

1 **Two Different Pathways toward Convective Self-aggregation in Radiative-**
2 **convective Equilibrium Simulations between SCALE and VVM**

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11

12 **Key points:**

13 ● Under the same SST, convective self-aggregation develops differently: gradual transition
14 in SCALE and fast growth in VVM.

15 ● Radiative cooling dominates convective self-aggregation developing in SCALE, while
16 convection efficiently drives the circulation in VVM.

17 ● The different pathways to convective self-aggregation in SCALE and VVM are associated
18 with the transition to large-size convective systems.

19

20 **Abstract**

21 Two cloud-resolving models (SCALE and VVM) take different pathways toward
22 convective self-aggregation (CSA) in the radiative-convective equilibrium simulations,
23 although they have similar domain-averaged properties. Analyses in the moisture space show
24 that radiative cooling in the dry area mainly drives CSA in SCALE, while subsidence triggered
25 by the convection in the moist region dominates in VVM. The change in the convective
26 structures is found on the isentropic diagram in VVM, but this transition is unclear in SCALE.
27 The object-based analysis provides that the convective systems with larger sizes are rare in
28 SCALE. In contrast, large-size convective systems frequently develop in the moist region as
29 CSA evolves in VVM. The large-size systems can efficiently drive the circulation between the
30 dry and moist areas. The different pathways to CSA are associated with the transition of
31 convective structures, which provides a new insight to understand CSA among cloud-resolving
32 models based on the perspective of the mechanism.

33 **Plain Language Summary**

34 A variety of deep convective clouds is found in the tropics, and they sometimes form
35 clusters. Previous studies have found that the mechanisms for the onset of the clustered
36 convection are very different in warmer and colder sea surface temperature conditions in
37 idealized numerical experiments. We discover that the mechanisms can be different among the
38 two models even though the sea surface temperature is the same. The clustering in one model
39 is driven by the radiative processes in the region without convection. In the other model, the
40 clustering is controlled by circulation from the region with larger convective clouds. This study
41 shows that the different mechanisms for the onset of the clustered convection are related to the
42 structures of convective clouds among models. This result improves our understanding of the
43 clustered convection in the models.

44

45 **1 Introduction**

46 Radiative convective equilibrium (RCE) is known as a conceptual model for
47 understanding tropical climate (Manabe and Strickler, 1964). In this model, moist convection
48 is essential to balance the radiative cooling and the surface warming to reach an equilibrium
49 climate state with a statically stable thermodynamic structure. This concept has been applied
50 using cloud-resolving models (CRMs), and the models reach equilibrium states with smaller
51 convective regions surrounded by larger and wider dry subsiding regions, which is called
52 convective self-aggregation (CSA; Nakajima and Matsuno, 1988; Held et al., 1993; Tompkins
53 and Craig, 1998; Bretherton et al., 2005; Muller and Held, 2012; Wing and Emanuel, 2014;
54 Yanase and Takemi, 2018). CSA changes the energy balance of the atmospheric column and
55 then leads to the impact on climate sensitivity (Mauritsen and Stevens, 2015; Holloway et al.,
56 2017; Wing, 2019). Wing et al. (2018, 2020) organized the RCE Model Intercomparison Project
57 (RCEMIP) to investigate the role of clouds and CSA in the climate sensitivity. Even though
58 CRMs are forced by the same sea surface temperature (SST), large differences in the vertical
59 structures of temperature, humidity, and cloudiness are found across the RCEMIP ensemble of
60 CRMs. These CRMs also exhibit discrepancies in the degree of CSA and its dependency on
61 SST. It is difficult to identify a specific process that causes the spread results in the RCEMIP
62 ensemble because these models are treated with different dynamics and physics.

63

64 Coppin and Bony (2015) showed that the leading mechanism for CSA varies with SST
65 using an atmospheric general circulation model. At low SST, the radiative cooling due to low
66 clouds in dry areas drives large-scale subsidence, which is called a radiative-driven cold pool.
67 The expansion of the radiative-driven cold pool forces convection to aggregate in the regions
68 with weak subsidence, and this mechanism mainly contributes to CSA under the cold SST
69 conditions. On the other hand, at high SST, deep convection develops and then induces strong

70 surface wind, which leads to enhanced surface enthalpy flux in the adjacent region. The
71 enhanced surface flux will favor the subsequent development of deep convection in similar
72 areas, and this feedback controls the development of CSA under high SST conditions. The idea
73 of different mechanisms provides a hint that the main process of maintaining CSA could be
74 distinct among CRMs, which causes the different sensitivities to the changing SST in the
75 RCEMIP ensemble.

76

77 This study investigates the crucial mechanism leading to CSA using two CRMs, and
78 the experimental setups follow the RCEMIP protocol (Wing et al., 2018), except for the domain
79 size. The equilibrium state with CSA is obtained in the simulations with a medium domain size
80 to reduce computational cost. We analyze the results in the moisture space to evaluate the
81 differences in the equilibrium state. The isentropic analysis (Pauluis and Mrowiec, 2013) and
82 the object-based analysis method are applied to examine the time evolution of the convective
83 structures as CSA develops. Section 2 describes the two models and the experimental setup.
84 Section 3 presents the differences in the equilibrium states, the mechanism for CSA, and the
85 convective structures between two CRMs. The summary and discussion are in section 4.

