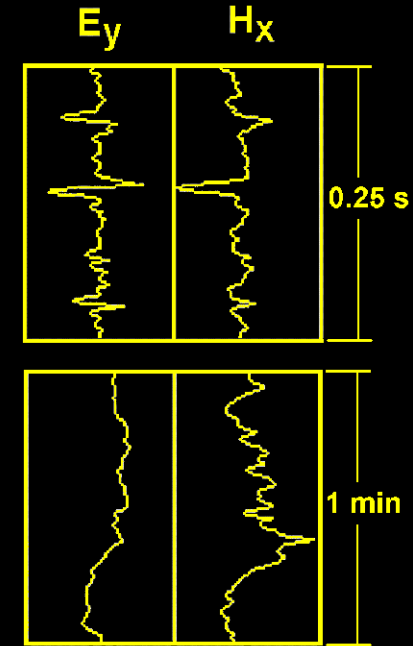
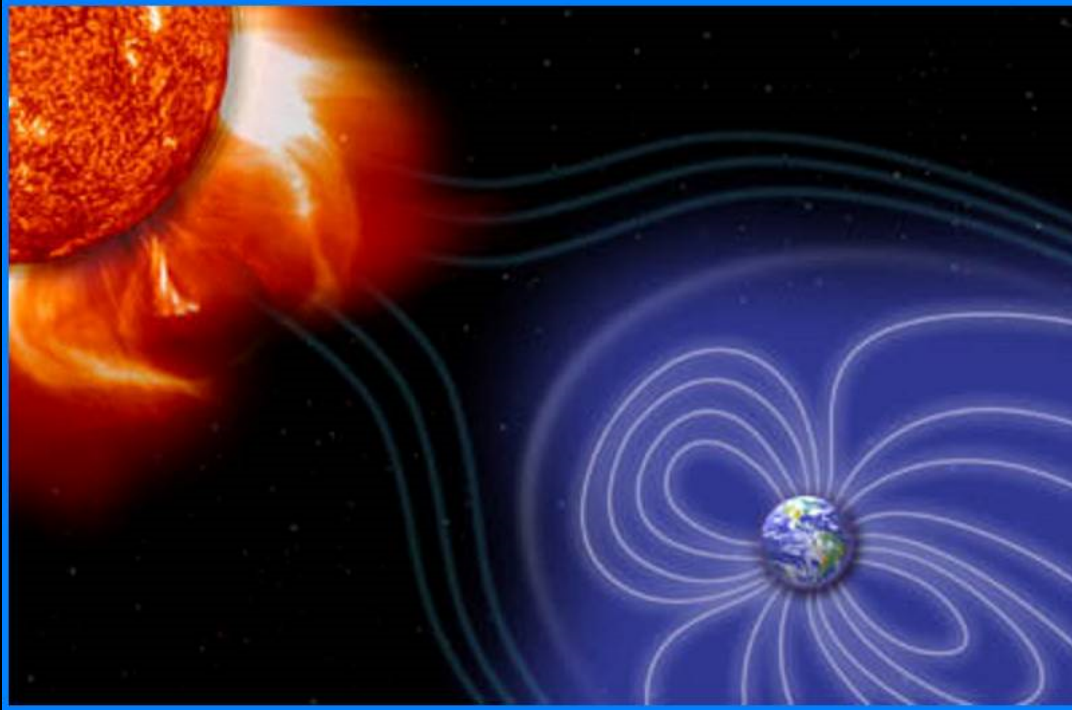




## **Development and Prospects of Continental-Scale Resistivity Surveying for Orogenic Processes and Resource Controls**

**Philip E. Wannamaker, University of Utah/EGI,  
423 Wakara Way, Ste 300, Salt Lake City, USA**

## Source Fields for the Magnetotelluric Method



Regional and Global Lightning Activity for  $f > 1$  Hz  
Solar Wind-Magnetospheric Interactions for  $f < 1$  Hz



# Outline

## Incl. Historical Perspectives

-MT Concepts Dev at MIT (T. Madden)

Tensor relation, Current Channeling,  
Staggered Grid 3D Modeling

*Vertical current channeling insights into  
crustal rheology and geothermal systems,  
Current 3D inversion platforms*

-Concepts Dev at UT Austin (F. Bostick)

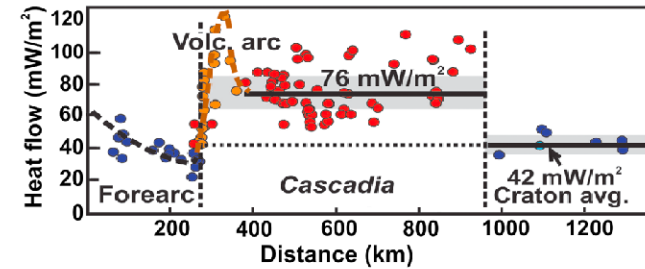
Spectral Estimation, Cascade Decimation,  
Electromagnetic Array Profiling

*Coherency sorting, Ultra-remote  
referencing*

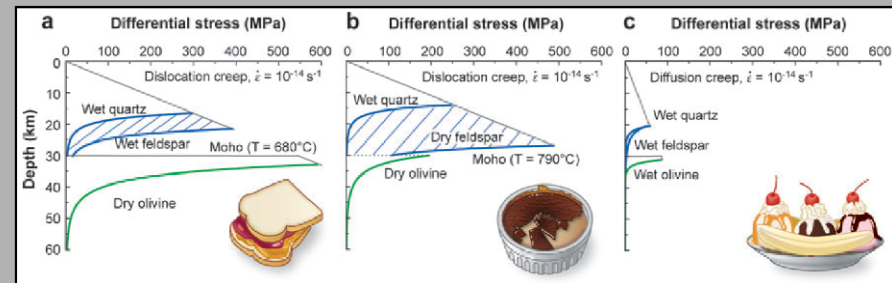
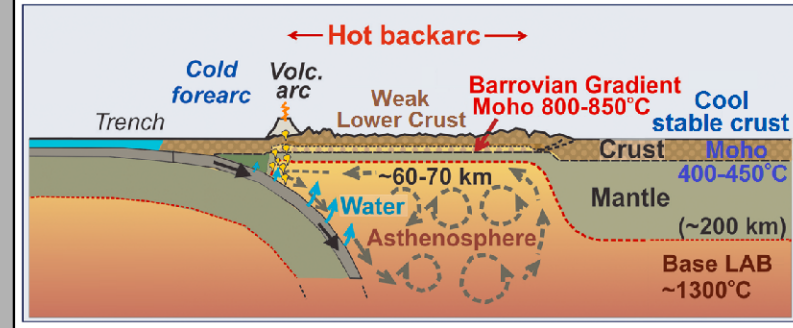
-Aqueous phase controls in lower crust  
and upper mantle

-MT surveying in polar regimes

## Subduction/Backarc Extension and Continental Growth



Modified from  
Hyndman (2018)



Burgmann and Dresen (2008)

$$\begin{aligned} H_2 &= \alpha_{21}E_1 + \alpha_{22}E_2 \\ H_1 &= \alpha_{11}E_1 + \alpha_{12}E_2 \end{aligned}$$

Cantwell (1960, MIT)  
Recognition of need for  
tensor relation

$$\begin{aligned} \begin{pmatrix} I \\ II \end{pmatrix} & \quad \begin{pmatrix} I \\ II \end{pmatrix} & \quad \begin{pmatrix} I \\ II \end{pmatrix} \\ \Phi_{h_1 h_1}(\theta) &= Y_{11}(\theta) \Phi_{h_1 e_1}(\theta) + Y_{12}(\theta) \Phi_{h_1 e_2}(\theta) \\ \begin{pmatrix} I \\ II \end{pmatrix} & \quad \begin{pmatrix} I \\ II \end{pmatrix} & \quad \begin{pmatrix} I \\ II \end{pmatrix} \\ \Phi_{h_2 h_2}(\theta) &= Y_{21}(\theta) \Phi_{h_2 e_1}(\theta) + Y_{22}(\theta) \Phi_{h_2 e_2}(\theta) \end{aligned}$$

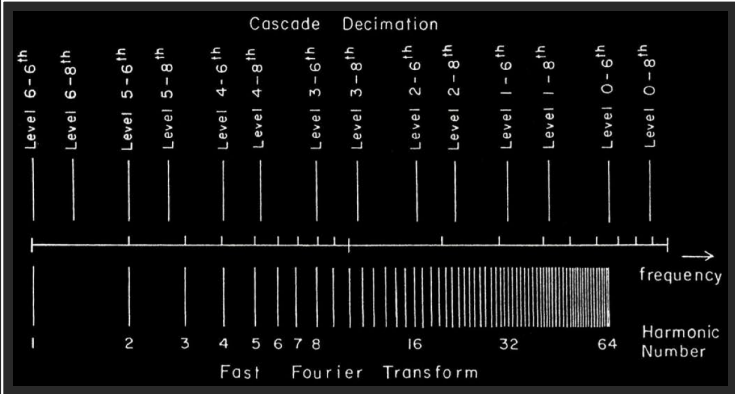
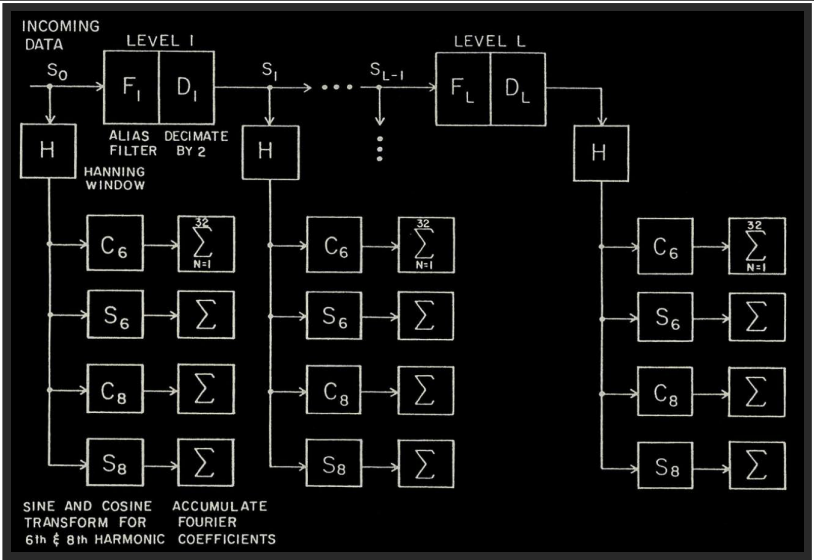
$$\begin{aligned} E_j(\theta) &= \beta_{jk} E_k(0) \\ H_i(\theta) &= \beta_{ik} H_k(0), \quad [\beta_{ik}] = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \end{aligned}$$

Bostick and Smith (1962, UTA)  
Impedance elements from spectral cross powers

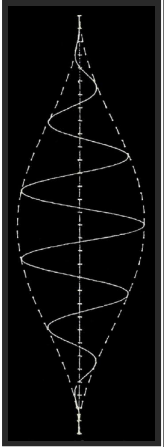
$$Z_{xy} = \frac{(\mathbf{H}_x \mathbf{H}_x^*) (\mathbf{E}_x \mathbf{H}_y^*) - (\mathbf{E}_x \mathbf{H}_x^*) (\mathbf{H}_x \mathbf{H}_y^*)}{(\mathbf{H}_x \mathbf{H}_x^*) (\mathbf{H}_y \mathbf{H}_y^*) - (\mathbf{H}_y \mathbf{H}_x^*) (\mathbf{H}_x \mathbf{H}_y^*)}$$

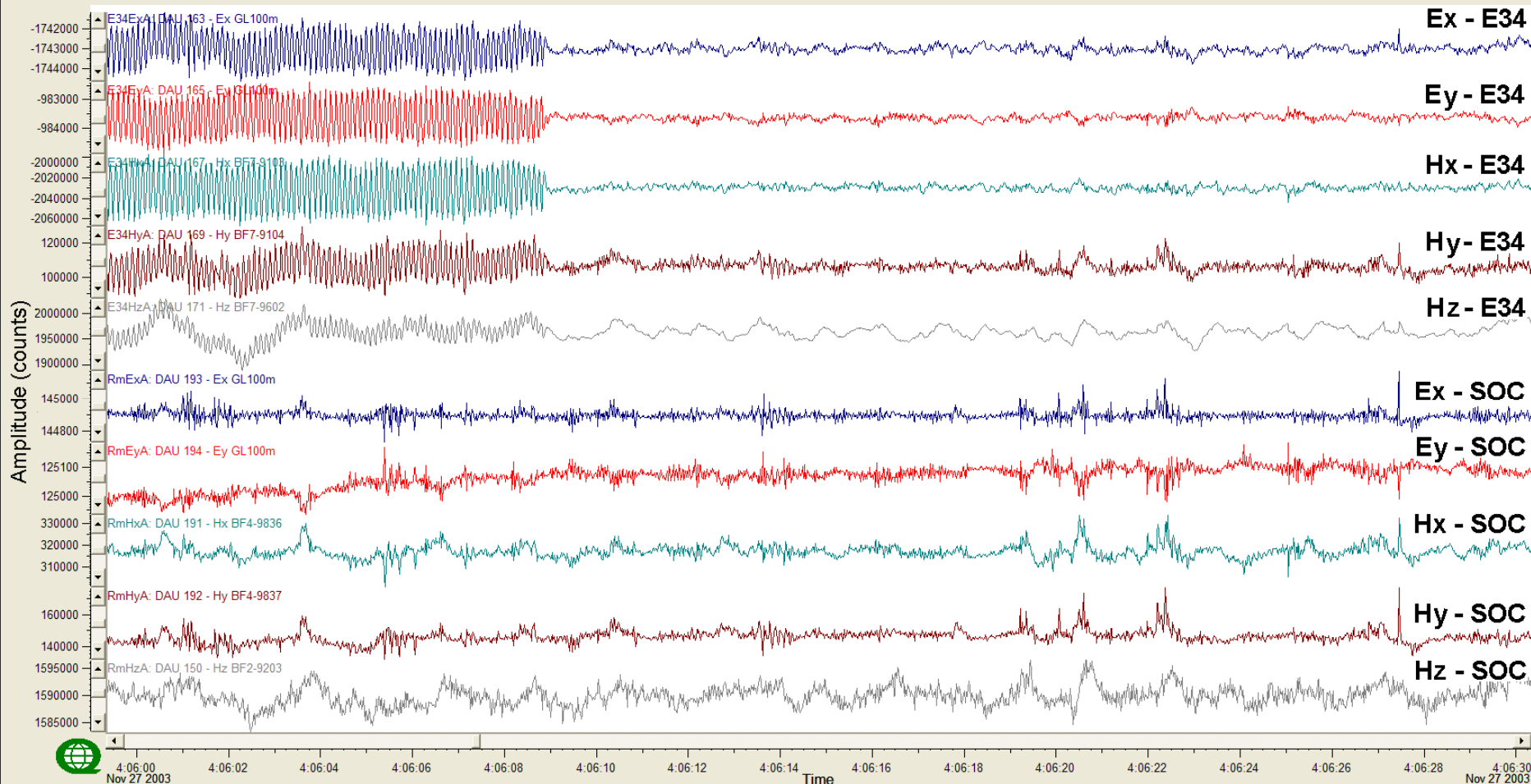
Sims et al  
(1971)

