surface velocities and subsurface stressing-rate tensors recover slip along closely spaced and branching faults, we utilize a complex, geologically constrained fault model that simulates the southern SAFS and San Jacinto fault system (SJFS) through the San Gorgonio Pass region (Figure 3B). The SAFS consists of two subparallel pathways for earthquake rupture through the San Gorgonio Pass region, but the relative activity of the two pathways remains a topic of debate (e.g., Kendrick et al., 2015; Blisniuk et al., 2021). Because these two pathways are less than one locking depth apart from one another, inversions of GNSS velocities alone may not uniquely recover slip-rate distributions along the pathways and at the fault branches. For the complex fault inversion, we intentionally include fault surfaces that are inactive in the forward models to assess how well the inversions can recover zero slip along inactive fault surfaces. The method we present here provides a new approach that may constrain the relative activity of closely spaced parallel faults, such as the two pathways for earthquake rupture through the San Gorgonio Pass.
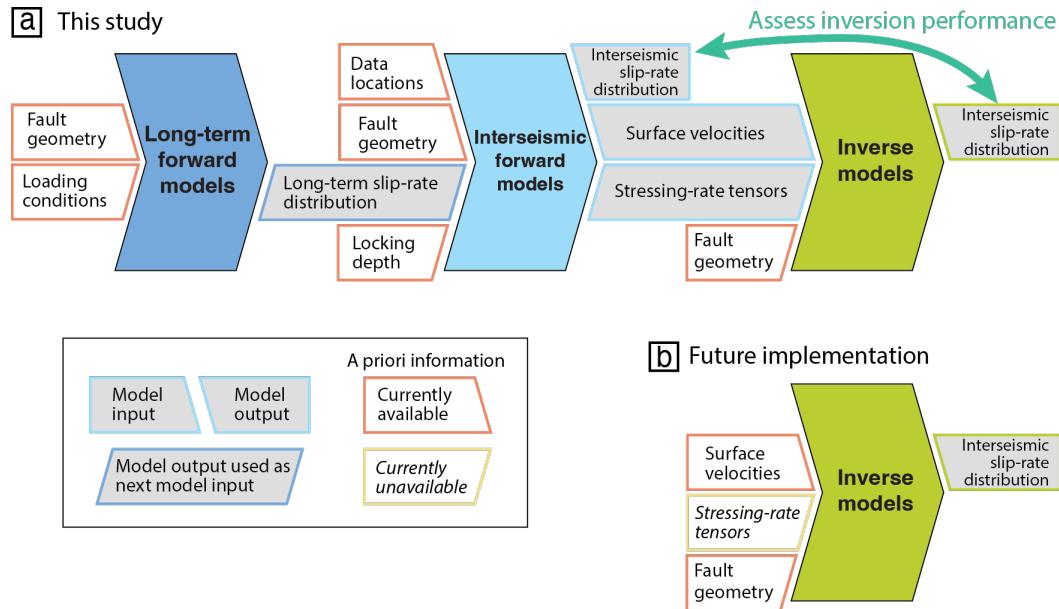

Figure 2. Flow chart showing the a) the methods we use to assess the new inverse method and b) the steps for a future application of the inverse method. Polygons on the left of a model are inputs. Polygons on the right of a model are outputs. Parallelograms indicate a model output is used as an input in the next model.

82 **2 Methods**

83   2.1 Crustal data processing

84   We utilize focal mechanism-derived stress states and GNSS estimated velocities in

85 southern California for multiple purposes. Previous studies show that long-term forward

86 mechanical models of the SAFS produce slip rates that fit geologic slip rate estimates well (e.g.,

87 Cooke and Dair, 2011; Devine et al., 2022; Hatch et al., 2023), and that the interseismic forward

88 model-generated surface velocities agree well with GNSS velocities (e.g., Herbert et al., 2014).

89 Previous studies have not compared stress states generated by a complex SAFS model to focal

90 mechanism-derived stress states. Here, we compare the horizontal maximum compression

91 orientations from interseismic forward models to focal mechanism-derived orientations to further

92 validate a complex SAFS model. Additionally, we use the locations of microseismicity and

93 GNSS stations to assess how deviations from the optimal spacing of data impact the inversions.

94 We also use the data uncertainties to weight the constraining data within the inversions. As the

95 purpose of this study is to test the new approach and stressing-rate tensors are not currently

96 available from crustal data, we do not directly invert the actual GNSS estimated velocities or the

97 focal mechanism-derived stress data, but instead use model-generated data.

98   2.1.1 GNSS surface velocity locations

99   We generate surface velocities within the complex SAFS forward models at the locations

100 of 201 permanent GNSS station locations (Figure 1) in the Southern California Earthquake

101 Center's Community Geodetic Model version 1 (Sandwell et al., 2016). We only use the

102 horizontal velocities to constrain the inverse models because this is what would be typically used

103 in GNSS inversions (e.g., Zeng, 2023).

104   2.1.2 Focal mechanism-derived stress states

105   Prior to deriving stress information from focal mechanisms of microseismicity, we assess

106 the completeness of and decluster the focal mechanism catalog to reduce effects of local events

107 (details provided in the Supporting Information; Martínez-Garzón et al., 2016; Abolfathian et al.,

108 2019). We start with 41,110 focal mechanisms from the Southern California Earthquake Data

109 Center from 1981 to 2020 (Hauksson et al., 2012; Yang et al., 2012) that have a nodal plane

110 uncertainty of < 45°. Removing focal mechanisms with magnitudes below the limit of

111   completeness reduces bias of small events that occur close to seismic stations but are not

112   represented across the entire region of interest. Following Cooke and Beyer (2018), we calculate

113   the completeness magnitude using the maximum curvature method (Wiemer & Wyss, 2000) and

114   identify three periods with completeness magnitudes that decrease as the density of seismic

115   stations increases. For 1981-2001 the completeness magnitude is 2.0, which decreases to 1.6 for

116   2002-2011 and to 1.1 for 2012-2020.

117   To decluster the focal mechanism catalog, we follow the nearest-neighbor approach

118   described by Zaliapin and Ben Zion (2013a, 2013b) and define a nearest-neighbor distance

119   threshold in the space-time-magnitude domain by assessing the distribution of the nearest-

120   neighbor distance for all the events. We exclude events that have a nearest-neighbor distance

121   smaller than the threshold because they may reflect short-term perturbations in the stress field

122   resulting from large events rather than background seismicity. The declustered catalog consists

123   of 10,758 events that have an average fault plane uncertainty of $27 \pm 9°$. The consistent average

124   slip sense over the 40-year catalog and the consistent rate of seismicity over each completeness

125   magnitude period (Supporting Information) confirms that the declustered catalog represents

126   background seismicity and does not include temporal stress state variations.

