

1 **A Deep Learning Network to Retrieve Ocean Hydrographic Profiles from Combined**
2 **Satellite and In Situ Measurements**

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9 **Key Points:**

- 10 • A novel deep learning technique to retrieve the 3D ocean hydrography combining
11 satellite and in situ observations is presented
- 12 • A stacked Long Short-Term Memory network is coupled to a Monte Carlo dropout
13 method to estimate vertical profiles and associated errors
- 14 • Applying the technique to 2010-2018 data collected in the North Atlantic leads to a
15 significant improvement in the reconstruction accuracy
- 16
17

18 **Abstract**

19 An efficient combination of the data collected by multiple instruments and platforms is needed to
20 obtain accurate 3D ocean state estimates, representing a fundamental step to describe ocean
21 dynamics and its role in the Earth climate system and marine ecosystems. Observations can
22 either be assimilated in ocean general circulation models or used to feed data-driven
23 reconstructions and diagnostic models. Here we describe an innovative deep learning algorithm
24 that projects sea surface satellite data at depth after training with sparse co-located in situ vertical
25 profiles. The technique is based on a stacked Long Short-Term Memory neural network, coupled
26 to a Monte-Carlo dropout approach, and is applied here to the measurements collected between
27 2010 and 2018 over the North Atlantic Ocean. The model provides hydrographic vertical profiles
28 and associated uncertainties from corresponding remotely sensed surface estimates,
29 outperforming similar reconstructions from simpler statistical algorithms and feed-forward
30 networks.

31

32 **Plain Language Summary**

33 Being able to monitor the ocean's interior structure is crucial to assess the impact of ocean
34 dynamics on the Earth climate and marine ecosystems. Available observations, acquired either
35 from satellite sensors looking at the sea surface or from sparse in situ measurements of the water
36 column, can only provide partial views of the 3D ocean state if analysed separately, due to their
37 instrumental and sampling limitations. Taking advantage of recent advances in artificial neural
38 network implementations, we present here a deep learning algorithm that is able to efficiently
39 exploit sensors' synergy and retrieve the vertical hydrographic structure of the sea from remotely
40 sensed data, including an estimate of associated uncertainties.

41

42 **1 Introduction**

43 Ocean dynamics comprises several processes (inter)acting over a wide range of spatial
44 and temporal scales, which may influence the Earth climate and contribute to modulate marine
45 ecosystem functioning. Notably, several crucial processes contributing to the transport of
46 momentum, energy, chemicals and marine organisms cannot be fully understood unless repeated
47 views of the 3D ocean state and surface forcings are available. This is particularly relevant for
48 processes in the mesoscale to sub-mesoscale range, given their intrinsic 3D nature (McWilliams,
49 2019; Pilo et al., 2018; Stukel et al., 2017). In turn, the dynamical response and feedbacks of
50 these processes to natural and anthropogenic pressures also remains largely uncertain. However,
51 given both theoretical and practical limitations of available technologies, observations can only
52 provide partial views of the ocean state, especially if analysed separately. Monitoring 3D ocean
53 processes from observation-based reconstructions thus requires ingenious combinations of data
54 acquired from different sensors looking at the sea surface from space, and from sparse in situ
55 measurements collected throughout the water column.

56 Scientists have followed two main complementary approaches to provide a description of
57 3D ocean dynamics: the assimilation of observations in numerical models and the combination
58 of purely data-driven reconstructions and diagnostic models. Both strategies are affected by
59 strengths and weaknesses, though.

60 The data assimilation in prognostic models can guarantee the ocean state to evolve in a
61 consistent way with the physics represented by the model (Carrassi et al., 2018; Moore et al.,
62 2019; Stammer et al., 2016). Models, however, are affected by uncertainties in initialization and
63 forcings, and need parameterizations of sub-grid scale processes, which may lead to inaccurate
64 representations of the physics, especially when aiming to reconstruct long timeseries for
65 decadal/climatological studies (due to grid size limitations and subsequent need to parameterize
66 also mesoscale processes, e.g. Forget et al., 2015). In general, models' ability to reproduce non-
67 assimilated observations is further hindered by the difficulty to properly account for model and
68 observation representativeness and errors.

69 Data-driven approaches are based on a synergic use of different satellite, in-situ
70 measurements and diagnostic models. They can reduce the differences between reconstructed
71 and independent observations (for 2D examples see Ciani et al., 2020; Rio et al., 2016;
72 Ubelmann et al., 2016), but usually allow only a much simpler description of the dynamics with
73 respect to general circulation models (sometimes limited to zero or first order balances, as
74 geostrophy and quasi-geostrophy, or simple Ekman models). Data-driven 3D reconstruction
75 techniques that found a systematic application are based on purely empirical and/or statistical
76 regressions/analyses (Buongiorno Nardelli et al., 2012, 2017, 2018; Guinehut et al., 2004, 2012;
77 Hutchinson et al., 2016; Meijers et al., 2011; Meinen and Watts, 2000), eventually coupled to
78 dynamical diagnostic tools (for full 3D examples see Mulet et al., 2012; Buongiorno Nardelli,
79 2020). Methodologies derived within the surface quasi-geostrophy framework make much
80 stronger assumptions on the ocean vertical stratification, though providing interesting theoretical
81 perspectives (Fresnay et al., 2018; Isern-Fontanet and Hascoët, 2014; LaCasce and Wang, 2015;
82 Lapeyre, 2017; Liu et al., 2019; Wang et al., 2013). More recently, mixed approaches have also
83 been explored (Yan et al., 2020).

