

Long-range Forecasting as a Past Value Problem: Using Scaling to Untangle Correlations and Causality

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Key Points:

- Scaling-based long-range stochastic forecasting is a past value problem not an initial value problem.
- Granger causality shows that spatial correlations of temperature cannot improve memory-based predictions of individual infinite time series.
- The statistics and teleconnection patterns of the real-world can be reproduced with stochastic simulations without causal relationships.

Abstract

Conventional long-range weather prediction is an initial value problem that uses the current state of the atmosphere to produce ensemble forecasts. Purely stochastic predictions for long-memory processes are “past value” problems that use historical data to provide conditional forecasts. Teleconnection patterns, defined from cross-correlations, are important for identifying possible dynamical interactions, but they do not necessarily imply causation. Using the precise notion of Granger causality, we show that for long-range stochastic temperature forecasts, the cross-correlations are only relevant at the level of the innovations – not temperatures. This justifies the Stochastic Seasonal to Interannual Prediction System (StocSIPS) that is based on a (long memory) fractional Gaussian noise model. Extended here to the multivariate case, (m-StocSIPS) produces realistic space-time temperature simulations. Although it has no Granger causality, emergent properties include realistic teleconnection networks and El Niño events and indices.

1 Introduction

For forecasts over the weather regime – below the ≈ 10 day deterministic predictability limit – Numerical Weather Prediction (NWP) and General Circulation Models, (GCMs) have been highly successful, yet for longer term macroweather (“long range”) forecasts, their skill is disappointing. This has motivated the development of stochastic alternatives. Successful stochastic forecasts require causal models and the search for causality typically starts with correlations. In the last years, two stochastic strands have emerged each inspired by different sources of strong correlations. A particularly well studied constellation of correlations are associated with large scale spatial structures – teleconnections – as vividly displayed in climate networks [e.g.: (Donges et al., 2009b; Ludescher et al., 2014)]. Teleconnection-inspired forecast models often use climate (especially El Niño) indices [see (Brown & Caldeira, 2020; Eden et al., 2015)]. An alternative source of correlations upon which to base causal models is the system’s long range memory (Blender & Fraedrich, 2003; Bunde et al., 2005; Rypdal et al., 2013; Varotsos et al., 2013), a consequence of temporal scaling, itself associated with long range

39 spatial scaling, a basic property of the governing equations that is well respected by both GCMs
40 and the empirical data [(Palmer, 2019), see also the review (Lovejoy & Schertzer, 2013)].

41 At the moment, these strands are at virtual antipodes. Models based on teleconnections
42 use only data from a few months – they are Markovian, short (exponential) memory models that
43 get their skill largely from spatial information. In this, they are almost as extreme as GCMs that
44 are zero-memory, initial value models based purely on the spatial information at $t = 0$. In
45 contrast, the scaling, long memory Stochastic Seasonal to Interannual Prediction System
46 (StocSIPS) model is at the opposite extreme (Del Rio Amador & Lovejoy, 2019, 2020). For each
47 pixel, it uses historical past data to forecast the future - but uses no other data as co-predictors: it
48 is a purely “past value” model. In spite of this apparent deficiency, for monthly, seasonal, and
49 annual temperature forecasts StocSIPS’ skill already rivals – or exceeds – those of GCMs.

50 This paper attempts to answer the obvious question: is it possible to make a model that
51 combines strong spatial correlations and long memory to produce even more skillful forecasts?
52 While it is well known that correlations and causality are not synonymous, the precise
53 relationship between the two is often unclear and there are no general tools for untangling them.
54 However, the present case is an important exception: the problem of improving StocSIPS using
55 spatial co-predictors can be precisely answered by using the theoretical framework of Granger
56 causality (Granger, 1969).

57 Two series are Granger causally related iff one can be used as a skillful co-predictor of
58 the other. Therefore, it suffices to enquire as to the Granger causality of the space-time StocSIPS
59 model. If the temperature teleconnections have no Granger causality, then they will not improve
60 StocSIPS forecasts. In the first part of the paper we propose a multivariate surface temperature
61 model (m-StocSIPS) for which the uncoupled regional StocSIPS model gives the optimal
62 forecast. m-StocSIPS also reproduces the empirical cross-correlation structure over a wide range
63 of time lags. This is made more convincing by making simulations that display numerous
64 realistic but emergent model properties including spatial teleconnection networks, realistic El
65 Niño patterns and indices. The optimal m-StocSIPS predictor at a given location is obtained from
66 its own past if the series is long enough. Even strongly spatially correlated series from other
67 locations do not help improve the skill, teleconnection correlations may be seductive, but without
68 Granger causality, they are misleading.

69 **2 Methods**

70 **2.1 Stochastic modeling of the temperature anomalies**

71 In macroweather temperature anomalies at position \mathbf{x} (after removing the annual cycle)
72 can be modeled as a trend-stationary process:

$$73 \quad T_{\text{anom}}(\mathbf{x}, t) = T_{\text{anth}}(\mathbf{x}, t) + T(\mathbf{x}, t), \quad (1)$$

74 where $T(\mathbf{x}, t)$ is a stochastic stationary component and $T_{\text{anth}}(\mathbf{x}, t)$ is a deterministic low-
75 frequency response to anthropogenic forcings as in (Del Rio Amador & Lovejoy, 2019).

