A 3D Full Stress Tensor Model for Oklahoma

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Key Points:

- We compute the stress field using finite element modeling by considering contributions from both gravitational and far-field tectonic forces
- The simulated stress field in Oklahoma agrees with observed stress indicators including the orientation of S_{Hmax} and the faulting type
- Gravitational contribution to the horizontal stress field has a comparable magnitude regarding tectonic contribution for the upper 5 km

Abstract

The stress tensor is an important property for upper crustal studies such as those that involve pore fluids and earthquake hazards. At tectonic plate scale, plate boundary forces and mantle convection are the primary drivers of the stress field. In many local settings (10s to 100s of km and <10 km depth) in tectonic plate interiors, we can simplify by assuming a constant background stress field that is perturbed by local heterogeneity in density and elasticity. Local stress orientation and sometimes magnitude can be estimated from earthquake and borehole-based observations when available. Modeling of the local stress field often involves interpolating sparse observations. We present a new method to estimate the 3D stress field in the upper crust and demonstrate it for Oklahoma. We created a 3D material model by inverting multiple types of geophysical observations simultaneously. Integrating surface-wave dispersion, local travel times and gravity observations produces a model of P-wave velocity, S-wave velocity and density. The stress field can then be modeled using finite element simulations. The simulations are performed using our simplified view of the local stress field as the sum of a constant background stress field that is perturbed by local density and elasticity heterogeneity and gravitational body forces. An orientation of N82˚E, for the maximum compressive tectonic force, best agrees with previously observed stress orientations and faulting types in Oklahoma. The gravitational contribution of the horizontal stress field has a magnitude comparable to the tectonic contribution for the upper 5 km of the subsurface.

1 Introduction

The stress tensor is an important geophysical property of the subsurface and is highly important to tectonic and earthquake studies (e.g., Heidbach et al., 2018; Levandowski et al., 2016, 2018; McGarr & Gay, 1978; M. L. Zoback & Magee, 1991; M. Lou Zoback & Zoback,

1980) and subsurface engineering (Liu et al., 2017; Martínez-Garzón et al., 2013; Nussbaum et al., 2017; M. D. Zoback et al., 2010). Principal stress orientations (sometimes with magnitude) have been modeled or observed at tectonic plate scales in the World Stress Map (Heidbach et al., 2018). Orientations of maximum horizontal principal stress (S_{Hmax}) are typically determined using borehole and surface techniques (Lin et al., 2018; Ljunggren et al., 2003) and heterogeneity likely exists at all scales (Hsu et al., 2010; Iio et al., 2017; Lund Snee & Zoback, 2016; Rivera & Kanamori, 2002; Schoenball & Davatzes, 2017). Below the deepest available stress measurements, much of what we know of shear stress magnitudes on faults is from stress rotations associated with large earthquakes as measured with focal mechanisms (see Hardebeck & Okada, 2018 and references therein). The World Stress Map (Heidbach et al., 2018) catalogs tens of thousands of orientations of the S_{Hmax}, some of which are associated with information on the style of faulting (e.g., normal, strike-slip, or reverse). The full stress tensor, including principal component magnitudes, is largely unknown away from boreholes and earthquakes.

Contributions from quasi-static forces to the stress tensor at any point in the Earth's upper crust in order of magnitude are (1) gravitational body forces (0-100s of MPa, increasing with depth), (2) tectonic (plate boundary and bottom tractions, 10s of MPa or more, (Richardson et al., 1979), and (3) local, related to slip on faults (~10 MPa or less) and poroelastic stress (< 2 MPa) (Segall, 1989). Stress changes due to recent slip on faults can be locally significant but are limited in spatial extent except for those associated with very large earthquakes (Wesson & Boyd, 2007). These forces act on subsurface structures with heterogeneous elastic properties, resulting in a heterogeneous stress field. Published continental and regional stress modeling results (e.g., Fleitout & Froidevaux, 1982; Flesch et al., 2000, 2007; Forte et al., 2007; Ghosh et al., 2013, 2019; Humphreys & Coblentz, 2007; Levandowski et al., 2016; Liu et al., 2017; Reiter

& Heidbach, 2014) have been used to explain large-scale deformations (e.g. mountain building) and seismicity (both interplate and intraplate). The importance of the gravitational contribution in stress modeling has been emphasized by Humphreys & Coblentz (2007) and Flesch et al. (2000, 2007). Forte et al. (2007) and Levandowski et al. (2016) suggest both tectonic forces and subsurface elastic property heterogeneity may have contributed to the seismicity of the New Madrid seismic zone. Flesch et al. (2007) found that the gravitational potential energy and tectonic forces contribute to the deviatoric stress magnitude almost equally in western North America. However, it is not clear whether the gravitational and tectonic contributions are similar to the deviatoric stress magnitude in other regions. We chose the Oklahoma area to study the 3D stress field variations since previously published stress observations in the area can validate our stress modeling method. We hypothesize that most of the observed deviations from the tectonic stress field in Oklahoma are due to gravitational effects and heterogeneity in material properties including density and elastic modulus. By modeling both the gravitational and tectonic components of the stress field, we can both test this hypothesis and constrain principal component magnitudes. For the purposes of this paper, “tectonic” stress refers to stresses that are imparted on our study area through boundary conditions and includes such things as ridge push, slab pull, and basal traction. More detailed material models have been suggested as one approach to improve stress models by several researchers (e.g., Ghosh et al., 2019; Reiter & Heidbach, 2014). In order to model the gravitational and tectonic components of the stress field in Oklahoma accurately, we require a detailed 3D material model and information (direction and magnitude) about tectonic forces. Since directions and magnitude of tectonic forces are not known for most regions, we estimate them with stress observations via multiple stress modeling tests. The material model can be obtained from subsurface seismic structure investigations.

A few detailed investigations have focused on the 3D crustal structure in the Oklahoma region. Evanzia et al. (2014) studied the upper mantle structure using teleseismic body wave tomography in the Texas and Oklahoma area. A few regional and continental scale studies mainly based on Earthscope Transportable Array data with nominal station spacing of ~70 km (e.g., Chai et al., 2015; Porter et al., 2016; Schmandt et al., 2015; Shen & Ritzwoller, 2016) imaged the broad-scale structure of the Oklahoma region. Limited by different scope and focus of these studies, fine scale subsurface structure of both P- and S-wave velocities in the study area is not well resolved. Seismic velocity models produced by these broader scale studies can be used as a starting model for more detailed investigations. The compiled global model Crust 1.0 (Laske et al., 2013) was produced by combining Earth models from active source surveys. However, the coverage and resolution of these earlier studies are not sufficient for our stress modeling. We constructed a material model to extend these earlier efforts.

