

1 **Dissolved oxygen modeling of an urban stream using grid partitioning and**
2 **subtractive clustering fuzzy techniques**

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8

9 **Abstract**

10 Dissolved oxygen is one of the prime parameters for assessing the water quality of any
11 stream and the health status of aquatic life. The dissolved oxygen present in the water body
12 plays an essential role in deciding water treatment processes to enhance water quality up to
13 the design standards for the specified water use. Thus, the accurate estimation of dissolved
14 oxygen concentration is necessary to evolve measures for maintaining the riverine ecosystem
15 and designing the appropriate water treatment plants. Machine learning techniques are
16 becoming useful tools for the prediction and simulation of water quality parameters. With
17 these viewpoints, a study was carried out in the Delhi stretch of Yamuna River, India, and
18 physiochemical parameters were examined for five years to simulate the dissolved oxygen
19 using different machine learning techniques. Simulation and prediction competencies of
20 ANFIS grid partitioning (ANFIS-GP) and ANFIS subtractive clustering (ANFIS-SC) were
21 tested on various water quality parameters. Variation in dissolved oxygen was examined on
22 various combinations of parameters. ANFIS-GP has been designed using the Gaussian
23 function, and ANFIS-SC works on the likelihood of cluster centers. Results obtained from the
24 models were evaluated using root mean square error (RMSE) and coefficient of
25 determination (R²) to identify the optimum solution and appropriate combination of
26 parameters that simulate the observed dissolved oxygen. Results of ANFIS-GP and ANFIS-
27 SC indicate that both the models produce suitable solutions for the prediction; however,
28 ANFIS-GP outperforms the ANFIS-SC and could act as a useful tool for defining, planning,
29 and management of water quality parameters.

30 **Keywords:** Grid partitioning, Subtractive clustering, Water quality, Dissolved oxygen

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32

33

34 1 INTRODUCTION

35 The production and consumption of dissolved oxygen (DO) in rivers are dynamic
36 (Zahraeifard and Deng, 2012). Dissolve oxygen remains in water as free oxygen, and its
37 concentration varies due to diffusion. The concentration of DO in water depends upon several
38 sources, sinks, and solubility rates. The atmosphere is the most significant external source of
39 oxygen to stream, and photosynthesis plays a significant role as an internal source of oxygen.
40 Photosynthesis contributes more oxygen to water, as the oxygen generated from the algae
41 contains pure oxygen, whereas the atmospheric diffusion contains only 20% oxygen in
42 overall gas transfer at the air-water interface. All the microorganisms, aquatic plants, and
43 aquatic animals consume the oxygen through respiration, known as sinks. All the sinks
44 consume oxygen throughout the day and night.

45 In contrast, photosynthesis generates oxygen during the daytime only, whereas the algae
46 act as both sources and the sink of oxygen (Arora and Keshari, 2020). There should be
47 synchronization in the source and sinks of oxygen to maintain a healthy riverine ecosystem.
48 Another factor is solubility that further depends upon the pressure, temperature, and salinity
49 of the water. The higher pressure increases the solubility of gas, whereas higher salinity and
50 temperature reduce the solubility rate. All these factors affect the DO concentration in the
51 river along with the depth of the water body. Mathematically, the concentration of DO can
52 be expressed as:

$$53 \quad DO = DO_{so}S - DO_{si}$$

54 Where, DO_{so} is the source of DO and DO_{si} is the sink of DO at S solubility. The low
55 concentration of dissolved oxygen in the river for a longer duration increases the inception of
56 several environmental problems (Kisi and Murat, 2012). The river system's Biota starts
57 getting affected if the oxygen content reduces below 30% to the saturation limit. Variation in
58 DO concentration occurs rapidly based on flow available in rivers, velocity, turbulence, the
59 number of organics, and atmospheric reactions involved in the riverine system (Cox, 2003).
60 Anthropogenic activities are becoming the significant sinks of oxygen that consume the
61 available DO through partially or untreated wastewater from the domestic, industrial,
62 commercial and agricultural sectors (Arora and Keshari, 2018). It is mandatory to maintain
63 the equilibrium between the sources and sinks for the aquatic ecosystem's sustainability.