Wight et al (1977, UTA)  
Cascade decimation and RT FT



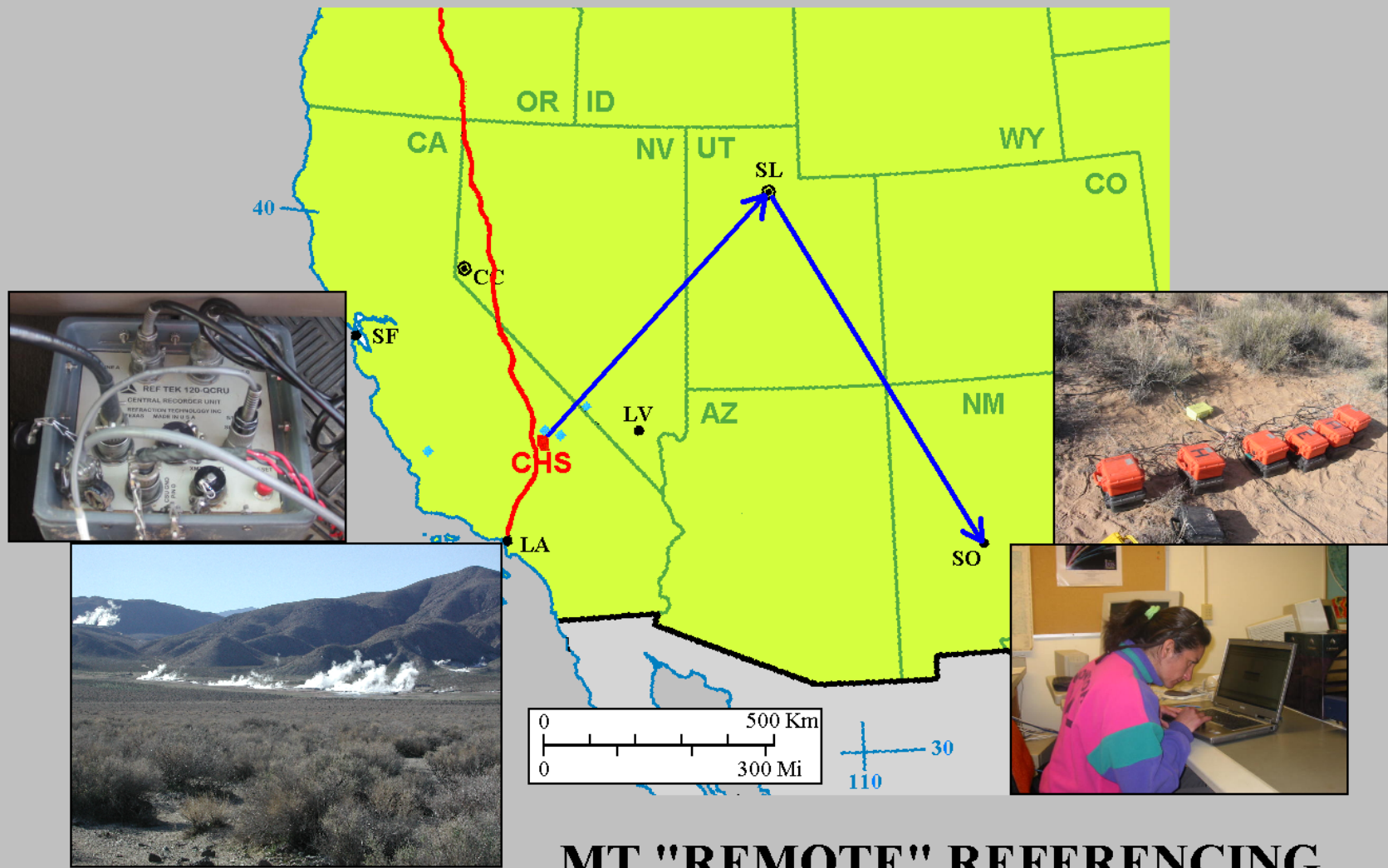
Cascade vs FFT log frequency spacing





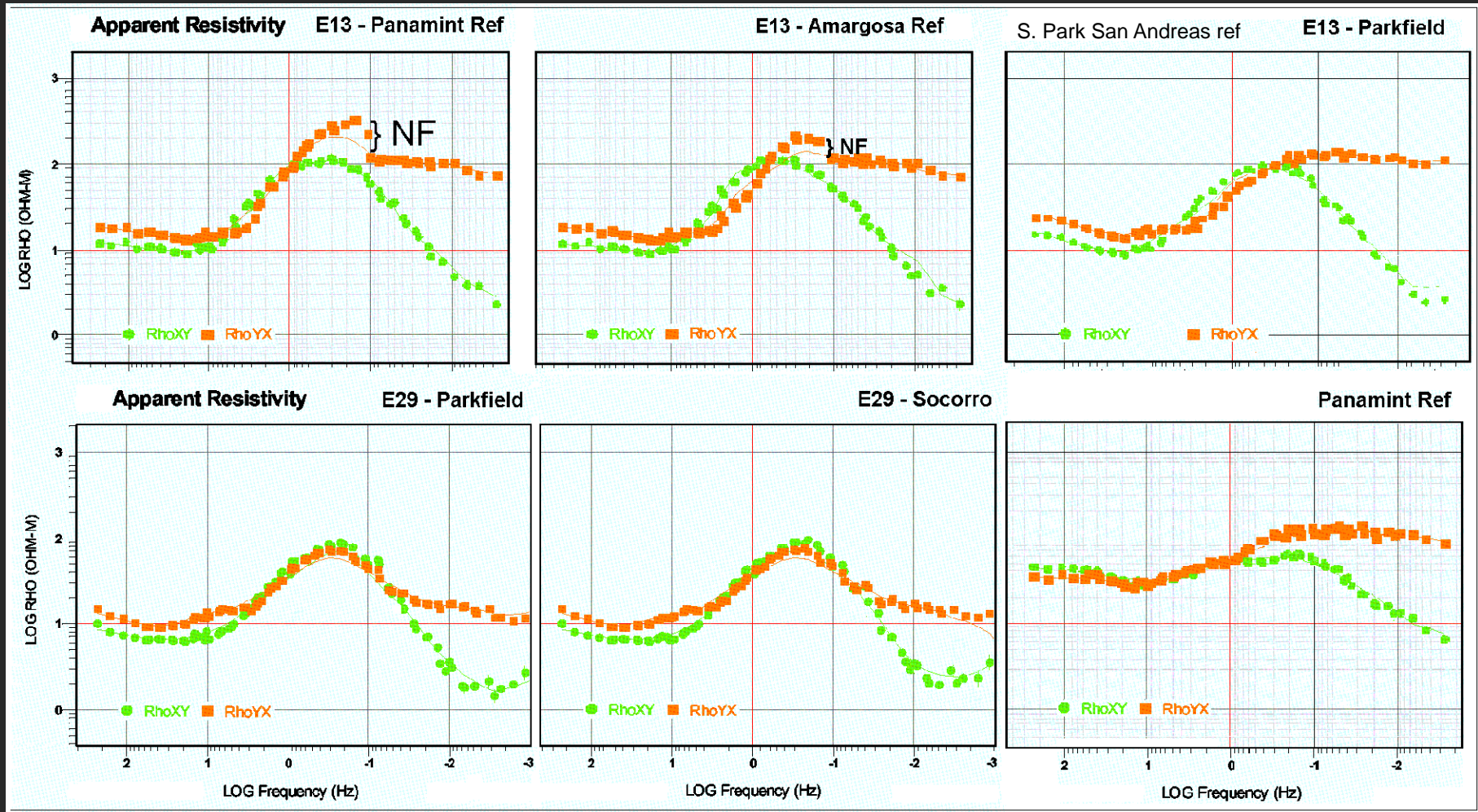
$$Z_{xy} = \frac{(H_x R_x^*) (E_x R_y^*) - (E_x R_x^*) (H_x R_y^*)}{(H_x R_x^*) (H_y R_y^*) - (H_y R_x^*) (H_x R_y^*)}$$

Clarke, Gamble,  
Goubau (1978)



## MT "REMOTE" REFERENCING

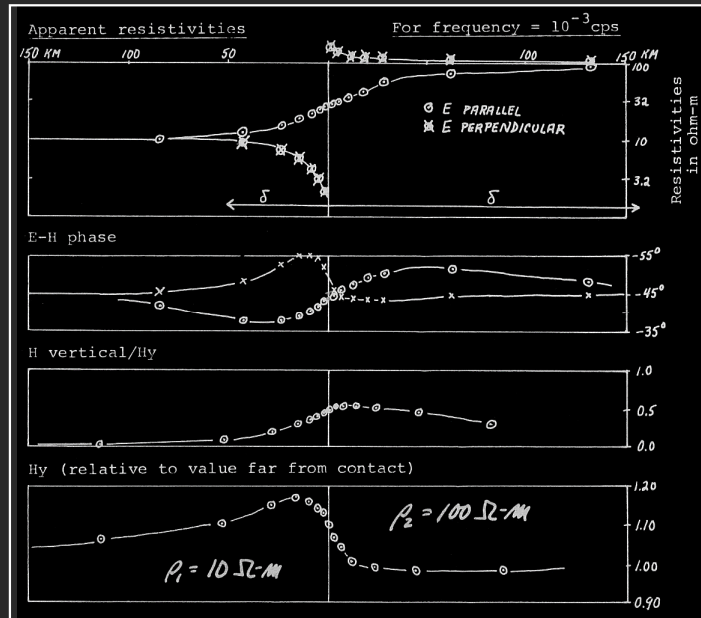




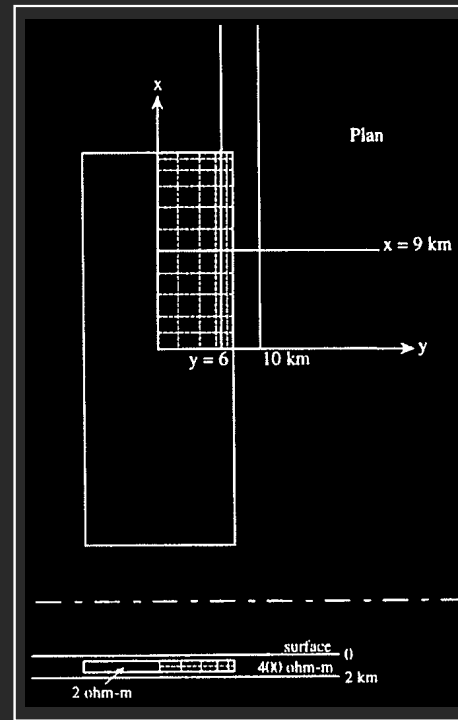
DC intertie near-field effect exceeds 150 km. Reference must be completely outside its field span even if plane wave by that point.

# Swift (1967, MIT)

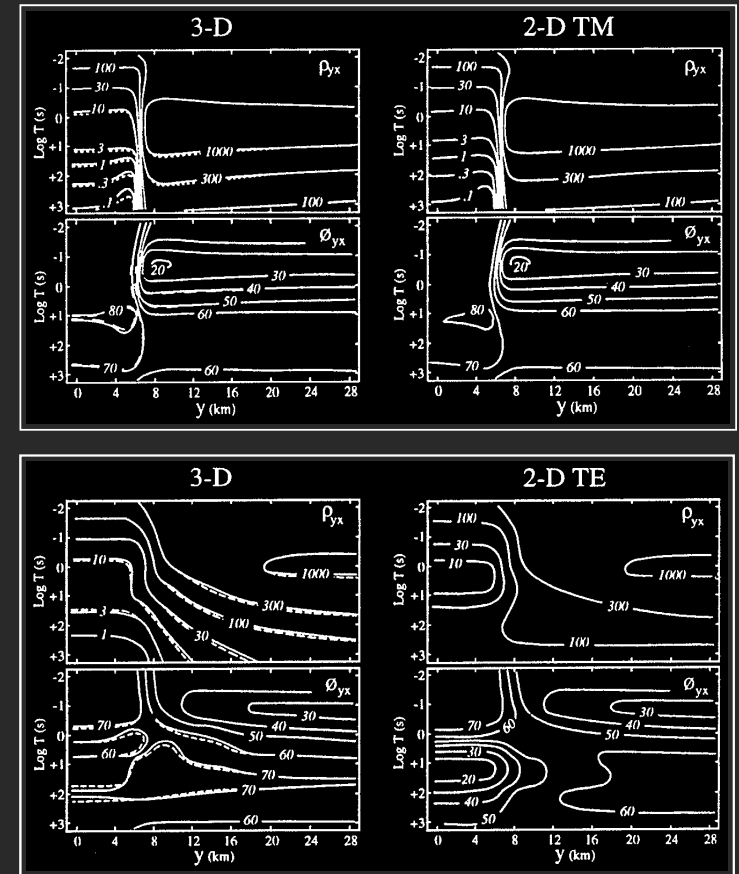
- Assumed tensor relation from start
- Elliptical traces in complex plane
- Spectral analysis from time segments
- Specified TE, TM modes



- Collected 7 tensor sites in AZ and NM using ~50 km telephone lines;  $T = \sim 1000 \text{ s}$  to  $\sim 1 \text{ da}$
- 2D forward modeling using FD code
- Deeper upper mantle 10-30 ohm-m
- Noted that "TE" response inside truncated graben could be depressed



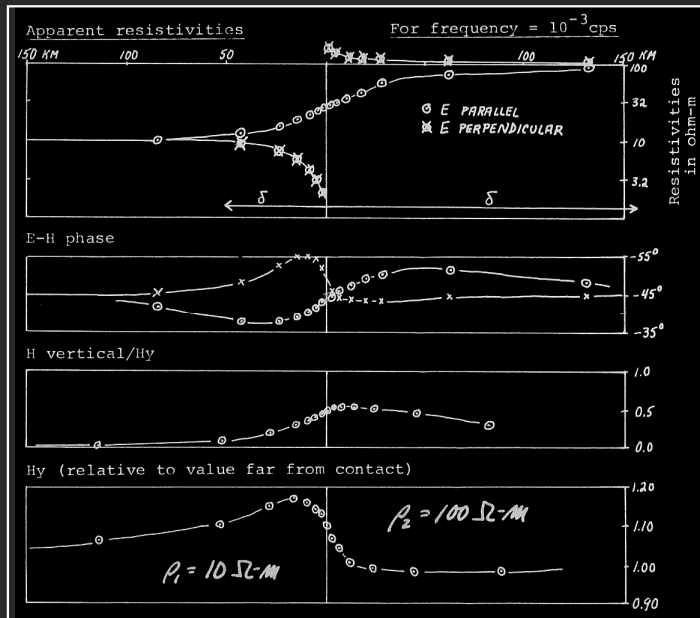
Wannamaker, Hohmann and Ward (1980, 1984); Ledo (2005)



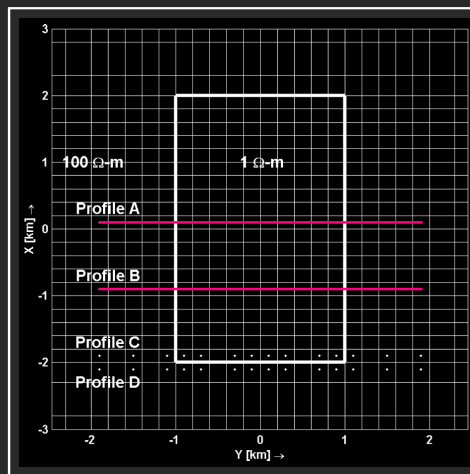
Similarity of 3D Zyx and 2D TM for simple bodies, incl. off-center  
Disagreement of 3D Zxy and 2D TE due to boundary charges  
More complex bodies increasingly 3D

# Swift (1967, MIT)

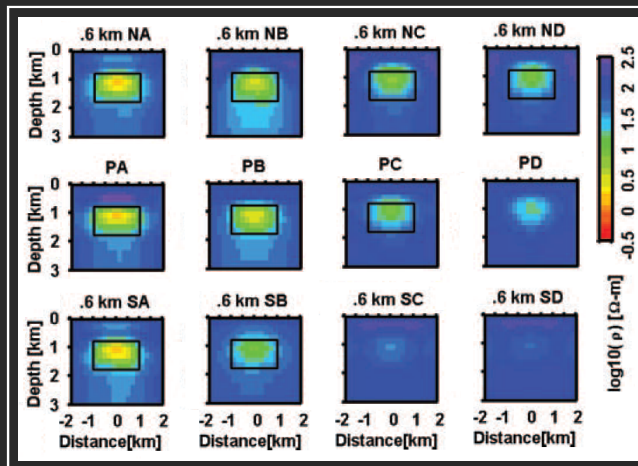
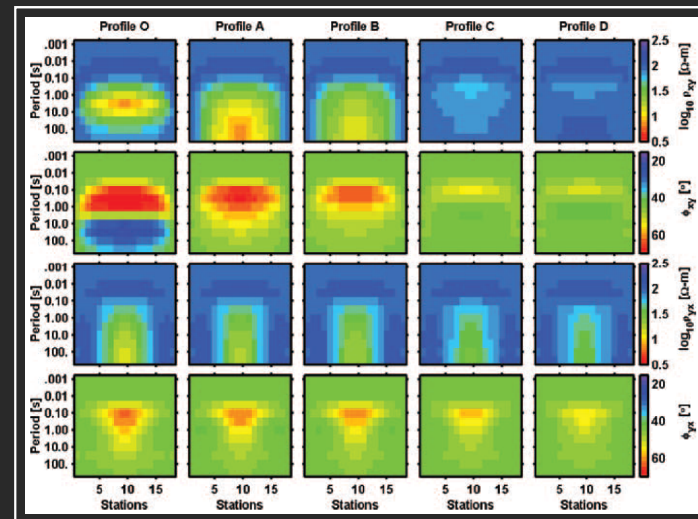
- Assumed tensor relation from start
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- Spectral analysis from time segments
- Specified TE, TM modes



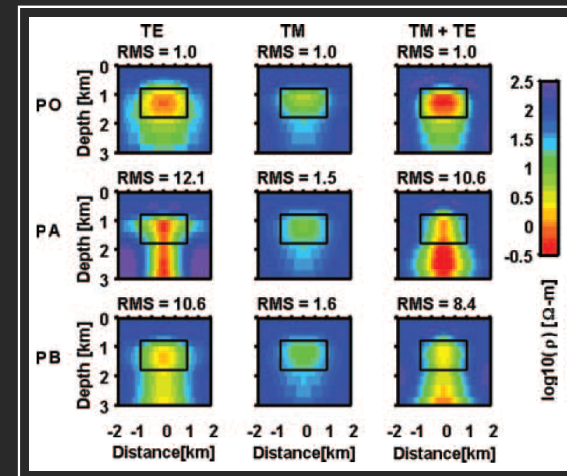
- Collected 7 tensor sites in AZ and NM using ~50 km telephone lines;  $T = \sim 1000$  s to  $\sim 1$  da
- 2D forward modeling using FD code
- Deeper upper mantle 10-30 ohm-m
- Noted that “TE” response inside truncated graben could be depressed



Siripunvaraporn et al, (2005)



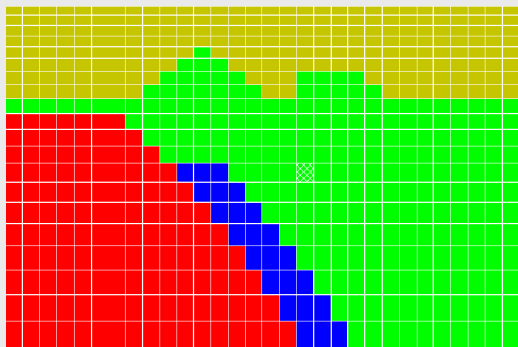
3D Profile Inversion  
Effective



2D “TE” Inversion Distorted

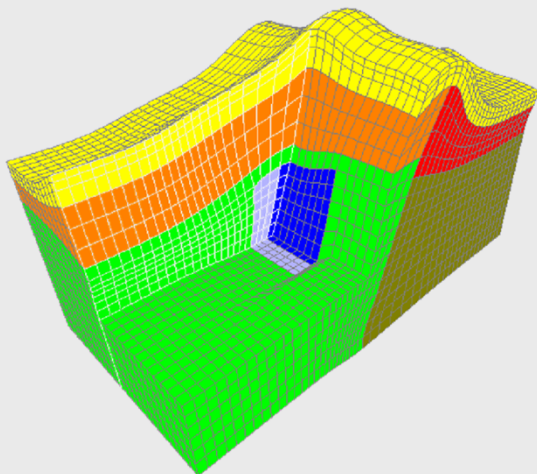


# Electromagnetic Simulation and Inversion With Conformal Receiver Surfaces (Topography)

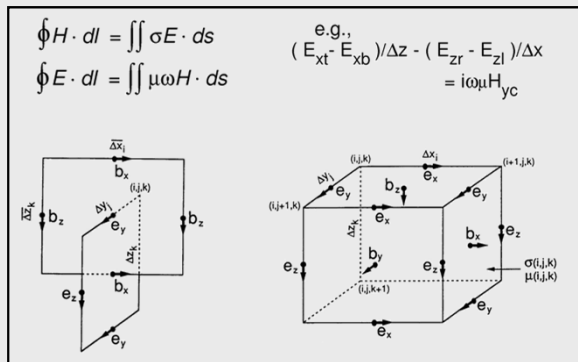


Finite Difference Topo Model

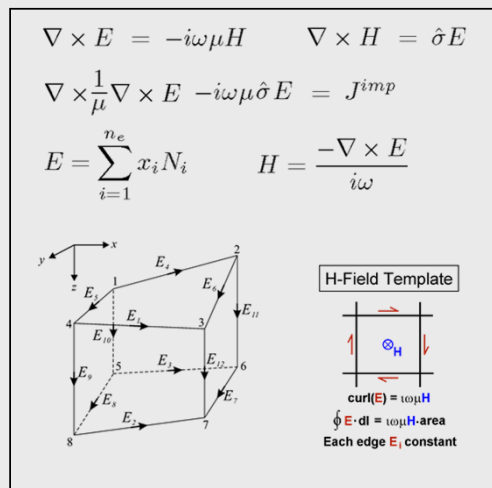
Graphics after Art Raiche



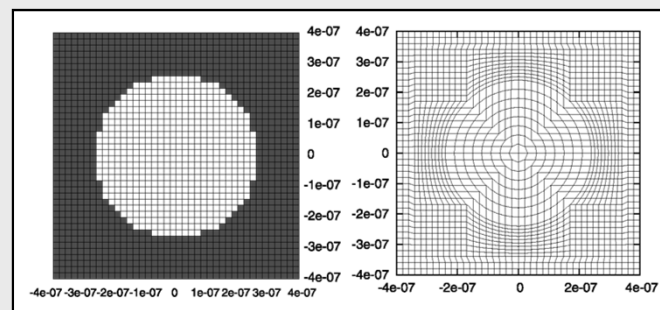
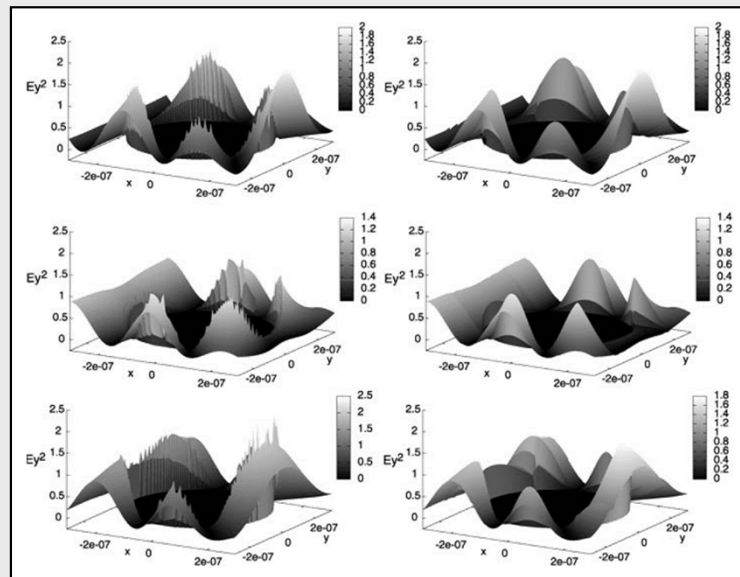
Finite Element Cutout View



FD: Madden and Mackie (1989) resurrected Yee (1966) staggered grid. Numerous followers.



