# Density Functional Theory Study of Ultrashort Metal-Metal Distance in Diberyllium Complexes Bearing Carbene Ligands 

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#### Abstract

Diberyllium complexes with an ultrashort metal-metal distance (USMMD, $d_{\mathrm{M}-\mathrm{M}}<1.900 \AA$ ) are fascinating for the nature of the valence electronic structure of beryllium. In this paper a family of diberyllium complexes, in which $\mathrm{Be}_{2} \mathrm{H}_{3}+$ was coordinated by $N$-heterocyclic carbenes or mesoionic carbenes, were studied using density functional theory which generated an ultrashort $\mathrm{Be}-\mathrm{Be}$ distance of $1.754-1.779 \AA$. Based on bonding nature and electronic structure studies, the ultrashort Be-Be distance was attributed to multiple bonding orbitals and directly orbital overlapping between the two beryllium atoms. These diberyllium complexes exhibited great stability with large HOMO-LUMO gaps and high dissociation energies, and were potential targets in future experiments.


## 1. Introduction

The nature of chemical bonding is a fundamental question in chemistry. Since Cotton et al. proposed the first quadruple metal-metal bond in $\mathrm{Re}_{2} \mathrm{Cl}_{8}^{2-[1]}$, great attention has been drawn to homonuclear transitional metal complexes with multiple metal-metal bond and ultrashort metal-metal distance (USMMD, $\mathrm{d}_{\mathrm{M}-\mathrm{M}}<$ $1.900 \AA$ ). In 2005, Power et al. reported the crystalline structure of a dichromium complex containing a quadruple $\mathrm{Cr}-\mathrm{Cr}$ bond of $1.835 \AA^{[2,3]]}$. This research has triggered the crystallographical study of varies dichromium complexes, in which the length of a quadruple $\mathrm{Cr}-\mathrm{Cr}$ bond was as short as $1.706 \AA^{[4-7]}$, and characterization of a sextuple $\mathrm{Cr}-\mathrm{Cr}$ bond ${ }^{[8,9]}$. USMMD was also reported as a parameter of the homonuclear complexes composed by other transitional metals, such as manganese and molybdenum ${ }^{[10,11]}$. Yet, how to realize USMMD in binuclear complexes of main group metals is challenging, especially in those of the s-block elements that do not have sufficient valence electrons.
Beryllium interrupts the homoatomic bonding of electron-deficient elements Li, Be and B. Previous studies showed the effective bond order (EBO) in $\mathrm{Li}_{2}$ and $\mathrm{B}_{2}$ was around 1 , while in $\mathrm{Be}_{2}$ it was as low as $0.2^{[12]}$, demonstrating an unusual bonding nature of beryllium dimers. Spectroscopic measurements ${ }^{[13]}$ and theoretical simulations ${ }^{[14]}$ determined the Be - Be distance in $\mathrm{Be}_{2}$ to be $2.45 \AA$ with bond dissociation energy ( BDE ) of $2.26 \mathrm{kcal} / \mathrm{mol}$, which chemists usually consider not to be a genuine chemical bond. Electronic structure studies of $\mathrm{Be}_{2}$ revealed that its two highest occupied molecular orbitals, HOMO and HOMO-1, were $\sigma$-antibonding and bonding, respectively, while the two lowest unoccupied molecular orbitals, LUMO and LUMO +1 , were of a $\pi$-bonding nature. Such findings sparked ideas of achieving short $\mathrm{Be}-\mathrm{Be}$ distances by withdrawing electrons from the antibonding HOMO of $\mathrm{Be}_{2}$ or filling its LUMO by binding electron-donating groups. Previous calculations proved that $\mathrm{Be}_{2}{ }^{+}$and $\mathrm{Be}_{2}{ }^{2+}$ had shorter $\mathrm{Be}-\mathrm{Be}$ distances compared with $\mathrm{Be}_{2}{ }^{[15]}$, indicating strengthened $\mathrm{Be}-\mathrm{Be}$ bonds. Brites and co-workers ${ }^{[16]}$ found the ground state of $\mathrm{Be}_{2} \mathrm{H}_{2}$ possessed a $\mathrm{Be}-\mathrm{Be}$ distance of $2.09 \AA$ with the BDE of about $75 \mathrm{kcal} / \mathrm{mol}$, and they attributed this stronger $\mathrm{Be}-\mathrm{Be}$ interaction in $\mathrm{Be}_{2} \mathrm{H}_{2}$ to electron donation from the antibonding orbital of $\mathrm{Be}_{2}$ to the 1s orbitals of two H atoms. In 2016, Cui et al. ${ }^{[15]}$ reported that $\mathrm{Be}_{2} \mathrm{~F}_{2}$ with a $\mathrm{Be}-\mathrm{Be}$ distance of $2.05 \AA$ and BDE of 76.9 $\mathrm{kcal} / \mathrm{mol}$, and they related this short distance to the $\sigma$-bonding HOMO of $\mathrm{Be}_{2} \mathrm{~F}_{2}$. Brea and Corral ${ }^{[17]}$ have
