

1 **Wave attenuation by sea ice in the Arctic marginal ice zone observed by spaceborne**
2 **SAR**

3
4 Bing Qing Huang^{1,2,3} and Xiao-Ming Li^{1,2}

5 ¹ Key Laboratory of Digital Earth Science, Aerospace Information Research Institute, Chinese
6 Academy of Sciences, Beijing, 100094

7 ² International Research Center of Big Data for Sustainable Development Goals, Beijing, 100094

8 ³ University of Chinese Academy of Sciences, Beijing, 100049.

9
10 Corresponding author: Xiao-Ming Li (lixm@radi.ac.cn)

11 **Key Points:**

- 12 • Wave attenuation rate in sea ice was derived based on non-linear inversion of two-
13 dimensional ocean wave spectra by SAR in the Arctic MIZ.
- 14 • The attenuation rate generally follows the exponential law, varying with sea state (wave
15 height and period) and sea ice conditions.
- 16 • Combining previous studies and this one, we may infer that the wave attenuation in the
17 Arctic MIZ is weakening due to sea ice retreat in recent decades.
18

19 **Abstract**

20 Attenuation of ocean waves by ice is a crucial process of the interaction between waves and sea
21 ice in marginal ice zone (MIZ), while such interaction can contribute to the retreating of sea ice
22 in the Arctic. Based on the retrieved two-dimensional ocean wave spectra by spaceborne SAR,
23 we investigated the attenuation of ocean waves in the MIZ in Svalbard and Greenland. The
24 results show that the energy attenuation rate ranges from $0.126 \times 10^{-4}/m$ to $0.618 \times 10^{-4}/m$.
25 Quantitative analysis suggests that the attenuation rate is significantly related to wave height and
26 peak wave period of coming waves. It is further found that the waves decay faster in the area
27 with ice thickness exceeding 0.5 m. We compared the derived wave attenuation rates in the
28 present study with those in previous studies based on in situ measurements, which reveals that
29 waves are becoming less attenuated by sea ice in the Arctic in recent decades.

30

31 **Plain Language Summary**

32 The interaction between sea ice and ocean waves is one of the key processes that accelerates the
33 retreat of sea ice in the Arctic. The attenuation of ocean waves by sea ice is crucial to
34 understanding the wave-ice interaction mechanism and predicting ice changes. Spaceborne
35 Synthetic Aperture Radar (SAR), capable of imaging ocean waves and sea ice in two-dimension
36 with high spatial resolution, has shown tremendous potential in studies on wave-ice interaction.
37 In this study, SAR images acquired in ice-covered areas near Svalbard and east of Greenland
38 were collected, and then ocean wave spectra were retrieved from these SAR images. Ocean wave
39 spectra depict sea states elaborately by showing the wave energy distribution in different
40 frequencies and directions. Subsequently, we derived the wave attenuation rate in sea ice from
41 these wave spectra. By comparing the derived attenuation rates with previous field observations,
42 the study reveals a lower attenuation rate, which suggests the waves were less attenuated by ice
43 in past decades under ongoing retreating and thinning of sea ice in the Arctic. This indicates that
44 waves can penetrate sea ice easier and deeper, which may further induce the retreating of sea ice.

45 **1 Introduction**

46 The interaction between sea ice and ocean waves in the Marginal Ice Zone (MIZ) can
47 contribute to the retreat of sea ice in the Arctic (Dumont et al., 2011; Kohout et al., 2014;
48 Thomson & Rogers, 2014). The retreat of sea ice and the northward shifting of MIZ (Jeffries et
49 al., 2013; Rolph et al., 2020; Serreze et al., 2007) increase the ocean fetches, consequently,
50 promoting the growth of ocean waves (Liu et al., 2016; Thomson & Rogers, 2014). The
51 enhanced waves break more sea ice and lead to further melting, with the combined effect of
52 winds and currents. Subsequently, positive feedback is formed and accelerates sea ice retreats
53 (Kohout et al., 2014; Rolph et al., 2020; Thomson & Rogers, 2014). On the other hand, the
54 energy of ocean waves is damped by sea ice. Determination of the wave attenuation rate is key to
55 estimating the ice-breaking extent (Kohout et al., 2014). In addition, the parametrizing of the
56 attenuation process is essential to improving the accuracy of model prediction, in the short and
57 long terms.

58 Previous studies have shown that attenuation of waves in sea ice is a multifaceted process
59 that can be influenced by incident sea states and ice conditions. Early field experiments carried
60 out in the Bering Sea and the Greenland Sea revealed an exponential decay of wave energy in
61 MIZ, with the attenuation rates ranging from $0.1 \times 10^{-4}/m$ to $8.7 \times 10^{-4}/m$ (Squire & Moore,

62 1980; Wadhams et al., 1988). Generally, the wave attenuation rate was found to decline with
63 increasing wave period (Squire & Moore, 1980; Wadhams et al., 1988). Recent studies show that
64 the wave energy attenuation rate (α_E) also varies with ice conditions. The two field experiments
65 conducted in the Barents Sea (near Svalbard) show that the α_E derived in 1991 experiment
66 (Frankenstein et al., 2001) was approximately 1.3 times larger than that in 2016 (Tsarau et al.,
67 2017). The significant difference between the two experiments was attributed to changes in ice
68 thickness and floe size. In the Antarctic MIZ, the study by Kohout et al. (2020) shows that strong
69 waves with significant wave height (SWH) greater than 3 m still follow the exponential law
70 along with traveling distance in sea ice, while the attenuation rate is also influenced by wave
71 period and sea ice concentration (SIC).

