Biennial-Aligned Lunisolar-Forcing of ENSO: Implications for Simplified Climate Models

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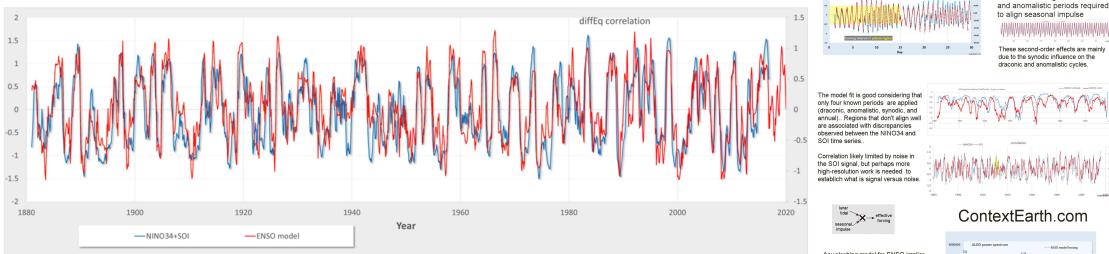
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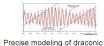
Abstract

By solving Laplace's tidal equations along the equatorial Pacific thermocline, assuming a delayed-differential effective gravity forcing due to a combined lunar+solar (lunisolar) stimulus, we are able to precisely match ENSO periodic variations over wide intervals. The underlying pattern is difficult to decode by conventional means such as spectral analysis, which is why it has remained hidden for so long, despite the excellent agreement in the time-domain. What occurs is that a non-linear seasonal modulation with monthly and fortnightly lunar impulses along with a biennially-aligned "see-saw" is enough to cause a physical aliasing and thus multiple folding in the frequency spectrum. So, instead of a conventional spectral tidal decomposition, we opted for a time-domain cross-validating approach to calibrate the amplitude and phasing of the lunisolar cycles. As the lunar forcing consists of three fundamental periods (draconic, anomalistic, synodic), we used the measured Earth's length-of-day (LOD) decomposed and resolved at a monthly time-scale [1] to align the amplitude and phase precisely. Even slight variations from the known values of the long-period tides will degrade the fit, so a high-resolution calibration is possible. Moreover, a narrow training segment from 1880-1920 using NINO34/SOI data is adequate to extrapolate the cycles of the past 100 years (see attached figure). To further understand the biennial impact of a yearly differential-delay, we were able to also decompose using difference equations the historical sea-level-height readings at Sydney harbor to clearly expose the ENSO behavior. Finally, the ENSO lunisolar model was validated by back-extrapolating to Unified ENSO coral proxy (UEP) records dating to 1650. The quasi-biennial oscillation (QBO) behavior of equatorial stratospheric winds derives following a similar pattern to ENSO via the tidal equations, but with an emphasis on draconic forcing. This improvement in ENSO and QBO understanding has implications for vastly simplifying global climate models due to the straightforward application of a well-known and well-calibrated forcing. [1] Na, Sung-Ho, et al. "Characteristics of Perturbations in Recent Length of Day and Polar Motion." Journal of Astronomy and Space Sciences 30 (2013): 33-41.

221914: Biennial-Aligned Lunisolar-Forcing of ENSO: Implications for Simplified Climate Models Paul Pukite, Context/Earth puk@umn.edu, @whut



It's well known that lunar gravitational forces lead to ocean tides and deep ocean mixing, but why not the oscillation in the equatorial Pacific Ocean thermocline? If a seasonal impulse that exaggerates the draconic and anomalistic lunar cycles is applied to Laplace's tidal equations, the result shown above is obtained. Model is very similar to conventional tidal analysis but operates on a long-period basis due to the seasonal impulse influence.



Any sloshing model for ENSO implies angular momentum changes. The forcing for the ENSO model aligns perfectly with measured LOD-based changes in the earth's anaular momentum

Laplace developed his namesake tidal equations to mathematically explain the behavior of tides by applying straightforward Newtonian physics. In their expanded form, known as the primitive equations, Laplace's starting formulation is used as the basis of almost all detailed climate models. The concise derivation for a model of ENSO depends on reducing Laplace's tidal equations along the equator.