86

87 **2 Models and Experiment Design**

88 2.1 Model description

89 2.2.1 SCALE

90 The first atmospheric model used in this study is a regional model constructed with
91 Scalable Computing for Advanced Library and Environment (SCALE, Version 5.3.6;
92 Nishizawa et al., 2015; Sato et al., 2015). The model is governed by the three-dimensional fully
93 compressible non-hydrostatic equations, which predicts the three-dimensional momentum (ρu ,
94 ρv , and ρw), total density (ρ), mass-weighted potential temperature ($\rho\theta$), and mass
95 concentration of tracers (ρq_s). The θ here is not the conventional potential temperature for dry
96 air, but the corresponding value for total air, considering water content. A six-class single-
97 moment bulk-type microphysics scheme is used in this study (Tomita, 2008). The subgrid-scale
98 turbulent process is parameterized through the Smagorinsky-Lilly type first-order closure
99 scheme (Brown et al., 1994; Scotti et al., 1993), and surface fluxes are calculated by a bulk
100 method using a universal function (Beljaars and Holtslag, 1991; Wilson, 2001). The radiative
101 processes are treated with a k-distribution-based broadband radiation transfer model (Mstrn-X,
102 Sekiguchi and Nakajima, 2008). SCALE has been used in studying the impacts of cloud
103 microphysics on convection (Sato et al., 2015, 2018), data assimilation (Honda et al., 2018,
104 2019), regional climate changes (Adachi et al., 2019), severe weather events (Yoshida et al.,
105 2019), the parameterization of physical processes (Iwabuchi and Okamura, 2017; Nishizawa
106 et al., 2018), and dynamical downscaling of blowing snow events (Tanji et al., 2019; Inatsu et
107 al., 2020).

108

109 2.2.2 VVM

110 The other model used in this study is the vector vorticity equation cloud-resolving
111 model (VVM) developed by Jung and Arakawa (2008). Horizontal components of anelastic

112 vorticity equations are predicted in the VVM, and velocities are diagnosed through solving a
113 three-dimensional elliptic equation. The use of the vorticity equations eliminates pressure
114 gradient force and inherently links the dynamics and the thermodynamics in the governing
115 equations. The direct couple in the equations can better capture local circulations associated
116 with strong thermal gradients, such as the land-sea breeze. Radiative fluxes are calculated by a
117 radiative transfer model using the correlated-k approach (Iacono et al., 2008), surface fluxes
118 are treated by the Monin-Obukhov similarity theory (Chen and Dudhia, 2001), microphysical
119 processes are parameterized by the two-moment bulk scheme that predicts properties of ice
120 particles (Morrison and Milbrandt, 2015; Huang and Wu, 2020), and the effects of the
121 topography are represented by the immersed boundary method in the VVM (Wu and Arakawa,
122 2011; Chien and Wu, 2016). VVM has been applied in many studies, such as unified
123 parameterization (Arakawa and Wu, 2013; Wu and Arakawa, 2014), stratocumulus dynamics
124 (Tsai and Wu, 2016), afternoon thunderstorms (Kuo and Wu, 2019), impacts of land surface
125 heterogeneity (Wu et al., 2019; Wu and Chen, 2021), cloud-aerosol interactions (Chang et al.,
126 2021), coastal convection during summer monsoon onset (Chen et al., 2019), and the
127 aggregated convection (Tsai and Wu, 2017; Chen and Wu, 2019).

128

129 2.2 Experiment design

130 VVM and SCALE used their own default physics settings with the same experimental
131 settings, such as solar insolation and greenhouse gas profiles, following the RCEMIP protocol
132 (Wing et al., 2018). The simulations are initialized from an analytically approximated sounding
133 of the moist tropics (Dunion, 2011) and integrated with a fixed SST of 300 K for 50 days with
134 hourly data outputs. Yanase et al. (2020) investigated and suggested that 384 km is the
135 minimum size for CSA in SCALE with the 2-km resolution. The domain size of 384×384 km²
136 with a 2-km horizontal resolution is used to have minimal costs for CSA.