72 A massive amount of data is needed to support a comprehensive understanding of
73 attenuation of waves by sea ice, particularly considering the emergence of rapidly changing ice
74 conditions in the Arctic. In-situ observations on a large scale and over a long period can be
75 challenging in the harsh environment of the pole regions. Synthetic Aperture Radar (SAR) has
76 shown significant potential for observing ocean waves in ice-covered areas (Dawe & Parashar,
77 1978; Lyden et al., 1988; Lyzenga et al., 1985; Raney et al., 1989; Schulz-Stellenfleth et al.,
78 2002; Vachon et al., 1993). Early attempts were made to derive energy attenuation rates in ice
79 based on SAR spectra contrast (Liu et al., 1991; Raney et al., 1989) and they yielded attenuation
80 rates ranging from $0.606 \times 10^{-4}/m$ to $5.7 \times 10^{-4}/m$. However, the method was used under the
81 assumption that imaging of waves by SAR is linear, which, however, often does not hold. The
82 non-linear imaging process of waves by SAR poses challenges in retrieving ocean wave
83 spectrum (OWS) in open water, not to mention in ice-covered areas where the modulation
84 transfer function (MTF) is changed by sea ice (Vachon et al., 1993). An MTF-independent
85 scheme to derive wave height by SAR data was proposed in 1985 (Lyzenga et al., 1985) and was
86 implemented and further developed in recent years (Ardhuin et al., 2015, 2017). With the
87 method, two wave energy attenuation rates were derived, with values of $0.15 \times 10^{-4}/m$ and
88 $0.024 \times 10^{-4}/m$, before and after ice leads, respectively (Stopa et al., 2018). Based on the
89 approach of non-linear retrieval for two-dimensional OWS by SAR in open water (K.
90 Hasselmann & S. Hasselmann, 1991, denoted the MPI approach hereafter), a new MTF-based
91 method to retrieve OWS in ice-covered areas was proposed (Huang & Li 2022), referred to MPI-
92 ICE hereafter. By neglecting the hydrodynamic modulation and involving a new tilt modulation
93 in ice in the MTF, the MPI-ICE reduced the squared error of simulated SAR spectra by
94 approximately 50%, compared to the original MPI approach. The progress further facilitates the
95 application of SAR data to quantitative analysis of waves in MIZ. In this study, we aim to derive
96 the attenuation rate of ocean waves propagating in sea ice in the Arctic MIZ based on the
97 retrieved OWS by spaceborne SAR data. Furthermore, the variations in attenuation with different
98 sea states and ice conditions are analyzed in detail.

99 This paper comprises four sections. Following the introduction, the used data and
100 methods to retrieve OWS by SAR data and to calculate wave attenuation rate are briefly
101 described. Section 3 presents the results based on representative cases. The influences of sea
102 states and ice conditions on wave attenuation were analyzed subsequently. Lastly, we discussed
103 the presented results with the previous observations, and conclusions were drawn.

104 2 Data and Method

105 2.1 Data and study area

106 This study focuses on wave attenuation in the MIZ in Svalbard and Greenland, where the
 107 energetic waves strongly interact with sea ice. The used SAR data are the Sentinel-1 (S1) IW
 108 (Interferometric Wide Swath) Mode GRDH (Ground Range Detect High resolution) product in
 109 Horizontal-Horizontal (HH) polarization. The high spatial resolution (a pixel size of 10 m) and
 110 large coverage (a swath of 250 km) of the IW GRDH data provide a clear view of sea ice and
 111 ocean waves in the MIZ. In the study area, we collected nine S1 IW images (Figure S1 in the
 112 supporting information, SI), presenting clear wave patterns in sea ice in March and April of
 113 2021, when the sea ice achieved the maximum extent of the year. Fourteen transects were
 114 selected along the direction of wave propagation to study wave attenuation, with 130 retrieval
 115 stations set on them. 82% of the stations were in the area with a thickness within 0.3 m, and 76%
 116 were in the compact ice zone with SIC greater than 80%. More details about the selected
 117 transects and additional data used for the attenuation study are described in the SI.

118 2.2 Brief introduction of the MPI-ICE method

119 Three statistic parameters were used to evaluate the accuracy of the retrieved OWS by
 120 SAR using the MPI-ICE method, namely the Converge Index (C.I.), the Correlation between the
 121 simulated and observed SAR spectrum (Cor.), and the squared error of the simulated SAR
 122 spectrum (Err.). The comparison with the results derived by the MPI approach used in open
 123 water shows that the MPI-ICE method reduces the C.I. from 0.83 to 0.54 and decreases the Err.
 124 by nearly 50%, suggesting that the proposed MPI-ICE method is more suitable for retrieval of
 125 two-dimensional wave spectra in ice-covered areas (Huang & Li, 2022). Using the MPI-ICE
 126 method, 130 ocean wave spectra were retrieved in ice-covered areas, and 107 were selected for
 127 further wave attenuation study. The selected data are highly accurate, with average C.I., Err., and
 128 Cor. of 0.37, 0.25, and 97.41%, respectively. The details of data selection and processing are
 129 described in SI.

130 2.3 Calculation of wave attenuation rate

131 As pointed out by previous studies, wave energy decays exponentially in ice-covered
 132 areas. The energy attenuation rate α_E can be calculated based on equation (1).

$$E = E_0 \exp(-\alpha_E x) \quad (1)$$

133 Where E and E_0 represent the energy of waves in the ice and the initial energy of waves when
 134 entering ice-covered areas, respectively. x is the distance that waves propagate in ice. As the
 135 wave energy is proportional to the Hs^2 , the wave energy attenuation rate α_E is twice the wave
 136 height attenuation rate α_H . The latter can be derived by fitting the linear relationship between
 137 $\ln(Hs)$ and x :

$$\ln Hs = -\alpha_H x + b \quad (2)$$

138 The constant b is introduced to represent the $\ln(Hs_0)$, as a reliable Hs_0 in the ice edge is
 139 difficult to determine, where the ice is highly mixed with open water. The inhomogeneous
 140 characteristics of SAR images pose challenges in retrievals. With the derivation of α_H by fitting,
 141 the α_E is derived subsequently.