In this paper, we first present data used in our technique that includes observations for material model inversion and for stress modeling. Details on the inversion for the material model and stress modeling are documented in the following section. Then, we present results for the material model and the stress model of the Oklahoma region. The major findings, assumptions, and limitations are discussed in the last section.

2 Data

Our analysis consists of constraining a material model (P- and S-wave velocity and density) and stress modeling, which requires both geophysical observations and stress measurements.

111 2.1 Observations for material model inversion

112 We simultaneously and jointly invert local P- and S-wave first arrival times, Rayleigh-
113 wave and Love-wave dispersion maps, and satellite-derived Bouguer gravity observations to
114 model the 3D subsurface P- and S-wave velocity and density structure. Each of these datasets
115 went through various quality control procedures. Interactive visualization tools (Chai et al.,
116 2018) were used to visually examine the datasets as well as the resulting material models. Details
117 of the data selection and preprocessing are documented in the following paragraphs.

118 The local body waves arrival time dataset (catalog locations and P- and S- arrivals) was
119 obtained from United States Geological Survey (McNamara et al., 2015). Catalog arrival times
120 that we suspected to be erroneous, such as those leading to more than 5 s misfits (unrealistically
121 large), were excluded from the inversion for material properties. Only events with 6 or more P-
122 wave arrival times are included in the inversion so the location of seismic events is well
123 constrained. The final arrival times dataset used in the inversion comprises 58,896 P-wave
124 arrivals and 20,155 S-wave arrivals from 3,740 earthquakes that were recorded at 157 seismic
125 stations between November 2011 and July 2015 (Figure 1a). Besides absolute catalog body wave
126 arrival times, differential catalog times were computed (Waldhauser, 2000) and included in the
127 inversion (Zhang & Thurber, 2003) because of their ability to further improve the relative
128 locations of neighboring earthquakes and their surrounding velocities. As shown in Figure 1,
129 most of the earthquakes are located in north central Oklahoma, and the station distribution is
130 reasonable with a good azimuthal coverage.

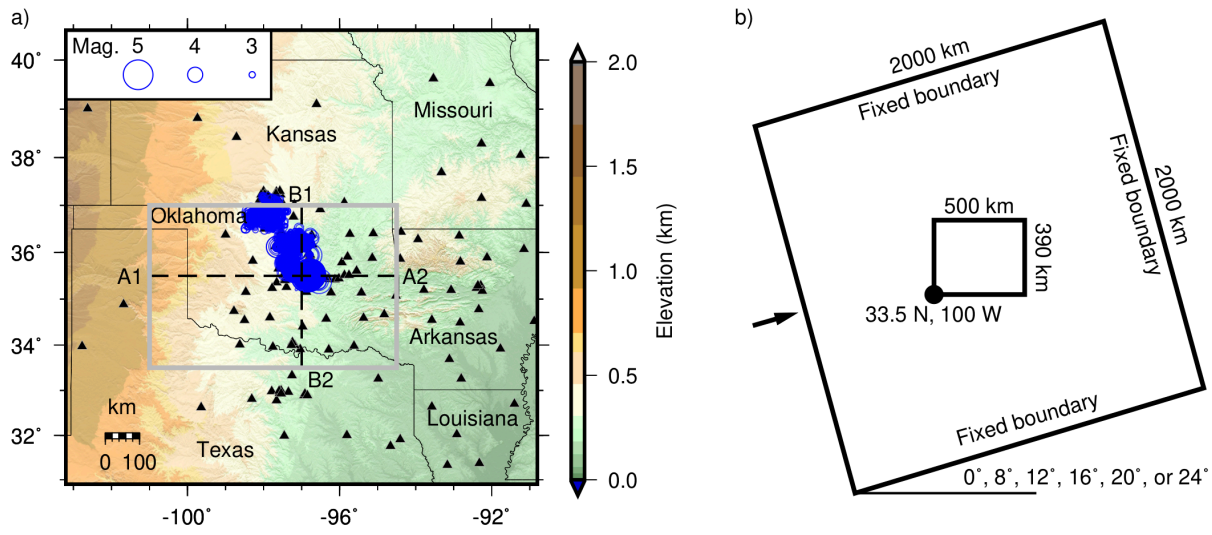


Figure 1. Study area map (a) and the finite element model design (b). The map shows the location of seismic events (blue open circles) and stations (black solid triangles) used to construct the body wave arrival time dataset. The size of the circles is a function of magnitude. The dashed lines indicate locations of the cross-sections in Figure 7. The gray box shows the area for Figure 6. The finite element model is a hexahedron with sides 2000 km long and depth of 200 km. The axes of the full model are aligned with the tested tectonic force directions in Figure 8. The axes of the rectangle bounding the study area are aligned west-east and south-north. The geographic origin of the study area is noted on the figure. The arrow indicates direction of displacements applied on the southwest boundary to produce a maximum horizontal compressive stress oriented southwest to northeast.

The surface wave dispersion estimates (used as observations in this study) were obtained from an update of Herrmann et al. (2016). The dispersion model was constrained with local earthquake and ambient noise measurements. Group and phase velocities of both Rayleigh and Love waves are available online (Herrmann et al., 2016). We use periods ranging from 5.0 s to 51.5 s with 24 data points per dispersion curve when sufficient data are available. The surface wave data were resampled from the dispersion model onto a 0.5˚ by 0.5˚ horizontal grid that covers the study area. Four dispersion curves at each of these horizontal grid nodes are included in the inversion when available. The Bouguer gravity data (observations for this study) was extracted from the global model WGM2012 (Balmino et al., 2012) and sampled to the same horizontal grid as for the dispersion observations. The gravity data was filtered in the wavelength domain to avoid overfitting and to remove long-wavelength features mainly caused by deep

density variations. Very short wavelength (less than 50 km) and long wavelength (longer than 200 km) anomalies were excluded since they are beyond our spatial resolution (50 km laterally). Gravity observations at the four edges (around 200 km wide) were not used in the inversion to avoid edge effects (no gravity contributions outside of the study area). We used a larger area (the entire region as shown in Figure 1a) for the velocity model inversion so that the edge effects do not influence our results.

2.2 Observations for stress modeling

During the stress modeling, we used S_{Hmax} orientations and A_ϕ (Simpson, 1997) as data constraints. A total of 94 S_{Hmax} orientations with uncertainties of 15°, 20° or 25° referred respectively as qualities A, B, and C (Heidbach et al., 2018) were accepted as stress observations. A_ϕ (Simpson, 1997) is determined from the magnitudes of the 3 principal stresses and ranges from 0 (radial extension) to 3 (radial constriction), where the values for pure normal, pure strike-slip, and pure reverse are 0.5, 1.5, and 2.5, respectively. We used A_ϕ values from (Levandowski et al., 2018) in our stress inversion because they cover our study area and have published uncertainties, though other interpretations exist (Lund Snee & Zoback, 2016).

