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# 1 Dynamics adsorption of the enhanced CH<sub>4</sub> recovery by CO<sub>2</sub> injection

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## 13 ABSTRACT

14 The dynamic adsorption isotherms of CO<sub>2</sub>-EGR were measured by using a  
15 Intelligent Gravimetric Analysis system. In the beginning stage of CO<sub>2</sub> injection, all  
16 the injected CO<sub>2</sub> enters into the adsorbent and the mole fraction of CH<sub>4</sub> ( $y_{CH_4}$ ) keeps  
17 1.0. The CH<sub>4</sub> recovery factor ( $R_{CH_4}$ ) increases. The during of this stage ( $t_{cd}$ ) depends on  
18 the selectivity of CO<sub>2</sub> over CH<sub>4</sub> ( $S_{CO_2/CH_4}$ ). A adsorbent with large  $S_{CO_2/CH_4}$  has long  $t_{CD}$ .  
19 When  $S_{CO_2/CH_4}$  is greater than 1.0, CO<sub>2</sub> reduces the fraction of CH<sub>4</sub> in the adsorbed  
20 phase ( $x_{CH_4}$ ) and more CH<sub>4</sub> is driven out. In the second stage, the injected CO<sub>2</sub>

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1 competes with CH<sub>4</sub> for adsorption. The cumulative  $R_{CH_4}$  of this stage is much larger  
2 than that of the initial stage. However,  $y_{CH_4}$  decrease sharply.  $p_{CH_4}$  in the whole CO<sub>2</sub>  
3 injection is always larger than that before CO<sub>2</sub> injection, suggesting CH<sub>4</sub> desorption  
4 results from the displacement by CO<sub>2</sub> rather than from pressure depletion.

5 **Keywords** : dynamic adsorption; CO<sub>2</sub>-EGR; CH<sub>4</sub> displacement; the CH<sub>4</sub> recovery  
6 factor ( $R_{CH_4}$ )

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## 8 **1 Introduction**

9 In the adsorption separation of mixed gas and energy extraction of conventional  
10 natural gas, CO<sub>2</sub> injection is being considered to improve the recovery of CH<sub>4</sub>. For  
11 example, CO<sub>2</sub> injection has been proposed to use as a displacement step of PSA  
12 (pressure swing adsorption) cycle in the separation of coal-bed gas extracted (CH<sub>4</sub>/N<sub>2</sub>  
13 mixture gas) using grain activated carbon (GAC) as adsorbent <sup>[1]</sup>. And CO<sub>2</sub> injection  
14 has also been proposed to enhance shale gas recovery (CO<sub>2</sub>-ESGR) <sup>[2,3]</sup> and coalbed  
15 methane recovery(CO<sub>2</sub>-ECBM) <sup>[4]</sup>. In fact, the adsorption principle of all these CO<sub>2</sub>-  
16 enhance gas recovery (CO<sub>2</sub>-EGR) processes is the same, that is, CO<sub>2</sub> can displace  
17 adsorbed CH<sub>4</sub> in the adsorbent/reservoir and drive out CH<sub>4</sub>. However, these processes  
18 have not been fully understood and have not been applied in the field except several  
19 test fields.

20 Because most CH<sub>4</sub> in the adsorbent/reservoir is adsorbed state, the effect of CO<sub>2</sub>-  
21 EGR depends largely on the competitive adsorption of CO<sub>2</sub> and CH<sub>4</sub>. Shale and coal  
22 are adsorbents because they are porous material. An adsorbent has selectivity for gas

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1 adsorption and the adsorption capacity of different gases on an adsorbent is different.

2 The adsorption selectivity mainly depends on the the properties of the adsorbent and

3 the adsorbed gas. The pore structure and surface properties of adsorbent and the

4 molecular size of adsorbed gas play an important role in the adsorption selectivity <sup>[5,6]</sup>.

5 The dynamics diameter of CO<sub>2</sub> molecular is 0.33nm, which is less than 0.38nm of

6 CH<sub>4</sub>, so it can enter the smaller pores that methane cannot enter. Therefore, the

7 adsorption capacity of CO<sub>2</sub> is always greater than that of CH<sub>4</sub> on most adsorbents

8 having micropores. The adsorption selectivity of CO<sub>2</sub> over CH<sub>4</sub> ( $S_{CO_2/CH_4}$ ) is often used

9 to evaluate the CO<sub>2</sub>/CH<sub>4</sub> competitive adsorption <sup>[7]</sup>. The  $S_{CO_2/CH_4}$  can be simply

10 expressed as the ratio of the adsorption capacity of CO<sub>2</sub> to CH<sub>4</sub>. In most cases,  $S_{CO_2/CH_4}$

11 is calculated by the parameters of the adsorption equation of gases<sup>[5]</sup>. Numerous work

12 were performed to get the adsorption isotherms of CO<sub>2</sub> and CH<sub>4</sub> on activated carbon

13 adsorbent <sup>[1,8]</sup>, some new adsorbent used for the separation CO<sub>2</sub> and CH<sub>4</sub><sup>[9]</sup>, coal<sup>[10]</sup> and

14 shale reservoirs <sup>[11,12]</sup> and establish adsorption isotherm equations.  $S_{CO_2/CH_4}$  is larger

15 than 1.0, indicating the feasibility of CO<sub>2</sub>-EGR.

16 The temperature and pressure studied for adsorption are mostly far away from

17 the supercritical point of CH<sub>4</sub> (pressure 4.59 MPa, temperature -82.6 °C). On the

18 contrary, they may close to the supercritical point of CO<sub>2</sub> (pressure 7.38 MPa,

19 temperature 31.26 °C). Therefore, CH<sub>4</sub> adsorption isotherm curves show a linear

20 increase followed by a plateau <sup>[1,3,5,8-12]</sup>, which can be described well by Langmuir

21 equation. Typical CO<sub>2</sub> adsorption isotherm consists of linear increase in gas

22 adsorption with pressure followed by a plateau or saturation region and finally

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1 decrease in a non-linear way on various rank coals, shale and activated carbon<sup>[1,3,8-12]</sup>.