84 All data driven approaches share the objective to project surface information at depth,
85 starting from synoptic satellite observations and some prior knowledge of the hydrography.
86 Despite the recent advancements in machine learning algorithms implementation and a growing
87 interest in the possibilities opened by artificial intelligence for data science, only few attempts
88 have been carried out until now to address this specific objective with artificial neural networks
89 (e.g. Bao et al., 2019; Gueye et al., 2014; Lu et al., 2019; Sammartino et al., 2018; Wu et al.,
90 2012), either based on generalized regression neural networks, self-organizing maps or feed-
91 forward neural networks. Models based on neural networks have also been proposed to
92 "augment" observed vertical profiles with variables that have not been directly measured (e.g.
93 Ballabrera-Poy et al., 2009; Bittig et al., 2018; Sauzède et al., 2016, 2017).

94 In this paper, a stacked Long Short-Term Memory (LSTM, Hochreiter and Schmidhuber,
95 1997) network is coupled to a Monte Carlo dropout approach and used to project surface data at
96 depth after training with sparse co-located in situ vertical profiles. LSTM is a deep learning
97 algorithm particularly suited to exploit sequential information as those present in hydrographic
98 profiles. Dropout provides both a regularization strategy, when applied during training, and a
99 "Bayesian" inference approximation if applied during both training and testing (Gal and
100 Ghahramani, 2016). As such, the technique proposed here is able to provide both vertical
101 hydrographic profiles and uncertainties on the predicted values.

102 This work was carried out within the European Space Agency World Ocean Circulation
103 project (ESA-WOC), as a preparatory step for the development of a daily 3D reconstruction of
104 the dynamics in the North Atlantic (down to 1500 m depth) at $1/10^\circ$ spatial resolution, covering

105 the period between 2010 and 2018. As such, the network was trained and tested taking as target
106 (output) the measurements collected by Argo profilers and CTD casts within a wide portion of
107 the North Atlantic over that period. Co-located satellite-derived sea surface temperature, sea
108 surface salinity and absolute dynamic topography values (extracted from operational and
109 experimental products) were used as input data.

110 The performance of the proposed LSTM network has been assessed by keeping part of
111 the in situ profiles as independent reference observations during test. Root mean squared errors
112 have been estimated from LSTM profiles, from climatological data and multivariate Empirical
113 Orthogonal Function reconstructions (mEOF-r, as in Buongiorno Nardelli et al., 2017), as well as
114 from the output of simpler feed-forward networks.

115

116 **2 Data**

117 2.1 Surface data

118 The SST used in the present study is the level 4 (L4, i.e. interpolated) multi-year
119 reprocessed Operational Sea Surface Temperature and Sea Ice Analysis (OSTIA) developed by
120 U.K. Met Office and distributed (upon free registration) through the Copernicus Marine
121 Environment Monitoring Service (CMEMS, [http://marine.copernicus.eu/services-
122 portfolio/access-to-products/](http://marine.copernicus.eu/services-portfolio/access-to-products/),
123 product_id=SST_GLO_SST_L4_REP_OBSERVATIONS_010_011). OSTIA combines the
124 reprocessed ESA SST CCI, C3S, EUMETSAT, REMSS and OSPO satellite data, and in-situ
125 data from HadIOD and provides daily maps of foundation SST (i.e. not affected by the diurnal
126 cycle). The analysis runs an optimal interpolation (OI) algorithm on a $1/20^\circ$ regular grid
127 (Roberts-Jones et al., 2012). OSTIA was sub-sampled here to $1/10^\circ$ resolution, and resulting grid
128 was used also for the pre-processing of the other surface datasets (see the SST example in figure
129 1a).

130 The SSS data have been developed within ESA-WOC project
131 (<https://doi.org/10.5281/zenodo.3943813>). They have been obtained by adapting to the $1/10^\circ$
132 North Atlantic grid the multidimensional optimal interpolation algorithm used to retrieve
133 CMEMS global dataset (<http://marine.copernicus.eu/services-portfolio/access-to-products/>,
134 product_id: MULTIOBS_GLO_PHY_REP_015_002, dataset_id: dataset-sss-ssd-rep-weekly).
135 This algorithm interpolates SMOS observations and in situ SSS observations considering a
136 space-time-thermal decorrelation function, estimated by including information from high-pass
137 filtered daily SST data (Droghei et al., 2016; Buongiorno Nardelli, 2012). This multivariate
138 approach effectively increases the SSS resolution by using satellite SST differences to constrain
139 the surface patterns (see figure 1b). Here, we ingested the SMOS L3OS 2Q debiased daily
140 salinity disseminated by the Centre Aval de Traitement des Données SMOS (CATDS, 2017),
141 OSTIA SST data and CORA5.2 surface values (see section 2.2) as input data, and used CMEMS
142 weekly SSS dataset to build our background field (linearly interpolating it in time between the
143 two closest analysis dates, and upsizing to the $1/10^\circ$ grid through a cubic spline). All other
144 interpolation parameters are set as in Droghei et al. (2018).

