Temporal turnover in species' ranks can explain variation in Taylor's slope for ecological timeseries

Shyamolina ${\rm Ghosh}^1$ and ${\rm Blake}~{\rm Matthews}^2$

 1 University of Zurich 2 Eawag

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Abstract

The scaling exponent relating the mean and variance of the density of individual organisms in space (i.e. Taylor's slope: z_{space}) is well studied in Ecology, but the analogous scaling exponent for temporal datasets (z_{time}) is underdeveloped. Previous theory suggests the narrow distribution of z_{time} (e.g. typically 1 - 2) could be due to interspecific competition. Here, using 1,694 communities time series, we show that z_{time} can exceed 2, and reaffirm how this can affect our inference about the stabilizing effect of biodiversity. We also develop new theory, based on temporal change in the ranks of species abundances, to help account for the observed z_{time} distribution. Specifically, we find that communities with minimal turnover in species' rank abundances are more likely to have higher z_{time} . Our analysis provides a deeper mechanistic understanding of how species-level variability affects our inference about the stability of ecological communities.

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3 Authors and emails:

- 4 Shyamolina Ghosh^{1*} (ghoshshyamolina89@gmail.com),
- 5 Blake Matthews² (blake.matthews@eawag.ch)

6 Affiliations:

- 7 1. Department of Evolutionary Biology and Environmental studies, University of Zurich;
- 8 Winterthurerstrasse 190, 8057 Zurich, Switzerland
- 9 2. Department of Fish Ecology and Evolution, Eawag, Swiss Federal Institute of Aquatic
- 10 Science and Technology; Seestrasse 79, Kastanienbaum, 6047 Switzerland

11 *Name, mailing address, email, phone number of corresponding author:

- 12 Dr. Shyamolina Ghosh, Senior researcher (Oberassistentin)
- 13 Department of Evolutionary Biology and Environmental Studies, University of Zurich,
- 14 Winterthurerstrasse 190, 8057 Zurich, Switzerland
- 15 Phone (+41) 779567848, email ghoshshyamolina89@gmail.com
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46 Abstract:

47 The scaling exponent relating the mean and variance of the density of individual organisms in 48 space (i.e. Taylor's slope: z_{space}) is well studied in Ecology, but the analogous scaling exponent 49 for temporal datasets (z_{time}) is underdeveloped. Previous theory suggests the narrow distribution 50 of z_{time} (e.g. typically 1 - 2) could be due to interspecific competition. Here, using 1,694 51 communities time series, we show that z_{time} can exceed 2, and reaffirm how this can affect our 52 inference about the stabilizing effect of biodiversity. We also develop new theory, based on 53 temporal change in the ranks of species abundances, to help account for the observed z_{time} 54 distribution. Specifically, we find that communities with minimal turnover in species' rank 55 abundances are more likely to have higher z_{time} . Our analysis provides a deeper mechanistic 56 understanding of how species-level variability affects our inference about the stability of 57 ecological communities.

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69 Introduction

70 Our understanding of the temporal variability of populations or communities, which is of 71 long-standing interest in ecology (Anderson et al. 1982; Bahram et al. 2015), often centers 72 around a scaling relationship between the mean and variance of species' abundances (aka 73 Taylor's Law, 1961). In a pioneering meta-analysis in 1961, L.R. Taylor proposed a general 74 scaling relationship, referred to as Taylor's (power) law (hereafter TL), relating the variance (v)75 of population density with its mean (m): $v = am^{z}$, for values of a > 0, z being called TL slope or 76 exponent. This scaling relationship is ubiquitously observed for many taxa in nature (e.g., 77 bacteria, fish, plants, insects, voles, etc.), and has also been applied outside of ecological systems 78 (Eisler et al. 2008; Kalyuzhny et al. 2014; Taylor 2019). Although Taylor's law was originally 79 developed for the analysis of spatial variation of population density (Taylor 1961), it is also 80 highly relevant, but less often studied, in the context of temporal analyses of communities 81 (reviewed by Cobain et al. 2019). In spatial analyses of density variation (TL_{space}), z_{space} is an 82 index of the degree of patchiness of the population density of a single species among sites (i.e. 83 metapopulations). Whereas, in temporal analyses of density variation (TL_{time}), z_{time} is an index of 84 temporal aggregation of the abundance fluctuations of multiple species in a community (i.e., 85 from the same site). The z_{time} exponent has been useful for assessing population persistence 86 (Pertoldi et al. 2008; Kalyuzhny et al. 2014), the stability of crop yields (Döring et al. 2015), and 87 fluctuations in fish stocks (Kuo et al. 2016; Xu et al. 2019; Segura et al. 2021).