2 The adsorption saturation of CO<sub>2</sub> appears near to its supercritical point. The shape of

3 adsorption isotherms of CO<sub>2</sub> vary greatly at different range of temperature and

4 pressure, which are described by different adsorption isotherm equations, such as

5 Langmuir equation, BET(Brunauer-Emmett-Teller) equation and Virial equation et.al.

6 However, all the adsorption works describe adsorption equilibrium of CH<sub>4</sub> and CO<sub>2</sub>

7 from thermodynamic view. Some study the kinetic adsorption to compared the

8 diffusion coefficient of CO<sub>2</sub> and CH<sub>4</sub><sup>[3,3-15]</sup>. However, these adsorption thermodynamic

9 and adsorption kinetic have not reflected the dynamic adsorption process of CO<sub>2</sub>

10 injection to adsorbent adsorbed CH<sub>4</sub>.

11 CO<sub>2</sub>-EGR is a dynamic process in which CH<sub>4</sub>/CO<sub>2</sub> competitive adsorption is

12 always changing with CO<sub>2</sub> injection. The core flooding test (fixed bed experiment) is

13 a directly experimental method to simulate the dynamic process <sup>[1-4,16]</sup>, whose results

14 are breakthrough curves of CO<sub>2</sub> and CH<sub>4</sub>. By fitting the breakthrough curves using

15 numerical models consist of the material balance equations, adsorption equations and

16 mass transfer equation, the CH<sub>4</sub> recovery factor ( $R_{CH_4}$ ), the cumulative CH<sub>4</sub> production

17 and CO<sub>2</sub> storage amount are obtained<sup>[1]</sup>. In addition, the transport properties of CO<sub>2</sub> in

18 adsorbents can be obtained by using some hydrodynamic models<sup>[2,16]</sup>, permeability

19 and porosity evolution models<sup>[17]</sup>.

20 In this paper, we obtained the dynamic adsorption isotherms of the whole CO<sub>2</sub>-

21 EGR process by conducting an experiment. The dynamic adsorption mechanisms of

22 CO<sub>2</sub>-EGR were analyzed based on the dynamic adsorption isotherms. Moreover, the

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1 CH<sub>4</sub> recovery factor ( $R_{CH_4}$ ) of CO<sub>2</sub>-EGR were also obtained. The CO<sub>2</sub>-EGR process  
2 was simulated by injecting CO<sub>2</sub> into the adsorbents that pre-adsorbed CH<sub>4</sub> and were  
3 conducted on the intelligent Gravimetric Analysis system (IGA 100B) with scale of  
4 200 mg. Because the amount of adsorbent that can be filled in sample basket of the  
5 IGA 100 equipment is less than 200mg, the adsorbent chosen should have a large  
6 adsorption capacity for CH<sub>4</sub> and CO<sub>2</sub> to reduce the fitting error of the adsorption  
7 curve. The specific surface area of shale and coal is much smaller than that of  
8 activated carbon, therefore, activated carbon are used instead of shale or coal sample.

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## 10 **Experimental**

### 11 2.1 Materials

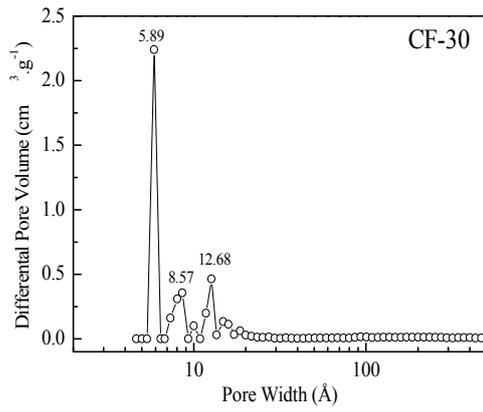
12 Activated carbons of CF-30 (prepared in our laboratory <sup>[5]</sup>) and RX3 (Norit  
13 Netherland B.V.) were used in the experiments. The BET (Brunauer-Emmett-Teller)  
14 surface area ( $S_{BET}$ ) and the pore size distribution (PSD) of CF-30 and RX3 were  
15 determined by ASAP2020 apparatus (Micromeritics, USA). The measured  $S_{BET}$  of CF-  
16 30 and RX3 are 426.49 m<sup>2</sup>/g and 1238.20 m<sup>2</sup>/g, respectively. The PSDs of the two  
17 GACs are shown in Fig. 1, which show that the pores of CF-30 are mainly contributed  
18 by micropores (pore size < 20 Å, 2nm). The RX3 has both micropores and many  
19 mesopores (20-500 Å, 2-5nm).

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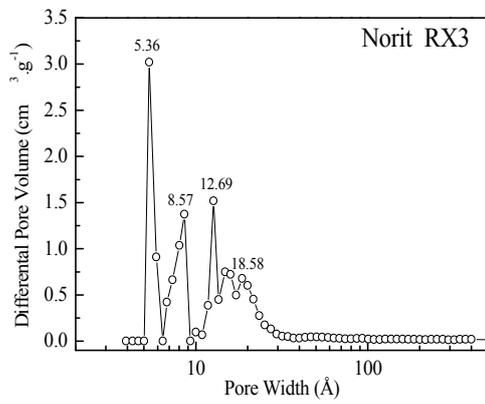
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3 **Fig.1.** The pore size distributions of CF-30 and RX3.

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5 The purities of CH<sub>4</sub> and CO<sub>2</sub> were 99.995% and 99.999%, respectively, as stated

6 by the supplier Tianke Co. China. The estimated uncertainty of the adsorption

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1 measurements due to gas purity was negligible.

## 2 2.2 Adsorption measurement

3 Intelligent Gravimetric Analysis (IGA) apparatus can determine accurately the  
4 increase of the weight of the adsorbent due to the adsorption of the gas. The IGA-  
5 100B used in this paper apparatus is manufactured by Hiden Isochema, Ltd. (UK)  
6 with a weight resolution of 0.2 mg.

7 The equilibrium adsorption isotherms of CH<sub>4</sub> and CO<sub>2</sub>, and the dynamic  
8 adsorption isotherms of CO<sub>2</sub>-EGR process were measured at 298K on IGA-100B  
9 apparatus.