64 River systems are greatly affected by water abstraction for the municipal supplies and
65 urban wastewater discharge through drains/tributaries during the low flow period. Estimating
66 DO concentration variation for the heavily polluted rivers based on the statistical methods is

67 not the appropriate approach nowadays due to the complex and nonlinear water quality
68 parameters (Cox, 2003; Parmar and Keshari, 2012). Various researchers have profoundly
69 used machine learning techniques to predict the variation in various water quality parameters.
70 For the simulation and forecasting of water quality parameters, artificial neural networks
71 (Singh et al., 2009; Heddam, 2016) and ANFIS (Chen and Liu, 2013; Ay and Kisi, 2016)
72 have been successfully utilized by several researchers. Cox (2003) illustrated various
73 mathematical models available for predicting DO concentration in a lowland river; however,
74 such models require a significant amount of data for the excellent prediction (Kannel et al.,
75 2011).

76

77 **1.1 Literature Review**

78 Fuzzy logic has several advantages in classification, data mining, interpretation, and
79 optimization of time series data of various fields (Nguyen et al., 2013; Wijayasekara and
80 Manic, 2014). The derivation of fuzzy models significantly depends on linguistic terms
81 designed via membership functions (MFs) and delivers input parameters to the optimization
82 model (Cordon, 2011). The fuzzy theory has been widely used to model the nonlinear
83 behavior for various hydrological applications (Altunkaynak et al., 2005; Keskin et al., 2006;
84 Chang et al., 2015; Khan and Valeo, 2015; Ay and Kisi, 2017; Arora and Keshari, 2020). The
85 fuzzy system can remove the uncertainties from the data and develop the model structure
86 through the rule-based system (Guyonnet et al., 2003; Huang et al., 2010). The identification,
87 validation, optimization, and interpretation can be applied before decision making using
88 fuzzy to manage water resources. Altunkaynak et al. (2005) used the Takagi–Sugeno fuzzy
89 logic approach to model fluctuations in DO at Golder Horn and compared the results with
90 ARMA models. The results reveal that the fuzzy models are more superior to ARMA in the
91 prediction of DO fluctuations. Guldal and Tongal (2010) identified the variation in the depth
92 of water in the lake and compared the accuracy of RNN, ANFIS, and stochastic models using
93 the coefficient of determination. Authors found that RNN and ANFIS perform exceptionally
94 over stochastic models. Moosavi et al. (2013) compared different data-driven models to
95 predict the reservoir's groundwater level at two distinct basins. The author used ANN, ANFIS
96 and ANN-ANFIS coupled models and found that the ANFIS and various combinations of
97 ANFIS perform better over the ANN due to the errors involved in selecting the adequate
98 number of neurons for the ANN model. ANFIS is also advantageous over ANN with the
99 capability of former of analyzing uncertainties in input parameters. Parmar and Bhardwaj
100 (2014) compared the regression, ANN, Wavelet, and ANFIS, to predict the COD in India's

101 Yamuna River. They also compared the conventional techniques with the wavelet coupled
102 model. Khan and Valeo (2015) applied fuzzy regression and compared it with the Tanaka and
103 Diamond method of fuzzy modeling to predict the DO and found that the ability to record
104 water quality parameters' uncertainty makes the fuzzy regression technique a substantial
105 approach for the prediction of DO. The literature review reflects that the fuzzy modeling
106 techniques can be applied to a wide area with high accuracy. However, detailed studies over
107 the differences between the two approaches (subtractive clustering and grid partitioning) of
108 fuzzy modeling are not available. The application of a correct approach for the prediction of
109 the parameter can improve the results significantly.

110 As the DO acts as the health indicator of the riverine system, accurate prediction of DO
111 for assessing the state of the water body, designing policies for the water resource
112 management, and appropriate allocation of available water keeping the sufficient amount of
113 flow in rivers are the predominant task. In this study, the grid partitioning and subtractive
114 clustering approaches are analyzed to model the stream passing through a highly urbanized
115 area, discharging tremendous wastewater from domestic, industrial, and agricultural sources
116 through multiple drains.