76 The stationary stochastic $T(\mathbf{x}, t)$, is the zero-mean residual natural variability that
77 includes “internal” variability and the response of the system to other natural forcings (e.g.:
78 volcanic and solar). These anomalies can be predicted by modelling each position independently
79 using an univariate representation [the regional StocSIPS model presented in (Del Rio Amador

80 & Lovejoy, 2020), hereafter DRAL]. However, to investigate whether forecasts for individual
 81 series can be improved using other data, a multivariate framework is needed. A quasi-Gaussian
 82 process, stationary in time, but inhomogeneous in space has a multivariate continuous-in-time
 83 Wold representation (moving average of infinite order MA(∞)) (Box et al., 2008; Brockwell &
 84 Davis, 1991; Wold, 1938):

$$85 \quad T_i(t) = \sum_j \int_{-\infty}^t \kappa_{ij}(t-t') \gamma_j(t') dt'. \quad (2)$$

86 The index “ i ” is a subscript indicating the spatially discrete position (“pixel”), the matrix $\kappa_{ij}(t)$
 87 is a kernel specifying the MA process and the innovations, $\gamma_i(t)$, are normalized Gaussian white
 88 noise processes with $\langle \gamma_i(t) \rangle = 0$, $\langle \gamma_i^2(t) \rangle = 1$ and cross-correlation matrix:

$$89 \quad \rho_{ij}(t-t') = \langle \gamma_i(t) \gamma_j(t') \rangle = a_{ij} \delta(t-t'), \quad (3)$$

90 where $\delta(t)$ is the Dirac function, $\langle \cdot \rangle$ denotes ensemble averaging and $-1 < a_{ij} < 1$. This “delta-
 91 correlated” innovation temporal structure implies that the latter are totally unpredictable and is
 92 the key property below.

93 The cross-covariance for time lag $\Delta t > 0$ for the temperature is:

$$94 \quad C_{ij}(\Delta t) = \langle T_i(t) T_j(t + \Delta t) \rangle = \sum_m \sum_n \int_0^{\infty} \kappa_{im}(t') \kappa_{jn}(t' + \Delta t) a_{mn} dt', \quad (4)$$

95 hence the cross-correlation is:

$$96 \quad R_{ij}(\Delta t) = \frac{C_{ij}(\Delta t)}{\sqrt{C_{ii}(0) C_{jj}(0)}}. \quad (5)$$

97 Since the process is Gaussian with zero mean, it is completely determined by the
 98 correlation structure. In the macroweather regime – with the possible exception of extremes –
 99 $T_i(t)$ is nearly Gaussian in time, but multifractal in space and the statistics of its fluctuations are
 100 scale-invariant over wide ranges (Lovejoy, 2018; Lovejoy et al., 2018; Lovejoy & Schertzer,
 101 2013). The scaling behaviour in time implies that there are power-law correlations and hence
 102 potentially a large memory that can be exploited. The simplest relevant scaling process is the
 103 statistically stationary fractional Gaussian noise (fGn) process.

104 The fGn based StocSIPS model was first developed for monthly and seasonal forecast of
 105 globally averaged temperature (Lovejoy et al., 2015; Del Rio Amador & Lovejoy, 2019).
 106 Recently, DRAL extended StocSIPS to the regional prediction of $T_i(t)$, where each grid point
 107 was considered as an independent time series. This univariate representation using a resolution τ
 108 fGn process (see the supporting information) can be extended to the multivariate case with the
 109 kernel:

$$110 \quad \kappa_{ij}(t) = \delta_{ij} \frac{1}{\tau} \frac{c_{H_i} \sigma_{T_i}}{\Gamma[H_i + 3/2]} \left[t^{H_i+1/2} - (t-\tau)^{H_i+1/2} \theta(t-\tau) \right], \quad (6)$$

111 where $\theta(t)$ is the Heaviside (step) function, Γ is the Gamma function, $H_i \in (-1,0)$ is the
 112 fluctuation exponent characterizing the scaling of the fluctuations in time, σ_{T_i} is the standard

113 deviation, c_{H_i} is a normalization constant and δ_{ij} is the Kronecker δ . The different temperature
 114 series, $T_i(t)$, are correlated, and the spatial correlation structure is inherited from the innovation
 115 cross-correlations, a_{ij} . The presence of the Kronecker δ in Eq. (6) implies that the temperature at
 116 grid point “ i ” is an fGn with parameters H_i and σ_{T_i} .

117 In DRAL it was shown that the fGn model (Eq. (6)) is an accurate univariate
 118 representation of the natural temperature variability for most of the globe. However, in the
 119 tropical ocean, the fGn model approximates the temperature increments, meaning that the actual
 120 temperature variability is modelled as a fractional Brownian motion (fBm) process with
 121 fluctuation exponent $H_i \in (0,1)$ (see Fig. 1(a)), although cut-off at multi-annual scales. The
 122 fluctuation exponents of fBm and fGn are related as $H_{\text{fBm}} = H_{\text{fGn}} + 1$. Both cases are high-
 123 frequency approximations of the more general fractional relaxation noise (fRn) process,
 124 introduced in (Lovejoy, 2019; Lovejoy et al., 2020).

