

# Comment on “Probability Distributions of Radiocarbon in Open Linear Compartmental Systems at Steady-State” by I. Chanca, S. Trumbore, K. Macario, and C. A. Sierra

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## Abstract

Chanca et al. (2022) construct radiocarbon ( $^{14}\text{C}$ ) distributions for compartmental ecosystem models and compare them to the variability of measured  $^{14}\text{C}$  data for soil respiration. However, their  $^{14}\text{C}$  distributions do not represent a measurable quantity and may not be used to draw any conclusions on the variability of  $^{14}\text{C}$  measurements.

1 **Comment on “Probability Distributions of Radiocarbon**  
2 **in Open Linear Compartmental Systems at**  
3 **Steady-State” by I. Chanca, S. Trumbore, K. Macario,**  
4 **and C. A. Sierra**

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7 **Key Points:**

- 8 • The radiocarbon ( $^{14}\text{C}$ ) distributions proposed by Chanca et al. (2022) are not mea-  
9 surable.  
10 • The  $^{14}\text{C}$  distributions proposed by Chanca et al. (2022) are not comparable to the  
11 distributions of  $^{14}\text{C}$  measurements.  
12 • The variability of  $^{14}\text{C}$  measurements of soil respiration can not be captured with  
13 deterministic models with constant parameters.

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## Abstract

Chanca et al. (2022) construct radiocarbon ( $^{14}\text{C}$ ) distributions for compartmental ecosystem models and compare them to the variability of measured  $^{14}\text{C}$  data for soil respiration. However, their  $^{14}\text{C}$  distributions do not represent a measurable quantity and may not be used to draw any conclusions on the variability of  $^{14}\text{C}$  measurements.

## 1 Measurability of the theoretical $^{14}\text{C}$ distributions

Chanca et al. (2022) construct radiocarbon ( $^{14}\text{C}$ ) distributions based on the age distributions of linear compartmental ecosystem models at steady state, where the “age” of a carbon atom is the time elapsed since the atom entered the system. The  $^{14}\text{C}$  distribution is created by associating each age in the age distribution to the decay-corrected  $\Delta^{14}\text{C}$  (a normalized, standardized measure of  $^{14}\text{C}$  content) of atmospheric  $\text{CO}_2$  at the time when the carbon atom entered the simulated system from the atmosphere (e.g. through photosynthesis). By definition, the random variable associated with the age distribution is the age of a randomly sampled carbon atom. Therefore, by extension, the random variable associated with the  $^{14}\text{C}$  distribution is the  $\Delta^{14}\text{C}$  of a randomly sampled carbon atom, or alternatively, the decay-corrected atmospheric  $\Delta^{14}\text{C}$  at the time when the randomly sampled carbon atom entered the system. However, it does not make sense to measure the  $\Delta^{14}\text{C}$  for one single carbon atom, since  $\Delta^{14}\text{C}$  can only be measured as the ratio between  $^{14}\text{C}$  and the stable carbon isotopes, thus requiring a sample of many atoms. Therefore, the theoretical  $^{14}\text{C}$  distributions are not measurable.

## 2 Comparing measured and theoretical $^{14}\text{C}$ distributions

Chanca et al. (2022) directly compare the means, modes, and standard deviations of their theoretical  $\Delta^{14}\text{C}$  distribution and the distribution of  $\Delta^{14}\text{C}$  measurements of  $\text{CO}_2$  outflux from soils. They observe that the measured distribution looks quite different from their theoretical distribution: even though the two distributions generally have the same mean, the measured distribution looks more unimodal, and its standard deviation is around 10 times smaller than that of the theoretical  $\Delta^{14}\text{C}$  distribution. Chanca et al. (2022) claim that the theoretical distribution in part explains the variability in the observations. However, we can not expect  $\Delta^{14}\text{C}$  measurements to depend on anything but the mean of the theoretical distribution. Modern accelerator mass spectrometry (AMS) instruments require at least  $10^{18}$  carbon atoms (or  $20\text{ }\mu\text{g}$  of carbon) to perform precise  $\Delta^{14}\text{C}$  measurements (Melchert et al., 2019). With such a large number of carbon atoms, we are bound to capture a wide range of ages in our sample, so we end up measuring a weighted average of past atmospheric  $\Delta^{14}\text{C}$  values (corrected for radioactive decay), thus creating a new, distinct  $\Delta^{14}\text{C}$  distribution. Furthermore, assuming the atoms in our carbon samples are random independent samples of the age distribution, the resulting measured  $\Delta^{14}\text{C}$  distribution becomes independent of the spread and shape of the theoretical  $\Delta^{14}\text{C}$  distribution. It is therefore inappropriate to compare the standard deviations and modes of the theoretical and measured  $\Delta^{14}\text{C}$  distributions.

## 3 Causes for the variability in $^{14}\text{C}$ measurements

Besides errors introduced during sample processing and measurement, the most important sources of variability in  $\Delta^{14}\text{C}$  measurements of pedogenic systems are small-scale spatial heterogeneity and temporal fluctuations (Hoffmann et al., 2017; Schöning et al., 2006; van der Voort et al., 2016), which cause the age distribution of the soil carbon outflux to be different for different samples. To correctly represent the variability of imperfect  $\Delta^{14}\text{C}$  measurements of samples which are not taken at the exact same location and at the exact same time, we would need a stochastic model with spatial and temporal res-

olution. However, Chanca et al. (2022) only use deterministic models with constant parameters (Harvard Forest model, Porce model, Emmanuel model), which are incapable of capturing the variability of  $\Delta^{14}\text{C}$  measurements.

## 4 Summary and conclusion

In this comment, we have shown that:

1. The random variable which defines the theoretical  $^{14}\text{C}$  distribution proposed by Chanca et al. (2022) does not represent a measurable quantity.
2. The variability in  $\Delta^{14}\text{C}$  measurements is not comparable to and does not depend on the shape and spread of the theoretical  $^{14}\text{C}$  distribution.
3. The actual variability of measured  $\Delta^{14}\text{C}$  cannot be captured with the models used as examples in Chanca et al. (2022).

We conclude that the theoretical  $\Delta^{14}\text{C}$  distributions do not serve a practical purpose, and that the results and conclusions in Chanca et al. (2022) which relate the theoretical  $^{14}\text{C}$  distributions to  $\Delta^{14}\text{C}$  measurements are invalid.

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