145 The Absolute Dynamic Topography (ADT) data considered here are based on the
146 altimeter Sea Level Anomaly (SLA) product provided by SSALTO/Data Unification and
147 Altimeter Combination System (DUACS). They are obtained by adding a Mean Dynamic

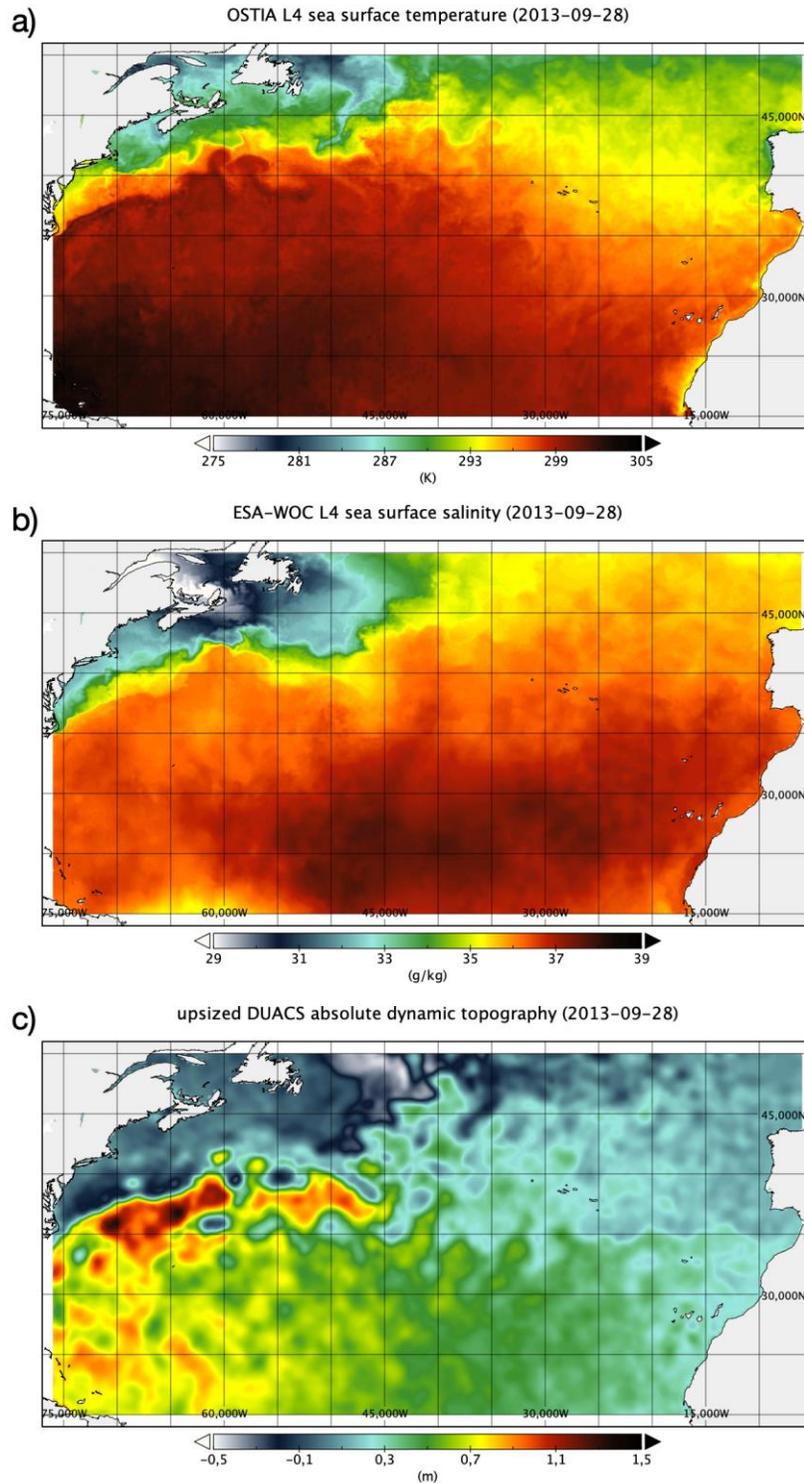
148 Topography (Rio et al., 2014) to the SLA field, and are distributed by CMEMS as reprocessed
149 data (<http://marine.copernicus.eu/services-portfolio/access-to-products/>, product_id:
150 SEALEVEL_GLO_PHY_L4_REP_OBSERVATIONS_008_047). ADT has been upsized here
151 to the ESA-WOC $1/10^\circ \times 1/10^\circ$ grid through a cubic spline (see example in figure 1c). ADT data
152 have been pre-processed to make them consistent with insitu steric heights. The adjustment is
153 carried out as in Buongiorno Nardelli et al. (2017), namely by regressing steric heights and co-
154 located ADT data in the neighbourhood of each grid point, considering matchups within a
155 temporal window of ± 10 days.