127   The MSATSI code, which is based on the SATSI algorithm (Hardebeck & Michael,

128   2006), performs formal stress inversions to derive normalized deviatoric stress tensors from

129   groups of focal mechanisms (Martínez-Garzón et al., 2014). Because the declustered catalog of

130   focal mechanisms generally has fault plane uncertainties $< 40°$, each group of focal mechanisms

131   must include a minimum of 40 events to robustly estimate the stress tensor (Martínez-Garzón et

132   al., 2016). The 40-year catalog along the southern SAFS and San Jacinto Fault system (SJFS)

133   yields 54 clusters of focal mechanisms from which we derive stress states. From 1000 bootstrap

134   resamplings of the fault plane, we estimate $\pm 10°$ uncertainty of the orientation of the principal

135   stress axes and 25% uncertainty of the deviatoric stress tensor components. We compare the

136   horizontal maximum stress orientations for the 54 stress states to those of the forward model.

137   2.2 Forward models

138   We utilize the Boundary Element Method (BEM) code Poly3D (Thomas, 1993), which

139   solves the governing equations of continuum mechanics to calculate displacements and stresses

140   within the model to simulate faulting within the crust (e.g., Crouch and Starfield, 1990). The

141   forward models simulate both long-term and interseismic loading of 1) a simple, isolated and

142   vertical strike-slip fault and 2) the complex southern SAFS and SJFS in the San Gorgonio Pass

143   region within a homogeneous and linear-elastic half space (Figure 3). For the complex fault

144   forward models, we utilize the inactive northern slip pathway geometry from Hatch et al. (2023),

145   which is primarily based on the Southern California Earthquake Center's Community Fault

146   Model version 5.3 (Marshall et al., 2021) with some modifications that improve the model fit to

147   geologic slip rates and uplift (e.g., Herbert and Cooke, 2012; Fattaruso et al., 2014; Hatch et al.,

148   2023). We discretize the fault surfaces into triangular elements that can capture fault curvature

149   and branching. Within all forward models, we prescribe zero opening/closing along all faults.

150   Faults in the long-term forward models intersect a horizontal basal crack at 35 km depth that

151   simulates distributed deformation below the seismogenic zone (Supporting Information;
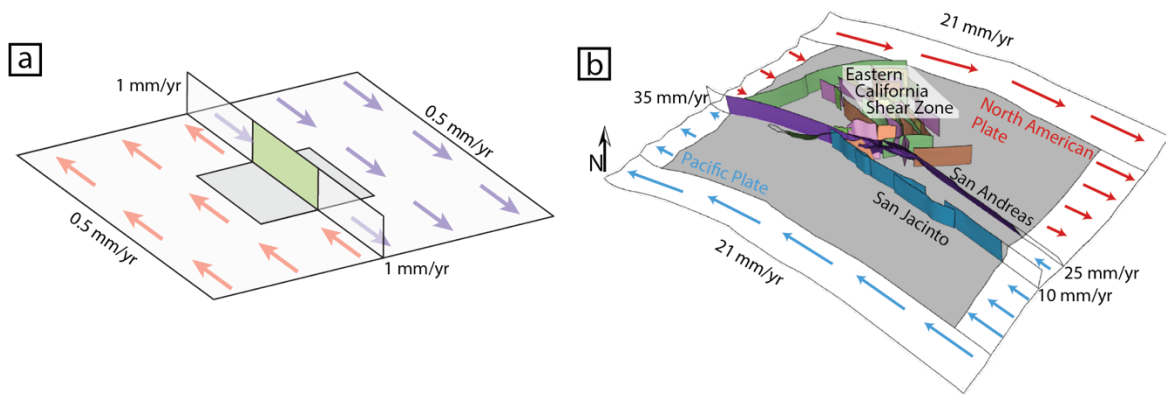
152   Marshall et al., 2009).

Figure 3. The long-term forward model geometries of the a) simple and b) complex fault models. a) The green surface indicates the area we use to calculate the inverse model misfit and show in Figure 4 and 5b-h. Rates adjacent to extended fault patches indicate the applied slip rates. Arrows on the far-field basal crack show applied loading. b) Modified from Beyer et al. 2018. Arrows indicate the applied tectonic velocities along the far-field basal crack.

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154   We simulate interseismic deformation in a two-step back-slip-like approach following

155   Marshall et al. (2009). In the first step, a suite of forward models simulates deformation over

156   several earthquake cycles. Shear-traction-free faults slip freely in response to loading along far-

157   field horizontal basal patches and slip along nearby faults. The zero shear traction condition

158   simulates low dynamic strength conditions, which is when most of the fault slip occurs (e.g., Di

159   Toro et al., 2006; Goldsby and Tullis, 2011). Following Beyer et al. (2018), we implement an

160   iterative technique to prescribe the desired loading velocity at the model edges (Figure 3). To

161   prevent fault slip rates from artificially going to zero at the lateral edges of the model, we apply

162   slip to driving patches for all faults that extend past the bounds of both models. For the simple

163   fault model of an idealized strike-slip fault, we prescribe far-field loading along the basal crack

164   and apply slip to driving patches that produces a nearly uniform strike-slip rate of 1 mm/yr along

165   the vertical fault (Figure 3a). For the complex fault model, we prescribe slip along far-field basal

166   patches consistent with 42 mm/yr of far-field loading at an orientation of 322° following Herbert

167   and Cooke (2012)(Figure 3b). Following Beyer et al. (2018), we apply slip rates to driving

168   patches in the complex fault model based on published slip rate estimates for each fault segment

169   (e.g., Sharp, 1981; Weldon and Sieh, 1985; Fay and Humphreys, 2005; Meade and Hager, 2005;

170   McPhillips and Scharer, 2018)

171   In the second suite of forward models, we apply the long-term model slip rates below a

172   prescribed locking depth to simulate interseismic deformation. For the simple fault model, we

173   test the inverse approach with forward model locking depths of 10, 15, and 20 km. For the

174   complex fault model, we utilize a locking depth of 20 km based on the maximum depth of

175   seismicity across the San Gorgonio Pass region (e.g., Yule and Sieh, 2003). To reduce artifacts

176   that would result from an abrupt change in prescribed slip at the locking depth, we create a

177   transition zone by prescribing half of the long-term slip rate to elements that have centroids

178   within 2.5 km of the locking depth. This study tests if the new inverse approach can recover deep

179   interseismic slip rates along complex fault geometries that include closely spaced and branched

180   faults. For simplicity of this test, the complex interseismic model only applies deep slip from the

181   first suite of forward models along the primary faults in the region, the San Andreas and San

182   Jacinto faults. The interseismic models produce surface velocities and stressing-rate tensors at

183   regularly spaced points for both the simple and complex fault models. Within the complex fault

184   model, we additionally query surface velocities at specific GNSS station locations and stressing-

185   rate tensors at locations of recorded microseismicity. To compare the interseismic principal

186   stress orientations with those derived from crustal focal mechanisms, the model includes all of

187   the faults shown in Figure 1, not only the primary faults.