125 The use of a parametric model considerably reduces the number of parameters and
 126 clarifies their interpretation. m-StocSIPS is fully determined by the symmetric innovation cross-
 127 covariance matrix a_{ij} , the amplitudes of the temperature fluctuations σ_{T_i} , and the memory
 128 exponents H_i . These characterize the internal dynamics; for example low values of σ_{T_i} over the
 129 oceans are a consequence of the greater heat capacity and thermal inertia and H_i characterizes the
 130 memory associated with the multiscale energy storage mechanisms (Lovejoy, 2020; Lovejoy et
 131 al., 2020).

132 m-StocSIPS is defined by $N(N + 3)/2$ parameters; in comparison, a vector
 133 autoregressive order p model (VAR(p)) needs pN^2 values (Box et al., 2008; Brockwell & Davis,
 134 1991) and for long-memory processes, p is large. These “black box” type models suffer from
 135 opaque physical interpretations, and their large number of VAR parameters makes them unstable
 136 and subject to overfitting. The same is true for general vector autoregressive-moving average
 137 VARMA(p, q) models.

138 Ultimately, the adequacy of a model must be checked. In this case, the diagnostics are
 139 primarily based on the examination of the whiteness and time-independence of the residual
 140 vectors $\gamma_i(t)$, which are obtained by inverting Eq. (2) with the estimated parameters. The
 141 whiteness was verified in DRAL using the theory in Appendix 1 of (Del Rio Amador & Lovejoy,
 142 2019). To verify the time-independence of the innovations (Eq. (3)), there exist many “goodness-
 143 of-fit” tests based on the residual cross-covariance matrices at several lags (Ali, 1989; Hosking,
 144 1980; Li & McLeod, 1981; Poskitt & Tremayne, 1982). In our case, they are either impractical –
 145 the matrices have more than $1.1 \cdot 10^8$ elements – or impossible since there is only one realization
 146 of our planet. Nevertheless, a visual inspection of the residual cross-correlation matrices for
 147 different lags (shown in Fig. S2 in the supporting information) may be enough. Our results
 148 indicate that m-StocSIPS is a good approximation, confirmed in Sect. 3.3 using global
 149 simulations that convincingly reproduce the space-time patterns (Fig. 2). Aside from minor
 150 numerical approximations, StocSIPS predictions presented in DRAL are optimal m-StocSIPS
 151 predictions in the minimum mean square error framework, explaining the high StocSIPS forecast
 152 skill.

153 **2.3 Correlation, causality and Granger causality**

154 m-StocSIPS uses an fGn model for most of the globe (where $H_i < 0$) and a (truncated)
 155 fBm model for the tropical ocean (where $H_i > 0$). The cross-correlation structure for the

156 temperature anomalies is thus determined by three kinds of interaction: 1) fGn-fGn, 2) fGn-fBm
 157 and 3) fBm-fBm. The fGn-fGn cross-correlation can be obtained directly by using Eq. (6) in Eq.
 158 (4). The exact result is given in the supporting information (Eq. S22). Similar expressions can be
 159 obtained for the other two cases (Coeurjolly et al., 2010).

160 While fGn is a stationary process and fGn-fGn cross-correlations only depend on the lag
 161 Δt , this is not the case for fBm. Nevertheless, under some approximations for long enough finite
 162 time series, it is possible to obtain expressions that only depend on Δt [see (Delignières, 2015)].
 163 The cross-correlations for $\Delta t \gg \tau$ (τ is the temporal resolution of the time series, i.e. 1 month)
 164 are:

165 Case 1: fGn-fGn ($H_i < 0$ and $H_j < 0$),

$$166 R_{ij}(\Delta t) \sim \varphi_{H_i, H_j} a_{ij} (\Delta t / \tau)^{H_i + H_j}. \quad (7)$$

167 Cases 2 and 3: fGn-fBm and fBm-fBm ($H_i > 0$ or/and $H_j > 0$),

$$168 R_{ij}(\Delta t) \sim \phi_{H_i, H_j} a_{ij} \left[1 - (\Delta t / \tau_r^{ij})^{H_i + H_j} \right], \quad (8)$$

169 for $\Delta t \ll \tau_r^{ij}$, where τ_r^{ij} is a characteristic relaxation time related to the ocean weather-ocean
 170 macroweather transition (Lovejoy, 2019; Lovejoy et al., 2018; Del Rio Amador & Lovejoy,
 171 2020), and φ_{H_i, H_j} and ϕ_{H_i, H_j} are proportionality constants that depend on H_i and H_j (see Eq. S25
 172 in the supporting information). As expected, these expressions coincide with the high-frequency
 173 approximations of the stationary fRn cross-correlations for H_i and H_j .

174 Equations (7) and (8) imply that the cross-correlation structure of the temperature field
 175 has a spatial correlation component given by the matrix a_{ij} , and a temporal component
 176 determined by the memory dependence of the individual series (H_i and H_j). In this sense, they
 177 are similar, but more general than the average Statistical Space-Time Factorization (SSTF)
 178 proposed earlier by (Lovejoy & de Lima, 2015). For a given location i and lag Δt , the cross-
 179 correlation with any other location j will be higher for series whose past is important (large H_i)
 180 as compared to series with short memories (small H_i).

181 Now consider the prediction problem for the general process given by Eq. (2). Since the
 182 process is Gaussian, we use the minimum mean square error framework. Although correlations
 183 play an important role in the statistical description and in pattern identification, it is wrong to
 184 infer causality based on the lagged cross-correlation structure alone. In the words of (Buchanan,
 185 2012): “Not only does correlation not imply causality, but lack of correlation needn’t imply a
 186 lack of causality either”. A classic example is two correlated systems without any dynamic
 187 interaction between them but with a common dependence on a third variable. Conversely, there
 188 are coupled chaotic systems, that exhibit a complete lack of long-term statistical correlation,
 189 despite sharing a clear cause-effect link (Sugihara et al., 2012).