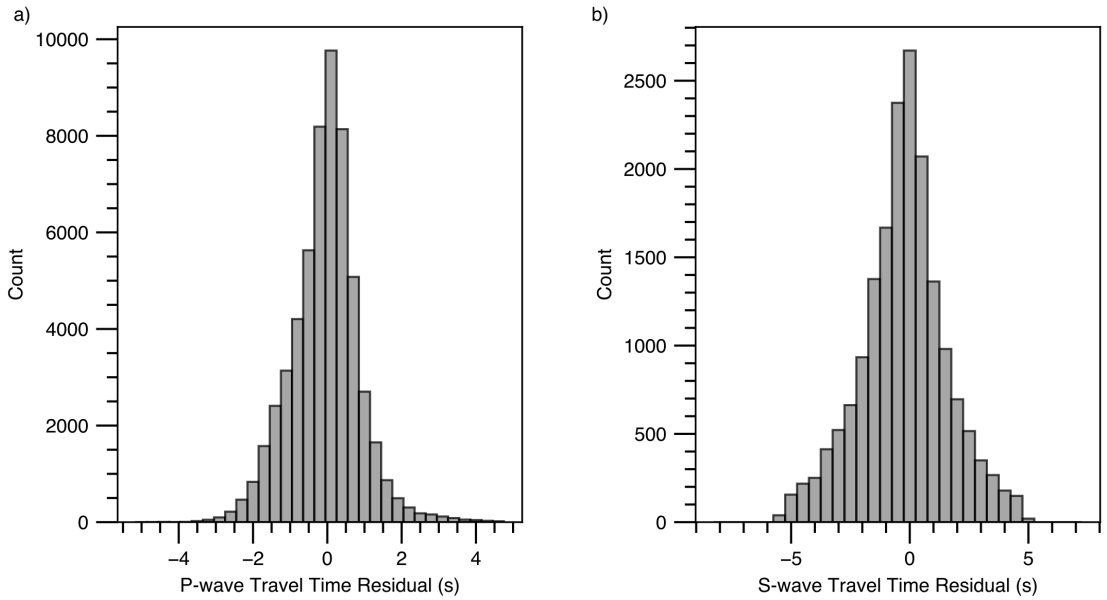
3 Method

We first describe the approach that we used to obtain the material model. Then, we document details on the stress modeling.

3.1 Inversion for the material model

The joint inversion technique we used is the same as that of Syracuse et al. (2016, 2017) which used multiple geophysical datasets to directly constrain P- and S-wave velocities, and

mass density. The inversion algorithm was developed based on tomoDD (Zhang & Thurber, 2003, 2006) and an inversion program that simultaneously inverts surface-wave and gravity data (Maceira & Ammon, 2009). The shear velocity-density relationship from Maceira & Ammon (2009) was used to relate gravity observations to seismic speeds. We started the inversion using a 3D initial model from Chai (2017), which was constrained with spatially smoothed P-wave receiver functions (Chai et al., 2015), surface-wave dispersion (Herrmann et al., 2016) and gravity observations (Balmino et al., 2012). The inversion iteratively updated the P- and S-wave velocity models by minimizing the data fits and taking into consideration other regularizations constraints such as smoothing and damping. Different weights were assigned to each type of data constraints. We performed two suites of inversions to find the optimal combination of weights using L-curve analysis as suggested by Syracuse et al. (2015). The first set of inversions searched for the appropriate damping and smoothing values (see Figure S1 and Visualization S1 in the electronic supplements). The second set explored the weights for gravity and surface-wave data (see Figure S2 and Visualization S2 in the electronic supplements). The optimal material model (P- and S-wave velocities and density) was selected by minimizing an objective function of data fits and regularization terms similar to Syracuse et al. (2016, 2017). The optimal material model fitted the travel times (Figure 2), gravity observations (Figure 3), and surface-wave dispersions (Figure 4-5 and Figure S3) reasonably well. Earthquake locations were updated during the inversion simultaneously as well.



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195 **Figure 2**. Histograms showing P- (a) and S- (b) wave travel time residuals associated with the
196 inversion of the material model.

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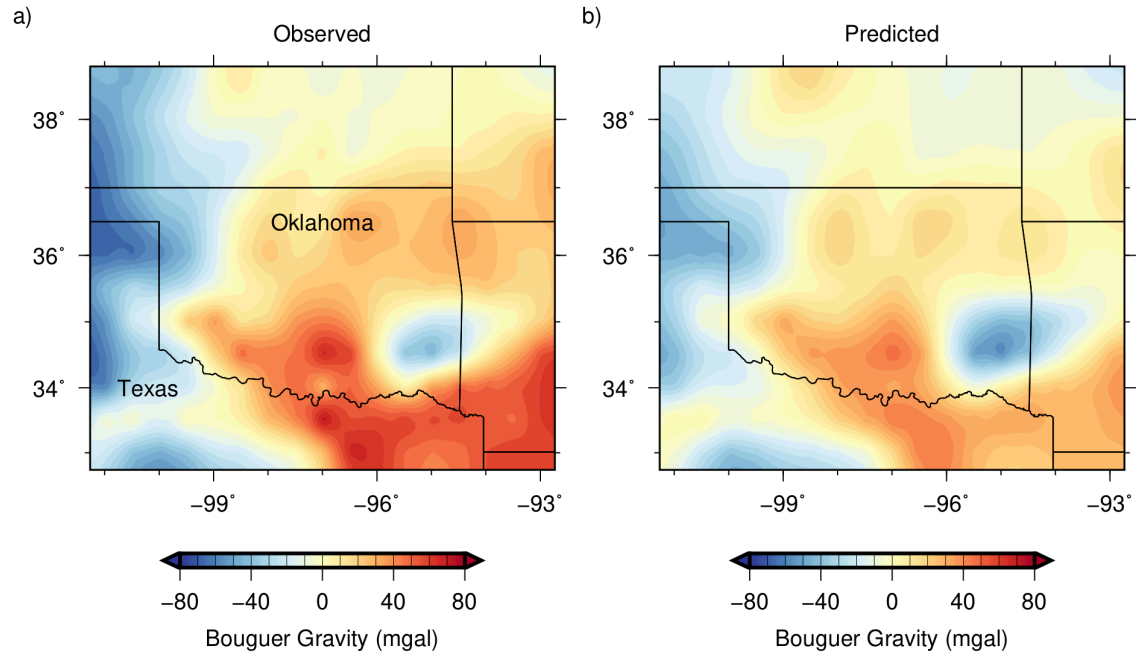

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199 **Figure 3**. A comparison of (a) the observed Bouguer gravity and (b) the predicted gravity for the
200 inversion of the material model.