also stabilized strong $\mathrm{Be}-\mathrm{Be}$ bonds by coordinating radical ligands to $\mathrm{Be}_{2}$; however, they did not achieve shorter $\mathrm{Be}-\mathrm{Be}$ distances in these diberyllium complexes.
In 2013, Couchman et al. ${ }^{[18]}$ measured $\mathrm{Be}-\mathrm{Be}$ distances in a range of $1.945-1.978 \AA$ in computationally designed $\mathrm{NHC}^{\mathrm{R}}-\mathrm{Be}-\mathrm{Be}-\mathrm{NHC}^{\mathrm{R}}(\mathrm{NHC}=N$-heterocyclic carbenes, $\mathrm{R}=\mathrm{H}$, Me, and Ph ) complexes; however, those complexes had small HOMO-LUMO gaps, thus possibly intrinsically unstable. As beryllium atom is highly electron deficient, it is possible that addition of bridging groups between two beryllium atoms can realize shorter $\mathrm{Be}-\mathrm{Be}$ distances and enhance the stability of diberyllium complexes simultaneously. Through this strategy diberyllium complexes with ultrashort $\mathrm{Be}-\mathrm{Be}$ distances were computationally and experimentally studied ${ }^{[15,19-22]}$. Yuan et al. ${ }^{[20]}$ obtained a Be-Be distance of $1.829 \AA$ in $\mathrm{NHC}^{\mathrm{H}}-\mathrm{Be}_{2} \mathrm{H}_{2}-$ $\mathrm{NHC}^{\mathrm{H}}$ by adding two bridging hydrogen atoms in $\mathrm{NHC}^{\mathrm{H}}-\mathrm{Be}-\mathrm{Be}-\mathrm{NHC}^{\mathrm{H}}$. Qin et al. ${ }^{[21]}$ further introduced a $-\mathrm{CH}_{2}-$ group and managed an ultrashort $\mathrm{Be}-\mathrm{Be}$ distance of $1.770-1.794 \AA$ in newly designed $\mathrm{L}-\mathrm{Be}_{2} \mathrm{H}_{2} \mathrm{CH}_{2}-$ $\mathrm{L}\left(\mathrm{L}=\mathrm{NHC}^{\mathrm{H}}, \mathrm{NH}_{3}, \mathrm{PH}_{3}\right)$ complexes. Zhao et al. ${ }^{[22]}$ found that $D_{3 h} \mathrm{Be}_{2} \mathrm{H}_{3}+$ possessed a Be-Be distance below $1.700 \AA$, and simulated a triple bond in $\left[\mathrm{L}-\mathrm{Be}_{2} \mathrm{H}_{3}-\mathrm{L}\right]^{+}\left(\mathrm{L}=\mathrm{NH}_{3}, \mathrm{PH}_{3}\right.$, and $\left.\mathrm{Ne}-\mathrm{Xe}\right)$ complexes with ultrashort $\mathrm{Be}-\mathrm{Be}$ distances between 1.692 A and 1.735 A , comparable to lengths of quintuple $\mathrm{Cr}-\mathrm{Cr}$ bonds.
It was pondered the possibility of stabilizing the $D_{3 h} \mathrm{Be}_{2} \mathrm{H}_{3}+$ and meanwhile protecting its ultrashort $\mathrm{Be}-\mathrm{Be}$ distance by other ligands. Compared with the long-studied NHCs ligands, mesoionic carbenes (MICs) are considered as stronger $\sigma$-donors and less good $\pi$-acceptors ${ }^{[23-25]}$. It is unknown if there will be difference when MICs coordinate to $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$. To answer this question, a family of diberyllium complexes were designed to consist of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$and NHCs or MICs ligands, including 1,3-dimethylimidazol-2-ylidenes ( $\mathrm{NHC}_{1}^{\mathrm{Me}}$ ), 1,4-dimethyl-1,2,4-triazol-5-ylidenes $\left(\mathrm{NHC}_{2}^{\mathrm{Me}}\right)$, imidazoline-4-ylidenes ( $\mathrm{MIC}_{1}$ ), pyrazoline-4-ylidenes ( $\mathrm{MIC}_{2}$ ), 1,2,3-triazol-5-ylidenes $\left(\mathrm{MIC}_{3}\right)$ and tetrazol-5-ylidenes ( $\mathrm{MIC}_{4}$ ) (Figure S 1 in Supporting Information), investigated by density functional theory. Calculations showed that diberyllium complexes bearing carbene ligands possessed ultrashort Be-Be distances of $1.754-1.779 \AA$ and super strong Be- $\mathrm{C}_{\text {carb }}$ bonds at once, and these complexes were highly stable with large HOMO-LUMO gaps and high dissociation energies and could be potential targets in future experiments.