117

118 **2 MATERIAL AND METHODOLOGY**

119 ANFIS models are developed for the simulation and prediction of DO. A hybrid
120 algorithm combining the least-squares method and the gradient descent method is used to
121 conserve the search space and minimize the model's operational time. The model's structure
122 is designed using subtractive clustering and grid portioning methods, and various
123 combinations of input parameters are tested out using both methods.

124

125 **2.1 Adaptive Neuro-Fuzzy Inference System**

126 Adaptive neuro-fuzzy inference system (ANFIS) is the combined structure of the neural
127 network and fuzzy logic. This composite structure allows neurons to record the input data and
128 fuzzy rules to optimize the solution. The fuzzy sets in the model define the fuzzy rule base
129 and make the ANFIS capable of simulating the nonlinear behavior of input parameters. The
130 rule base of the network increases with the number of input parameters. However, it also
131 increases the computational time of the model (Chang and Chang 2006). The ANFIS
132 structure is designed using five different layers that include input, fuzzification,
133 normalization, defuzzification, and output layers. The number of input parameters is defined

134 in the first layer. Fuzzification includes the distribution of membership function to each input
 135 parameter and allocation of type of membership function.

136 If-then rules bases are formed based on the number and type of membership functions
 137 defined in the previous step. The fuzzification covers the input into breakable fuzzy sets, and
 138 defuzzification again converts the fuzzy sets into output after applying inference processes,
 139 normalization, and optimization (Chang and Chang, 2006). However, the FIS rule base can
 140 be altered by understanding the relationship between input parameters and reducing the
 141 computational time with optimized output. The alteration of the rule base and the modified
 142 structure of FIS make it worthwhile for wide application over neural networks (Arora and
 143 Keshari, 2020). FIS is designed using Gaussian type membership functions with a hybrid
 144 learning algorithm to optimize the model. The structure of FIS dominantly depends upon the
 145 type and number membership function selected for modeling. (Babuska and Verbruggen
 146 2003; Sonmez et al. 2017). The overall architecture of the FIS model is shown in figure 1.

147
 148 [Insert Figure 1]

149
 150 **2.2 Grid Partitioning**

151 Grid partitioning is commonly used to design the FIS, which is a fuzzy portioning
 152 method. The minimum distance between two variables is required for each input parameter.
 153 The problem region is divided into sub-regions, and input space is further divided into sub-
 154 regions to refine the space depending upon the type and number of membership functions
 155 selected for designing the model. The rule base of grid partitioned FIS is defined as:

156
$$x_1 = A_1^{k_1}, x_2 = A_2^{k_2}, \dots, x_n = A_m^{k_n}$$

157
 158
$$y_m = y^{k_1, k_2, \dots, k_n}, k_i = 0, 1$$

159
 160 If, $k_i=0$, then $A_m^{k_n} = a_i$, where a_i is the minimal value of the input parameter. If, $k_i=1$, then
 161 $A_m^{k_n} = b_i$, where b_i is the maximal value of the input parameter, and both the values would be
 162 computed using the least square method. The input sub-region is divided into m^{th} sub-regions,
 163 where $x = x_1, x_2, x_3, \dots, x_m$. The membership function for the fuzzy term $A_m^{k_i}$ would be:

164
$$\mu_m^0(x_i) = \frac{b_m - x_i}{b_m - a_m}$$

165 For $k_i=0$

166

$$\mu_m^1(x_i) = \frac{x_i - a_m}{b_m - a_m}$$

167

For $k_i=1$ 168 The output corresponding to m^{th} sub-region is written as:

$$169 \quad O = \sum_{k_1, k_2, \dots, k_n} A_m^{k_1, k_2, \dots, k_n}(x_i) * y_m^{k_1, k_2, \dots, k_n}$$

170

171 The sub-regions are divided on the maximum value of error from the training
 172 samples. Once the maximum errors of every sub-region are achieved, the region splits into
 173 two regions, and the new approximation error is the minimum of the new sub-region. The
 174 sub-region splitting continues until the two regions' errors become constant, as shown in
 175 Figure 2. The maximum error obtained from the sub-region at which split occur is written as:

$$176 \quad E_m = \frac{1}{N_m} \sum_{x_m} \left[\frac{1}{2} (x_j - t_j)^2 \right]$$

177 Where, E_m is the error obtained from m^{th} sub-region from the N_m training samples and x_j and
 178 t_j are the output generated from the model and targeted respectively from j^{th} training samples.

