MESSENGER Observations of Standing Whistler Waves Upstream of Bow Shock of Mercury

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Abstract

This paper reports on the standing whistler waves upstream of Mercury's quasi-perpendicular bow shock. Using MESSENGER's magnetometer data, 36 wave events were identified during interplanetary coronal mass ejections (ICMEs). These elliptic or circular polarized waves were characterized by: (1) a constant phase with respect to the shock, (2) propagation along the normal direction to the shock surface, and (3) rapid damping over a few wave periods. We inferred the speed of Mercury's bow shock as ~31 km/s and a shock width of 1.76 ion inertial length. These events were observed in 20% of the MESSENGER orbits during ICMEs. We conclude that standing whistler wave generations at Mercury are generic to ICME impacts and the low Alfvén Mach number (MA) collisionless shock, and are not affected by the absolute dimensions of its bow shock. Our results further support the theory that these waves are generated by the current in the shock.

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- 16 Key Points:

1

- We identify 36 Mercury's bow shock crossings with standing whistler waves during
 interplanetary coronal mass ejection intervals.
- The amplitude, polarization, and damping length of the standing whistler waves were
 identified and statistically analyzed.
- These standing whistler waves may be generated by currents in shock, and the shock is not the largest-amplitude circle of the waves.

23 Abstract

This paper reports on the standing whistler waves upstream of Mercury's quasi-perpendicular 24 25 bow shock. Using MESSENGER's magnetometer data, 36 wave events were identified during interplanetary coronal mass ejections (ICMEs). These elliptic or circular polarized waves were 26 characterized by: (1) a constant phase with respect to the shock, (2) propagation along the normal 27 direction to the shock surface, and (3) rapid damping over a few wave periods. We inferred the 28 29 speed of Mercury's bow shock as ~31 km/s and a shock width of 1.76 ion inertial length. These events were observed in 20% of the MESSENGER orbits during ICMEs. We conclude that 30 31 standing whistler wave generations at Mercury are generic to ICME impacts and the low Alfvén Mach number (M_A) collisionless shock, and are not affected by the absolute dimensions of its 32 33 bow shock. Our results further support the theory that these waves are generated by the current in the shock. 34

35 Plain Language Summary

The strength of planetary bow shocks varies with the planet's heliocentric distance from the Sun. 36 37 Studying the bow shocks of other planets is important for extending our understanding of 38 collisionless-shock physics. In the solar system, the bow shocks of Mercury are unique as they are produced by low Mach numbers and low plasma beta solar wind blowing over a small 39 40 magnetized body that is 1–2 orders smaller than Earth. The standing whistler waves upstream of the bow shock of Mercury were determined through statistical analyses. Similar to the 41 observations at Earth, these waves were rapidly damping with a proportion of the wave periods; 42 however, the damping distance at the spacecraft frame was considerably shorter at only a few 43 kilometers upstream in the small-scale bow shock of Mercury. The high occurrence rate of 44 standing whistler waves suggests that Mercury's bow shock is a natural plasma laboratory, which 45 can be used to further investigate low M_A planetary shocks during the upcoming BepiColombo 46 mission. 47

48 **1 Introduction**

Whistler waves are common upstream features of planetary bow shocks and are involved in shock formation and particle interactions (Balogh et al., 2013; Oka et al., 2017; Oka et al., 2019). Two types of whistler waves emitting from shock ramps have been previously identified: propagating and phase standing (Russell et al., 1995). The propagation direction of propagating

whistler waves has a small angle with the magnetic field and they propagate far upstream 53 54 (Russell et al., 2007). They have been widely observed upstream of the bow shock of Earth and are typically called "1 Hz" waves. Furthermore, they are also commonly observed in other 55 planetary shocks, such as those of Mercury, Venus, Mars, and Saturn (Fairfield et al., 1976; 56 Orlowski et al., 1991; Le et al., 2013; Sulaiman et al., 2017; Ruhunusiri et al., 2018). In contrast, 57 phase standing whistler waves are generated when the wave propagation speed equals the 58 component of the solar wind velocity that is normal to the bow shock (Perez et al., 1970). They 59 propagate along the shock-normal direction at a constant phase with respect to the shock ramp 60 and can rapidly damp within a few wave periods. The right-handed wave polarization relative to 61 its average field direction is a key observational feature, when an observer moves upstream to 62 downstream. In contrast, the left-handed wave polarization can be observed when the observer 63 moves in the opposite direction. Standing whistler waves have been rarely observed upstream of 64 the bow shock of the Earth (e.g., Fairfield et al., 1975; Mellott et al., 1984; Farris et al., 1993) as 65 they commonly occur under low M_A conditions, such as during an ICME passage. 66