142 The fitting process is sensitive to data fluctuations, especially in transects with limited
 143 reasonable retrievals. Therefore, a method of seeking a median was employed to determine the
 144 α_H as a supplement. Based on Equations (3) and (2), the set of α_H can be calculated. The SWH
 145 retrieved at station i and its preceding station j are represented as $Hs(i)$ and $Hs(j)$. dx
 146 represents the distance between stations i and j . In instances where the available retrievals along
 147 the transect are less than five, the other transects with comparable incident sea states and ice
 148 conditions were gathered to calculate a set A . The α_H is determined subsequently by seeking the
 149 median. For the transects with a data volume larger than six, the α_H determined by median
 150 seeking is used as a referee.

$$A = \{\alpha_{21}, \alpha_{31}, \alpha_{32} \dots \dots \alpha_{ij}, \dots \dots, \alpha_{NN-1}\} \quad 2 \leq i \leq N, 1 \leq j < i \quad (3)$$

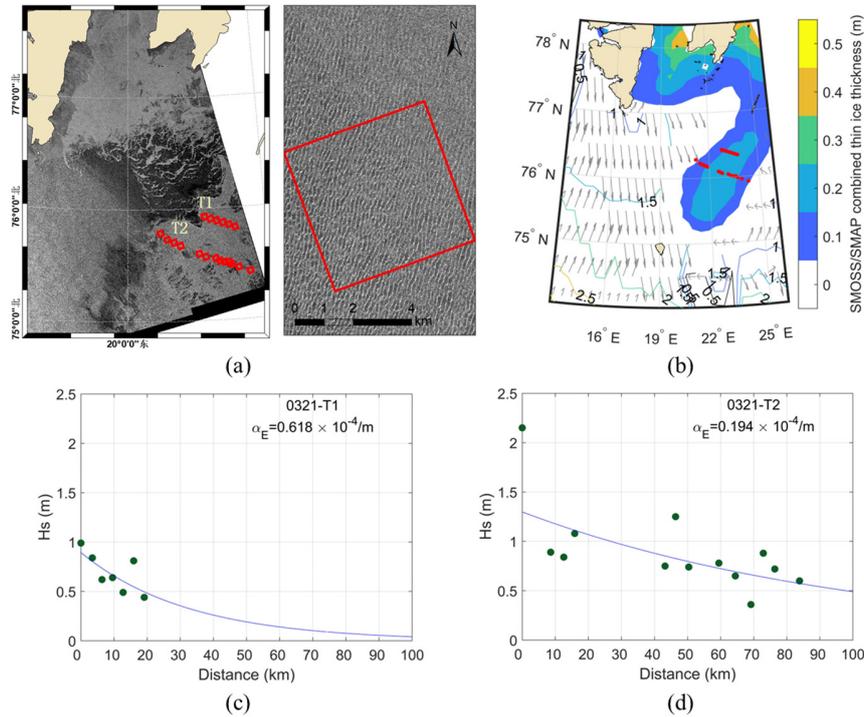
$$\alpha_{ij} = -\frac{d \ln(Hs)}{dx} = -\frac{\ln(Hs(i)) - \ln(Hs(j))}{dx} \quad (2)$$

151 3 Results

152 The α_E derived in this study ranges from $0.126 \times 10^{-4}/m$ to $0.618 \times 10^{-4}/m$ and varies
 153 with ice conditions and sea states. Details of each transect are shown in Table S1. In the cases
 154 selected near Svalbard, where the new ice and young ice with a thickness smaller than 0.3 m
 155 predominated, the waves entered with peak wave period (PWP) shorter than 12 s and initial
 156 SWH ranges from 0.52 m to 2.15 m. The calculated α_E ranges from $0.198 \times 10^{-4}/m$ to
 157 $0.618 \times 10^{-4}/m$. In the cases east of Greenland, in addition to the dominated young ice and thin
 158 first-year ice, thick first-year ice and old ice with thickness exceeding 0.5 m existed in the inner
 159 of selected transects. Waves entered the Greenland ice-covered areas with PWP over 13 s and an
 160 initial SWH of approximately 2 m. The α_E ranges from 0.126 to $0.270 \times 10^{-4}/m$, generally
 161 lower than those achieved near Svalbard ($0.198 \sim 0.618 \times 10^{-4}/m$). Two cases in Svalbard and
 162 Greenland are presented in the following for detailed analysis.

163 3.1 Wave attenuation of representative cases

164 The first case presented is that ocean waves propagated in the Svalbard MIZ on March
 165 21, 2021. Figure 1 (a) displays the S1 IW image and the enlarged view of a sub-image showing
 166 clear wave patterns in ice-covered areas. The two transects 0321-T1 and 0321-T2 were selected
 167 from the ice edge to the edge of the S1 image along the propagation direction of the
 168 southeastward wave, spanning the distance of 28 km and 97 km, respectively. Figure 1 (b) shows
 169 the SMOS (Soil Moisture and Ocean Salinity)/SMAP (Soil Moisture Active Passive) combined
 170 sea ice thickness (SIT) of the day. The ice thickness along both transects was less than 0.3 m.
 171 The ERA5 (European Center for Medium-Range Weather Forecasts Reanalysis v5) wave
 172 product (the contours and arrows in Figure 1 (b)) shows the incident waves had SWH of 1.9 m
 173 and propagated southeastward.