156 2.2 Vertical profiles

157 The vertical hydrographic profiles have been taken from the quality controlled Argo and
158 CTD profiles produced by CMEMS CORA 5.2 ([http://marine.copernicus.eu/services-
159 portfolio/access-to-products/](http://marine.copernicus.eu/services-portfolio/access-to-products/), product_id:
160 INSITU_GLO_TS_REP_OBSERVATIONS_013_001_b, doi: 10.17882/46219TS1, Szekely et
161 al., 2019). The data considered here are restricted to the 2010-2018 period, and were interpolated
162 through a spline on a regularly spaced vertical grid (with 10 m intervals). Steric heights have
163 been computed taking 1500 m as reference level.

164 2.3 Climatology

165 Temperature and salinity monthly climatological fields computed by the World Ocean
166 Atlas 2013 have been used to convert all daily observations to anomaly fields (see section 3).
167 These climatologies are estimated on a $1/4^\circ \times 1/4^\circ$ grid by applying an objective analysis
168 algorithm (Locarnini et al., 2013; Zweng et al., 2013). The values in the first 1500 m, provided
169 on 125 levels, have been interpolated through a spline on a regularly spaced vertical grid (with
170 10 m intervals), and upsized to the $1/10^\circ$ ESA-WOC grid through a cubic spline.



171

172 **Figure 1.** Examples of the surface daily data taken as input to the reconstruction techniques:
173 OSTIA L4 reprocessed SST (a), SSS L4 developed within ESA-WOC project (b), adjusted ADT
174 L4 derived from DUACS data (c).

175 **3 Reconstruction techniques**

176 3.1 Multivariate Empirical Orthogonal Function reconstruction (mEOF-r)

177 The multivariate Empirical Orthogonal Function reconstruction (mEOF-r) was taken as
178 reference for the retrieval of the 3D hydrographic fields. This methodology has been applied in
179 many previous studies (Buongiorno Nardelli, 2013; Buongiorno Nardelli et al., 2006, 2012,
180 2017; Buongiorno Nardelli and Santoleri, 2005), and it is thus only briefly recalled hereafter. It
181 starts by building a state vector by concatenating (normalized) temperature, salinity and steric
182 heights anomaly profiles, and decomposing its variability in EOF modes (thus called multivariate
183 EOF). Anomalies are defined with respect to monthly WOA13 data (linearly interpolated in time
184 between the central day of each month, and through a cubic spline horizontally). The EOFs are
185 computed from available in situ observations, and the decomposition is truncated to a maximum
186 of three modes. The three elements in the state vector reconstructed from the truncated EOF that
187 correspond to the surface are equated to the anomalies of SST, SSS and adjusted ADT. In this
188 way, a linear system is obtained, the unknowns being the three EOF amplitudes. Once solved
189 through a trivial matrix inversion, full profiles associated with each mode can be estimated and
190 finally summed up to get the synthetic vertical reconstruction.

191 In order to account for local differences in the dynamics, the configuration proposed in
192 Buongiorno Nardelli et al., (2017) has been adopted also here. The North Atlantic domain is
193 divided into subdomains with a maximum extension of 30° both in latitude and in longitude.
194 Multivariate EOFs are estimated considering only the in situ profiles collected within ± 20 days
195 with respect to the reconstruction day. To remove eventual discontinuities in the reconstruction,
196 all neighbouring subdomains are overlapped by one half of their latitudinal and longitudinal
197 extensions. In the grid points where multiple reconstructions are available, these are averaged out
198 by bilinearly weighting them with the inverse of the distance to each subdomain centre. In some
199 cases, two modes (or even one mode) may be sufficient to retrieve most of the variability and the
200 reconstruction error may increase if more modes are added (more than 95% of the variance is
201 generally explained by the selected modes). Consequently, the optimal number of modes for the
202 3D reconstruction is chosen by evaluating the mean hindcast error within each subdomain, so as
203 to minimize the root mean square difference between the input profiles and the synthetic profiles
204 reconstructed from corresponding in situ surface measurements.

205 3.2 Feed-forward neural networks

206 Feed-forward networks represent the simplest type of artificial neural networks and
207 consist of one input layer (the input vector) and one output layer (the output vector) connected
208 through a variable number of hidden layers (if that number is >1 we speak about a “deep
209 network”). Each of the layers is made up by a variable number of units: the elements of the
210 vectors in the case of the input/output layers, and the artificial “neurons” (or computing nodes) in
211 the hidden layers. Each of the units in one layer is connected to all units in the following layer
212 through weights that are estimated during the network training, and each computing node
213 processes the sum of its weighted input by passing it through an activation function which
214 provides the neuron’s output. FFNN networks are designed to model complex flows of
215 information from the input to the output and are common candidates to solve non-linear
216 regression problems. The definition of a proper model for each specific problem, however,
217 requires optimizing the choice of several “hyper-parameters”, starting from the number of hidden

218 layers, the number of units within each hidden layer, to the activation function to apply within
219 each hidden layer. For a given architecture, network training also implies a number of additional
220 choices. In fact, training is performed by minimising some model loss function while iteratively
221 feeding the network with several input-output samples. Various algorithms exist to this aim, and
222 the same network trained in a different way on the same data may indeed lead to different results
223 ("local" optima). Different results can be obtained depending also on the number of iterations
224 (epochs) considered.