188   2.3 Inverse models

189   We use the MATLAB code TriInv (Loveless & Evans, 2020), which is based on

190   algorithms from Meade (2007), to calculate partial derivatives that relate the stressing rates or

191   surface velocities at specific locations to unit slip rate on each triangular dislocation element

192   within each model. Because MSATSI produces normalized deviatoric stress tensors, we set up

193   separate inversions for the forward model-generated full, deviatoric, and normalized deviatoric

194   stressing-rate tensors. For deviatoric and normalized deviatoric stressing-rate tensor inversions,

195   we remove the mean stress component of the partial derivative. Laplacian smoothing within the

196   inversions prevents abrupt steps in slip rates that would not be expected along crustal faults. We

197   test a range of smoothing weighting parameters to optimize the surface velocity, stressing rate,

198   and joint inverse model performance. The results of the smoothing parameter value testing are

199   independent of the surface velocity and stressing-rate tensor spacing. Within all inversions,

200   elements in direct contact with the free surface of the model (0 km depth) are locked and

201   opening/closing is prohibited. However, we do not constrain the locking depth or sense of slip on

202   any faults in the inverse models.

203   We assess the performance of individual and joint inversions that use forward model-

204   generated surface velocities and stressing-rate tensors. The simple fault model allows us to

205   determine the optimal stressing-rate tensor configuration and smoothing weight. Inversions of

206   regularly gridded surface velocities have 10 km spacing, which is based on the approximate

207   current permanent GNSS station density in the San Gorgonio Pass region (Figure 1). We test 60

208   stressing-rate tensor configurations that are based on the microseismicity in the San Gorgonio

209   Pass region, which generally occurs above 20 km depth. Because each stressing-rate tensor

210   represents a potential centroid of a group of microseismic focal mechanisms with a radius

211   between 2.5 and 7.5 km, we limit the stressing-rate tensor depths to between 15 and 7.5 km. All

212   the stressing-rate tensor configurations include either a single row of tensors at a single depth

213   (7.5, 10, 12.5, or 15 km) or two rows of tensors at two separate depths (7.5 and 15 km) on either

214   side of the simple fault. To reduce overlap of focal mechanisms within each group, we define a

215   10 km minimum along-strike spacing of stressing-rate tensors and only test two rows for

216   stressing-rate tensors at 7.5 and 15 km depths. To reduce the chance that a focal mechanism

217   group would include microseismicity on both sides of the same fault, all stressing-rate tensor

218   locations are at least 5 km away from the fault. We assess the same spacings for the simple

219   interseismic forward model with three different locking depths: 10, 15, or 20 km; this allows us

220   to assess the impact of locking depth on the stressing-rate tensor configuration that best recovers

221   the forward model slip rates.

222   We use the complex fault model to assess the performance of inversions on a

223   geometrically complicated fault system consisting of multiple closely spaced (< 12 km) and

224   interconnected faults. We invert the forward model-generated stressing-rate tensors and surface

225   velocities using a model with two slip pathways from Hatch et al. (2023) to assess how well the

226   inversions recover slip along the portion of the northern slip pathway that is inactive in the

227   forward models. The complex fault model inversions utilize regularly spaced surface velocities

228   and the configuration of stressing-rate tensors that optimizes the simple fault model inversion

229   performance as well as surface velocities at GNSS station locations and stressing-rate tensors at

230   locations of microseismicity groups. We prescribe an uncertainty of 0.3 mm/yr to all surface

231   velocity components, which is based on the lowest estimates of GNSS errors for stations that we

232   include (Sandwell et al., 2016). We query stressing-rate tensors at 100 locations following the

233   optimal distribution informed by the simple fault model. Inverse models utilize either all 100

234   tensors or only 54 tensors at locations with more than 39 nearby cataloged focal mechanisms,

235   which allows for a robust stress state estimate. We prescribe a conservative uncertainty of 25%

236   to all stressing-rate tensor components, at the high end of the estimated uncertainty. When

237   describing the inversions that use only the 54 stressing-rate tensors at locations with more than

238   39 nearby focal mechanisms and the surface velocities at locations of GNSS stations, we refer to

239   these inversions as using crustal limited locations or as crustal limited inversions.

240   To assess how well each inversion of forward model-generated stress rate and velocity

241   predictions recovers the prescribed fault slip rates, we calculate the misfit of the inverse model

242   slip rate distribution to the forward model applied slip rate. Because the root-mean-square error

243   can overestimate the model error by emphasizing outliers (Willmott et al., 2017), we define the

244   model performance based on the inverse model misfit to the forward model slip distribution with

245   the area-weighted average misfit per element using Equation 1, where j is the number of

246   elements, S_I is the inversion estimated slip rate for an element, S_F is the forward model slip rate

247   for an element, and A is the area for an element.

248    $\text{Misfit} = \dfrac{\sum_1^j |S_I - S_F| * A}{\sum_1^j A}$ (Equation 1)

3 Simple Fault Model Results

3.1 Determination of the optimal stressing-rate tensor spacing

An assessment of 60 different stressing-rate tensor configurations reveals the spatial configuration of stressing-rate tensors that best recover the forward-model slip rate distribution (Figure 4a-e). Figures 4 and 5 present results from inversions of stressing-rate tensors and surface velocities generated by a forward model with a 15 km locking depth, and the Supporting Information contains results from the models with 10 and 20 km locking depths. The forward-model prescribed locking depth does not significantly impact the optimal stressing-rate tensor spacing (Figure S2). Twenty-three of the 60 stressing-rate tensor spacings that we test produce misfits less than or equal to the surface velocity inversion misfit of 0.08 mm/yr. Increasing the tensor depth and distance from the fault generally improves the inverse model performance (Figure 4a-d). Inverting stressing-rate tensors at two separate depths rather than at a single depth improves model performance (Figure 4a-e). Inverting stressing-rate tensors at both 7.5 and 15 km depth at points that are 5 or 10 km away from the fault with along-strike spacing of 10 km best recover the forward model prescribed slip rate distribution (Figure 4a-e and Figure S2). As the along-strike spacing increases to 15 and 20 km, the inverse model performance generally decreases.
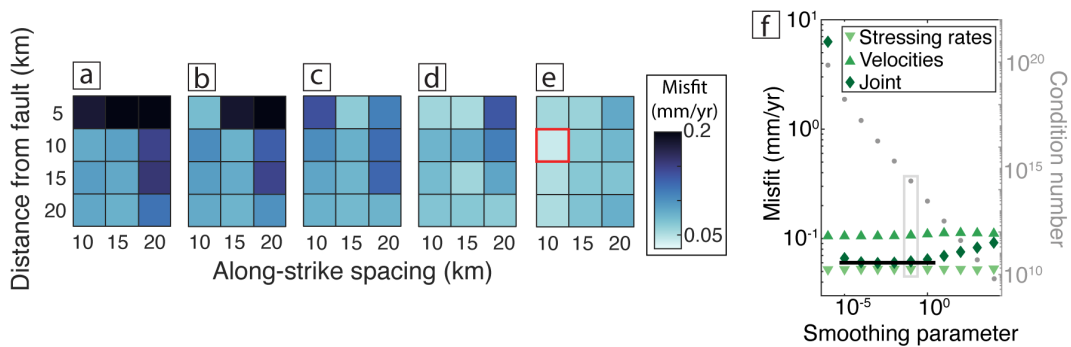