179

180 2.3 Subtractive Clustering

181 The partitioning method is preferred when the knowledge about the center's distribution
 182 is not adequate (Benmouiza and Cheknane, 2018). In subtractive clustering, the rule base
 183 formed is equivalent to the membership function formed. In this method, each data point is
 184 considered the center, and the importance of each center is identified through the data point in
 185 the center's neighborhood. The process runs through several iterations and allocates the center
 186 by identifying the most influential center with the highest number of data points in its
 187 surrounding. The radius of the cluster of points is identified using the center of neighboring
 188 points. The process repeats until all the data points fall within the radius of every cluster. The
 189 potential of the data point is written as:

$$190 \quad P_i = \sum_{j=1}^n \exp\left(\frac{-\|x_i - x_j\|^2}{0.5 r^2}\right)$$

191 P_i is the potential index of x_i data points, r is the radius where all the neighborhood's data
 192 points fall. The second iteration is calculated as:

$$193 \quad \dot{P}_i = P_i - P_{c1} \exp\left(\frac{-\|x_i - x_{c1}\|^2}{0.5 r_a^2}\right)$$

194 Where, P_{c1} represents the potential of cluster 1 and r_a is the K_r , where K_r is the positive integer
195 usually 1.5. The process is repeated, and a radius of cluster is recalculated until a sufficient
196 number of cluster centers are not generated.

197 [Insert Figure 2]

198

199 **2.4 Model Development**

200 The sampling data is divided into two parts of 70:30 to design the model, where 70
201 percent of sampling data points are used for model training, and 30 percent are used for
202 testing the model. Different sets of parameters are selected for designing the model. The four
203 models are designed using temperature, BOD, COD, conductivity, and ammonia. To estimate
204 the DO of any stream, the concentration of organic matter present in water plays a significant
205 role as for the decomposition of organic content, DO acts as a source of energy for aerobic
206 bacteria. The type of bacteria that would develop depends upon the temperature of the stream.
207 Hence, the first model (M1) is developed with the temperature, BOD, and COD as input
208 parameters. The addition parameter selected in the second model (M2) is conductivity. The
209 amount of DO also varies with dissolved solids due to the oxygen demand of solids. The
210 presence of ammonia reflects the generation of algae in the water, which acts as both the
211 source and sink of oxygen. The third model (M3) is designed by combining the base
212 parameters with ammonia. Moreover, the fourth model (M4) is designed to look at the
213 combined effect of conductivity and ammonia and the base parameters on the river's
214 dissolved oxygen.

215 Both the fuzzy partitioning methods are used to design the model with similar
216 parameters. The input parameters selected to design the FIS models, as shown in Table 1, are
217 used for both the grid partitioning and subtractive clustering method.

218

219 [Insert Table 1]

220

221 The coefficient of determination (R^2) and root mean square error (RMSE) are
222 evaluated and compared with the observed dissolved oxygen to analyze models' performance.
223 The lowest RMSE nears to zero value indicates the adequate model and when R^2 nears to 1
224 represents a better correlation between the observed and the predicted values obtained from
225 the FIS model. Formulas used to identify the performance of models are as follows:

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (p_i - o_i)^2}{n}}$$

$$R^2 = 1 - \frac{\sum_{i=1}^n (p_i - o_i)^2}{\sum_{i=1}^n (p_i - \bar{o}_i)^2}$$