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89 Currently, understanding the importance of mean-variance fluctuation scaling (i.e. z_{time}) for 90 making inferences from community dynamics is limited by uncertainty in i) the distribution of 91 z_{time} in natural communities, ii) how z_{time} variability affects interpretations of community stability, 92 and iii) the mechanisms underlying z_{time} variability. We address each of three gaps (referred to 93 below as G1-G3). First, existing studies of natural communities have documented a limited range 94 of variation in z_{time} (Cobain *et al.* 2019; Xu & Cohen 2019), but with the increasing availability 95 of long-term community time series we can improve our inference about the distribution of z_{time} 96 in nature.

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98 Second, there is longstanding theory about how variation in z_{time} is relevant for interpreting 99 community stability (Cottingham et al. 2001; Kilpatrick & Ives 2003; Kalyuzhny et al. 2014; 100 Cobain et al. 2019; Zhao et al. 2019), but these interpretations are somewhat sensitive to mean 101 variance scaling. Importantly, when z is greater than 1, the expected temporal variance of the 102 total community abundance is less than that of a single population for that same mean abundance 103 (Fig. 1), meaning that species-level variance increases nonlinearly in relation to mean 104 abundances. This reduced variance arises because of the statistical averaging of independently 105 varying population time series, which is known as the portfolio effect concept (hereafter PE) 106 (Doak et al. 1998; Schindler et al. 2015). PE has been widely used to quantify the importance of 107 species diversity for overall community stability (i.e., inverse of community variability, CV), but 108 its interpretation depends on z_{time} for that community (Cottingham *et al.* 2001). For example, the 109 magnitude of the PE is negligible when $z_{time} \sim 1$, and increases with z_{time} (Fig. 1E, red line). This 110 means that estimates of community stability (i.e. 1/CV), for a given species richness, decrease 111 with the increase in z_{time} for a community (Fig. 1E, black line). Importantly, the consistently 112 negative relationship between stability and z over a wide range of species diversity (Fig. 2A) 113 means that the expected slope of the relationship between species richness and stability decreases 114 substantially as z_{time} increases (Fig. 2A, inset). Often, PEs are estimated by comparing the overall

115 community variability with the average variability of constituent populations, or, in a spatial 116 context, by comparing the CV of overall the meta-population abundance with the average CVs of 117 the subpopulations (Schindler *et al.* 2010). However, Anderson et al. (2003) showed that the 118 above-mentioned approach is appropriate only for $z_{time}=2$, and they provided an alternate 119 approach accounting for the potential heterogeneity of z among communities.

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121 Third, existing theory can explain why z_{time} often varies between 1 and 2 (Taylor & Woiwod 122 1982; Tokeshi 1995; Xiao et al. 2015), but provides no general mechanistic explanation for the 123 entire empirically observed range of z_{time}. For spatial TL context, several proposed mechanisms 124 that explain variation in z_{space} have considered density dependence (Perry 1994), 125 density-independent and stochastic population growth (Cohen et al. 2013), population synchrony 126 (Cohen & Saitoh 2016), and random sampling from skewed distribution (Cohen & Xu 2015). 127 Whereas for z_{time} proposed mechanisms have considered interspecific competition (Kilpatrick & 128 Ives 2003), environmental variability (Cohen & Saitoh 2016), correlated reproduction 129 (Ballantyne & J. Kerkhoff 2007), sampling error (Kalyuzhny et al. 2014), and limited sampling 130 effort (Giometto et al. 2015). However, all of these previous studies have focused on explaining 131 why z_{time} is typically less than 2, and only a few previous studies have provided a mechanistic 132 explanation for why it can be greater than 2. In spatial models, z_{space} can be greater than 2 due to 133 synchrony among metapopulations (Reuman et al. 2017) especially when they are rare (Ghosh et 134 al. 2020a), and due to growing stochasticity (Cohen et al. 2013) or unexpected changes in a 135 smoothly autocorrelated environment (Cohen 2014). In the case of z_{time} , only one previous study 136 of a fish community found that environmental variability can lead to a size-based Taylor's slope 137 greater than 2 (Cobain et al. 2019).