Figure 4. a-e) Each square represents one stressing-rate tensor spacing with the color indicating the average element misfit. We invert one row of stressing-rate tensors at a) 7.5, b) 10, c) 12.5, or d) 15 km depth or two rows of stressing-rate tensors at e) 7.5 and 15 km depths. The red box indicates the optimal spacing. f) Average element misfit (left y-axis) and joint inversion condition number (right y-axis) against smoothing parameter for inversions that use surface velocities with 10 km spacing and stressing-rate tensors with the optimal spacing (red box in e). The black line shows the minimum misfit for the joint inversion. The gray rectangle indicates the smoothing parameter value we use.

267   We present the smoothing parameter value assessment results from inversions that utilize

268 two rows of stressing-rate tensors at 7.5 and 15 km depths that are 10 km away from the fault

269 with 10 km along-strike spacing (Figure 4f). Varying the smoothing parameter impacts both the

270 inversion misfit and condition number. A lower condition number indicates the inversion has

271 greater numerical stability. Because using a smoothing parameter value of 0.1 produces misfits

272 within 2% of the minimum misfit and a condition number three orders of magnitude lower than

273 the inversions that produce minimum misfits (Figure 4f), we use this smoothing parameter value

274 for all the inversions.

275   3.2 Assessment of the inversion performance

276   We compare the area-weighted average element misfit for the portion of the fault

277 displayed in Figure 5a to determine which inverse model best recovers the forward model slip

278 rate distribution (Figure 5b). The inversions that use surface velocities and stressing-rate tensors

279 that include magnitude recover both the magnitude and pattern of forward model slip rates well

280 (Figure 5c-g). Even without prescribing a locking depth within the inversion, the inverse models

281 recover the forward-model locking depth well. The inversions estimate a broader locking depth

282 transition zone than is prescribed in the forward model, but the inversions recover slip rates

283 slower than 0.1 mm/yr for all elements above 10 km, which are locked in the forward model

284 (Figure 5). The inversion of the surface velocities produces a misfit of 0.08 mm/yr, which

285 exceeds that of the stressing-rate tensor inversion of 0.06 mm/yr. The joint inversion that utilizes

286 both full stressing-rate tensors and surface velocities outperforms both individual inversions

287 producing a misfit of 0.04 mm/yr.

288   The largest difference between the inverse models and the forward model applied slip

289 rates are along elements with at least one vertex at the locking depth of 15 km (Figure 5c-h). The

290 inversions overestimate slip on elements just above the locking depth transition zone and

291 underestimate slip on elements within and below the locking depth transition zone. This result

292 highlights the limit of this inverse approach to capture sharp changes in slip rate along faults due

293 to the applied Laplacian smoothing. Because we do not have evidence that locking depth

294 transition zones within the crust are as sharp as we prescribe in the forward models, this

295 smoothing across the locking depth does not cause concern. However, implementing a sparsity-

296 promoting regularization instead of Laplacian smoothing could better recover sharp changes in

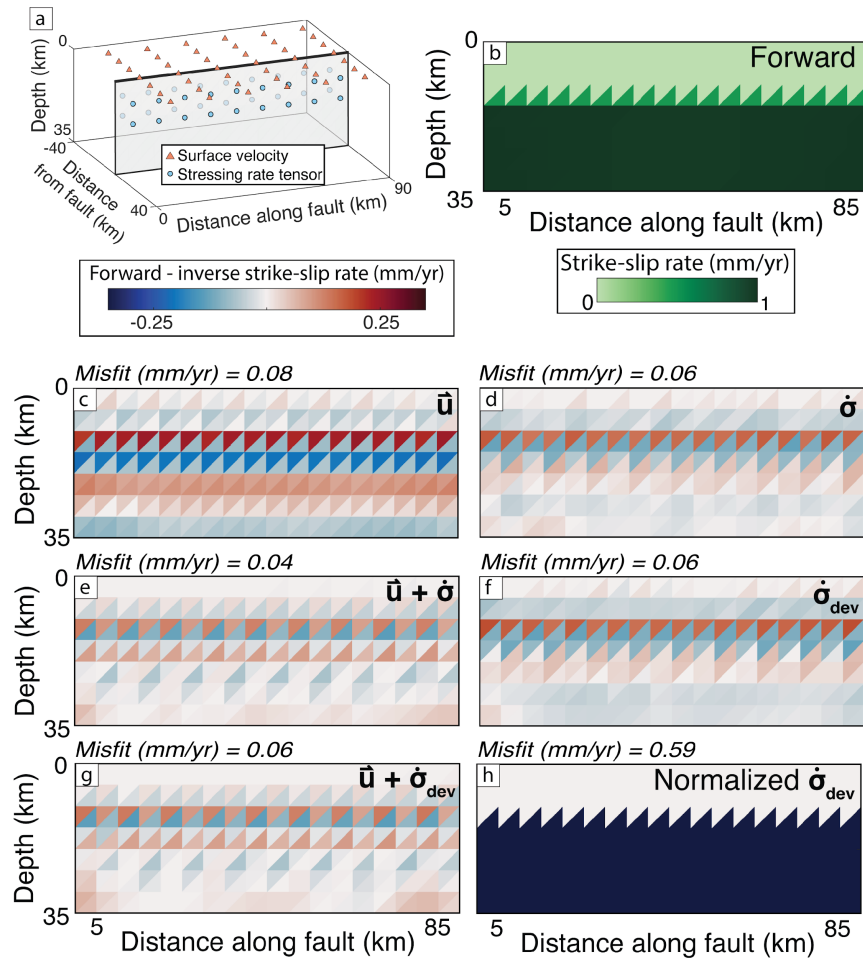297   slip rates (e.g., Evans and Meade, 2012).