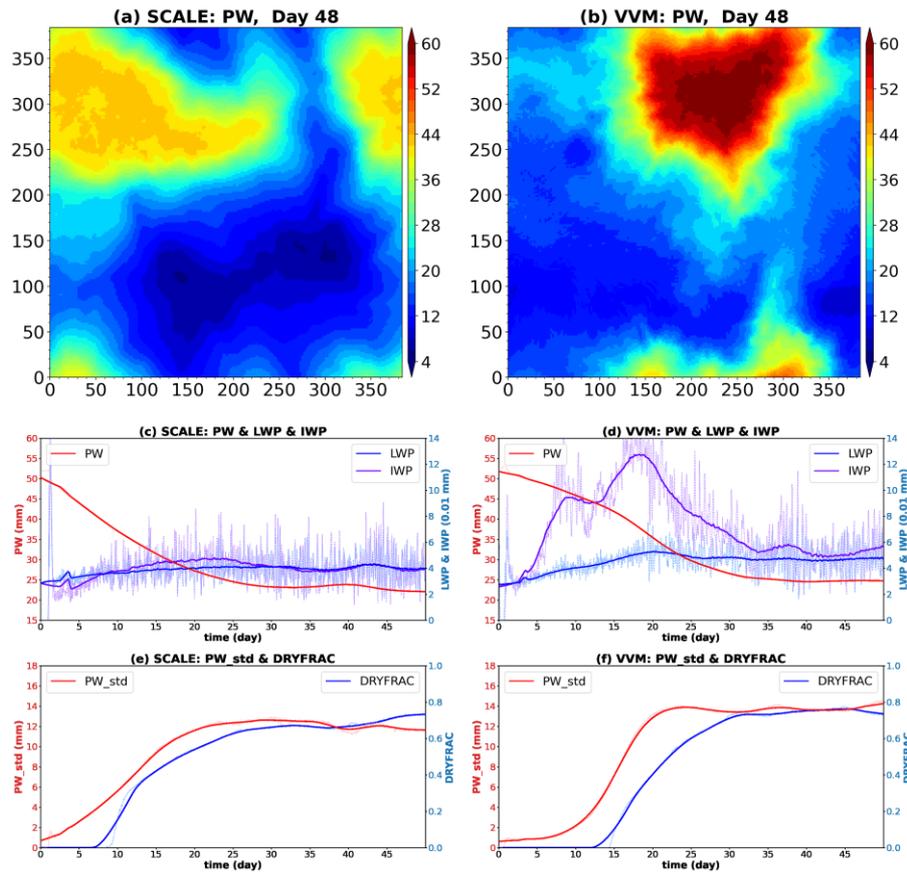
138 **3 Result**

Fig. 1. The horizontal distribution of daily averaged PW on day 48 for SCALE (a) and VVM (b). The time evolutions of domain-averaged precipitable water (PW), liquid water path (LWP), and ice water path (IWP) for SCALE (c) and VVM (d). The time series of the standard deviation of PW (PW_std) and the dry area fraction (DRYFRAC) for SCALE (e) and VVM (f). The solid lines represent the 5-day moving averages of each variable, and the dashed lines are shown without the temporal smoothing.

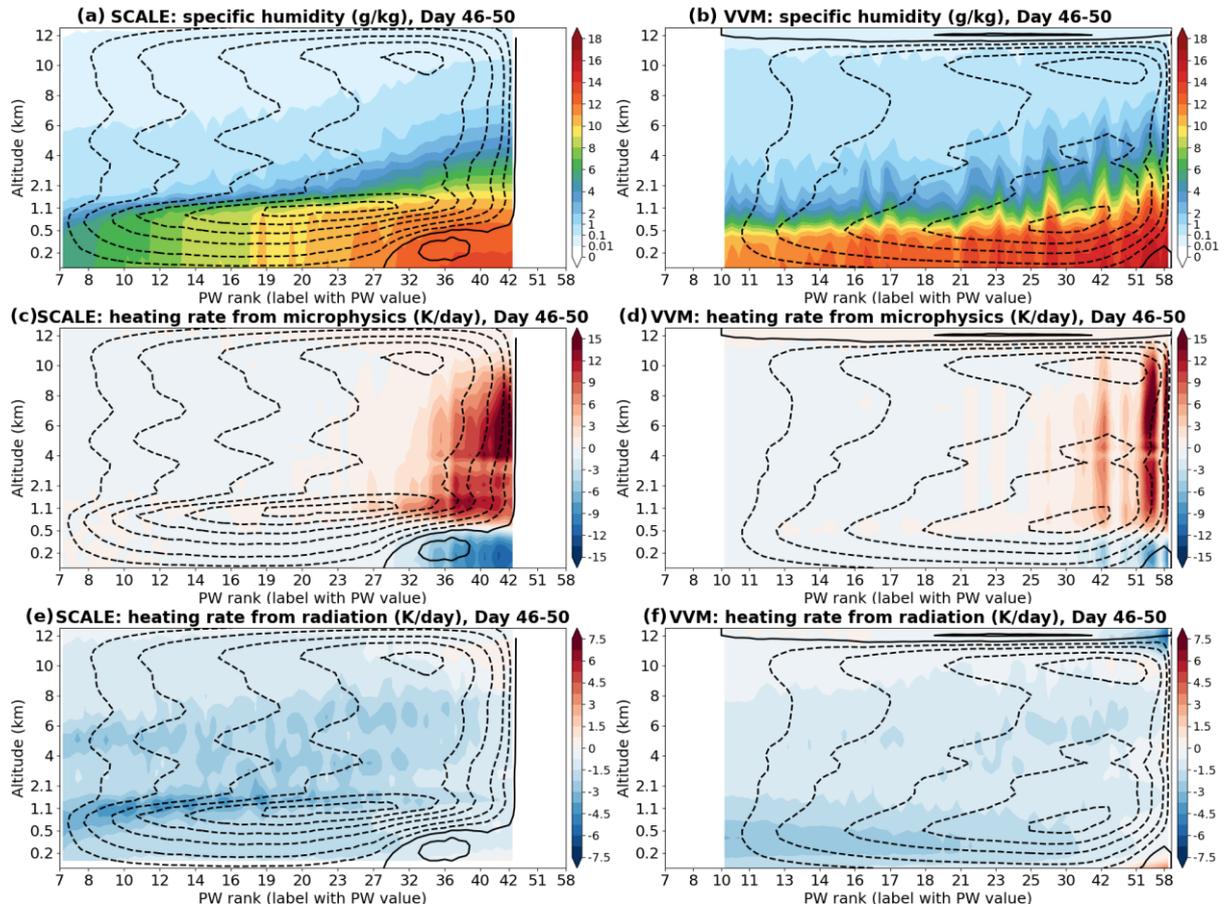
139 **3.1 Overall behaviors of two models**

140 The occurrence of CSA can be visualized by the spatial distribution of daily averaged
 141 precipitable water (PW) on day 48 in SCALE (Fig. 1a) and VVM (Fig. 1b). A clear structure
 142 that a moist region surrounded by the dry area can be seen in both models. PW in the moist
 143 region reaches 56 mm in VVM, which is significantly greater than that in SCALE (42 mm).