139 In this paper, we will address each of those three aforementioned gaps. First (for G1), we 140 estimate the distribution of z_{time} (hereafter z) in nature by compiling thousands of long-term (>20 141 years) community time series (>15 species). Second (for G2), we use this dataset to explore the 142 consequence of variation in z for interpreting stability in general, and the portfolio effect in 143 particular. Third (for G3), we propose a novel and general mechanism that can help explain the 144 wide range of z observed in natural communities. Our mechanism is based on how species' 145 rank-abundance distribution in a community change over time (MacArthur 1957; McGill *et al.* 146 2007). Although the rank-abundance curves are widely studied in ecology (Whittaker 1965), 147 their temporal turnover has not been previously explored in the context of explaining variation in 148 mean-variance scaling among communities (i.e. variability in z).

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150 Materials & Methods

151 We compiled long-term abundance (or biomass when abundance was not available for 379 plant 152 communities) annual time series (20 to 57 years) data from a public database (Ghosh *et al.* 2023) 153 for 1,694 communities in total, and for multiple taxa (e.g., birds, fish, terrestrial and freshwater 154 invertebrates, phytoplankton, plants with a minimum of 15 species sampled annually). We 155 included species that were present for at least for 70% of the total sampling period, thus, 156 following other studies (Sasaki & Lauenroth 2011; Valencia *et al.* 2020), we focused on the 157 dynamics of dominant species in communities. For each of the 1,694 communities, we computed 158 the average correlation between years (r), and five additional metrics using the *ecofolio* 159 R-package (Anderson *et al.* 2013). They are temporal Taylor's slope (z), community-level 160 temporal synchrony among species as variance ratio, VR, (Loreau & de Mazancourt 2008), 161 temporal community stability (as CV⁻¹), and two types of portfolio effects (Anderson *et al.* 162 2013), PE, considering without (i.e. based on an average-CV based approach) and with 163 mean-variance scaling. We also computed net tail-dependence among species' ranks (i.e. 164 dependence between lower ranks minus dependence between higher ranks, rarest species got 165 lowest rank) between any two years of the whole study period, using *partial Spearman* 166 *correlation* approach (Ghosh *et al.* 2020a, b).

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168 We addressed the first gap (G1) by evaluating the wide variation in z for the largest collection of 169 such long-term natural communities. We also simulated communities with different 170 combinations of richness (varying from 30 to 70) and z (varying from 1 to 3) to test whether the 171 two types of PE differ from each other when z is not equal to 2. We later used both of these 172 empirical and simulated communities to address G2 and verified how the average-CV based 173 approach overestimated PE when z<2, and underestimated when z>2 (results in Figs. 2B-3, see 174 Box 1 for theoretical expectations). We also developed a rank abundance curve (RAC) turnover 175 model to provide a general mechanism behind the wide variation in z found for natural 176 communities (addressing G3). We then used the model to help us understand potential 177 explanations for the observed variation of zin nature (results are shown in Figs. 4D, 5).