Figure 5. a) The 3-D fault model geometry with the optimal stressing-rate tensor spacing and the grid of surface velocities. b-h show the strike-slip rate or strike-slip rate difference for the patch shown in a. b) The 15 km locking depth interseismic forward model applied strike-slip rates. c-h) The difference between the forward model applied strike-slip rates and the inversion estimated strike-slip rates. Blue indicates the inversion underestimates slip rates and red indicates the inversion overestimates slip rates.

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299   Because current methods of deriving stress information from focal mechanisms produce

300   normalized deviatoric stress tensors (e.g., Martínez-Garzón et al., 2014), we assess the

301   performance of inverse models that use either deviatoric or normalized deviatoric stressing-rate

302   tensors. These inversions reveal the impact of removing the mean normal stress component and

303   stress magnitude from the inverse model constraint. Removing the mean normal stress from the

304   full stressing-rate tensor does not significantly impact the inverse model performance. The

305   deviatoric stressing-rate tensor inversion produces a misfit equal to that of the full stressing-rate

306   tensor inversion (0.06 mm/yr). Because the normalized deviatoric stressing-rate tensors lack

307   magnitude, the inversion is poorly posed to recover slip rates with magnitude. As we expect,

308   removing the stressing-rate tensor magnitude leads to the inverse model estimating near zero slip

309   rates along the entire fault. Consequently, the inversion recovers the locked, shallow portion of

310   the fault well but not the deep slip rates or the locking depth. Because the normalized deviatoric

311   stressing-rate tensor inversion for the simple fault model failed to recover the forward model slip

312   rate distribution, henceforth, we only discuss results from model inversions that use full or

313   deviatoric stressing-rate tensors that include magnitude.

314   Overall, the joint inversions recover the forward model slip better than or as well as the

315   individual inversions (Figure 5). Although the individual deviatoric and full stressing-rate tensor

316   inversions perform similarly, the joint inversion that utilizes the deviatoric stressing-rate tensors

317   does not recover the slip rates near the locking depth transition zone as well as the joint inversion

318   that utilizes the full stressing-rate tensors. Simultaneously inverting the surface velocities and

319   deviatoric stressing-rate tensors recovers the forward model slip rate distribution better than or as

320   well as all the individual inversions.

321   **4 Complex Fault Model Results**

322   4.1 Forward model validation

323   To validate the complex forward fault models, we compare the maximum horizontal

324   compression orientation for the model and focal mechanism-derived stress tensors (Figure 6). At

325   29 of the 54 crustal locations, the forward interseismic model produces maximum horizontal

326   compression orientations that are within 2 standard deviations (3-15°) of the crustal orientations.

327   The stress states derived from focal mechanisms show spatial variations in the maximum

328   horizontal compression orientation whereas the forward model-generated stressing-rate tensors

329   produce relatively uniform approximately north-south oriented maximum horizontal

330   compression orientations across the region of interest. Most of the locations where the model

331   results do not match the crustal data well are at 7.5 km depth and near the inactive portion of the

332   northern slip pathway (Figure 6). Where the model results differ from crustal data, the model

333   may not completely capture the crustal faulting behavior. For example, some fault structures may

334   be oversimplified or missing from the model, such as the Cox Ranch and Beaumont Plain fault

335   zones (e.g., Yule and Sieh, 2003), which could impact the maximum horizontal compression

336   orientation at specific locations. Further exploration of the activity and geometry of faults along

337   and near the northern slip pathway along the SAFS in the San Gorgonio pass region may provide

338   insight on how to improve the model fit to the crustal data. Overall, the forward model results are

339   consistent with regional studies that invert focal mechanisms for the entire area and show

340   approximately north-south oriented horizontal maximum compression (e.g., Hardebeck and
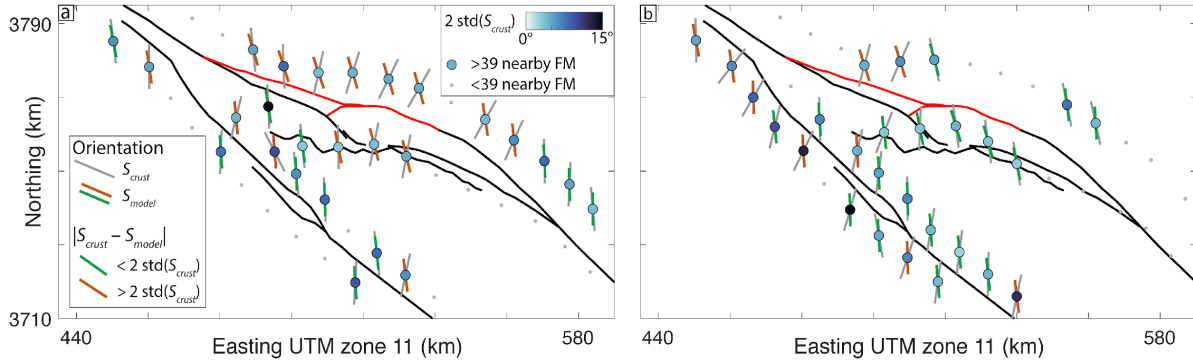
341   Hauksson, 2001).

Figure 6. Maximum horizontal compression orientation (red line) for the focal mechanism derived normalized deviatoric stress tensors (S_{crust}, gray lines) and the forward model generated stressing-rate tensors (S_{model}, green/orange lines) at 7.5 (a) and 15 km (b) depths. Green lines indicate the model results are within 2 standard deviations (std) of the focal mechanism derived results. Circle color shows 2 std of the focal mechanism derived results. Black lines show surface traces of active faults in the forward interseismic models and red lines indicate surface traces of faults that are inactive in the forward models.

342

343   ### 4.2 Inverse model results

344   We present results from inversions of forward model-generated deviatoric stressing-rate

345   tensors and surface velocities that are either regularly spaced or only at locations where data is

346   currently available from the southern California focal mechanism catalog and GNSS stations

347   (Figures 1 & 7). Similar to the simple fault model inversions, all the complex inverse models

348   recover the approximate locking depth applied in the forward model. For all the complex fault

349   model inversions, the area-weighted average element misfit increases with depth until ~22.5 km

350   depth, below which the average misfits remain high (Figure 8a). In general, the misfit for the

351   joint inversions increases less with depth compared to the individual inversions, meaning that for

352   the joint inversions, the resolution of slip rates is more equal at all depths compared to individual

353   inversions (Figure 8a). As a consequence of the smoothing, the inversion underestimates slip

354   rates below the locking depth. Because this misfit is pervasive across the entire model and is not

355   localized to one fault strand or segment, the overall misfit with depth is generally largest within 5

356   km of the 20 km locking depth (Figure 8a). The joint inversions produce smaller misfits than