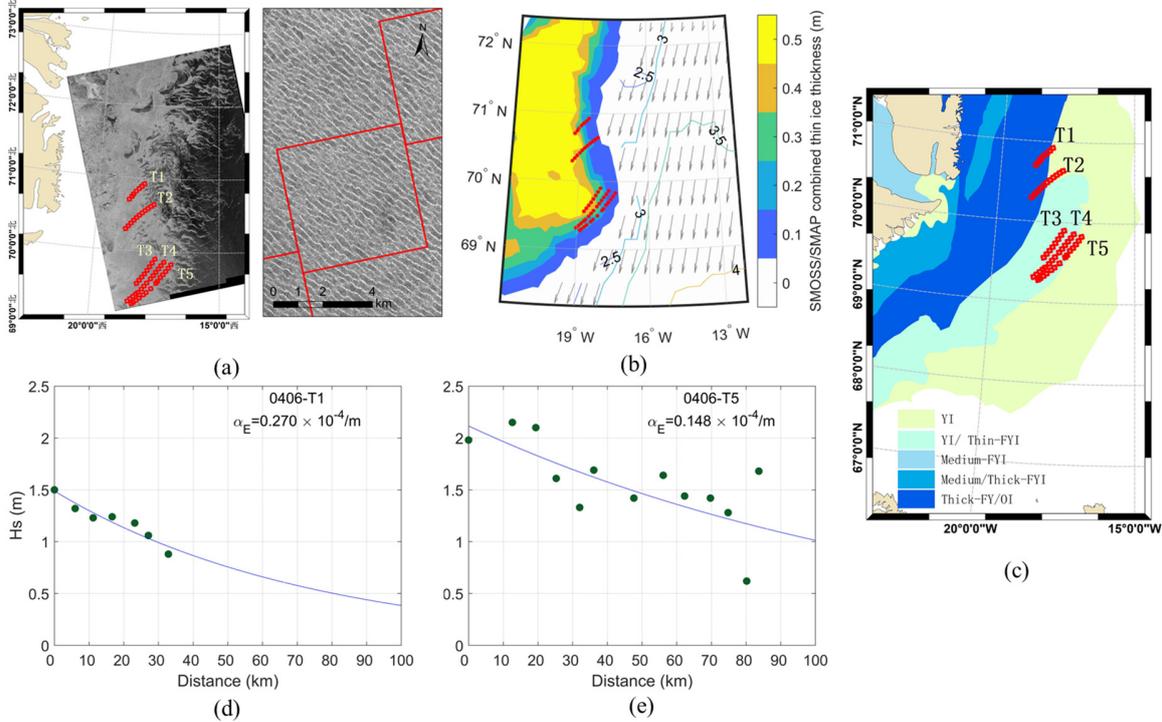
174

175 **Figure 1.** The case on March 21, 2021, in Svalbard: (a) shows the S1 IW image acquired
 176 covering part of Svalbard (the northern part of the image). The red squares in the two transects
 177 represent the sub-images selected for retrievals of OWS. The enlarged view of a sub-image in
 178 transect 0321-T2 is shown in the right panel. (b) is the corresponding map of thin ice thickness.
 179 The red dots in the image represent the locations of sub-images. The contours and gray arrows
 180 show the SWH and mean wave direction of the most energetic wave system in this region. (c)
 181 and (d) show the attenuation of SWH along the transects 0321-T1 and 0321-T2, with the blue
 182 lines representing the fitted line based on the exponential model.

183 The changes of SWH along the transects 0321-T1 and 0321-T2 are shown in Figure 2(c)
 184 and (d). The α_E in 0321-T1 is $0.618 \times 10^{-4}/m$, which is much higher than that
 185 ($0.194 \times 10^{-4}/m$) in transect 0321-T2. The difference can be partially attributed to the initial
 186 SWH (0.99 m vs. 2.15 m), while the ice condition (new ice and young ice) and initial PWP (~ 10
 187 s) along the two transects were nearly identical. Although the two transects are only
 188 approximately 30 km away, the major discrepancy of initial SWH is caused by the shadow effect
 189 of Svalbard. Moreover, sea ice also covers a partial region in the northwest of transect 0321-T1,
 190 and the fetch is significantly reduced for the growth of waves as the wind blows from the
 191 northwest (inferred from the ERA-5 wave data).

192 错误!未找到引用源。 shows the case east of the Greenland Sea on April 6, 2021.
 193 Figure 2 错误!未找到引用源。 (a) is the S1 IW image and the enlarged view of a sub-image in
 194 0406-T4, presenting clear wave patterns. From the ice edge to where wave patterns vanished
 195 (visual inspection), transects 0406-T1, T2, and T3 were selected with lengths of 33 km,
 196 and 46 km, respectively. As the map of sea ice thickness in Figure 2 (b) reveals, the three
 197 transects were located partially in the area where ice thickness exceeded 0.5 m. Especially the
 198 transect 0406-T1, as shown from the map of ice type on April 8 (Figure 2 (c), based on the U.S.

199 National Ice Center Arctic Sea Ice Charts and Climatologies in Gridded Format product, referred
 200 to NIC ice chart hereafter), the transect located in the area dominated by thick first-year ice and
 201 old ice with the typical ice thickness exceeded 1.2 m (WMO, 2010). Transects 0406-T4 and
 202 0406-T5 were chosen near the ice edge, where the ice thickness was less than 0.4 m. The waves
 203 propagated over 80 km along transects T4 and T5 before entering the open sea again.