190 An example from (Barnston, 2014; Lyon & Barnston, 2005) may clarify the discussion.
 191 They argue that El Niño events *lead* to a cascade of global impacts, e.g.: wet Central Asias.
 192 However, in GCM terms, a given set of initial conditions is the ultimate cause of both an El Niño
 193 and a wet season in Central Asia. The chain of events starting from those initial conditions
 194 explains the mutual correlations without mutual causation. In traditional mechanistic terms, the
 195 best that can be done to reconcile the two viewpoints is the notion of causal chain (e.g. Bunge,

196 2017). In this fairly qualitative view, the ultimate cause – the initial conditions – triggers a causal
 197 chain of events in which El Niño is a “proximate” link leading to a wet season in Central Asia.

198 From a stochastic point of view, (Andree, 2019) argues that a time series (e.g. the
 199 temperature at a given location) has a memory part depending on its own past and a causal part
 200 from the past at other locations. For short-memory processes, this causal contribution may be
 201 important, explaining how some empirical models obtain their skill by effectively borrowing
 202 memory from co-predictors. However, the longer the memory – the more autoregressive steps
 203 that are needed – the lower the influence of the causal component. In the limit, all the causal
 204 chain for a given time series may be embedded in its own past, so that GCMs and StocSIPS
 205 exploit a whole chain of causation, not only the last links in the chain so that their skill is higher
 206 than models that only exploit proximate causes.

207 The precise tool needed to clarify stochastic causality issues is Granger causality
 208 (Granger, 1969). We say that the temperature T_j at location j fails to Granger-cause the
 209 temperature T_i , if for all future times $t > 0$, the mean square error (MSE) of a forecast of $T_i(t)$
 210 based on its own past ($T_i(s)$ for $s \leq 0$) is the same as the MSE of a forecast of $T_i(t)$ based on
 211 both $T_i(s)$ and $T_j(s)$. The notion of Granger causality is intuitive and provides a much more
 212 rigorous criterion for causation than simple lagged cross-correlations. While other notions of
 213 causality exist, Granger causality does imply forecasting ability, which is our only concern here.

214 We now investigate the Granger causality of m-StocSIPS. A necessary and sufficient
 215 condition for the optimality of an estimator is given by the orthogonality principle (Box et al.,
 216 2008; Brockwell & Davis, 1991; Palma, 2007; Straškraba, 2007; Wold, 1938), that states that the
 217 error of the optimal predictor (in a mean square error sense) is orthogonal to any possible
 218 estimator:

$$219 \quad \langle \hat{T}_i(t) E_i(t) \rangle = 0, \quad (9)$$

220 where $\hat{T}_i(t)$ is the temperature predictor for position i at a future time $t > 0$ and $E_i(t) = T_i(t) -$
 221 $\hat{T}_i(t)$ is the error.

222 From the integral representation (Eq. (2)) and given a diagonal kernel $\kappa_{ij}(t)$ as in Eq. (6),
 223 we find that the optimal predictor satisfying this principle is:

$$224 \quad \hat{T}_i(t) = \int_{-\infty}^0 \kappa_{ii}(t-t') \gamma_i(t') dt', \quad (10)$$

225 with error:

$$226 \quad E_i(t) = \int_0^t \kappa_{ii}(t-t'') \gamma_i(t'') dt''. \quad (11)$$

227 E_i only depends on future innovations $\gamma_i(t'')$ ($t'' > 0$), while the estimator, $\hat{T}_i(t)$, depends only
 228 on past innovations $\gamma_i(t')$ ($t' < 0$). Since the white noise innovations are δ -correlated in time
 229 (Eq. (3)), for any i, j we have:

$$230 \quad \langle T_j(s) E_i(t) \rangle = 0; \quad s < 0, t > 0. \quad (12)$$

231 This means that any predictor that is a linear combination of past temperature values from
 232 any position j , is orthogonal to the error of the predictor obtained from the past at location i ,
 233 given by Eq. (10). Hence, the predictor (Eq. (10)) is optimal given the full field $T(\mathbf{x}, t)$ for $t \leq 0$.
 234 This is a precise statement of Granger causality. Although there are large cross-correlations
 235 inherited from the innovation matrix a_{ij} (Eqs. (7) and (8)), the information of past temperatures
 236 from other locations does not help improve the forecast. For StocSIPS predictions, it is the lack
 237 of innovation connectivity at non-zero lags that implies that the optimal predictor for any given
 238 location is obtained from its past. In effect, these occasionally strong spatial correlations “were
 239 already used” for building the past of any given time series, whose past is therefore enough to
 240 yield the optimal predictor for that specific series.

241 3 Results

242 3.1 Empirical cross-correlations

243 Our analysis were based on monthly, 2.5° resolution surface temperatures (T2m: $73 \times$
 244 $144 = 10512$ points) from 1948 to 2019 (864 months in total) from the National Centers for
 245 Environmental Prediction/National Center for Atmospheric Research Reanalysis 1 (Kalnay et al.,
 246 1996; NCEP/NCAR, 2020).