225 Large feed-forward networks (in terms of number of layers/units) are prone to over-
226 fitting, as distinct sets of neighbouring neurons might adjust to reproduce individual samples,
227 leading to complex co-adaptations which would not allow to generalize the network to unseen
228 data. Again, different strategies can be followed to avoid co-adaptation: the dropout approach
229 followed here is described in section 3.4.

230 In our tests, two different input/output vectors have been initially considered. In the first
231 case, somehow imitating simple multilinear regression approaches, the input vector was made up
232 of: the target depth for the retrieval, the anomalies of SST, SSS and adjusted ADT (same as in
233 mEOF-r), the latitude, longitude, and the day of the year projected on a circle (as in Sammartino
234 et al., 2018), while the output included the co-located values of temperature, salinity and steric
235 heights anomalies at the target depth. In the second configuration, the depth has been dropped
236 from the input data and the concatenated temperature, salinity and steric heights anomaly profiles
237 were taken as output (same as mEOF-r state vector). All vectors are preliminary normalized
238 through min-max algorithm.

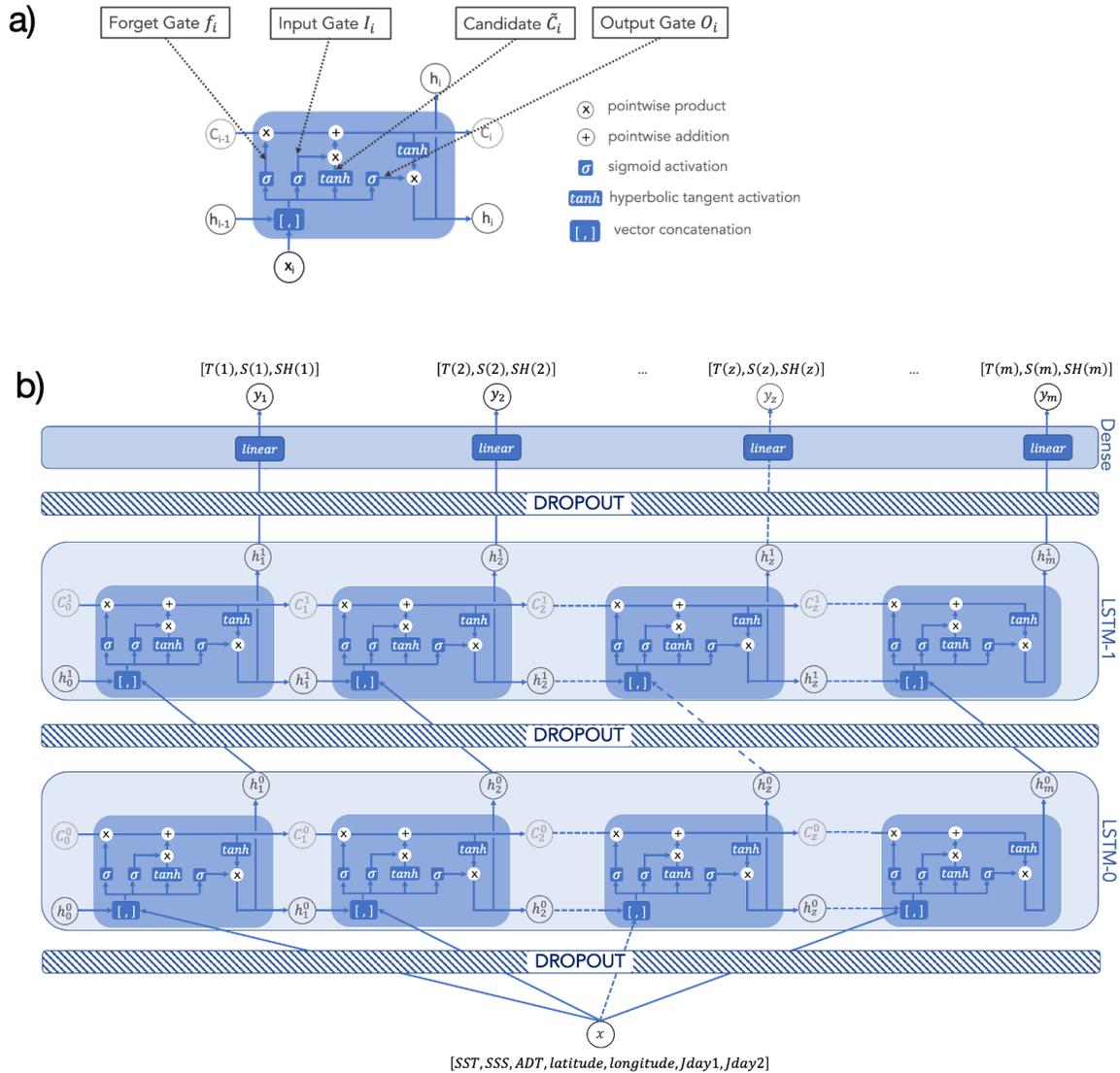
239 Several preliminary hyper-parameter tuning tests have been carried out, considering one
240 to three hidden layers, and a variable number of units within each, ranging between 5 and 50,
241 with a 5 units increase step. The sigmoid performed better than hyperbolic tangent as activation
242 function. "Adam" was selected as network optimizer, taking the mean squared error as loss
243 metrics. 15% of input samples were randomly kept as a holdout validation dataset at each
244 iteration. The number of optimal training epochs was found by monitoring model performance
245 (*early stopping*).