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To develop the model, we simulated three types of communities with the same number of species (R) and the same between-year correlation (r). They are - type I, Fig. 4A: having more the dependence among the dominant group of species (i.e., consistent upper ranks in RAC and more late turnover in lower ranks), type II, Fig. 4B: having more dependence among the not-so-common or ranks rare group of species (i.e., consistent lower ranks in RAC and more turnover in upper ranks), and

184 type III, Fig. 4C: having no dependence in any specific group (i.e., complete and random annual 185 turnover among species ranks). "Copula", a mathematical tool and a rank-based approach, has 186 been used to compute tail-dependence (i.e., dependence in the extremely high or low values) 187 among two correlated ecological variables in past studies (Ghosh et al. 2020a, b, c, 2021; Walter 188 et al. 2022). Copulas make the marginal distribution uniform so that the dependence information 189 remains unique on its own. For example, with the same sample set (x_i, y_i) ; i = 1, 2, ..., R one 190 can generate type I, type II, and type III dependence using three particular single-parameter 191 "copula" families: Survival Clayton, Normal, Clayton, respectively (see iRho function from 192 copula R-package for details (Yan 2007)). We used this approach in the community matrix, M, 193 (with abundance or biomass for R number of species that are sampled for N years; species along 194 columns and years along rows) so that the Spearman correlation between any two years are the 195 same. Specifically, we first constructed such a community from Clayton family that has 196 dependence in lower ranks (type II), and then we permuted M in such a way to eliminate the 197 tail-dependence structure but preserve the same between-year correlation, r (up to sampling 198 error). In doing so, this permutation generated a Normal copula (type III). Then, we again 199 permuted the community matrix M to get upper tail-dependence (i.e., dependence in upper ranks) 200 preserving between-year correlations and leading to the Survival Clayton copula (i.e. a 201 180-degree rotation of Clayton family). We generated 1,000 surrogates for each type of 202 community (see Simulation zmorethan2.R script from the Zenodo repo: https://doi.org/10.5281/zenodo.8373892). A similar algorithm was previously used in Spatial 203 204 Taylor's law context to generate surrogate communities with the same correlation but different 205 dependence structures among sites (Ghosh et al. 2020a).

207 Given this set of community types, we hypothesized that the third type (i.e. Fig. 4: Case III) 208 would lead to z values within the commonly observed range of 1 and 2, irrespective of the value 209 of the r. However, we also suspected that any tail-dependencies in the ranks (e.g. lower or upper 210 tail dependencies in Case 1 and II) could expand the range of z both below 1 and above 2 (i.e., 211 for the Case I, II). To explore this, we simulated for a given year-to-year correlation, r, three 212 types of communities each with 1,000 surrogates (or replicates), and species richness R = 40213 where we tracked species abundance for N = 22 years. Therefore, each replicate community type 214 has the same year-to-year correlation, r, and we varied r over a range from 0.2 to 0.9 (results 215 shown in Fig. 4D). R and N for this simulation are chosen to have same median values for 216 richness and timeseries length found in our dataset, so that we can compare the results.

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218 Results

219 Our data compilation confirms that most of communities had values of z within the commonly 220 reported range from previous studies (i.e., between 1 to 2), but also reveals that nearly 5% of 221 communities had values of z outside that range (Fig. 3A), addressing G1. Consistent with 222 previous theory, and confirmed with simulated community timeseries (Fig. 2A), stability was 223 higher for communities having z<2 than the communities with z>2 (Fig. 3B, addressing G2). 224 The positive effect of diversity (i.e. richness) on stability was weaker (slope is less steep) for 225 communities with z>2. This result highlights the potential need to account for heterogeneity in z 226 values when comparing the stability among communities. We additionally find that such 227 heterogeneity is important for interpreting stabilizing mechanisms of community stability, such 228 as the portfolio effect (for G2). Simulated communities show the limitations of previous 229 approaches (i.e. based on average-CVs following Box 1) that overestimate PE for z<2 (Fig. 2B, 230 solid lines), and the underestimate PE for z>2 (Fig. 2B, dashed lines). As expected, these 231 approaches converge to the same answer when z=2, and so the relevance of this improved 232 method depends on how often the mean-variance scaling exponent in natural communities 233 deviates from 2. Consistent with this previous theory, our empirical estimates of PE were higher 234 without accounting for the mean-variance scaling (Fig. 3C), because the majority of communities 235 had z<2. Comparing these two approaches (i.e. with and without accounting for mean-variance 236 scaling) clearly shows larger values for PE without mean-variance scaling (i.e. green points, 237 n=1,610, above the diagonal line, Fig. 3D) for z<2, whereas communities with z>2 had larger PE 238 when accounting for mean-variance scaling (i.e. pink points, n=80, below the diagonal line, Fig. 239 3D).