247 The validity of the univariate fGn (StocSIPS) model was confirmed in DRAL by testing
 248 the whiteness of the innovations $\gamma_i(t)$ for every grid point i , which were obtained by inverting
 249 the discrete version of Eq. (2) (see the supporting material for the theoretical details). We used
 250 the fact that a white noise process is a particular case of fGn with fluctuation exponent $H_\gamma =$
 251 $-1/2$. Maximum likelihood estimates for the residuals at 10512 grid points give $H_\gamma =$
 252 -0.498 ± 0.003 and standard deviations $\sigma_\gamma = 1.000 \pm 0.002$, which confirms that the
 253 innovations are unit variance δ -correlated white noise and hence the adequacy of the fGn model
 254 for the natural temperature variability in the univariate case.

255 To show that the multivariate model is also realistic, we must check that the lagged cross-
 256 correlations between the innovations at different locations (Eq. (3)) are negligible. For this
 257 analysis, we obtained the lagged cross-correlation matrices involving the 10512 grid points for
 258 the innovations, $\rho_{ij}(\Delta t)$, and for the temperature variability, $R_{ij}(\Delta t)$, for Δt from 1 to 12
 259 months. These matrices are shown in the supporting information (Fig. S2) for $\Delta t = 0, 1, 2$ and 3
 260 months. For the temperature, the correlations decrease with Δt , but large values are often
 261 obtained for relatively large lags, following Eqs. (7) and (8). For the innovation cross-
 262 correlations, the values decrease much faster. For $\Delta t = 0$, the elements $\rho_{ij}(0) = a_{ij}$ are
 263 relatively large, but even for $\Delta t = 1$ month, almost all the correlation is lost. This indicates that
 264 the innovations closely satisfy the discrete version of the time-independence condition Eq. (3).

265 Another way of testing the model is by checking that Eqs. (7) and (8) are good
 266 approximations of the empirical $R_{ij}(\Delta t)$. Fig. 1(a) shows the results for ensembles with similar
 267 a_{ij}, H_i and H_j values ($a_{ij} = 0.5 \pm 0.025$ gives 10490 pairs). Comparisons are shown for the
 268 three cases (fGn-fGn, fGn-fBm and fBm-fBm):

269 Case 1: fGn-fGn (marked as “+” in Fig.1(a)), we chose the series with $H_i = -0.1 \pm$
 270 0.025 (red symbol) and $H_j = -0.3 \pm 0.025$ (yellow), 380 pairs.

271 Case 2: fGn-fBm (marked as “o”), the series with $H_i = -0.1 \pm 0.025$ (purple) and $H_j =$
 272 0.25 ± 0.025 (green), 569 pairs.

273 Case 3: fBm-fBm (marked as “x”), the series with $H_i = 0.3 \pm 0.025$ (black) and $H_j =$
 274 0.4 ± 0.025 (cyan), 323 pairs.

275 Fig. 1(b) shows the average cross-correlations functions of the lag $\lambda = \Delta t/\tau$ ($\tau = 1$
 276 month), with fits from Eqs. (7) and (8). For case 1, we included the dashed red curve
 277 corresponding to higher order corrections for fRn processes (Lovejoy, 2019; Lovejoy et al.,
 278 2020). The small values of the cross-correlation innovation pairs (“*” in the figure) confirm the
 279 independence of these series. Although the expressions (Eqs. (7) and (8)) are only first order