144 PW in both models is similar in the dry areas, but PW in some small regions is less than 10
145 mm in SCALE. We used several variables to quantify the differences in the evolutions of CSA
146 (Fig. 1c and 1d). The domain average of PW declines as the time proceeds in both models, and
147 they reach a quasi-steady state after day 40 with the mean PW of 25 mm. Throughout the
148 transition toward CSA, the liquid water path (LWP) similarly evolves in both models, but the
149 evolution of the ice water path (IWP) is different between SCALE and VVM. IWP in VVM
150 significantly increases before day 20 and then settles to equilibrium, while a smaller temporal
151 variation of IWP is found in SCALE. The difference in IWP suggests that VVM undergoes a
152 drastic transition of cloud structures during the development of CSA.

153

154 We apply the dry fraction and the standard deviation of PW to identify the differences
155 in the degree of CSA between SCALE and VVM (Fig. 1e and 1f). The dry fraction (DRYFRAC)
156 is defined as the fraction of areas where precipitable water is lower than 30 mm (Yanase et al.
157 2020). DRYFRAC of SCALE starts its increase at day 8, while DRYFRAC of VVM starts
158 increasing at day 13. DRYFRAC in both models reaches 0.7 in the quasi-equilibrium states.
159 DRYFRAC in SCALE gradually grows from 0.6 at day 25 to 0.7 at day 44, while it in VVM
160 reaches 0.7 at day 30 and remains a quasi-steady state. On the other hand, the standard deviation
161 of PW (PW_{std}) shows evident differences in the degree of CSA in both the developing stage
162 and quasi-equilibrium state. In SCALE, PW_{std} linearly increases before day 20 and then
163 remains the quasi-equilibrium state with 12 mm PW_{std} . In VVM, PW_{std} exponentially grows
164 in the first twenty days, and the sharp growth in days 10-20 accompanies the significant change
165 in IWP. In the quasi-equilibrium state, PW_{std} of VVM is 2 mm greater than that of SCALE,
166 which suggests that CSA in VVM would be more aggregated. These results show that the
167 development of CSA is gradual in SCALE, while the quick transition in VVM could be related
168 to the drastic changes in the cloud structures.



169

Fig. 2. The vertical profiles of specific humidity (a, b), microphysical latent heating rate (c, d), radiative heating rate (e, f) are ranked by precipitable water with the same sample size in each rank for SCALE (left) and VVM (right) in days 46-50 (Note that the PW range is different for SCALE and VVM). Contours show the streamfunction with intervals of $0.05 \text{ kg m}^{-2} \text{ s}^{-1}$, and the contours of -0.02 and $0.02 \text{ kg m}^{-2} \text{ s}^{-1}$ are added to show subsidence in the drier region and clockwise circulation in the moister region, respectively. The solid and dash lines, respectively, represent clockwise and counterclockwise circulations in the moisture space.

170 3.2 CSA in the moisture space

171 The characteristics of CSA in the quasi-equilibrium state are evaluated by the vertical
 172 profiles ranked by PW following Bretherton et al. (2005). Fig 2a and 2b show that
 173 counterclockwise circulations in the moisture space are evident in both models with a narrower

174 upward branch in the moister region (over 36 mm for SCALE and over 51 mm for VVM) and
175 wider subsidence in the drier region (7-23 mm in SCALE and 10-25 mm for VVM). The overall
176 range of PW in VVM is moister compared to that in SCALE. Even though atmospheric
177 columns have the same PW in the two models, the values of water vapor mixing ratio in both
178 boundary layer and free atmosphere are smaller in SCALE. Another notable difference in the
179 circulations in the dry areas is that the counterclockwise circulations of SCALE are stronger
180 and have a gap at the top of the boundary layer, while the boundary layer circulation of VVM
181 is weaker and more smoothly connected with the free-atmospheric circulation. Besides, the
182 ascending branch of the circulation is confined in the moister 10 % region in VVM, while that
183 in SCALE has a wider upward motion region in the moisture space. The moisture space
184 analyses show that the structures of moisture and circulation are quite different even though
185 CSA occurs with similar domain-averaged quantities.