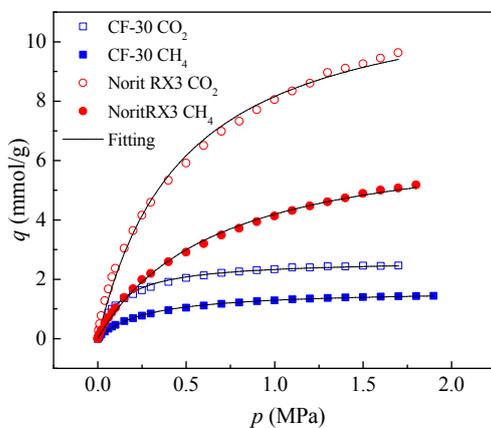
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## 11 13 Results and discussion

### 12 3.1 The selectivity of CO<sub>2</sub> over CH<sub>4</sub>

#### 13 3.1.1 Adsorption isotherms of CH<sub>4</sub> and CO<sub>2</sub>

14 The adsorption isotherms of CH<sub>4</sub> and CO<sub>2</sub> on GACs are shown in Fig.2. It is  
15 obviously that adsorption amount of CO<sub>2</sub> is larger than CH<sub>4</sub>, meaning that the  
16 preferential adsorption of CO<sub>2</sub> over CH<sub>4</sub>.



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1 **Fig.2.** Adsorption isotherms and Langmuir fitting curve of CH<sub>4</sub> and CO<sub>2</sub> on CF-30  
2 and RX3 GACs

3 The shape of each of these isotherms fall into Type I in the IUPAC classification  
4 <sup>[5]</sup>, single-gas Langmuir equation (Eq. 1) is used for the simulation of these isotherms.

$$q_i = \left( \frac{q_{mi} b_i p}{1 + b_i p} \right) \quad (1)$$

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6 where  $q_i$ (mol/g),  $q_{mi}$  (mol/g) and  $b_i$  are the adsorption amount, maximum adsorption  
7 capacity and adsorption equilibrium constant of pure gas  $i$ , respectively;  $p$  is the  
8 equilibrium pressure.

9 The fitting parameters of Eq.(1) for the adsorption isotherms of CH<sub>4</sub> and CO<sub>2</sub> are  
10 listed in Table 1. High values of correlation coefficient ( $R$ ) indicate that Eq.1 describes  
11 these isotherms well. However, there are still some errors between adsorbed amount  
12 measured and predicted by Eq.(1). The relative errors of adsorbed amount for CH<sub>4</sub> are  
13 less than 2% on both GACs at all pressures. It is noted that the CO<sub>2</sub> predictions at  
14 pressures lower than 0.15MPa show negative relative errors for RX3, but positive for  
15 CF-30.

16 **Table1** Langmuir equation fitting parameters for CH<sub>4</sub> and CO<sub>2</sub>

Adsorbent	CH <sub>4</sub>			CO <sub>2</sub>		
	$q_{mCH4}$	$b_{CH4}$	$R^2$	$q_{mCO2}$	$b_{CO2}$	$R^2$
	(mmol/g)	(MPa <sup>-1</sup> )		(mmol/g)	(MPa <sup>-1</sup> )	
CF-30	1.65	3.66	0.999	2.65	7.24	0.997
RX3	6.96	1.51	0.999	12.04	2.10	0.998

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1 A higher  $b$  indicates a higher affinity of the adsorbent for the adsorbate. The  $b$   
2 values of  $\text{CO}_2$  ( $b_{\text{CO}_2}$ ) are larger than those of  $\text{CH}_4$  ( $b_{\text{CH}_4}$ ) for both GAC samples,  
3 suggesting that the interaction forces of  $\text{CO}_2$ -GAC are larger than those of  $\text{CH}_4$ -GAC.  
4 Moreover, CF-30 has much stronger affinity for  $\text{CO}_2$  than RX3.

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### 6 3.1.2 The adsorption selectivity of $\text{CO}_2$ over $\text{CH}_4$

7  $S_{\text{CO}_2/\text{CH}_4}$  can be calculated by Eq. (2) [3,5] for gases adsorption isotherms follow the  
8 adsorption isotherm of Langmuir equation ,

$$9 \quad S_{\text{CO}_2/\text{CH}_4} = \frac{x_{\text{CO}_2} / y_{\text{CO}_2}}{x_{\text{CH}_4} / y_{\text{CH}_4}} = \frac{q_{m\text{CO}_2} \cdot b_{\text{CO}_2}}{q_{m\text{CH}_4} \cdot b_{\text{CH}_4}} \quad (2)$$

10 where  $x_{\text{CH}_4}$  and  $x_{\text{CO}_2}$  are the mole fractions of component  $\text{CH}_4$  and  $\text{CO}_2$  in adsorbed-  
11 phase, respectively;  $y_{\text{CH}_4}$  and  $y_{\text{CO}_2}$  are the mole fractions of  $\text{CH}_4$  and  $\text{CO}_2$  in the gas-  
12 phase respectively. The  $b$  and  $q_m$  of  $\text{CH}_4$  and  $\text{CO}_2$  are listed in Table1.

13  $S_{\text{CO}_2/\text{CH}_4}$  of CF-30 is 3.19 and of RX3 is 2.41.  $S_{\text{CO}_2/\text{CH}_4}$  greater than unity implies that  
14  $\text{CO}_2$  is a greater affinity of  $\text{CO}_2$  over  $\text{CH}_4$ , and the process of enhanced  $\text{CH}_4$  by  $\text{CO}_2$   
15 can be feasible from the thermodynamic point of view. The pores of carbonaceous  
16 materials are usually slit-shape. The minimum widths of the slit like pores for  $\text{CO}_2$   
17 and  $\text{CH}_4$  molecules entering are 0.578 nm and 0.62 nm, respectively<sup>[18]</sup>. That is one  
18 reason why  $S_{\text{CO}_2/\text{CH}_4}$  is always greater than unity for most adsorbents having  
19 micropores. Moreover, the adsorption energy ratios of  $\text{CO}_2/\text{CH}_4$  in the slit-shape pores  
20 size range from 0.62 to 1.6 nm decreases from 2.1 to 1.06<sup>[18]</sup>. Therefore, only smaller  
21 size micropores have larger selectivity for small molecules of  $\text{CO}_2$  and  $\text{CH}_4$ <sup>[5,9,18]</sup>. In

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1 the pores larger than 1.6 nm, the competitive adsorption between CO<sub>2</sub> and CH<sub>4</sub> is  
2 weak. Because RX3 activated carbon has much more pores larger than 1.6nm, the  
3 percentage of the pores whose size less than 1.6nm in CF-30 is larger than in RX3, the  
4  $S_{CO_2/CH_4}$  of CF-30 is larger than that of RX3.