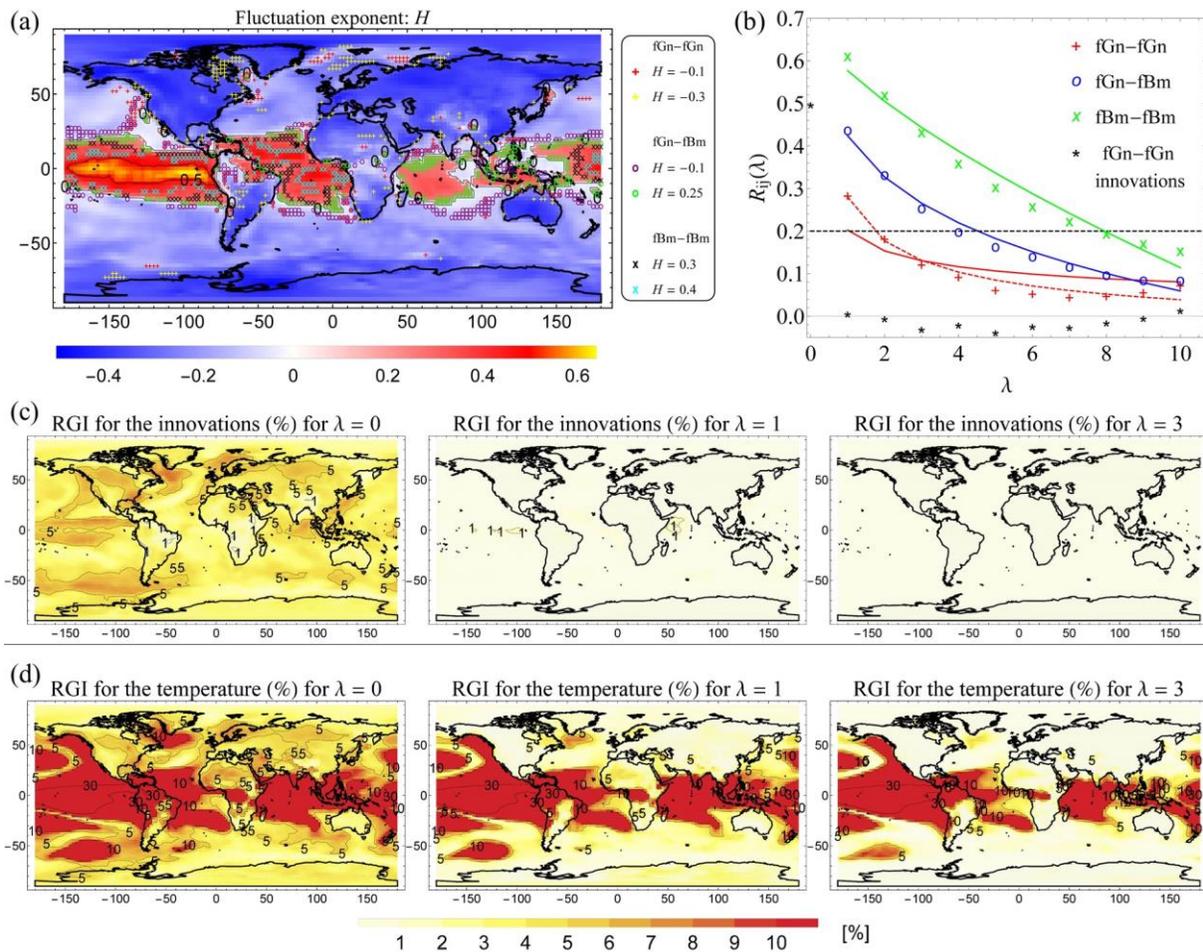


Fig. 1 (a) Maximum likelihood estimates of the fluctuation exponent, H . The grid points forming the pairs used to calculate the average ensemble cross-correlations (shown in (b)) are marked as: “+” for fGn-fGn, “o” for fGn-fBm and “x” for fBm-fBm. The colours indicate the values of H . (b) Average cross-correlations for $\lambda = 1 - 10$ for the cases 1, 2 and 3 (described in the text), with the corresponding fits from Eqs. (7-8) (we also included in dashed red the curve corresponding to higher order corrections for fRn processes). The average cross-correlations for the pairs of innovations corresponding to the series selected in Case 1 were included as reference (“*” symbol). (c) Ratio of Global Influence (RGI) for innovations for $\lambda = 0, 1$ and 3 . (d) RGI for temperature anomalies. The RGI for pixel i was defined as the fraction of the area of the planet for which the cross-correlation $|R_{ij}(\lambda)| > 0.2$ for all j .

280 approximations, there is good agreement with the empirical values. This supports the model and
 281 shows that the correlation structure has an intrinsic spatial component proportional to a_{ij} , and a
 282 temporal, memory-dependent component that depends on H_i and H_j .

283 **3.2 Ratio of global influence**

284 Empirical Orthogonal Functions (EOF) or Principal Component Analysis (PCA)
 285 decomposition techniques are often used to interpret the lagged cross-correlations (the matrices
 286 $R_{ij}(\Delta t)$, Fig. S2). This includes temperature teleconnection patterns, even though – if our model
 287 is valid – these have no Granger causality. An alternative to EOF teleconnection analysis is
 288 provided by network analysis (Donges et al., 2009a; Steinhäuser et al., 2012; Tsonis, 2018;
 289 Tsonis et al., 2006; Yamasaki et al., 2008) based on the zero lag cross-correlations that define the
 290 area weighted connectivity (AWC).

291 Since the zero-lag statistics have no causal information, we generalized the AWC to
 292 nonzero lags by defining the ratio of global influence (RGI). The RGI for pixel i is the fraction of
 293 the area of the planet for which $|R_{ij}(\lambda)| > 0.2$, averaged over all j (for innovations $|\rho_{ij}(\lambda)| >$
 294 0.2), for zero lags it is equal to the AWC. Values below 0.2 (dashed line in Fig. 1(b)) are
 295 considered to be of low influence. In climate networks, a threshold of 0.5 is typically used for
 296 defining connectivity, but innovation correlations – relevant to Granger causality – are much
 297 weaker, hence 0.2 was chosen

298 Figure 1(c) and (d) shows RGI maps for innovations and temperatures, respectively, for
 299 $\lambda = 0, 1$ and 3. For the innovations, almost all the correlation is lost for $\lambda > 0$, in agreement with
 300 Eq. (3): there is no significant influence on future values for any pixel. For $\lambda = 0$, we see that the
 301 region of largest innovation influence is the tropical Pacific where $\text{RGI} \approx 5\%$. For temperature
 302 anomalies (panel (d)), much larger correlations and RGIs are obtained. For $\lambda > 0$, almost all the
 303 influence from land disappears, but the ocean’s influence is preserved up to around 1 year (not
 304 shown). Unsurprisingly, the tropical ocean has the largest correlations. As we mentioned earlier,
 305 this is a consequence of the long memory (large H , Fig. 1(a)).

