Identification of plasma environments within the terrestrial magnetotail and its global structure from the Magnetospheric Multiscale Mission

Tien Vo^{1,2}, Robert Ergun^{1,2,3}, Maria Usanova¹, and Alexandros Chasapis¹

¹Laboratory for Atmospheric and Space Physics, University of Colorado ²Department of Physics, University of Colorado ³Department of Astrophysical and Planetary Sciences, University of Colorado

June 30, 2023

Identification of plasma environments within the terrestrial magnetotail and its global structure from the Magnetospheric Multiscale Mission

T. $Vo^{1,3}$, R. E. Ergun^{1,2}, M. E. Usanova¹, and A. Chasapis¹

¹ Laboratory for Atmospheric and Space Physics, University of Colorado, Boulder, CO, USA
 ² Department of Astrophysical and Planetary Sciences, University of Colorado, Boulder, CO, USA

³ Department of Physics, University of Colorado, Boulder, CO, USA

Key Points:

2

3

4

6

7

8

- Inner-magnetotail environments are statistically identified with background plasma
 conditions and their global 3D structure is studied.
- Warping effects attributed to changes in the Earth's dipole tilt angle leads to an
 apparent dawn-dusk asymmetry during the summer months.
- We utilize a large volume of MMS data with partial plasma moments calculated
 from low-energy plasma and energetic particle instruments.

Corresponding author: Tien Vo, Tien.Vo@lasp.colorado.edu

15 Abstract

Using MMS orbits in the Earth's magnetotail from 2017 to 2020, plasma conditions 16 and the 3D spatial structure of inner-magnetotail plasma environments (with a focus on 17 the plasma sheet) are studied with different approaches. Threshold conditions for dis-18 tinguishing the plasma sheet, plasma sheet boundary layers, and lobes are derived from 19 the statistical properties of background plasma parameters. Our results support previ-20 ous studies that employed similar methods using Cluster data. However, stronger cur-21 rents are observed in both the lobes and plasma sheet, likely due to the smaller space-22 craft separation ($\lesssim 70 \, \mathrm{km}$) that can resolve thin electron-scale currents. Threshold con-23 ditions are used together with magnetic field and electric field measurements to image 24 the spatial structure of the plasma sheet. Results are in good agreement with a global 25 neutral sheet model based on solar wind conditions and magnetospheric configurations. 26 Furthermore, the Earth's dipole tilts towards the Sun around June solstice, which warps 27 the magnetotail as much as \sim 2–4 $\rm R_{E}$ in Z GSM. This warping effect is relaxed towards 28 September equinox. Consequently, as MMS travels through the magnetotail from dawn 29 to dusk during this period, there is an apparent dawn-dusk asymmetry in plasma con-30 ditions between June and September. Kink-like flapping waves and IMF twisting are other 31 mesoscale processes attributed with a few R_E of flaring near the flanks. These findings 32 reveal important insights into the mesoscale structure and dynamics of the magnetotail. 33

34

Plain Language Summary

Data from four years of observations by NASA's MMS mission are used to statis-35 tically identify distinctive regions within the Earth's magnetospheric tail. This study re-36 veals insights into the spatial structure of this "magnetotail" and seasonal variations at-37 tributed with changes in the Earth's magnetic field configurations, particularly those of 38 the orientation of the Earth's dipole. Our results agree with reported findings from ESA's 39 Cluster mission. However, certain aspects unique to MMS lead to some improved mea-40 surements and features relating to MMS orbital design. The presented results are highly 41 beneficial to future large statistical studies with MMS data. 42

43 1 Introduction

Situated at the nightside of the Earth's magnetosphere, the magnetotail can stretch 44 as far as $\sim 10^3$ Earth radii (R_E) (Dungey, 1965; Cowley, 1991) and can exceed $30 R_E$ 45 in radius (Coroniti & Kennel, 1972; Shukhtina et al., 2004). Driven by interactions with 46 the solar wind and the interplanetary magnetic field (IMF) as well as changes in geo-47 magnetic configurations and plasma conditions, it plays a central role in magnetospheric 48 dynamics from global to kinetic scales. Therefore, to understand the multiscale dynam-49 ics within the magnetotail, there has been great interest to identify its complex struc-50 ture and plasma conditions. 51

From global to meso-scales, the magnetotail is subjected to distinct types of de-52 formation, three of which are known as flapping, twisting, and warping (Dayeh et al., 53 2015). Solar wind directional changes can cause it to flap either steadily in the north-54 south direction, or drive kink-like waves propagating towards the flanks (Lui et al., 1978; 55 Sergeev et al., 2003; Zhang et al., 2005; Gao et al., 2018). The flapping and the waves 56 have periods on the order of 1–10 minutes with wavelengths of $1-4 R_E$ (Rong et al., 2018; 57 Wang et al., 2019). Non-zero IMF B_y can apply a torque and twist the tail as high as 58 50° about the Sun-Earth line (Owen et al., 1995; Tsyganenko, 1998). Due to the $\sim 11^{\circ}$ 59 tilt of the Earth's dipole axis with respect to its rotational axis (Amit & Olson, 2008), 60 the magnetotail is periodically displaced $\sim 1-2\,\mathrm{R_E}$ above and below the equatorial plane 61 (Hammond et al., 1994) with a hinge radius of $\sim 10 R_E$ (Tsyganenko & Fairfield, 2004). 62 Under these effects, the tail shape is extremely complex and variable on time scales from 63 a few minutes to many days and spatial scales up to many Earth radii. 64

There are several distinct plasma environments in the magnetotail. Boundary lay-65 ers at the flanks can bring magnetosheath plasma into the inner magnetosphere via mix-66 ing instabilities (e.g. Otto & Fairfield, 2000; Fairfield et al., 2000; Nykyri et al., 2006; 67 Johnson et al., 2014). In the middle of the tail, a plasma sheet (PS), which is a few R_E 68 in thickness under normal conditions (Russell & McPherron, 1973; McComas et al., 1986; 69 Sanny et al., 1994; Zhou et al., 1997), contains high-beta plasma and low equatorial mag-70 netic field (Baumjohann et al., 1989). To the contrary, the northern and southern lobes 71 enclosing the PS are often characterized by low-beta plasma and high equatorial mag-72 netic field, predominantly pointing sunward or antisunward. Separating the PS and the 73 lobes, the plasma sheet boundary layers (PSBLs) mix hot and cold plasmas from these 74

-3-

two environments (Eastman et al., 1984) and often display signatures of nonlinear ki-75 netic structures (Cattell et al., 1986; Nakamura et al., 2004; Ergun et al., 2009; Malaspina 76 et al., 2015; Tong et al., 2018). Embedded within the PS is a neutral sheet (NS), often 77 characterized as the null point of the equatorial magnetic field. The NS is the locus of 78 many explosive geomagnetic activities during substorms (Sitnov et al., 2019, and refer-79 ences therein) which include, for example, kinetic instabilities, magnetic reconnection, 80 locally generated turbulence, particle energization, etc (Zimbardo et al., 2010; Sitnov & 81 Schindler, 2010; Liu et al., 2014; Ukhorskiy et al., 2017; Chen et al., 2019; Ergun et al., 82 2020a, 2020b, 2022; Usanova & Ergun, 2022). 83

The complex evolution of mesoscale dynamics and kinetic-scale structures often make 84 identifying the various plasma environments a non-trivial task. Previous attempts to iden-85 tify plasma environments and their spatial variations in the inner magnetotail have in-86 cluded a number of different methods. Combining decades of data, multi-mission stud-87 ies (Hammond et al., 1994; Tsyganenko & Fairfield, 2004; Dayeh et al., 2015; Xiao et al., 88 2016) have imaged the neutral sheet under twisting and warping effects by observing the 89 sign of magnetospheric B_x , from which global models are constructed. Multi-spacecraft 90 missions, e.g. Cluster (Escoubet et al., 2001) and THEMIS (Angelopoulos et al., 2008), 91 allow for timing analysis, often used to study the flapping motion (Runov et al., 2005, 92 2009). Most commonly, statistical threshold conditions based on averaged background 93 parameters such as the plasma beta, number density, current density, magnetic field and/or 94 plasma flow are used to distinguish the NS, PS, PSBL, and lobe (Baumjohann et al., 1988; 95 Angelopoulos et al., 1994; Åsnes et al., 2008; Boakes et al., 2014). Assuming a certain 96 time scale of the magnetic fluctuations, threshold conditions can also be defined based 97 on magnetometer data alone to distinguish the lobe and PS (Coxon et al., 2016). When 98 the threshold approach fails, the outer layer of the PS and PSBL may be determined on 99 a case-by-case basis by analyzing beam-like populations in the 3D distribution function 100 (Grigorenko et al., 2012) or ionospheric photoelectrons (Pedersen et al., 1985; Baumjo-101 hann et al., 1988). 102

The Magnetospheric Multiscale mission (MMS), launched in 2015, is a NASA fourspacecraft mission (Burch et al., 2016) that targets electron-scale magnetospheric physics, building upon the success of Cluster. Capable of higher time resolution and higher accuracy electromagnetic field and particle measurements, MMS has the potential to reinforce past studies of global models, threshold conditions, and kinetic-scale properties.

-4-

As apparent from previous experiences, it is challenging to achieve a definitive identification of the inner-magnetotail plasma environments at any given time. Nevertheless, knowledge of mesoscale factors and background parameters from MMS data can provide insights into the magnetotail configuration at various scales. We remark that identifying plasma regions and boundaries is essential to a systematic statistical study of kineticscale magnetotail physics.

In this paper, we utilize a large volume of MMS observations to investigate the prop-114 erties of magnetotail plasma environments through a few different approaches, with a 115 focus on the plasma sheet. Statistically, we derive threshold conditions based on back-116 ground plasma conditions to distinguish different environments. Results are discussed 117 in comparison with those from a previous study using Cluster data (Boakes et al., 2014). 118 Furthermore, the large volume of data allows for enough spatial coverage to image the 119 global structure of the neutral sheet (i.e. through magnetic field measurements similar 120 to Tsyganenko & Fairfield, 2004; Xiao et al., 2016). The structure of the NS based on 121 B_x will be compared with that of the PS identified from the threshold approach, and 122 the NS model fitted by Xiao et al. (2016). Since the NS is embedded within the PS, we 123 show that all of these approaches (threshold, imaging, modeling) generally agree, thereby 124 revealing insights into both the statistical properties of background plasma conditions 125 and the spatial variations of the NS/PS within the magnetotail. For example, since MMS 126 always visits the magnetotail from June solstice to September equinox (correspondingly, 127 from the dawn to dusk sectors in GSM coordinates), observations of the PS spatial struc-128 ture reveal that warping effects are prominent around June and insignificant around Septem-129 ber, resulting in an apparent dawn-dusk asymmetry in plasma conditions. Our data also 130 feature the combination of partial plasma moments from low-energy plasma and ener-131 getic particle instruments, the technicality and motivation for which are presented in this 132 paper. 133

This paper is organized as follows. In Section 2, we describe relevant details of MMS instrumentation. In Section 3, we describe our dataset, which is compiled from a broad array of MMS instruments measuring fields and particles, where we also present the combined plasma moments and the motivation for their consideration. In Section 4, we discuss the exclusion of outer magnetotail environments and present the properties of background plasma conditions in the inner magnetotail. In Section 5, we examine the 3D global structure of the neutral sheet and plasma sheet using the threshold, imaging, and mod-

-5-

eling approaches. Finally, we discuss the implications of these results and provide con-

¹⁴² cluding remarks in Section 6.

¹⁴³ 2 Instrumentation

A broad array of MMS instruments are used enable and optimize statistical magnetotail studies of the electromagnetic field, particle properties, and their correlation. While the present paper only concerns with statistical, mesoscale quantities, we recognize that the large volume of data considered here also can be generically advantageous for future large-scale studies of kinetic physics in the magnetotail.