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### 6 **3.1.3 The distribution of CO<sub>2</sub> and CH<sub>4</sub> in the adsorbed and gas phase at** 7 **equilibrium state**

8 At an equilibrium state, the mole fraction of CH<sub>4</sub> in adsorbed phase ( $x_{CH_4}$ ) is  
9 related to that in gas phase ( $y_{CH_4}$ ) by  $S_{CO_2/CH_4}$ , which is <sup>[19]</sup>

$$10 \quad \frac{1}{x_{CH_4}} = \frac{S_{CO_2/CH_4}}{y_{CH_4}} + (1 - S_{CO_2/CH_4}) \quad \frac{1}{x_{CH_4}} = \frac{S_{CO_2/CH_4}}{y_{CH_4}} + (1 - S_{CO_2/CH_4}) \quad (3)$$

11 Combined with Eq.(4) and Eq.(5), the correlations of  $x_{CH_4}$ - $y_{CH_4}$  and  $x_{CO_2}$ - $y_{CO_2}$  are  
12 decided and are shown in Fig.4.

$$13 \quad y_{CH_4} + y_{CO_2} = 1 \quad (4)$$

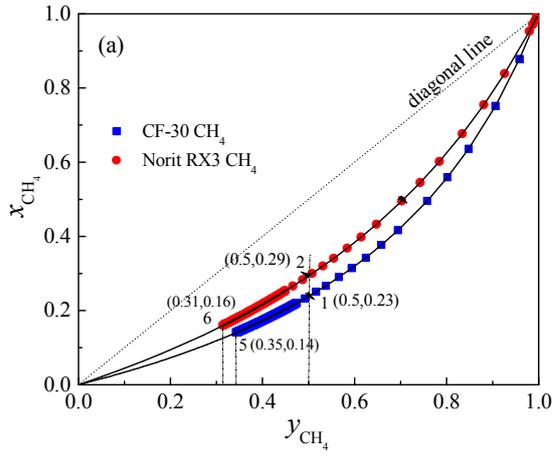
$$14 \quad x_{CH_4} + x_{CO_2} = 1 \quad (5)$$

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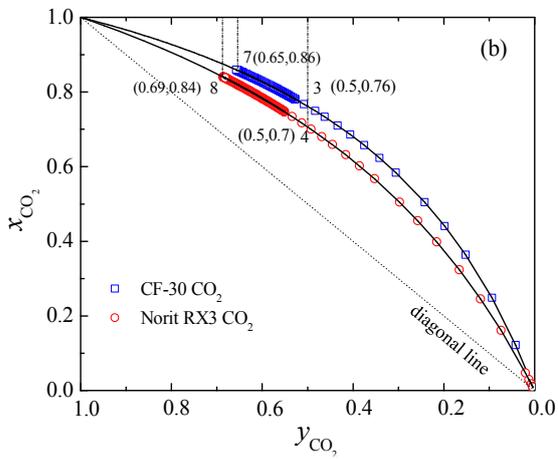
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3 **Fig. 3.** The relationships  $x_{CH_4}$ - $y_{CH_4}$  (a) and  $x_{CO_2}$ - $y_{CO_2}$  for CF-30 and RX3(b).

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5 If there is no adsorption competition between two gas components  $i$  and  $j$ , the

6 adsorption selectivity of  $CO_2$  over  $CH_4$  ( $S_{i/j}$ ) is 1.0. Hence, the correlations of  $x,y$  are

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1 straight diagonal line, as shown as dot lines in Fig 3. On the contrary, any deviation  
2 from the diagonal  $x,y$  line means the occurrence of adsorption competition. For  $\text{CH}_4$   
3 adsorption shown in Fig.3a,  $x_{\text{CH}_4}$ - $y_{\text{CH}_4}$  curves locate below the diagonal line, indicating  
4 that the  $\text{CO}_2$  hinders  $\text{CH}_4$  adsorption and reduces fractions of  $\text{CH}_4$  in adsorbed-phase  
5 ( $x_{\text{CH}_4}$ ). This is why  $\text{CH}_4$  displacement by  $\text{CO}_2$  is possible for  $S_{\text{CO}_2/\text{CH}_4} > 1$ . For example,  
6 at the same  $y_{\text{CH}_4}$  values of 0.5,  $x_{\text{CH}_4}$  for CF-30 and RX3 is 0.23 (point 1) and 0.29  
7 (point 2), respectively. Moreover,  $x_{\text{CH}_4}$  decreases much with a large  $S_{\text{CO}_2/\text{CH}_4}$ . On the  
8 contrary,  $x_{\text{CO}_2}$ - $y_{\text{CO}_2}$  of  $\text{CO}_2$  adsorption curves in Fig.3b locate above diagonal line.  $x_{\text{CO}_2}$   
9 increases much with a large  $S_{\text{CO}_2/\text{CH}_4}$ . For example,  $x_{\text{CO}_2}$  is 0.76 for CF-30 and is 0.7 for  
10 RX3 when  $y_{\text{CO}_2}$  is 0.5, as shown by point 3 and point 4 in Fig.3b. It is concluded that  
11 more relative  $\text{CH}_4$  molecules are driven out and the mole fraction of  $\text{CO}_2$  is higher in  
12 the adsorbent with high  $S_{\text{CO}_2/\text{CH}_4}$ .

### 13 **3.2 The adsorption dynamic of $\text{CO}_2$ -EGR**

#### 14 **3.2.1 The adsorption dynamic isotherms of $\text{CO}_2$ -EGR**

15 The dynamic adsorption isotherms ( $q_t$ - $t$ ) and their corresponding pressure  
16 histories are shown in Fig.4. AC stage of the  $q_t$ - $t$  curve corresponds to the adsorption  
17 of  $\text{CH}_4$ . In the AB stage, the pressure increased from 0.0 MPa to 0.1 MPa, and the  
18 adsorption amount of  $\text{CH}_4$  increased from 0.0 mg/g to 6.1mg/g. Then in the BC stage,  
19 the pressure is kept at 0.1 MPa for about 20min to reach the equilibrium state of  $\text{CH}_4$   
20 adsorption. The CF phase corresponds to  $\text{CO}_2$  injection process after  $\text{CH}_4$  pre-  
21 adsorption. The pressure is increased from 0.1 MPa to 0.3 MPa (CE phase) and  
22 maintained at 0.3 MPa for about 46min to reach an adsorption equilibrium (EF phase).