67 Mercury has a miniature and weak bow shock, which is created by the interaction of low Mach number solar wind and a relatively small planetary magnetosphere in the inner 68 hemisphere. The average bow shock subsolar distance has been determined to be only $\sim 2 R_M$ 69 (radius of Mercury, $1 R_M = 2440 \text{ km}$), which is approximately 1–2 orders smaller than that of the 70 71 Earth (Winslow et al., 2013). The "1 Hz" whistler waves have been commonly observed upstream of the bow shock of Mercury (Fairfield et al., 1976; Le et al., 2013), in which they 72 propagate along the magnetic field and farther upstream (~30000 km). Although phase standing 73 whistler waves have been observed at Mercury, they have not yet been analyzed (Gedalin et al., 74 2022). 75

Due to the nature of close-in orbit, there is higher probability for observing low M_A 76 shocks at Mercury than other planets. The typical MA at Mercury orbit is ~4-6 (Slavin et al., 77 1981). Especially, the M_A can be less than 3 during ICMEs (Liu et al., 2005; Sarantos et al., 78 2009). The ICME impact on Mercury's magnetosphere was first analyzed by Slavin et al. (2014). 79 They showed that Mercury's dayside magnetosphere is highly dynamic and greatly compressed 80 by ICME impacts. The bow shock and magnetopause reconfigurations during the impact of 81 ICMEs deviates greatly from normal conditions (Slavin et al., 2014; Winslow et al., 2015; 82 83 2017), and the dayside magnetosphere may even occasionally disappeared (Slavin et al., 2019;

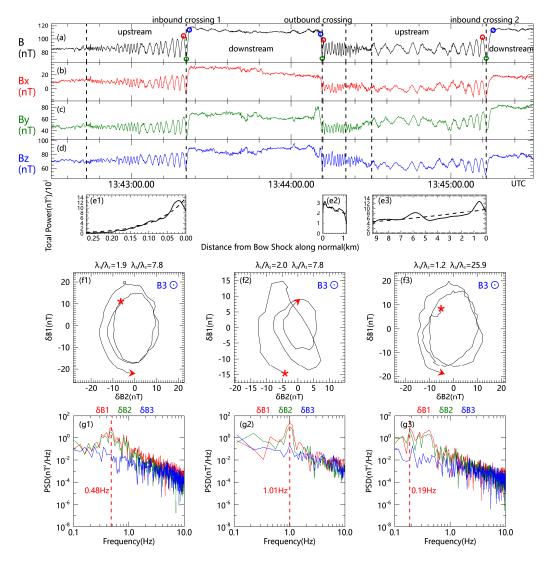
84 Winslow et al., 2020). MESSENGER orbited Mercury during the maximum of solar cycle 24.

Over the four-year mission from February 2011 to April 2015, a total of 69 ICMEs were detected
by MESSENGER (Winslow et al. 2015, 2017). We use the 69 ICMEs to study standing whistler
waves.

88 Here we report the MESSENGER observations of the standing whistler wave upstream 89 Mercury's bow shock during ICMEs collated by Winslow et al. (2015, 2017). Among 69 ICMEs, 89 we identified 36 standing whistler wave events corresponding to at least 20% of the orbits. Our 91 results suggest that Mercury is a natural plasma laboratory for the understand the physics of 92 standing whistler waves and low M_A collisionless shocks. It is likely that our understanding of 93 such low Mach number shocks will be greatly advanced by measurements to be collected by the 94 upcoming Bepi-Colombo mission.

95 2 Case Analysis of Standing Whistler Wave

The dynamics of dayside magnetosphere and magnetotail response to an ICME observed 96 by MESSENGER on November 23, 2011 have been analyzed in detail by Slavin et al. (2014) 97 and Zhong et al. (2020), respectively. This study analyzes its effects on the bow shock. Figures 98 1a-d show an overview of MESSENGER's bow shock crossings during this ICME. High-99 resolution magnetic field data (20 vectors s^{-1}) obtained from the magnetometer (MAG; Anderson 100 et al., 2007) were used and displayed in the aberrated Mercury solar magnetic (MSM) 101 coordinates. The MSM coordinate system was centered on the offset internal dipole of Mercury 102 (Anderson et al., 2011), wherein the X-axis was pointed toward the Sun, the Y-axis was pointed 103 104 in the opposite direction of the orbit motion, and the Z-axis completed the right-handed system. The average radial solar wind speed of 700 km s⁻¹ during the ICME was applied to correct for the 105 aberration. The spacecraft crossed the bow shock thrice; the crossings are denoted as inbound 106 crossing 1, outbound crossing, and inbound crossing 2 in Figure 1. The multiple crossings may 107 be attributed to the temporal variations of the upstream solar wind conditions. 108