186

187 We compare the latent and radiative heating to investigate the mechanisms for the
188 different characteristics of CSA observed in the moisture space. In both models, the condensate
189 heating is consistent with their ascending branch of the circulation in the moisture space (Fig.
190 2c and 2d). There are large differences in the dry areas between the two models. Fig. 2e and 2f
191 show that the radiative cooling in the dry areas is generally stronger in the free atmosphere in
192 SCALE. The sharp transition of the circulation at the boundary layer top in SCALE
193 corresponds to the most significant radiative cooling (Fig. 2e). The results suggest that the
194 mechanism for CSA in SCALE is similar to the radiative-driven cool pool mechanism proposed
195 by Coppin and Bony (2015). The mechanism describes that the radiative cooling due to low
196 clouds in the dry areas drives low-level circulations, and convection is then pushed by the
197 circulation to the humid areas. The low-cloud in their study plays a critical role in the radiation-
198 circulation interaction. In our study, the features of the stronger radiative cooling and enhanced

199 low-level circulation are found in SCALE, but there is no low cloud developing in the dry
200 region. We attribute the strong radiative cooling to the drier free atmosphere in SCALE. The
201 drier environment reduces the emissivity of the free atmosphere and leads to efficient cooling
202 at the boundary layer top, which can drive shallow circulation as low clouds. Besides, the drier
203 environment in SCALE enhances the evaporation of rain water, so the boundary layer in the
204 moist region has significant cooling signals in SCALE (Fig. 2c). The mechanism for CSA in
205 SCALE is close to the leading mechanism under the cold mean states in Coppin and Bony
206 (2015), but it is due to a drier environment rather than the low clouds in the dry areas.

207

208 The features of VVM in the moisture space provide a possible mechanism for CSA.
209 The ascending branch is confined in the region where PW greater than 51 mm accompanying
210 with considerable microphysical heating (Fig. 2d). The radiative cooling in VVM is weaker
211 compared to SCALE (Fig. 2e and 2f). CSA is mainly driven by the convection in the narrow
212 moist areas in VVM, which indicates that the condensate heating is more efficient in driving
213 circulation (Hack and Schubert 1986). The mechanism for CSA in VVM would be similar to
214 the wind-induced surface heat exchange (WISHE) mechanism under the warm mean states in
215 Coppin and Bony (2015). The circulations triggered by convection enhance the surface wind
216 and turbulent enthalpy flux, and it can lead to the convergence of heat in the convective region
217 from the far region. These responses favor the subsequent development of convection in the
218 adjacent areas of existing convection. This mechanism is consistent with that CSA is controlled
219 by convection in VVM. Besides, the more humid PW range and boundary layer in VVM could
220 be attributed to the enhanced surface enthalpy flux. Although the two models are forced by the
221 same SST, the analyses in the moisture space clarify that different mechanisms for CSA are the
222 radiative-driven cool pool feedback in SCALE and the WISHE feedback in VVM.