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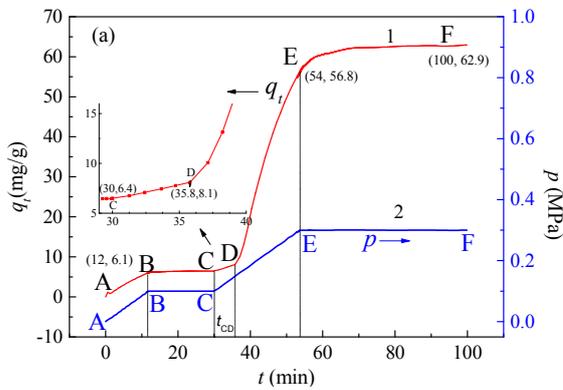
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1 The adsorption amount ( $q_t$ ) is the total adsorption amount of  $\text{CH}_4$  and  $\text{CO}_2$ , which  
2 reflects the adsorption competitive change  $\text{CO}_2\text{-CH}_4$  with  $\text{CO}_2$  injection. In the CE  
3 phase,  $p$ - $t$  is a line, while  $q$ - $t$  is not a line.

4 The  $q$ - $t$  curves obtained by using shale sample is exactly the same as that shown  
5 in Figure 4. We chose the results of GAC adsorbent to analyse the dynamic  
6 adsorption process, because the GAC has a much larger adsorption amount than shale,  
7 and hence the error in the numerical simulation is smaller.

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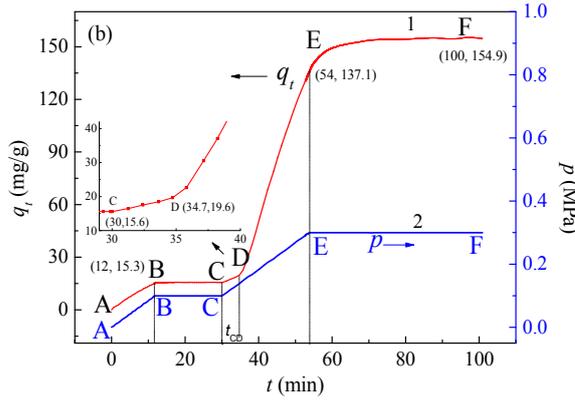


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2 **Fig. 4.** Adsorption dynamic isotherms and pressure history of the CO<sub>2</sub>-EGR in  
3 different adsorbents (a) CF-30; (b) RX3

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5 The slope of CD segment is much smaller than that of DE segment, which  
6 indicates that the adsorption capacity in CD phase increases little, but the adsorption  
7 capacity increases sharply in DE process. Moreover, the time for CD stage ( $t_{CD}$ ) is  
8 much shorter than the time for DE stage ( $t_{DE}$ ). As shown in Fig.4, the  $t_{CD}$  is 5.8min and  
9 4.7min;  $t_{DE}$  is 18min and 19.3 min for CF-30and RX3, respectively.

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### 11 3.2.2 The mole fractions of CH<sub>4</sub> and CO<sub>2</sub> in the gas phase of CO<sub>2</sub>-EGR

12 The co-adsorption isotherms of CO<sub>2</sub>/CH<sub>4</sub> binary mixtures on both of the GACs can  
13 be well fitted by multi-component Langmuir equations, Eq.6 and Eq.7, <sup>[5]</sup>

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$$q_{CH_4} = \frac{q_{mCH_4} b_{CH_4} p y_{CH_4}}{1 + b_{CH_4} p y_{CH_4} + b_{CO_2} p (1 - y_{CH_4})} \quad (6)$$

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$$q_{CO_2} = \frac{q_{mCO_2} b_{CO_2} p (1 - y_{CH_4})}{1 + b_{CH_4} p y_{CH_4} + b_{CO_2} p (1 - y_{CH_4})} \quad (7)$$

16 where  $p$  is total pressure,  $q_{CH_4}$  and  $q_{CO_2}$  (mol/g) are the adsorption amounts of

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1 components CH<sub>4</sub> and CO<sub>2</sub> from a binary gas mixture, respectively.  $q_{mCH_4}$ ,  $b_{CH_4}$ ,  $q_{mCO_2}$   
2 and  $b_{CO_2}$  are the Langmuir parameters of pure CH<sub>4</sub> or CO<sub>2</sub> listed in Table 1.  $y_{CH_4}$  and  
3  $y_{CO_2}$  are CH<sub>4</sub> and CO<sub>2</sub> in the gas-phase respectively.

4 In the process of CO<sub>2</sub> injection, the adsorption amount  $q_t$  is the total adsorbed  
5 amount of CH<sub>4</sub> and CO<sub>2</sub>.  $q_t$  is expressed by weight (mg / g) as Eq. (8).

$$6 \quad q_t = q_{CH_4} M_{CH_4} + q_{CO_2} M_{CO_2} \quad (8)$$

7 where  $q_{CO_2}$  (mmol/g) and  $M_{CO_2}$  (44g/mol) are the adsorbed amount and molecular  
8 weight of CO<sub>2</sub>, respectively;  $q_{CH_4}$  (mmol/g) and  $M_{CH_4}$  (16g/mol) are the adsorbed  
9 amount and molecular weight of CH<sub>4</sub>, respectively.

10 The mole fraction of CH<sub>4</sub> ( $y_{CH_4}$ ) at different pressure is calculated by Eq. which  
11 is derived from Eq.6 combined with Eq. 8. Combined with  $p-t$  curve, the curve of CH<sub>4</sub>  
12 concentration in the gas phase with time ( $y_{CH_4}-t$ ) during CO<sub>2</sub> injection is obtained, as  
13 shown in Fig. 5a.  $y_{CO_2}$  is calculated by Eq. (4), and  $y_{CO_2}-t$  is shown in Fig. 5b.

$$14 \quad y_{CH_4} = \frac{q_{mCO_2} b_{CO_2} p M_{CO_2} - b_{CO_2} q_t p - q_t}{p(b_{CH_4} q_t - b_{CO_2} q_t - M_{CH_4} b_{CH_4} q_{mCH_4} + M_{CO_2} b_{CO_2} q_{mCO_2})} \quad (9)$$

15 It is obviously that there are two stages (CD and DE) before  $y_{CH_4}$  and  $y_{CO_2}$  reaches  
16 a constant value. In the initial stage (CD stage) of CO<sub>2</sub> injection process,  $y_{CH_4}$  keeps a  
17 constant about 1.0. In CD stage,  $y_{CH_4}$  should be 1.0 theoretically. There is a little  
18 deviation between the calculated  $y_{CH_4}$  and 1.0, which is due to the error in the  
19 prediction of CO<sub>2</sub> and CH<sub>4</sub> adsorption capacity in Eq. (1), which has been discussed in  
20 3.1.1.