## 2. Computational Methods

A family of diberyllium complexes $\left[\mathrm{L}-\mathrm{BeH}_{3} \mathrm{Be}-\mathrm{L}\right]^{+}(\mathrm{L}=$ NHCs, MICs $)$ were studied by the density functional theory. All structures were optimized and characterized as stationary points at B3LYP ${ }^{[26-30]}$ level of theory using $6-311+\mathrm{G}(\mathrm{d}, \mathrm{p})^{[31,32]}$ basis set and re-optimized at B3LYP/cc-pVTZ ${ }^{[33,34]}$ level unless otherwise specified. Vertical electron affinities (VEAs) and vertical detachment energies (VDEs) were calculated at B3LYP/cc-pVTZ level. Adaptive Natural Density Partitioning (AdNDP) ${ }^{[35]}$ analyses were completed at B3LYP $/ 6-31 G(d){ }^{[36-39]}$ level. Geometry optimizations, frequency calculations, and Natural Bond Orbital (NBO) ${ }^{[40]}$ calculations were completed by Gaussian 09 package ${ }^{[41]}$. AdNDP analysis and Charge Decomposition Analysis (CDA) $)^{[42-44]}$ were performed by Multiwfn ${ }^{[45]}$. Balsac ${ }^{[46]}$ and $\mathrm{VMD}^{[47]}$ software was used for visualization and analysis of molecular geometries and electronic structures.

## 3. Results and Discussion

### 3.1. Molecular Geometries

First of all, the chosen computational method was validated by optimizing a $D_{2 h} \mathrm{NHC}^{\mathrm{H}}-\mathrm{BeH}_{2} \mathrm{Be}-$ $\mathrm{NHC}^{\mathrm{H}}$ complex. As in Figure 1, the calculated $\mathrm{Be}-\mathrm{Be}, \mathrm{Be}-\mathrm{H}$ and $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ distances were $1.830 \AA, 1.434$ $\AA$, and $1.676 \AA$, respectively, almost identical to those obtained by a $\operatorname{CCSD}(\mathrm{T}) \operatorname{method}^{[22]}$. Wiberg Bond Indexes (WBIs) for $\mathrm{Be}-\mathrm{Be}, \mathrm{Be}-\mathrm{H}$ and $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bonds, and NBO charges on the $-\mathrm{BeH}_{2} \mathrm{Be}-$ core and carbene center ( $\mathrm{C}_{\text {carb }}$ ) were closed to results obtained by higher level calculations ${ }^{[22]}$. Overall, this chosen level of theory was reliable.

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\mathrm{WBI}_{\mathrm{Be}-\mathrm{Be}}=0.78, \mathrm{WBI}_{\mathrm{Be}-\mathrm{H}}=0.47, \mathrm{WBI}_{\mathrm{Be}-\mathrm{C}}=0.85
$$



Figure 1. Selected geometrical parameters ofNHC ${ }^{H}-\mathrm{BeH}_{2} \mathrm{Be}-\mathrm{NHC}^{H}$ complexes obtained at B3LYP/ccpVTZ level. Unit for bond length was angstrom $(\AA)$, and for angle was degree $\left({ }^{\circ}\right)$. NBO charges at $\mathrm{C}_{\text {carb }}$, Be , and H atoms were in italic.