246 The performance of the first set of models (those retrieving values at individual depths)
247 never improved with respect to the climatology, while a visible improvement was found in the
248 second configuration, especially when the choosing two hidden layers. The successive tests were
249 thus restricted to this latter configuration, significantly increasing the number of hidden units
250 (tests were run with up to 5000 units per layer). The final FFNN architecture considered in the
251 following, which further improved the reconstruction accuracy) includes 1000 units in the two
252 hidden layers (above that number, performance substantially stabilized).

253 3.3 Long Short-Term Memory networks

254 Recurrent neural networks (RNN) can be described as sequences of sub-networks (also
255 called "cells") designed to include information from the previous cell in a sequence as input to
256 the successive one. This makes them particularly fit to model ordered sequences of data. Simple
257 recurrent networks, however, are not able to efficiently process information from cells that lie
258 too far along the sequence, due to vanishing/exploding values in the gradient-descent based
259 optimizations.

260 Long Short-Time Memory (LSTM) network is a particular type of RNN, that is
 261 specifically designed to avoid vanishing/exploding gradients and preserve the relevant
 262 information flow throughout the network (Hochreiter and Schmidhuber, 1997). Within LSTM
 263 cells, the external input vector (x_i) is concatenated to the previous cell hidden state (h_{i-1}) and then
 264 passed through different "gates", each one aimed at carrying out a specific task to update both the
 265 hidden state itself (h_i) and a cell state (C_i), that is directly transmitted to the next cell and
 266 basically acts as a network "memory". The LSTM cell specifically includes a forget gate, an
 267 input gate, and an output gate, as depicted in figure 2a:



268
 269 **Figure 2.** Diagram showing the elements of a single LSTM cell (a). Stacked LSTM model for
 270 the reconstruction of vertical hydrographic profiles (b).

271

272 whose equations thus read:

$$f_i = \sigma(W_f[h_{i-1}, x_i] + b_f)$$

$$\begin{aligned}
I_i &= \sigma(W_I[h_{i-1}, x_i] + b_I) \\
\tilde{C}_i &= \tanh(W_C[h_{i-1}, x_i] + b_C) \\
O_i &= \sigma(W_O[h_{i-1}, x_i] + b_O) \\
C_i &= f_i * C_{i-1} + I_i * \tilde{C}_i \\
h_i &= O_i * \tanh(C_i)
\end{aligned}$$

273 where σ and \tanh represent the sigmoid and hyperbolic tangent activation functions,
274 respectively.

275 LSTM networks can include a single layer of LSTM cells or multiple LSTM layers
276 stacked one on top of the other, potentially leading to quite deep architectures. The number of
277 cells in each layer matches the length of the sequence by definition, but the number of hidden
278 units still needs to be configured.

279 Here, the sequential information to exploit is provided by a multivariate output state
280 vector comprising temperature, salinity and steric height anomaly profiles. In practice, each cell
281 in the sequence considers in input the same surface values (i.e. the anomalies of SST, SSS and
282 adjusted ADT), but takes as the output values at increasing depths (with depth “acting” as time in
283 more standard applications of LSTM). As for FFNN models, all vectors are scaled within the 0-1
284 range before feeding the network.

285 The number of hidden units considered ranged between 5 and 50, with a 5 units increase
286 step, and three different network architectures have been tested: a simple LSTM and two stacked
287 LSTMs (with 2 and 3 layers each). The optimization algorithm and related parameters were
288 exactly the same used for the FFNN reconstruction training, as well as the dropout strategy
289 applied to avoid overfitting and obtain reconstructed profile uncertainties (see next section).

290 The best performance was obtained with a 2-layers stacked network, including 35 hidden
291 units in each LSTM layer, as depicted in figure 2b.