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241 Our model of RAC turnover provides new insight into explaining the wide variation observed in 242 in our empirical dataset (Figs. 4D, 5), addressing G3. The simulation from RAC turnover model, 243 as depicted in Fig. 4D, shows communities exhibiting high annual turnover among all species 244 had z values within the expected range (black solid points ~1.5 showed the mean of 1,000 245 estimates, Case III). Moreover, we find that communities with high turnover for any particular 246 group (rare: Case I, dominant: Case II) show a much wider range of z. For above-average 247 year-to-year correlation (r>0.5), communities where rare species change their ranks more 248 frequently are more likely to have z less than 1 (Case I, follow blue dotted lines in Fig. 4D after 249 the crossing at r=0.5). Whereas, communities in which dominant species changed their ranks 250 more frequently are more likely to have z greater than 2 (Case II, follow red dotted lines in Fig. 251 4D beyond r=0.5). The patterns are opposite below r=0.5, where Case I and Case II have a 252 higher probability to have z>2, and z<1, respectively. Our repeated simulation for different 253 combinations of richness (*R*), and time series length (*N*) gives similar general finding, and is 254 robust to the choice of both *R* and *N*.

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256 When analysing empirical community time series, we found that the year-to-year correlation, r, 257 was often greater than 0.5. This range of r led to our expectation, from the above-mentioned 258 simulation result, that communities showing more dependence in species' upper ranks (Case I 259 from Fig. 4D) would likely to have z<1, whereas, communities with more dependence in 260 species' lower ranks (Case II from Fig. 4D) would likely to have z>2. Indeed, our empirically 261 observed distribution of the net tail-dependence of communities is broadly in line with our 262 modeling outcomes (Fig. 5D). Specifically, we find higher z values to be associated with 263 communities that also show more dependence in lower ranks. In our analysis of the natural 264 communities, we interpret more negative values to indicate stronger dependence in upper ranks 265 (i.e. dominant species), and less negative to positive values mean increasing contribution of 266 dependence in lower ranks (i.e. rare species). Overall, the qualitative match between our 267 simulation results in Fig. 4 and our analysis of empirical analysis in Fig. 5 support our 268 predictions. Specifically, communities with high annual turnover over their entire 269 rank-abundance distribution tend to have z-values within the range of 1 and 2, whereas 270 communities with high annual turnover in just their most dominant or more rare species can have 271 z-values less than 1 or greater than 2.

272

273 In our compilation of community timeseries, the species richness varies from 15 to 89 274 (median=40 species, Fig. 5A), the length of timeseries sampled varies from 20 to 57 years 275 (median=22 years), the correlations between years are typically >0.5 (Fig. 5B), and the

276 synchrony among species (as measured by the variance ratio) is typically <0.75 (Fig. 5C). The 277 Variance Ratio (VR) has a range of (0, 1). VR values close to 0 implies less synchrony and 278 values of 1 indicate perfect synchrony. Though most data lies in the bottom-left box of Fig. 5C 279 with low synchrony (VR<0.5, 1<z<2), there are also some communities with z>2 but low 280 synchrony (in the top-left box).

281

282 Discussion

283 Overall, our data compilation, analysis, and simulation model allows us to explore how 284 heterogeneity in z can affect inferences about stability-diversity relationships and the portfolio 285 effect (PE) (Fig. 3), and provides a novel explanation for the wide distribution of temporal 286 Taylor's slope (z) observed in ecological communities (Fig. 4). Previous work has established 287 that strong positive relationships between richness and stability are only expected when z<2 (Fig. 288 3B), and that variability in z among communities can mask how we estimate the contribution of 289 PE to community stability (Fig. 3C-D). Although the majority of empirical observations of 290 communities find z between 1 and 2 (Fig. 3A), large values of z are common enough to affect 291 inferences about the causes of stability variation. For example, measuring the PE without 292 considering the mean-variance scaling relationship can lead to substantial overestimates of 293 stability when z<2, and increasingly large underestimates when z>2 (Fig. 2B). As the statistical 294 averaging effect is likely a fundamental mechanism of stability (Zhao *et al.* 2022), it is essential 295 to make accurate assessments in order to support conservation and management efforts.

