

Global well-posedness for the generalized Navier-Stokes-Coriolis equations with highly oscillating initial data

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Abstract

We study the small initial data Cauchy problem for the generalized incompressible Navier-Stokes-Coriolis equations in critical hybrid-Besov space $\dot{B}^{-2, \frac{5}{2-2\alpha}, \frac{3}{p-2\alpha+1}}(\mathbb{R}^3)$ with $\frac{1}{2} < \alpha < 2$ and $2 \leq p \leq 4$. We prove that hybrid-Besov spaces norm of a class of highly oscillating initial velocity can be arbitrarily small. and we prove the estimation of highly frequency L^p smoothing effect for generalized Stokes-Coriolis semigroup with $1 \leq p \leq \infty$. At the same time, we prove space-time norm estimation of hybrid-Besov spaces for Stokes-Coriolis semigroup. From this result we deduce bilinear estimation in our work space. Our method relies upon Bony's high and low frequency decomposition technology and Banach fixed point theorem.

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