The four identical MMS spacecrafts travel in a tetrahedral formation with a highly 149 eccentric, near-Earth-equatorial orbit with an initial apogee of $12 \, R_E$ and a perigee of 150 roughly $1.2 R_{\rm E}$ (Fuselier et al., 2016). The natural (inertial) orbital precession is small, 151 but as the Earth orbits the Sun, the apogee rotates between the subsolar region and the 152 magnetotail in roughly one year. Annually, magnetotail observations occur for MMS pri-153 marily in the summer months between June solstice and September equinox. To max-154 imize encounters with the neutral sheet during these seasons, the night-side apogee was 155 raised to $25 R_E$ in early 2017 and subsequently to $28 R_E$ in 2019 (Tedla et al., 2018). Through-156 out the magnetotail, MMS instruments operate in two data acquisition rates (fast sur-157 vey and burst). Fast survey data provide continuous coverage, and burst data are se-158 lected short-duration intervals of high time-resolution measurements. In this paper, we 159 use fast survey data from 2017 to the end of 2020 to optimize statistical observations of 160 magnetotail processes occurring between 12 and $28 R_E$. 161

In fast survey mode, the FIELDS investigation provides measurements of the DC 162 magnetic field and DC electric field in resolutions of 62.5 ms and 31.25 ms through the 163 Fluxgate Magnetometers (FGM) and Electric Double Probes (EDP) instruments (Torbert 164 et al., 2016; Russell et al., 2016; Ergun et al., 2016). At apogee, the tetrahedral forma-165 tion is targeted to have a geometric quality factor $Q \ge 0.7$ (Q = 1 being a perfect tetra-166 hedron) and an average spacecraft separation of 40 km, enabling measurements of field 167 gradients on several electron scales (Fuselier et al., 2016). Particularly, the current den-168 sity $\mathbf{J} = \mathbf{\nabla} \times \mathbf{B}/\mu_0$ can be estimated using the curlometer technique (Paschmann & Daly, 169 1998; Dunlop et al., 2021). Simultaneous multi-spacecraft measurements also allow for 170 calculations of barycentric quantities so that, for example, plasma dissipation measures 171

-6-

¹⁷² such as $\mathbf{J} \cdot (\mathbf{E} + \mathbf{u} \times \mathbf{B})$ (Zenitani & Hoshino, 2005; Ergun et al., 2018) or $(\mathbf{P} \cdot \nabla) \cdot \mathbf{u}$ (Chasapis ¹⁷³ et al., 2018; Yang et al., 2022) may be examined.

The Fast Plasma Investigation (FPI) samples plasma populations in the low-energy 174 range from $10 \,\mathrm{eV}$ to $30 \,\mathrm{keV}$ with time resolutions of $30 \,\mathrm{ms}$ for electrons and $150 \,\mathrm{ms}$ for 175 ions (Pollock et al., 2016). FPI instruments utilize top-hat electrostatic analyzers, form-176 ing 512 distributed field-of-views (FOVs) over the full 4π -sr solid angle, each measuring 177 32 energy channels. The fast survey FPI data products used in this study are 3D elec-178 tron and ion distribution functions that are integrated on-board high time-resolution mea-179 surements and reduced to 4.5-s resolution. FPI also provides partial plasma moments 180 (associated with its capable energy range) integrated in velocity space from the 4.5-s prod-181 ucts. 182

At the high-energy range, the Energetic Particle Detector (EPD) investigation com-183 prises the Fly's Eye Energetic Particle Sensor (FEEPS) and Energetic Ion Spectrome-184 ter (EIS) instruments, utilizing micro-channel plates and solid-state detectors to sam-185 ple energetic particles in the range of 60–500 keV (Mauk et al., 2016; Blake et al., 2016). 186 For better ion data availability and energetic electron measurements, we utilize FEEPS 187 data in this study. On each spacecraft, two FEEPS instruments are mounted 180° apart 188 on the spin plane, providing 9 electron FOVs (5 operating in fast survey) and 3 ion FOVs, 189 each measuring energy with 16 channels. Although this configuration provides instan-190 taneous measurements of the particle distribution over a 3π -sr solid angle, the main data 191 products are electron and ion energy-angle distributions, averaged in 2.5-s resolution by 192 means of rotation. As opposed to the full 3D distribution functions measured by FPI 193 at low energies, the most reliably available of the FEEPS measurements are spin-scanned, 194 omni-directional distribution functions. Therefore, the partial plasma moments that can 195 be calculated from FEEPS data are more limited than those from FPI data. 196

197

3 Methodology and Data

In the previous section, it is clear that low-energy ($\leq 30 \text{ keV}$) and high-energy ($\geq 60 \text{ keV}$) particles are measured by MMS with instruments that have quite distinct techniques (FPI and FEEPS, respectively), resulting in different time resolutions, angular coverages, and an energy-coverage gap of about 30 keV. Therefore, it is not trivial how partial plasma moments may be calculated (in the high-energy range) and combined from

-7-

the two instruments. While the combination of partial plasma moments has been ap-203 plied for previous capable missions such as THEMIS (Angelopoulos et al., 2008; Hietala 204 et al., 2015; Shustov et al., 2019) and Cluster (Haaland et al., 2010), it has not been rou-205 tinely performed for MMS and is often the constraining factor in previous studies, par-206 ticularly those investigating ion properties. For example, Artemyev et al. (2021) acknowl-207 edges the importance of contributions of 100-keV ions to the plasma moments in the mag-208 netotail, but because of the aforementioned constraint, these contributions are extrap-209 olated using THEMIS data by a scaling argument instead of direct calculations. In the 210 following, we provide another motivation for the necessity of combined plasma moments 211 in the magnetotail through a case study. At the same time, we present a demonstration 212 of our methodology in estimating the contributions of energetic particles to the plasma 213 moments. Technical details of this combination are specific to MMS data products and 214 discussed at length in Appendix A. 215

Consider a well-documented observation of a strongly turbulent, retreating recon-216 nection X-line in the magnetotail in Fig. 1 (Ergun et al., 2018, 2020a, 2020b). In (a–c), 217 an ion flow reversal occurs around 07:29, together with strong electromagnetic fluctu-218 ations persisting about 15 minutes, in which many intermittent structures are found such 219 as double layers, magnetic holes, electron phase-space holes, and thin current sheets. At 220 the same time, increases in energetic ion and electron energy fluxes are observed in (d) 221 and (e). The energy fluxes at some time before, during, and after the turbulent event 222 (denoted in (a-h) with vertical blue, green, and red lines) are also plotted in (i) and (j). 223 The particle distributions in (d–e) and (i–j) are omni-directional and contain both mea-224 surements from FPI (below the lower-energy, magenta dashed line) and FEEPS (above 225 the higher-energy dashed line). FEEPS measurements are interpolated to FPI resolu-226 tion. 227

From past statistical studies (Huang et al., 2020; Chong et al., 2022), it is reason-228 able to assume that the plasma bulk flow rarely surpasses FPI capabilities (about $2,000 \,\mathrm{km/s}$ 229 for ions and 100,000 km/s for electrons). So the contribution from thermal (low-energy) 230 particles to the plasma moments can be calculated from the FPI 3D distribution func-231 tions, correctly accounting for drifted particles. Subsequently, the non-thermal contri-232 bution may be considered isotropic and calculated from omni-directional distribution func-233 tions as detailed in Appendix A. However, this calculation is limited to directionless quan-234 tities, such as the number density and scalar pressure. Most clearly seen in (i-j), the energy-235

-8-

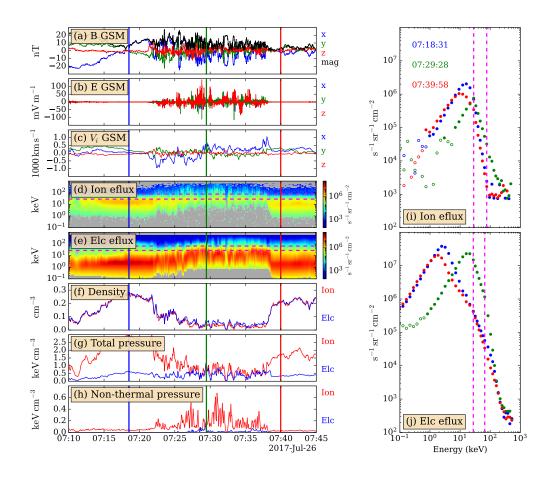


Figure 1. Example of FPI-FEEPS combined moment calculations for a strong turbulent reconnection event in the magnetotail. (a) Barycentric magnetic field. (b) Barycentric electric field. The rest of the panels show data from MMS1. (c) Ion velocity. (d) Combined omni-directional ion energy flux. (e) Combined omni-directional electron energy flux. (f) Combined ion (red) and electron (blue) density. (g) Combined ion and electron total pressure. (h) Pressure contribution of non-thermal, energetic (larger than FPI energy threshold) particles. In (a-h), the blue, green, red vertical lines are times before, during, and after the turbulent event. (i) The ion energy flux during vertical snapshots in (a-h). (j) Similarly, snapshots in electron energy flux. Hollow markers are noise-level or background measurements. The dashed magenta lines [horizontal in (d) & (e), vertical in (i) & (j)] denote the extrapolated energy gap between FPI and FEEPS. There are 5 extrapolated points in that gap.

coverage gap (between the dashed lines) may contain a significant contribution to the
plasma moments. Thus, we extrapolate the distribution function in this gap from FPI
and FEEPS measurements and include its contribution in the non-thermal moment calculations (see Appendix A). In (f-h), we show the total (thermal + non-thermal) number density, total pressure, and non-thermal pressure.

In this event, one significant feature emphasized by the Ergun et al studies is that 241 the reconnection inflow does not resupply particles from the lobe as fast as plasma sheet 242 particles are depleted by the outflow, which results in a density drop in the turbulent 243 region in (f) and the depletion of low-energy particles in (i-j). What we emphasize here 244 is that because of this depletion of low-energy particles, when comparing (g) and (h), 245 the contribution of non-thermal and/or energetic ions to the total pressure (character-246 istic energy density $P_s = nk_BT_s$ of species s) is on the order of 10% and can be as high 247 as 50%. While most electrons are within the thermal (FPI) energy range, there can also 248 be a significant fraction of non-thermal electrons ($\sim 10-20\%$ of total electron pressure) 249 in this type of events. Since the frequency of events similar to the one shown in Fig. 1 250 is not yet established, pressure and temperature calculations solely based on the FPI in-251 strument in the magnetotail may be underestimated for these occurrences. Therefore, 252 it may be crucial for statistical studies of particle energization in the magnetotail to con-253 sider plasma moments combined from both FPI and FEEPS. 254

The calculation of combined plasma moments above requires that there is simultaneous availability from both particle instruments. We also require that electromagnetic field observations (from FGM and EDP) are available to enable future statistical studies of the correlation between field and particle observations. Such a study will be able to establish the statistical occurrence between turbulence, reconnection, and particle energization events such as the example in Fig. 1.

For this study, we have compiled continuous intervals (no significant time gap; duration from minutes to hours) of good availability from the magnetic field, electric field, low-energy plasma, and energetic particle instruments during MMS magnetotail seasons from 2017 to 2020. Additionally, 1-minute averaged solar wind conditions are obtained from the OMNI dataset (King & Papitashvili, 2005), which is used to correlate the magnetotail dynamics with solar wind conditions. In total, there are 437,728,300 field (FGM resolution) and 6,078,827 particle (FPI resolution) data points, amounting to about 316 continuous days of observation. Details of compilation of these intervals are highly tech-

nical and are laid out in the Supporting Information (SI). The principal conditions are
listed below.

271 1. X < 0

272 2. $R \ge 12R_E$

- 273 3. $Q \ge 0.75$
- 4. No periods of thruster firing, EDP probe saturation, shadow spikes, or bad bias settings.
- 5. FGM, EDP available from MMS(1–4).
- 6. FPI, FEEPS available from MMS1.
- ²⁷⁸ 7. Interval at least 1-minute long.

Above, $\mathbf{R} = (X, Y, Z)$ is the spacecraft position in GSM. While most global models of 279 the neutral sheet, one of which is later on analyzed and compared, are fitted in aberrated 280 GSM (AGSM), we have found little difference between GSM and AGSM in our results. 281 Thus, we retain the usage of GSM for all coordinates in subsequent sections. Conditions 282 (3) and (5) ensures that the barycentric electromagnetic fields and the curlometer cur-283 rent density may be accurately estimated. (4) ensures intervals of adequate EDP data 284 for analysis. (6) ensures the partial plasma moments can always be combined. (7) en-285 forces that the intervals are adequately long for spectral analysis. 286

²⁸⁷ 4 Properties of the magnetotail background plasma conditions

In this section, we first distinguish the inner magnetotail from the solar wind and flank-side boundary layers, the properties of which are outside the scope of the present paper. Then, we present the statistical properties of the inner-magnetotail plasma conditions and compare our results with those in Boakes et al. (2014), hereby referred to as B14. Also, as done in B14, threshold conditions for the PS, PSBL, and lobe are derived based on the statistical properties of the plasma.