296

297 Several previous mechanisms have been proposed to explain variability in z, and have speculated 298 about causal drivers of community stability. Interspecific competition and environmental 299 variability, for example, can explain some variation in z that can impact stability (Kilpatrick & 300 Ives 2003; Cobain *et al.* 2019). For example, negative interactions among species (e.g. 301 competition) is a commonly proposed mechanism for explaining why abundant species are less 302 variable than expected given their mean abundance, leading to communities with z<2 (Kilpatrick 303 and Ives 2003). Here, our proposed mechanism can explain z values both less than and greater 304 than 2 (Fig. 4). This implies there can be multiple reasons for the observed range of z values in 305 natural communities, and also multiple explanations, beyond simply competition, for why 306 communities can both have low synchrony and have z-values less than and greater than two (Fig. 307 5C).

308

309 Our simulations demonstrate how high turnover among all species' ranks (reordering all species) 310 can yield communities with z-values in the range of [1, 2], whereas group-specific turnover, 311 namely rank-inconsistency only for the dominant species or rare species throughout the years, 312 can yield communities with z values outside the range of [1, 2]. Few previous studies have 313 connected species abundance distribution with Taylor's law (Ma 2015; Cohen 2020), but doing 314 so can reveal how changes in rank abundance distribution (Fig. 5) can impact our assessment of 315 community stability (Fig. 3). Our results show that monitoring the RACs for rare vs. dominant 316 groups of species can help explain the broad range of z observed in nature. There is a long 317 history of tracking RACs to understand community dynamics in response to global change 318 drivers (Collins *et al.* 2008; Avolio *et al.* 2015, 2019; Jones *et al.* 2017). Our work suggests we 319 need a better understanding of the reasons for temporal variation in RACs and z. For a specific 320 richness, RAC can change due to both species reordering and changes in eveness without 321 reordering ((Collins *et al.* 2008; Avolio *et al.* 2015, 2019; Jones *et al.* 2017). A previous study 322 (Wohlgemuth *et al.* 2016) highlighted the role of species reordering rather than evenness in 323 maintaining ecosystem functioning. Our study also highlights that changes in species reordering, 324 rather than eveness, is most likely to affect z and hence how we make inferences from observed 325 community dynamics (Figs. 1, 2, and 5).

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327 Earlier studies also showed that environmental variability (e.g., temperature, soil quality, 328 drought) can affect the dynamics of species turnover, and hence the temporal variation in the 329 identity of dominant and rare species in a community (Ulrich et al. 2016; Castillioni et al. 2020). 330 Changes in the dominance structure of communities is expected due to differences in species 331 environmental tolerance and competitive ability in a given environment (Shurin 2007). 332 Reordering of the identity of species in rank-abundance curves is also likely when a community 333 responds to environmental change (e.g., forb vs grass (Hoover et al. 2014)). For example, in a 334 long-term study on desert grassland, the reordering of which species were dominant varied 335 through time in response to both pulse (wildfire) and press (changes in Pacific decadal 336 oscillation) climatic perturbations (Collins et al. 2020). There is overwhelming evidence that 337 environmental change can drive community dynamics that substantially alter RACs (McCarthy 338 et al. 2018). However, more work is clearly needed to test the hypotheses about how climatic 339 change, for example, can alter the tail-dependence in species' ranks, and whether mean-variance 340 relationships are stable in relation to their temporal Taylor's slope (i.e. z). A recent study (Tippett 341 & Cohen 2020) showed seasonal variation in variance-to-mean relationship for all-India daily 342 rainfall pattern (low during peak monsoon, high during otherwise). Such mean-variance 343 relationships in climatic factors might affect communities' mean-variance scaling relationship in 344 a similar way.