223

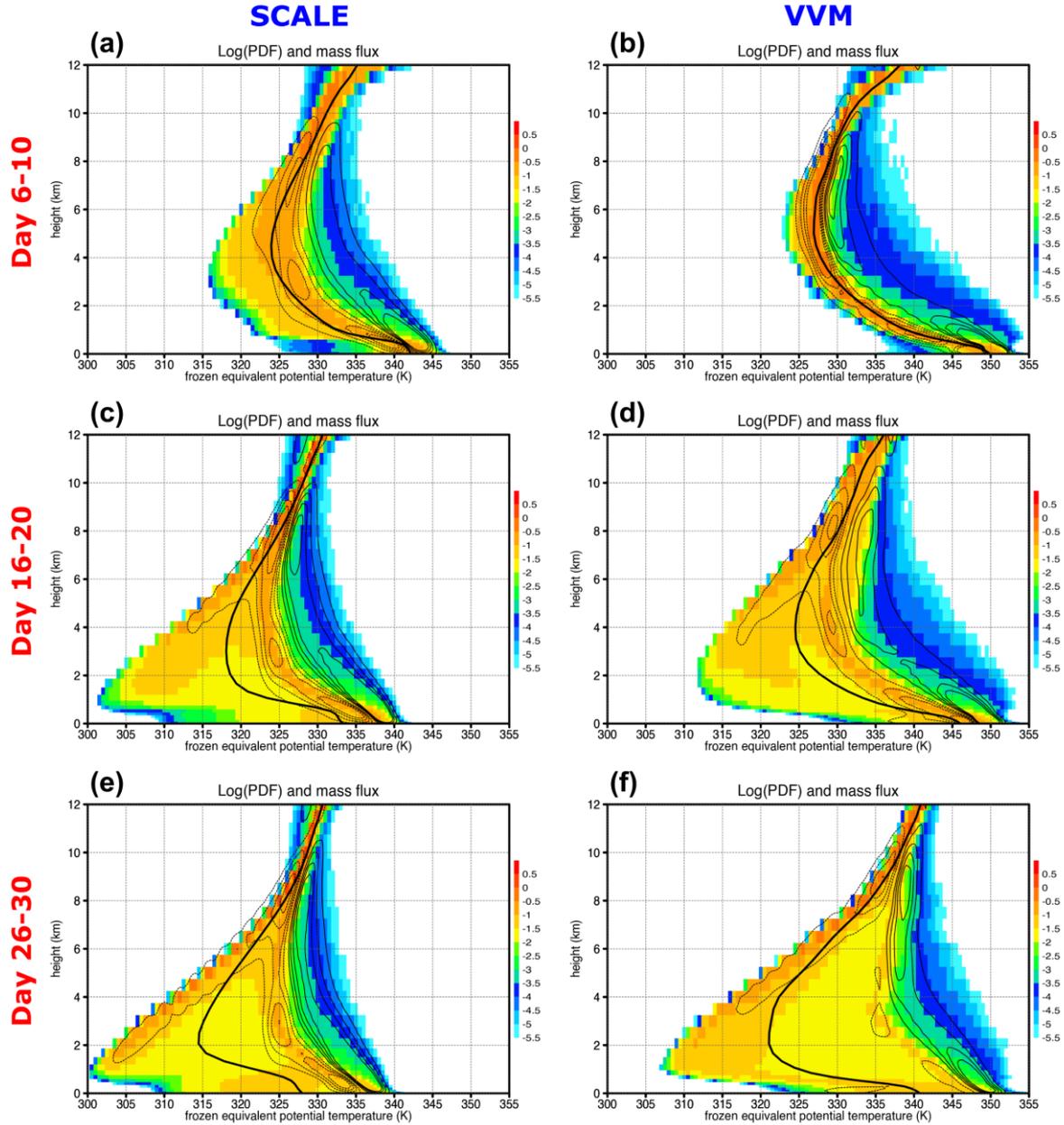


Fig. 3. The isentropic analysis of SCALE (left panels) and VVM (right panels) for days 6-10 (a, b), days 16-20 (c, d), and days 26-30 (e, f). The solid black line represents the mean frozen equivalent potential temperature (θ_{ei}) and the color shading represents the logarithmic probability density function of θ_{ei} . The isentropic mass fluxes are presented by the contours with the interval of $0.003 \text{ kg m}^{-2} \text{ K}^{-1}$.

225 3.3 Isentropic analyses on the evolution of CSA

226 During the developing stage of CSA, the drastic changes in the temporal evolution of
227 IWP in VVM hints on the transitions of cloud structures. The different mechanism for CSA in
228 SCALE and VVM could be related to the cloud structure changes. We apply the isentropic
229 analysis (Pauluis and Mrowiec, 2013) to investigate the convective structures via the energetic
230 perspective (Huang and Wu 2020). The isentropic distribution is calculated through conditional
231 sampling by the air parcel's frozen equivalent potential temperature (θ_{ei}) following Pauluis
232 (2016). The isentropic mass fluxes could be approximated as the convective parcels'
233 trajectories on the energy space. The isentropic analysis is applied to days 6-10 (Fig. 3a and
234 3b), days 16-20 (Fig. 3c and 3d), and days 26-30 (Fig. 3e and 3f) for both models to focus on
235 the changes in the developing stage of CSA.

236

237 In days 6-10, the isentropic distributions are single-peak with maximum occurrences
238 around the mean θ_{ei} profile. The subsiding mass fluxes associated with the high occurrences
239 indicate that the subsidence occurs in vast areas, and convection develops in the limited areas.
240 SCALE has wider isentropic distributions for the altitudes between 1 km and 8 km during days
241 6-10 because dry areas start to expand (Fig. 3a). In VVM, CSA does not develop yet, so
242 isentropic distributions are concentrated and close to the domain-averaged θ_{ei} profile (Fig. 3b).
243 Both models have a local maximum of upward and downward isentropic mass fluxes below 2
244 km height due to the boundary layer mixing. In SCALE, the updraft extends from 2 km to 8
245 km with 5 K changes in θ_{ei} , which indicates the influence of the entrainment, especially in
246 low-levels. The impacts of entrainment are greater in VVM because of the changes of θ_{ei} (10
247 K) along with upward mass fluxes from 2 km to 4 km. Above the freezing level (5 km), the
248 updraft remains at constant with the increase of height.

249

250 During days 16-20, SCALE and VVM share some similarities on the isentropic
251 diagrams (Fig. 3c and 3d). The domain-averaged θ_{ei} profiles shift to lower θ_{ei} region, and the
252 isentropic distributions become bimodal in both models compared to day 6-10. One peak
253 locates at low θ_{ei} region smaller than averaged θ_{ei} , and the other peak remains at the high θ_{ei}
254 region. These features in the isentropic diagrams indicate that CSA develops and leads to the
255 expansion of the dry areas, and the two peaks at high and low θ_{ei} can, respectively, represent
256 the moist and dry regions. An extra subsiding branch of mass flux develops along with the peak
257 at low θ_{ei} in the layer between 4 km and 6 km. The upward mass fluxes become stronger in
258 the moist region compared to days 6-10. These similar features in both models reflect the
259 development of CSA, and these changes from days 6-10 to days 16-20 become more significant
260 as CSA continue developing in days 26-30.

261

262 Notable differences can be seen in the evolutions of the isentropic distributions as CSA
263 develops. The first one is that the overall isentropic distribution in SCALE shifts toward the
264 low θ_{ei} region (surface θ_{ei} is 345 K in days 6-10 and 337 K in days 26-30). In VVM, the peak
265 at low θ_{ei} shifts only, and the peak at high θ_{ei} remains at similar values of θ_{ei} (surface θ_{ei} is
266 350 K). The drier range of PW in the moisture space during the quasi-equilibrium state is highly
267 related to the shift in SCALE. The result suggests that SCALE and VVM undergo different
268 pathways to CSA and finally reach quasi-equilibrium states driven by distinct mechanisms. A
269 hypothesis for the different pathways in SCALE and VVM is provided based on the differences
270 in the evolutions of isentropic mass fluxes in the high θ_{ei} regions. The upward mass fluxes
271 considerably strengthen without large changes in its vertical structure in SCALE. In VVM, the
272 strength of ascending mass fluxes moderately enhances, and its structure becomes steeper in
273 days 26-30 (Fig. 3e) compared to days 6-10 (Fig. 3a). The steeper structure indicates that the
274 effects of the entrainment are reduced. The results suggest that convective structures change as