228

229 3 STUDY AREA

230 Delhi is one of India's biggest and dense cities, and all the wastewater generated from
 231 various sectors (domestic, commercial, industrial, and agricultural) of Delhi joins the
 232 Yamuna River. Some part of the wastewater before its confluence with the river passes
 233 through the treatment processes. However, the percentage of wastewater that gets treatment is
 234 too less than the wastewater directly discharged into the drain through irregular means,
 235 ultimately joining the river. The samples were collected from Nizamuddin, Delhi, 16 km
 236 downstream of the Wazirabad barrage in Delhi. Yamuna river travels around 375 km before
 237 reaching Delhi, and the flow of the river gets obstructed at the Wazirabad Barrage for water
 238 supply to Delhi. The fresh water remains low in the river throughout the year, and only
 239 wastewater from Delhi flows in the river except during the monsoon period. In between the
 240 Wazirabad barrage and the Nizamuddin, Yamuna River receives effluents from several
 241 drains, out of which maximum effluents are discharged from the Najafgarh drain, which
 242 contains the flows 2.5 times to the water available in the river. As the Najafgarh drain joins
 243 the river just after the Wazirabad barrage (0.5 km downstream), it causes maximum damage
 244 to the river's water quality (CPCB, 2006).

245 The stretch of river Yamuna in Delhi is one of the most polluted sections of the river,
 246 having a total length of 1376 km. The water quality falls in category E, which indicates that
 247 the river's water is not designated for any use. The BOD load increases in the river up to 80
 248 tons/day after the Najafgarh drain's confluence. The sampling location also receives the
 249 effluents from a thermal power plant located at the river's right bank. The river observes one
 250 road bridge, one railway bridge, and one metro railway bridge that further obstructs the flow
 251 and causes silting near the bridges' piers. The dissolved oxygen content of the river falls to
 252 zero in this stretch and causes the significant degradation of aquatic plants and animals. The
 253 generation of anaerobic conditions has also been observed in the river due to the
 254 decomposition of organic matter in the absence of oxygen.

255 The sampling location is selected after considering the distance from the Wazirabad
256 barrage, upstream of which water quality is much clear, time taken by the flow to provide
257 sufficient mixing of wastewater with the river water to collect the homogeneous sample. The
258 river receives the effluent load from the right bank only and has heavy habitation close to the
259 right bank, as shown in Figure 3. On the left bank, the river has a flood plain to cater to the
260 excess water during the flood; however, the encroachment of the flood plain is another
261 problem of Yamuna River that causes the frequent release of flow during the monsoon period
262 and the rest of the time river flow with low discharge.

263

264 [Insert Figure 3]

265

266 The water samples were collected for five years every month, and physiochemical
267 analyses have been carried out as per the standard procedure (APHA, 2005) after preserving
268 the samples with the recommended reagent. During summers, the average temperature
269 remains around 32°C, affecting the saturation rate of dissolved oxygen in the river. Delhi
270 receives the precipitation in the form of rainfall from July to September, and sufficient water
271 flows in the river during this period, BOD level falls below 50 mg/l, and DO rises to 2 mg/l.
272 However, these conditions still indicate the riverine ecosystem's terrible health, but somewhat
273 better than the river's non-monsoon state.

274

275 **4 RESULTS AND DISCUSSION**

276 An appropriate combination of parameters is selected for the development of ANFIS
277 models after several trial and error. Takagi-Sugeno (TS) algorithm is used for the
278 development of the model. Three MFs are selected for each input parameter with Gaussian
279 function type membership function, and constant type MF is selected for the output
280 generation. To generate the FIS, both the methods, grid partitioning and subtractive clustering,
281 are used and compared. The structures of the models are shown in Table 2. In all the models
282 developed using grid partitioning, three membership functions are used for each input,
283 whereas the number of membership functions varies with the number of input parameters in
284 each model in the case of subtractive clustering. In M1, there are three input parameters, and
285 five membership functions are used; however, in M2 and M3, have four input parameters in
286 each model. Therefore six membership functions are used in both models. However, M4
287 contains five input parameters, and nine membership functions are used to design the model.

288 Along with the increase in input parameters, the rule base also elevates exponentially in
289 Grid partitioning whereas, and this does not hold the truth in the case of subtractive
290 clustering. The optimization is carried out for both the partitioning method using hybrid
291 learning for all the models. The varying numbers of epochs for each model are used until the
292 observed error gets constant or reduced to the minimum.