109

Figure 1. MESSENGER observations of standing whistler waves upstream of the bow shock of 110 Mercury during the ICME on 23 November 2011. (a)–(d) Magnetic field strength and its three 111 components in the aberrated MSM coordinate system; the red, green, and blue dots correspond to 112 the peak, wave trough, and end of the shock ramp, respectively. (e) Total power as a function of 113 the distance from the bow shock along shock normal. (f)–(g) Magnetic field data of the wave in 114 the maximum-intermediate plane and the power spectral density in the minimum variance 115 analysis (MVA) after removing the background magnetic field. The T_{ramp} refers to the interval 116 time between the blue and green dots. The T_{wave} refers to twice the interval time between the red 117 and green dots. 118

119 The shock normal was determined using the magnetic coplanarity method (Lepping et al.,

120 1971) that substitutes the average magnetic field upstream and downstream of the shock; it is

121 expressed as $\mathbf{n} = \frac{(B_1 \times B_2) \times (B_2 - B_1)}{|(B_1 \times B_2) \times (B_2 - B_1)|}$. The shock normals for the inbound crossing 1, outbound

122 crossing, and inbound crossing 2 were observed to be very close at (0.56, -0.05, -0.82), (0.71, -

- 123 0.02, -0.70), and (0.76, -0.06, -0.65), respectively, and their mean upstream magnetic fields were
- 124 (9.24, 46.57, 72.37), (2.40, 45.41, 71.94), and (1.33, 55.94, 64.86) nT, respectively. The angles
- between the mean upstream magnetic field \mathbf{B}_{up} and the shock normal **n** were $\theta_{Bn} = 49.13^{\circ}$,
- 126 52.23°, and 58.49°, indicating quasi-perpendicular shocks.

The accompanying upstream waves are considered key features of these bow shock 127 crossings. The polarizations and vectors of these waves were obtained from the results of the 128 minimum variance analysis (MVA) of the magnetic field within an upstream wave time interval 129 130 (Sonnerup et al., 1967). Using these, the direction of propagation for an assumed planar wave can be estimated. For inbound crossing 1, the small ratio of the maximum to intermediate 131 eigenvalues $\lambda_1/\lambda_2 = 1.9$ and the large ratio of the intermediate to minimum eigenvalues $\lambda_2/\lambda_3 =$ 132 7.8 suggest that the waves had relatively stable elliptic polarizations. The wave vector **k** 133 corresponds to the minimum variance eigenvector e_3 (0.70, -0.11, -0.69), whereas the 134 corresponding mean magnetic field (\mathbf{B}_0) is directed out of the maximum-intermediate plane. The 135 hodograms of the magnetic field for several wavelengths in the MVA coordinates are shown in 136 137 Figure 1f. The gyration of the magnetic field with respect to B_0 indicates that the wave polarization was right-handed in the spacecraft coordinate frame (SCF). The angles between k 138 139 and **n** (θ_{kn}) and **k** and **B**_{up} (θ_{kB}) were 11.85° and 55.49°, respectively, wherein the small θ_{kn} and large θ_{kB} suggest that the wave propagated approximately along the shock normal direction 140 141 rather than the magnetic field.

The waves observed during the outbound crossing and inbound crossing 2 were also elliptically polarized (Figures 1f2 and f3), with $\theta_{kn} = 23.18^{\circ}$, 2.82° and $\theta_{kB} = 64.17^{\circ}$, 58.14° , respectively. Moreover, the polarization direction of the outbound crossing was opposite to that of the inbound crossing, wherein it was left-handed, which is consistent with the characteristics of standing whistler waves (Fairfield et al., 1975; Mellott et al., 1984).

Wavelet analysis was used to calculate the total power at each moment. Figure 1e shows the variations of the total power along **n** in the SCF. The function $P = P_0 e^{-T/T0}$ was fit to the total power. For inbound crossing 1, the damping time (T₀) was 11.17 s, which was 5.32 times the wave period (T_{wave}), indicating rapid damping. The damping distance was 1.83 km along **k** and the normalized wave amplitude ($\delta B_{wave}/B_u$) was 0.40. This rapid damping of waves was also observed during the outbound crossing and inbound crossing 2. 153 The power spectral density shown in Figure 1e demonstrates that these waves were

mainly restricted to the plane perpendicular to e_3 , as indicated by the PSD₁, and PSD₂ \gg PSD₃

around the wave frequency (f_{sc}) in the SCF. The f_{sc} for the inbound crossing 1, outbound

156 crossing, and inbound crossing 2 were ~0.48, 1.01, and 0.19 Hz, respectively; the different

- values indicate the change in the relative velocity between the spacecraft and bow shock in the
- 158 normal direction.