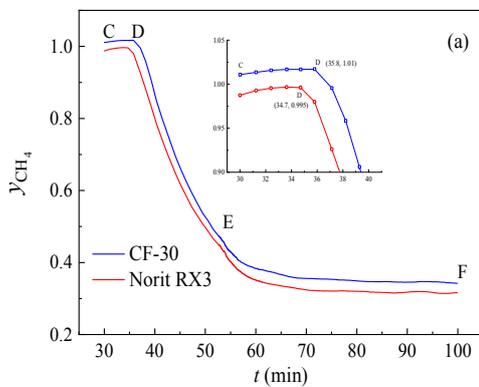
21  $y_{CH_4}-t$  curves reflect the time evolution of the the effluent composition, as the

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1 same as breakthrough curves obtained by core flooding tests. The patterns of  $y_{CH_4}-t$   
 2 shown in Fig.5a are in agreement with all the  $CH_4$  breakthrough curves obtained in  
 3 the  $CO_2$  injection process for enhancing gas shale<sup>[2,16,17]</sup>, coal bed gas<sup>[4]</sup> and for  
 4 enriching  $CH_4$  in separation for  $CH_4/N_2$ <sup>[1]</sup> by PSA experiments. In all the breakthrough  
 5 curves,  $y_{CH_4}$  remained at 1.0 at the beginning of  $CO_2$  injection.  $CO_2$  breakthrough at  $D$ ,  
 6 and the second DE stage begins.  $y_{CH_4}$  decreases dramatically in this stage. It is should  
 7 be noted that in the whole  $CO_2$  injection process, the duration of the initial stage  $t_{cd}$  is  
 8 very short. The early breakthrough of  $CO_2$  was also found in in  $CO_2$ -ESGR and  $CO_2$ -  
 9 ESGR ( $CO_2$ -ECBM) <sup>[1-3,16,17]</sup>, which was unfavorable for  $CH_4$  production. The  $CH_4$   
 10 product is contaminated by  $CO_2$  after  $CO_2$  breakthrough. For the PSA separation, the  
 11 time length of  $CO_2$  displacement step must shorter than  $t_{cd}$ .

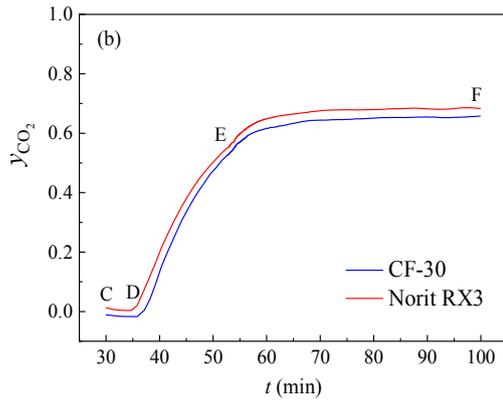


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2 **Fig. 5.** The time evolution of the mole fraction of CH<sub>4</sub> (a) and CO<sub>2</sub> (b) in the gas

3 phase with CO<sub>2</sub> injection

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### 5 3.2.3 The partial pressure of CO<sub>2</sub> and CH<sub>4</sub> of CO<sub>2</sub>-EGR

6 The absolute partial pressure of CH<sub>4</sub> ( $p_{CH_4}$ ) and CO<sub>2</sub> ( $p_{CO_2}$ ) in the gas phase are

7 calculated according to Eq.10 and Eq.11, in which  $p$  is the total pressure shown in

8 Fig.1. The calculated results of  $p_{CH_4}$ - $t$  and  $p_{CO_2}$ - $t$  curves are shown in Figure 6.  $p_{CO_2}$

9 deviates a little bit from 0.0 in the CD stage, and  $p_{CH_4}$  deviates a little bit from 1.0 at C

10 point, which are also due to the fitting error of Langmuir equation(as discussed in

11 3.1.1).

12

$$p_{CH_4} = p y_{CH_4} \quad (10)$$

13

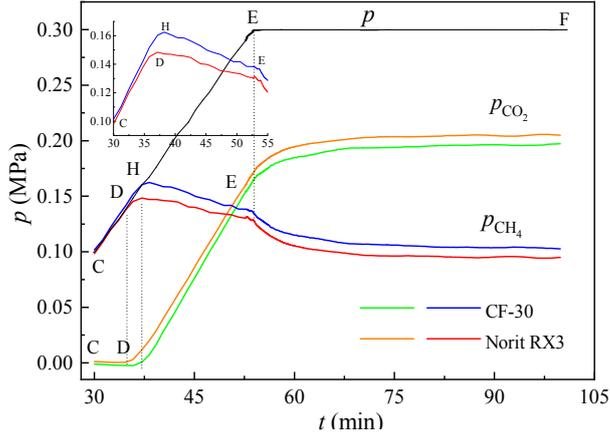
$$p_{CO_2} = p y_{CO_2} = p (1 - y_{CH_4}) \quad (11)$$

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2 **Fig.6** The change of  $p_{CH_4}$  and  $p_{CO_2}$  with time in the process of  $CO_2$  injection

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4 In the CD stage of  $CO_2$  injection,  $p_{CH_4}$  raises sharply with the  $CO_2$  injection;  
 5 while  $p_{CO_2}$  keeps zero. It is should be noted that  $p_{CH_4}$  is always higher than that before  
 6  $CO_2$  injection (0.1MPa). This results show that  $CH_4$  absorption always occurs in the  
 7  $CO_2$  injection process.  $p_{CH_4}$  still increases for a little time after  $CO_2$  breakthrough. This  
 8 is because the total pressure  $p$  increased, although  $y_{CH_4}$  decreases. Then,  $p_{CH_4}$  decreases,  
 9 but  $p_{CO_2}$  increases dramatically. At the EF stage,  $p_{CH_4}$  and  $p_{CO_2}$  reach a constant value  
 10 gradually under the maintain pressure of 0.3 MPa.