347 community variability, stability, portfolio effects, and species abundance distribution over time. 348 There are several important insights from our study. First, identifying the causes of 349 mean-variance scaling of population abundances is important for the longstanding challenge of 350 understanding relationships between diversity and stability of communities (McCann 2000). 351 Importantly, greater species richness does not necessarily ensure more temporal stability if **352** abundant species are more variable than expected, such that communities have z > 2 (Fig. 3B). 353 Second, identifying the importance of portfolio effects as a stabilizing mechanism of 354 communities can be both over- or underestimated if the mean-variance scaling relationship is not 355 carefully considered (Zhao et al. 2022). Third, we establish a novel and general biological **356** mechanism that can help explain observed wide variation in z (i.e., <1 or >2) seen in natural 357 communities. We confirm our hypothesis with simulated (i.e., from the *RAC-turnover model*; 358 Fig. 4) and empirical data (i.e., from 1,694 long-term natural communities; Fig. 5) that temporal 359 turnover in RACs via species-reordering is an important factor determining the value of z. This 360 finding is consistent with earlier studies that showed global change drivers can reshape RACs via 361 species reordering (Avolio et al. 2015, 2022), and could be crucial for better understanding the 362 mechanism behind the community response to global change drivers.

363

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369 Figures:



Figure 1: The concept of temporal Taylor's law: in ecological communities population and a variance to mean scaling relationship. Temporal variance can fluctuate with an exponent (z) to the temporal mean - in log scale, the relationship would be a fitted straight line of are slope z. Taylor's slope (z) can be below <2, A or >2, C, with z=2 often considered as a limiting are species anong a total of 70 species in the community

376 (thinner lines) and total community abundance timeseries on the top (thicker lines). Species are 377 very weakly related in each of these simulated communities (synchrony or variance ratio <378 0.025). Due to the fluctuation scaling relationship, the variance of total community abundance is 379 often lower (symbol X) than the predicted value on the dotted line for a given community mean, 380 D. Higher value of z results in a larger difference, and lowers community stability (i.e., the 381 inverse of variability in total community abundance timeseries), E.



Figure 2: Temporal Taylor's law slope, z, affects stability (A) and portfolio effect (B) for three different levels of richness: R=30, 50, and 70. The diversity-stability relationship has a steeper slope for lower z, but a weaker positive slope at higher z (inset, A). Within the feasible slope for [1, 2] portfolio effect (PE) computed based on average-CV (i.e., without mean-variance scaling, solid lines, B) gives an overestimate of accurate measure of PE (i.e. considering mean-variance scaling, dashed lines, B). For z>2, PE without mean-variance scaling underestimates the true effort. At z=2, both measures are exactly the same.



Figure 3: Empirical observations verify the concepts of Fig 2. The majority of the communities had temporal Taylor's law slope (z) <2 (n=1610), and 5% of communities had z>2 (n=84) (A). Stability, the inverse of variability in total community abundance (=1/CV), was lower for communities with z>2 and the stability-diversity relationship had a weaker positive slope compared to communities that had z<2 (B). Distributions of portfolio effects computed with and

without mean-variance relationship are depicted in C. For communities having z>2, the portfolio app effect due to mean-variance scaling was higher (pink points below the dotted 1:1 line) than the app portfolio effect if mean-variance scaling had not been considered. On the other hand, for app communities with z<2, the pattern was opposite (green points above the dotted 1:1 line), i.e., a app higher estimate for portfolio effect happened without considering mean-variance scaling.



405 Figure 4: Mechanism explaining variation in temporal Taylor's law slope (z) for ecological 406 communities when species show a positive year-to-year correlation (r>0) in the *RAC-turnover* 407 model (see Materials & Methods). In a community where some dominant species are always 408 dominant throughout the years (so consistent in high rank-abundances) but rare species show a 409 more annual turnover, z could be <1 or >2 depending on the value of r (Case I: A, the blue line

410 in D). In an opposite scenario, in a community where some rare species are always rare 411 throughout the years (so consistent in low rank-abundances) but dominant species show a more 412 annual turnover, z could also be <1 or >2 depending on the value of r (Case II: B, the red line in 413 D). When in a community all species would fluctuate in their annual rank abundance, 1 < z < 2414 would happen, irrespective of r values (Case III: C, the black line in D). Simulation with 415 surrogate communities (40 species were simulated for 22 years to match the median values of 416 sampled richness and years from empirical communities) shows dependence in either rank 417 (lower or upper) can make z<1 or z>2, whereas turnover for all species always results in 1 < z < 2; 418 for details see *Materials & Methods*. The bars are due to two standard deviations for the 419 estimates from 1,000 surrogate communities, and plotted around the mean (solid points).