294

4.1 Exclusion of solar wind and flank-side boundary layers

Fig. 2 shows the X-Y distribution of (a) the coverage of MMS trajectory, (b) the ion density n_i , (c) the electron temperature T_e , and (d) the standard deviation of the

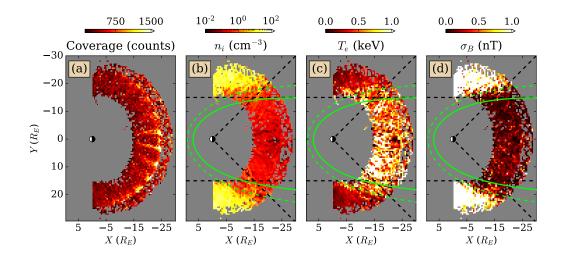


Figure 2. Spatial distribution in the X-Y plane of (a) MMS coverage during tail seasons in 2017–2020, (b) the ion density n_i , (c) the electron temperature T_e , and (d) standard deviation of the magnetic field σ_B . The lime curves are a 5° (clockwise) tilted magnetopause model (Lin et al., 2010) constructed with zero IMF B_z and total solar wind pressure of 5 nPa (dashed) and 20 nPa (solid). Dashed black lines denote $|Y| \leq 15 R_E$ and $|Y| \leq |X|$. The color scales are chosen to saturate solar wind values to also reveal typical plasma values in the tail.

magnetic field σ_B (over a 5-s moving window). In the magnetotail, the electron density 297 (n_e) measurement is more accurate than n_i . However, the reverse is true in the solar wind. 298 Here, we use n_i to reveal the differences between the solar wind and the magnetotail. 299 Later, we use n_e when characterizing the magnetotail. 3D histograms are calculated with 300 $0.5 R_{\rm E} \times 0.5 R_{\rm E} \times 0.5 R_{\rm E}$ cubic bins then averaged over the Z direction, except for (a), 301 which is summed instead. Hereafter, all data (e.g. the magnetic field, electric field, and 302 current density) are averaged over a 5-s moving window and subsequently down-sampled 303 to FPI resolution $(4.5 \,\mathrm{s})$ so that particle and field measurements can be compared. Thus, 304 in (a), each count represents a 5-s observation and the total count in each bin represents 305 the dwell time of MMS spacecrafts. 3D bins that have lower than 100 counts are excluded 306 as they may not be statistically representative. 307

In (a), the dwell time is not uniform. The highly-eccentric orbit has MMS spend more time near the apogee to maximize the chance of observing the diffusion region at reconnection sites (Fuselier et al., 2016). However, bins that have statistically significant counts are distributed over a large and uniform enough area so that the spatial distri-

-12-

bution of plasma parameters can be studied. Most notably in (b-d), the solar wind is 312 observed (as saturated colors) at $|Y| \gtrsim 15 \,\mathrm{R_E}$, where averaged values are $n_i \sim 10 - 100 \,\mathrm{cm^{-3}}$, 313 $\sigma_B \sim 1-5\,\mathrm{nT}$, and $T_e \sim 0.01-0.1\,\mathrm{keV}$. In contrast, plasma parameters in the inner mag-314 netotail are generally 1–2 orders of magnitude smaller, where $n_i \sim 0.1$ –1 cm⁻³, $\sigma_B \sim 0.1$ – 315 $0.5\,\mathrm{nT}$, and $T_e \sim 1\,\mathrm{keV}$. Fig. 2 shows that in general, background plasma parameters such 316 as the density, temperature, and magnetic field fluctuations are distinctive between the 317 inner and outer magnetotail. Thus, we can use these differences to statistically exclude 318 regions more likely associated with the solar wind or flank-side boundary layers. 319

OMNI solar wind observations during MMS magnetotail seasons indicate average 320 IMF $B_z \sim 0$ and total pressure $P_{\rm sw} \sim 1-5$ nPa. We use these parameters to construct 321 an asymmetric magnetopause model (Lin et al., 2010), plotted as dashed $(P_{sw} = 5 \text{ nPa})$ 322 and solid $(P_{sw} = 20 \text{ nPa})$ lime curves in (b–d). Details about the average OMNI obser-323 vations and the Lin10 model are provided in Appendix B. The dashed curve agrees well 324 with the change in plasma parameters. Thus, to be conservative when eliminating bound-325 ary layers, we define the inner magnetotail as the region bounded by the solid lime curve. 326 In subsequent sections, all statistical results are obtained with data located strictly within 327 this region. 328

For comparison, previous statistical studies have typically constrained the inner magnetotail region either with (i) $|Y| \leq |X|$ (Ergun et al., 2015) or (ii) with a threshold $|Y| \leq Y_0$ (Boakes et al., 2014; Chong et al., 2022). These two constraints are plotted as dashed black lines in (b–d). On a closer look, they are all somewhat equivalent conditions. (i) tends to work for smaller radial distances $R \leq 12 R_E$, and (ii) is good for small enough threshold Y_0 , although the popular choice $Y_0 = 15 R_E$ may include some mixed plasma data.

336

4.2 Identification of inner tail plasma environments

Fig. 3 shows the statistical profile of background plasma parameters in terms of the ion beta $\beta_i = P_i/(B^2/2\mu_0)$, where P_i is the ion pressure. For comparison, it is plotted in the same format as Figure 1 in B14. (a) and (b) show the current density components parallel (J_{\parallel}) and perpendicular (J_{\perp}) to the background magnetic field. (c) shows the electron density n_e , and (d) shows the equatorial magnetic field B_{xy} . Due to the solenoidal condition $(\nabla \cdot \mathbf{B} = 0)$, the noise level of the curlometer currents in (a-b) can

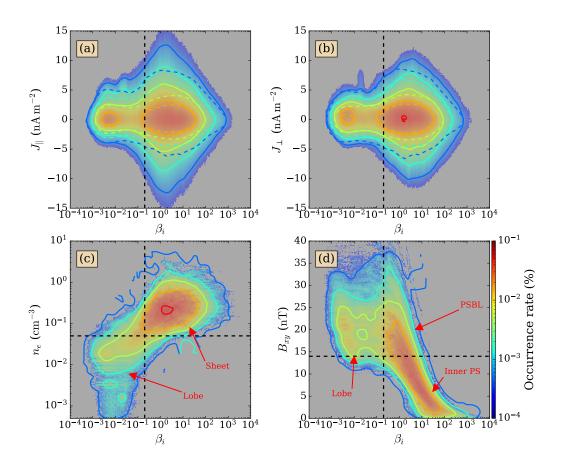


Figure 3. Occurrence rates of (a) the parallel current density J_{\parallel} , (b) the perpendicular current density J_{\perp} (in the cross-tail direction, $\hat{\mathbf{z}} \times \mathbf{B}$), (c) the electron density n_e , and (d) the equatorial magnetic field B_{xy} in terms of the ion plasma beta β_i . Solid lines are contours of the colored distributions. In (a) and (b), the overplotted colored dashed lines are contours of the noise estimation of the curlometer current, $\nabla \cdot \mathbf{B}/\mu_0$. In all panels, the vertical dashed line denotes $\beta_i = 0.2$. In (c), the horizontal dashed line is the FPI 1-count level $n_e = 0.05 \text{ cm}^{-3}$. In (d), the horizontal dashed line denotes $B_{xy} = 14 \text{ nT}$.

Plasma environment	Condition
Lobe	$\beta_i < 0.2$
Plasma sheet	$\beta_i \geq 0.2~\&~B_{xy} \leq 14\mathrm{nT}$
Plasma sheet boundary layer	$\beta_i \geq 0.2 ~\&~ B_{xy} > 14\mathrm{nT}$

Table 1. Threshold conditions distinguishing tail plasma environments derived from Fig. 3.

³⁴³ be estimated as $J_{\text{noise}} = \nabla \cdot \mathbf{B}/\mu_0$. In these panels, we have overplotted the contours of ³⁴⁴ J_{noise} for comparison with the current amplitude. At a given color, currents larger than ³⁴⁵ noise are measured if the solid line is wider than the dashed line.

In general, the features in this plot are consistent with the Cluster study. Most clearly 346 in all panels, there are two distinct populations separated by β_i . The lobe-like popula-347 tion has low density $(n_e \sim 0.01 \,\mathrm{cm}^{-3})$, low beta $(\beta_i \sim 0.01)$, and high equatorial mag-348 netic field $(B_{xy} \sim 20 \,\mathrm{nT})$. In contrast, the plasma sheet-like population has high den-349 sity $(n_e \sim 0.1 \,\mathrm{cm}^{-3})$, high beta $(\beta_i \sim 1)$, and low field $(B_{xy} \sim 5 \,\mathrm{nT})$. One note of cau-350 tion is the region of low electron density. The FPI instrument has a large uncertainty 351 if the electron density is below $0.05 \,\mathrm{cm}^{-3}$ [horizontal dashed line in (c)]. However, noise 352 and background in the combined FPI-FEEPS distribution function has been treated care-353 fully in the low-density region such that the accuracy is improved (see Appendix A for 354 details). In subsequent sections, the threshold conditions for the plasma sheet are the 355 main subject of study, where the density is typically higher than the FPI threshold. 356

To systematically determine the thresholds, B14 used changes in the current and 357 electron densities with respect to β_i to define the PS/lobe separation and similarly, the 358 statistical spread in B_{xy} to distinguish between the PSBL and the outer/inner regions 359 of the plasma sheet. The threshold conditions were then reported annually. However, 360 we deem it unnecessary for that level of detail in this study. It suffices to define by vi-361 sual inspection the threshold conditions as tabulated in Table 1 and annotated in Fig. 3. 362 We also make no attempt to distinguish the inner PS from the outer PS as done in B14. 363 In general, our thresholds are all consistent with averages from the yearly results in B14. 364 The beta threshold is slightly higher (by a factor of 2), most probably due to the usage 365 of combined plasma moments (only partial moments with energies $\lesssim 40 \,\mathrm{keV}$ were used 366 in the B14 study). 367

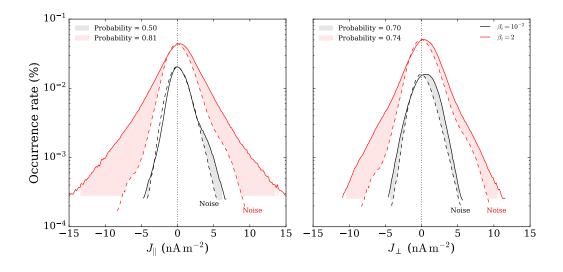


Figure 4. Vertical cuts of the statistical distribution of the currents in Fig. 3(a–b) at $\beta_i = 10^{-2}$ (in black) and $\beta_i = 2$ (in red). The corresponding dashed lines with the same colors are the noise estimation J_{noise} . The shaded areas are those where more occurrence is observed at a given amplitude than the noise estimation. The probability of these observations based on the shown conditional distribution functions (on β_i) is provided in the legends (shaded area versus total area under the solid lines).

