

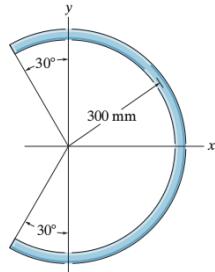
Problema sobre centroides,

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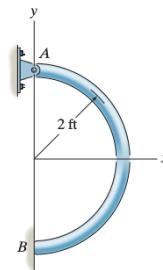
2 de abril de 2019

9-1. Locate the center of mass of the homogeneous rod bent into the shape of a circular arc.



Prob. 9-1

9-2. Locate the center of gravity \bar{x} of the homogeneous rod bent in the form of a semicircular arc. The rod has a weight per unit length of 0.5 lb/ft. Also, determine the horizontal reaction at the smooth support B and the x and y components of reaction at the pin A .



Prob. 9-2

$$\bar{x} = r \cos \theta$$

$$p = 0,5 \frac{lb}{ft}$$

$$\bar{y} = r \sin \theta$$

$$p = \frac{w}{L} = 0,5 \frac{lb}{ft}$$

$$dt = rd\theta$$

$$w = \left(0,5 \frac{lb}{ft}\right) (2ft \cdot \pi) = \pi lb$$

$$\lim ites = -120^a 120^{= \frac{2\pi}{3}, \frac{2\pi}{3}}$$

$$\bar{x} = \frac{\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} (r \cos \theta)(rd\theta)}{\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} rd\theta}$$

$$\bar{y} = \frac{r^2 \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos \theta d\theta}{r \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \theta d\theta} = \frac{r[\sin \theta]}{[\theta]} = \frac{300mm[0,866+0,866]}{\frac{4}{3}\pi} = 124,04mm$$

$$\Sigma M = 0 - \left(\frac{4}{\pi} ft\right) w + (4ft) Bx$$

$$\bar{y} = \frac{r^2 \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin \theta d\theta}{r \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \theta d\theta} = \frac{r[\cos \theta]}{[\theta]} = -0,5 + 0,5 = 0mm$$

$$(4ft) Bx = \frac{4ft}{lb}$$

$$El punto es : (124,04, 0)$$

$$Bx = 1lb$$

$$Ax = 1lb$$

$$Ay = \pi lb$$