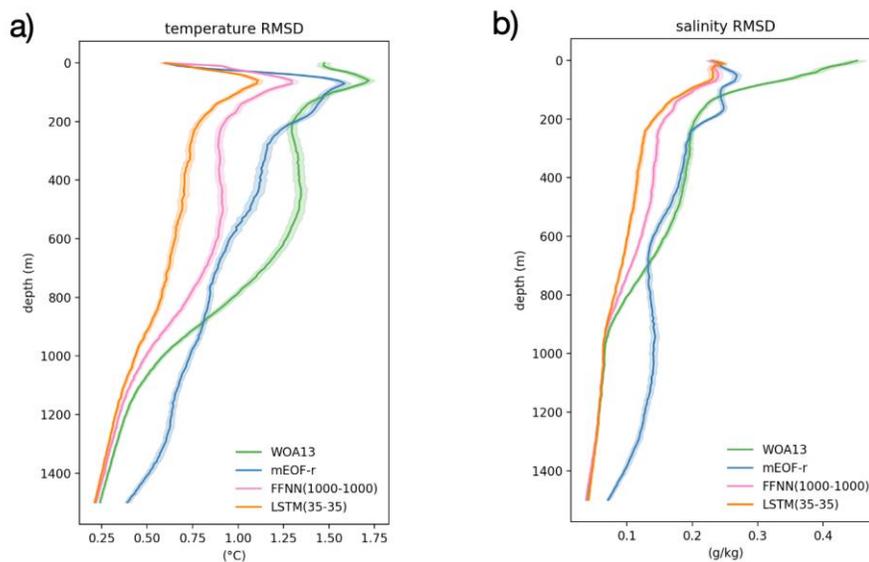
292 3.4 Monte-Carlo Dropout

293 Standard dropout consists in randomly excluding a percentage of units during network
294 training. Dropout provides a very efficient regularization strategy if applied during training,
295 significantly reducing the risk of co-adaptation, thus limiting overfitting and improving model
296 performance (Hinton et al., 2012; Srivastava et al., 2014). Moreover, dropout provides also an
297 extremely simple and powerful approach to quantify a neural network uncertainty, if applied
298 during both training and testing. In fact, running a regression neural network several times with
299 dropout during testing generates different output for the same input. It was shown
300 mathematically that these output are equivalent to Monte-Carlo sampling (Gal and Ghahramani,
301 2016). Hence, ensemble mean and variance provide the network’s output values and related
302 uncertainty, respectively. During learning, 20% of the units have been dropped here.

303 4 Technique assessment

304 The assessment of the techniques has been performed by estimating temperature and
305 salinity root mean squared differences (RMSD) with respect to fully independent test data
306 (fig.3). To this aim, a randomly selected 15% of the 35344 in situ profiles collected in the area

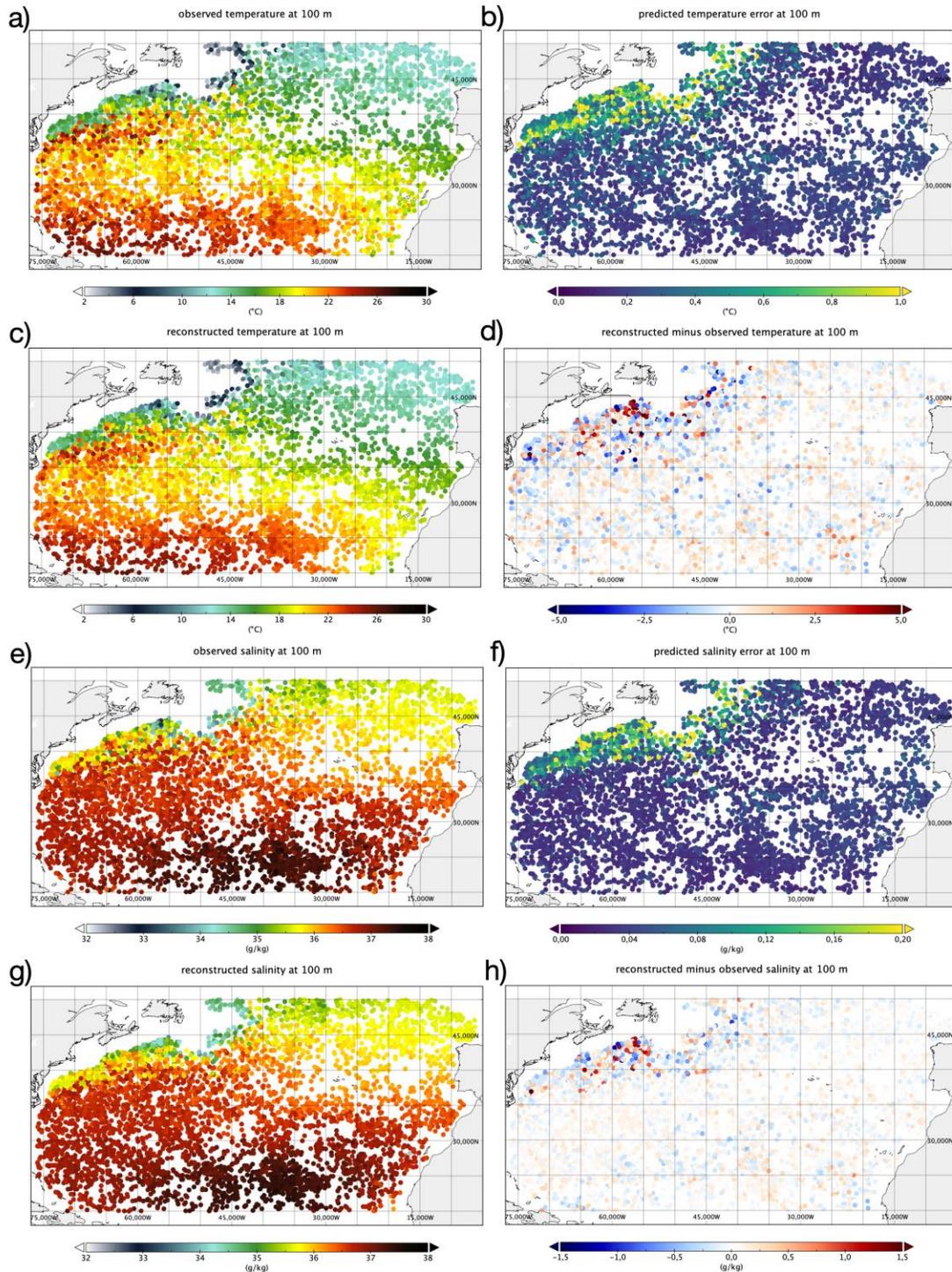
307 (totalling 5125 profiles) have been excluded from the network training. All techniques
 308 considered process anomalies with respect to WOA13 data, and are thus intended as corrections
 309 to the climatological profiles. Climatological temperature RMSD attains around 1.5°C at the
 310 surface, reaches a maximum of up to 1.7°C at ~100 m depth (at the base of the upper mixed
 311 layer) and then gradually decreases to the minimum error <0.25 °C at 1500 m, with a wide
 312 secondary maximum positioned around 500 m characterized by errors >1°C down to 800 m. The
 313 temperature retrieved with mEOF-r shows a moderate improvement in the upper 100 m and then
 314 in the 200-900 m layer, but then significantly degrades the climatology below 900 m.
 315 Conversely, both the FFNN with 2 hidden layers (each with 1000 units) and the stacked LSTM
 316 (with 2 layers and 35 hidden units in each cell) significantly improve the reconstruction all along
 317 the water column. Noticeably, LSTM clearly outperforms any of the other methodologies, with a
 318 RMSD never exceeding 1°C, and attaining below 0.75°C already at 200 m depth. Salinity RMSD
 319 show similar behaviours, with the climatological estimates reaching up to ~0.5 g/kg, and
 320 remaining above 0.2 in the upper 600 m, the mEOF-r displaying only a partial improvement in
 321 the upper 100 m (keeping its error close to that associated with the surface input data, i.e. around
 322 0.25 g/kg), and FFNN and LSTM reducing the RMSD to almost one half, the LSTM further
 323 improving in the 200-800 m layer (fig. 3b).