In (a) and (b), the average current amplitude in the PS is consistent with results 368 in B14 $(0.5-2 \text{ nA/m}^2)$. However, a difference among our results is in the lobe (low-beta 369 region). B14 only observed noise in this region $(J \sim 0.5 \,\mathrm{nA/m^2})$. But the wider (green/blue) 370 contours than J_{noise} show that there are detections of statistically significant lobe cur-371 rents above the noise level. To better visualize this difference, Fig. 4 shows vertical cuts 372 of these panels at $\beta_i = 10^{-2}$ (black) and $\beta_i = 2$ (red). The occurrence rate of high-beta 373 currents is higher than those with low β_i . The shaded regions indicate that there are "wings" 374 in the probability distribution functions (PDFs) that is more significant than the statis-375 tics of noise (dashed lines). At any occurrence rate below 2×10^{-3} % for low β_i , the de-376 tected current amplitudes are higher than the estimated noise, which means wider con-377 tours in Fig. 3. Finally, to show the partition between noise-level currents (in the "core" 378 of the PDFs) and non-noise currents (in the wings), we calculate the probability of the 379 latter (see the figure legends) and discover that at least half of the observations are not 380 noise. That said, the low overall occurrence rate indicates that their detection is not com-381 mon. 382

In the magnetotail, the typical Cluster spacecraft separation is 1000s of km (Escoubet 383 et al., 2001), which is comparable to the average ion inertial length. About $\sqrt{m_i/m_e} \sim 40$ 384 times smaller, the typical electron inertial length is $\sim 20 \,\mathrm{km}$. Since the target of MMS 385 is electron physics, 97% of the dataset has spacecraft separation $\leq 70 \,\mathrm{km}$ (not shown). 386 As a result, intense electron-scale currents are resolved in MMS data, but may be un-387 derestimated in Cluster data due to the linear spatial interpolation in the curlometer tech-388 nique (Paschmann & Daly, 1998). Therefore, we hypothesize that the presence of sig-389 nificant lobe currents in our statistics is due to the smaller spacecraft separation. Fu-390 ture studies are necessary to reveal their origin and properties. Overall, these results still 391 provide strong support of Cluster observations from the MMS mission, with an improve-392 ment on current density measurements. 393

³⁹⁴ 5 Global structure of the magnetotail plasma sheet

In this section, we investigate the three-dimensional global structure of the plasma 395 sheet. As mentioned in Section 1, the magnetotail is influenced by processes such as flap-396 ping, twisting, and warping. Therefore, the plasma sheet may be highly deformed on mesoscales. 397 In that case, it is interesting to study the spatial variations of the background plasma 398 conditions, based on which the PS threshold condition is established in Table 1. From 399 solar wind observations in Appendix B, the average IMF B_y is around 2 nT with near-400 zero IMF B_z , suggesting that the twisting angle should not be significant for radial dis-401 tances smaller than $30 \, \text{R}_{\text{E}}$ (Tsyganenko & Fairfield, 2004), which leaves flapping and warp-402 ing as the main deforming factors during MMS magnetotail seasons. 403

To investigate the warping of the magnetotail plasma sheet, we consider the Earth's 404 dipole tilt angle Ψ obtained from the MMS Magnetic Ephemerides Coordinates (MEC) 405 dataset generated by Henderson et al. (2018). In GSM coordinates, Ψ , constrained in 406 the X-Z plane, is the angle between the Earth's dipole tilt axis and the Z axis, which 407 is positive when the Earth tilts toward the Sun and negative away from the Sun. Due 408 to the daily Earth rotation, Ψ varies almost sinusoidally with an amplitude of about 10° 409 and a period of about 1 day (not shown). Fig. 5 shows the distribution of Ψ with respect 410 to (a) the time of year and (b) the concurrent MMS spacecraft position in Y. 411

In (a), there are two peaks separated by $\sim 20^{\circ}$ due to the daily variation of Ψ and the seasonal variation of the dipole tilt (Ψ is lower in October). The daily variation is

-17-

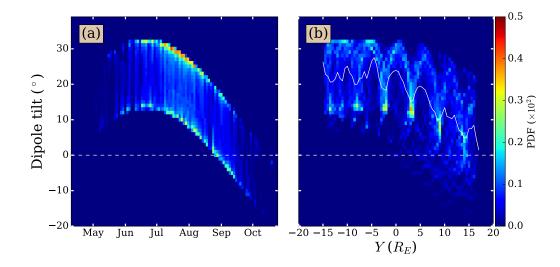


Figure 5. Distribution of the dipole tilt angle Ψ (a) in time and (b) in Y. The average Ψ is plotted as the solid white line in (b).

also seen in panel (b). However, (b) also shows that Ψ is lower at higher Y. The cor-414 relation between Ψ and Y is due to low natural precession of the MMS orbit, which causes 415 MMS to visit the magnetotail only in the summer months. In these seasons, MMS en-416 ters the magnetotail from the dawn-side flank $(Y \sim -15 \,\mathrm{R_E})$ around May when Ψ is high 417 and exits to the dusk-side flank $(Y \sim 15 R_E)$ around October when Ψ is low. The solid 418 white line in (b) shows the average value of Ψ in terms of Y, which is around 20° in the 419 dawn sector (Y < 0) and gradually decreases to zero in the dusk sector (Y > 0). The dif-420 ference in average Ψ between these two sectors can lead to significant variations as a func-421 tion of Y due to dipole tilt warping effects. 422

⁴²³ Using the same bin size as that in Fig. 2 (0.5 R_E), Fig. 6 shows the (Y averaged) ⁴²⁴ spatial structure of (a) the ion plasma beta β_i , (b) the equatorial magnetic field B_{xy} , and ⁴²⁵ (c) the normal electric field E_z . Similarly, Fig. 7 shows the (X averaged) spatial struc-⁴²⁶ ture of (a) B_x and (b) Ψ . The structures of these parameters altogether provide a 3D ⁴²⁷ picture of the plasma sheet, with the tilt angle Ψ indicating the degree of warping.

In Fig. 6 from (a) to (c), the bins are marked with a dot if they satisfy the beta condition, the magnetic field condition, and both (the plasma sheet condition in Table 1), respectively. The features in this figure correspond one-to-one with those discussed in Table 1. First, in Fig. 6(a), while constraining β_i to high values mostly excludes envi-

-18-

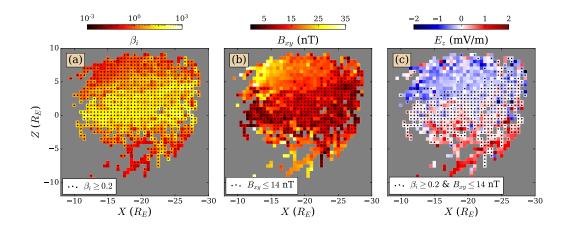


Figure 6. Spatial distribution in the X-Z plane of (a) β_i , (b) B_{xy} , and (c) E_z . In (a), marked bins (those with a circle marker at the center) satisfy the PS beta condition $\beta_i \ge 0.2$ in Table 1. Similarly, the marked bins satisfy the PS field condition $B_{xy} \le 14 \text{ nT}$ in (b). Those in (c) satisfy both, the full PS condition.

ronments consistent with the lobe, the PSBL and PS can extend widely in Z. So the beta 432 condition does not reveal much about the spatial extent. In Fig. 6(b), the magnetic field 433 condition excludes the PSBL regions, leaving the remaining PS, which is more narrow 434 along Z = 0. In Fig. 6(c), the normal electric field E_z that supports the cross-tail drift 435 current $J_y \propto -E_z B_x$ also roughly follows this spatial structure. This electric field always 436 points towards the inner PS (negative/positive in the northern/southern lobe) and tends 437 to zero at the NS. This plot shows that the PS threshold condition agrees with the spa-438 tial structure of the PS, as drawn out by the normal electric field (E_z) and equatorial 439 magnetic field (B_{xy}) . 440

The spatial extent of E_z in the Z direction seemingly flares up to $\sim 8-10 \,\mathrm{R_E}$ be-441 yond $|X| \gtrsim 20 \,\mathrm{R_E}$, while at closer distances, its structure is mainly located within $5 \,\mathrm{R_E}$ 442 of the equator. This flaring in the Z direction of the plasma sheet can be explained with 443 variations in the Y direction caused by the dipole tilt. In Fig. 7(a), the two lobes are clearly 444 distinguishable, with $B_x > 0$ indicating the northern hemisphere and $B_x < 0$ indicating 445 the southern hemisphere. The null point $B_x \sim 0$ is the location of the neutral sheet. In 446 (b), the distribution of Ψ also reflects the aforementioned dawn-dusk asymmetry in Fig. 5, 447 where Ψ varies between 10° and 30° in the dawn sector (Y < 0) and between -10° and 448 10° in the dusk sector (Y > 0). 449

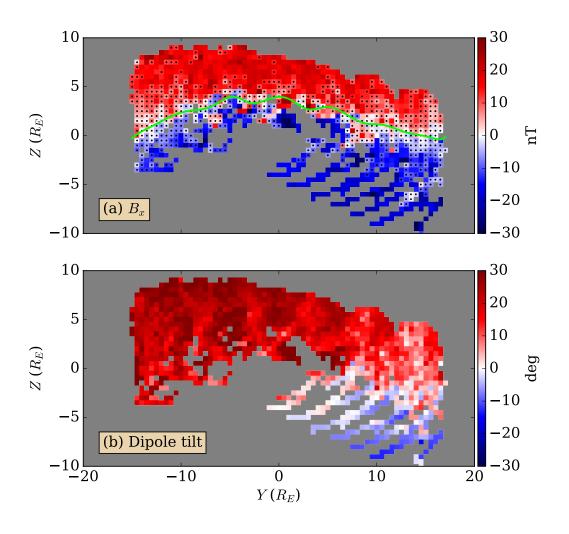


Figure 7. Spatial distribution in the Y-Z plane of (a) B_x and (b) the dipole tilt angle Ψ . The solid lime line in (a) is a global tail neutral sheet model (Xiao et al., 2016) dependent on Ψ and the average solar wind pressure $P_{sw} = 2 nPa$. Similar to Fig. 6(c), the marked bins satisfy the plasma sheet condition (plotted in the same format).

Bins marked with a dot in Fig. 7(a) indicate the region satisfying the PS condi-450 tion in Table 1. The reversal of B_x shows that the neutral sheet is located within the 451 marked plasma sheet. The lime curve is a global NS model from Xiao et al. (2016), de-452 pendent on the dipole tilt angle and the solar wind pressure (see Appendix B). We use 453 the average value of Ψ obtained from Fig. 5(b) (solid white line) for the former, and av-454 erage OMNI observations $P_{sw} = 2 nPa$ for the latter. The small variations in this model 455 are highly dependent on those in Ψ , which in turn is affected by the spacecraft apogee. 456 However, its average shows a remarkable agreement with the B_x reversal. 457

In Fig. 7(b), the high values of Ψ in the dawn sector causes the magnetotail to be 458 warped to $\sim 2-4 R_E$ in Z, while in the dusk sector, there is little warping. The combi-459 nation of warping in the dusk sector with no warping in the dawn sector contributes to 460 the apparent flaring in X-Z seen in Fig. 6, as the Y direction is averaged in that figure. 461 The plasma sheet extent around the neutral sheet in Fig. 7(a) seems to increase towards 462 the flanks ($\sim 2-3 R_{\rm E}$). This increase may be explained by kink-like flapping waves that 463 are commonly observed in these regions (Gao et al., 2018). As the magnetic field con-464 dition is more strictly constrained to lower threshold, the outer PS is excluded and will 465 result in a spatial distribution that follow the NS more closely. 466

⁴⁶⁷ 6 Discussions and Conclusions

In summary, using a large volume of MMS data with combined plasma moments 468 from the low-energy plasma and energetic particle instruments, we have investigated the 469 background plasma conditions and the 3D spatial structure of the magnetotail plasma 470 sheet using the threshold, imaging, and modeling approaches. Consequently, we have sta-471 tistically distinguished inner-magnetotail environments corresponding to the plasma sheet, 472 plasma sheet boundary layers, and lobes. We find that these methods are in good agree-473 ments, showing that the neutral sheet is embedded within a thick region of the plasma 474 sheet, and they are both highly warped in the dawn sector and less deformed in the dusk 475 sector. 476

This asymmetry is attributed to changes in the dipole tilt angle as the Earth orbits the Sun (see Figs. 5 and 7). But this observation is, in part, also specific to MMS, since the mission always visits the magnetotail in the summer months due to its orbital design. Fig. 8 provides a schematic of the Earth's magnetospheric configurations dur-

-21-

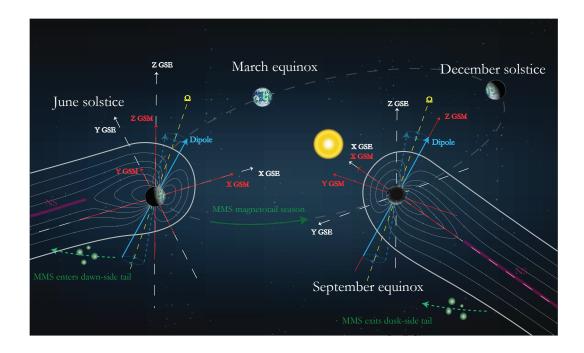


Figure 8. Schematic of Earth's magnetospheric configurations during an MMS magnetotail season. The Earth's rotational axis (Ω , dashed yellow) is constant. The magnetic dipole moment (solid blue arrow) rotates around this axis once a day, warping the magnetotail up and down in Z GSM. Around June solstice, MMS (green dots) enters the magnetotail from the dawn side. During this period, GSM (red) coincides with GSE (white) coordinates whenever the moment lies in the XZ plane. The tilt angle is large, resulting in a highly warped magnetotail in the positive Z direction. Towards September equinox, MMS exits the magnetotail from the dusk side. During this period, whenever the moment lies in the YZ plane, the Z axis of GSM coordinate is parallel with the dipole moment. The small tilt angle results in a relaxed magnetotail.

ing these periods. As MMS enters the magnetotail from the dawn-side flank around June solstice, the Earth's dipole on average tilts around 20° towards the Sun, resulting in a highly warped neutral sheet at $Z \sim 2-4 R_E$ [see Fig. 7(a)]. But when it exits the magnetotail from the dusk-side flank around September equinox, the average tilt angle is zero, leading to a less deformed and displaced neutral sheet.