306 Rigorously, the orthogonality condition (Eq. (12)) was derived for infinitely long time
 307 series with complete knowledge of the infinite past. In practice, we only have finite series and for
 308 each pixel, the memory effects of the unknown past will depend on the H values. For a fixed,
 309 finite length of past data, series with H closer to zero have more past information that can be
 310 borrowed. In the supporting information, we confirm that there is a small improvement in skill
 311 using a co-predictor series from different locations, but this improvement decreases with the
 312 memory, m , and is very small when sufficient past data points are used to build the predictor (see
 313 Fig. S3). For 20 months of past data, forecast skill improves by a maximum of 2%, which is
 314 roughly the noise level of the skill estimates (see Fig. S6). If only a few memory-steps are used,
 315 then the improvement in skill from borrowing memory from co-predictors is larger, but in all
 316 cases the combined predictor / co-predictor skill is lower than for the single long-memory
 317 predictor (see Figs. S4 and S5).

318 **3.3 Simulations and emergent properties**

319 At each pixel, m-StocSIPS has the same statistics as StocSIPS, which DRAL showed to
 320 be quite accurate. However in addition, m-StocSIPS takes into account the spatial correlations: to

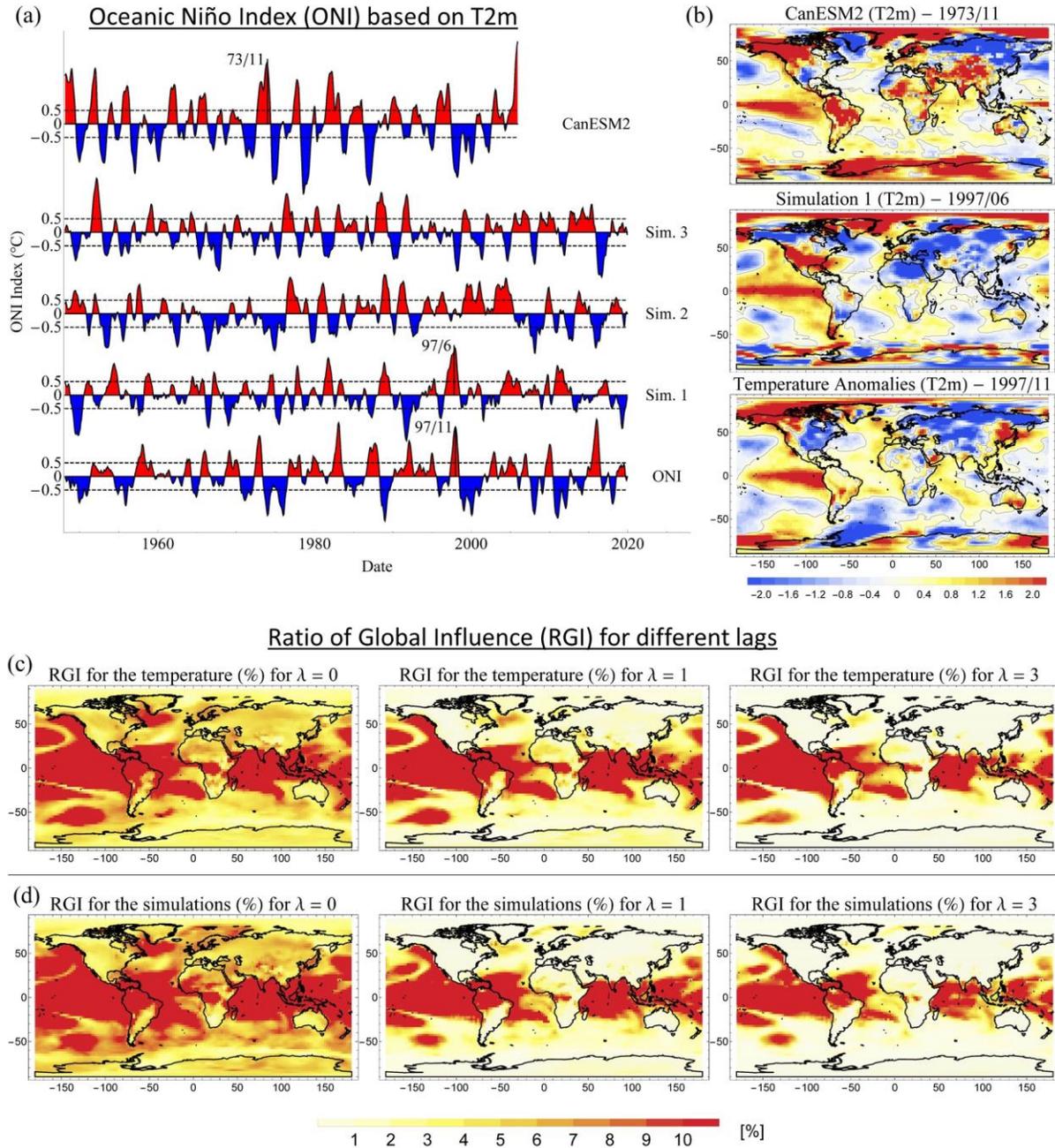


Fig. 2 (a) Comparison between series of the Oceanic Niño Index (ONI) derived for surface temperature (T2m) as the 3-month running mean of the average over the region (5°N-5°S, 170°W-120°W). In the bottom, we show the series computed from reanalysis (labelled as ONI); in the middle, samples from three different simulations (marked as Sim.1-3) and in the top, the index computed from one of the historical runs of the second generation Canadian Earth System Model (CanESM2) for the period 1948-2005. (b) Canonical anomaly pattern associated with the El Niño peaks marked in the series in Fig. 2(a) for each respective case. (c) Ratio of Global Influence (RGI) for the observational reference dataset for $\lambda = 0, 1$ and 3. (d) RGI for the Simulation 1 dataset.