### 11 3.3.4 The $CH_4$ recovery factor of $CO_2$ -EGR

12 Because the pressures of the gas are low, the equation of state (EOS) for an ideal  
 13 gas can be used,

$$14 \quad pV = nRT \quad (12)$$

15 where  $V$  is the volume,  $p$  is the partial pressure of gas,  $R$  is the gas constant,  $n$  is  
 16 number of moles and  $T$  is the temperature.

17 Let  $p_1$  and  $n_1$  be the partial pressure and number of moles of  $CH_4$  before  $CO_2$

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1 injection,  $p_2$  and  $n_2$  be the partial pressure and number of moles of  $\text{CH}_4$  after  $\text{CO}_2$   
2 injection. And hence  $(n_2 - n_1)$  is the  $\text{CH}_4$  displacement amount by  $\text{CO}_2$ . Their  
3 relationship of  $p$  and  $n$  is given by Eq.(13). The  $\text{CH}_4$  recovery factor ( $R_{\text{CH}_4}$ ) is given by  
4 Eq.(14).

$$\frac{p_2}{p_1} = \frac{n_2}{n_1} \quad (13)$$

$$R_{\text{CH}_4} \% = \frac{n_2 - n_1}{n_1} \times 100 \% = \left( \frac{n_2}{n_1} - 1 \right) \times 100 \% = \left( \frac{p_2}{p_1} - 1 \right) \times 100 \% \quad (14)$$

7 The calculated  $R_{\text{CH}_4}$  with time is shown in Figure 7, which show that  $R_{\text{CH}_4}$  raises  
8 rapidly in the CD stage, and then declines rapidly in the HE stage.  $R_{\text{CH}_4}$  decreased  
9 slowly in EF, and then reached a stable value. The results are consistent with the shale  
10 gas analysis results [20].

11 In the CD phase,  $R_{\text{CH}_4}$  of CF-30 and RX3 increased to 51.02% and 35.75%,  
12 respectively. The accumulation of  $R_{\text{CH}_4}$  in CF-30 is 1.7 times that of RX3. This is  
13 because the CF-30 has more small pores which only  $\text{CO}_2$  can enter into. It is noted  
14 that the peaks of  $R_{\text{CH}_4}$  and  $p_{\text{CH}_4}$  did not appear in the initial stage of CD. The maximum  
15 values of  $R_{\text{CH}_4}$  are 61.1% and 47.6% which appear at H point of DE stage, and the  
16 corresponding  $y_{\text{CH}_4}$  are 0.95 and 0.92, respectively. Wang [20] also noted that the peak  
17 productivity would not appear in the first month. At the end of DE phase,  $R_{\text{CH}_4}$   
18 decrease to 36.1% and 27.7%, and  $y_{\text{CH}_4}$  is 43.9% and 41.8% in CF-30 and RX3,  
19 respectively. In DE stage, the cumulative  $R_{\text{CH}_4}$  value of CF-30 is 1.23 times that of  
20 RX3. In addition, the accumulation of  $R_{\text{CH}_4}$  in DE stage was much higher than that in

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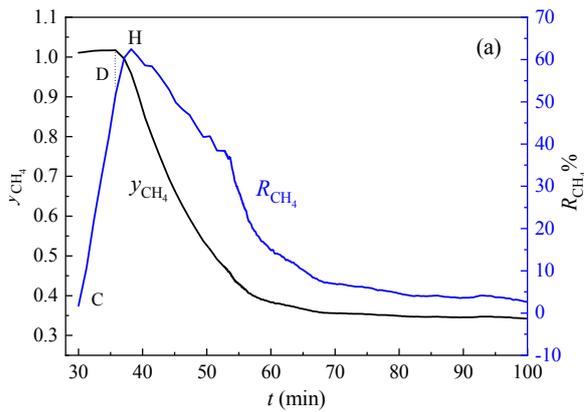
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1 CD stage. The cumulative  $R_{CH_4}$  of CF-30 and RX3 in DE phase are 63.1 and 86.5  
2 times of that in CD phase, respectively. With the increase of cumulative  $R_{CH_4}$ ,  $y_{CH_4}$   
3 decreases after  $CO_2$  breakthrough at D point. At the equilibrium stage (EF), the  $R_{CH_4}$  is  
4 very small. As seen from Fig. 5, at point F of the equilibrium stage (EF),  $y_{CH_4}$  of CF-  
5 30 and RX3 are 0.35 and 0.31, which result show that more  $CH_4$  is displaced to the  
6 gas phase on CF-30 than on RX3. As shown in Fig.3a,  $y_{CH_4}$  of 0.35 corresponds to  $x_{CH_4}$   
7 of 0.14 (point 5) for CF-30, and  $y_{CH_4}$  of 0.31 corresponds to  $x_{CH_4}$  of 0.16 (point 6) for  
8 RX3. These results show that the residual  $CH_4$  in RX3 ( $x_{CH_4}$  of 0.16) is more than that  
9 in CF-30 ( $x_{CH_4}$  of 0.14). Therefore, a larger  $S_{CO_2/CH_4}$  results in a larger  $R_{CH_4}$ .

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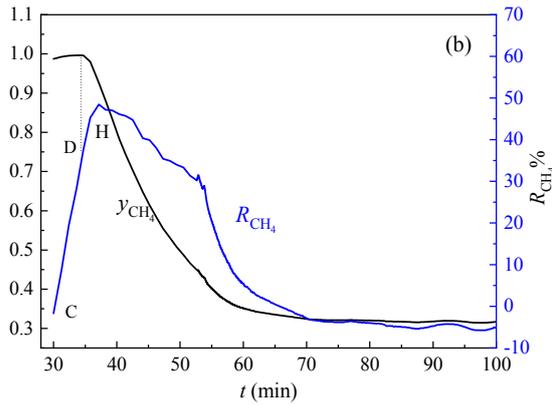


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2 Fig.7 The time evolution  $CH_4$  recovery ( $R_{CH_4}$ ) and  $y_{CH_4}$  during  $CO_2$  injection

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### 4 3.3 The dynamic adsorption mechanism of $CO_2$ -EGR

5 The dynamic curves of the  $q_t$ ,  $y_{CH_4}$ ,  $p_{CH_4}$  and  $p_{CO_2}$  with time demonstrate that there  
6 are two adsorption stages during the continue  $CO_2$  injection before adsorption  
7 equilibrium. These two stages also appear in the breakthrough curves<sup>[1-3]</sup> and the  
8 permeability curve with time in other studies<sup>[17]</sup>. The duration of the initial  $CO_2$   
9 injection stage( $t_{CD}$ ) relies on the selectivity of  $CO_2$  over  $CH_4$  ( $S_{CO_2/CH_4}$ ). A larger  $S_{CO_2/CH_4}$   
10 of an adsorbent (reservoir) have longer  $t_{CD}$  and high  $R_{CH_4}$  in the  $CO_2$  injection process.