Figure 2 showed the optimized structures of diberyllium complexes $\left[\mathrm{L}-\mathrm{BeH}_{3} \mathrm{Be}-\mathrm{L}\right]^{+}(\mathrm{L}=$ NHCs and MICs), in which the $-\mathrm{BeH}_{3} \mathrm{Be}$ - core was coordinated by two carbene ligands. The molecular geometries of all complexes were in $C_{2}$ symmetry. The Be-Be distance varied from $1.754 \AA$ to $1.779 \AA$, much shorter than those in $\mathrm{NHC}^{\mathrm{H}}-\mathrm{Be}-\mathrm{Be}-\mathrm{NHC}^{\mathrm{H}[18]}$ and $\mathrm{NHC}^{\mathrm{H}}-\mathrm{BeXBe}-\mathrm{NHC}^{\mathrm{H}}\left(\mathrm{X}=\mathrm{H}_{2}, \mathrm{H}_{2} \mathrm{CH}_{2}\right)^{[20,22]}$. In particular, A and G had the shortest Be-Be distance of $1.754 \AA$ among all complexes, while E had the longest $\mathrm{Be}-\mathrm{Be}$ bond $(1.779 \AA)$. The individual average length of six $\mathrm{Be}-\mathrm{H}$ bonds in complexes $\mathrm{A}^{\sim} \mathrm{G}$ varied from $1.478 \AA$ to 1.488 $\AA$, slightly longer than in a free $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}\left(1.453 \AA\right.$, Figure S2), suggesting the $\mathrm{Be}-\mathrm{H}$ bond in $-\mathrm{BeH}_{3} \mathrm{Be}-$ core got weakened by carbene ligands coordinated to it. The calculated $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bond length, ranging from 1.732 $\AA$ to $1.745 \AA$, was compatible to experimental values ${ }^{[48]}$. Among all complexes E owned the shortest $\mathrm{Be}-$ $\mathrm{C}_{\text {carb }}$ bond, followed by D and F , demonstrating stronger $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bonds. Compared with corresponding free carbenes, the $\angle \mathrm{X}-\mathrm{C}_{\text {carb }}-\mathrm{Y}(\mathrm{X}, \mathrm{Y}=\mathrm{C}, \mathrm{N})$ in diberyllium complexes increased by $2.4^{\circ}-3.0^{\circ}$ with a maximum bond length change of $\pm 0.02 \AA$. C-N bond lengths of the complexes ranged from $1.293 \AA$ to $1.397 \AA$, between the lengths of C-N single and double bonds ( $1.476 \AA$ and $1.291 \AA$, respectively ${ }^{[49]}$ ), and C-C bond lengths varied from $1.353 \AA$ to $1.398 \AA$, between the lengths of C-C single and double bonds ( $1.510 \AA$ and $1.336 \AA$, respectively ${ }^{[50]}$ ), suggesting high conjugation of the carbene ligands in these diberyllium complexes.
Figure 2. Optimized structures and selected geometrical parameters of diberyllium complexes A~G. Bond length unit: angstrom $(\AA)$, angle unit: degree $\left({ }^{\circ}\right)$. For each complex, length with a bar was an average value of six $\mathrm{Be}-\mathrm{H}$ bonds.

### 3.2. Chemical Bonding Analysis

AdNDP analysis ${ }^{[35]}$ was conducted for complexes A, E and G that had extremums of the Be-Be distance to have a better understanding of chemical bonding. Based on an electron-pair bonding model, the AdNDP describes the electronic structure of a molecule in terms of $n$ center-two electrons ( $n \mathrm{c}-2 \mathrm{e}$ ) orbitals or bonds, covering both Lewis bonding elements and delocalized bonding elements. In this work two equivalent schemes were used to generate AdNDP orbitals: a small $n$-value for delocalized bonding elements in Scheme 1, and a large $n$ in Scheme 2. Using Schemes 1 and 2, AdNDP analysis generated identical 1c-2e lone pair electrons and $2 \mathrm{c}-2 \mathrm{e} \sigma$-orbitals, and meanwhile, found two $\mathrm{Be}-\mathrm{C}_{\text {carb }} 2 \mathrm{c}-2 \mathrm{e} \sigma$-orbitals in all three complexes. In A and G , the occupation number (ON) is $1.96|\mathrm{e}|$ for both two $\mathrm{Be}-\mathrm{C}_{\text {carb }} 2 \mathrm{c}$ - $2 \mathrm{e} \sigma$-orbitals (Figure 3 and S3). The short $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bond ( $1.732 \AA$ ) in E suggested strong covalent interaction between Be and $\mathrm{C}_{\text {carb }}$ atoms, while E had a smaller ON of $1.93 \mid \mathrm{e}$ for $\mathrm{Be}-\mathrm{C}_{\text {carb }} 2 \mathrm{c}$-2e $\sigma$-orbitals, which demonstrated these bonds were influenced not only by covalent interaction but also by electrostatic interaction. For the delocalized bonding elements AdNDP generated three $\mathrm{Be}-\mathrm{H}-\mathrm{Be} \sigma$-orbitals with an ON of $1.98|\mathrm{e}|$ for the three complexes employing Scheme