FE: E-field discontinuity treated with edge elements. Unambiguous placement of sharp interfaces.

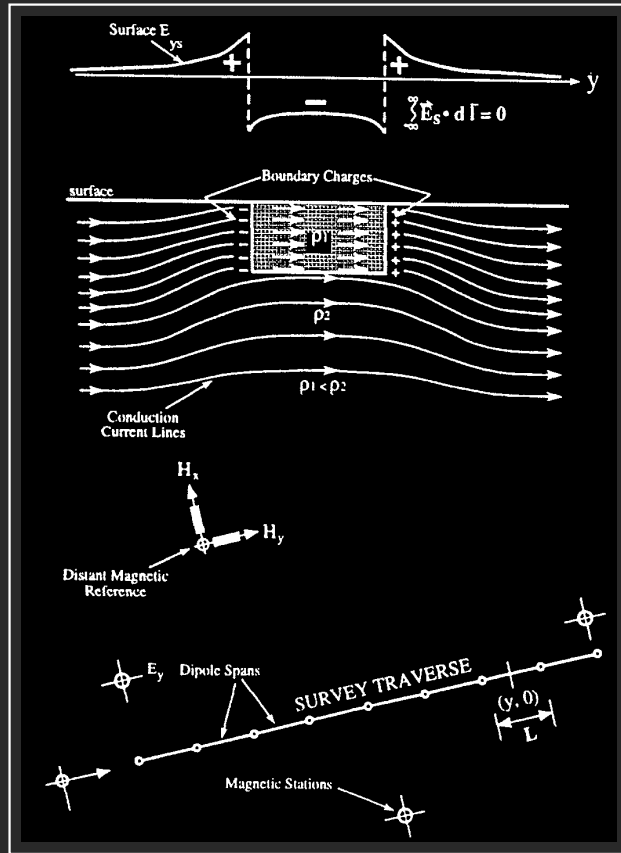


Scattered E Power  
Liu et al., 2009

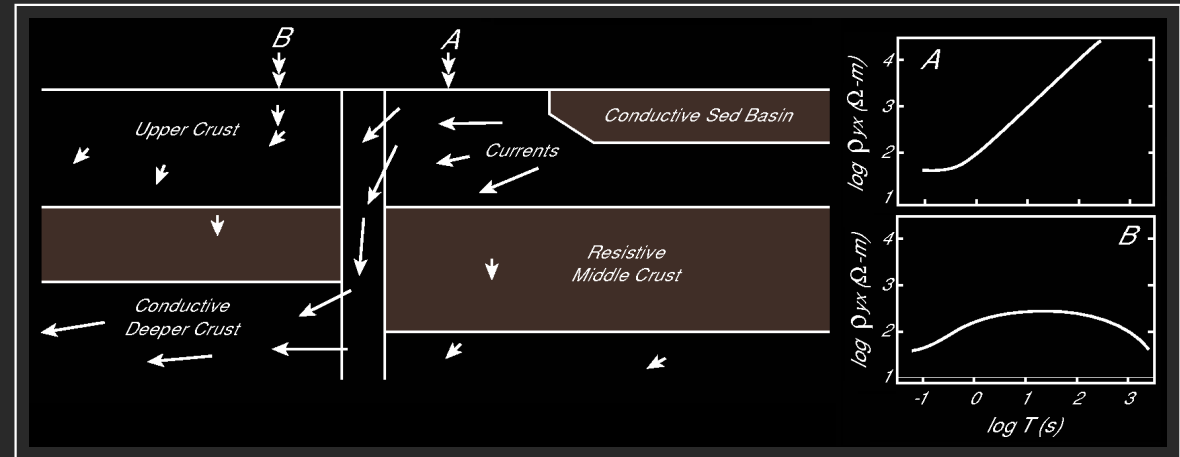
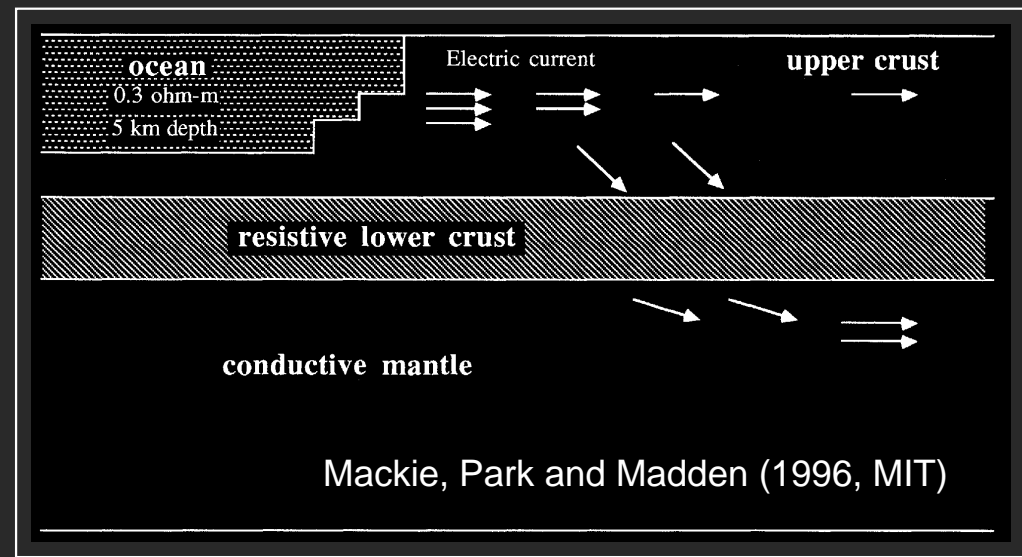


Torres-Verdin and Bostick (1992, UTA)

- Sampling challenge in natural environs
- E-field anomalies zero-mean, incl. 3D

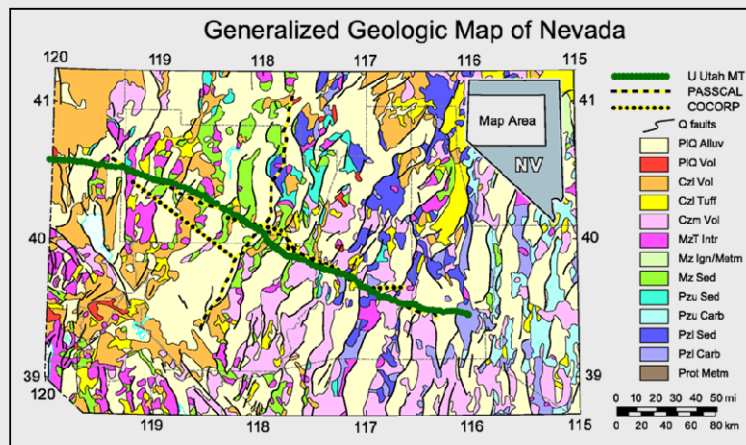


- Thus both  $Z_{xy}$  and  $Z_{yx}$  are zero-mean
- $Z_{av} = [Z_{xy} - Z_{yx}]/2$  a logical background

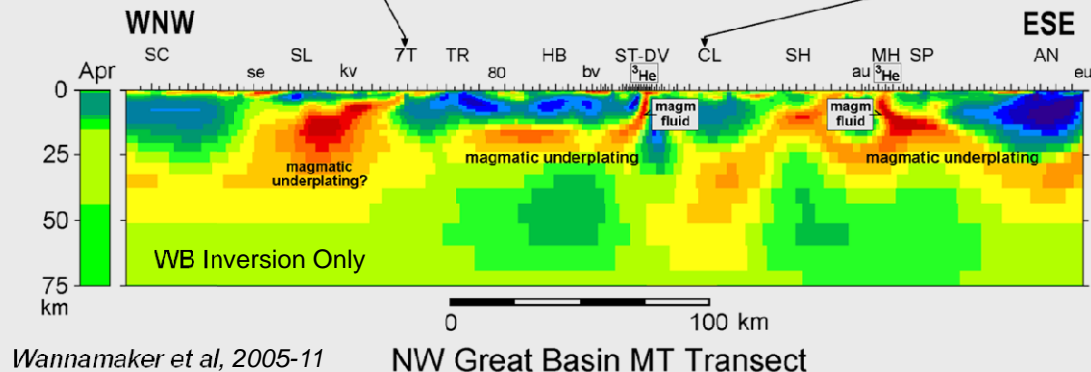
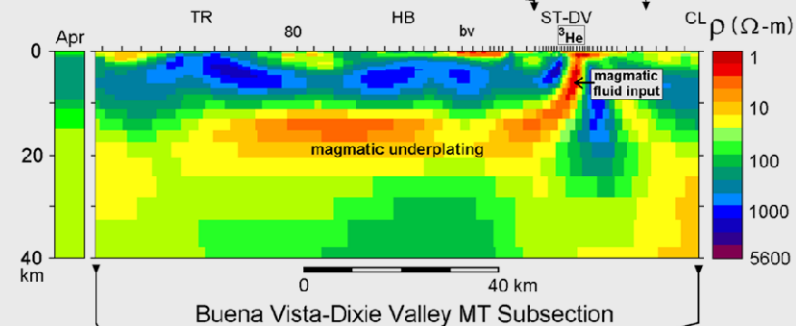
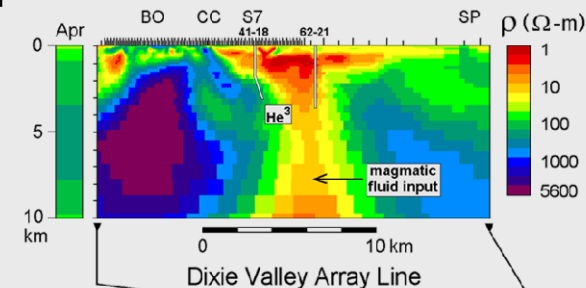
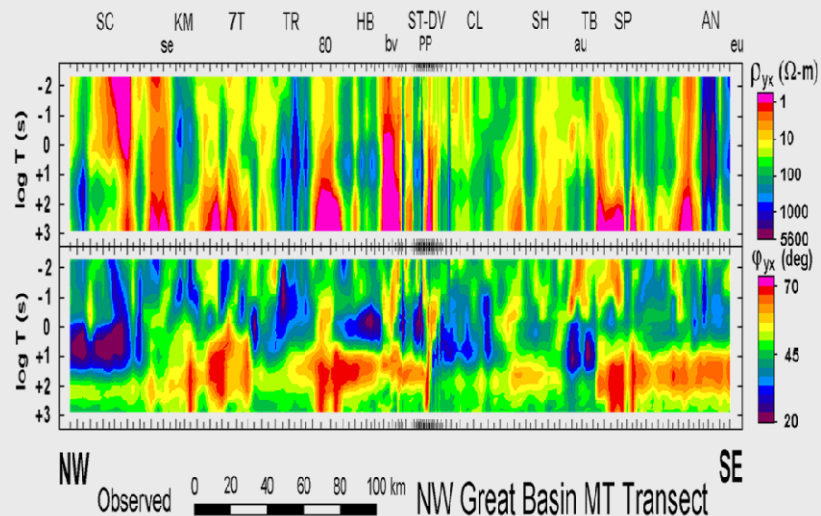


Vertical Current Channeling down Crustal-Scale Fault Zone

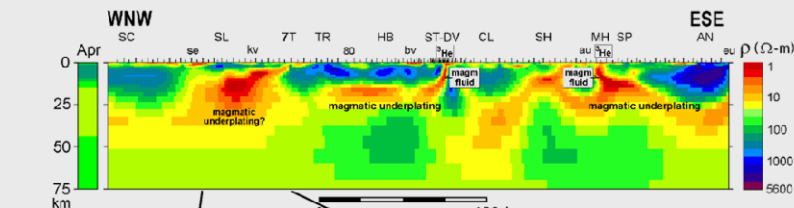
# Crustal-Scale Breaks and Multiscale Magmatic/Hydrothermal Connections



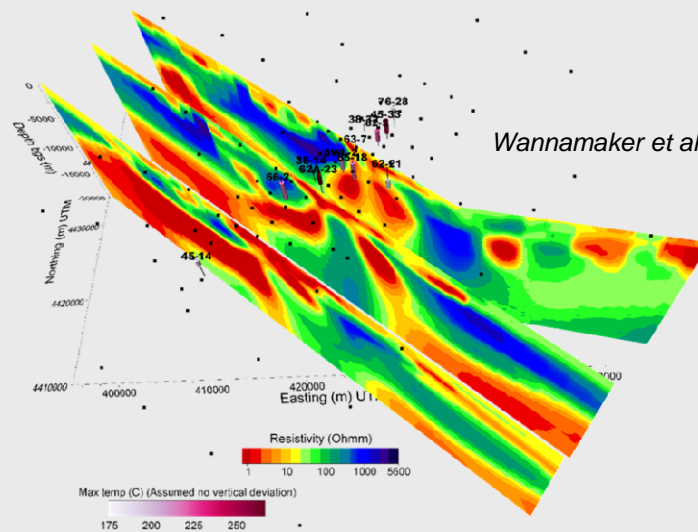
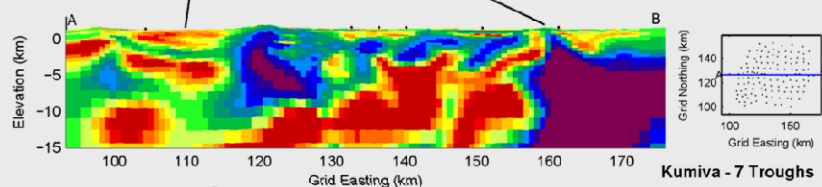
CA | NV



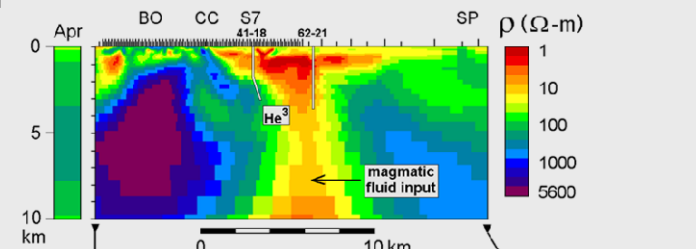
# Crustal-Scale Breaks and Multiscale Magmatic/Hydrothermal Connections