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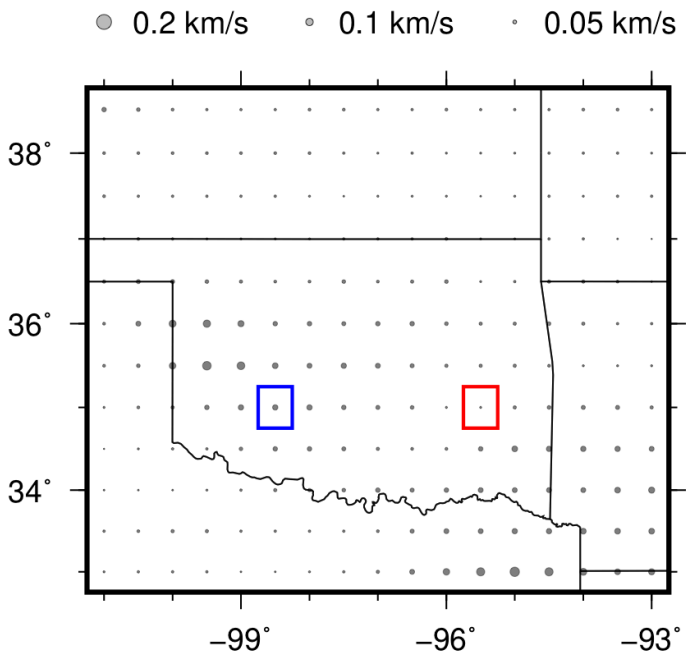


Figure 4. A map showing misfits between surface-wave dispersion observations and predictions with the optimal material model. Smaller dots indicate lower misfits. The red box indicates the location of the data showing in Figure 5. The blue box shows the location of the data showing in Figure S3. The largest misfit is 0.13 km/s. The minimum misfit is 0.02 km/s.

3.2 Stress modeling

We used a commercial finite element code (ABAQUS standard/implicit, version 2018) to model both the tectonic and gravitational body force components of the stress field. The full finite element model is 2000 km along each horizontal dimension and 200 km in depth (Figure 1b). The model was designed to accurately represent stress in the uppermost crust (<10 km), and we do not interpret any results for the deeper crust or upper mantle. Our study area, which falls geographically within 33.5 to 37.0 N latitude and 100 to 94.5 W longitude and is approximately 390 km south to north and 500 km west to east, is centrally embedded within the full model. The axes of this central part of the model were oriented west-east and south-north while the full model was rotated by 0°, 8°, 12°, 16°, 20°, or 24° counterclockwise to correspond to the principal orientations of the modeled tectonic stress field. These directions correspond to azimuths of N90°E, N82°E, N78°E, N74°E, N70°E, and N66°E, respectively, mimicking the

general ENE-WSW S_{Hmax} orientations in central and eastern North America (Alt & Zoback, 2017; Heidbach et al., 2018; Levandowski et al., 2018; Walsh & Zoback, 2016). The source of this regional stress field is not the focus of this study, but such directions closely accord with either Mid-Atlantic Ridge push or basal drag of North American absolute motion (M. Lou Zoback & Zoback, 1980).

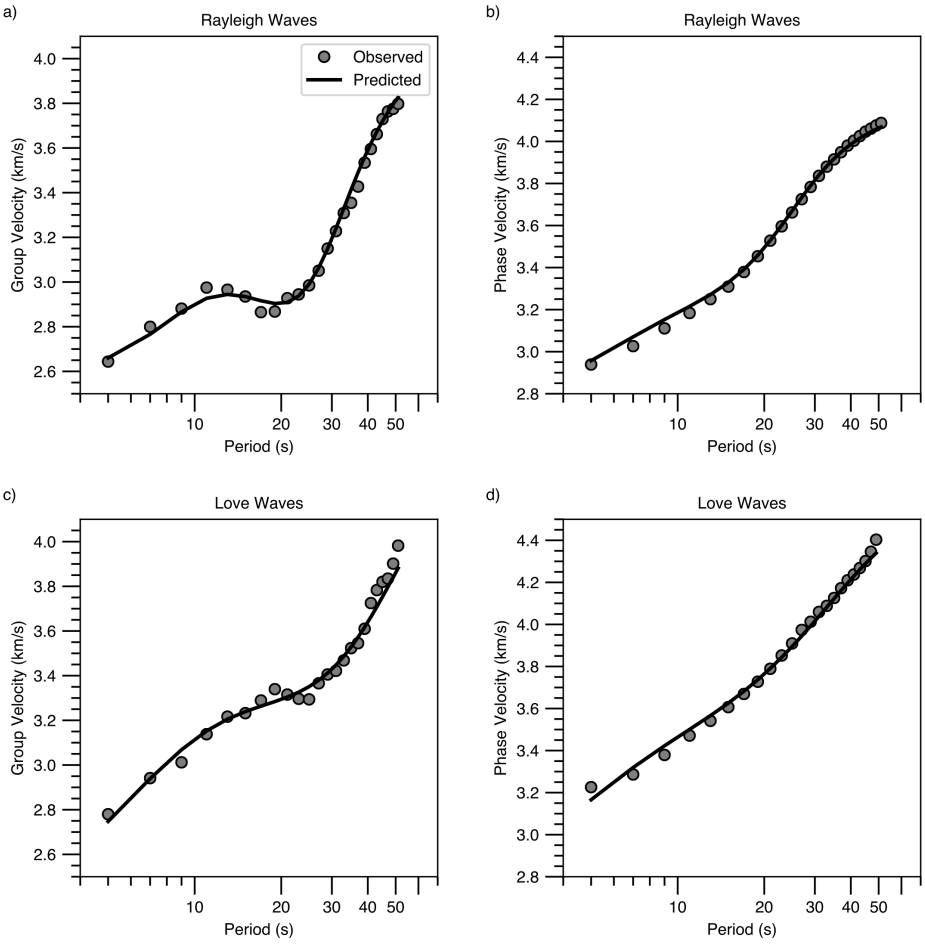


Figure 5. Examples of observed and predicted dispersion curves for an example grid point shown in Figure 4, a) Rayleigh wave group velocities, b) Rayleigh wave phase velocities, c) Love wave group velocities, d) Love wave phase velocities.