204

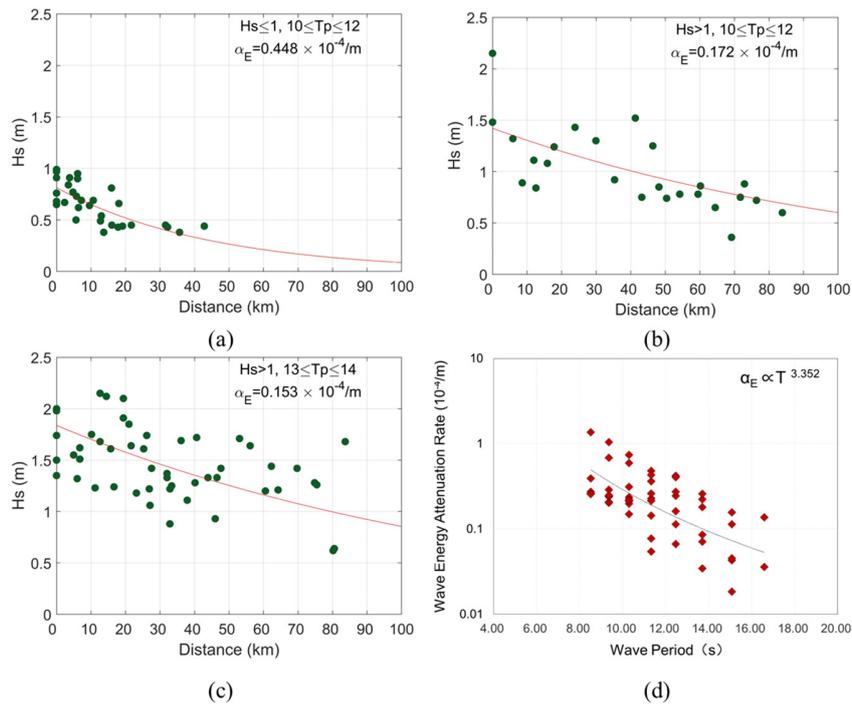
205 **Figure 2.** (a) S1 IW images acquired on April 6, 2021, in the east of the Greenland Sea, and the
 206 enlarged view of the sub-image is shown in the right panel. The red squares represent the sub-
 207 sub-images selected for retrieval. (b) is the corresponding map of the SMOS/SMAP SIT. The red
 208 dots represent the sub-image locations. (c) shows the map of ice type based on the NIC ice chart
 209 product on April 8. (d) and (e) show SWH changes along the transects 0406-T1 and 0406-T5,
 210 respectively, with the blue line representing the fitted line.

211 Here only the variations of SWH in transect 0406-T1 and T5 are presented in Figure 2 (d)
 212 and (e), respectively. Along the transect 0406-T1, the waves were attenuated faster than those in
 213 0406-T5, with an energy attenuation rate of $0.270 \times 10^{-4}/m$ vs. $0.148 \times 10^{-4}/m$. Besides, the
 214 wave patterns in SAR images can reveal that the waves were attenuated with different rates in
 215 the two transects. In 0406-T1, wave patterns are invisible in the S1 image after propagating
 216 approximately 50 km in the ice-covered area, whereas the waves in 0406-T5 propagated over 80
 217 km before entering the open water again. The difference is considered to be attributed to ice
 218 conditions. As shown in Figure 2 (c), the inner parts of transects 0406-T1 were occupied by thick
 219 first-year ice and old ice. Therefore, it is inferred that the SIT in 0406-T1 should be much thicker
 220 than that in 0406-T5 (where the young ice and thin first-year ice with a thickness within 0.4 m
 221 dominated). The discrepancy in ice thickness may explain why the α_E in 0406-T1 is
 222 approximately two times higher than that in 0406-T5, while their initial SWH and PWP are
 223 comparable.

224 In addition to the influence of initial SWH on wave attenuation rate, the influence of
 225 incident PWP is demonstrated through the comparison between the two presented cases in
 226 transect 0321-T2 (Figure 1(d)) and 0406-T5 (Figure 2 (e)). Both transects were selected in the
 227 area with ice thickness smaller than 0.4 m, and the initial SWHs are approximately 2 m.
 228 However, the PWP of waves in 0406-T5 was longer (13.11 s) than that (10.08 s) of 0321-T2.
 229 Consequently, the waves in 0406-T5 attenuated with a smaller α_E of $0.148 \times 10^{-4}/m$,
 230 compared with the α_E in 0321-T2 of $0.194 \times 10^{-4}/m$.

231 3.2 Variation of wave attenuation with sea state

232 To gain further insight into the characteristics of attenuation rates, the retrieved results
 233 were divided into three groups based on the initial SWH (represented as H_s) and PWP
 234 (represented as T_p), as displayed in Figure 3. The results show that the waves with $H_s \leq 1$ m
 235 and $10 \leq T_p \leq 12$ s exhibit the largest α_E , with a value of $0.448 \times 10^{-4}/m$. For waves with
 236 $H_s > 1$ m and $10 \leq T_p \leq 14$ s, the attenuation rate has some fluctuations, as demonstrated in
 237 Figure 3 (b) and (c). In Figure 3 (b), the α_E of $0.172 \times 10^{-4}/m$ is achieved for waves with
 238 higher SWH ($H_s > 1$ m) yet still with $10 \leq T_p \leq 12$ s. For (c), the α_E of $0.0153 \times 10^{-4}/m$ is
 239 achieved under the condition that waves with initial SWH greater than 1 m (but not higher than
 240 2.15 m) and $T_p \geq 13$ s (but no longer than 14 s).