357   both individual inversions that use regularly spaced and crustal limited locations (Figure 8).
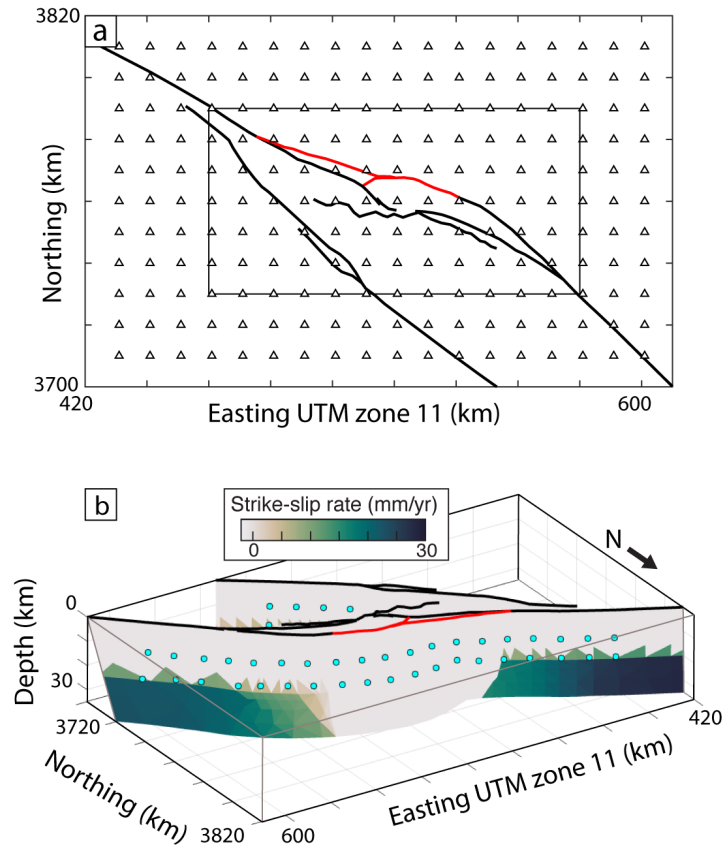

Figure 7. Locations of regularly spaced a) surface velocities (triangles) and b) stressing-rate tensors (circles) for the complex fault model. Red fault trace indicates the inactive portion of the northern slip pathway in forward models. a) Map view with black box indicating the region used for misfit calculations. b) Oblique view of SAFS and SJFS geometry colored by the forward model slip rates.

358

359   To determine which inversion of regularly spaced data best recovers the forward model

360   slip distribution for the entire region of interest, we compare the area-weighted average element

361   slip rate misfit (Equation 1; Figure 8). The regularly spaced surface velocity inversion produces

362   an overall slip rate misfit of 1.4 mm/yr, which is slightly larger than the 1.3 mm/yr misfit of the

363   regularly spaced deviatoric stressing-rate tensor inversion (Figure 8b). The regularly spaced

364   stressing-rate tensor inversion recovers forward model slip better above and within the locking

365   depth transition zone than the regularly spaced surface velocity inversions (Figure 8b). Inverting

366   the regularly spaced data jointly produces the lowest misfit (1.0 mm/yr; Figure 8b).

367   Inversions that utilize stressing-rate and velocity data only at crustal limited locations

368   generally recover the forward model locking depth and slip rate distribution (Figure 8). For

369   individual inversions, inverting crustal limited deviatoric stressing-rate tensors produces a larger

370   misfit than the crustal limited surface velocity misfit (1.8 > 1.4 mm/yr). Below the locking depth,

371   the inversion of deviatoric stressing-rate tensors at crustal limited locations does not recover

372   deep slip rates as well as the inversion of surface velocities at GNSS station locations (Figure 8).

373   The crustal limited joint inversion produces a lower misfit (1.2 mm/yr) than the individual

374   crustal limited and regularly spaced inversions (Figure 8b).
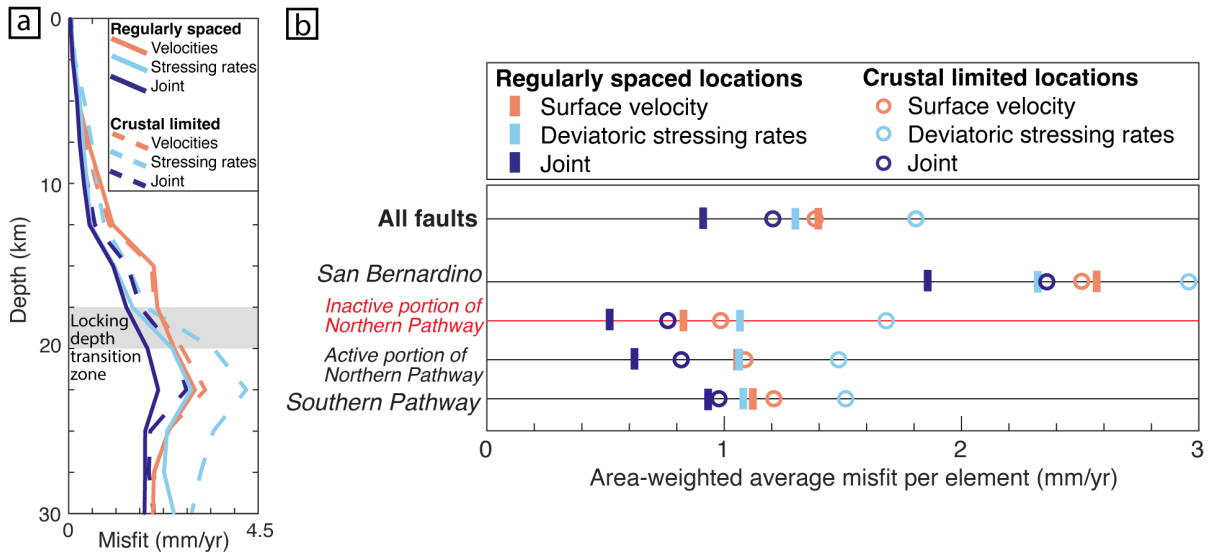

Figure 8. The area-weighted average element misfit a) with depth and b) for the entire region of interest and individual fault segments for the deviatoric stressing-rate tensor (light blue), surface velocity (orange) and joint (indigo) inversions. a) Each point is the misfit for elements within 2.5 km of the specified depth. Solid lines – regularly spaced inversions. Dashed lines – crustal limited inversions. b) Vertical lines – regularly spaced inversions. Open circles – crustal limited inversions.

375

376   Inverting regularly spaced stressing-rate tensors and surface velocities improves the

377   overall inversion performance compared to inverting only information at crustal limited

378   locations. The regularly spaced surface velocity inversion includes 198 surface velocity

379   locations, and the crustal limited surface velocity inversion includes 201 locations. The small

380   difference in the number of constraining data may explain the similar misfit of both surface

381   velocity inversions, but the difference in spatial distribution of the constraining data could

382   contribute to the differences in the misfits along individual fault strands or segments (Figure 8).