1, and Scheme 2 provided one $\mathrm{Be}-\mathrm{H}_{3}-\mathrm{Be} 5 \mathrm{c}-2 \mathrm{e} \sigma$-orbital with an ON of $1.98|\mathrm{e}|$ and two $5 \mathrm{c}-2 \mathrm{e} \mathrm{Be}-\mathrm{H}_{3}-\mathrm{Be}$ $\pi$-orbitals with ONs of $1.99|\mathrm{e}|$ and $1.98|\mathrm{e}|$ (Figure 3 ). The three $5 \mathrm{c}-2 \mathrm{e}$ orbitals can be considered as a virtual triple bond ${ }^{[22]}$. Schemes 1 and 2 were equivalent as combination of three $3 c-2 e \sigma$-orbitals afforded the $5 c-2 e$ $\sigma$-orbital, and combination of two $3 \mathrm{c}-2 \mathrm{e} \sigma$-orbitals afforded the $5 \mathrm{c}-2 \mathrm{e} \pi$-orbitals.

## Scheme 1



Two 2c-2e $\sigma$-bonds $\mathrm{ON}=1.96|\mathrm{e}|$


Three 3 c -2e $\sigma$-bonds $\mathrm{ON}=1.98|\mathrm{e}|$

## Scheme 2



Two 2 c -2e $\sigma$-bonds $\mathrm{ON}=1.96|\mathrm{e}|$


One 5 c -2e $\sigma$-bond
$\mathrm{ON}=1.98|\mathrm{e}|$

Two 5 c -2e $\pi$-bonds
$\mathrm{ON}=1.99|\mathrm{e}| / 1.98|\mathrm{e}|$

Figure 3. The AdNDP-generated $n c-2 e$ orbitals relating to beryllium atoms employing Schemes 1 and 2. Similar AdNDP-orbitals for E and G were presented in Figure S3.

To characterize the covalent and electrostatic interaction in the diberyllium complexes, WBIs and NBO charges were analyzed. As listed in Table 1, the total WBI of every $\mathrm{C}_{\text {carb }}$ atom $\left(\mathrm{WBI}_{C_{\text {carb }}}\right)$ in the complexes was significantly larger than those of the corresponding free carbenes, so as to support the formation of Be- $\mathrm{C}_{\text {carb }} \sigma$-bonds. The total WBI of every beryllium atom $\left(\mathrm{WBI}_{\mathrm{Be}}\right)$ varied from 2.72 to 2.77 , and beryllium atom had a valence of two. The exceeding numbers ( $0.72-0.77$ ) came from the electron donation of carbene center, suggesting $\mathrm{Be}-\mathrm{C}_{\text {carb }} \sigma$-bonds are dative. Among all complexes E had the smallest $\mathrm{WBI}_{B e-C_{\text {carb }}}$ value of 0.67 , suggesting the weakest covalent interaction between Be and $\mathrm{C}_{\text {carb }}$ atoms, which agreed with the results of AdNDP analysis, while complexes $\mathrm{A}^{\sim} \mathrm{E}$ had a largerWBI $\mathrm{Be}_{B e-C_{c a r b}}$ value of 0.70 , indicating strong covalent interactions.

Table 1. The Wiberg Bond Indexes (WBIs) of selected interatomic interaction ( $\mathrm{Be}-\mathrm{Be}, \mathrm{Be}-\mathrm{H}$, and $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ ) and atoms ( $\mathrm{Be}, \mathrm{H}$ and $\mathrm{C}_{\text {carb }}$ ), and selected NBO charges ( $q$, in $|\mathrm{e}|$ ) for $D_{3 h} \mathrm{Be}_{2} \mathrm{H}_{3}+$ and complexes $\mathrm{A}^{\sim} \mathrm{G}$. For the complexes, WBIs presented for $\mathrm{Be}-\mathrm{H}$ interaction and H atoms were average values, as is NBO charges on the H atoms $\left(q_{\mathrm{H}}\right)$.