159 3 Statistical Results and Discussion

160 3.1 Statistical Results

We use 69 ICMEs (94 orbits) collated by Winslow et al. (2015, 2017) to find bow shock 161 crossings during ICMEs. As standing whistler waves typically occur upstream of the quasi-162 perpendicular bow shock, the θ_{Bn} was calculated, wherein 486 quasi-perpendicular bow shock 163 crossings ($\theta_{Bn} > 45^{\circ}$) were identified to select the events. Multiple bow shock crossings are 164 common during inbound or outbound crossings in each orbit owing to the up-and-down 165 displacement of the shocks. MVA was performed on the magnetic field data upstream for each 166 quasi-perpendicular shock crossing under the assumption that the eigenvalues conform to $\lambda_1/\lambda_2 <$ 167 2 and $\lambda_2/\lambda_3 > 7$, which indicate that the waves are elliptically or circularly polarized. In all 168 elliptically polarized waves, 36 perpendicular bow shock crossings with rapid damping were 169 identified, including 20 inbound and 16 outbound crossings. They occurred during 19 orbits, 170 with an orbital occurrence rate of $\sim 20\%$. 171

The characteristics of the wave during each event were observed (Supplement Table 1).A statistical analysis indicated the following:

Wave polarization. Right-handed polarization was observed in 16 of the 20 upstream to
downstream traversals, whereas left-handed polarization was observed in all 16 downstream to
upstream traversals. These polarizations were consistent with the previous theory and
observation of standing whistler waves presented by Perez et al. (1970) and Fairfield et al.
(1975).

179 *Propagation direction.* The calculated θ_{kn} ranged from ~0° to 50°, while the θ_{kB} ranged 180 from ~45° to 90° (Figure 2a). The mean θ_{kn} and θ_{kB} were 17.31° and 69.55°, respectively. These 181 results suggest that the waves were propagating along the shock normal instead of the magnetic 182 field. These results are also consistent with the observations at Earth (Mellott et al., 1984);

183 however, they are different from the propagating direction of "1 Hz" waves observed at Mercury

184 (Fairfield et al., 1976; Le et al., 2013).

Wave damping. Figure 2b shows the distance from the wave damping to e^{-1} to the ramp on the **n** in the SCF, wherein the amplitudes of most waves damp at e^{-1} within 10 km. This was significantly less than the damping distance of the "1 Hz" wave within ~30000 km at Mercury (Le et al., 2013). The ratio of T₀ and T_{wave} was nearly <10 (Figure 2c). The standing whistler waves on Earth also exhibit this rapid damping, which is <10 times the wave periods (Mellott et al., 1984); hence, the damping mechanism can be considered as Landau damping (Gary et al., 1985).

Wave frequency. The mean frequency of standing whistler waves was 1.67 Hz in the
SCF. Here, 70% of the events had a frequency <2 Hz (Figure 2d), suggesting that the standing
whistler waves have a lower frequency than the "1 Hz" waves at Mercury (2–3 Hz, Russell,
2007).

Based on the statistical results of these events, it was discovered that its characteristics were similar with those of the standing whistler wave. Meanwhile, other properties (Figures 2e and f) of the waves are described in detail in the Discussion Section.

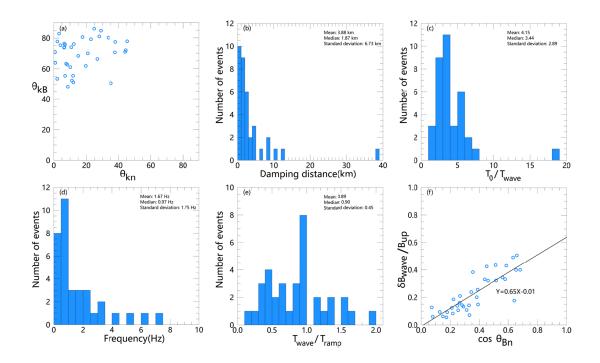
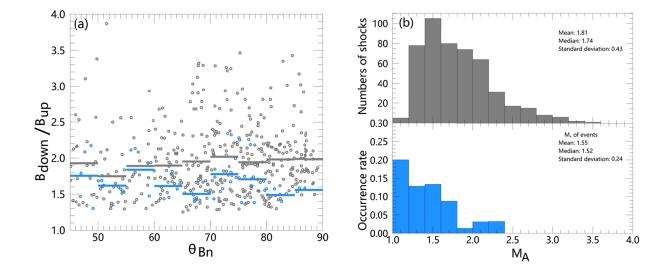
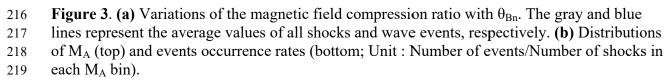