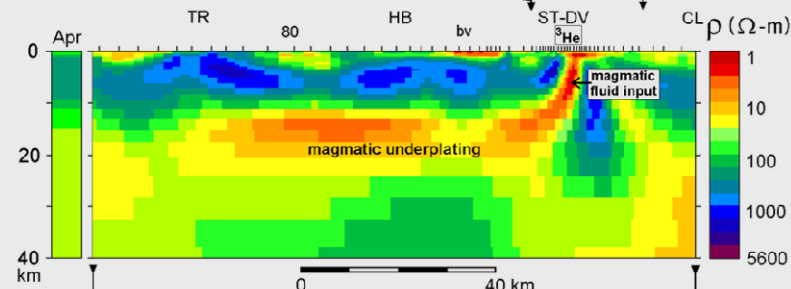
Wannamaker et al, 2019



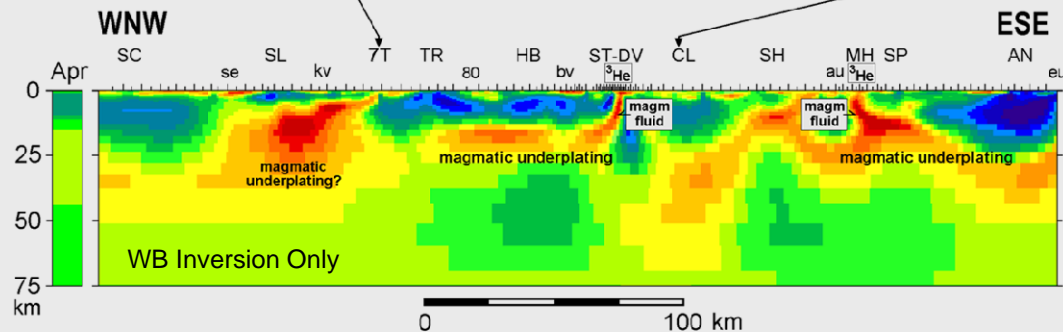
Wannamaker et al, 2013



Dixie Valley Array Line

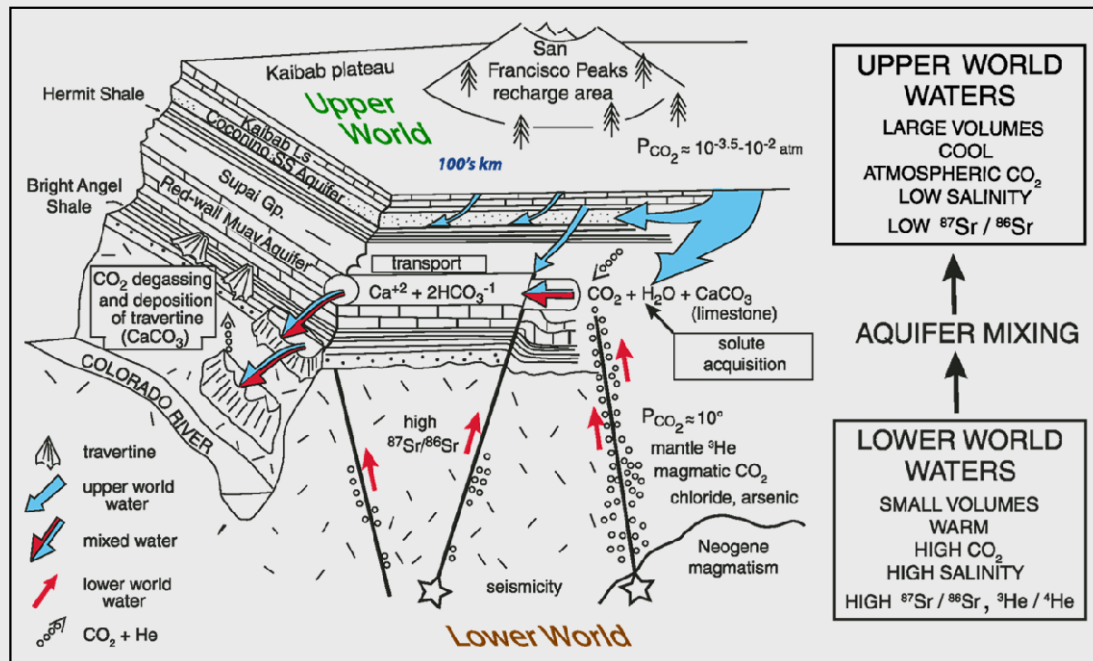


Buena Vista-Dixie Valley MT Subsection



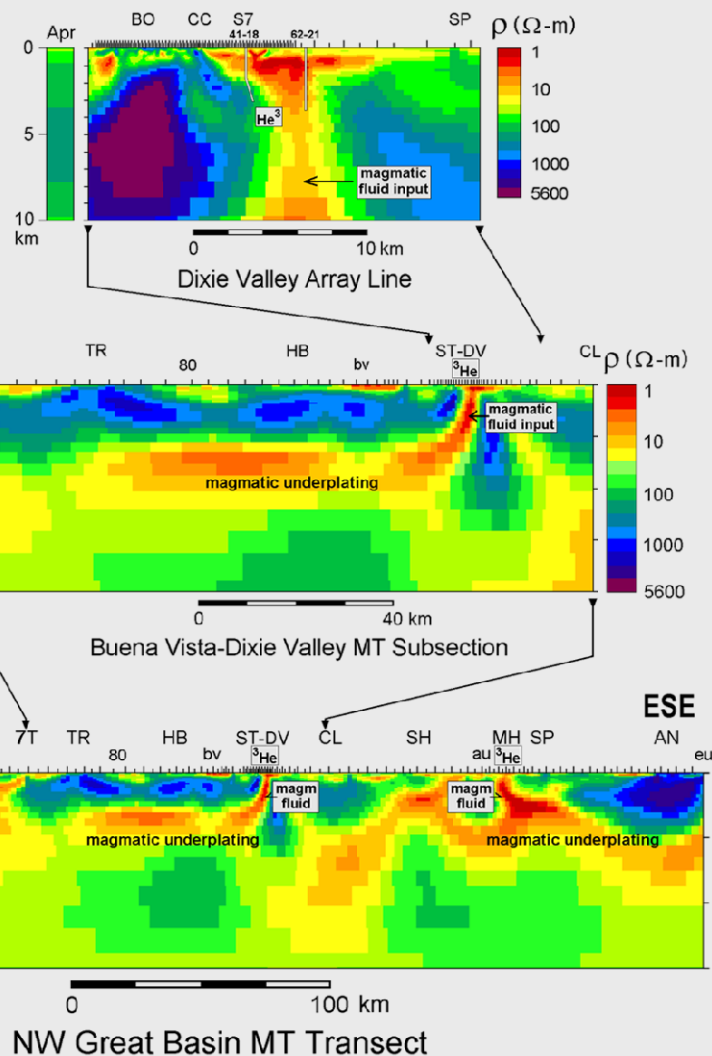
Wannamaker et al, 2005-11

NW Great Basin MT Transect



## Multiscale Magmatic/Hydrothermal Connections

Grand Canyon Hydrological Model  
 (Crossey and Karlstrom, 2012)

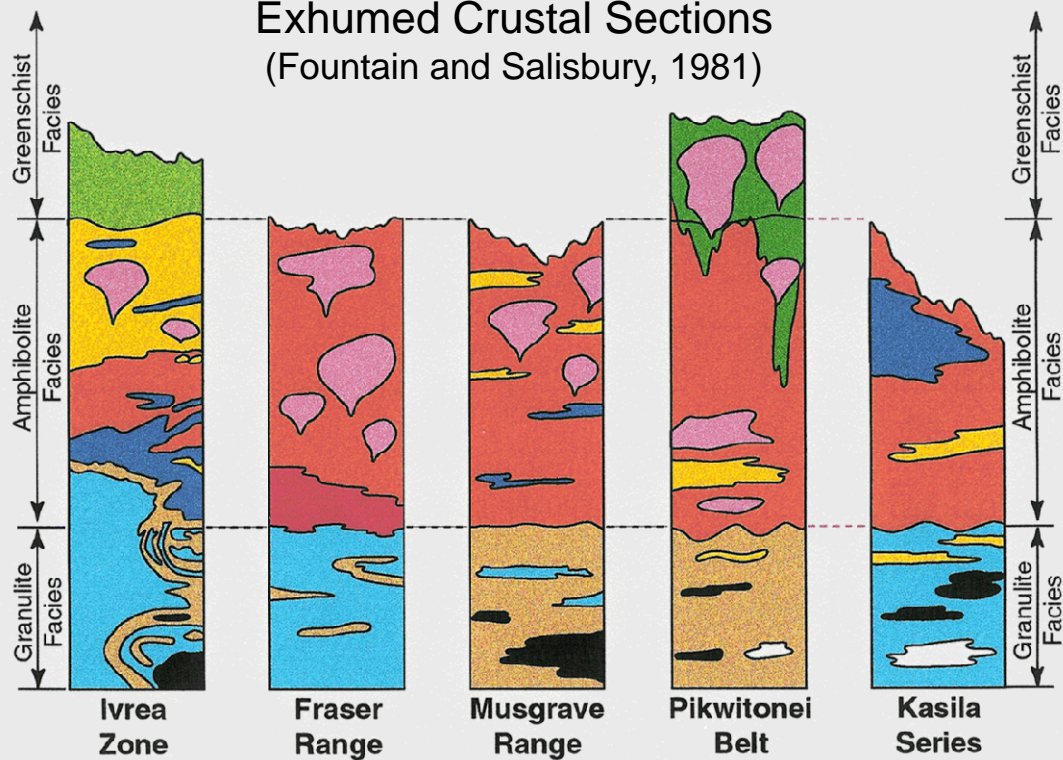


Wannamaker et al, 2005-11

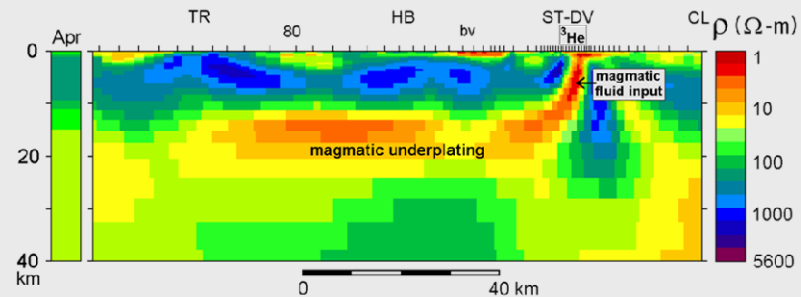
NW Great Basin MT Transect



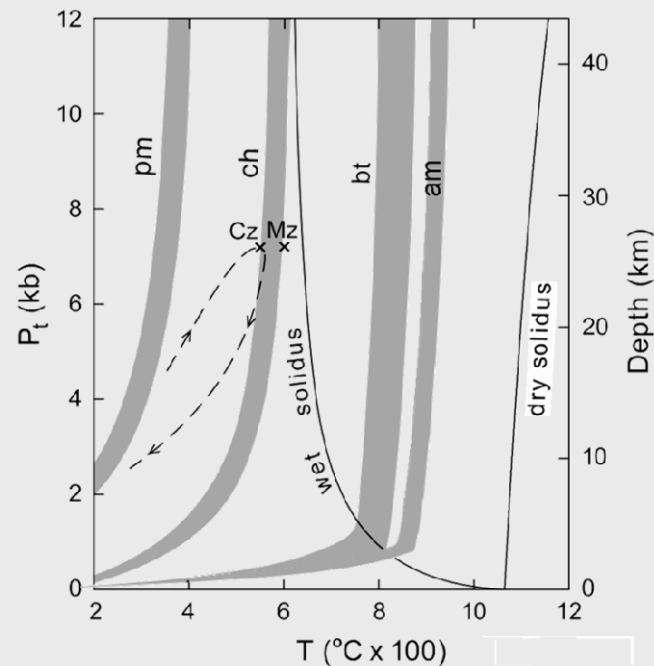
## Exhumed Crustal Sections (Fountain and Salisbury, 1981)



- Free water not compatible with granulite-upper amphibolite facies- resorbed to more amph/biotite
- Any present fluid must be of low  $a(\text{H}_2\text{O})$
- Complex salts may provide a mechanism
- Comment/Reply Yardley (1997, 2000), Wannamaker (2000)

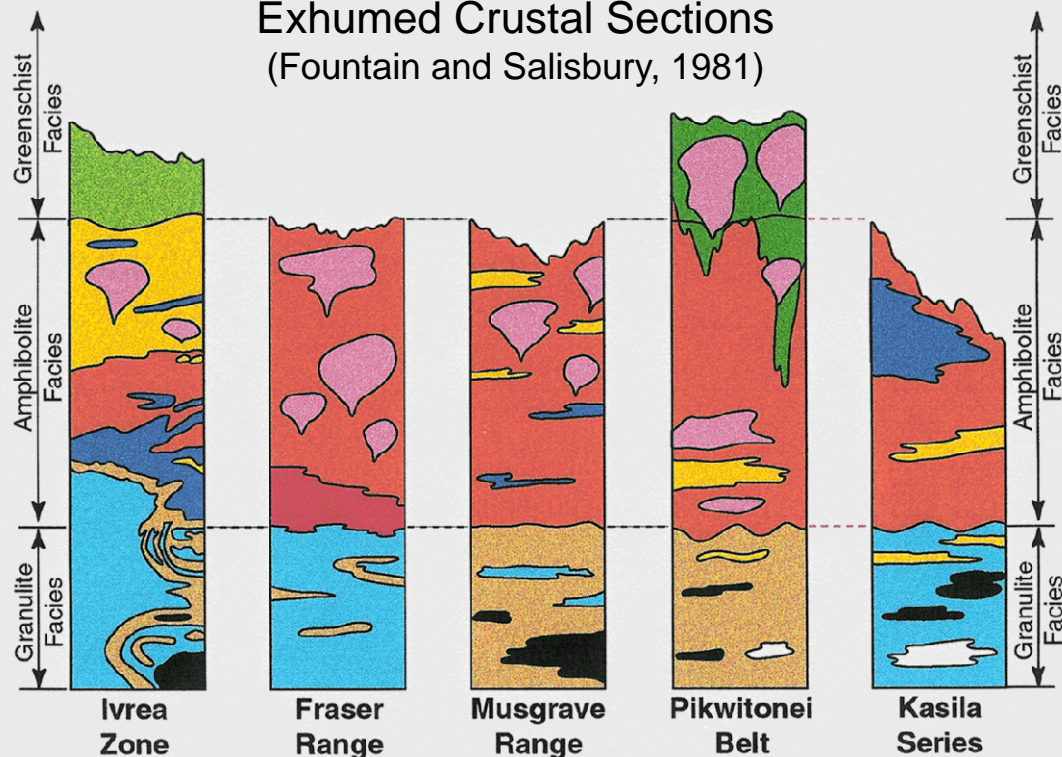


Buena Vista-Dixie Valley MT Subsection



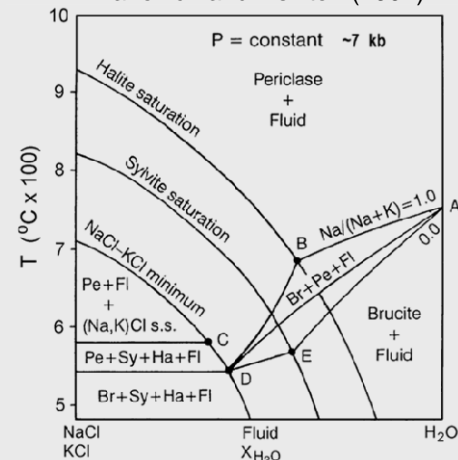
Diorite-H<sub>2</sub>O petrogenetic grid

## Exhumed Crustal Sections (Fountain and Salisbury, 1981)

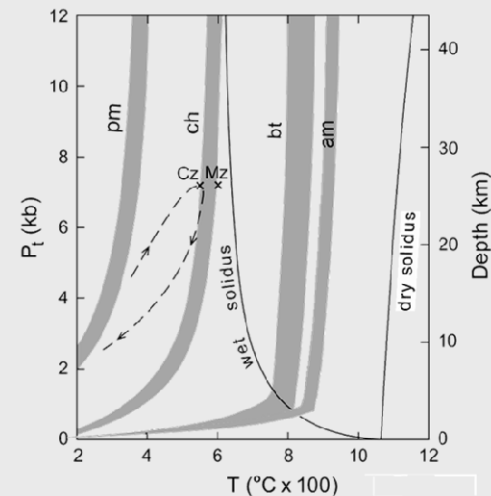


- Free water not compatible with granulite-upper amphibolite facies- resorbed to more amph/biotite
- Any present fluid must be of low  $a(\text{H}_2\text{O})$
- Complex salts may provide a mechanism
- Comment/Reply Yardley (1997, 2000), Wannamaker (2000)

Aranovich and Newton (1997)

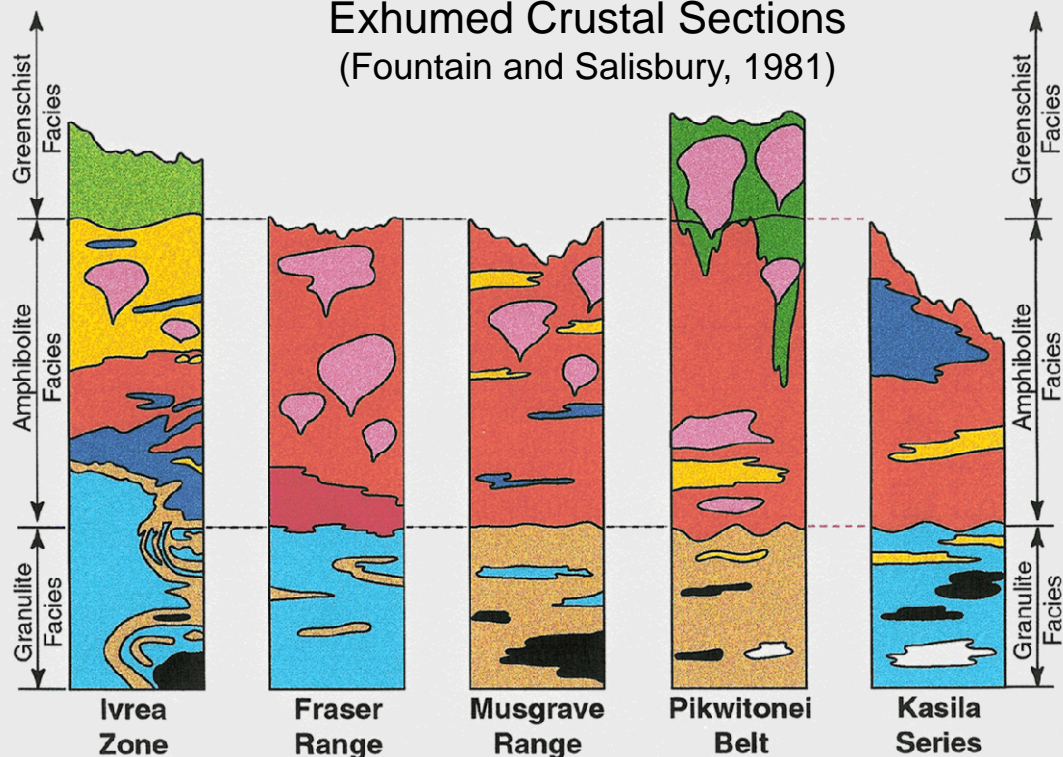


Complex salts reduce T of last fluid

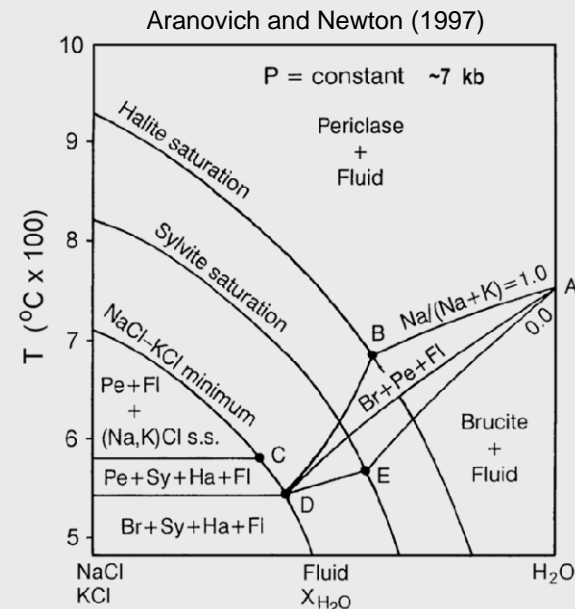
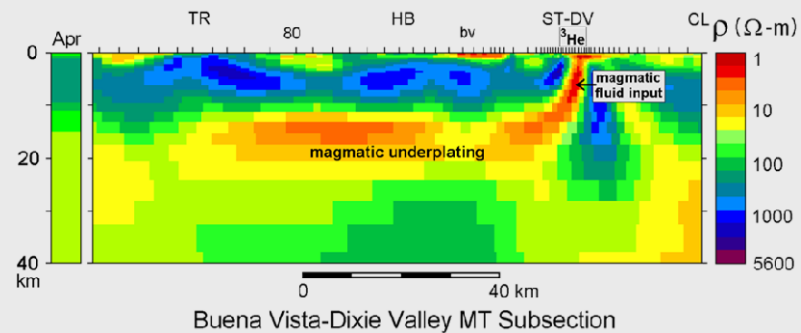