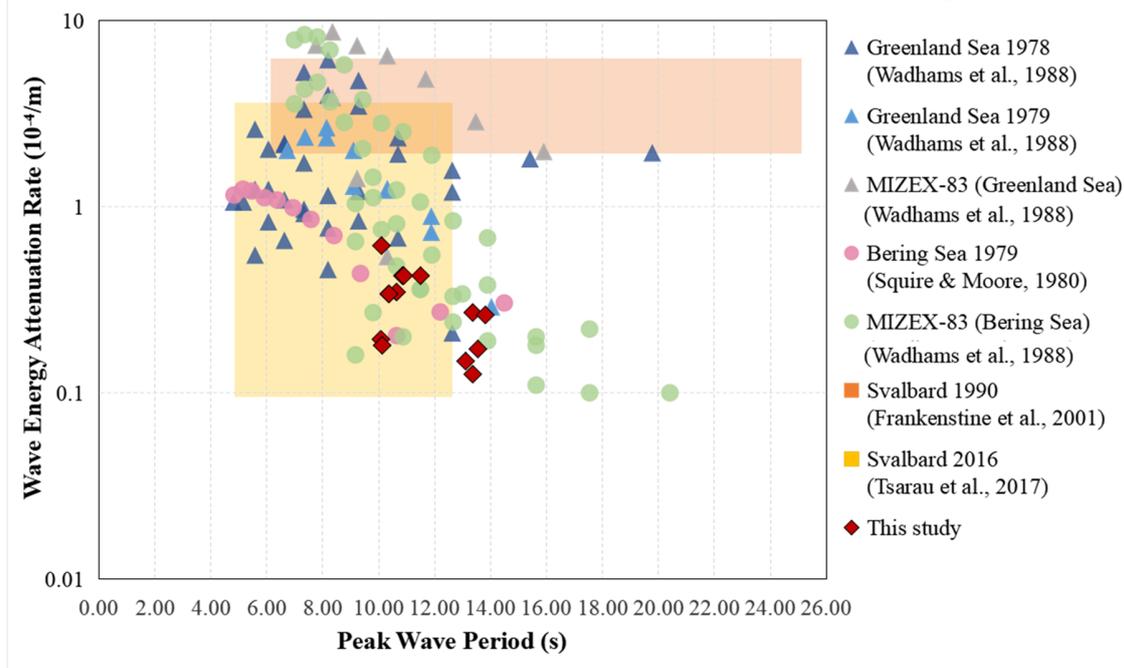
241
 242 **Figure 3.** Wave attenuation rates under various sea states: (a) $H_s \leq 1$ m and $10 \leq T_p \leq 12$ s; (b)
 243 $H_s > 1$ m and $10 \leq T_p \leq 12$ s; (c) $H_s > 1$ m and $13 \leq T_p \leq 14$ s. (d) shows the attenuation rate
 244 changes with the wave period.

245 By Integrating all the S1-retrieved ocean wave spectra along the directions, the frequency
 246 spectra were derived, and then the energy attenuation rate at each frequency bin was calculated.

247 As illustrated by Figure 3 (d), the wave energy attenuation rate declines with the increasing wave
 248 period. It is inversely proportional to $T^{3.4}$.

249 **4 Discussion and conclusion**

250 We compared the SAR-derived wave energy attenuation rate in this study with those
 251 achieved in previous studies based on in situ measurements, as illustrated in Figure 4.



252 **Figure 4.** Comparison of the wave attenuation rate in the present study (red diamonds) with
 253 those achieved in previous studies in the Arctic MIZ.
 254

255 The α_E achieved in the Greenland Sea in the Marginal Ice Zone Experiment (MIZEX)
 256 and earlier field experiments (Wadhams et al., 1988) are depicted in Figure 4, with navy blue,
 257 blue, and gray rectangles representing the results derived based on the experiments in 1978,
 258 1979, and 1983, respectively. The α_E derived in the east of Greenland has a range of
 259 $0.21 \sim 8.72 \times 10^{-4}/m$, with 91% of results exceeding $0.618 \times 10^{-4}/m$ (the maximum value of
 260 wave attenuation rate derived in this study). We noticed that the multiyear ice with an average
 261 thickness of 3.1 m existed during the experimental period in the Greenland Sea (Wadhams et al.,
 262 1988). However, the study area of this paper was primarily dominated by new ice, young ice, and
 263 thin first-year ice. As thick ice is known to damp wave energy more effectively than thin ice
 264 (Robin 1963; Rogers et al., 2021), it is no surprise that a higher α_E was found in the early
 265 observations. In contrast, thin and small floes dominated the Bering Sea during the MIZEX
 266 (Wadhams et al., 1988) and early field experiments (Squire & Moore, 1980), similar to the ice
 267 conditions in this study. The α_E derived in the Bering Sea experiments ranges from
 268 $0.1 \times 10^{-4}/m$ to $8.41 \times 10^{-4}/m$ with 55% results lower than $1 \times 10^{-4}/m$, which is
 269 comparable to the results derived in this study ($0.126 \sim 0.618 \times 10^{-4}/m$). However, the short
 270 waves with peak periods shorter than 10 s were observed in the Bering Sea field experiments,
 271 while the wave period in this study ranges from 10 s to 14 s. Correspondingly, the attenuation
 272 rates derived in this study have a lower up boundary than those observed in the Bering Sea field
 273 experiment. Additionally, the thickness of sea ice in the Bering Sea ranged from 0.4 m to 1.2 m,

274 which is thicker than those in this study (with an average of 0.2 m). The thick ice also
275 contributed to the higher attenuation rates derived from the Bering Sea experiments.

276 The yellow and orange blocks represent the α_E ranges derived in the experiments
277 conducted near Svalbard in the spring of 1990 (Frankenstein et al., 2001) and 2016 (Tsarau et al.,
278 2017), respectively. We noticed an interesting phenomenon that the wave attenuation rates
279 achieved near Svalbard show a declining trend. In the experiment Svalbard 1991, the area was
280 predominated by ice with an average thickness of 1.3 m and a SIC of nearly 100%. The derived
281 α_E ranges from $2 \times 10^{-4}/m$ to $6 \times 10^{-4}/m$, which is generally higher than those derived in the
282 experiment Svalbard 2016 ($0.1 \sim 3.5 \times 10^{-4}/m$). In our study, the attenuation rates in the
283 Svalbard cases are in the range of $0.126 \sim 0.618 \times 10^{-4}/m$, which is near the low boundary of
284 Svalbard 2016 ($0.1 \times 10^{-4}/m$). The ice conditions in this study (average thickness of 0.2 m) are
285 similar to that in 2016 (with an average of 0.3 m) and show a significant decline in ice thickness
286 since the 1990 experiment. Waves were less damped by thin ice and yielded smaller α_E
287 correspondingly.