11 In the initial  $CO_2$  injecting (CD stage),  $p_{CO_2}$  keeps zero, suggesting that all the  
12  $CO_2$  injected enters into adsorbent. Both of the CF-30 and RX3 GACs have many  
13 pores whose size is less than 0.62 nm, where  $CO_2$  can enter into, but  $CH_4$  is inhibited.  
14 Moreover,  $CO_2$  is adsorbed some surface sites larger than 0.62nm where have not  
15 been occupied by  $CH_4$ . The entering of  $CO_2$  reduces the  $CH_4$  partial pressure in the  
16 adsorbent, and hence  $CH_4$  desorbs and enters the gas phase. The desorption rate of  
17  $CH_4$  and  $R_{CH_4}$  rate are fast because no competitive adsorption occurs.

18 In the DE stage of  $CO_2$  injection,  $CO_2$  enters into adsorption sites where  $CH_4$

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1 have occupied and competitive adsorption between CH<sub>4</sub> and CO<sub>2</sub> occurred. Once  
2 competitive adsorption occurs, CO<sub>2</sub> mixes with CH<sub>4</sub>. Therefore, the desorption gas is a  
3 mixture of CH<sub>4</sub>/CO<sub>2</sub>, which is confirmed by the  $y_{CH_4}$  less than 1.0. Because of the  
4 continue CH<sub>4</sub> desorption, more pores are left and more CO<sub>2</sub> is adsorbed. The  
5 cumulative  $R_{CH_4}$  of the initial stage are much larger than that of the initial stage,  
6 confirms that most CH<sub>4</sub> in the adsorbent as adsorbed state.

7  $p_{CH_4}$  is always larger than 1.0 MPa in the whole CO<sub>2</sub> injection. It is suggested that  
8 CH<sub>4</sub> desorption is not by the gas phase pressure depletion. According to the common  
9 sense, CH<sub>4</sub> should be adsorbed rather than desorbed when the CH<sub>4</sub> partial pressure in  
10 the gas phase increases. However, CH<sub>4</sub> always desorption during CO<sub>2</sub> continue  
11 injection, which confirms the strong adsorption and displacement capacity of CO<sub>2</sub>.  
12  $p_{CH_4}$  and  $R_{CH_4}$  raise with high rate in the CD stage of CO<sub>2</sub> injection. More important,  
13  $y_{CH_4}$  keeps 1.0 only in the CD stage and then declines a lot. The CD stage of CO<sub>2</sub>  
14 injection is ideal for the CO<sub>2</sub>-EGR. The CH<sub>4</sub> product is pure,  $R_{CH_4}$  rate increases. An  
15 adsorbent with large  $S_{CO_2/CH_4}$  has long  $t_{CD}$ .

16

#### 17 **4 Conclusions**

18 The results in this paper presented a better understanding of the dynamic  
19 adsorption mechanism of gas recovery by CO<sub>2</sub> injection(CO<sub>2</sub>-EGR). CO<sub>2</sub>-EGR  
20 experiment was contacted by the continuous injection of CO<sub>2</sub> into the adsorbent pre-  
21 adsorbed with CH<sub>4</sub>.

22 (1) The adsorption selectivity of CO<sub>2</sub> over CH<sub>4</sub> ( $S_{CO_2/CH_4}$ ) is an important

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1 parameter that evaluates the possibility and effectiveness of the CO<sub>2</sub>-EGR. When  $S_{\text{CO}_2/}$   
2  $\text{CH}_4$  is larger than 1.0, CO<sub>2</sub> hinders CH<sub>4</sub> adsorption and reduces fractions of CH<sub>4</sub> in  
3 adsorbed-phase ( $x_{\text{CH}_4}$ ). The adsorbent with more micropore size has larger  $S_{\text{CO}_2/\text{CH}_4}$ .  
4 More CH<sub>4</sub> molecules will be driven out from the adsorbent of high  $S_{\text{CO}_2/\text{CH}_4}$ .

5 (2) The adsorption dynamic isotherms of CO<sub>2</sub>-EGR were measured. There are  
6 two adsorption stages in CO<sub>2</sub> injection process. At the beginning of CO<sub>2</sub> injection (CD  
7 stage), all of the injected CO<sub>2</sub> is adsorbed in the adsorbent and  $p_{\text{CO}_2}$  keeps zero.  $p_{\text{CH}_4}$   
8 and  $R_{\text{CH}_4}$  raise fast. This stage is the ideal period for CO<sub>2</sub>-EGR. The during of this  
9 stage ( $t_{\text{cd}}$ ) depends on  $S_{\text{CO}_2/\text{CH}_4}$ . A large  $S_{\text{CO}_2/\text{CH}_4}$  has a longer  $t_{\text{cd}}$ .

10 (3) In the second stage, the cumulative  $R_{\text{CH}_4}$  is much larger than that of the CD  
11 stage, confirming that most CH<sub>4</sub> was desorbed is driven out at this stage. The injected  
12 CO<sub>2</sub> enters the adsorption site occupied by CH<sub>4</sub>, competes with CH<sub>4</sub> for adsorption,  
13 and mixes with CH<sub>4</sub>. The gas released from the adsorbent is CH<sub>4</sub>/CO<sub>2</sub> mixture.  $p_{\text{CO}_2}$   
14 increase and  $y_{\text{CH}_4}$  decreases sharply.

15 (4)  $p_{\text{CH}_4}$  in the whole CO<sub>2</sub> injection is always larger than that before CO<sub>2</sub>  
16 injection, suggesting CH<sub>4</sub> desorption results from the displacement by CO<sub>2</sub> rather than  
17 from pressure depletion.

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