421 Figure 5: Empirical observations show results consistent with the mechanism from Fig. 4. A 422 total of 1,694 communities have richness in between [15, 88], A, an on-average correlation 423 between years r>0.5, B, and interspecific synchrony (variance ratio) <0.75, C. Range of r424 indicates z can be greater than 2 if ranks of rare species were consistent throughout years as 425 shown for the red line in Fig. 4D. Empirical communities also show z>2 is possible as 426 consistency or dependence increases in the lower ranks (Pearson correlation, R, from the linear 427 regression is significantly positive, shown in panel D).

429 Box 1: Quantifying portfolio effect, PE, for a community considering with or without

430 mean-variance fluctuation relationship

Let us consider we are monitoring a community with n number of species for N years, where mean, m_i , and variance, v_i , of species abundance or biomass are related via temporal Taylor's law slope z:

$$v_i = am_i^z$$
; $i = 1, 2, ..., n$ (1)

Portfolio effect, PE is defined as the CV of a single species timeseries compared to the CV of the total community abundance (or biomass) timeseries.

$$PE = CV_{sp} / CV_{com} \dots (2)$$

Following the recipe given by Anderson et al. (Anderson *et al.* 2013), we computed *PE* in two ways: (i) type I: based on the average *CV* of species in the community as PE_{avgCV} and (ii) type II: considering the effect of the mean-variance relationship as PE_{mv} .

Both types of PE have the same denominator, i.e., CV for total community timeseries

$$CV_{com} = \frac{\sqrt{m_1^z + m_2^z + \dots + m_n^z}}{m_1 + m_2 + \dots + m_n} = \frac{\sqrt{\sum_{i=1}^n m_i^z}}{\sum_{i=1}^n m_i} \dots \dots \dots \dots (3)$$

For type I average-CV based approach, CV_{sp} is computed as the average of individual species' CV that leads to following relationship for PE:

$$PE_{avgCV} = CV_{sp} / CV_{com} = \left(\frac{1}{n}\sum_{i=1}^{n}\frac{\sqrt{m_i^z}}{m_i}\right) \times \frac{1}{CV_{com}} = \frac{1}{nCV_{com}}\sum_{i=1}^{n}m_i^{(z/2)-1} \dots \dots \dots \dots (4)$$

For type II mean-variance scaling approach, CV_{sp} is computed as the single species' CV, as if only one species equivalent to total community (abundance or biomass) is present. This leads to following relationship for *PE*:

Now we will compare between two types of PE from Eqs. (4-5), for different values of z.

Case I: when
$$z = 2$$
, $PE_{avgCV} / PE_{mv} = 1$.

Case II: when z<2, to illustrate say, z=1:

then $PE_{avgCV} / PE_{mv} = \frac{\sum_{i=1}^{n} m_i^{-1/2}}{n\left(\sum_{i=1}^{n} m_i\right)^{-1/2}}$, i.e., $PE_{avgCV} > PE_{mv}$ (see (Ramanujan 1915)). This

inequality indicates if we do not consider the fluctuation scaling relationship, average *CV* based method will overestimate stability.

Case III: when z>2, to illustrate say, z=4: then

 $PE_{avgCV} / PE_{mv} = 1/n$, i.e., $PE_{avgCV} < PE_{mv}$. This inequality indicates if we do not consider

the fluctuation scaling relationship, average CV based method will underestimate stability.

Both Case II and case III can be verified trivially with mathematical induction and also consistent with the metapopulation context (spatial Taylor's law; (Anderson *et al.* 2013)).

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