

## 1. ABSTRACT

- We investigated the occurrence of large aftershocks following the most significant earthquakes that occurred in **North-eastern Italy** and **Western Slovenia**.
- Clusters are defined as “**type A**” if, given a main shock of magnitude  $M_m$ , the **subsequent strongest earthquake** in the cluster has **magnitude  $M_a \geq M_m - 1$** ; of type B otherwise.
- We used an improved version of a pattern recognition method developed by **Gentili and Di Giovambattista 2017** for medium-high seismicity in Italy.
- In particular, we investigated the **radiated energy** and the **the spatio-temporal evolution of the aftershocks** occurring within a few days and the probability to have a strong earthquake depending on the time elapsed after the mainshock.
- In order to characterize the feature depending on the cluster type, we used **decision trees** as classifiers on single feature separately. The **performances** of the classification are tested by **leave-one-out method**.
- The **analysis** was performed on **different time-spans** after the mainshock to simulate the increase of information available as time passes during the seismic clusters.
- The method has been **successfully applied** to the **1976 Friuli cluster**, in which a swarm of large earthquakes happened 4 months after the first mainshock and on two small cluster this year in the same area

## 2. DATABASE

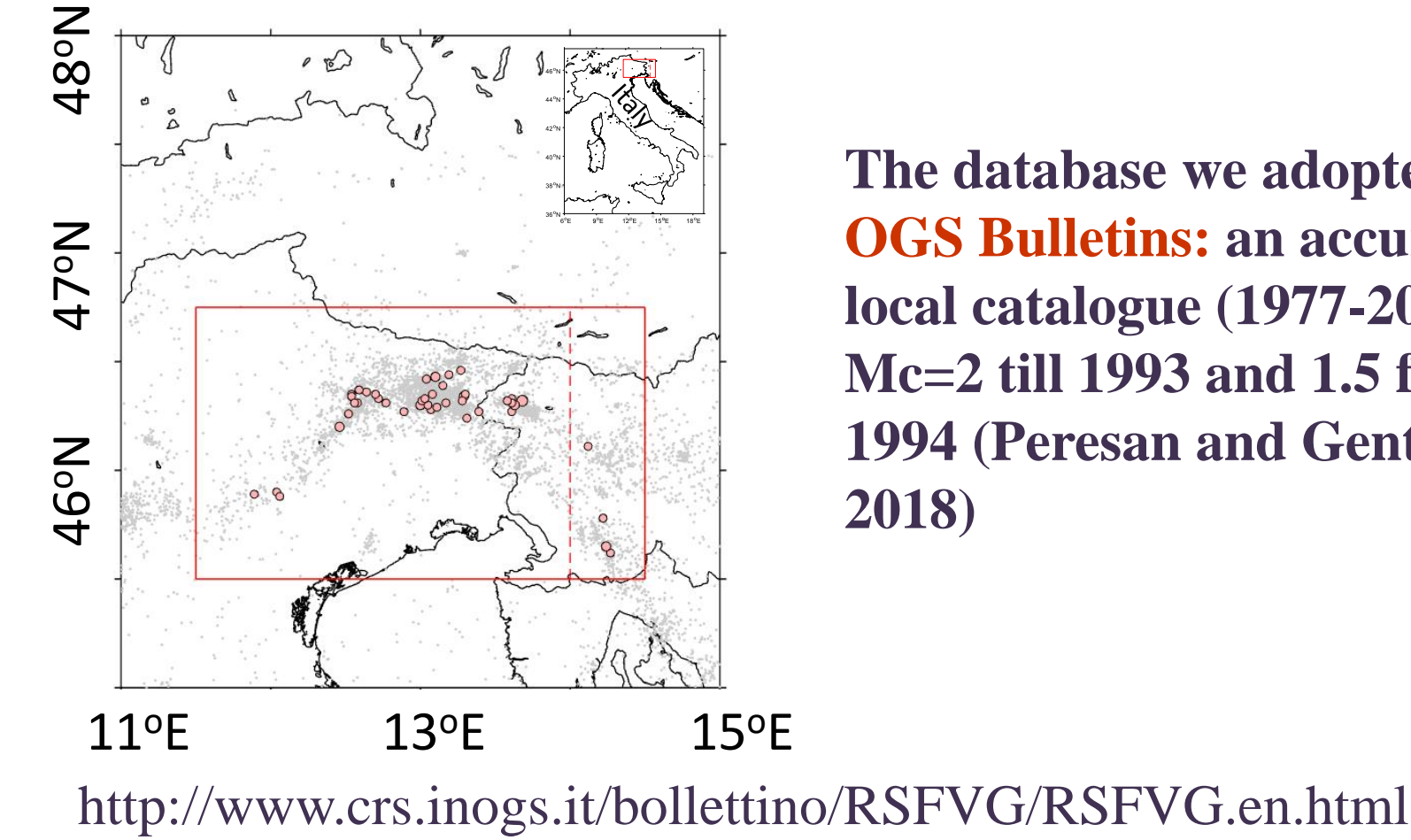


Fig. 1: Selected area (before and after 2008) and clusters' epicenters (42 clusters)

- The area of sufficient completeness is detected based on the **ratio R** ( $R > 0.8$ ) between the **number of ISC earthquakes that have an equivalent** in OGS catalogue and the **total number of earthquakes** in ISC catalogue (Kossobokov et al. 1999, Peresan and Gentili, 2018).

- From 2008, the area could be **extended 0.5 degrees eastward** thanks to the collaboration with ARSO (Environmental Agency of the Republic of Slovenia)

## 3. CLUSTER IDENTIFICATION

- Clusters were selected by a **windowing algorithm** for the radius ( $\rho$ ) and its duration ( $\tau$ ) identification. In this work the “**mainshock**” is the first event with  $M \geq 3.7$  in a cluster and “**aftershocks**” are the following events. **42 clusters were detected**.

