

PROBLEMAS SOBRE EL TEOREMA DE VARIGNON

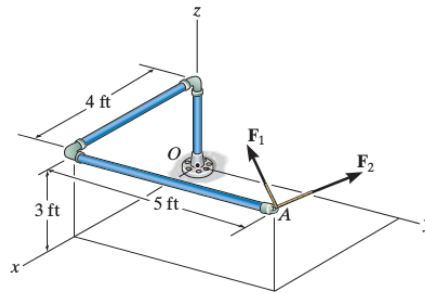
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En esta practica siguiente se vera problemas sobre calcular los momentos que son a través de los vectores y las fuerzas.

F4-12. If $\mathbf{F}_1 = \{100\mathbf{i} - 120\mathbf{j} + 75\mathbf{k}\}$ lb and $\mathbf{F}_2 = \{-200\mathbf{i} + 250\mathbf{j} + 100\mathbf{k}\}$ lb, determine the resultant moment produced by these forces about point O . Express the result as a Cartesian vector.



$$\mathbf{F}_1 = (100 - 120\mathbf{j} + 0\mathbf{k}) \text{ lb} \quad \mathbf{F}_2 = (-200\mathbf{i} + 250\mathbf{j} + 100\mathbf{k}) \text{ lb}$$

$$\mathbf{r}_{OA} = (0\mathbf{i} + 0\mathbf{j} + 0\mathbf{k}) \quad \mathbf{r}_{OB} = (4\mathbf{i} + 5\mathbf{j} + 3\mathbf{k})$$

$$M_O + M_1 + M_2 = r_{Ax}F_1 + r_{Bx}F_2$$

$$\mathbf{r}_A \times \mathbf{F}_1 =$$

$$\begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 0 & 0 \end{vmatrix}$$

$$\begin{vmatrix} 0 & 0 & 0 \end{vmatrix} = 0\mathbf{i} + 0\mathbf{j} + 0\mathbf{k}$$

$$\begin{vmatrix} 100 & 120 & 75 \end{vmatrix}$$

$$\begin{aligned} \mathbf{r}_B \times \mathbf{F}_2 &= \\ \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 4 & 300 & j \\ 520 & -(-500) & k \end{vmatrix} &= \\ (875 - 390) \mathbf{i} - (700 - (-)) \mathbf{j} - 100 \mathbf{i} &= 130 \mathbf{j} + 1020 \mathbf{k} \\ \mathbf{M}_O &= 485 \mathbf{i} - 1000 \mathbf{j} + 1020 \mathbf{k} \end{aligned}$$

$$F_{AX} = F_A \cos \theta = \frac{4}{5} F_A$$

$$F_{AY} = F_A \sin \theta = \frac{3}{5} F_A \quad F_{BX} = F_B \cos 60^\circ$$

$$F_{BY} = F_B \sin 60^\circ$$

$$\sum F_{bx} = 0$$

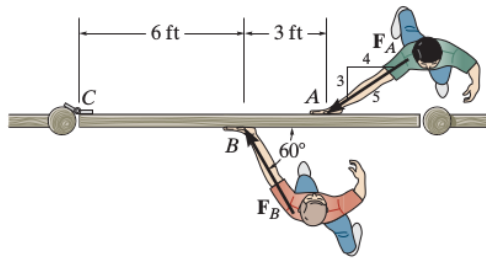
$$\sum F_{by} = 0$$

$$-30 \text{ lb} \cos 60^\circ - \frac{4}{5} F_A = 0 \quad -30 \text{ lb} \cos 60^\circ - \frac{4}{5} F_A = 0$$

$$F_A = \frac{5}{4} (-30 \text{ lb} \cos 60^\circ) = -18.75 \text{ lb} \quad \text{resultado}$$

EJERCICIO 2

4-14. Two boys push on the gate as shown. If the boy at B exerts a force of $F_B = 30 \text{ lb}$, determine the magnitude of the force F_A the boy at A must exert in order to prevent the gate from turning. Neglect the thickness of the gate.



PARA B

$$F_{Ax} = 30 \text{ lb} \cos 60^\circ$$

$$r_{Bx} = 6 \text{ ft}$$

$$r_{By} = 0$$

$$F_{Ay} = 30 \text{ lb} \sin 60^\circ$$

PARA A

$$r_{Ax} = 9$$

$$F_{Bx} = \frac{4}{5} F_A$$

$$r_{Ay} = 0$$

$$M_A = r_{Ax} \times F_{Ay} - r_{Ay} \times F_{Ax}$$

$$F_{By} = \frac{3}{5} F_A$$

$$(9f) \left(\frac{3}{5}FA\right) - (0) \left(\frac{4}{5}\right) = \frac{27}{5}FA \text{ lb ft}$$

$$\text{rbx} \quad \quad \quad \text{x}$$

$$155.88 \text{ lb ft}$$

$$\text{Fby - rby}$$

$$\text{x Fb} = (6) (30 \sin 60) - (0) (30 \cos 60) =$$

$$\Sigma M = 0$$

$$Mb - Ma = 0 \quad 155.88 \text{ lb ft} - \frac{27}{5}FA \text{ lb ft}$$

$$\frac{27}{5}FA = 155.88$$

$$FA = \left(\frac{27}{5}\right) (155.88 \text{ lb ft})$$

$$FA = 29.9 \text{ lb ft respuesta}$$