While we have demonstrated that the deformation of the magnetotail mainly comes from warping, there remains flaring effects due to kink-like flapping waves or IMF twisting near the flanks that are not discussed in details in this paper. Future studies may need to consider smaller-scale evolution and utilize timing analysis to investigate properties of the flapping in further details. However, the insights about the plasma sheet

-22-

spatial variations reported in this paper will be useful for future MMS magnetotail stud-

491 492

ies when considering its configuration and the state of the plasma sheet.

The threshold conditions in Fig. 3 and Table 1 are also in good agreement with a 493 previous Cluster study (Boakes et al., 2014). The average current amplitude in the PS 494 agrees with Cluster observations. However, lobe currents with amplitude comparable to 495 those in the PS are also detected, albeit their occurrence rate is lower [Fig. 3(a-b), Fig. 4]. 496 One interpretation of their presence is that thin electron-scale currents are resolved in 497 the curlometer calculation due to MMS mission design with smaller average spacecraft 498 separation in the magnetotail (Paschmann & Daly, 1998; Dunlop et al., 2021). While small-499 scale current systems have been observed with Cluster via the particle distribution func-500 tion (Teste et al., 2007), its larger average separation inherently leads to underestima-501 tion of electron-scale currents via the curlometer technique. Finally, the ion plasma beta 502 condition is slightly higher (by a factor of 2), probably due to the additional contribu-503 tion of energetic $(60-500 \,\mathrm{keV})$ ions to the total pressure. However, the threshold is still 504 on the same order as that reported by B14, so our results are still consistent. Neverthe-505 less, this might also be a demonstration that the combined plasma moments (discussed 506 in Fig. 1) are important for studies of the magnetotail, especially those involving ion prop-507 erties. While the difference in large statistical averages is small, that on a case-by-case 508 basis might be significant. Finally, the region of interest (inner magnetotail) is more me-509 thodically defined, well-separated from solar wind data and mixed plasma regions near 510 the flank-side boundary layers. 511

To perform the statistical analysis in this paper, we utilize around 316 continuous 512 days of magnetotail observations by MMS (about 400 million field measurements and 513 6 million particle measurements), with data from a broad array of field and particle in-514 struments. The dataset compiled in this study is useful not only for studying background 515 plasma properties, but also for kinetic-scale dynamical evolution. Particularly, the in-516 tervals in our data contain continuous high-quality electric field measurements from EDP 517 of at least 1 minute. Combined with accurate spatial gradient calculations, spectral anal-518 ysis, and particle measurements, this enables future statistical studies of field fluctua-519 tions, particle energization, and their correlation. Further investigations of this data will 520 reveal insights in the frequency of events such as the one in Fig. 1, and the properties 521 and spatial variations of plasma turbulence and reconnection in the inner magnetotail. 522

-23-

523 Availability Statement

The MMS dataset, including ephemerides MEC data, is publicly available at the MMS Science Data Center (https://lasp.colorado.edu/mms/sdc/public/). Data are analyzed using the SPEDAS software package (http://spedas.org/blog/). All figures are generated with matplotlib, a Python visualization package (https://matplotlib.org/).

528 Acknowledgments

This work is supported by NASA'S MMS (NNG04EB99C) mission. The authors thank the entire MMS team for their work on the mission. Specifically, they thank B. Mauk, B. Giles, and A. Narges for helpful conversations about the EPD, FPI, and EDP instruments and data products, S. Schwartz for suggesting the number-energy flux conversion table in the ISSI/ESA report, and P. Reiff for helpful comments on the sketch in Figure 8.

⁵³⁵ Appendix A FPI-FEEPS combined plasma moments

In this section, we describe the technical details pertaining to the combined FPI 536 and FEEPS moment calculations. Since the data products for the distribution function 537 from each instrument and their limitations are different, their combination is non-trivial. 538 Every instrument is constrained within a certain energy range. So the derived plasma 539 moments from the distribution function are only partial contributions. However, the main 540 moments of interest for this study, the number density and scalar pressure, are additive 541 scalars. So it is possible to sum the low- and high-energy contributions to get a total par-542 tial plasma moments. In the following, "low-energy" refers to the FPI measurements, while 543 "high-energy" contains both the FEEPS measurements and the extrapolated energy-coverage 544 gap between the two instruments. 545

At the low energy range, the FPI instrument provides a 3D distribution function $f(E, \varphi, \theta)$ in spherical coordinates with the energy $E = (1/2)mv^2$ measured at 32 different channels from 6.32 eV to 27.5 keV for electrons and from 2.16 eV to 28.3 keV for ions (Pollock et al., 2016). *m* is the mass of the particle species. Averaged over a solid angle $d\Omega = d(\cos \theta) d\varphi$, the differential energy flux, defined as (Larsen et al., 2022)

-24-

	Start	Stop
1	2017-07-04/04:50	2017-07-04/05:20
2	2017-07-07/02:30	2017-07-07/03:20
3	2017-07-10/07:20	2017-07-10/09:20
4	2017-07-13/09:30	2017-07-13/10:10
5	2017-07-15/15:20	2017-07-15/16:40

Table A1. Periods of lobe observations used for background estimation.

$$\frac{d\mathcal{F}}{dE} = \frac{v^4}{2} \frac{\int d\Omega f(E,\varphi,\theta)}{\int d\Omega},\tag{A1}$$

is solely a function of energy, provided in the FPI data products as an energy-angle spec-551 trogram. While FPI also provides partial moments calculated from the full 3D distri-552 bution function (which undergoes multiple conditioning and processing steps by default 553 for integration such as spin-tone correction, penetrating radiation removal, etc, while the 554 energy flux does not), those moments are not reliable when there is significant cold ($\sim 10-100 \, \text{eV}$) 555 plasma contribution. In particular, the ion energy flux can be contaminated with back-556 ground radiation (energetic electrons) up to keV energies, and the electron distribution 557 is often contaminated with photoelectrons due to spacecraft charging effects (up to $\sim 100 \,\mathrm{eV}$). 558 Thus, as a rule of thumb, caution to the plasma moments is needed when the density 559 is below $0.05 \,\mathrm{cm}^3$. 560

To push the limits of FPI in our combined moments calculation, we apply the usual 561 processing steps to the omni-directional energy flux with an addition of a background 562 removal. Fig. A1 shows the average energy fluxes of ions and electrons during 5 nom-563 inally quiet lobe periods in July 2017 (selected by eyes, see Table A1). In (a), the ion 564 distribution shows two constant background populations for the FPI and FEEPS energy 565 ranges, respectively. In (b), there are a cold photoelectron background up to about 1 keV, 566 and a variable population throughout the remaining FPI range. In our dataset, we re-567 move these populations using the displayed step functions (solid black). The resulting 568 omni-directional energy flux is used in conjunction with FEEPS data to calculate a com-569 bined spectrum, as shown in Fig. 1(d–e). 570

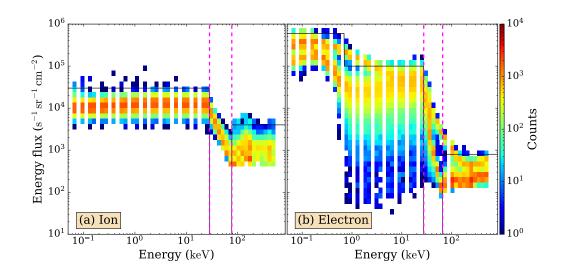


Figure A1. Average values of the (a) ion and (b) electron energy fluxes during nominal lobe periods. The step functions (in black) are used to remove background populations in the data used in this study.

At the high energy range, the FEEPS instrument provides a coarse instantaneous all-sky view of electrons and ions, whose angular coverage can be refined by means of rotation (Blake et al., 2016; Mauk et al., 2016). While the design of the field-of-view is different for each particle species, the all-sky measurements can be combined into an omnidirectional number flux spectrogram, which is related to the energy flux (see Table D.2 of Wüest et al., 2007) by

$$\frac{d\mathcal{N}}{dE} = \frac{1}{E} \frac{d\mathcal{F}}{dE},\tag{A2}$$

with E measured from 33.2 keV to 509.2 keV for electrons and from 57.9 keV to 558.6 keV for ions. The lowest-energy channel in FEEPS is excluded due to noise. In Fig. 1(d–e), the FEEPS number flux has been converted to energy flux with Eq. (A2) in the combined spectrogram. Five data points are linearly extrapolated to cover the energy gap between the two instruments. While a linear extrapolation might not be adequate to estimate the missing data in the gap, we note that this method of extrapolation does not add false data and only underestimate the contribution of missing data in the gap.

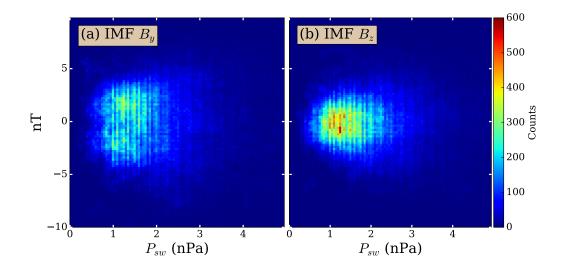


Figure B1. Distribution of (a) the IMF B_y and (b) the IMF B_z with respect to total (dynamical and magnetic) solar wind pressure during MMS magnetotail observations.

It is reasonable to assume that the bulk flow rarely surpasses the FPI energy range. Therefore, the omni-directional, high-energy contribution to the partial number density and scalar pressure can be integrated as (see also Mauk et al., 2004)

$$n_{\rm hi} = 4\pi \sqrt{\frac{m}{2}} \int \left(\sqrt{E}dE\right) \left(\frac{1}{E}\frac{d\mathcal{N}}{dE}\right), \quad \text{and} \quad P_{\rm hi} = 4\pi \sqrt{\frac{m}{2}} \int \left(\sqrt{E}dE\right) \frac{d\mathcal{N}}{dE}, \quad (A3)$$

where $\sqrt{E}dE \sim v^2 dv$ and from Eqs. (A1) and (A2), $(1/E)d\mathcal{N}/dE \sim f$. The energy 587 range in above integrals covers both the extrapolated range and FEEPS range. Finally, 588 the total number density and scalar pressure, shown in Fig. 1(f-g), are $n_{\text{total}} = n_{\text{lo}} +$ 589 $n_{\rm hi}$ and $P_{\rm total} = P_{\rm lo} + P_{\rm hi}$. Potentially, these considerations can also be extended to 590 other quantities such as the isotropic parts of the temperature and the heat flux. In gen-591 eral, the resulting ion and electron densities calculated with the steps as laid out above 592 preserve charge quasi-neutrality very well, even during periods of low FPI density (see 593 Fig. 1f), which provides confidence in the statistical analyses discussed in the main text. 594

Appendix B Solar wind and IMF conditions during MMS magnetotail observations and global magnetospheric models

The OMNI dataset (King & Papitashvili, 2005) provides 1-minute averaged solar wind and interplanetary magnetic field (IMF) conditions. From this dataset, we plot in Fig. B1 the distribution of (a) the IMF B_y and (b) the IMF B_z with respect to the total solar wind pressure (including magnetic field pressure and dynamical pressure) during the magnetotail seasons constrained by the criteria in Section 3. Different from the counting statistics discussed in the main text, each count here represents a 1-min observation. From this figure, B_y averages around 1–2 nT, while B_z averages around zero. The total solar wind pressure averages around 1–2 nPa, with the most extreme pressure around 4–5 nPa.