$$\rho = 10^{0.41M_m - 1} + 2$$

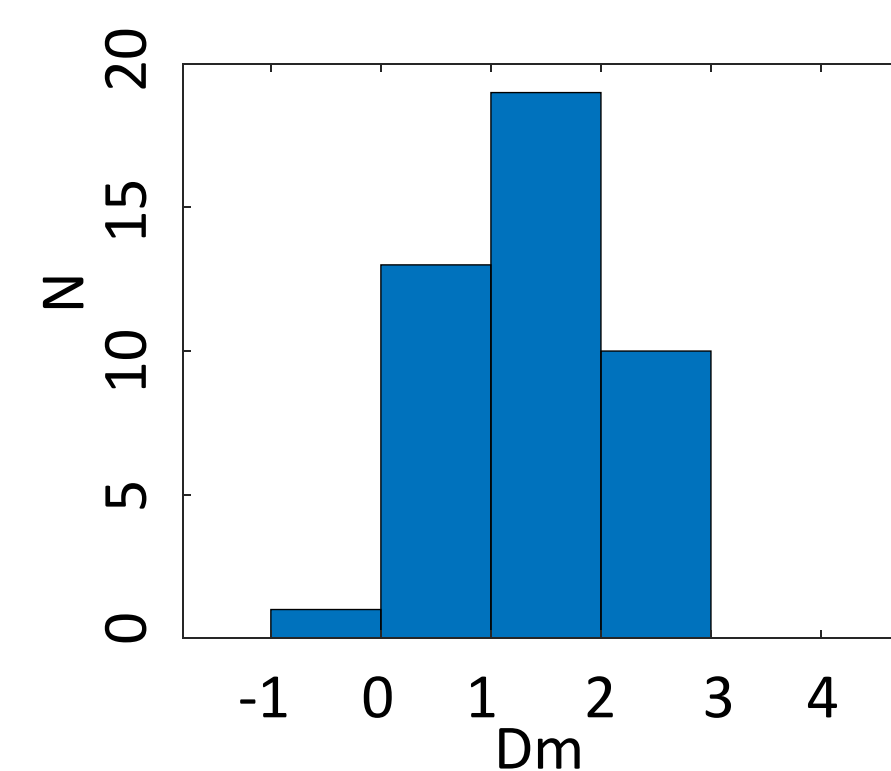
$$\tau = 10^{0.33M_m + 0.42}$$

Gentili and Bressan (2008) + 2 km

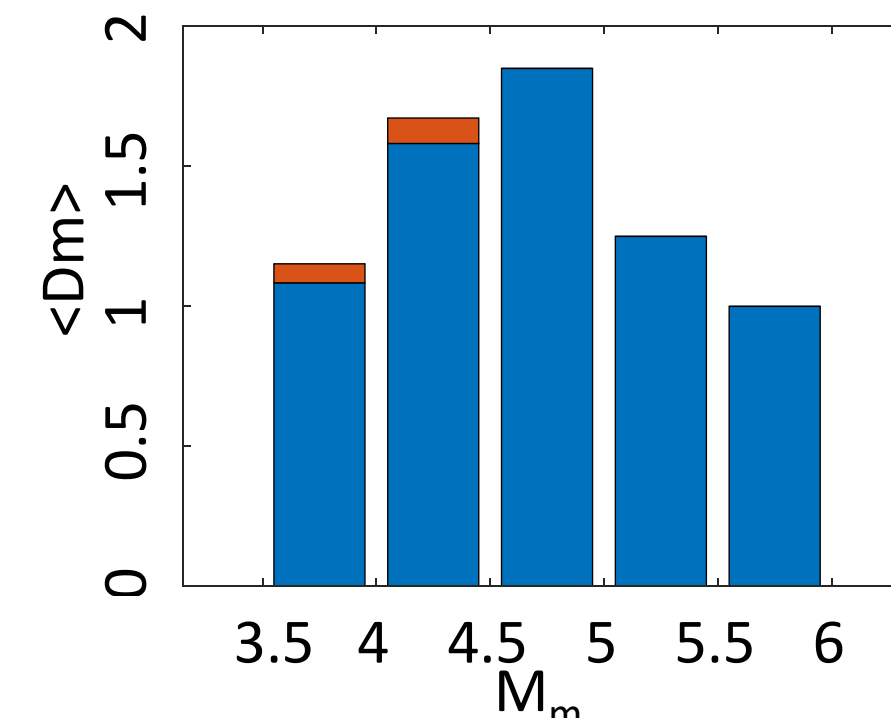
- If after the “mainshock” **another event with magnitude  $\geq M_m - 1$  occurs**, the cluster is labeled as being of type “**A**”; **otherwise** it is considered of type “**B**” (Vorobieva 1999).

Fig. 3: Percentage (Perc) of clusters that have had the strongest aftershock. Red=A, Blue=B, black=all.