The finite elements are 8 node hex, elastic elements with horizontal dimensions of 12 km by 12 km and vertical dimensions of 2 km near the surface, increasing to 20 km vertical spacing near the base. The material properties (P- and S-wave velocities, and density) from the joint

inversion were mapped to the geographically appropriate elements. Elements that fall outside the boundaries of our material model were assigned the median value for their depth. We converted the P- and S-wave velocities, and density into Young's modulus and Poisson's ratio (input for ABAQUS) using formulas from Shearer (2009). The formulas are also included in Text S1.

We modeled the effect of body forces (gravity) by holding constant normal displacement boundary conditions on the four sides and bottom and then apply the gravitational field. This process was performed using a "geostatic" step in ABAQUS. Normally, a volume with body forces applied and zero normal displacement boundary conditions on the bottom and all horizontal boundaries would compress under its own weight. In this geostatic procedure, we determined equilibrium stress conditions for the model due to the applied body forces and boundary conditions, while maintaining the original dimensions. With this procedure, we began with a model that is pre-stressed with overburden before we apply tectonic stress. The overburden stress is approximately the product of density and gravitational acceleration integrated over the depth. Due to 3D heterogeneity in density and elasticity, the stress field caused by overburden is also heterogeneous.

We modeled tectonic stress by imposing a small, uniform (inward) displacement of 61 m along the southwest facing boundary of the full model and zero displacement boundary conditions on the northwest, southeast, and northeast sides (Figure 1b). The displacement applied is approximately equivalent to a tangential compressional stress of 1.9 MPa in the direction of the displacement in the upper 5 km. Since the elastic model is linear, we increment the resulting stress field to model different tectonic stress magnitudes. We intend the applied boundary conditions to approximate any regional contributions to the stress field including plate boundary forces and uniform tractions at the bottom of the lithosphere.

We determined the magnitude of the tectonic force for the best overall fit to the available stress measurements. The depth of measured S_{Hmax} orientations varies, with those derived from borehole measurements at 1 km or more and earthquake moment tensor solutions at 4-5 km. To determine fit to S_{Hmax} orientations, we compared the modeled S_{Hmax} orientations with observed S_{Hmax} orientations (Figure 9). We also used faulting type as a constraint because faulting type is determined by the relative magnitudes of the principal stresses (e.g., Simpson, 1997). In our study area, the dominant style of faulting is strike-slip (Dziewonski et al., 1981), but there are significant and spatially variable amounts of net horizontal extension accommodated by oblique-normal and normal faulting (Levandowski et al., 2018; Walsh & Zoback, 2016).

Using the orientation of 94 available stress indicators (S_{Hmax}) and the faulting types in Oklahoma, we search for the orientation and magnitude of the tectonic force by finding the model that best fits the stress observations. When both the magnitude and orientation of S_{Hmax} are available, alternative approaches (Reiter & Heidbach, 2014) can also be used to determine the orientation and magnitude of the tectonic force. We calculated all plausible magnitudes for a set of orientations and identified the best magnitude and orientation of the tectonic force by minimizing the following function

$$(\boldsymbol{G}m - d)^T \boldsymbol{C}_d^{-1} \qquad (1)$$

where $\boldsymbol{G}$ is the Jacobian matrix describing the relationship between the model parameters and the model predictions, m is model vector, $\boldsymbol{C}_d$ are the reported data uncertainties, and d is the data vector. The model vector has two values, the tectonic force magnitude and orientation. The data vector is composed of observed stress orientations (S_{Hmax}), and A_ϕ. The misfit of each prediction is scaled by the uncertainty of the underlying observation using $\boldsymbol{C}_d$. S_{Hmax} is a measure of the relative magnitudes of the two horizontal principal stresses, while A_ϕ is a measure of the

relative magnitudes of all three principal stresses. Combining these two types of stress observations provide constraints on both the direction and magnitude of the tectonic force.

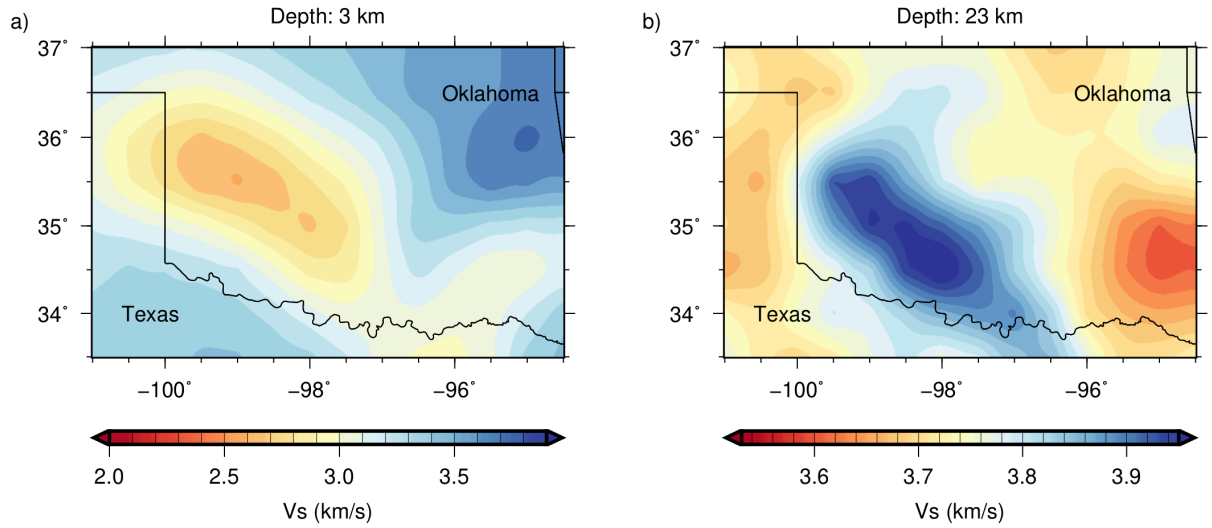


Figure 6. Depth slices of the shear velocity model at 3 (a) and 23 (b) km. The corresponding color scale is shown beneath the depth slice. The black line is the state boundary between Oklahoma and Texas.