In this study, two global magnetospheric models are utilized for our analysis of MMS 606 observations. Lin et al. (2010) used a database of magnetopause crossings (observed from 607 1994 to 2008) from Cluster, Geotail, GOES, IMP 8, Interball, LANL, Polar, TC1, and 608 THEMIS, together with solar wind conditions from ACE and Wind to construct an asym-609 metric 3D magnetopause model in aberrated GSM coordinates. This model (see Equa-610 tions (19–20) in their paper) depends on the IMF B_z , the total solar wind pressure, and 611 the Earth's dipole tilt angle Ψ . since the average Ψ changes between the dawn and dusk 612 sectors [see Figs. 5 and 7], we set $\Psi = 0$ and use average values in Fig. B1(b) for the 613 magnetopause shapes in Fig. 2(b-d). The models also need to be tilted 5° clockwise to 614 better fit the changes in background plasma conditions between the solar wind and in-615 ner magnetotail. This rotation is needed due to either the seasonal variations of Ψ , or 616 the usage of GSM coordinates throughout the paper. 617

Xiao et al. (2016) used magnetic field data from Cluster, Geotail, TC-1, and THEMIS 618 from 1995 to 2013 to fit the average shape and position of the magnetotail neutral sheet. 619 Their model (see Equations (4–7) in their paper) is consistent with that in Tsyganenko 620 and Fairfield (2004) and depends on the Y coordinate, the Earth's dipole tilt angle Ψ , 621 and scaling parameters normalized for a downtail distance of $20, R_E$ and solar wind pres-622 sure of 2 nPa. This pressure is typical from OMNI observations in Fig. B1. We use the 623 average value of Ψ in terms of Y from Fig. 5(b) so that this NS model, as shown in Fig. 7(a), 624 is only dependent on the Y coordinate. In our analysis, we have also found little vari-625 ations of the results for different X downtail distance, so the scaling parameters normal-626 ized for $X = -20 \,\mathrm{R_E}$ are reasonable. 627

628 References

Amit, H., & Olson, P. (2008, feb). Geomagnetic dipole tilt changes induced by

-28-

manuscript submitted to JGR: Space Physics

630	core flow. Physics of the Earth and Planetary Interiors, 166(3-4), 226–
631	238. Retrieved from https://linkinghub.elsevier.com/retrieve/pii/
632	S0031920108000253 doi: 10.1016/j.pepi.2008.01.007
633	Angelopoulos, V., Kennel, C. F., Coroniti, F. V., Pellat, R., Kivelson, M. G.,
634	Walker, R. J., Gosling, J. T. (1994). Statistical characteristics of bursty
635	bulk flow events. Journal of Geophysical Research, 99(A11), 21257. Retrieved
636	from http://doi.wiley.com/10.1029/94JA01263 doi: 10.1029/94JA01263
637	Angelopoulos, V., Sibeck, D., Carlson, C. W., McFadden, J. P., Larson, D.,
638	Lin, R. P., Sigwarth, J. (2008, dec). First Results from the THEMIS
639	Mission. Space Science Reviews, 141(1-4), 453–476. Retrieved from
640	http://link.springer.com/10.1007/s11214-008-9378-4 doi: 10.1007/
641	s11214-008-9378-4
642	Artemyev, A., Lu, S., El-Alaoui, M., Lin, Y., Angelopoulos, V., Zhang, X.,
643	Russell, C. (2021, mar). Configuration of the Earth's Magnetotail Cur-
644	rent Sheet. Geophysical Research Letters, 48(6), 1–9. Retrieved from
645	https://onlinelibrary.wiley.com/doi/10.1029/2020GL092153 doi:
646	10.1029/2020GL092153
647	Åsnes, A., Friedel, R. W. H., Lavraud, B., Reeves, G. D., Taylor, M. G. G. T., &
648	Daly, P. (2008, mar). Statistical properties of tail plasma sheet electrons
649	above 40 keV. Journal of Geophysical Research: Space Physics, 113(A3), n/a-
650	n/a. Retrieved from http://doi.wiley.com/10.1029/2007JA012502 doi:
651	10.1029/2007JA012502
652	Baumjohann, W., Paschmann, G., & Cattell, C. A. (1989, jun). Average plasma
653	properties in the central plasma sheet. Journal of Geophysical Research: Space
654	<i>Physics</i> , <i>94</i> (A6), 6597–6606. Retrieved from http://doi.wiley.com/10.1029/
655	JA094iA06p06597 doi: 10.1029/JA094iA06p06597
656	Baumjohann, W., Paschmann, G., Sckopke, N., Cattell, C. A., & Carlson, C. W.
657	(1988). Average ion moments in the plasma sheet boundary layer. Jour-
658	nal of Geophysical Research, 93(A10), 11507. Retrieved from http://
659	doi.wiley.com/10.1029/JA093iA10p11507 doi: 10.1029/JA093iA10p11507
660	Blake, J. B., Mauk, B. H., Baker, D. N., Carranza, P., Clemmons, J. H., Craft,
661	J. V., Westlake, J. (2016, mar). The Fly's Eye Energetic Parti-
662	cle Spectrometer (FEEPS) Sensors for the Magnetospheric Multiscale

-29-

663	(MMS) Mission. Space Science Reviews, 199(1-4), 309–329. Retrieved
664	from http://link.springer.com/10.1007/s11214-015-0163-x doi:
665	10.1007/s11214-015-0163-x
666	Boakes, P. D., Nakamura, R., Volwerk, M., & Milan, S. E. (2014, aug). ECLAT
667	Cluster Spacecraft Magnetotail Plasma Region Identifications (2001–
668	2009). Dataset Papers in Science, 2014, 1–13. Retrieved from https://
669	www.hindawi.com/journals/dpis/2014/684305/ doi: $10.1155/2014/684305$
670	Burch, J., Moore, T. E., Torbert, R. B., & Giles, B. L. (2016, mar). Magnetospheric
671	Multiscale Overview and Science Objectives. Space Science Reviews, 199(1-4),
672	5-21. Retrieved from http://link.springer.com/10.1007/s11214-015-0164
673	-9 doi: 10.1007/s11214-015-0164-9
674	Cattell, C. A., Mozer, F. S., Hones, E. W., Anderson, R. R., & Sharp, R. D. (1986).
675	ISEE observations of the plasma sheet boundary, plasma sheet, and neutral
676	sheet: 1. Electric field, magnetic field, plasma, and ion composition. Journal of
677	Geophysical Research, 91(A5), 5663. Retrieved from http://doi.wiley.com/
678	10.1029/JA091iA05p05663 doi: 10.1029/JA091iA05p05663
679	Chasapis, A., Yang, Y., Matthaeus, W. H., Parashar, T. N., Haggerty, C. C., Burch,
680	J., Russell, C. T. (2018, jul). Energy Conversion and Collisionless Plasma
681	Dissipation Channels in the Turbulent Magnetosheath Observed by the Mag-
682	netospheric Multiscale Mission. The Astrophysical Journal, 862(1), 32. Re-
683	trieved from https://iopscience.iop.org/article/10.3847/1538-4357/
684	aac775 doi: 10.3847/1538-4357/aac775
685	Chen, L., Wang, S., Hesse, M., Ergun, R. E., Moore, T., Giles, B., Lindqvist,
686	P. (2019, jun). Electron Diffusion Regions in Magnetotail Reconnection
687	Under Varying Guide Fields. $Geophysical Research Letters, 46(12), 6230-$
688	6238. Retrieved from https://onlinelibrary.wiley.com/doi/10.1029/
689	2019GL082393 doi: 10.1029/2019GL082393
690	Chong, G. S., Pitkänen, T., Hamrin, M., & Kullen, A. (2022, apr). Dawn-Dusk
691	Ion Flow Asymmetry in the Plasma Sheet: Interplanetary Magnetic
692	Field B y Versus Distance With Respect to the Neutral Sheet. Jour-
693	nal of Geophysical Research: Space Physics, 127(4). Retrieved from
694	https://onlinelibrary.wiley.com/doi/10.1029/2021JA030208 doi:
695	10.1029/2021JA030208

696	Coroniti, F. V., & Kennel, C. F. (1972, jul). Changes in magnetospheric con-
697	figuration during the substorm growth phase. Journal of Geophysical Re-
698	search, 77(19), 3361-3370. Retrieved from http://doi.wiley.com/10.1029/
699	JA077i019p03361 doi: $10.1029/JA077i019p03361$
700	Cowley, S. (1991, jul). The structure and length of tail-associated phenomena in the
701	solar wind downstream from the Earth. $Planetary and Space Science, 39(7),$
702	1039-1043. Retrieved from https://linkinghub.elsevier.com/retrieve/
703	pii/003206339190110V doi: 10.1016/0032-0633(91)90110-V
704	Coxon, J. C., Jackman, C. M., Freeman, M. P., Forsyth, C., & Rae, I. J. (2016, feb).
705	Identifying the magnetotail lobes with Cluster magnetometer data. Journal
706	of Geophysical Research: Space Physics, 121(2), 1436–1446. Retrieved from
707	https://onlinelibrary.wiley.com/doi/abs/10.1002/2015JA022020 doi:
708	10.1002/2015JA022020
709	Dayeh, M. A., Fuselier, S. A., Funsten, H. O., McComas, D. J., Ogasawara, K.,
710	Petrinec, S. M., Valek, P. (2015, apr). Shape of the terrestrial plasma
711	sheet in the near-Earth magnetospheric tail as imaged by the Interstel-
712	lar Boundary Explorer. Geophysical Research Letters, 42(7), 2115–2122.
713	Retrieved from http://doi.wiley.com/10.1002/2015GL063682 doi:
714	10.1002/2015GL063682
715	Dungey, J. W. (1965, apr). The length of the magnetospheric tail. Journal of Geo-
716	physical Research, 70(7), 1753-1753. Retrieved from http://doi.wiley.com/
717	10.1029/JZ070i007p01753 doi: 10.1029/JZ070i007p01753
718	Dunlop, M. W., Dong, X., Wang, T., Eastwood, J. P., Robert, P., Haaland, S.,
719	De Keyser, J. (2021, nov). Curlometer Technique and Applications.
720	Journal of Geophysical Research: Space Physics, 126(11). Retrieved from
721	https://onlinelibrary.wiley.com/doi/10.1029/2021JA029538 doi:
722	10.1029/2021JA029538
723	Eastman, T. E., Frank, L. A., Peterson, W. K., & Lennartsson, W. (1984). The
724	plasma sheet boundary layer. Journal of Geophysical Research, 89(A3), 1553.
725	Retrieved from http://doi.wiley.com/10.1029/JA089iA03p01553 doi: 10
726	.1029/JA089iA03p01553
727	Ergun, R. E., Ahmadi, N., Kromyda, L., Schwartz, S. J., Chasapis, A., Hoilijoki, S.,
728	Giles, B. L. (2020a, aug). Observations of Particle Acceleration in Magnetic