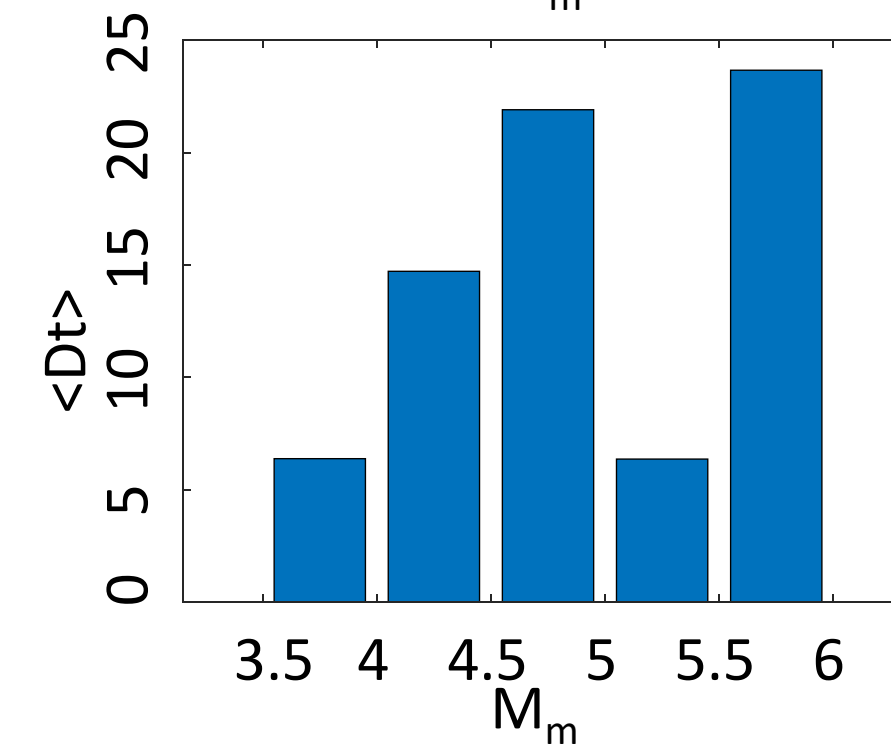
## 4. RESULTS: CLUSTERS' CHARACTERISTICS



Mean  $D_m$  1.3-1.4 in good agreement with **Båth law** (Båth, 1965).



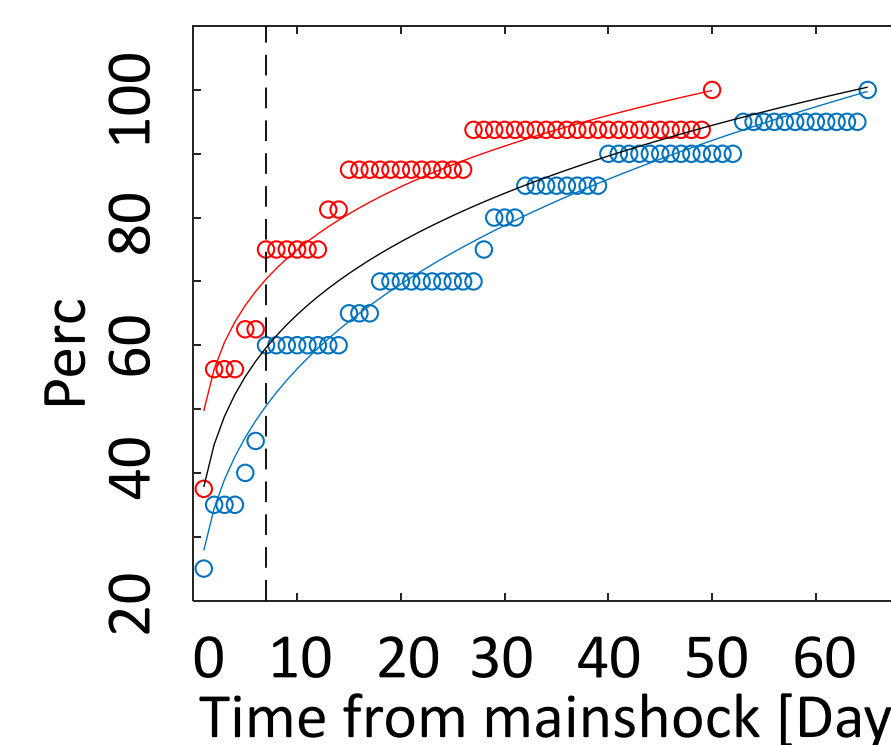
For  $M_m > 5$   $D_m$  **decreases** (orange: uncertainty when  $M_a < M_c$ ).