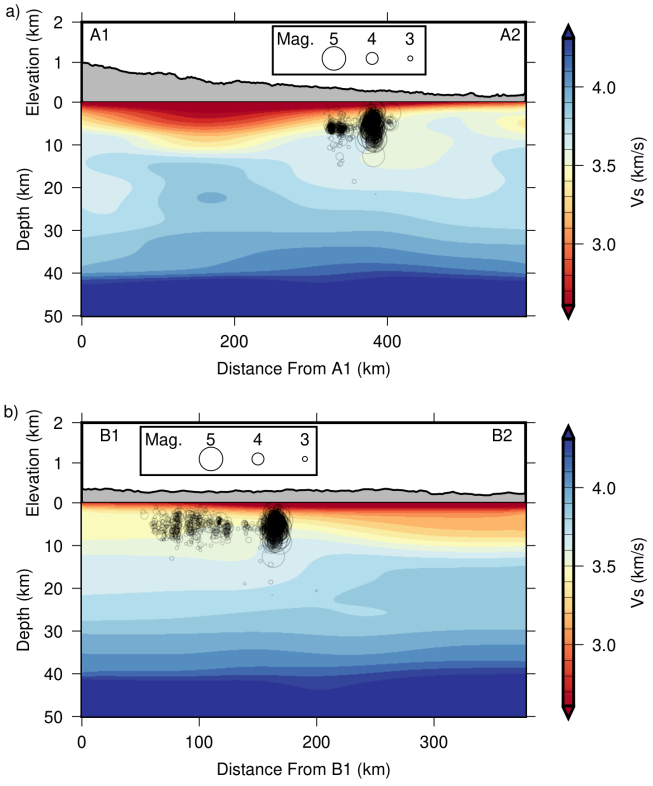
4 Results

Our results include a 3D material model and a 3D stress model.

4.1 Material model

We use depth slices, cross-sections, and interactive visualization to present the 3D material model. Depth slices and two cross-sections of the S-wave velocity model are shown in Figure 6 and 7, respectively. Depth slices of the P-wave velocity and density models are shown in Figure S3, and S4 in the electronic supplements, respectively. An interactive tool (Chai et al., 2018) is provided in the electronic supplements (Figure S5 and Visualization S3) to view the seismic velocities at other locations in the model. Our material model confirms previous geophysical and geological surveys but with a more complete image. At 3 km depth (Figure 6), the slow anomaly in southwest Oklahoma corresponds to the Anadarko basin. The anomaly

295 extends more than 10 km in depth as we can see in the cross-section A1-A2 (Figure 7), which
296 agrees with Johnson's geological compilation (Johnson, 2008). Low seismic velocities (upper 10
297 km in Figure 7) are likely associated with the Anadarko basin. The relative location between the
298 imaged low velocities and the majority of the earthquakes is consistent with Isken & Mooney
299 (2017)'s results. In the mid and lower crust (~15-40 km in depth), we image a high-velocity
300 anomaly beneath the Anadarko basin. The high-velocity anomaly may be related to the past
301 igneous activity associated with the Southern Oklahoma Aulacogen (Gilbert, 1983). We found a
302 slower upper mantle beneath the southern Oklahoma that is consistent with Evanzia et al.
303 (2014)'s model.



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305 **Figure 7**. Cross-sections A1-A2 (a) and B1-B2 (b) of the shear velocity model. Locations of the
306 cross-sections are shown in Figure 1. The black circles indicate the refined earthquake locations.
307

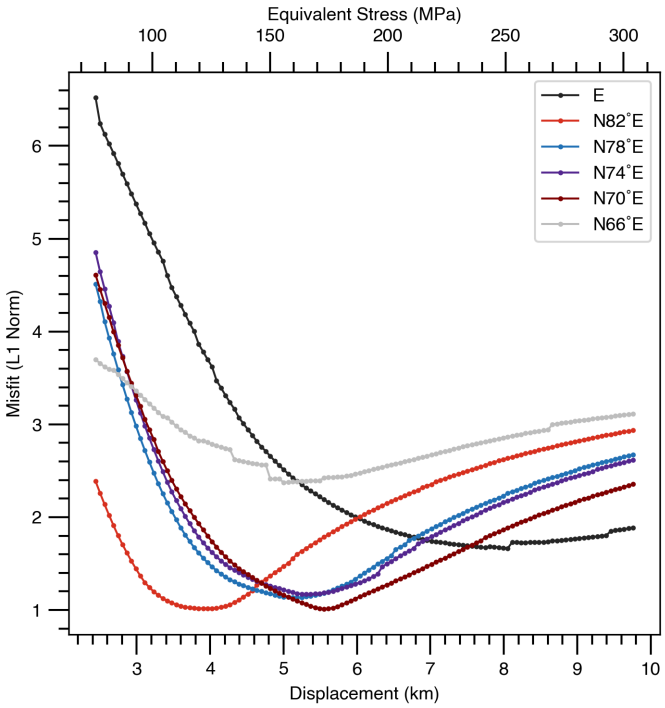


Figure 8. A comparison of misfits of stress indicators and faulting type for five different tectonic orientations as a function of magnitude of tectonic force.

4.2 Stress model

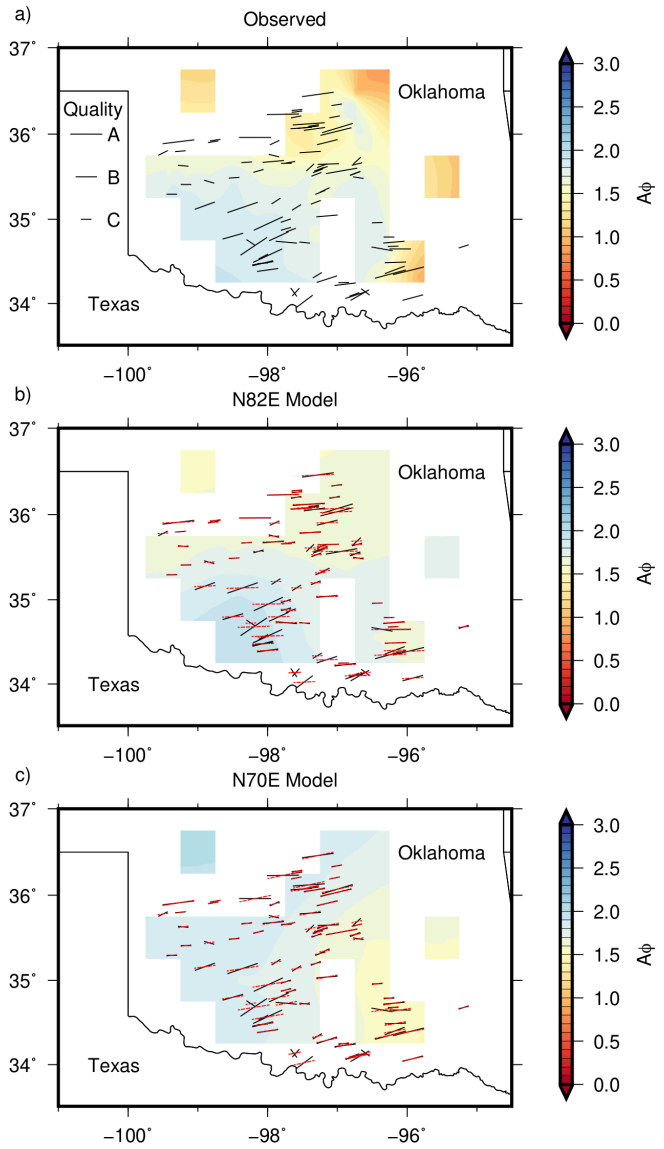
The orientation of the maximum horizontal principal stress (S_{Hmax}) for majority of the stress indicators varies between East and N60˚E. In an attempt to constraint the orientation of the tectonic forces applied to our model, the misfit between the observed and predicted stress orientation was evaluated for a range of boundary force orientations which represent the far-field tectonic forces (Figure 8). For all the cases considered, the misfit is high for very low magnitudes of tectonic force (displacements < 3 km). We interpret this high misfit as a consequence of gravitational body forces dominating the calculated stresses. Conversely, the high misfit for very high tectonic forces (displacements >7 km) is the consequence of tectonic stresses dominating the predicted stress orientations. For most of the cases considered the misfit is minimized for tectonic stresses imparted by a range of ~4 to ~6 km displacement. For orientations in the range of E-N66˚E, the two best fits are models with a displacement of 3965 m (~123 MPa) with an