|  | WBI | WBI | WBI | WBI | WBI | WBI | $q$ | $q$ | $q$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $\mathrm{Be}-\mathrm{Be}$ | $\mathrm{Be}-\mathrm{H}$ | Be- $C_{\text {carb }}$ | Be | H | $C_{\text {carb }}{ }^{\text {a }}$ | Be | H | $C_{\text {carb }}$ |
| $\mathrm{Be}_{2} \mathrm{H}_{3}+$ | 0.46 | 0.47 | - | 1.87 | 0.95 | - | +0.84 | -0.23 | - |
| A | 0.58 | 0.48 | 0.70 | 2.77 | 0.99 | $3.61(2.85)$ | +0.21 | -0.11 | +0.15 |
| B | 0.56 | 0.48 | 0.70 | 2.77 | 0.99 | $3.62(2.86)$ | +0.21 | -0.12 | +0.14 |
| C | 0.57 | 0.48 | 0.70 | 2.77 | 0.99 | $3.62(2.86)$ | +0.21 | -0.12 | +0.14 |
| D | 0.55 | 0.47 | 0.69 | 2.74 | 0.99 | $3.67(3.02)$ | +0.23 | -0.13 | -0.17 |
| E | 0.55 | 0.47 | 0.67 | 2.72 | 0.99 | $3.74(3.24)$ | +0.25 | -0.14 | -0.44 |
| F | 0.56 | 0.48 | 0.68 | 2.74 | 0.99 | $3.68(3.02)$ | +0.24 | -0.13 | -0.16 |
| G | 0.57 | 0.48 | 0.68 | 2.75 | 0.99 | $3.63(2.91)$ | +0.23 | -0.12 | +0.09 |

${ }^{\text {a }}$ NBO charges at $\mathrm{C}_{\text {carb }}$ atoms for free carbenes were in parentheses.
Electrostatic interaction between beryllium and its neighboring carbene center was characterized by NBO charges. As in Table 1, the NBO charges on each beryllium atom $\left(q_{\mathrm{Be}}\right)$ in the complexes varied from $+0.21|\mathrm{e}|$ to $+0.25|\mathrm{e}|$, considerably smaller than $q_{\mathrm{Be}}$ in the free $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}(+0.84|\mathrm{e}|)$, which could be attributed to the electron-donation from carbenes to the $-\mathrm{BeH}_{3} \mathrm{Be}-$ core. Among all complexes the carbine center of E was the most negatively charged $\left(q_{C_{\text {carb }}}=-0.44|\mathrm{e}|\right)$, and strong electrostatic attraction between Be and $\mathrm{C}_{\text {carb }}$ atoms would strengthen this weak covalent interaction to create a short $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bond ( $1.732 \AA$ ). The $\mathrm{C}_{\text {carb }}$ atom was less negatively charged in D and F , and as a result, the electrostatic attraction between Be and $\mathrm{C}_{\text {carb }}$ atoms decreased. In $\mathrm{A}^{\sim} \mathrm{C}$ and G , the carbene center was positively charged, and the covalent interaction between Be and $\mathrm{C}_{\text {carb }}$ atoms got cancelled by electrostatic repulsion. With the same $\mathrm{WBI}_{B e-C_{\text {carb }}}$ value (0.68), F possesses $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bond length of $1.735 \AA$ because of the favorable electrostatic attraction between Be and $\mathrm{C}_{\text {carb }}$ atoms, while G had a longer bond length $(1.745 \AA$ ) caused by electrostatic repulsion. A C had a larger $\mathrm{WBI}_{B e-C_{c a r b}}$ value (0.70) than others; however, the strong covalent interaction between Be and $\mathrm{C}_{\text {carb }}$ atoms was neutralized by the interatomic electrostatic repulsion, resulting in a $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bond length of 1.741-1.745 $\AA$.
The $\mathrm{WBI}_{\mathrm{Be}-\mathrm{Be}}$ values for all complexes were $0.55-0.58$, reflecting orbital overlapping between the two Be atoms. For complex E with the smallest $\mathrm{WBI}_{\mathrm{Be}-\mathrm{Be}}$ (0.55), weak $\mathrm{Be}-\mathrm{Be}$ orbital overlapping matched the small ON of $\mathrm{Be}-\mathrm{H}-\mathrm{Be} 3 \mathrm{c}-2 \mathrm{e} \sigma$-bonds calculated by the AdNDP analysis, while A and G with large $\mathrm{WBI}_{\mathrm{Be}-\mathrm{Be}}$ had a much shorter $\mathrm{Be}-\mathrm{Be}$ distance of $1.754 \AA$. The average values of $\mathrm{WBI}_{\mathrm{Be}-\mathrm{H}}$ of all complexes were between 0.47 and 0.48 , and the total WBI value of individual H atom was close to 1 , reflecting that bridging H atoms linked two Be atoms in $-\mathrm{BeH}_{3} \mathrm{Be}-$ core to form multiple bonding orbitals.