729	Reconnection–driven Turbulence. The Astrophysical Journal, 898(2), 154.
730	Retrieved from https://iopscience.iop.org/article/10.3847/1538-4357/
731	ab9ab6 doi: 10.3847/1538-4357/ab9ab6
732	Ergun, R. E., Ahmadi, N., Kromyda, L., Schwartz, S. J., Chasapis, A., Hoilijoki, S.,
733	Burch, J. (2020b, aug). Particle Acceleration in Strong Turbulence in the
734	Earth's Magnetotail. The Astrophysical Journal, 898(2), 153. Retrieved from
735	https://iopscience.iop.org/article/10.3847/1538-4357/ab9ab5 doi:
736	10.3847/1538-4357/ab9ab5
737	Ergun, R. E., Andersson, L., Tao, J., Angelopoulos, V., Bonnell, J. W., McFadden,
738	J. P., Baumjohann, W. (2009, apr). Observations of Double Layers in
739	Earth's Plasma Sheet. Physical Review Letters, 102(15), 155002. Retrieved
740	from https://link.aps.org/doi/10.1103/PhysRevLett.102.155002 doi:
741	10.1103/PhysRevLett.102.155002
742	Ergun, R. E., Goodrich, K. A., Stawarz, J. E., Andersson, L., & Angelopou-
743	los, V. (2015, mar). Large-amplitude electric fields associated with
744	bursty bulk flow braking in the Earth's plasma sheet. Journal of Geo-
745	physical Research: Space Physics, 120(3), 1832–1844. Retrieved from
745 746	physical Research: Space Physics, 120(3), 1832–1844.Retrieved fromhttps://onlinelibrary.wiley.com/doi/10.1002/2014JA020165doi:
746	https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi:
746 747	https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165
746 747 748	https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriks-
746 747 748 749	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbu-
746 747 748 749 750	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi:
746 747 748 749 750 751	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from
746 747 748 749 750 751 752	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi:
746 747 748 749 750 751 752 753	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi: 10.1002/2018GL076993
746 747 748 749 750 751 752 753 754	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi: 10.1002/2018GL076993 Ergun, R. E., Tucker, S., Westfall, J., Goodrich, K. A., Malaspina, D. M., Summers,
746 747 748 749 750 751 752 753 754 755	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi: 10.1002/2018GL076993 Ergun, R. E., Tucker, S., Westfall, J., Goodrich, K. A., Malaspina, D. M., Summers, D., Cully, C. M. (2016, mar). The Axial Double Probe and Fields Signal Processing for the MMS Mission. <i>Space Science Reviews</i>, 199(1-4), 167–188. Retrieved from http://link.springer.com/10.1007/s11214-014-0115-x
746 747 748 749 750 751 752 753 754 755 756	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi: 10.1002/2018GL076993 Ergun, R. E., Tucker, S., Westfall, J., Goodrich, K. A., Malaspina, D. M., Summers, D., Cully, C. M. (2016, mar). The Axial Double Probe and Fields Signal Processing for the MMS Mission. <i>Space Science Reviews</i>, 199(1-4), 167–188.
746 747 748 749 750 751 752 753 754 755 756 757	 https://onlinelibrary.wiley.com/doi/10.1002/2014JA020165 doi: 10.1002/2014JA020165 Ergun, R. E., Goodrich, K. A., Wilder, F. D., Ahmadi, N., Holmes, J. C., Eriksson, S., Vaivads, A. (2018, apr). Magnetic Reconnection, Turbulence, and Particle Acceleration: Observations in the Earth's Magnetotail. <i>Geophysical Research Letters</i>, 45(8), 3338–3347. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1002/2018GL076993 doi: 10.1002/2018GL076993 Ergun, R. E., Tucker, S., Westfall, J., Goodrich, K. A., Malaspina, D. M., Summers, D., Cully, C. M. (2016, mar). The Axial Double Probe and Fields Signal Processing for the MMS Mission. <i>Space Science Reviews</i>, 199(1-4), 167–188. Retrieved from http://link.springer.com/10.1007/s11214-014-0115-x

Geophysical Research Letters, 49(11).

Radiation Belt.

761

Retrieved from

762	https://onlinelibrary.wiley.com/doi/10.1029/2022GL098113 doi:
763	10.1029/2022GL098113
764	Escoubet, C. P., Fehringer, M., & Goldstein, M. (2001, sep). The Cluster mis-
765	sion: Introduction. Annales Geophysicae, $19(10/12)$, $1197-1200$. Retrieved
766	from https://angeo.copernicus.org/articles/19/1197/2001/ doi:
767	10.5194/angeo-19-1197-2001
768	Fairfield, D. H., Otto, A., Mukai, T., Kokubun, S., Lepping, R. P., Steinberg, J. T.,
769	Yamamoto, T. (2000, sep). Geotail observations of the Kelvin-Helmholtz
770	instability at the equatorial magnetotail boundary for parallel northward
771	fields. Journal of Geophysical Research: Space Physics, 105(A9), 21159–
772	21173. Retrieved from http://doi.wiley.com/10.1029/1999JA000316 doi:
773	10.1029/1999JA000316
774	Fuselier, S. A., Lewis, W. S., Schiff, C., Ergun, R., Burch, J., Petrinec, S. M., &
775	Trattner, K. J. (2016, mar). Magnetospheric Multiscale Science Mission
776	Profile and Operations. Space Science Reviews, 199(1-4), 77–103. Retrieved
777	from https://link.springer.com/10.1007/s11214-014-0087-x doi:
778	10.1007/s11214-014-0087-x
779	Gao, J. W., Rong, Z. J., Cai, Y. H., Lui, A. T. Y., Petrukovich, A. A., Shen, C.,
780	Wan, W. X. (2018, sep). The Distribution of Two Flapping Types
781	of Magnetotail Current Sheet: Implication for the Flapping Mechanism.
782	Journal of Geophysical Research: Space Physics, 123(9), 7413–7423. Re-
783	trieved from http://doi.wiley.com/10.1029/2018JA025695 doi:
784	10.1029/2018JA025695
785	Grigorenko, E. E., Koleva, R., & Sauvaud, JA. (2012, sep). On the problem
786	of Plasma Sheet Boundary Layer identification from plasma moments in
787	Earth's magnetotail. Annales Geophysicae, 30(9), 1331–1343. Retrieved
788	from https://angeo.copernicus.org/articles/30/1331/2012/ doi:
789	10.5194/angeo-30-1331-2012
790	Haaland, S., Kronberg, E. A., Daly, P. W., Fränz, M., Degener, L., Georgescu, E., &
791	Dandouras, I. (2010, aug). Spectral characteristics of protons in the Earth's
792	plasmasheet: statistical results from Cluster CIS and RAPID. Annales Geo-
793	physicae, 28(8), 1483-1498. Retrieved from https://angeo.copernicus.org/
794	articles/28/1483/2010/ doi: 10.5194/angeo-28-1483-2010

795	Hammond, C. M., Kivelson, M. G., & Walker, R. J. (1994). Imaging the effect
796	of dipole tilt on magnetotail boundaries. Journal of Geophysical Research,
797	99(A4), 6079. Retrieved from http://doi.wiley.com/10.1029/93JA01924
798	doi: 10.1029/93JA01924
799	Henderson, M., Morley, S., Niehof, J., & Larsen, B. A. (2018). LANLGeoMag. Zen-
800	odo. Retrieved from https://doi.org/10.5281/zenodo.1195041 doi: 10
801	.5281/zenodo.1195041
802	Hietala, H., Drake, J. F., Phan, T. D., Eastwood, J. P., & McFadden, J. P.
803	(2015, sep). Ion temperature anisotropy across a magnetotail reconnec-
804	tion jet. Geophysical Research Letters, $42(18)$, 7239–7247. Retrieved from
805	https://onlinelibrary.wiley.com/doi/10.1002/2015GL065168 doi:
806	10.1002/2015GL065168
807	Huang, S. Y., Wei, Y. Y., Yuan, Z. G., Jiang, K., Deng, X. H., Xu, S. B., Zhang,
808	Z. H. (2020). Electron Jets in the Terrestrial Magnetotail: A Statistical
809	Overview. The Astrophysical Journal, $896(1)$, 67. doi: $10.3847/1538-4357/$
810	ab8eb0
811	Johnson, J. R., Wing, S., & Delamere, P. A. (2014, nov). Kelvin Helmholtz Instabil-
812	ity in Planetary Magnetospheres. Space Science Reviews, $184(1-4)$, 1–31. Re-
813	trieved from http://link.springer.com/10.1007/s11214-014-0085-z doi:
814	10.1007/s11214-014-0085-z
815	King, J. H., & Papitashvili, N. E. (2005). Solar wind spatial scales in and com-
816	parisons of hourly Wind and ACE plasma and magnetic field data. Jour-
817	nal of Geophysical Research, 110(A2), A02104. Retrieved from http://
818	doi.wiley.com/10.1029/2004JA010649 doi: 10.1029/2004JA010649
819	Larsen, K., Burch, J., Giles, B., Clapsadle, J., Fowler, G., Torbert, R., Pankratz,
820	C. (2022). Magnetospheric Multiscale (MMS) Project - Calibration and Mea-
821	surement Algorithms Document (CMAD) (Tech. Rep. No. October). Retrieved
822	from https://lasp.colorado.edu/mms/sdc/public/
823	Lin, R. L., Zhang, X. X., Liu, S. Q., Wang, Y. L., & Gong, J. C. (2010, apr). A
824	three-dimensional asymmetric magnetopause model. Journal of Geophysical
825	Research: Space Physics, 115(A4). Retrieved from http://doi.wiley.com/
826	10.1029/2009JA014235 doi: 10.1029/2009JA014235
827	Liu, Y., Birn, J., Daughton, W., Hesse, M., & Schindler, K. (2014, dec). On-

-34-

828	set of reconnection in the near magnetotail: PIC simulations. Journal of
829	Geophysical Research: Space Physics, 119(12), 9773–9789. Retrieved from
830	https://onlinelibrary.wiley.com/doi/10.1002/2014JA020492 doi:
831	10.1002/2014JA020492
832	Lui, A. T. Y., Meng, CI., & Akasofu, SI. (1978, apr). Wavy nature of the
833	magnetotail neutral sheet. $Geophysical Research Letters, 5(4), 279-282.$
834	Retrieved from http://doi.wiley.com/10.1029/GL005i004p00279 doi:
835	$10.1029/\mathrm{GL005i004p00279}$
836	Malaspina, D. M., Wygant, J. R., Ergun, R. E., Reeves, G. D., Skoug, R. M., &
837	Larsen, B. A. (2015, jun). Electric field structures and waves at plasma bound-
838	aries in the inner magnetosphere. Journal of Geophysical Research: Space
839	<i>Physics</i> , 120(6), 4246–4263. Retrieved from https://onlinelibrary.wiley
840	.com/doi/10.1002/2015JA021137 doi: 10.1002/2015JA021137
841	Mauk, B. H., Blake, J. B., Baker, D. N., Clemmons, J. H., Reeves, G. D., Spence,
842	H. E., Westlake, J. H. $(2016, mar)$. The Energetic Particle Detector (EPD)
843	Investigation and the Energetic Ion Spectrometer (EIS) for the Magnetospheric
844	Multiscale (MMS) Mission. Space Science Reviews, 199(1-4), 471–514. Re-
845	trieved from http://link.springer.com/10.1007/s11214-014-0055-5 doi:
846	10.1007/s11214-014-0055-5
847	Mauk, B. H., Mitchell, D. G., McEntire, R. W., Paranicas, C. P., Roelof, E. C.,
848	Williams, D. J., & Krimigis, S. M. (2004). Energetic ion characteristics and
849	neutral gas interactions in Jupiter's magnetosphere. Journal of Geophysical
850	Research, 109(A9), A09S12. Retrieved from http://doi.wiley.com/10.1029/
851	2003JA010270 doi: 10.1029/2003JA010270
852	McComas, D. J., Russell, C. T., Elphic, R. C., & Bame, S. J. (1986). The near-
853	Earth cross-tail current sheet: Detailed ISEE 1 and 2 case studies. Journal of
854	Geophysical Research, 91(A4), 4287. Retrieved from http://doi.wiley.com/
855	10.1029/JA091iA04p04287 doi: 10.1029/JA091iA04p04287
856	Nakamura, R., Baumjohann, W., Nagai, T., Fujimoto, M., Mukai, T., Klecker, B.,
857	Bogdanova, Y. (2004) . Flow shear near the boundary of the plasma sheet
858	observed by Cluster and Geotail. $Journal of Geophysical Research, 109(A5),$
859	A05204. Retrieved from http://doi.wiley.com/10.1029/2003JA010174 doi:
860	10.1029/2003JA010174