orientation of N82ºE and a displacement of 5551 m (~173 MPa) with an orientation of N70ºE. These two models have a nearly identical overall misfit and this bimodal misfit surface is due to the interplay between S_{Hmax} and A_ϕ (Figure 8). The N82ºE model fits the spatial variations of the observed A_ϕ a little better than the observed S_{Hmax} directions (Figure 9). Compared to the N82ºE model, the N70ºE model fits the observed S_{Hmax} directions equally well, but not as well for the observed A_ϕ (Figure 9). For this reason, we choose the N82ºE model as our preferred model.

Higher displacements produce models more towards reverse faulting and a more spatially uniform orientation for predicted S_{Hmax}, and lower values produce a model more towards normal faulting and more variable spatial orientations for predicted S_{Hmax}. An arbitrarily high tectonic force is not supported by the data both in terms of the orientation of S_{Hmax} and the faulting type for the best fitting stress orientations (Figure 8). The best fitting model, that does not consider gravitational body forces, is for a stress orientation of N66ºE with an arbitrary displacement magnitude, and has a normalized misfit of 3.85 compared to 1.01 for our preferred model (Eq. 1). This means that stress caused by gravitational body forces explains most of the residual misfit of a uniform model, supporting our hypothesis.

According to previous studies, A_ϕ ranges from ~1.0 in northernmost Oklahoma to 1.5 in central and southern Oklahoma (Levandowski et al., 2018; Lund Snee & Zoback, 2016; Walsh & Zoback, 2016). Though poorly constrained by focal mechanism inversions, portions of southern Oklahoma may have A_ϕ of up to 1.7 (Levandowski et al., 2018; Lund Snee & Zoback, 2016). A_ϕ of the N82°E stress model falls within the range for strike slip faulting with some regions in the southwest having higher values. The models with a tectonic force orientation of E and N66˚E have considerably higher misfits to the weighted sum of S_{Hmax} and A_ϕ (Figure 9). The resulting stress field has a S_{Hmax} orientation from southwest to northeast, consistent with average S_{Hmax}

346 measurements (Alt & Zoback, 2017; Heidbach et al., 2018) and focal mechanism inversions
347 (Levandowski et al., 2018; Walsh & Zoback, 2016). The deviatoric shear stress associated with
348 these stress magnitudes are in the range of 10 to 30 MPa on optimally oriented faults at
349 earthquake depths. The stress orientations and deviatoric stress magnitudes predicted here are
350 consistent with the intraplate stress field predicted in Oklahoma (Alt & Zoback, 2017) and mid-
351 plate North America as described in a number of previous studies; including qualitative
352 assessments of the states of stress (e.g., M. Lou Zoback, 1992; M. Lou Zoback & Zoback, 1980),
353 numerical models of the intraplate stress field using whole-plate linear elastic shell models (e.g.,
354 Humphreys & Coblentz, 2007; Richardson & Reding, 1991), as well as more recent evaluations
355 of the relative stress magnitudes and orientations (Heidbach et al., 2007, 2010, 2018; Lund Snee
356 & Zoback, 2020). While the orientation of the S_{Hmax} for the intraplate stress field is farily well-
357 constrained and understood in the context of local heterogeneities (see discussion in Schoenball
358 & Davatzes, 2017), the magnitude of the intraplate stress field remains more elusive. The stress
359 magnitudes predicted here are consistent with the body of evidence that the tectonic stresses in
360 the lithosphere are generally of the order of tens of MPa averaged over the thickness of the
361 lithosphere.



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363 **Figure 9**. (a) Stress observations and modeled results using a displacement of (b) 3965 m (the
364 orientation of the tectonic force is N82˚E) and (c) 5551 m (the orientation of the tectonic force is
365 N70˚E). Black lines are observed orientations of S_{Hmax} from Alt & Zoback (2017) and Heidbach
366 et al. (2018). Red dashed lines represent the modeled S_{Hmax} orientations. The length of the lines
367 indicates the quality of the observations. The background shows A_ϕ (Simpson, 1997) values
368 computed from the stress model. A_ϕ value of 1.5 corresponds to strike-slip faulting. As A_ϕ values
369 increase from 1.5, the faulting type evolves towards reverse faulting and as values decrease from
370 1.5 faulting type evolves towards normal faulting.