321 be a realistic macroweather model it must also reproduce the observed spatial patterns including
 322 teleconnection networks (AWC, RGI), and El Niño events and indices. Since – just as in GCMs –

323 m-StocSIPS does not put these features in “by hand”, they are emergent model properties that are
 324 notoriously difficult to reproduce so that their realism (or lack thereof) provide stringent quality
 325 checks. Using m-StocSIPS simulations, (detailed in Sects. S2 and S7 of the supporting
 326 information) we now show that indeed, these emergent properties are well reproduced.

327 In order to compare StocSIPS space-time statistical structures to reanalysis and to GCM
 328 outputs, we produced simulations with the same resolutions and overall length as our reference
 329 NCEP/NCAR Reanalysis 1 dataset (864 months, 2.5° resolution). Although full movies of the
 330 model outputs are available (Movie S1), here we focus on El Niño events that are particularly
 331 difficult to simulate. First consider the Oceanic Niño Index (ONI) derived for surface
 332 temperature (T2m) as the 3-month running mean of the average over the region (5°N-5°S,
 333 170°W-120°W), Fig 2(a). The bottom (“ONI”) is a reanalysis series above which are samples
 334 from three different m-StocSIPS realizations (“Sim.1-3”, middle). The top series is from a
 335 historical run of the CanESM2 GCM (CCCma, 2020), the ONI was estimated after standard
 336 detrending (but without variance adjustments).

337 Except for the larger GCM amplitude, the time series in Fig. 2(a) are difficult to
 338 distinguish. Both deterministic and stochastic simulations produce realistic-looking ONI
 339 anomalies sequences. More impressively, the stochastic simulations reproduce huge regional
 340 emergent patterns including El Niño and La Niña events. In Fig. 2(b), we see canonical El Niño
 341 anomaly patterns corresponding to El Niño peaks marked in Fig. 2(a) (see also Fig. S11 for map
 342 sequences). While the deterministic models explain these events as an expression of the
 343 dynamics implicit in the governing equations, in the stochastic model they emerge from random
 344 synchronizations from places sharing high H values (see Fig. 1(a)) and long ocean weather-
 345 macroweather transition times.

346 StocSIPS also produces realistic and emergent teleconnections patterns: RGI maps, see
 347 Fig. 2(c) and (d) for lags $\lambda = 0, 1$ and 3. Despite these striking spatial patterns, there is no
 348 Granger causality connecting any two points: the optimal predictor is obtained from the past of
 349 each individual series without any contribution from the teleconnection patterns. These
 350 correlations do not imply any Granger causality.

351 4 Conclusions

352 GCMs long range forecasting skill is low, and this has stimulated the development of
 353 stochastic alternatives often inspired by correlations. Two competing approaches have
 354 developed, one that primarily exploits teleconnections (space) with only a short memory in time
 355 (Markovian), the other – StocSIPS – that only exploits the long memory in time without using
 356 any spatial information. While Markovian models are approximately initial value problems
 357 GCMs are strictly so. In comparison, StocSIPS exploits the system’s (scaling) long range
 358 memory; it is a “past value” model. Although it is tempting to try to improve StocSIPS skill by
 359 using spatially correlated co-predictors, to be useful the correlations must also be causal.

360 Untangling correlations and causality is possible thanks to the precise notion of Granger
 361 causality. To apply this, we first extended StocSIPS to the full space-time process, m-StocSIPS,
 362 that has identical single pixel statistics but that includes pixel-pixel cross-correlations. Although
 363 m-StocSIPS’s time-lagged temperature cross-correlations are strong, they are generated by
 364 temporally uncorrelated innovations and it has no Granger causality. For a given position, past
 365 information from other locations cannot be used to improve on the forecast obtained as an

366 optimal linear combination of past data: those correlations “were already used”. Whereas the
 367 ultimate causation in deterministic models is their initial conditions, the ultimate cause in
 368 StocSIPS is its white noise innovations.

369 To make this convincing, we provided a full space-time macroweather model, producing
 370 global space-time stochastic simulations at one month and 2.5° resolution over 864 months
 371 (Movie S1). Emergent model properties include realistic teleconnection networks and El Niño
 372 and La Niña events that have both realistic spatial warming patterns as well as Oceanic El Niño
 373 indices. For real data, only a finite length of the past series is known, but even in this case, we
 374 showed that by exploiting the correlations in the temperature series, maximum improvements in
 375 skill of only 1-2% are possible (and this is in the noise).

376 What then is the status of causal mechanisms such as those linking El Niño events to a
 377 wet central Asia (Barnston, 2014)? GCMs and StocSIPS provide ultimate causes that eschew
 378 such mechanisms. At best, it may be argued that ultimate causes initiate a causal chain in which
 379 an El Niño could be regarded as a proximate cause, and this proximate cause could presumably
 380 be captured in short memory empirical models. However, thanks to Granger causality we can
 381 now affirm that at best, at a given pixel i , the short memory models (partially) compensate for
 382 their under-exploitation of the memory by effectively “borrowing” the memory of particularly
 383 strong memory pixels j such as those in the El Niño region. StocSIPS obviates the need to
 384 borrow memory from pixel j by fully exploiting the memory at pixel i .

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 389 references: (CCCma, 2020; NCEP/NCAR, 2020)

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