$AZ(t) + \frac{1}{\alpha cont(\alpha t)} \times \frac{\partial}{\partial t} \frac{Z'(t)}{\alpha cont(\alpha t)} = 0$ infruite as and local take & discrimina- $\frac{\partial v}{\partial x} = \cosh(\sqrt{A} \sum_{i=1}^{d=N} k_i \sin(\omega_i t) + \theta_0)$ $\frac{d}{d}(\operatorname{sec(t,\omega)} Z'(t)) + A \omega^2 \cos(t,\omega) Z(t) = 0$ $\left[\frac{1}{\alpha \cos(\omega)} \left[\frac{\partial}{\partial 1}(uD) + \frac{\partial}{\partial z}(vD\cos(\omega))\right] = 0$ $Z(t) = c_2 \sin(\sqrt{A} \sin(t\omega)) + c_1 \cos(\sqrt{A} \sin(t\omega))$ $\frac{\partial u}{\partial t} - v \left(2\Omega \sin(\varphi)\right) + \frac{1}{a \cos(\varphi)} \frac{\partial}{\partial \lambda} \left(g\zeta + U\right) = 0,$ vet 2 : Deriving the Junar foreing period $\frac{\partial v}{\partial u} + u (2\Omega \sin(\varphi)) + \frac{1}{2} \frac{\partial}{\partial u} (g\zeta + U) = 0,$ $\frac{\partial \zeta}{\partial z} = \frac{\partial \zeta}{\partial t} \frac{\partial t}{\partial z}$ $L(t) = k \cdot sin(\omega_L t + \phi)$ $\frac{\partial u}{\partial t} + \frac{1}{g} \frac{\partial}{\partial \lambda} (g\zeta + U) = 0,$ $s(t) = \sum_{i=1}^{n} a_i \sin(2\pi t i + \theta_i)$ $A\zeta(t) + \frac{1}{2k} \cdot \frac{\partial}{\partial t} \frac{\zeta'(t)}{2k} = 0$ $\frac{\partial v}{\partial t} + \frac{1}{a} \frac{\partial}{\partial x} (g\zeta + U) = 0,$ $a \frac{\partial^2 \zeta}{\partial M} + \frac{\partial}{\partial H} \left[\frac{\partial}{\partial Y} (uD) + \frac{\partial}{\partial x_0} (vD) \right] = 0$ $\frac{\partial \varphi}{\partial u} = \sum_{i=N}^{i=N} k_i \omega_i \cos(\omega_i t)$

 $a\frac{\partial^{2}\zeta}{\partial \theta^{2}} + D\left[\frac{\partial}{\partial \lambda}(\frac{\partial u}{\partial \theta}) + \frac{\partial}{\partial u}(\frac{\partial v}{\partial \theta})\right] = 0,$

 $\frac{\partial u}{\partial u} = -\frac{1}{2} \frac{\partial}{\partial x} (g\zeta + U)$ $\frac{\partial v}{\partial t} = -\frac{1}{\pi} \frac{\partial}{\partial x} (g\zeta + U)$

 $a^2 \frac{\partial^2 \zeta}{\partial t^2} - D \left[\frac{\partial}{\partial \lambda} (\frac{\partial}{\partial \lambda} (g\zeta + U)) + \frac{\partial}{\partial x} (\frac{\partial}{\partial x} (g\zeta + U)) \right] = 0$

is the similar model, SW(a) share a is a second other $\cos(\sqrt{A}\sum_{i=1}^{i=N}k_i\sin(\omega_i t) + \theta_0)$ $\frac{\partial^2 \zeta}{\partial t^2} - D\left[(SW(s)\zeta) + \frac{\partial}{\partial \varphi} (\frac{\partial}{\partial \varphi} (g\zeta + U)) \right] = 0$

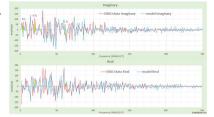
require a rework to the closed-form solution. The Part 1 derivation provides the closed-form natural response $F(t) \propto -\frac{a^{\prime}(t)+d^{\prime}(t)}{P_{0,t,\alpha}(t)+d^{\prime}(t)}$

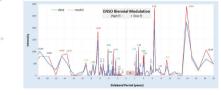
 $\zeta(t) = \sin(\sqrt{A}\sum k_i \sin(\omega_i t) + \theta_0)$ $f(t) = k \sum_{i=1}^{n} a_i \sin(\omega_L t + \phi) \sin(2\pi t i + \theta_i)$

 $sin(x)sin(y) = \frac{1}{2}(cos(x - y) - cos(x + y))$ adiabatic process, with the phase being the internal sin modulation

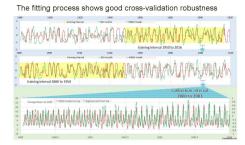
 $f(t) = k/2 \sum_{i=1}^{n} a_i \sin((\omega_L - 2\pi i)t + \psi_i) + ...$

observed sloshing in the thermocline - which can be derived from ω_{2} terms on reduced in frequency by multiples of 2π until it. the above by applying the solution to Laplace's third tidal equation

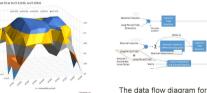




Much of tidal analysis has been performed by Fourier analysis, whereby one can straightforwardly deduce the frequency components arising from the various lunar and solar orbital factors. But in a non-linear world such as ENSO where the tidal forces interact with the seasonal cycle via modulated feedbacks the picture is guite different. What happens is that the cycles interact and get folded multiple times until what originally were three cycles (yearly plus draconic and anomalistic lunar periods) end up appearing as above. Further, most of the peak positions in Fourier space are easily related to the physical aliasing, as the biennial mode splits each peak into two paired satellite peaks (a high f and low f value)



Over-fitting is reduced by constraining the tidal cycles to match other observations such as LOD and 2nd-order shaping.



the forcing mechanism is

shown above. There are

processes that likely result

from tidal forcing, that of

QBO and the Chandler

wobble

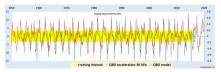
two other system-wide

A good fit is sensitive to the precise values of the draconic and tropical periods. Any deviation results in degraded correlation





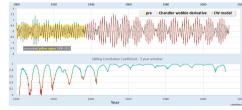
This shows excellent cross-validattion with a small training interval



The full QBO is recovered by integrating the acceleration



The Chandler wobble provides more evidence that the draconic cycle controls the angular variations, and not a resonance



f(t) = s(t)L(t)