### 3.3. Orbital Analysis

Charge decomposition analysis (CDA) ${ }^{[42-44]}$ was conducted to understand the interaction between the $\mathrm{BeH}_{3} \mathrm{Be}$ - core and carbene ligands. The CDA constructed molecular orbitals (MOs) of a complex in terms of a linear combination of the donor and acceptor fragmental orbitals (FOs). Selected MOs of A that related to beryllium atoms and decomposition of these MOs into FOs of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$and $\left(\mathrm{NHC}^{\mathrm{H}}\right)_{2}$ were presented in Figure 4 a and 4 b , respectively. The low-lying HOMO-30 and HOMO-29 of A represented $\mathrm{Be}-\mathrm{Be} \sigma$ - bonding and antibonding orbitals, respectively, and were obviously contributed by 1 s orbitals of two Be atoms, corresponding to FO 1 and FO 2 of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$(Figure S4). As HOMO-30 and HOMO-29 were far below other selected MOs of A, they were not included in Figure 4b for brevity. HOMO- 8 were the $\mathrm{Be}-\mathrm{H}_{3}-\mathrm{Be} \sigma$-bonding orbital contributed by the FO 3 of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$. HOMO-7 and HOMO-6 pictured $\mathrm{Be}-\mathrm{C}_{\text {carb }} \sigma$-bonding orbitals, which were attributed to the electron donation from carbene ligands to the unoccupied FO6 and FO7 of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$, respectively. HOMO-3 ${ }^{\sim} \mathrm{HOMO}$ of A were two sets of $\pi$-orbitals, representing $\mathrm{Be}-\mathrm{H}-\mathrm{Be} \pi$-bonding, and generated by the combination of $\mathrm{FO} 4 / \mathrm{FO} 5$ of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$and $\pi$-orbitals of $\left(\mathrm{NHC}^{\mathrm{H}}\right)_{2}$ fragments (FO33 and FO34). The two lowest unoccupied MOs (LUMO and LUMO+1) of A that represented the $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ $\pi$-bonding were established by two degenerated $\mathrm{Be}-\mathrm{Be} \pi$-antibonding orbitals ( FO 8 and FO 9 of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$) and $\pi$-orbitals of carbene ligands (FO41 and FO 42 of $\left.\left(\mathrm{NHC}^{\mathrm{H}}\right)_{2}\right)$. Similar pattern was found in the occupied

MOs of other complexes as well, related to the FOs of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$(E and G as examples in Figure S4); however, $\mathrm{LUMO} / \mathrm{LUMO}+1$ of E and G were pure $\pi$-orbitals of carbene ligands and irrelevant to FO8 and FO9 of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$.

There was a link between the occupied MOs and the AdNDP-generated orbitals of A. As in Figures 3 and 4, the two Be- $\mathrm{C}_{\text {carb }} 2 \mathrm{c}-2 \mathrm{e} \sigma$-orbitals were combined to generate HOMO-7 and HOMO-6, and HOMO8 was related to the $5 \mathrm{c}-2 \mathrm{e} \mathrm{Be}-\mathrm{H}_{3}-\mathrm{Be} \sigma$-orbital generated employing Scheme 2, while HOMO-3~HOMO corresponded to the $5 \mathrm{c}-2 \mathrm{e} \mathrm{Be}-\mathrm{H}_{3}-\mathrm{Be} \pi$-orbitals. HOMO- 8 and HOMO- $3 \sim \mathrm{HOMO}$ can also be achieved by combination of $\mathrm{Be}-\mathrm{H}-\mathrm{Be} 3 \mathrm{c}-2 \mathrm{e} \sigma$-orbitals based on Scheme 1. The connection between MOs and AdNDPgenerated orbitals for A also demonstrated that removing electrons would destroy the multiple bonding orbitals in the $-\mathrm{BeH}_{3} \mathrm{Be}$ - core, and large detachment energies were critical to retain an ultrashort $\mathrm{Be}-\mathrm{Be}$ distance.


Figure 4. (a) Selected molecular orbitals (MOs) bounding to Be atoms for complex A, and (b) charge decomposition analysis (CDA) for these MOs. Orbital energy level unit: eV. Fragmental orbitals (FOs) of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$and $\left(\mathrm{NHC}^{\mathrm{H}}\right)_{2}$ were shifted by +2.0 eV and -5.0 eV , respectively. Occupied and unoccupied MOs/FOs were drawn in solid and dash lines, respectively, in which the one and three gaps were double and quadruple degenerate, respectively. Criterion for degeneration was set at 0.10 eV . Contributions from FOs to MOs of A were in red and italic. FO37-FO40 of $\left(\mathrm{NHC}^{\mathrm{H}}\right)_{2}$ were not presented as their contributions to MOs of A were less than $10 \%$. Decomposition of the low-lying HOMO-30 and HOMO-29 of A was not shown as these two MOs are pure FOs of $\mathrm{Be}_{2} \mathrm{H}_{3}{ }^{+}$and far below other selected MOs.