Diorite-H<sub>2</sub>O petrogenetic grid

## Exhumed Crustal Sections (Fountain and Salisbury, 1981)

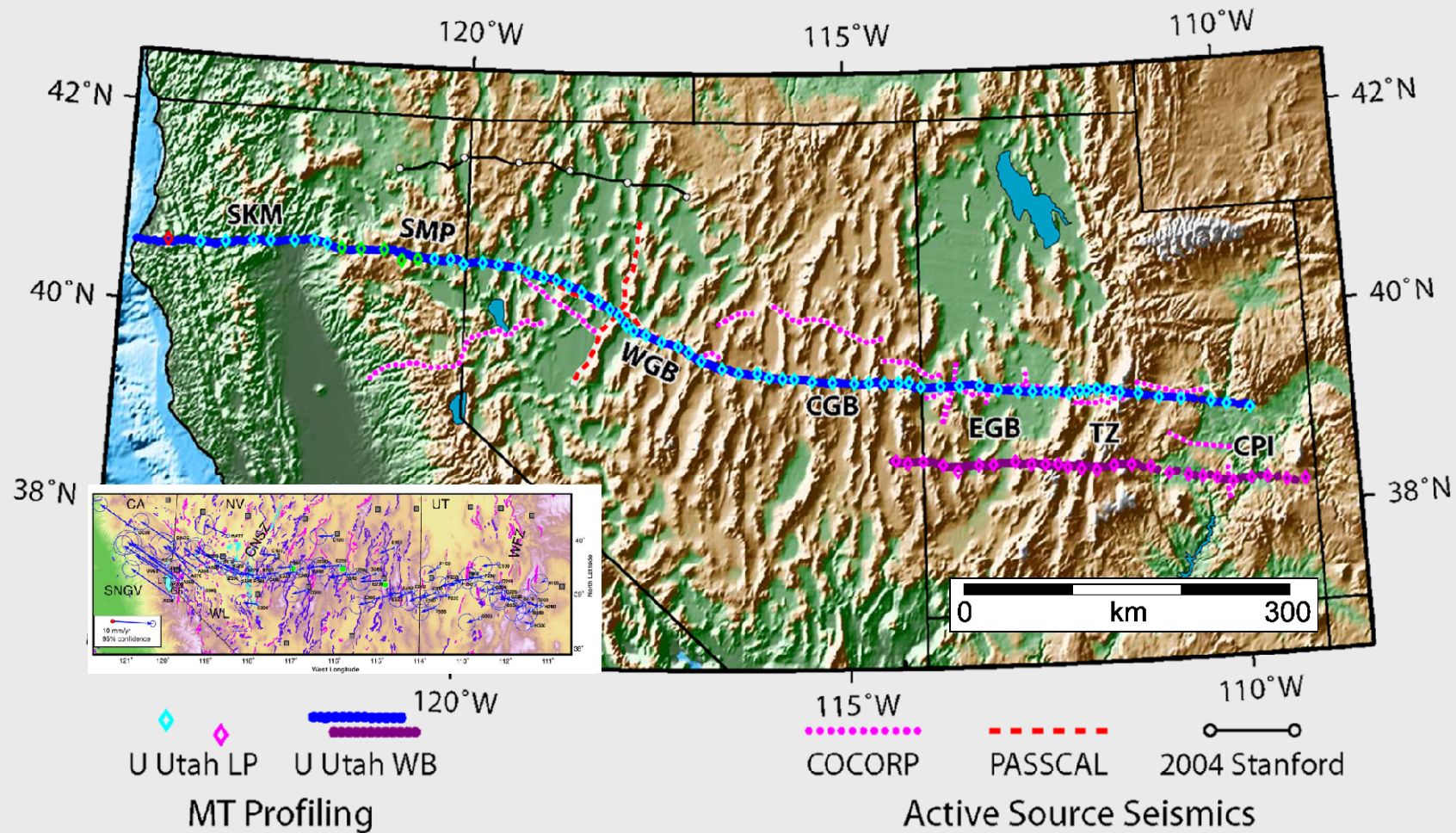


- Free water not compatible with granulite-upper amphibolite facies- resorbed to more amph/biotite
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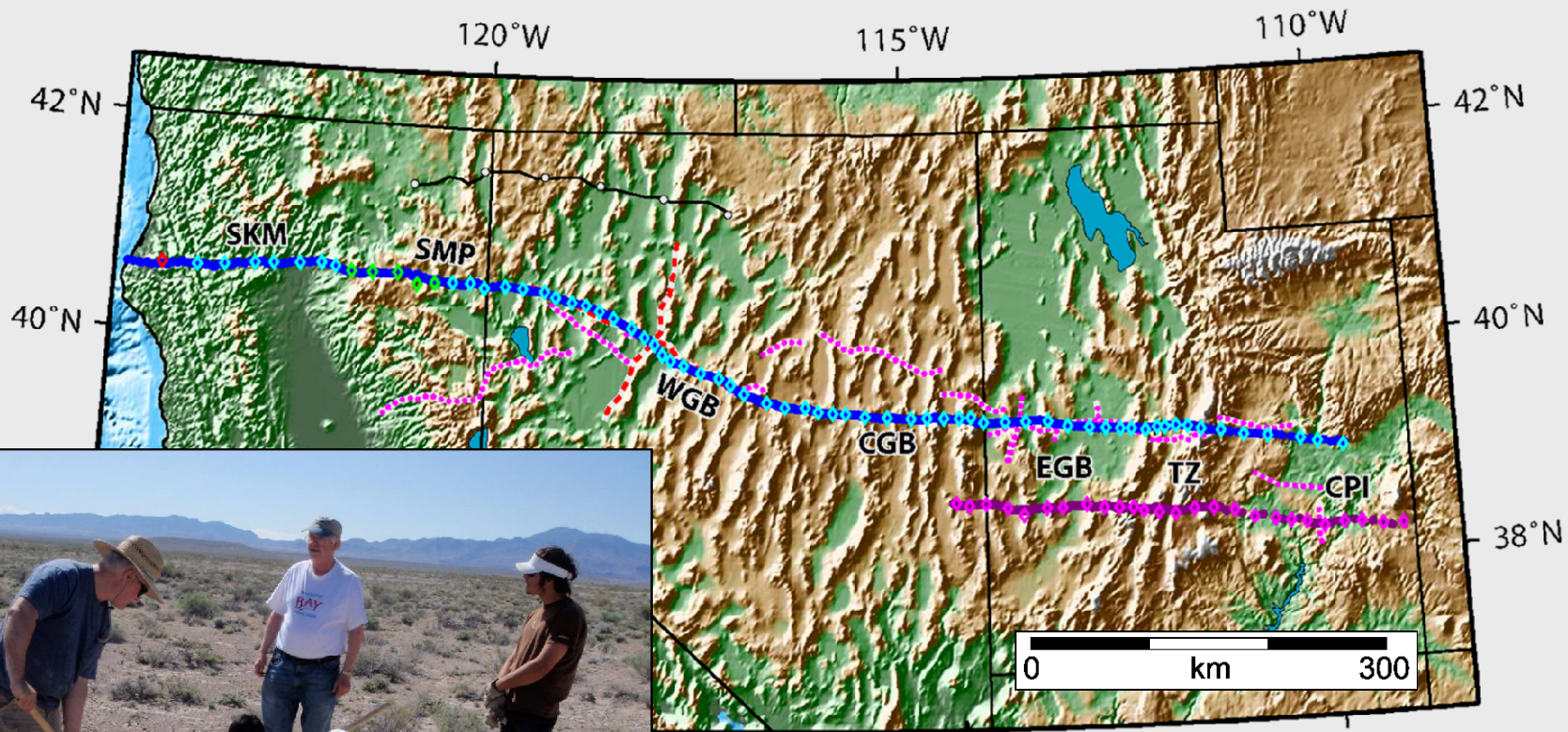
Complex salts reduce T of last fluid





**S Klamath Mtns – Great Basin – Colorado Plateau MT**  
 Approx. coincident with COCORP, PASSCAL seismic profiling

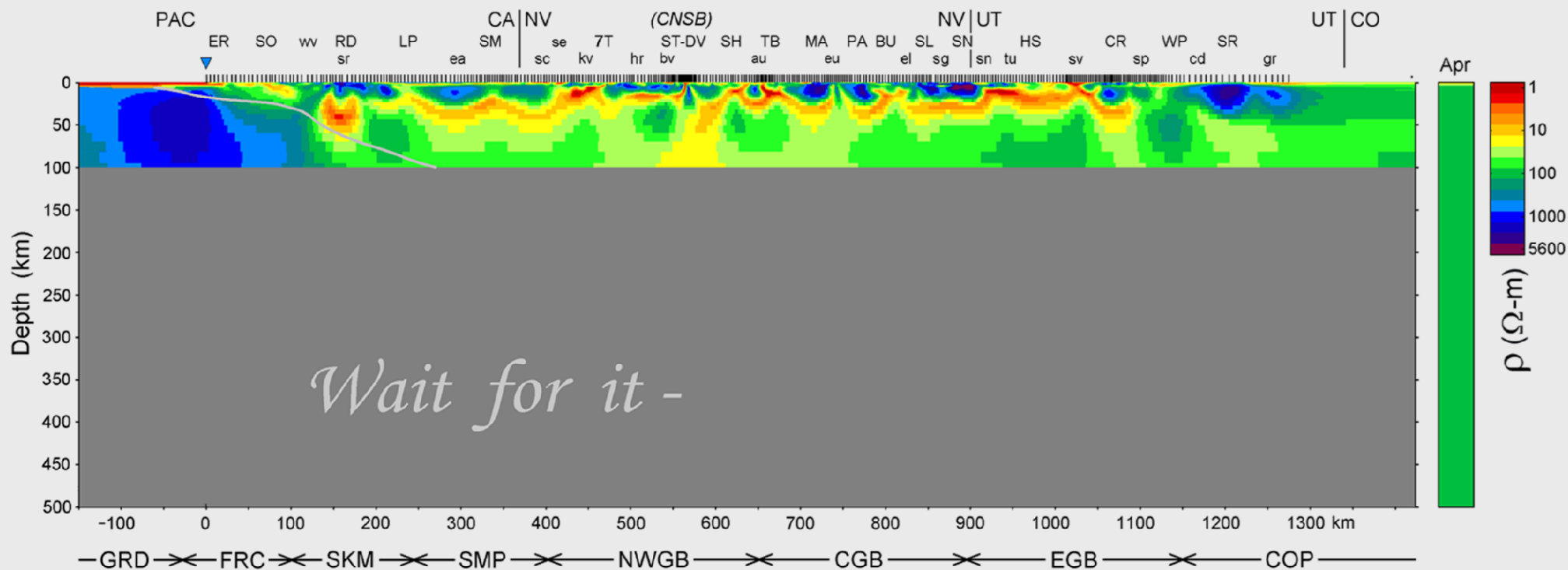
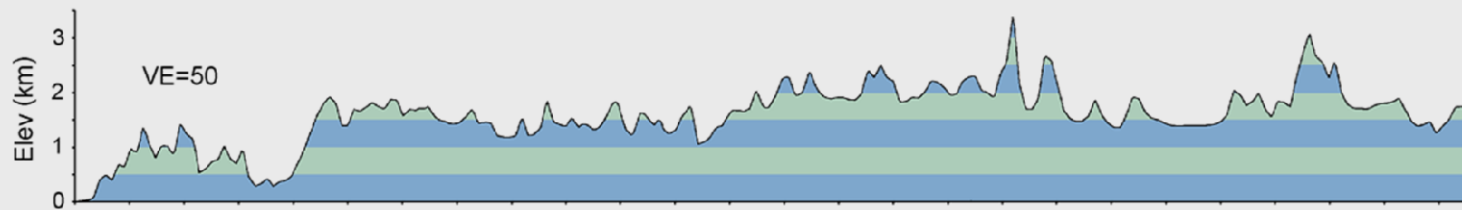




115°W 110°W  
 COCORP PASSCAL 2004 Stanford

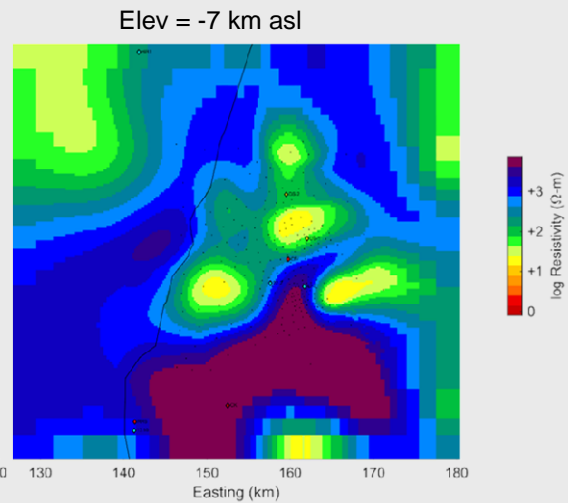
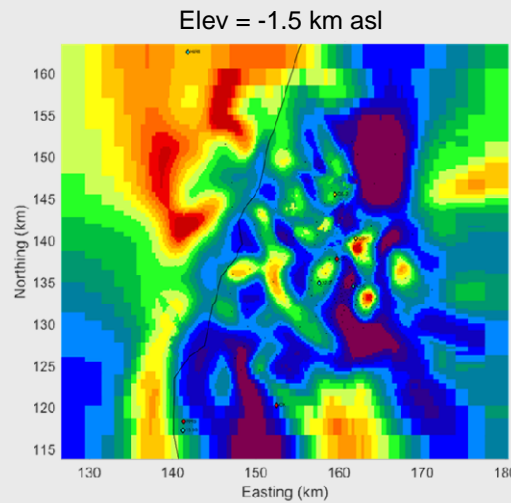
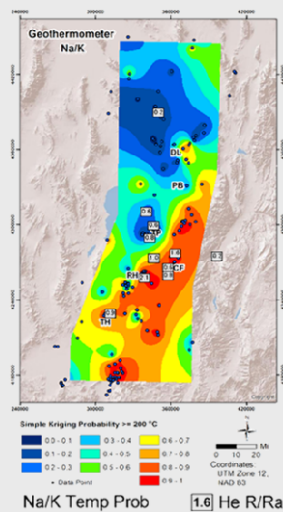
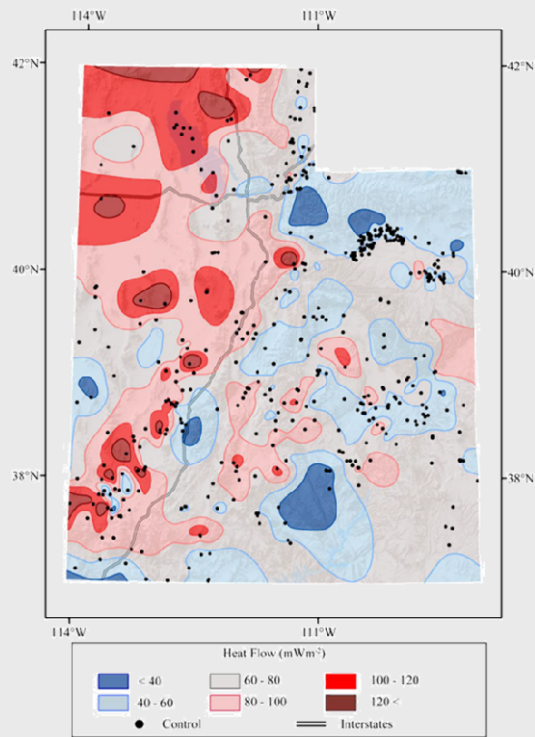
Active Source Seismics

S Klamath – Great Basin  
 – Colorado Plateau MT

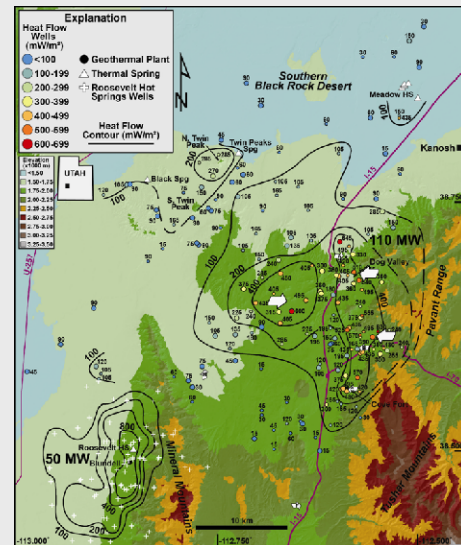
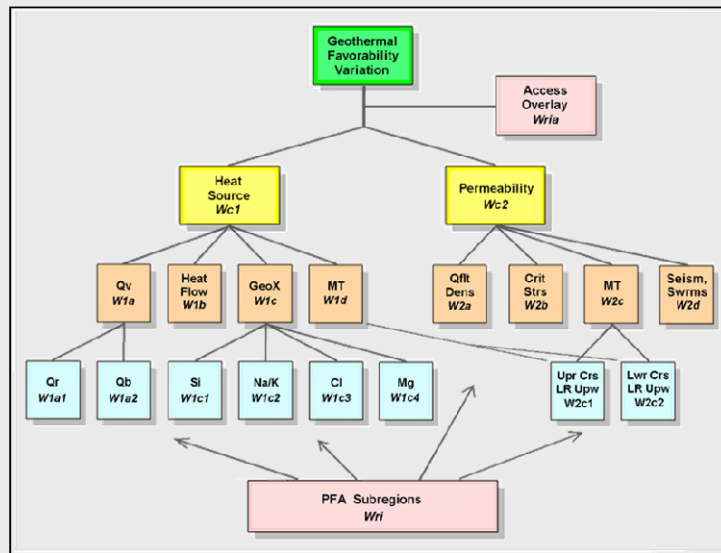


Klamath - S Modoc - Great Basin - Colorado Plateau  
MT Transect (~40 N lat.)