324

325 **Figure 3.** RMSD between temperature (a) and salinity (b) climatological and reconstructed
 326 profiles. RMSD confidence intervals (one σ) have been estimated with bootstrapping, and they
 327 are displayed here as shadowed areas.

328



329

330 **Figure 4.** Independent observations of temperature (a) and salinity (e) at 100 m depth and
 331 corresponding LSTM reconstructions (c, g); temperature (b) and salinity (f) predicted LSTM
 332 reconstruction error and temperature (d) and salinity (h) differences between test data and
 333 synthetic reconstructions at 100 m.

334 As anticipated, the neural network methods coupled with Monte-Carlo dropout present
 335 another significant advantage with respect to mEOF-r and similar statistical reconstruction

336 techniques, being able to deliver not only retrieved values, but also associated uncertainties.
337 Comparing RMSD predicted by the LSTM with observed differences between test data and
338 synthetic reconstructions at 100 m shows consistent patterns (clearly related to the areas where
339 mesoscale variability is strongest, i.e. the Gulf Stream), both in the temperature and salinity
340 fields (fig.4).

341 **5 Conclusions**

342 We have developed an innovative deep learning algorithm to project sea surface satellite
343 observations at depth after learning from sparse co-located in situ hydrographic data. The
344 proposed technique, based on a stacked Long Short-Term Memory neural network, coupled to a
345 Monte-Carlo dropout approach, provides vertical profiles and associated uncertainties,
346 outperforming both neural network reconstructions based on simpler feed-forward networks and
347 multivariate EOF reconstruction. This technique will find immediate application for the
348 development of a 3D product covering the North Atlantic in the framework of the European
349 Space Agency World Ocean Circulation project (ESA-WOC). The work described here,
350 however, covers only the development and assessment of the LSTM reconstruction methodology
351 based on presently available data, as a new training of the network will be needed once updated
352 ADT estimates will be made available by the project.

353 Remarkably, adaptation of this technique to other areas/periods is easy and
354 straightforward. Simultaneous availability of uncertainties associated with individual profiles
355 also suggests that this deep learning methodology could be tested to extend present data
356 assimilation approaches in numerical models by ingesting consistent remotely sensed sea surface
357 data and synthetic profile estimates.

358 **Acknowledgments, Samples, and Data**

359 I thank Daniele Ciani for providing upsized ADT data remapped over the study area, and
360 Michela Sammartino and Francesca Elisa Leonelli for helpful discussions at the initial stage of
361 the study.

362 The data used for the technique assessment can be found at
363 <https://doi.org/10.5281/zenodo.3943700>.

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