### 3.4. Stability Analysis

Complex stability was evaluated based on calculation of their HOMO-LUMO gaps and dissociation energies of losing two carbene moieties in the reaction of $\left[L-B e H_{3} B e-L\right]^{+} \rightarrow \mathrm{Be}_{2} H_{3}{ }^{+}+2 L$. As in Table 2, the HOMO-LUMO gaps of the seven complexes ranged from 5.58 eV to 6.75 eV , much larger than the $\mathrm{E}_{\mathrm{G}}$ of $\mathrm{NHC}^{\mathrm{Me}}-\mathrm{Be}-\mathrm{Be}-\mathrm{NHC}^{\mathrm{Me}}(0.51 \mathrm{eV})^{[18]}$ and $\mathrm{NHC}^{\mathrm{H}}-\mathrm{BeH}_{2} \mathrm{Be}-\mathrm{NHC}^{\mathrm{H}}(1.78 \mathrm{eV}){ }^{[21]}$, and these complexes exhibited high stability with super strong $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bonds dissociation energies (BDEs) of which ranged from $184.9 \mathrm{kcal} / \mathrm{mol}$ to $239.0 \mathrm{kcal} / \mathrm{mol}$, suggesting these complexes could be potential targets in future experiments. The stability study was also confirmed by vertical detachment energies (VDEs, between 10.4
to 12.3 eV ) and vertical electron affinities (VEAs, between 2.4 and 3.8 eV ), which indicated that it would be difficult to remove or gain even one additional electron in these diberyllium complexes.
Table 2. The HOMO-LUMO gaps $\left(\mathrm{E}_{\mathrm{G}}, \mathrm{eV}\right)$, bond dissociation energies (BDEs, kcal/mol), VEAs and VDEs (eV) for $\mathrm{A}^{\sim} \mathrm{G}$.

|  | $\mathrm{E}_{\mathrm{G}}$ | BDEs | VEAs | VDEs |
| :--- | :--- | :--- | :--- | :--- |
| A | 6.50 | 193.3 | 2.7 | 11.9 |
| B | 6.43 | 197.6 | 2.6 | 11.4 |
| C | 6.75 | 184.9 | 3.1 | 12.3 |
| D | 5.89 | 225.3 | 2.4 | 10.5 |
| E | 5.59 | 239.0 | 2.5 | 10.4 |
| F | 5.86 | 210.8 | 3.1 | 11.3 |
| G | 5.58 | 194.7 | 3.8 | 12.2 |

## 4. Conclusion

In this work, a family of diberyllium complexes $\left[\mathrm{L}-\mathrm{BeH}_{3} \mathrm{Be}-\mathrm{L}\right]^{+}(\mathrm{L}=\mathrm{NHCs}, \mathrm{MICs})$ were computationally designed with a $-\mathrm{BeH}_{3} \mathrm{Be}-$ core supported by NHC and MIC ligands. The density functional theory studies showed these complexes possessed ultrashort Be-Be distances of $1.754-1.779 \AA$ and super strong Be- $\mathrm{C}_{\text {carb }}$ bonds. Electronic structure analysis demonstrated the ultrashort Be-Be distance was attributed to the multiple bonding orbitals in the $-\mathrm{BeH}_{3} \mathrm{Be}-$ core and the direct orbital overlapping between the two Be atoms. The strong $\mathrm{Be}-\mathrm{C}_{\text {carb }}$ bonds originated from the electron donation of two carbene ligands coordinated to the $-\mathrm{BeH}_{3} \mathrm{Be}$ - core, influenced by the electrostatic interaction between Be and its neighboring carbene center. These complexes were highly stable because of the large HOMO-LUMO gaps and high dissociation energies, high VDEs and low VEAs, and could be potential targets in future.

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Scheme 1


Two 2c-2e $\sigma$-bonds $\mathrm{ON}=1.96|\mathrm{e}|$


Three 3c-2e $\sigma$-bonds $\mathrm{ON}=1.98|\mathrm{e}|$

## Scheme 2



Two 2 c - $2 \mathrm{e} \sigma$-bonds $\mathrm{ON}=1.96|\mathrm{e}|$


One $5 \mathrm{c}-2 \mathrm{e} \sigma$-bond $\mathrm{ON}=1.98|\mathrm{e}|$

Two 5 c -2e $\pi$-bonds
$\mathrm{ON}=1.99|\mathrm{e}| 1.98|\mathrm{e}|$


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