$D_t$  **generally increases** with  $M_m$

Fig. 2: Clusters' characteristics:  $D_m = M_m - M_a$ ;  $D_t = t_a - t_m$  ([Days]); <.> mean of .; a=strongest aftershock

**Hp: larger earthquakes activate more complex tectonic structures => the probability to have a subsequent strong event and a longer interval between the mainshock and the strong event is higher.**



	$\gamma$	$\lambda$
All data	0.234±0.003	37.8±0.3
A data	0.178±0.005	49.7±0.7
B data	0.306±0.004	27.9±0.6

## 5. PATTERN RECOGNITION APPROACH

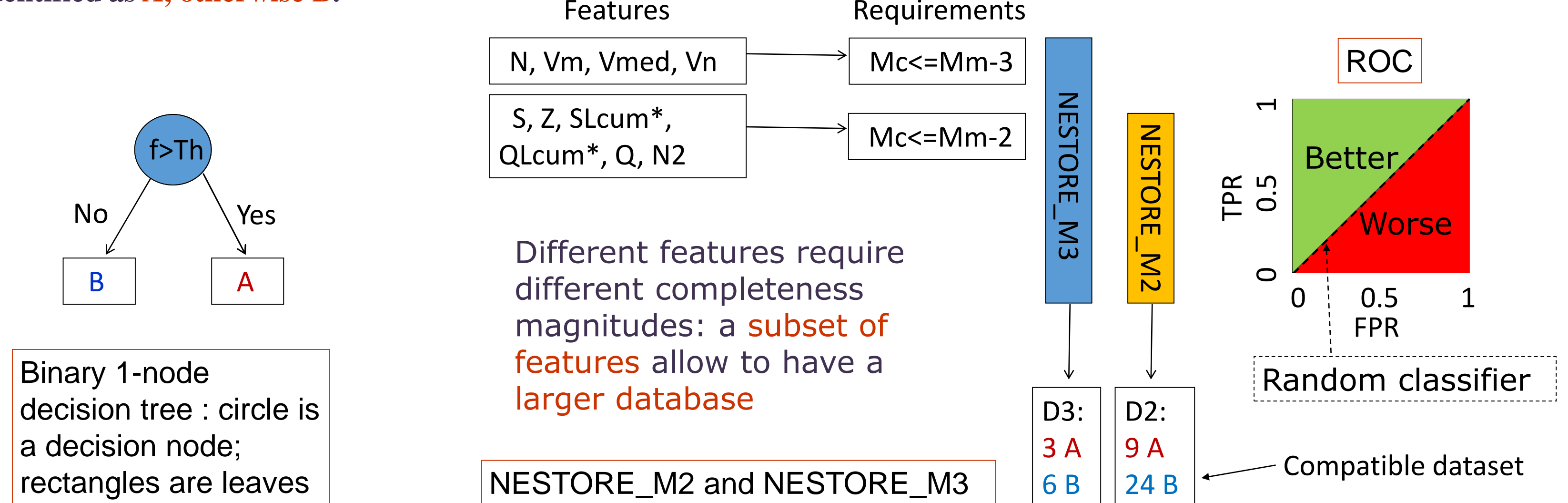
- NESTORE – (NExt STrOng Related Earthquake)** is a software package for A clusters forecasting based on **pattern recognition** approach. It analyses the seismic data at increasing time intervals  $T$  after the mainshock.

- Tested features:

- N**, **N2**=number of aftershocks (with magnitude  $M_m - 2$  and  $M_m - 1$ , respectively)
- S**=total equivalent source area
- Q**=cumulative radiated energy
- Vm**=variation of magnitude from event to event
- Vmed**=variation of average magnitude from day to day
- Vn**=variation of the number of aftershocks from day to day
- Z**=linear concentration of aftershock
- SLcum**, **SLcum2**=deviation of S from the long term trend (SLcum2 with sliding window)
- QLcum**, **QLcum2**=deviation of Q from the long term trend (QLcum2 with sliding window)

- Accordingly with Gentili and Di Giovambattista (2017), **each feature** has been evaluated by a pattern recognition approach using an **independent decision tree** (Jang et al., 1997).