Figure 2. Statistical properties of the standing whistler waves upstream of the bow shock of 200 Mercury. (a) Occurrence of events as functions of θ_{kn} and θ_{kB} . (b)–(e) Distributions of damping 201 distance, T_0/T_{wave} , frequency, and T_{wave}/T_{ramp} . (f) Correlation between θ_{Bn} and $\delta B_{wave}/B_{up}$. 202 Considering that the solar wind beam view of MESSENGER's fast imaging plasma 203 spectrometer was obstructed by the sunshade, the upstream solar wind MA could not deviate 204 directly. The M_A was approximatively estimated using the following formula: $M_A - 1 =$ 205 $(B_{down}/B_{up}-1)\sin^2\theta_{Bn}$, which is suitable for low Mach number and low- β shocks. (Balikhin et 206 al., 2008). The magnetic field compression ratio (B_{down}/B_{up}: magnetic field intensity (average 207 value of $\sim 1 \text{ min}$) ratio of downstream to upstream) of all perpendicular bow shock crossings 208 during ICMEs are plotted in Figure 3a, wherein it can be observed that most of the identified 209 wave events (blue) had lower magnetic field compression ratios than the mean ratio during 210 ICMEs. The distributions of the calculated MA and wave event occurrence rates are plotted in 211 Figure 3b, wherein the occurrence rate can be observed to increase as M_A decreases; 89% of the 212 wave events obtained lower MA values than the average value during ICMEs. Therefore, these 213 waves have a high likelihood of occurrence under a relatively lower Mach number. 214







220 3.2 Discussion

221 On Earth, the theoretical wavelengths of standing whistler waves are consistent with

those observed by Mellott et al. (1984). Hence, single spacecraft observations are normally used

to infer the bow shock speed (Fairfield et al., 1975) based on theoretical predictions of the 223 wavelength (Tidman et al., 1971): $\lambda = \frac{2\pi c \cos \theta_{Bn}}{\omega_{pi} (M_A^2 - 1)^{1/2}}$, where ω_{pi} is the proton plasma frequency. 224 By applying the typical values from the ICME model at 0.38 AU (Liu et al., 2005), $\omega_{pi} =$ 225 10034 rad/s, mean $M_A = 1.55$, and mean $\theta_{Bn} = 68^\circ$ of all wave events, the theoretically 226 predicted wavelength of $\lambda = -59$ km was calculated. The average T_{wave} was -1.89 s; hence, the 227 shock speed (λ/T_{wave}) can be inferred as ~31 km/s. Notably, this was slightly less than the shock 228 speed of ~40 km/s estimated through overshoot observations under normal conditions (Masters 229 et al., 2015). 230

The shock ramp scale was also estimated using the scale relationship between the standing whistler waves and the shock ramps. A shock ramp scale of 53 km was obtained using the formula $\lambda \times T_{ramp}/T_{wave}$ (59 km × 0.89). Considering an ion inertial length (c/ ω_{pi}) of 30 km, the width of the ramp was 1.76 c/ ω_{pi} . Based on the results of Hobara et al. (2010), the scale can be larger than 1 c/ ω_{pi} when M_A is low.

Previous theories have suggested that standing whistler waves are generated by a stable current in the shock ramp, from which the formula for the wave amplitude can be derived (Tidman et al., 1971). This theory suggests that $\delta B_{wave}/B_{up}$ has a positive correlation with $\cos\theta_{BN}$, and this relationship is demonstrated in Figure 2f. The best linear fit produced Y = $[0.65\pm0.15]X$ - $[0.01\pm0.06]$, which was also consistent with this theory. Based on the fitted values, the maximum amplitude of the standing whistler wave was approximately 0.8 times the intensity of the background magnetic field.

The shock is hypothesized to be the largest-amplitude circle of the upstream standing 243 whistler wave, wherein its width is half of the wavelength. However, this results in conflicting 244 ratios of the standing whistler wave wavelength to the shock thickness at Earth and 245 246 interplanetary shock, as some researchers have estimated this ratio to be two (Goncharov et al., 2014) while others have estimated it to be closer to one (Mellott et al., 1984; Farris et al., 1993). 247 In the SCF, the ratio between the period (T_{wave}) of the upstream whistler waves and the shock 248 ramp crossing time (T_{ramp}) can be a good approximation of the shock width to wavelength ratio. 249 250 Figure 2e shows the T_{wave}/T_{ramp} in the spacecraft frame of the upstream standing whistler waves of Mercury. In cases where T_{wave} was less than $2 \times T_{ramp}$, the average ratio of the two was 0.89, 251

indicating that the initial hypothesis must be reexamined to further determine the scale of therelationship between standing whistler waves and shock ramps.