288 The α_E achieved in the Svalbard 2016 experiment has a high-up boundary
289 ($3.5 \times 10^{-4}/m$), which corresponds to the waves with a period ranging from 5 s to 10 s.
290 However, the wave period in this study ranged from 10 s to 14 s and the analysis in the previous
291 subsection suggests that waves with longer periods have lower attenuation rates than those with
292 short periods. Therefore, the corresponding α_E in this study is generally lower than those
293 achieved in the 2016 experiment. Within the same period range, i.e., 10~12.5 s, the attenuation
294 rates derived in the 2016 experiment were approximately $0.1 \times 10^{-4}/m$, which is lower than
295 those derived in this study ($0.180 \sim 0.618 \times 10^{-4}/m$). We noticed that the waves observed in the
296 Svalbard 2016 experiment entered ice-covered areas with SWH up to 3 m. However, the incident
297 waves carried less energy in this study, with the largest initial SWH of 2.15 m, and therefore,
298 they are easier damped by sea ice and result in higher attenuation rates.

299 In this study, based on SAR-derived two-dimensional OWS in ice-covered areas, we
300 analyzed wave attenuation in the MIZ in Svalbard and Greenland through a few cases. The
301 attenuation rate of wave energy follows the exponential law against traveling distance, consistent
302 with previous studies conducted in the Arctic. This also suggests the reliability of the MPI-ICE
303 retrievals based on SAR observations to derive ocean wave attenuations, compared with previous
304 studies using in situ buoy observations.

305 The analysis illustrates that the attenuation of waves in ice is a complex process
306 vulnerable to sea states and ice conditions. Among the cases, the largest α_E is achieved for SWH
307 lower than 1 m and PWP shorter than 12 s. The higher waves with longer periods (swells)
308 generally decay slower. For waves in ice-covered areas with thickness exceeding 0.5 m, the α_E is
309 approximately 2 times higher than that derived in thin-ice areas. Although the attenuation of
310 waves in sea ice is governed by a few factors of sea state and sea ice conditions, the changing
311 trend of the wave attenuation in Svalbard may reflect a reality that the ocean waves are less
312 attenuated by sea ice in the Arctic MIZ in recent decades. The dramatic change of sea ice
313 emerging in the Arctic triggers more complicated wave-ice interaction than ever. We need to
314 collect extensive data on various sea states and ice conditions for a comprehensive understanding
315 of such interactions and their feedback on ice retreats.

317 **Acknowledgments**

318 We thank the European Space Agency for providing the Sentinel-1 data, and the National
 319 Marine Environment Forecasting Center for providing the WW3 model data. The ERA5
 320 reanalysis data were downloaded from
 321 [https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels-monthly-](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels-monthly-means?tab=form)
 322 [means?tab=form](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels-monthly-means?tab=form). The SMOS and SMAP combined thickness of thin ice product, as well as the
 323 AMSR-2 sea ice concentration product, were downloaded from [https://seaice.uni-](https://seaice.uni-bremen.de/data/)
 324 [bremen.de/data/](https://seaice.uni-bremen.de/data/). The U.S. National Ice Center Arctic and Antarctic Sea Ice Charts were
 325 downloaded from <https://nsidc.org/data/g10013/versions/1>. The study was supported by the
 326 National Science Fund for Distinguished Young Scholars (42025605).
 327

328 **References**

- 329 Arduin, F., Collard, F., Chapron, B., Girard-Arduin, F., Guitton, G., Mouche, A., et al. (2015).
 330 Estimates of ocean wave heights and attenuation in sea ice using the SAR wave mode on
 331 Sentinel-1A. *Geophysical Research Letters*, 42, 2317-2325.
 332 <https://doi.org/10.1002/2014GL062940>
- 333 Arduin, F., Stopa, J., Chapron, B., Collard, F., Smith, M., Thomson, J., et al. (2017). Measuring
 334 ocean waves in sea ice using SAR imagery: A quasi-deterministic approach evaluated with
 335 Sentinel-1 and in situ data. *Remote Sensing of Environment*, 189, 211-222.
 336 <http://dx.doi.org/10.1016/j.rse.2016.11.024>
- 337 Dawe, B., & Parashar, S. (1978). *SAR Imaging of waves in ice*. Paper presented at Oceans '78,
 338 Washington, DC. <https://doi.org/10.1109/OCEANS.1978.1151122>
- 339 Dumont, D., Kohout, A.L., & Bertino, L. (2011). A wave-based model for the marginal ice zone
 340 including a floe breaking parameterization. *Journal of Geophysical Research Oceans*, 116(C4),
 341 1-10. <https://doi.org/10.1029/2010JC006682>
- 342 Fernand, M. (1994). Topographic distance and watershed lines. *Signal Processing*, 38, 113-125.
 343 [https://doi.org/10.1016/0165-1684\(94\)90060-4](https://doi.org/10.1016/0165-1684(94)90060-4)
- 344 Frankenstein, S., Løset, S., & Shen, H.H. (2001). Wave-ice interactions in Barents Sea marginal
 345 ice zone. *Journal of Cold Regions Engineering*, 15 (2), 91-102.
 346 [https://doi.org/10.1061/\(asce\)0887-381x\(2001\)15:2\(91\)](https://doi.org/10.1061/(asce)0887-381x(2001)15:2(91))
- 347 Hasselmann, K., & Hasselmann, S. (1991). On the nonlinear mapping of an ocean wave
 348 spectrum into a synthetic aperture radar image spectrum and its inversion. *Journal of*
 349 *Geophysical Research Oceans*, 96(C6), 10713-10729. <https://doi.org/10.1029/91JC00302>
- 350 Huang, B. & Li, X-M. (2022). Study on retrievals of ocean wave spectrum by spaceborne SAR
 351 in ice-covered areas. *Remote Sensing*. 2022, 14(23), 6086. <https://doi.org/10.3390/rs14236086>