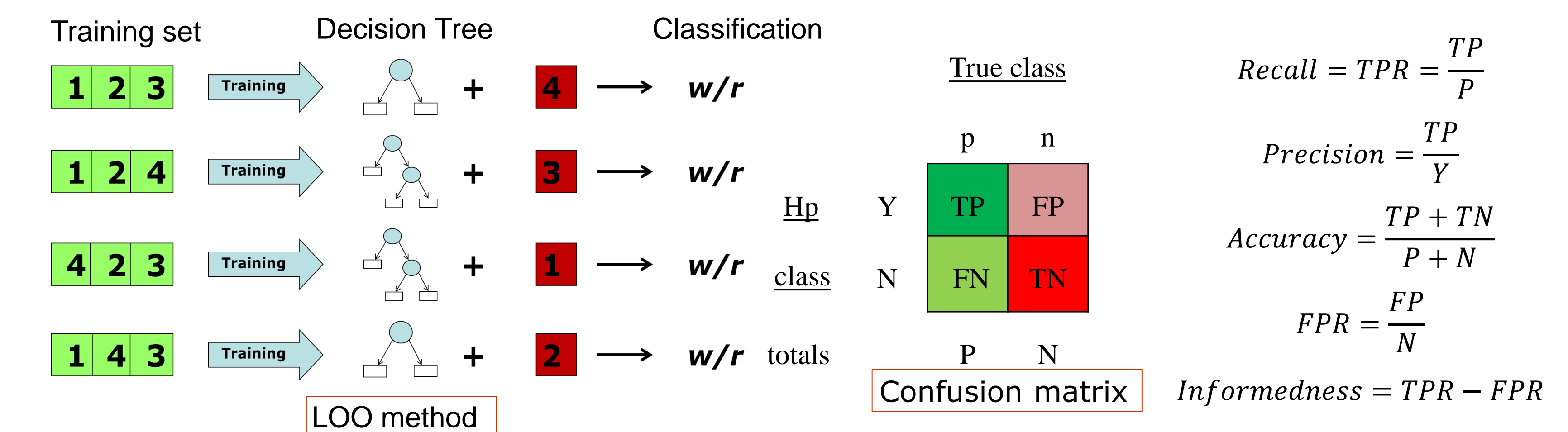
- A **one-node decision tree** is trained: the algorithm identifies for each feature  $f$  a threshold  $Th$  so that if  $f \geq Th$  the cluster is identified as **A**, **otherwise B**.



- Using  **$Mc \leq M_m - 3$**  the number of clusters that can be analyzed is **low** => we developed **NESTORE\_M2**
- In order to compare precursors performances we selected 6 different time periods (in days: **[0, 0.25] [0, 0.5] [0, 0.75] [0, 1], [0, 2], [0, 3]**) and for each time period we calculated the values of all the tested precursors.

- We checked the performances by the **LeaveOneOut (or LOO)** method: each learning set is created by taking **all the samples except one**, the **test set** being **the sample left out**. The procedure is **repeated for all the samples**

- The test allowed to obtain the **confusion matrix** and derived information like **ROC diagrams** ( $A = p$ ;  $B = n$ ).

