

# Problemas sobre el teorema de Varignon

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en esta practica aprenderemos a calcular momentos a través de fuerzas y vectores

$$f1=(100-120j+75k)lb$$

$$f2=(-200i+250j+100k)lb$$

$$rA=(0i+0j+0k)$$

$$rB=(4i+5j+3k)$$

$$Mo= M1+M2=rAxF1+rBxF2$$

$$rA \times F1 = \begin{vmatrix} I & J & K \\ 0 & 0 & 0 \\ 100 & 120 & 75 \end{vmatrix} = 0i+0j+0k$$

$$rB \times F2 = \begin{vmatrix} I & J & K \\ 4 & 5 & 3 \\ -100 & 130 & 175 \end{vmatrix} = (875-390)i - (700-(-300))j + (520-(-500))k$$

$$MOT=485i-1000j+1020k$$

$$FAX = FA \cos \theta = \frac{4}{5}FA$$

$$FAY = FA \sin \theta = \frac{3}{5}FA$$

$$FBX = FB \cos \theta 60^\circ$$

$$FbY = FB \sin \theta 60^\circ$$

$$\Sigma Fx = 0$$

$$\Sigma Fbx - Fby = 0$$

$$-30lb \cos 60 - \frac{4}{5}FA = 0$$

$$FA = \frac{5}{4}(-30lb \cos 60^\circ) = 18.75$$

Este valor solo solo seria valido si las fuerzas estuvieran actuando con el mismo brazo.

para B

$$rbx= 6 \text{ ft}$$

$$ray=0$$

para A

$$rbx=9 \text{ ft}$$

$$rby=0$$

$$MA=rax \times Fay - ray \times Fax$$

$$=(9ft) \left( \frac{3}{5}FA \right) - (0) \left( \frac{4}{5} \right) = \frac{27}{5}FA \text{ lb ft}$$

$$rbx \times Fby - rby \times Fbx = (0)(30 \cos 60^\circ) - (0)(30 \cos 60^\circ) = 155.88 \text{ lb ft}$$

$$\Sigma M = 0$$

$$Mb - Ma = 0$$

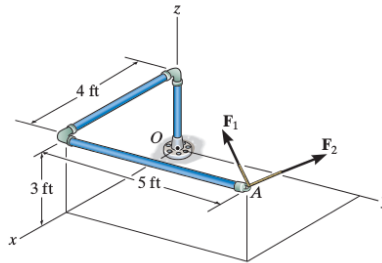
$$155.88 \text{ lb ft} - \frac{27}{5}FA \text{ lb ft}$$

$$\frac{27}{5}FA = 155.88$$

$$FA = \left( \frac{27}{5} \right) (155.88 \text{ lb ft})$$

$$FA = 28.9 \text{ lb ft}$$

**F4-12.** If  $\mathbf{F}_1 = \{100\mathbf{i} - 120\mathbf{j} + 75\mathbf{k}\}$  lb and  $\mathbf{F}_2 = \{-200\mathbf{i} + 250\mathbf{j} + 100\mathbf{k}\}$  lb, determine the resultant moment produced by these forces about point  $O$ . Express the result as a Cartesian vector.



**4-14.** Two boys push on the gate as shown. If the boy at  $B$  exerts a force of  $F_B = 30$  lb, determine the magnitude of the force  $F_A$  the boy at  $A$  must exert in order to prevent the gate from turning. Neglect the thickness of the gate.