861	Nykyri, K., Otto, A., Lavraud, B., Mouikis, C., Kistler, L. M., Balogh, A., & Rème,
862	H. (2006, oct). Cluster observations of reconnection due to the Kelvin-
863	Helmholtz instability at the dawnside magnetospheric flank. Annales $Geophys$ -
864	<i>icae</i> , 24(10), 2619-2643. Retrieved from https://angeo.copernicus.org/
865	articles/24/2619/2006/ doi: 10.5194/angeo-24-2619-2006
866	Otto, A., & Fairfield, D. H. (2000, sep). Kelvin-Helmholtz instability at the mag-
867	netotail boundary: MHD simulation and comparison with Geotail observa-
868	tions. Journal of Geophysical Research: Space Physics, 105(A9), 21175–
869	21190. Retrieved from http://doi.wiley.com/10.1029/1999JA000312 doi:
870	10.1029/1999JA000312
871	Owen, C. J., Slavin, J. A., Richardson, I. G., Murphy, N., & Hynds, R. J. (1995).
872	Average motion, structure and orientation of the distant magnetotail de-
873	termined from remote sensing of the edge of the plasma sheet boundary
874	layer with $E > 35$ keV ions. Journal of Geophysical Research, 100(A1),
875	185. Retrieved from http://doi.wiley.com/10.1029/94JA02417 doi:
876	10.1029/94JA02417
877	Paschmann, G., & Daly, P. (1998). Analysis Methods for Multi-Spacecraft Data.
878	Pedersen, A., Cattell, C. A., Fälthammar, CG., Knott, K., Lindqvist, PA.,
879	Manka, R. H., & Mozer, F. S. (1985). Electric fields in the plasma sheet
880	and plasma sheet boundary layer. Journal of Geophysical Research, $90(A2)$,
881	1231. Retrieved from http://doi.wiley.com/10.1029/JA090iA02p01231
882	doi: $10.1029/JA090iA02p01231$
883	Pollock, C., Moore, T., Jacques, A., Burch, J., Gliese, U., Saito, Y., Zeuch, M.
884	(2016, mar). Fast Plasma Investigation for Magnetospheric Multiscale. Space
885	Science Reviews, 199(1-4), 331-406. Retrieved from http://link.springer
886	.com/10.1007/s11214-016-0245-4 doi: 10.1007/s11214-016-0245-4
887	Rong, Z. J., Cai, Y. H., Gao, J. W., Lui, A. T. Y., Shen, C., Petrukovich, A. A.,
888	Wan, W. X. (2018, jul). Cluster Observations of a Dispersive Flapping
889	Event of Magnetotail Current Sheet. Journal of Geophysical Research: Space
890	<i>Physics</i> , 123(7), 5571-5579. Retrieved from http://doi.wiley.com/10.1029/
891	2018JA025196 doi: 10.1029/2018JA025196
892	Runov, A., Angelopoulos, V., Sergeev, V. A., Glassmeier, KH., Auster, U., Mc-
893	Fadden, J., Mann, I. (2009, jan). Global properties of magnetotail current

-36-

894	sheet flapping: THEMIS perspectives. Annales Geophysicae, 27(1), 319–328.
895	Retrieved from https://angeo.copernicus.org/articles/27/319/2009/
896	doi: $10.5194/angeo-27-319-2009$
897	Runov, A., Sergeev, V. A., Baumjohann, W., Nakamura, R., Apatenkov, S., Asano,
898	Y., Rème, H. (2005, jun). Electric current and magnetic field geometry in
899	flapping magnetotail current sheets. Annales Geophysicae, $23(4)$, $1391-1403$.
900	Retrieved from https://angeo.copernicus.org/articles/23/1391/2005/
901	doi: $10.5194/angeo-23-1391-2005$
902	Russell, C. T., Anderson, B. J., Baumjohann, W., Bromund, K. R., Dearborn,
903	D., Fischer, D., Richter, I. (2016, mar). The Magnetospheric Multi-
904	scale Magnetometers. Space Science Reviews, 199(1-4), 189–256. Retrieved
905	from http://link.springer.com/10.1007/s11214-014-0057-3 doi:
906	10.1007/s11214-014-0057-3
907	Russell, C. T., & McPherron, R. L. (1973). The magnetotail and substorms. Space
908	Science Reviews, 15(2-3), 205-266. Retrieved from http://link.springer
909	.com/10.1007/BF00169321 doi: 10.1007/BF00169321
910	Sanny, J., McPherron, R. L., Russell, C. T., Baker, D. N., Pulkkinen, T. I., &
911	Nishida, A. (1994). Growth-phase thinning of the near-Earth current sheet
912	during the CDAW 6 substorm. Journal of Geophysical Research, 99(A4),
913	5805. Retrieved from http://doi.wiley.com/10.1029/93JA03235 doi:
914	10.1029/93JA03235
915	Sergeev, V., Runov, A., Baumjohann, W., Nakamura, R., Zhang, T. L., Volw-
916	erk, M., Klecker, B. (2003, mar). Current sheet flapping motion and
917	structure observed by Cluster. $Geophysical Research Letters, 30(6), 2-$
918	5. Retrieved from http://doi.wiley.com/10.1029/2002GL016500 doi:
919	10.1029/2002GL016500
920	Shukhtina, M. A., Dmitrieva, N. P., & Sergeev, V. A. (2004, mar). Quantitative
921	magnetotail characteristics of different magnetospheric states. $Annales Geo-$
922	physicae, 22(3), 1019-1032. Retrieved from https://angeo.copernicus.org/
923	articles/22/1019/2004/ doi: 10.5194/angeo-22-1019-2004
924	Shustov, P. I., Zhang, X., Pritchett, P. L., Artemyev, A., Angelopoulos, V.,
925	Yushkov, E. V., & Petrukovich, A. A. (2019, jan). Statistical Properties of
926	Sub-Ion Magnetic Holes in the Dipolarized Magnetotail: Formation, Struc-

927	ture, and Dynamics. Journal of Geophysical Research: Space Physics, 124(1),
928	342-359. Retrieved from https://onlinelibrary.wiley.com/doi/10.1029/
929	2018JA025852 doi: 10.1029/2018JA025852
930	Sitnov, M., Birn, J., Ferdousi, B., Gordeev, E., Khotyaintsev, Y., Merkin, V.,
931	Zhou, X. (2019, jun). Explosive Magnetotail Activity. Space Science Re-
932	views, 215(4), 31. Retrieved from http://link.springer.com/10.1007/
933	s11214-019-0599-5 doi: 10.1007/s11214-019-0599-5
934	Sitnov, M., & Schindler, K. (2010, apr). Tearing stability of a multiscale mag-
935	netotail current sheet. $Geophysical Research Letters, 37(8), 1-5.$ Re-
936	trieved from http://doi.wiley.com/10.1029/2010GL042961 doi:
937	10.1029/2010GL042961
938	Tedla, Y. T., Davis, G., & Arocho, R. (2018, may). Magnetospheric Multiscale
939	(MMS) Mission: Surviving Extended Mission Long Eclipse. In 2018 spaceops
940	conference. Reston, Virginia: American Institute of Aeronautics and Astronau-
941	tics. Retrieved from https://arc.aiaa.org/doi/10.2514/6.2018-2389 doi:
942	10.2514/6.2018-2389
943	Teste, A., Fontaine, D., Sauvaud, JA., Maggiolo, R., Canu, P., & Fazaker-
944	ley, A. (2007, May). CLUSTER observations of electron outflowing
945	beams carrying downward currents above the polar cap by northward
946	IMF. Annales Geophysicae, 25(4), 953–969. Retrieved 2023-06-13,
947	from https://angeo.copernicus.org/articles/25/953/2007/ doi:
948	10.5194/angeo-25-953-2007
949	Tong, Y., Vasko, I., Mozer, F. S., Bale, S. D., Roth, I., Artemyev, A., Torbert,
950	R. B. (2018, nov). Simultaneous Multispacecraft Probing of Electron Phase
951	Space Holes. Geophysical Research Letters, 45(21), 11,513–11,519. Retrieved
952	from https://onlinelibrary.wiley.com/doi/10.1029/2018GL079044 doi:
953	10.1029/2018GL079044
954	Torbert, R. B., Russell, C. T., Magnes, W., Ergun, R. E., Lindqvist, PA., LeCon-
955	tel, O., Lappalainen, K. (2016, mar). The FIELDS Instrument Suite on
956	MMS: Scientific Objectives, Measurements, and Data Products. Space Science
957	Reviews, 199(1-4), 105-135. Retrieved from http://link.springer.com/
958	10.1007/s11214-014-0109-8 doi: 10.1007/s11214-014-0109-8
959	Tsyganenko, N. A. (1998, oct). Modeling of twisted/warped magnetospheric

-38-

960	configurations using the general deformation method. Journal of Geo-
961	physical Research: Space Physics, 103(A10), 23551–23563. Retrieved from
962	http://doi.wiley.com/10.1029/98JA02292 doi: 10.1029/98JA02292
963	Tsyganenko, N. A., & Fairfield, D. H. (2004). Global shape of the magnetotail cur-
964	rent sheet as derived from Geotail and Polar data. Journal of Geophysical Re-
965	search, 109(A3), A03218. Retrieved from http://doi.wiley.com/10.1029/
966	2003JA010062 doi: 10.1029/2003JA010062
967	Ukhorskiy, A. Y., Sitnov, M. I., Merkin, V. G., Gkioulidou, M., & Mitchell, D. G.
968	(2017, mar). Ion acceleration at dipolarization fronts in the inner magne-
969	tosphere. Journal of Geophysical Research: Space Physics, 122(3), 3040–
970	3054. Retrieved from https://onlinelibrary.wiley.com/doi/10.1002/
971	2016JA023304 doi: 10.1002/2016JA023304
972	Usanova, M. E., & Ergun, R. E. (2022). Electron Energization by High-Amplitude
973	Turbulent Electric Fields: A Possible Source of the Outer Radiation
974	Belt. Journal of Geophysical Research: Space Physics(2015), 1–16. doi:
975	10.1029/2022ja 030336
976	Wang, G. Q., Zhang, T. L., Wu, M. Y., Schmid, D., Cao, J. B., & Volwerk, M.
977	(2019, jan). Solar Wind Directional Change Triggering Flapping Motions
978	of the Current Sheet: MMS Observations. Geophysical Research Letters,
979	46(1), 64-70. Retrieved from https://onlinelibrary.wiley.com/doi/abs/
980	10.1029/2018GL080023 doi: 10.1029/2018GL080023
981	Wüest, M., Evans, D. S., & von Steiger, R. (2007). Calibration of Particle Instru-
982	ments in Space Physics (M. Wüest, D. S. Evans, & R. von Steiger, Eds.). ESA
983	Publications.
984	Xiao, S., Zhang, T., Ge, Y., Wang, G., Baumjohann, W., & Nakamura, R.
985	(2016, feb). A statistical study on the shape and position of the magne-
986	totail neutral sheet. Annales Geophysicae, 34(2), 303–311. Retrieved
987	from https://angeo.copernicus.org/articles/34/303/2016/ doi:
988	10.5194/angeo-34-303-2016
989	Yang, Y., Matthaeus, W. H., Roy, S., Roytershteyn, V., Parashar, T. N., Bandy-
990	opadhyay, R., & Wan, M. (2022, apr). Pressure–Strain Interaction as the
991	Energy Dissipation Estimate in Collisionless Plasma. The Astrophysical Jour-
992	nal, 929(2), 142. Retrieved from https://iopscience.iop.org/article/

manuscript submitted to JGR: Space Physics

993	10.3847/1538-4357/ac5d3e doi: $10.3847/1538-4357/ac5d3e$
994	Zenitani, S., & Hoshino, M. (2005, jan). Relativistic Particle Acceleration in a
995	Folded Current Sheet. The Astrophysical Journal, 618(2), L111–L114. Re-
996	trieved from https://iopscience.iop.org/article/10.1086/427873 doi:
997	10.1086/427873
998	Zhang, T. L., Nakamura, R., Volwerk, M., Runov, A., Baumjohann, W., Eichel-
999	berger, H. U., Fornacon, KH. (2005, nov). Double Star/Cluster observation
1000	of neutral sheet oscillations on 5 August 2004. Annales Geophysicae, 23(8),
1001	2909-2914. Retrieved from https://angeo.copernicus.org/articles/23/
1002	2909/2005/ doi: 10.5194/angeo-23-2909-2005
1003	Zhou, X., Russell, C. T., Gosling, J. T., & Mitchell, D. G. (1997, jan). Three
1004	spacecraft observations of the geomagnetic tail during moderately disturbed
1005	conditions: Structure and evolution of the current sheet. Journal of Geo-
1006	physical Research: Space Physics, 102(A7), 14415–14424. Retrieved from
1007	https://onlinelibrary.wiley.com/doi/abs/10.1029/97JA00038 doi:
1008	10.1029/97JA00038
1009	Zimbardo, G., Greco, A., Sorriso-Valvo, L., Perri, S., Vörös, Z., Aburjania, G.,
1010	Alexandrova, O. (2010, oct). Magnetic Turbulence in the Geospace
1011	Environment. Space Science Reviews, 156(1-4), 89–134. Retrieved
1012	from http://link.springer.com/10.1007/s11214-010-9692-5 doi:

1013 10.1007/s11214-010-9692-5