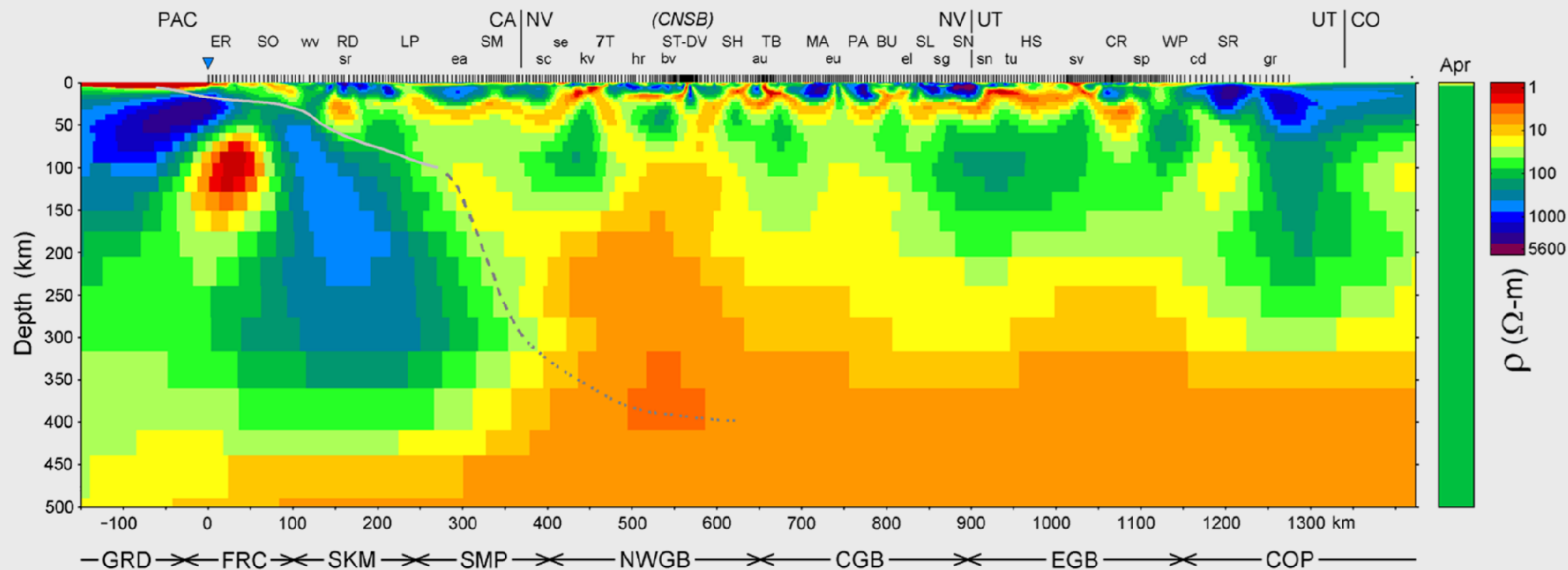
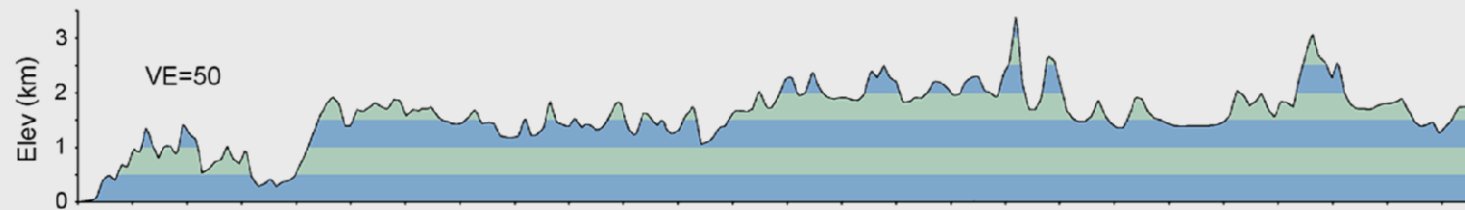




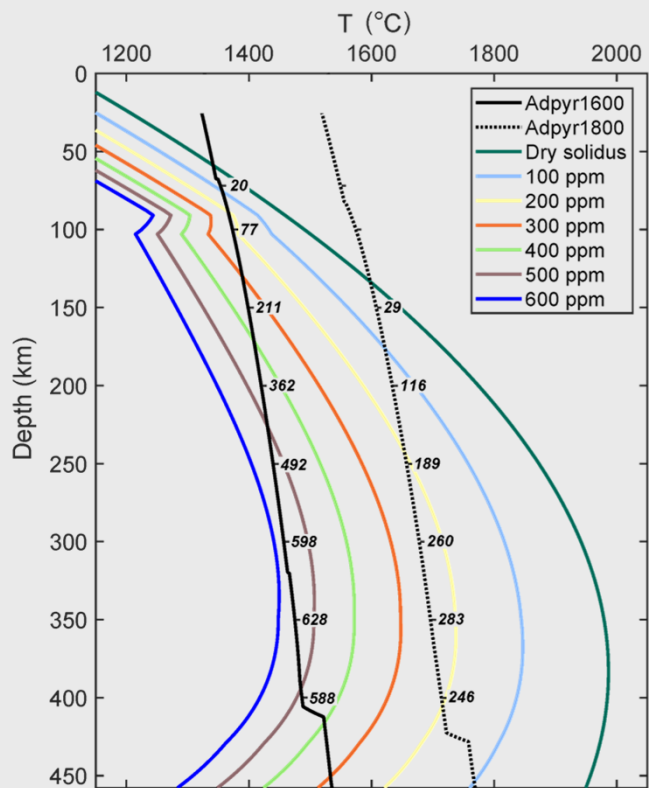
## Multi-Criteria Decision Making (MCDM) Implementation for Geothermal Prospectivity (Wannamaker et al., 2017)



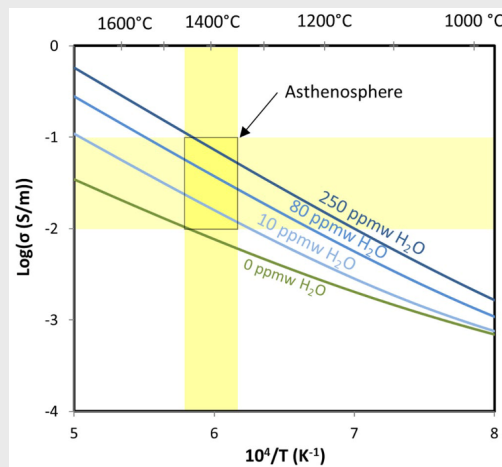
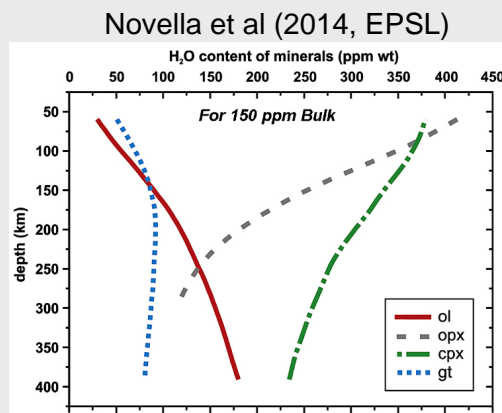




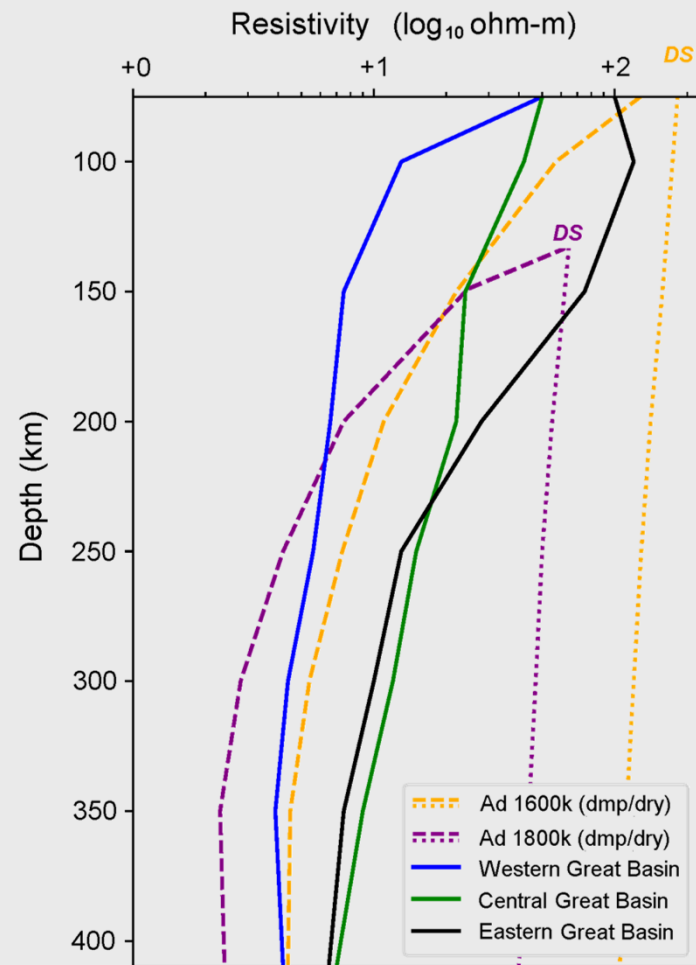
Klamath - S Modoc - Great Basin - Colorado Plateau  
MT Transect (~40 N lat.)



Hirschmann et al (2009, PEPI)  
Stixrude and Lithgow-Bertelloni (2011, GJI)



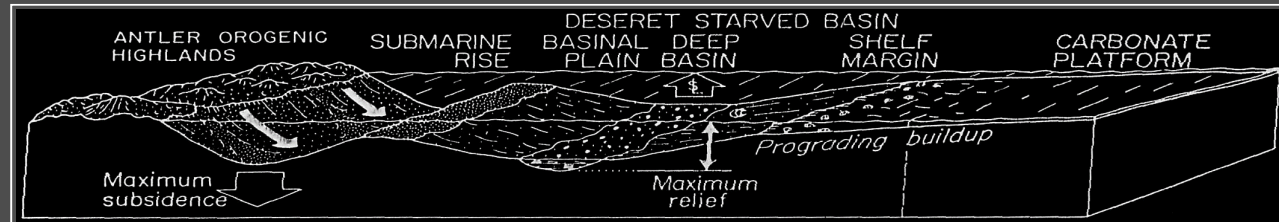
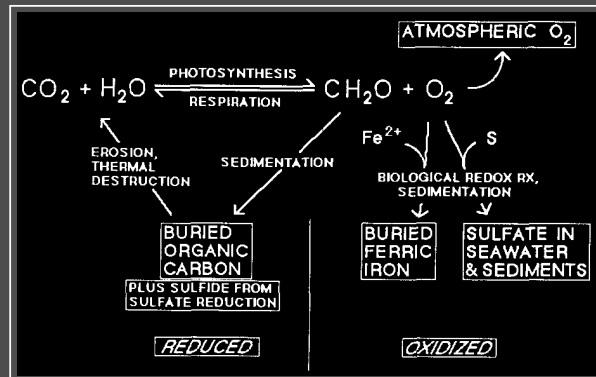
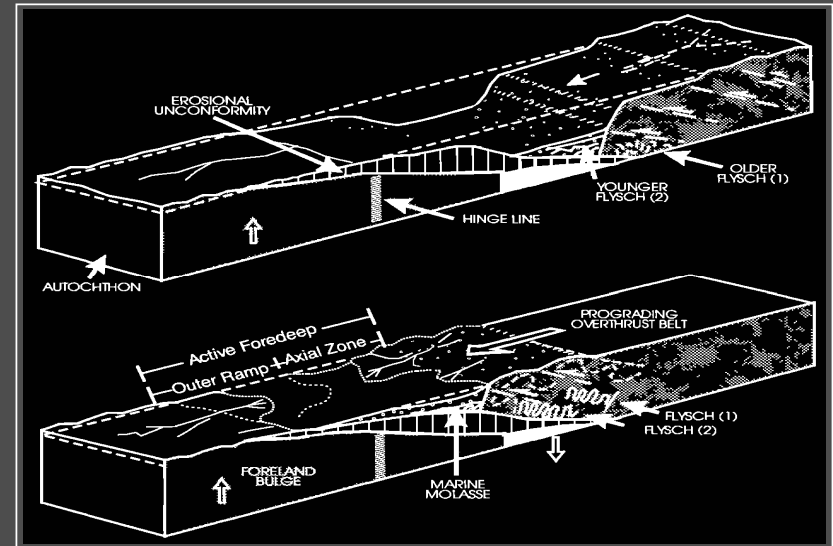
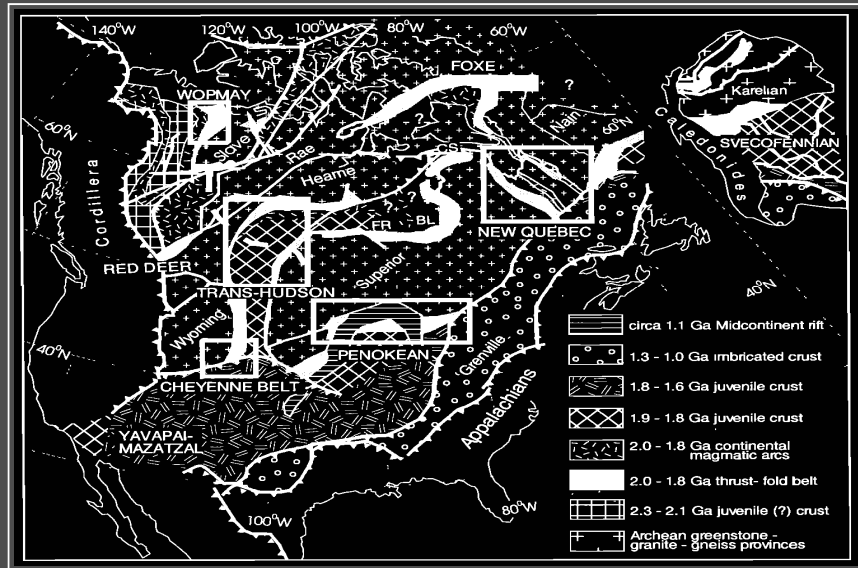
Novella et al (2017, Sci Rpt)



# Electrical conductivity and Paleo-Proterozoic foredeeps

D.E. Boerner, R.D. Kurtz, and J.A. Craven

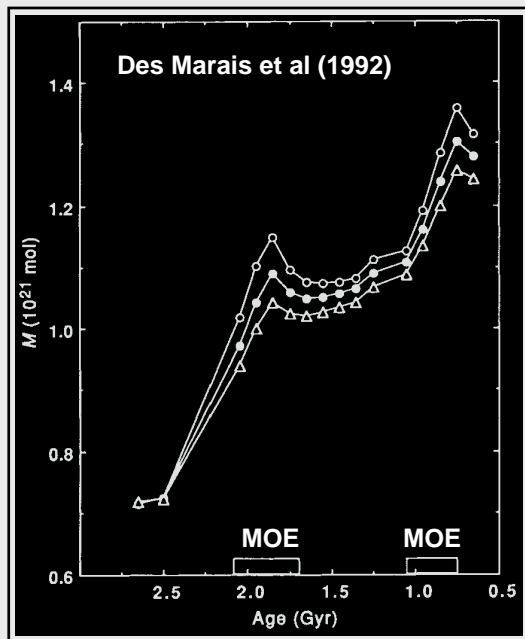
JOURNAL OF GEOPHYSICAL RESEARCH, VOL. 101, NO. B6, 1996



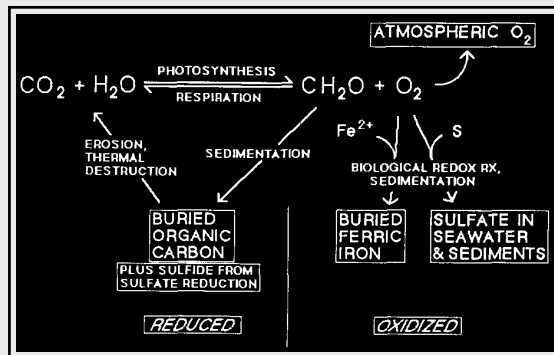
Cyanobacterial O<sub>2</sub> production  
 ← and oC-Sd sequestration  
 Des Marais (1994)

C-S concentration in starved basins  
 Sandberg and Gutschick (1983)

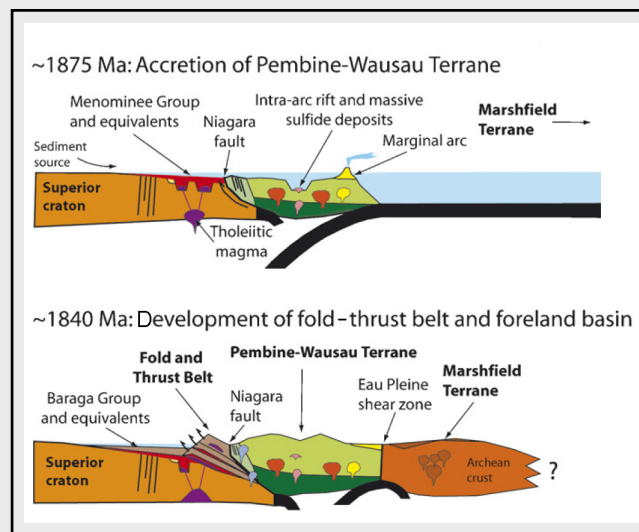




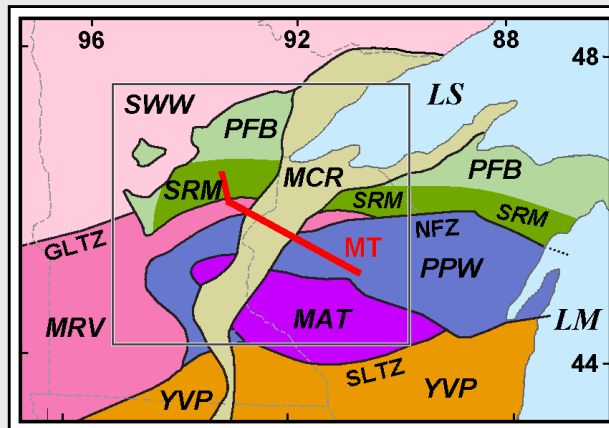
oC-Sd global primary production



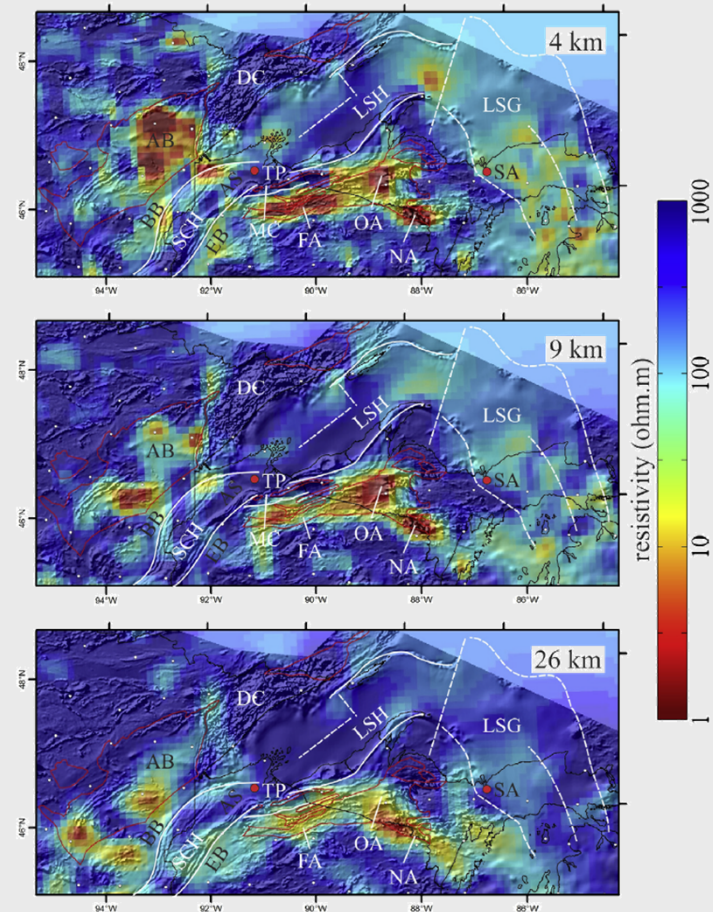
oC-Sd sequestration



Mod from Schulz and Cannon (2007)