275 CSA develops in VVM. The convection then becomes more efficient in driving circulations
276 between dry and moist regions even with less upward transports compared to SCALE in days
277 26-30 (Fig. 3e and 3f). The stronger ascending transports is need to keep developing CSA in
278 SCALE. The downward mass fluxes nearby the ascending ones on the isentropic diagram (Fig.
279 3e) indicate that the compensating subsidence occurs in adjacent regions of existing convection
280 in physical space. The subsidence in the moist region causes the lower efficiency in driving the
281 circulations and the suppression of accumulating PW in atmospheric columns. The transition
282 of the convective structures is hypothesized to be critical for the different pathways to CSA in
283 SCALE and VVM.

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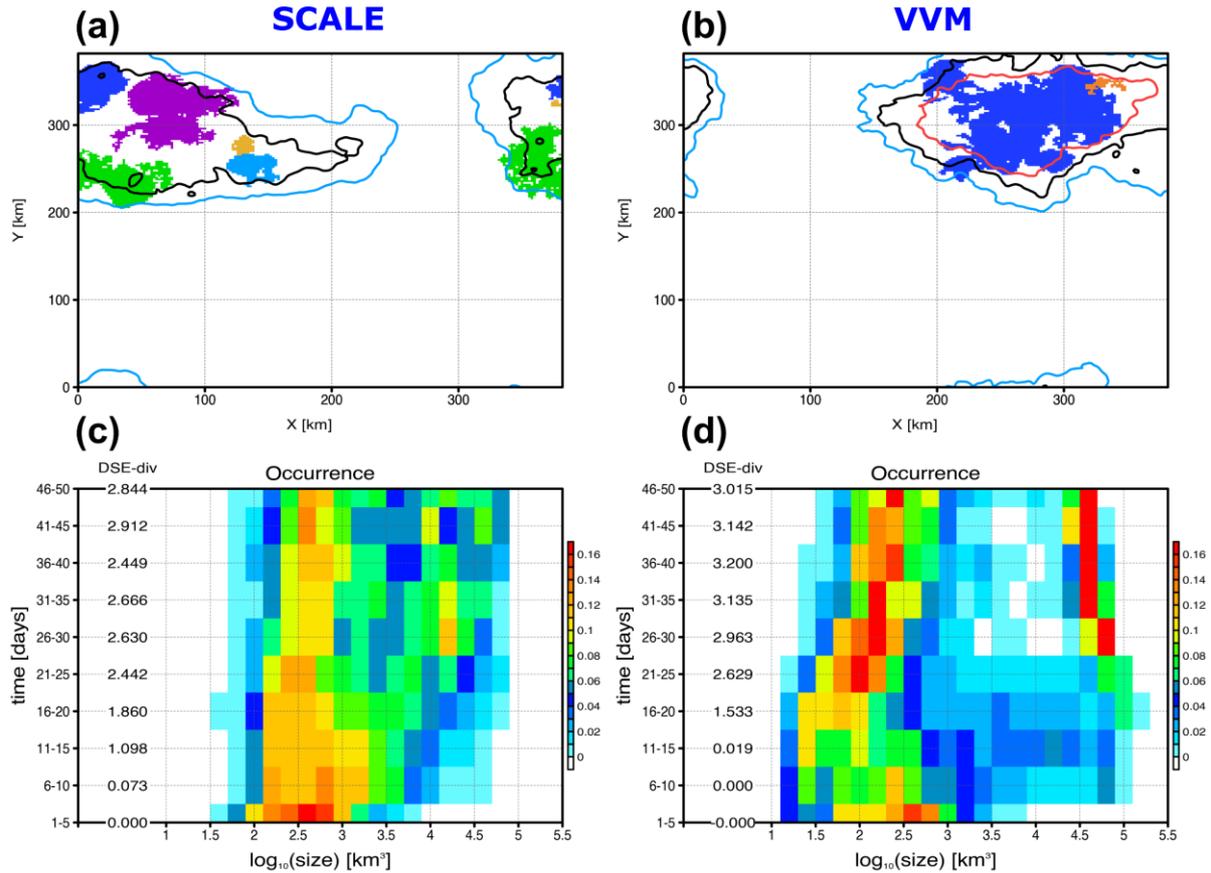


Fig. 4. The surface projections of convective cloud on day 48 for SCALE (a) and VVM (b). Precipitable water of 30, 40, and 50 mm are presented by the cyan, black, and red contours, respectively. Time evolutions of cloud size distribution for SCALE (c) and VVM (d) are shown by the color shading with 5-day intervals. The values with the unit of $10^6 \text{ J m}^{-2} \text{ s}^{-1}$ at the left part of the panels present the temporal averages of column flux divergence of dry static energy (DSE-div) in the moist region where PW is greater than 30 mm.