254 **4** Conclusions

In this study, we reported and statistically analyzed the standing whistler waves upstream 255 of the bow shock of Mercury during ICMEs. These waves occur at lower MA and propagate 256 along the normal of the bow shock. It was observed that, similar to the waves at Earth, these 257 waves were rapidly damping with few wave periods; however, the damping distance in SCF was 258 significantly shorter, only a few kilometers upstream of the bow shock of Mercury. Our results 259 support that these waves are generated by the current in the shock and that the shock is not the 260 largest-amplitude circle of the waves. Hence, the generation of standing whistler waves was 261 determined to be generic to the low Mach number collisionless shock. Additionally, a high 262 occurrence rate of the standing whistler waves observed during ICMEs suggests that the bow 263 shock of Mercury can be a natural plasma laboratory that can be used to further study low MA 264 planetary shocks. Considering that BepiColombo will arrive at Mercury in 2025 during the 265 ascending and maximum phases of solar cycle 25, it is expected to encounter a large number of 266 267 ICMEs. This study provides an understanding of standing whistler wave generation and their underlying physics, which can be used for the upcoming high-resolution BepiColombo 268 observations. 269

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- data are available from the Planetary Data System (MAG).

278 Open Research

- 279 The MESSENGER MAG data used in this study are available at NASA's Planetary Data
- 280 System:
- 281 <u>https://pds-ppi.igpp.ucla.edu/search/view/?f=yes&id=pds://PPI/mess-mag-calibrated/data/mso;</u>
- 282 The list of the identified standing whistler wave events is available in the supplemental
- information for the purposes of peer review. The data will eventually be deposited at NSSDC
- 284 Space Science Article Data Repository (https://sadr-en.nssdc.ac.cn) by the time it is accepted.
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Supporting Information for

MESSENGER Observations of Standing Whistler Waves Upstream of Bow Shock of Mercury

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Additional Supporting Information (Files uploaded separately)

- 1. Caption for Tables S1
- 2. Caption for Figure S1

Introduction

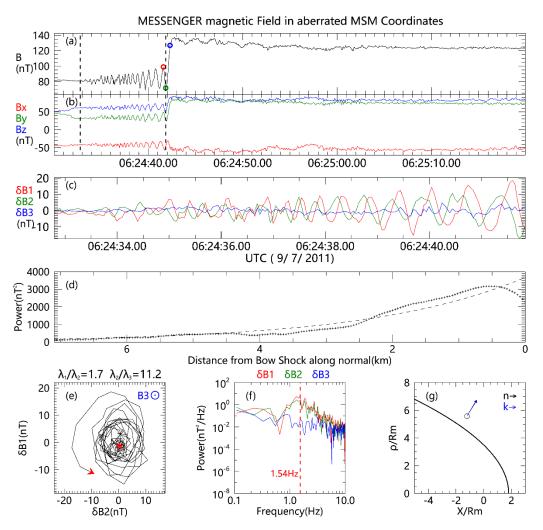
In file Tables S1, we list some parameters of 36 standing whistler waves, and the description of parameters in each column is as follows:

- 1. Column "Event", the serial number of the wave events.
- 2. Column "Start", the start time of the wave events.
- 3. Column "End", the end time of the wave events.
- 4. Column "Obn/°", the angle between upstream magnetic field and shock normal.
- 5. Column "Okn/°", the angle between wave vector and shock normal.
- 6. Column "Okb/°", the angle between wave vector and upstream magnetic field.
- 7. Column "Damping ditance/km", the distance from shock along wave vector when amplitude of waves damp to 1/e in the spacecraft coordinate frame (SCF).
- 8. Column "To/Twave", ratio between the time interval To from shock when amplitude of waves damp to 1/e and wave periods in the SCF.
- 9. Column "Frequency/Hz", the frequency of waves in the SCF.
- 10. Column "δBwave/Bup", relative wave amplitude: ratio of wave amplitude to upstream magnetic field intensity.
- 11. Column "Bdown/Bup", ratio of downstream magnetic field intensity to upstream magnetic field intensity.
- 12. Column "MA", Alfvén Mach number

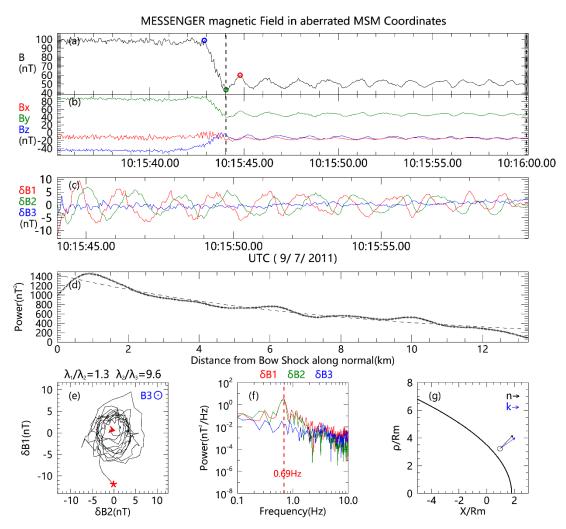
In file Figure S1, we compressed all figure of wave events into this file, and the description of every figure as follows:

- 1. Subgraph "(a)", magnetic field intensity.
- 2. Subgraph "(b)", component of magnetic field in aberrated Mercury solar magnetic (MSM) coordinates.
- 3. Subgraph "(c)", component of the magnetic field of wave after removing the background magnetic field in minimum variance analysis (MVA).
- 4. Subgraph "(d)", the variations of the total power along shock normal in the SCF.
- 5. Subgraph "(e)", magnetic field of the wave in the maximum-intermediate plane after removing the background magnetic field.
- 6. Subgraph "(f)", power spectral density of magnetic field after removing the background magnetic field.
- 7. Subgraph "(g)", location of bow shock in the X- $\rho(\sqrt{Y^2 + Z^2})$ plane .Black curve is best fit conic section from Winslow et al. (2017) . Black arrow is shock normal. Blue arrow is wave vector.

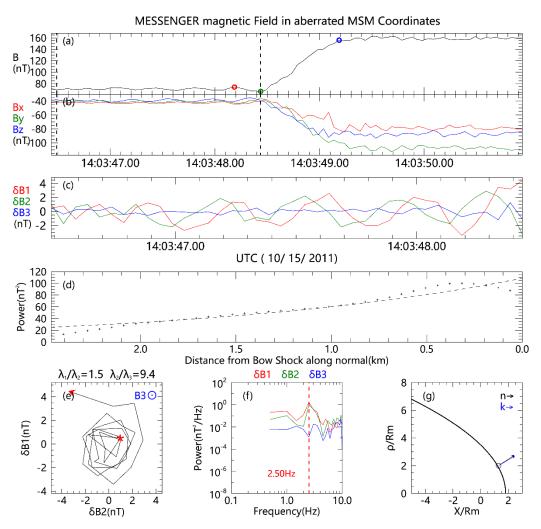
Event 1



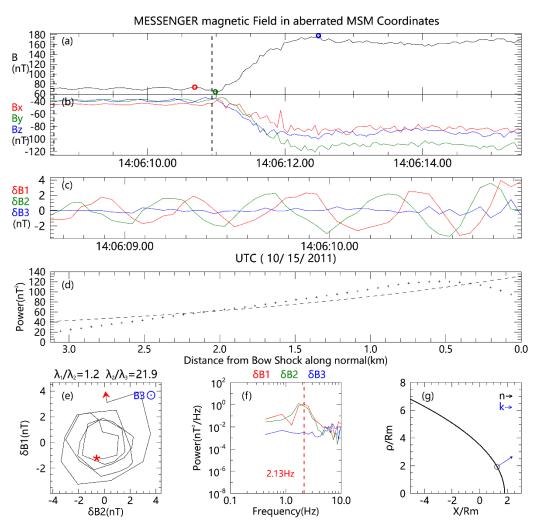




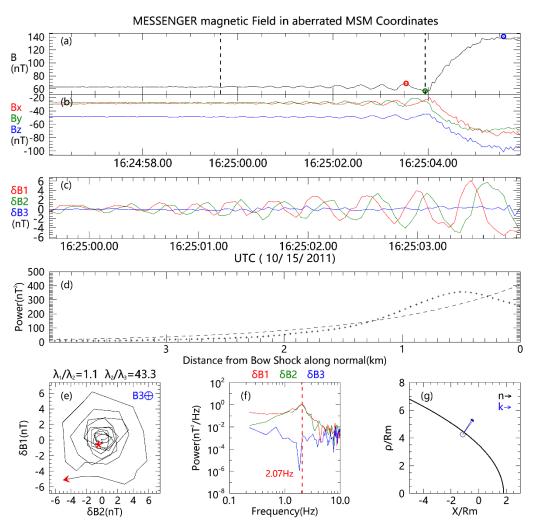




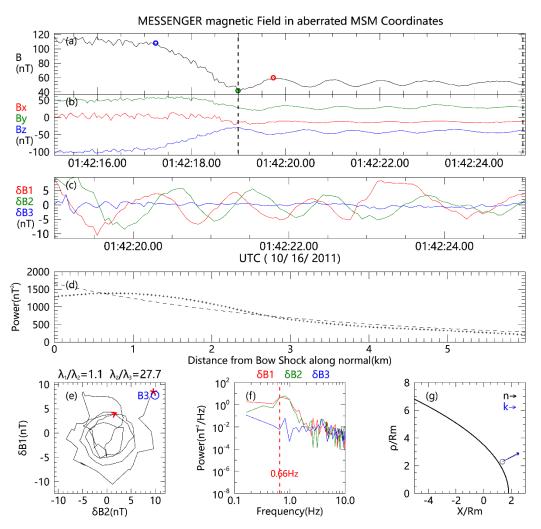




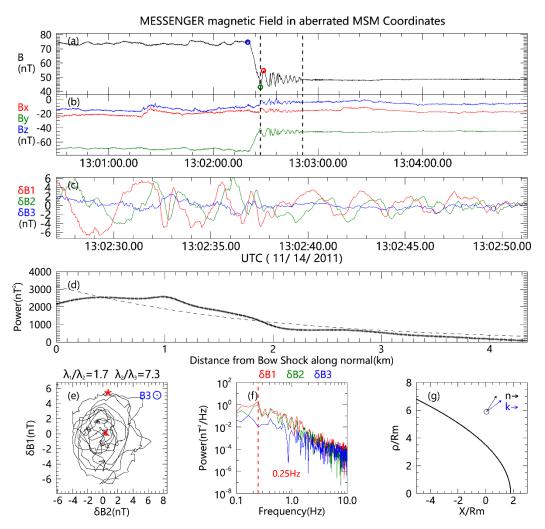




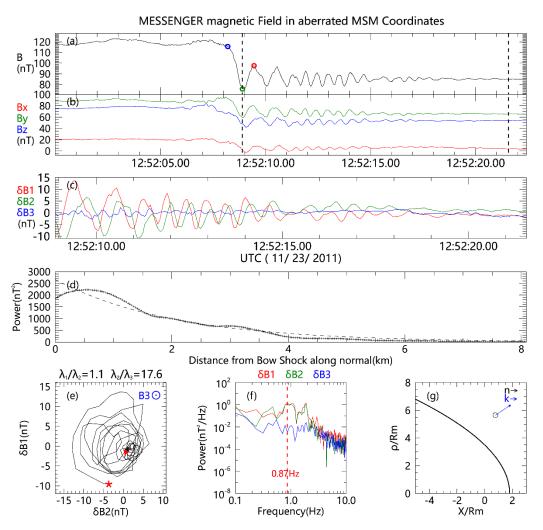




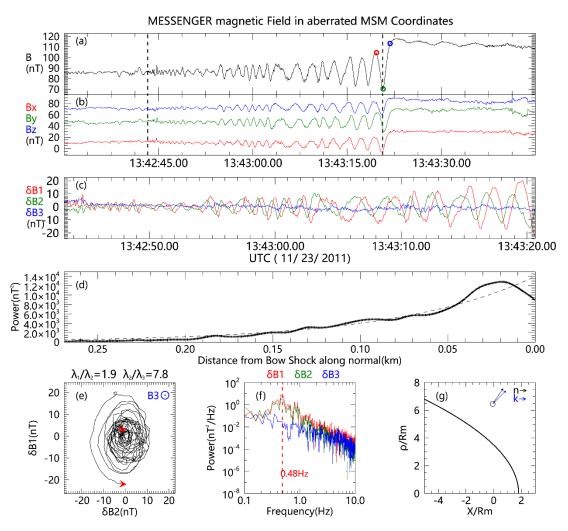




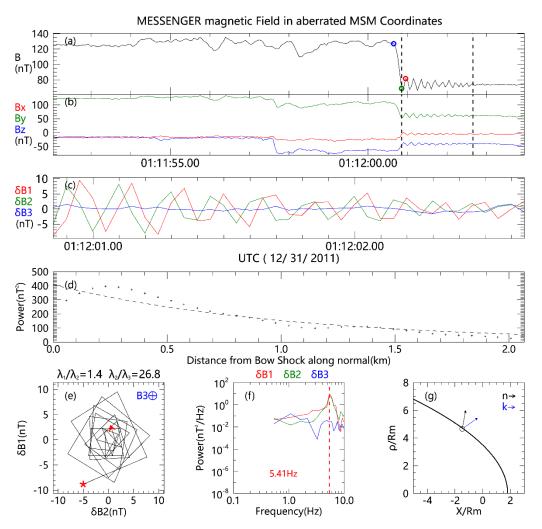




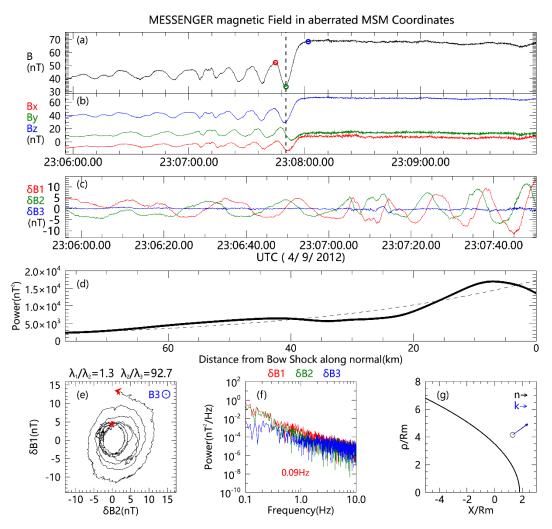












Event 12