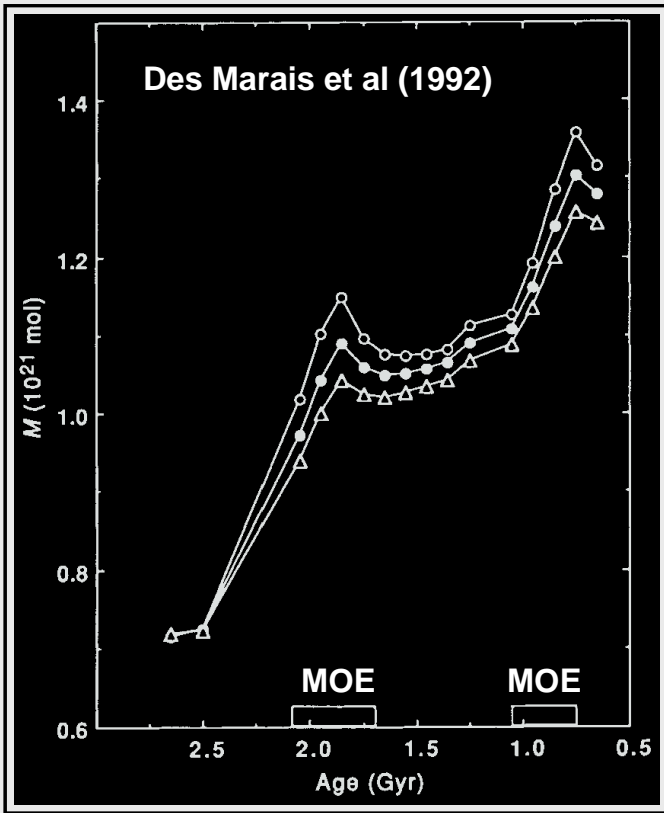
Mod from Southwick (2014)



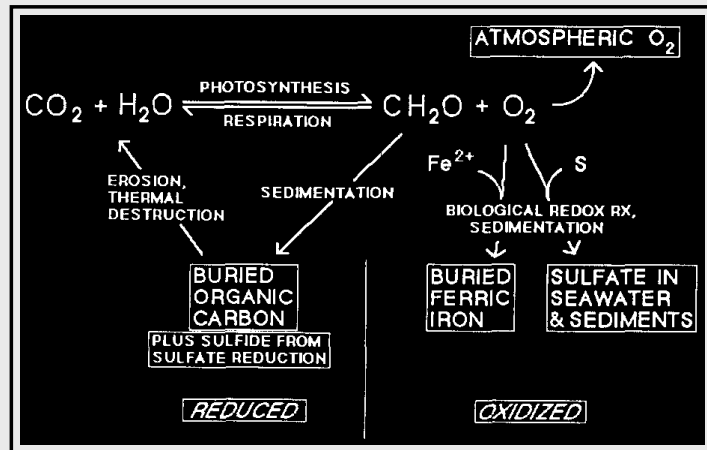
Bedrosian (2016)



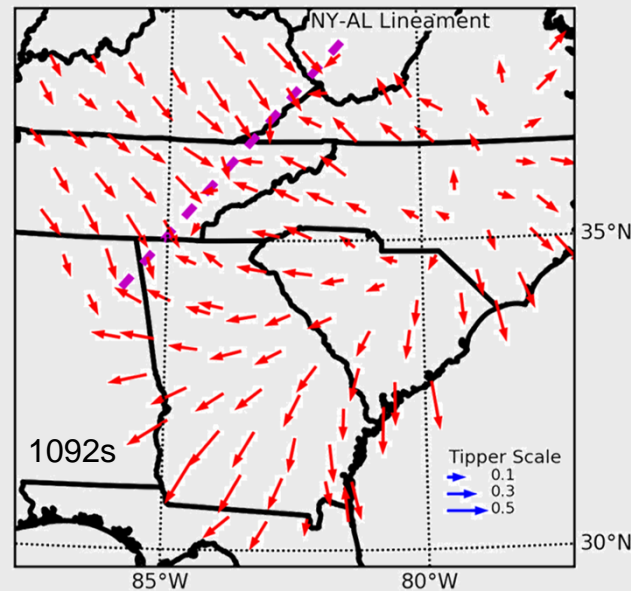




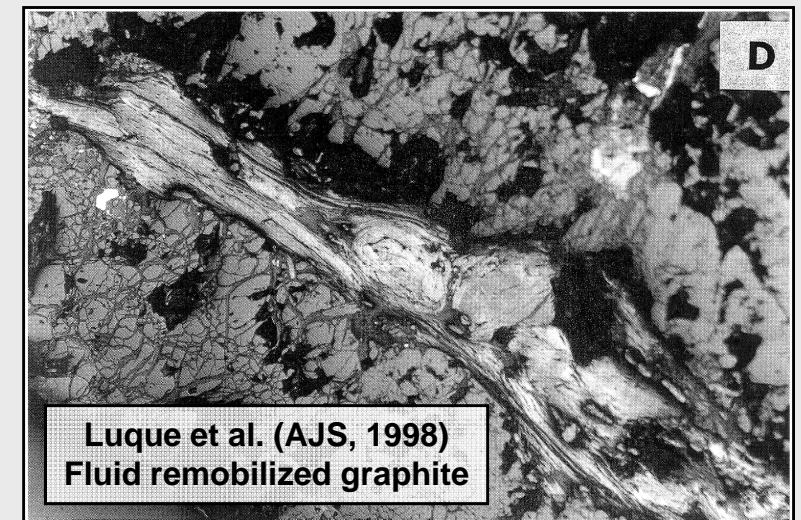
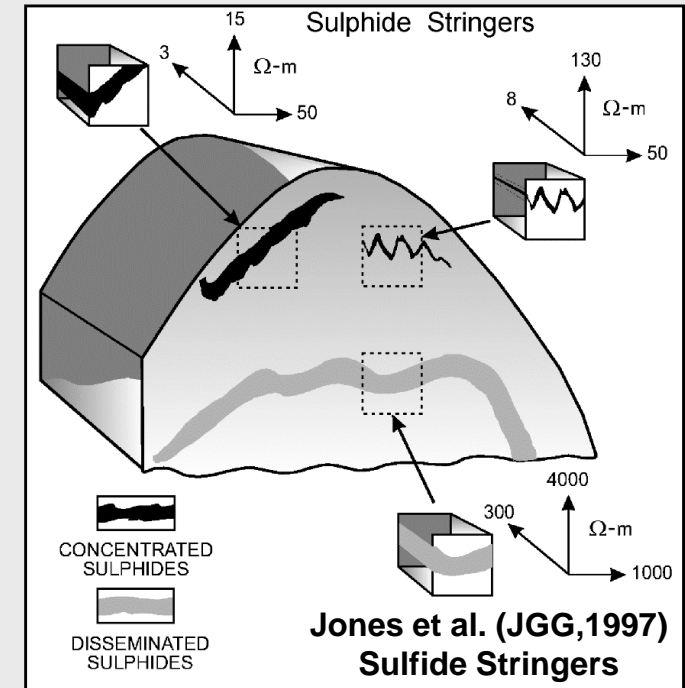
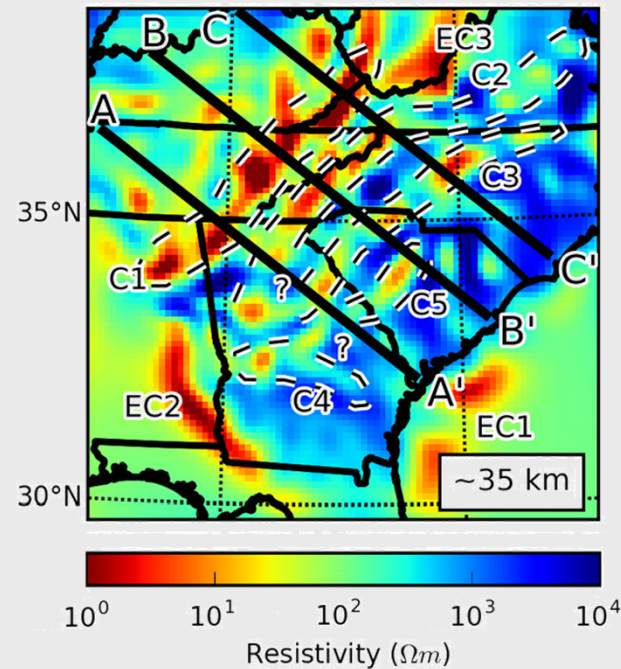
oC-Sd global primary production



oC-Sd sequestration



Murphy and Egbert (2017)



Graphite-sulfide textures in crustal-scale conductors

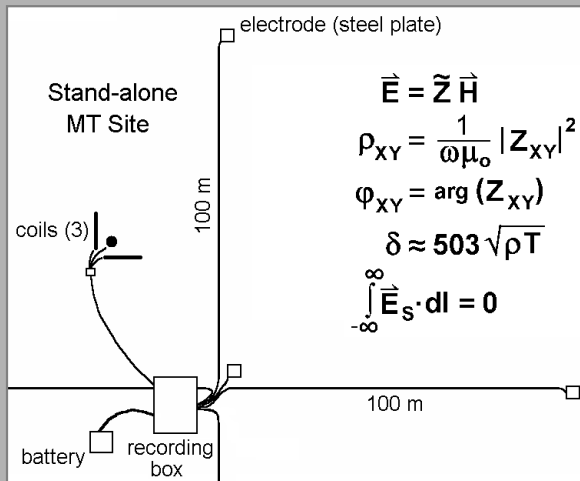




Induction Coil  
(Solenoid)



Ti Electrode w/  
High-Z Preamp



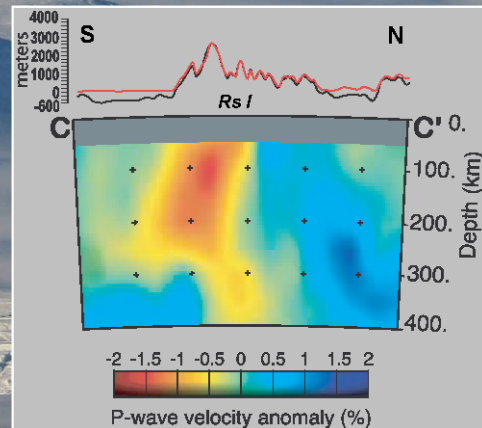
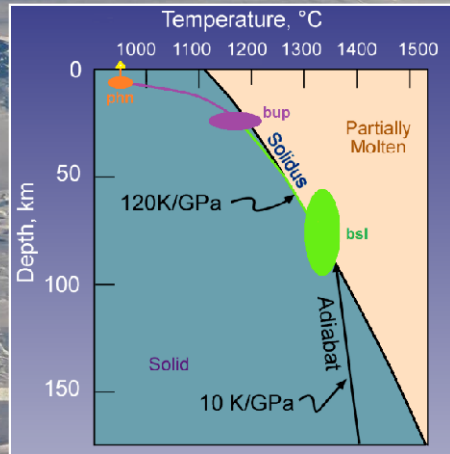
## MT Recording Components For Polar Deployment



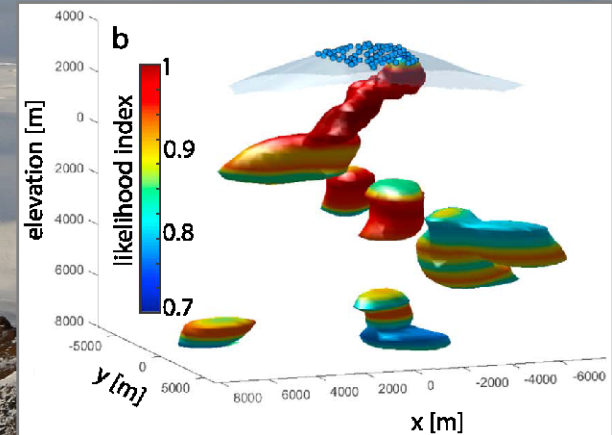
Sync'd MT recorders



# Mount Erebus, Ross Island (G. Hill, P. Wannamaker)

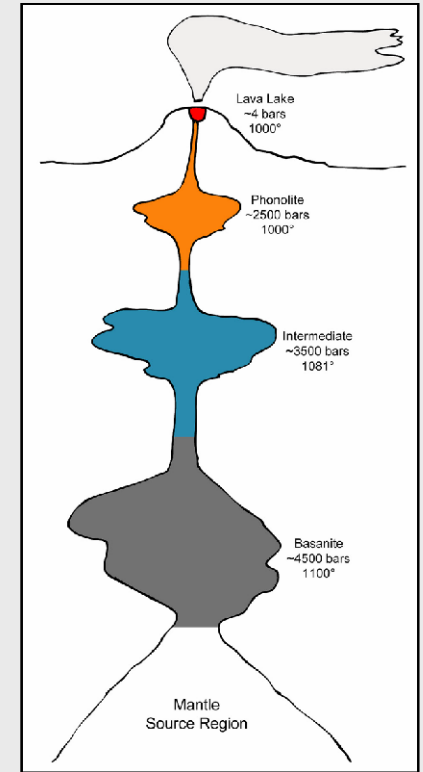
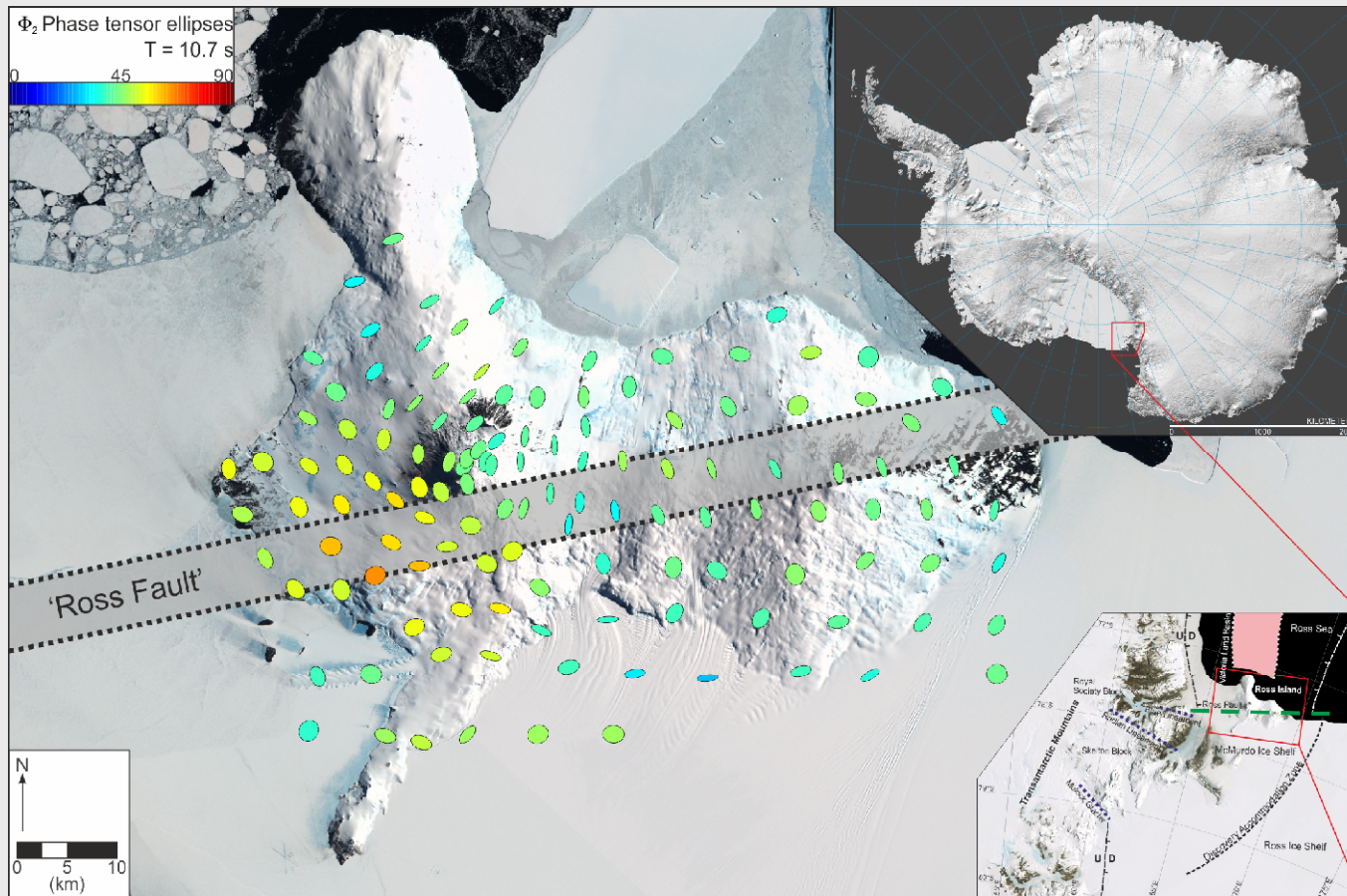