285 3.4 The statistics of convective structure changes

286 We apply the object-based analysis method to investigate the transition of convective
 287 structures. This method has been used to study the changes in the convective structure among
 288 different environments (Tsai and Wu, 2017; Su et al., 2019). The definition of cloud objects in
 289 this study follows Wu and Chen (2021). Contiguous cloudy grids where the total cloud

290 condensates are greater than 10^{-5} kg kg⁻¹ are connected and then identified as a convective
291 cloud object using the six-connected segmentation method. Here, we add a condition that the
292 cloud object base is lower than 2 km to ensure convective clouds develop from the boundary
293 layer. Additionally, a criterion that the cloud top height greater than 6 km is used to select the
294 deep convection, which can largely influence the environment and the circulation. The features
295 of convective cloud objects are projected to the surface at day 48 (Fig. 4a and 4b).

296

297 Both models have a similar coverage of the moist area where precipitable water is
298 greater than 30 mm, but the horizontal scales of the convective cloud objects are quite different
299 between SCALE and VVM. Convective cloud objects in SCALE scatter within the moist area
300 with a smaller size. In VVM, the largest cloud object almost occupies the moist area, and some
301 smaller cloud objects surround the largest one. The moist area of VVM is more humid than that
302 of SCALE, and it would support the development of larger convective clouds. The evolution
303 of the size distribution shows that the size of convective clouds tends to be smaller than 10^3
304 km³ in both models. As CSA develops, the size distributions in both models become a bimodal
305 distribution with peaks of smaller and larger sizes, and the bimodal distribution in VVM is
306 more obvious than that in SCALE. The large-size peak splits from the small-size peak in days
307 6-30 and shifts to about 10^4 km³ gently in SCALE, while the large-size peak in VVM leaps to
308 $10^{4.5}$ km³ in days 11-25. The convective cloud objects with a size greater than 10^4 km³ rarely
309 appear in SCALE, while they frequently develop with larger sizes in VVM. The results suggest
310 that the convective systems in VVM become more organized during the development of CSA.

311

312 The organized convective clouds mostly covering the moist region in VVM can more
313 efficiently drive the circulations between dry and moist regions. In contrast, the smaller
314 convective clouds in SCALE lead to the subsidence in the clear-sky region between the systems,

315 which corresponds to the subsidence nearby the upward motion on the isentropic diagram. That
316 the organized convection can efficiently drive circulations is supported by the divergence of
317 column-integrated dry static energy (DSE-div) in the moist region where PW larger than 30
318 mm. DSE-div in both models increases with the emerge of the large-size peak in the size
319 spectrum. The increase of DSE-div accompanies by the gentle shift of the large-size peak in
320 SCALE, while DSE-div rapidly grows in days 11-25 in VVM when the size distribution sharply
321 transits. After day 30, the exports of DSE in the moist region are greater in VVM, and the
322 greater exports accompany with the larger convective clouds frequently develop. The results
323 confirm that the transition of convection to more organized systems in VVM enhances the
324 efficiency in driving circulations, while the convection without the structure changes is
325 inefficient in SCALE. The discrepancy in the organized structures leads to the different
326 pathways to CSA.

327

328 **4 Summary and Discussion**

329 In this study, RCE simulations are conducted using two CRMs (SCALE and VVM)
330 following the RCEMIP protocol (Wing et al. 2020), and the setups of the horizontal domain
331 and resolution are adopted from Yanase et al. (2020). Our results show that two models undergo
332 two different pathways to CSA even though the two models reach CSA after 40 days. The
333 analyses in the moisture space indicate that CSA in SCALE develops through the strong
334 shallow circulation induced by the enhanced radiative cooling near the boundary layer top. The
335 isentropic and object-based analyses provide evidence that the convective systems in VVM
336 become more organized and then enhance the circulation between the dry and moist regions.
337 The pathways to CSA in SCALE and VVM are, respectively, similar to the mechanisms in cold
338 and warm SST scenarios in Coppin and Bony (2015). In their study, the critical mechanism for
339 the development of CSA varies among SST. Our study highlights that even though CSA in both
340 models is driven by the same SST of 300 K, the critical mechanism for CSA is different
341 between SCALE and VVM.

342

343 The different pathways to CSA between SCALE and VVM provide a process-based
344 perspective to understand the diverse results in the RCEMIP ensemble. The different
345 mechanisms also imply different climate sensitivities among models. In SCALE, the
346 development of CSA is driven by radiative cooling, which could largely change the radiative
347 energy budget. The enhanced longwave cooling in the dry areas can offset the warming due to
348 the imbalance of radiative forcing such as the greenhouse gases. As radiative cooling dominates
349 the development of CSA, the climate sensitivity would be smaller in SCALE. On the other
350 hand, CSA develops with the transition of convective structures like VVM. The response of
351 radiation would be inefficient, which leads to larger climate sensitivity. The difference in
352 outgoing longwave radiation is 15 W m^{-2} between SCALE and VVM in the quasi-equilibrium

353 state. It is worth further investigating how the different mechanisms for CSA lead to the spread
354 of CRMs in the RCEMIP ensemble.

355

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361 Number JP16H04048 and JP20H05729. The two models used in this study can be obtained
362 from <https://scale.riken.jp/> (SCALE, version 5.3.6) and
363 <https://doi.org/10.6084/m9.figshare.14866260.v1> (VVM, version 1.5.1). The analyzing codes
364 and post-processing data are available in the online open access repository
365 (<https://doi.org/10.6084/m9.figshare.11933091.v3>).

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