- 352 Jeffries, M.O., Overland, J.E., & Perovich, D.K. (2013). The Arctic shifts to a new normal.
353 *Physics Today*, 66 (10), 35. <https://doi.org/10.1063/PT.3.2147>
- 354 Kohout, A.L., Williams, M.J.M., Dean, S.M., & Meylan, M.H. (2014). Storm-induced sea-ice
355 breakup and the implications for ice extent. *Nature*, 509, 604-607.
356 <https://doi.org/10.1038/nature13262>
- 357 Kohout, A. L., Smith, M., Roach, L. A., Williams, G., Montiel, F., & Williams, M. J. M. (2020).
358 Observations of exponential wave attenuation in Antarctic sea ice during the PIPERS campaign.
359 *Annals of Glaciology*, 61(82), 196-209. <https://doi.org/10.1017/aog.2020.36>
- 360 Liu, A.K., Holt, B., & Vachon, P.W. (1991). Wave propagation in the marginal ice zone: Model
361 predictions and comparisons with buoy and synthetic aperture radar data. *Journal of Geophysical*
362 *Research Oceans*, 96(C3), 4605-4621. <https://doi.org/10.1029/90JC02267>
- 363 Liu, Q., Babanin, A.V., Zieger, S., Young, I.R., & Guan, C. (2016). Wind and wave climate in
364 the Arctic Ocean as observed by altimeters. *Journal of Climate*, 29(22), 7957-7957.
365 <https://doi.org/10.1175/JCLI-D-16-0219.1>
- 366 Lyden, J., Schuchman, R., Zago, C., Rottier, R., Wadhams, P., & Jahannessen, O. (1988). SAR
367 imaging of ocean waves in the Marginal Ice Zone. *IEEE Geoscience and Remote Sensing*
368 *Symposium 1988*, IEEE, Edinburgh, Scotland. <https://doi.org/10.1109/IGARSS.1988.569488>
- 369 Lyzenga, D.R., Shuchman, R.A., & Lyden, J.D. (1985). SAR imaging of waves in water and ice:
370 Evidence for velocity bunching. *Journal of Geophysical Research Oceans*, 90(C1), 1031-1036.
371 <https://doi.org/10.1029/JC090iC01p01031>
- 372 Raney, R.K., Vachon, P.W., De Abreuet, R.A., & Bhogal, A.S. (1989). Airborne SAR
373 observations of ocean surface waves penetrating floating ice. *IEEE Transactions on Geoscience*
374 *and Remote Sensing 1989*, 27(5), 492-500. <https://doi.org/10.1109/TGRS.1989.35932>
- 375 Robin, G.Q. (1963). Wave propagation through fields of pack ice. *Philosophical Transactions of*
376 *the Royal Society of London*, 255(1057),313-339. <https://doi.org/10.1098/rsta.1963.0006>
- 377 Rogers, W.E., Meylan, M.H., & Kohout., A.L. (2021). Estimates of spectral wave attenuation in
378 Antarctic sea ice, using model/data inversion. *Cold Regions Science and Technology*, 182,1-13.
379 <https://doi.org/10.1016/j.coldregions.2020.103198>
- 380 Rolph, R.J., Feltham, D.L., & Schröder, D. (2020). Changes of the Arctic marginal ice zone
381 during the satellite era. *The Cryosphere*, 14(6), 1971-1984. [https://doi.org/10.5194/tc-14-1971-](https://doi.org/10.5194/tc-14-1971-2020)
382 [2020](https://doi.org/10.5194/tc-14-1971-2020)
- 383 Schulz-Stellenfleth, J., & Lehner, S. (2002). Spaceborne synthetic aperture radar observations of
384 ocean waves traveling into sea ice. *Journal of Geophysical Research Oceans*, 107(C8), 20-1-20-
385 19. <https://doi.org/10.1029/2001JC000837>
- 386 Serreze, M. C., Holland, M. M., & Stroeve J. (2007). Perspectives on the arctic's shrinking sea-
387 ice cover. *Science*, 315(5818), 1533-1536. <https://doi.org/10.1126/science.1139426>

- 388 Squire, V. A., & Moore, S. C. (1980). Direct measurement of the attenuation of ocean waves by
389 pack ice. *Nature*, 283, 365–368. <https://doi.org/10.1038/283365a0>
- 390 Stopa, J. E., Arduin, F., Thomson, J., Smith, M.M., Kohout, A.L., Doble, M., & Wadhams, P.
391 (2018). Wave attenuation through an Arctic marginal ice zone on 12 October 2015: 1.
392 Measurement of wave spectra and ice features from Sentinel 1A. *Journal of Geophysical*
393 *Research: Oceans*, 123(5), 3619-3634. <https://doi.org/10.1029/2018JC013791>
- 394 The WAVEWATCH III Development Group (WW3DG). (2019). User manual and system
395 documentation of WAVEWATCH III version 6.07. Maryland, USA,
396 NOAA/NWS/NCEP/MMAB.
- 397 Thomson, J., & Rogers W. E. (2014). Swell and sea in the emerging Arctic Ocean. *Geophysical*
398 *Research Letter*, 41, 3136–3140. doi:10.1002/2014GL059983.
- 399 Tsarau, A., Shestov, A., & Løset, S. (2017). *Wave attenuation in the Barents Sea marginal ice*
400 *zone in the spring of 2016*. The 24th International Conference on Port and Ocean Engineering
401 under Arctic Conditions, Busan, South Korea
- 402 Vachon, P.W., Olsen, R., Krogstad, H.E., & Liu, A.K. (1993). Airborne synthetic aperture radar
403 observations and simulations for waves in ice. *Journal of Geophysical Research*, 98(C9),
404 16411-16425. <https://doi.org/10.1029/93JC00914>
- 405 Wadhams, P., Squire, V. A., Goodman, D. J., Cowan, A.M., & Moore, S.C. (1988). The
406 attenuation rates of ocean waves in the marginal ice zone. *Journal of Geophysical Research*,
407 93(C6), 6799-6818. <https://doi.org/10.1029/JC093iC06p06799>
- 408 World Meteorological Organization (WMO). (2010). SIGRID-3: A vector archive format for sea
409 ice charts. Intergovernmental Oceanographic Commission.
410 https://library.wmo.int/index.php?lvl=notice_display&id=11295#.Yh1CrSxlCqR
411