383   Reducing the number of deviatoric stressing-rate tensors that constrain the individual inversions

384 from 100 to 54 leads to an overall increase in the inverse model misfit to the forward model slip-

385 rate distribution. Furthermore, the 54 deviatoric stressing-rate tensor crustal limited locations are

386 not evenly distributed across the region of interest. A significant gap in microseismicity along

387 the southern SAFS reduces the number of stressing-rate tensors constraining the inversion by

388 33% (Figures 1 & 6). This reduction could explain why the crustal limited deviatoric stressing-

389 rate tensor inversion cannot resolve slip rates along some fault segments as well as the regularly

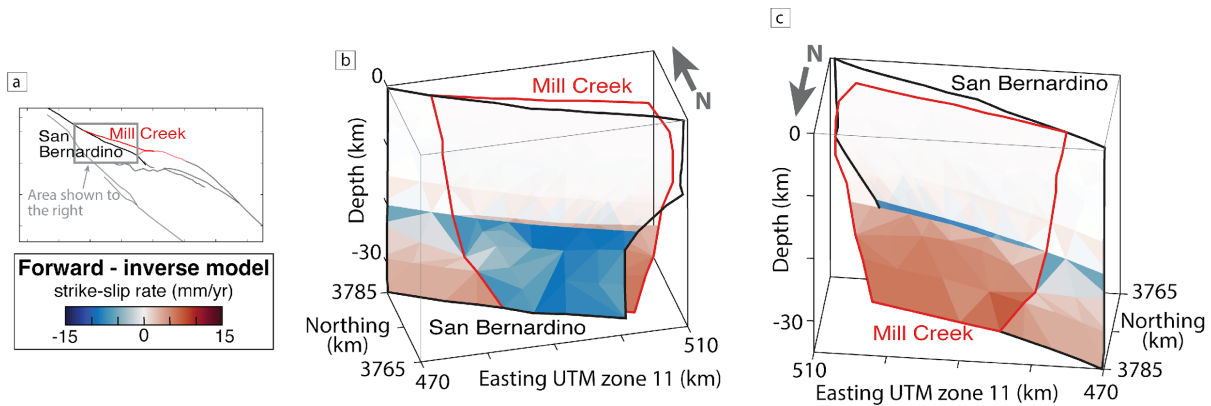390 spaced deviatoric stressing-rate tensor inversion.

Figure 9. The difference between the forward model applied and the regularly spaced stressing-rate tensor inversion estimated strike-slip rates along the Mill Creek strand (red outline) and the San Bernardino segment (black outline). a) Map of region of interest with gray box indicating the area shown in perspective views in b (from the south) and c (from the north). b and c) Red elements indicate the inverse model overestimates slip rates while blue elements indicate the inverse model underestimates slip rates. Fault elements are transparent above the 20 km locking depth.

391

392 We expect the largest misfits around fault branches and along closely spaced faults where

393 inversions cannot uniquely resolve slip rates. The San Bernardino segment directly connects to

394 both the inactive portion of the northern slip pathway and the active southern pathway of the

395 southern SAFS forming a branched fault (Figure 1). Comparing the slip rate misfits along

396 individual fault segments and strands provides insight on how well each inversion can recover

397 slip rates at fault branches and along the two subparallel slip pathways of the southern SAFS.

398 The San Bernardino segment of the SAFS yields the greatest misfit for all the inversions (Figure

399 8b). Due to smoothing of slip rate across faults within the inversion, the inverse models

400 overestimate slip rates along the inactive portion of the northern pathway (Figure 9 red colors)

401 and underestimate slip rates along the adjacent San Bernardino segment (Figure 9 blue colors).

402 The tradeoff in slip rates among the branched fault segments is lesser for the joint inversion. As a

403   result, the joint inversion misfits along the inactive portion of the northern pathway and the San

404   Bernardino segment are smaller than the misfits for the inversions of individual constraints.

5 Discussion

405

5.1 Constraint weighting in joint inversions

406

407   The weighting of surface velocities and stressing-rate tensors within the inversions

408   depends on three parameters: 1) the relative numbers of constraint components, 2) the prescribed

409   uncertainties, and 3) smoothing weighting. Because multiple factors impact the weighting of

410   differing data types, the surface velocities and stressing-rate tensors are likely not equally

411   weighted in the joint inversions. Each stressing-rate tensor consists of six components (three

412   shear and three normal), and each surface velocity consists of two components (east and north).

413   For the regularly spaced joint inversions, a greater number of stressing-rate tensor components

414   constrain the inversion than surface velocity components; this means that the stressing-rate

415   tensors may have more weight in the joint inversion than the surface velocities. In contrast, for

416   the crustal limited joint inversions, a greater number of surface velocity components constrain

417   the inversion than stressing-rate tensor components. Regardless of the ratio of stressing-rate

418   tensor to surface velocity components constraining the inversions, increasing the amount of

419   constraining information improves the inverse model's recovery of forward model slip rates.

420   Increasing the number of surface velocity locations by utilizing campaign GNSS stations or

421   InSAR data could potentially improve the inversion performance. The second factor that impacts

422   the weighting of the two data types is the uncertainty we prescribe to each component. Because

423   each component for surface velocities and stressing-rate tensors has uncertainty of 20-40% of the

424   component, the two data types have similar weighting in the joint inversions. Since the

425   smoothing weighting can also impact how the inverse model constraining information is

426   weighted, we assess the impact of varying the smoothing weighting on the slip rate misfit for the

427   complex fault inversions. We find that a range of smoothing weightings (varying by a factor of

428   10^4) for all the inversions produce slip rate misfits that vary by < 0.05 mm/yr (Supporting

429   Information), which suggests that the inversions are more sensitive to the number and location of

430   constraining data than the smoothing weighting.

431   5.2 Comparison of individual inverse model results

432   The regularly spaced stressing-rate tensor inversions may have better overall performance

433   than the surface velocity inversions because the stressing-rate tensors are at depth, closer to the

434   locking depth transition zone and the slipping portion of faults. The stressing-rate tensor spacing

435   assessment shows that for inversions that utilize stressing-rate tensors at a single depth the misfit

436   generally decreases as the stressing-rate tensor depth increases. Many of the simple fault model

437   stressing-rate tensor inversions that utilized tensors at a single depth outperformed the surface

438   velocity inversion, and the addition of stressing-rate tensors at a second depth further improved

439   the stressing-rate tensor inversion performance. Furthermore, the joint inversions include

440   constraints at three separate depths (0, 7.5 and 15 km) and best recover forward model slip rates

441   for both the simple fault and complex fault models. Inverting velocity and stressing-rate data at

442   multiple depths may more robustly capture spatial variations in the stressing-rate and velocity

443   field than inversions that utilize constraints at a single depth. More information on spatial

444   variations of conditions may yield more accurate inversions for slip rate.