Watson et al (2006)



Blondel et al (2018)



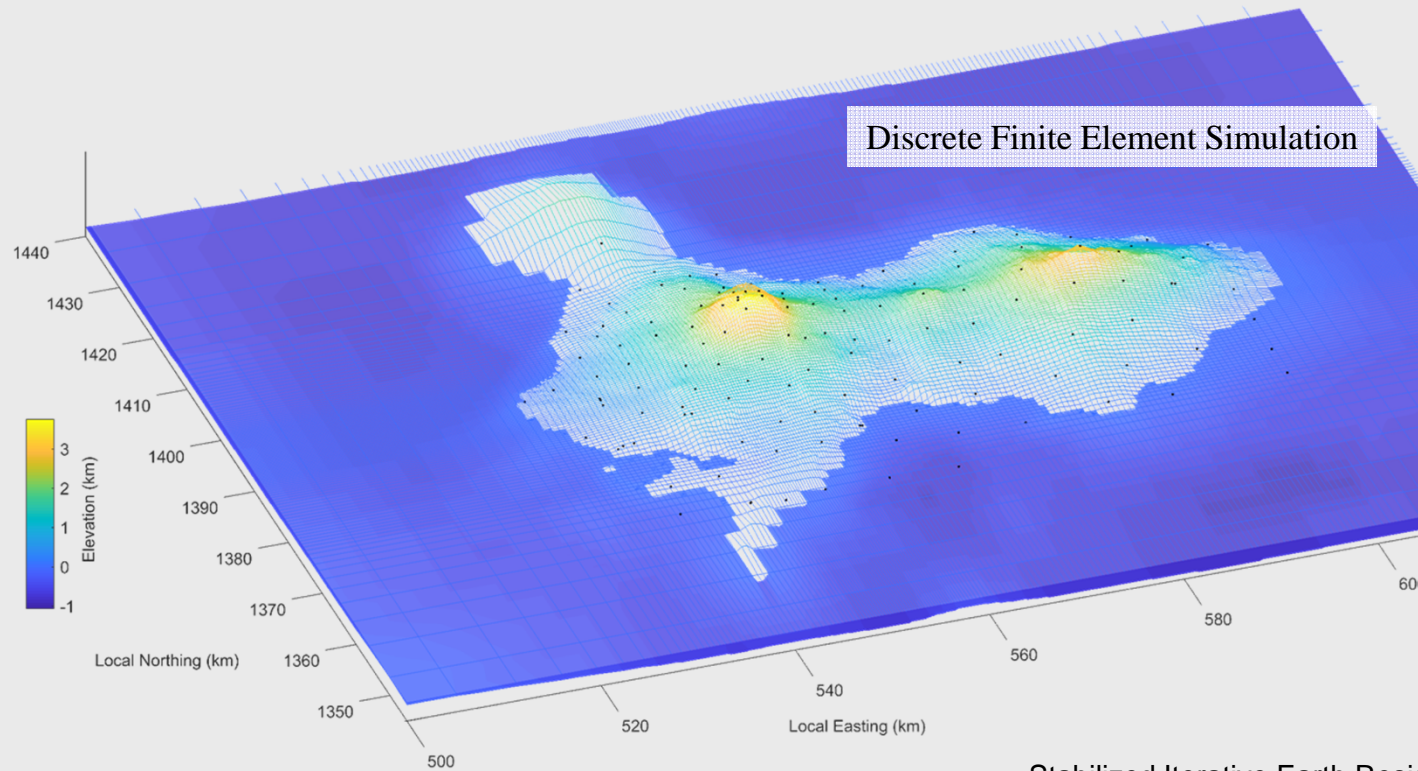


Mount Erebus Magma  
Source and Staging  
(Iacovino et al, 2015,  
after Oppenheimer, 2008)

## Mt Erebus MT Field Campaign: NSF/USAP and RSNZ/AntNZ

**Hill, Wannamaker, Maris, Stodt, Kordy, Wallin,  
Unsworth, Bedrosian, Uhlmann (2014-7)**





$$\begin{aligned}\nabla \times E &= -i\omega\mu H & \nabla \times H &= \partial E \\ \nabla \times \frac{1}{\mu} \nabla \times E - i\omega\partial E &= J^{imp} \\ E &= \sum_{i=1}^{n_e} x_i N_i & H &= \frac{-\nabla \times E}{i\omega}\end{aligned}$$

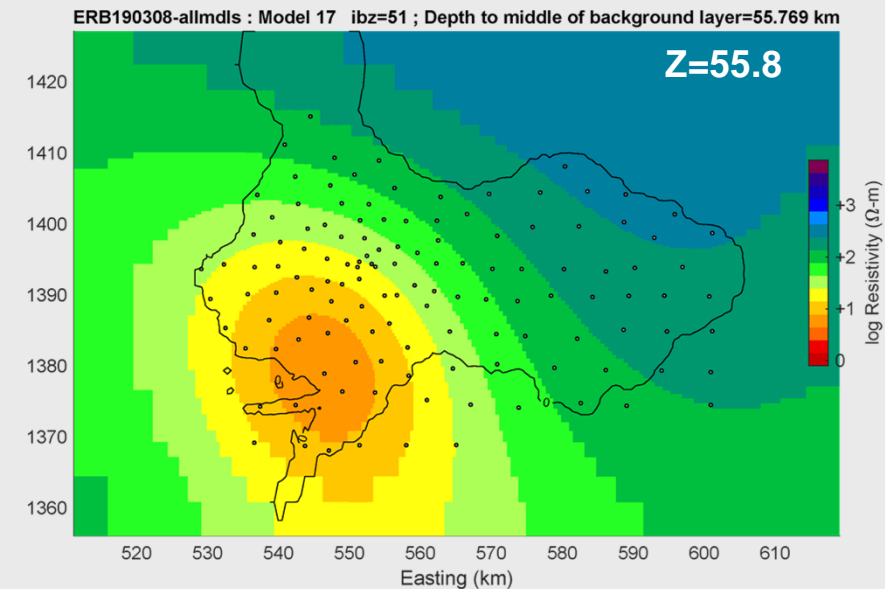
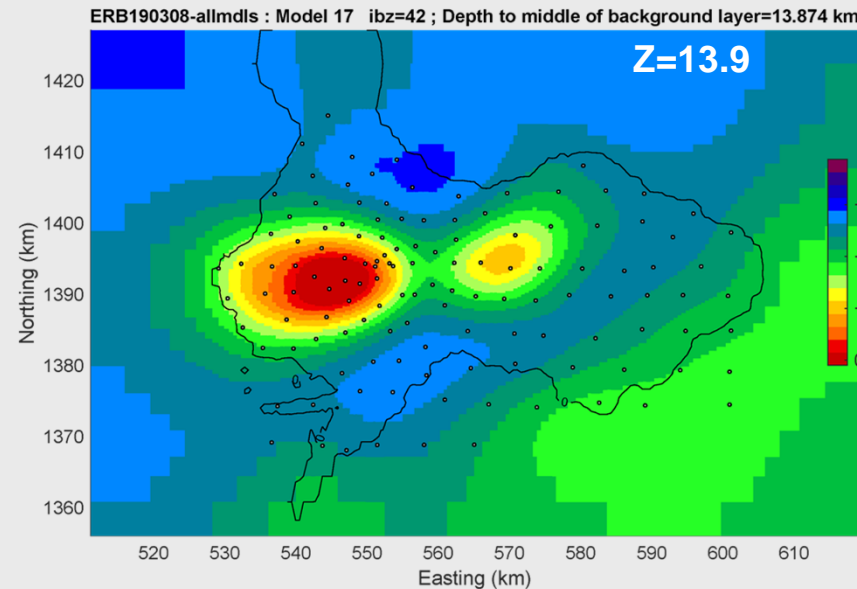
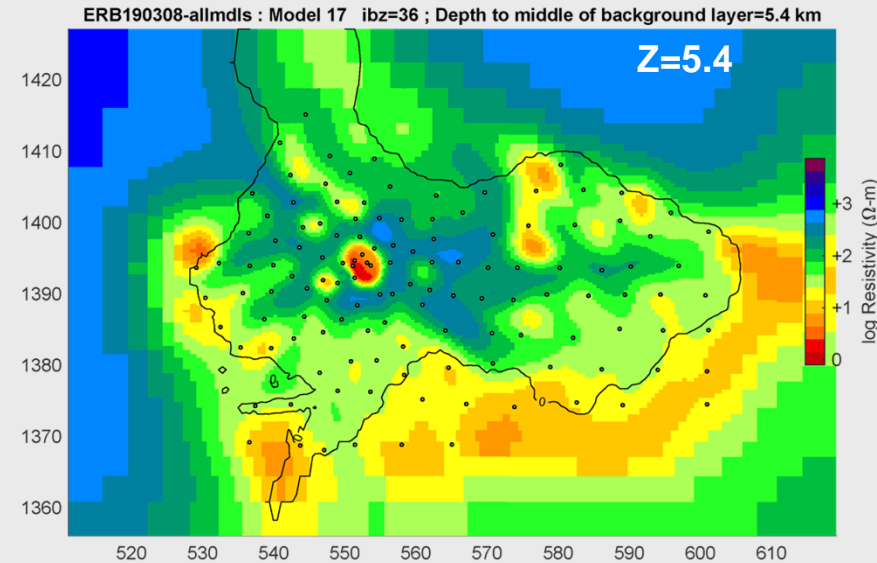
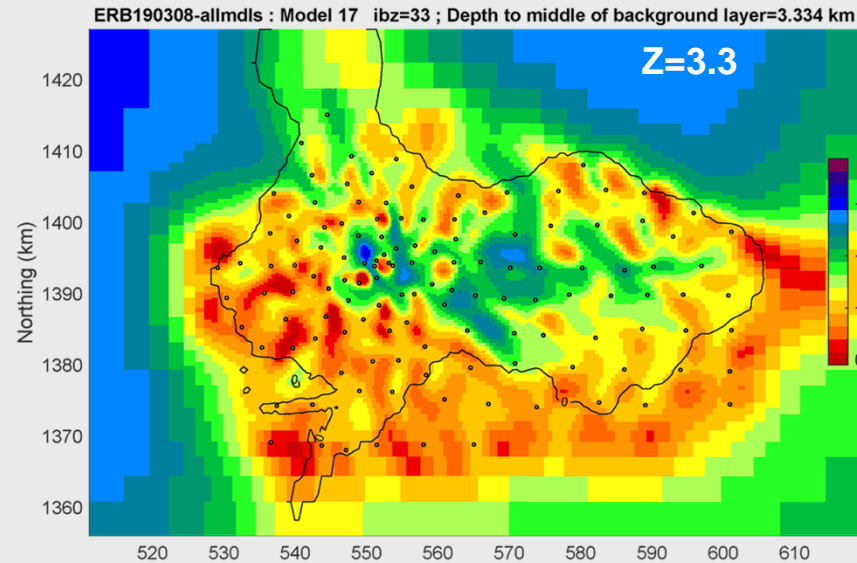
**EM Field (Maxwell) Equations  
And Deformed Finite Element**

Objective:  $W_\lambda(m) = \{(d - F[m])^T C_d^{-1} (d - F[m])\} + \lambda \{(m - m_0)^T C_m^{-1} (m - m_0)\}$

NL Step:  $m_{k+1} - m_k = \{J_k^T C_d^{-1} J_k + \lambda C_m^{-1}\}^{-1} \{J_k^T C_d^{-1} (d_k - F[m_k]) - \lambda C_m^{-1} (m_k - m_0)\}$

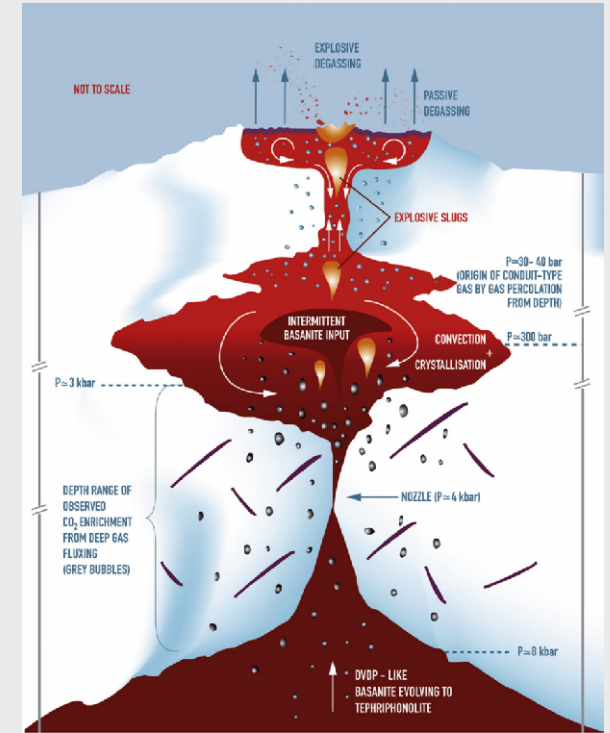
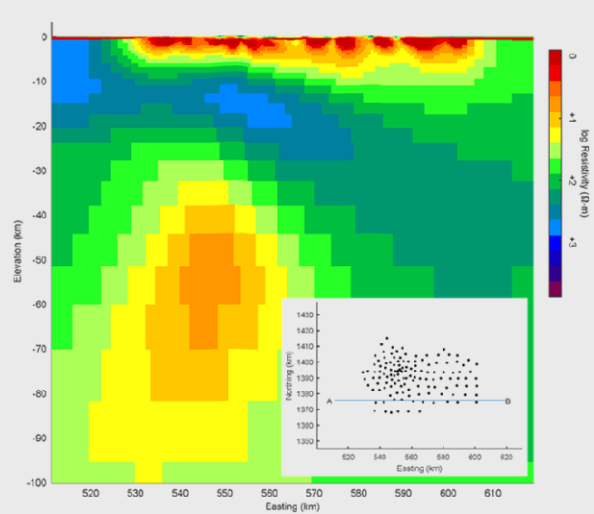
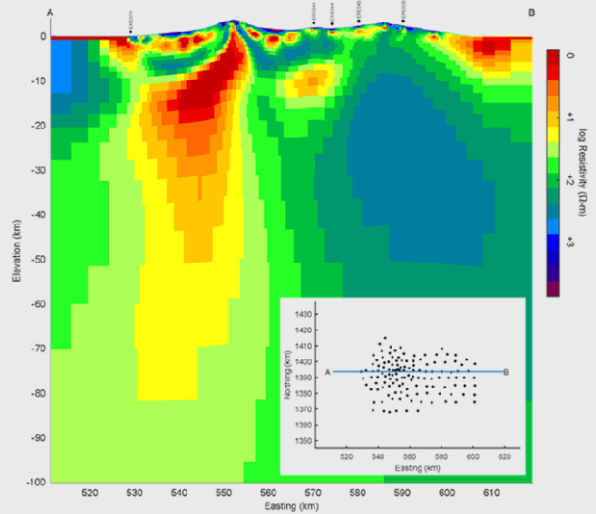
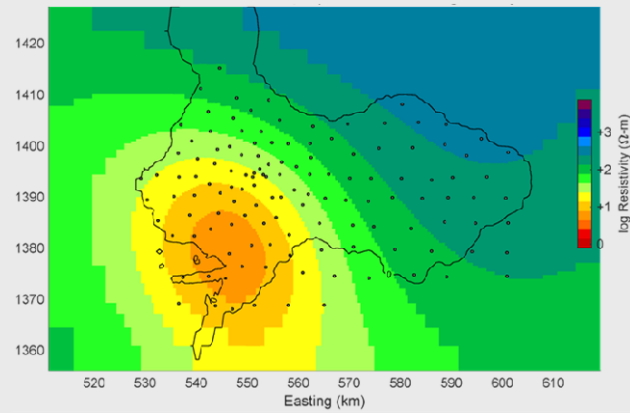
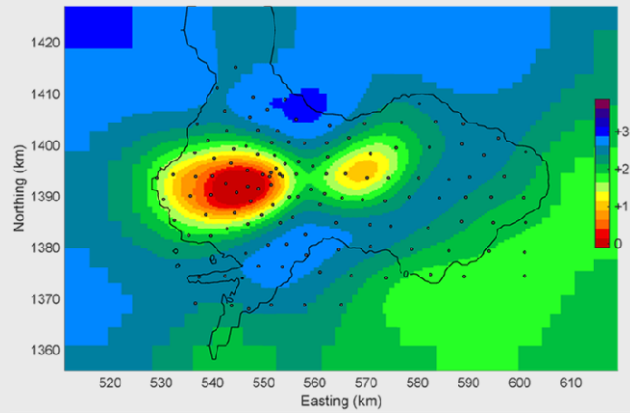
Stabilized Iterative Earth Resistivity Voxel Estim. (Tarantola, 1987)  
NL Step Recast to Data-Space Formulation (Parker, 1994)  
Can Invert for Impedance Static Distortions (Avdeeva et al., 2015)  
Direct Matrix Solutions Used Throughout (Metis, Pardiso, Plasma)  
Parallelized on Large RAM, Single-Box Workstations

**3D MT Inversion of Using Deformable Edge Finite Element Algorithm**  
(Kordy, Wannamaker, et al., 2016, GJI)



## Mount Erebus MT Inversion Resistivity Plan Sections:

- General clay alteration blanket at shallow levels.
- Clear visibility of magmatic conduit and upper chamber by 5 km depth.
- migration of magmatic structure westward along apparent controlling E-W trend.
- Movement of magmatic plumbing southward from lower middle crust and deeper.



Schematic Mount Erebus magmatic plumbing (Oppenheimer et al., 2008). Note “Nozzle” interpreted at 4 kbar for periodic basanite replenishment.

Mount Erebus MT Inversion Plan and Section Views



## Conclusions and Outlook:

- Key elements of MT method in t/s processing and in recognizing heterogeneity developed in 1970s & 80s
- 1990s saw methods for stable modeling of discontinuous E-field
- Current inversion algorithms capable of 1000+ sounding sets
- Proper understanding of petrological principles needed for consistent interpretation and to advance beyond “It’s fluids”
- External constraints on temperature most useful
- Active Great Basin extensional regime seems to exhibit “banana-split” model of crustal rheology
- Potential to evaluate geothermal resources for baseload power
- Wide-scale Juan de Fuca-Gorda hydration of upper mantle
- Carbonized horizons may assist resolving terrane assembly
- Encourage progress in understanding physico-chemical controls on earth material resistivity

The End!