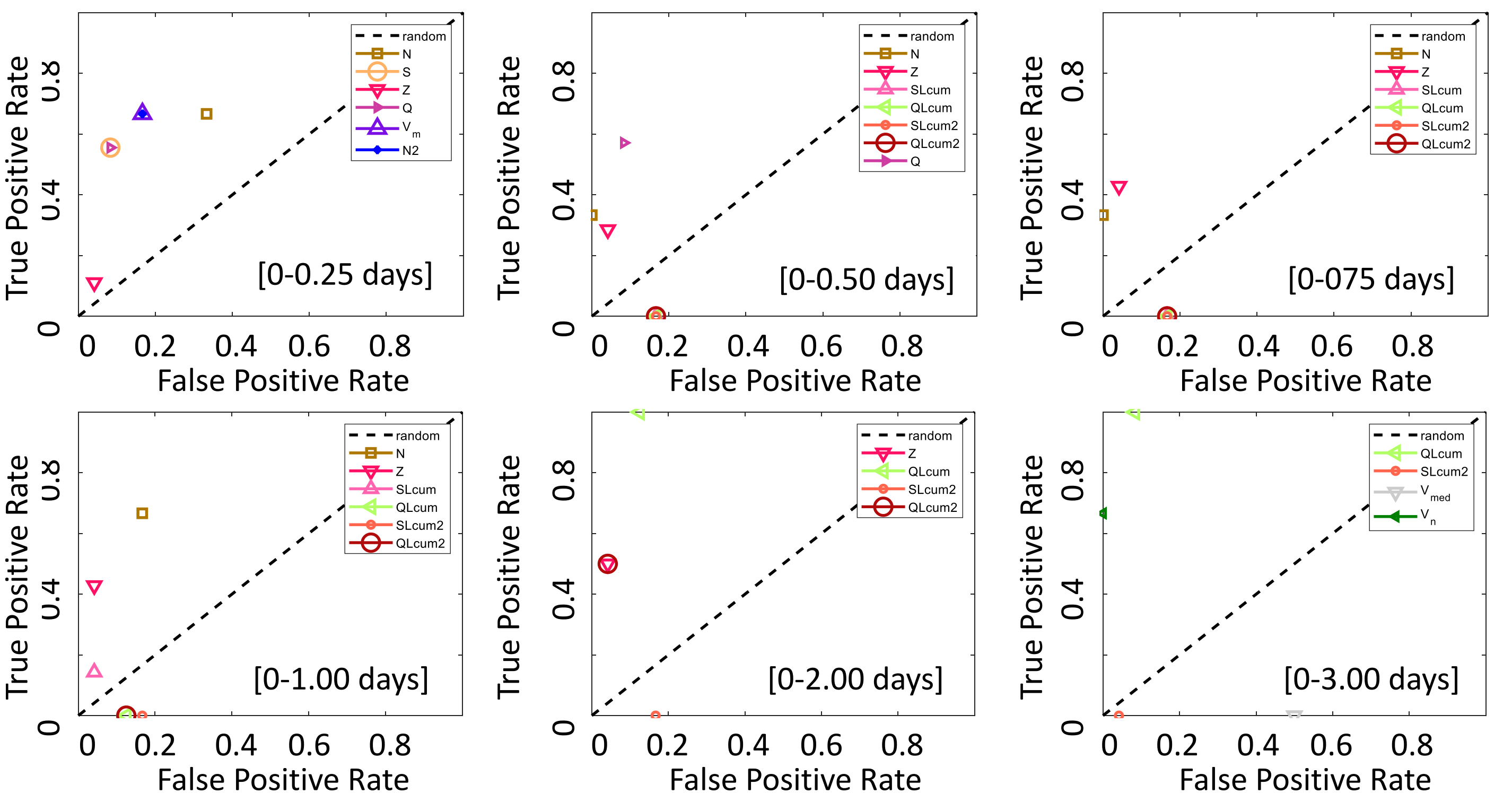
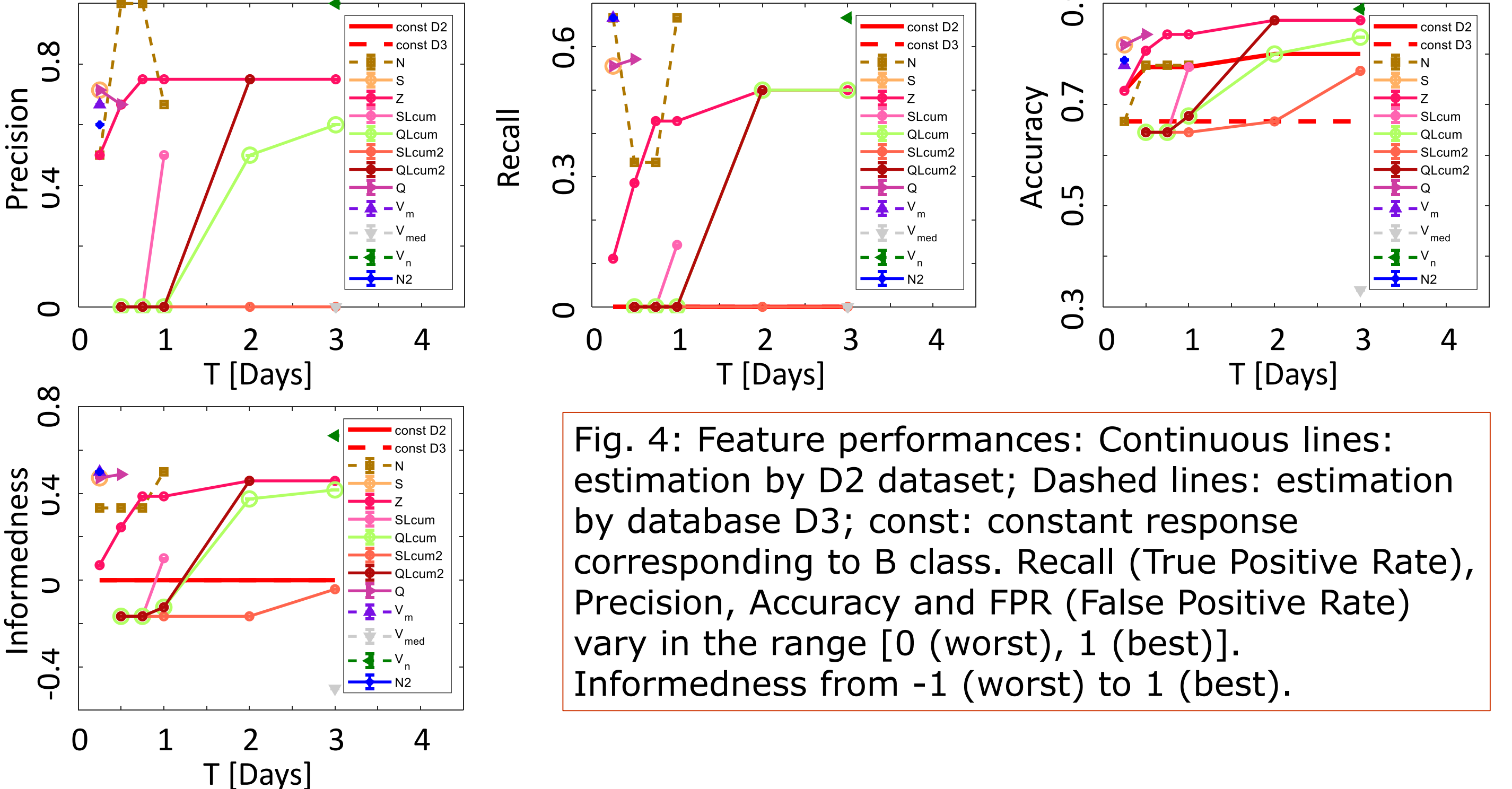


- NESTORE method trains a set of classifiers based on independent features. The different classification results need to be combined in a unique classification “Probability of Class A”. We used a **Bayesian approach** (Bailer-Jones et al. 2011):

$$P(A|D_1 \dots D_N) = \frac{[N(B)]^{N-1} \prod_{n=1}^N p_n}{[N(B)]^{N-1} \prod_{n=1}^N p_n + [N(A)]^{N-1} \prod_{n=1}^N (1 - p_n)}$$

$p_n = P(A|D_n)$  is the probability to have A cluster given a value  $D_n$  of the  $n$  feature,  $N(A)$ ,  $N(B)$ : number of A, B, N: number of classes.

## 6. RESULTS: PATTERN RECOGNITION; SINGLE FEATURES



## 7. RESULTS: PROB(A) FORECASTING ON INDEPENDENT DATA