445   For the complex fault model, the surface velocity inversions can recover deep

446   interseismic slip rates (> 25 km depth) better than stressing-rate tensor inversions (Figure 8a).

447   The assessment of the optimal spacing of stressing-rate tensors shows that decreasing the along-

448   strike tensor spacing from 20 km to 10 km can improve the inversion performance (Figure 4a-e),

449   suggesting that stressing-rate tensors may provide higher resolution slip rate information over

450   short distances (10-15 km). Consequently, the stressing-rate tensors provide better slip rate

451   information along portions of faults closest to the tensors (< 25 km depth) than below the locking

452   depth. Even though the interseismic surface velocities are farther from the slipping portions of

453   faults than the subsurface stressing-rate tensors, the ability of the surface velocities to resolve

454   slip rates is less sensitive to their distance from the fault. As a result, surface velocity inversions

455   may better constrain interseismic slip rates along deep portions of the fault (> 25 km depth) than

456   stressing-rate tensor inversions (Figure 8a). In addition to having a greater number of inputs, the

457   joint inversion takes advantage of the benefits of both data types, which improves the inverse

458   model performance compared to individual inversions (Figure 8).

459   5.3 Future application to natural fault systems

460   The complex fault models show that joint inversions of stressing-rate tensors and surface

461 velocities could improve current estimates of slip rates along closely spaced and branching

462 faults; the distribution of these rates can help constrain both the locking depth and relative

463 activity of closely spaced faults. For example, joint inversions resolve slip rates well along the

464 northern pathway of the southern SAFS through the San Gorgonio Pass where fault activity

465 remains debated (e.g., Kendrick et al., 2015; Blisniuk et al., 2021).

466   Implementing the inverse method that we present here for any crustal fault system

467 requires a priori information including geodetic and microseismic catalogs as well as a three-

468 dimensional fault geometry, and uncertainty or inaccuracy in the inverse model inputs

469 propagates through the model. Because we invert forward model generated stressing-rate tensors

470 and surface velocities, we know that the fault geometry used in the inversions is accurate. As a

471 consequence, the inversion misfits that we calculate exclude uncertainty that may stem from

472 uncertainty or inaccuracy in the model fault geometry. In addition to uncertainty related to the a

473 priori information, model parameters, such as fault element size, may impact the inverse model

474 performance. In this study, the simple and complex fault models have average element lengths of

475 3-5 km. Future applications of the inverse method we present here should consider that the

476 average element length could impact the optimal stressing-rate tensor spacing.

477   Because microseismicity in the crust is generally not evenly distributed across a region

478 (Figure 1), the optimal regular spacing that we determine from the idealized simple fault model

479 may not be available for crustal data sets. For the complex SAFS model, limiting the stressing-

480 rate tensor locations to points with sufficient nearby recorded focal mechanisms increases the

481 average misfit of the joint inversion, but the inversion estimates < 2.0 mm/yr of strike-slip along

482 the inactive northern pathway. With time and additional microseismicity, focal mechanism

483 catalogs may enable additional tensor locations to be included in the model, which would

484 improve the spatial consistency in model performance.

485   Another challenge prevents us from applying this new method to crustal data at this time:

486 we do not know of a method to reliably estimate deviatoric stress magnitude and stressing rate

487 within the crust. The results of this study show that inversions of deviatoric stressing-rate tensors

488 perform as well as inversions that utilize full stressing-rate tensors, meaning that inversions of

489 crustal data would not require mean normal stress state information. The stress states inferred

490 from focal mechanisms provide normalized stress due to microseismicity but not magnitudes. A

491 recent study provides a method to estimate absolute stress magnitude from focal mechanisms and

492 precisely located earthquakes (Fialko, 2021). However, absolute stress does not directly

493 correspond to interseismic stressing rates that are necessary to invert for slip rates. Absolute

494 stress evolves with time since the last earthquake so that microseismicity responds to the total

495 stress state, which includes the effect of accumulated tectonic loading, not solely stressing rates

496 from interseismic loading. If we can derive crustal deviatoric stressing rates, then we may be

497 able to provide additional constraint on deep slip rates along faults in the San Gorgonio Pass

498 region, which would reveal locking depths and relative fault activity.

499 **6 Conclusions**

500   We present a new method that utilizes interseismic surface velocities and subsurface

501 stressing-rate tensors to estimate three-dimensional slip rate distributions along a simple, isolated

502 strike-slip fault model and a complex fault model that simulates the southern SAFS. The

503 inversions of forward model-generated stressing-rate tensors and surface velocities for the simple

504 fault model reveal that a sparse, regularly spaced distribution of stressing-rate tensors can

505 recover the forward model slip rate distribution better than surface velocity inversions alone.

506 Additionally, inversions that utilize deviatoric stressing-rate tensors recover the slip rates along

507 faults as well as inversions of full stressing-rate tensors. Inverting forward-model-generated

508 surface velocities and subsurface stressing-rate tensors jointly recovers both the simple and

509 complex forward model applied slip rate distributions better than inverting velocity and stress

510 information individually. For the complex fault model that simulates the SAFS through the San

511 Gorgonio Pass region, inversions of regularly spaced velocity and stress information recover the

512 forward model slip rates better than inversions of velocity and stress information only at

513 locations where crustal data is currently available.

514   Joint inversions of surface velocities from GNSS stations and subsurface deviatoric

515 stressing rates potentially derived from microseismic focal mechanisms could provide additional

516 constraint on the deep slip distribution and as a result both the interseismic locking depth and

517 relative activity of faults along closely spaced faults. The complex fault inversions generally

518 recover very slow slip rates along the northern pathway of the SAFS that is inactive in the

519 forward model, suggesting that the method we present here could be used to inform the activity

520   of the northern and southern pathways of the SAFS through the San Gorgonio Pass. However,

521   prior to applying this new method to invert crustal datasets, we require a method to reliably

522   estimate the deviatoric stressing rates that include magnitude. With an increase in the number of

523   available microseismic focal mechanisms with time and a method to calculate stressing rates

524   from focal mechanisms or other data, the method we present here could improve constraints on

525   fault slip rate distributions in regions with closely spaced and branching faults.

Open Research

531   The crustal deformation software Poly3D is made available by the Stanford Tectonic

532   Geomorphology lab at https://github.com/stgl/poly3d. The inversion software TriInv is available

533   at https://github.com/jploveless/triinv. The Poly3D and TriInv input files for the simple and

534   complex fault models are available for download via figshare (Elston et al., 2023).

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