371

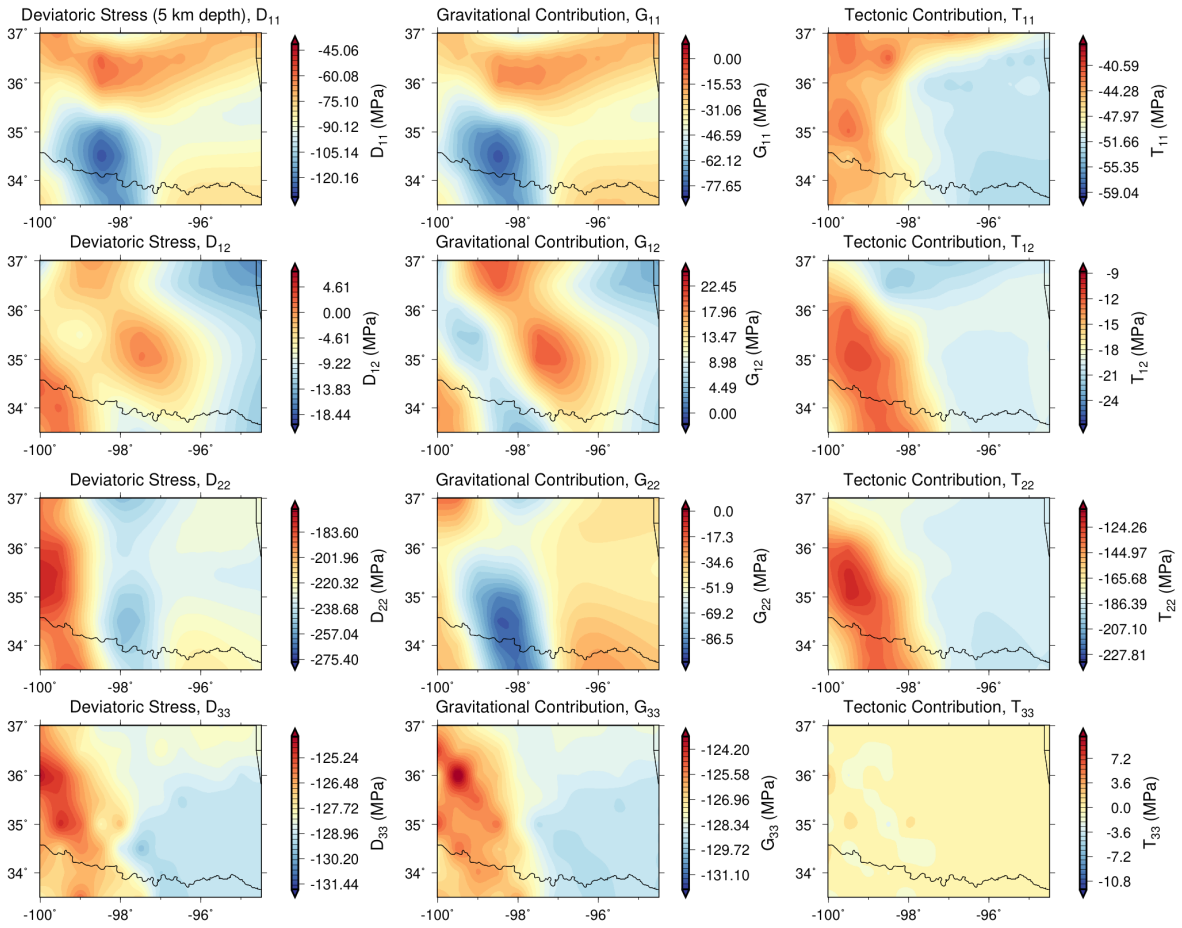

Figure 10. A comparison of magnitudes of deviatoric stress (left column) and its gravitational (middle column) and tectonic contributions (right column) at 5 km depth using the preferred stress model. The color scale changes for each image. The deviatoric stress tensor D is the sum of the gravitational contribution G and the tectonic contribution T. The first subscript is the orientation of the surface that the tensor component acts on. The second subscript of the tensor component is the direction of component. Subscript 1 represents north, 2 for east, and 3 for down.

We examine the stress field at the 5 km depth for the Oklahoma area. Comparing the horizontal component of the gravitational contribution with the tectonic contributions (Figure 10), we found the gravitational contributions to the horizontal components of the deviatoric stress field (subtracting out the hydrostatic stress) is on the same order of magnitude to the tectonic contribution. The vertical component of the stress field is dominated by the gravitational contribution. Due to spatial changes in density and elastic properties, both the gravitational

386 contributions and the tectonic contributions are non-uniform for the horizontal components. The
387 spatial distributions of gravitational and tectonic contributions show different patterns. The
388 resulting modeled deviatoric stress field shows spatial variability across Oklahoma. As a result,
389 we need to include both the gravitational and tectonic contributions in the stress field calculation,
390 which confirms previous studies for other regions (e.g., Levandowski et al., 2016; Reiter &
391 Heidbach, 2014). The tectonic contribution to stress on optimally oriented faults is between 10-
392 30 MPa within the study area; the gravitational contribution is 0-20 MPa, mostly of opposite
393 sign, but of similar magnitude.

394 We acknowledge that tectonic forces acting on the study area through the boundaries are
395 almost certainly not uniform in the Earth. But a uniform force at the boundaries is sufficient for
396 testing the hypothesis that variations from a uniform stress field in the upper crust are primarily
397 due to heterogeneous elasticity and density in the crust at local and regional scales. As our model
398 is fully elastic, we are also neglecting the effect of viscoelastic behavior in the lower crust and
399 upper mantle, which would have the effect of relaxing stresses at those depths with some time
400 dependence. Our intent in this study is to present a method to model stresses in the upper crust
401 where earthquakes and other activities occur, not calculate a stress model throughout the crust
402 and upper mantle. Earth curvature will need to be considered when applying this method to a
403 larger spatial scale.

404 Both the material model and stress model are available in the supplementary materials.

405 **5 Discussion and Conclusions**

406 We jointly inverted surface-wave dispersion, gravity, and local travel time observations
407 for a 3D elastic property model for the Oklahoma region. The material model can be further

improved with deep learning and transfer learning derived travel time observations (Chai et al., 2020). Utilizing the 3D material model, a model of the 3D stress tensor field for Oklahoma was computed by considering both gravitational and tectonic contributions. A model that includes both gravitational and tectonic components of the stress field fits observed stress indicators better than the tectonic component alone, indicating that the gravitational component helps to explain small-scale variations in principal stress orientations. We used observed stress indicators and faulting types to constrain the tectonic force orientation and magnitude equivalent. Our preferred model has a tectonic force orientation of N82°E and explains well the stress observations and the faulting types. An equivalent stress magnitude near 123 MPa (shortening of 3965 m) fits the stress observations and the faulting types better than other magnitudes. This corresponds to a deviatoric shear stress of 10-30 MPa on optimally oriented faults. The stress field in the upper 5 km due to gravitational body forces has a comparable magnitude to the tectonic-driven stress field and the modeled stress field in the Oklahoma region has significant spatial variations.

Our results demonstrate that a reliable 3D stress field for the upper crust can be computed using a 3D material model and stress observations. When previous localized stress orientation measurements and focal mechanisms are known, the orientation and magnitude of the regional tectonic forces can be constrained through stress modeling. 3D stress modeling has significant advantages over traditional methods (e.g., interpolation, extrapolation) including the ability to obtain stress magnitudes and the ability to use measurements away from boreholes and earthquake focal mechanisms. As small-scale stress variations may favor or oppose future deformation, our technique can also help with subsurface engineering problems and natural hazards. Though our model closely recovers most available stress indicators, the stress tensor continues to be a difficult property to validate, which could be done with new observations.

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454 declare that they have no conflict of interest.

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