293

294 [Insert Table 2]

295

296 The performance of the models is identified using RMSE and R^2 . Results of ANFIS-
297 GP and ANFIS-SC indicate that both the models produce suitable solutions for the prediction.
298 The M1 of both the ANFIS-GP and ANFIS-SC produces considerable but high RMSE
299 compared to other models. It indicates that the input parameters used for modeling are
300 insufficient to explain the phenomenon of dissolved oxygen variation in the river. However,
301 R^2 of more than 0.75 indicates that input parameters are substantial factors that affect the
302 variability in dissolved oxygen concentration. The performance of M2 increases considerably
303 over M1, where M2 includes conductivity as an extra parameter other than temperature,
304 BOD, and COD as considered in M1. The M3 model contains ammonia as an extra
305 parameter, including parameters considered in M1; however, the RMSE in M3 increases
306 compared to M2 for the grid partitioning method. Comparing M2 and M3 of ANFIS-GP
307 indicates that conductivity is more significant than ammonia to predict dissolved oxygen.
308 Simultaneously, the combination of both the conductivity and ammonia and other parameters
309 is considered in M4 and produces magnificent results over other methods. The RMSE of M4
310 is found only 0.049, and R^2 is 0.953 for ANFIS-GP. The correlation between the observed
311 and predicted dissolved oxygen from all the ANFIS models obtained using both the
312 partitioning methods are shown in Figure 4.

313

314 [Insert Figure 4]

315

316 The performance of ANFIS-SC shows similar results for models. The highest RMSE
317 is found in M1 and lowest in M4 as similar to ANFIS-GP. The M2 and M3 deliver
318 approximately similar results as both the models contain a similar number of input
319 parameters and membership functions, which indicates that the output of ANFIS-SC
320 essentially depends upon the number of membership functions rather than the characteristics
321 of input parameters. The M4 produces the RMSE of 0.150, which is the lowest among all the

322 ANFIS-SC models, however higher than the M4 of ANFIS-GP. The ANFIS-GP classifies the
323 model based on the rule base developed for each model, and that is the necessary condition
324 that results in better performance. Therefore, from the results, it is evident that the ANFIS-GP
325 outperforms the ANFIS-SC and could act as an effective tool for defining, planning, and
326 managing water quality parameters.

327

328 [Insert Table 3]

329

330 **5 Conclusion**

331 The study was carried out for the simulation of dissolved oxygen using ANFIS. The
332 models are developed using two proportioning methods, grid partitioning and subtractive
333 clustering, and obtained results were compared to simulate the dissolved oxygen in a river.
334 Various combinations of input parameters are used to develop the models using both the
335 ANFIS method (ANFIS-GP and ANFIS-SC), and the applicability of ANFIS models are
336 tested using water quality parameters of the Yamuna River. The M4 model of ANFIS-GP is
337 found with the lowest RMSE and the maximum R^2 of 0.953. However, all the models of the
338 ANFIS-GP worked well over the ANFIS-SC and have shown a good correlation with the
339 observed values of the dissolved oxygen. The extensive formulation of the rule base helps
340 identify vital parameters and improves the accuracy of the model. However, it is expected
341 that the accuracy of the model can be further improved with the large data set.

342

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Table 1: Development of ANFIS models

Model	Parameters	Output
M1	Temp., BOD, COD	DO
M2	Temp., BOD, COD, Cond.	DO
M3	Temp., BOD, COD, Ammonia	DO
M4	Temp., BOD, COD, Cond., Ammonia	DO

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Table2: ANFIS model structure

	Grid Partitioning	Subtractive Clustering
No. of MF	3 for each input in each model	5 for M1 6 for M2 and M3 9 for M4
Type of MF	Gaussian	Gaussian
Optimization model	Hybrid learning	Hybrid learning
Fuzzy rules	M1 – 27 M2 – 81 M3 – 81 M4 – 243	M1 – 5 M2 – 6 M3 – 6 M4 – 9

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Table 3: Performance of developed models

	Grid Partitioning		Subtractive Clustering	
	RMSE	R ²	RMSE	R ²
M1	0.642	0.758	0.458	0.824
M2	0.181	0.908	0.287	0.872
M3	0.308	0.861	0.284	0.871
M4	0.049	0.953	0.150	0.911

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