

# Spatial-temporal Bayesian hierarchical model for summer monsoon precipitation extremes over India

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## Abstract

India receives more than 80% of annual rainfall during the summer monsoon season of June – September. Extreme rainfall during summer monsoon season causes severe floods in many parts of India, annually. The floods in Kerala in 2019; Chennai during 2015 and Uttarakhand in 2013 are some of the major floods in recent years. With high population density and weaker infrastructure, even moderate precipitation extremes result in substantial loss to life and property. Thus, understanding and modeling the return levels of extreme precipitation in space and time is crucial for disaster mitigation efforts. To this end, we develop a Bayesian hierarchical model to capture the space-time variability of –summer season 3-day maximum precipitation over India. In this framework, the data layer, the precipitation extreme – i.e., seasonal maximum precipitation, at each station in each year is modeled using a generalized extreme value (GEV) distribution with temporally varying parameters, which are decomposed as linear functions of covariates. The coefficients of the covariates, in the process layer, are spatially modeled with a Gaussian multivariate process which enables capturing the spatial structure of the rainfall extremes and covariates. Suitable priors are used for the spatial model hyperparameters to complete the Bayesian formulation. With the posterior distribution of spatial fields of the GEV parameters for each year, posterior distribution of the nonstationary space-time return levels of the precipitation extremes are obtained. Climate diagnostics will be performed on the 3-day maximum precipitation field to obtain robust covariates. The model is demonstrated by application to extreme summer precipitation at 357 stations from this region. Preliminary model validation indicates that our model captures historical variability at the stations very well. Maps of return levels provide spatial and temporal variability of the risk of extreme precipitation over India that will be of great help in management and mitigation of hazards on natural resources and infrastructure.

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# Spatial-temporal Bayesian hierarchical model for summer monsoon precipitation extremes over India

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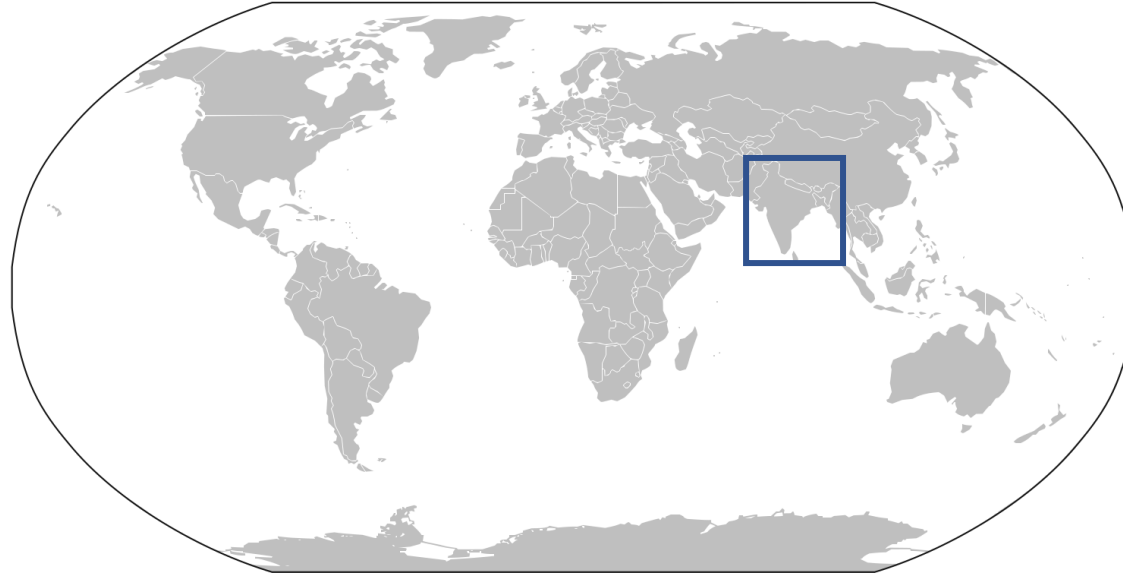
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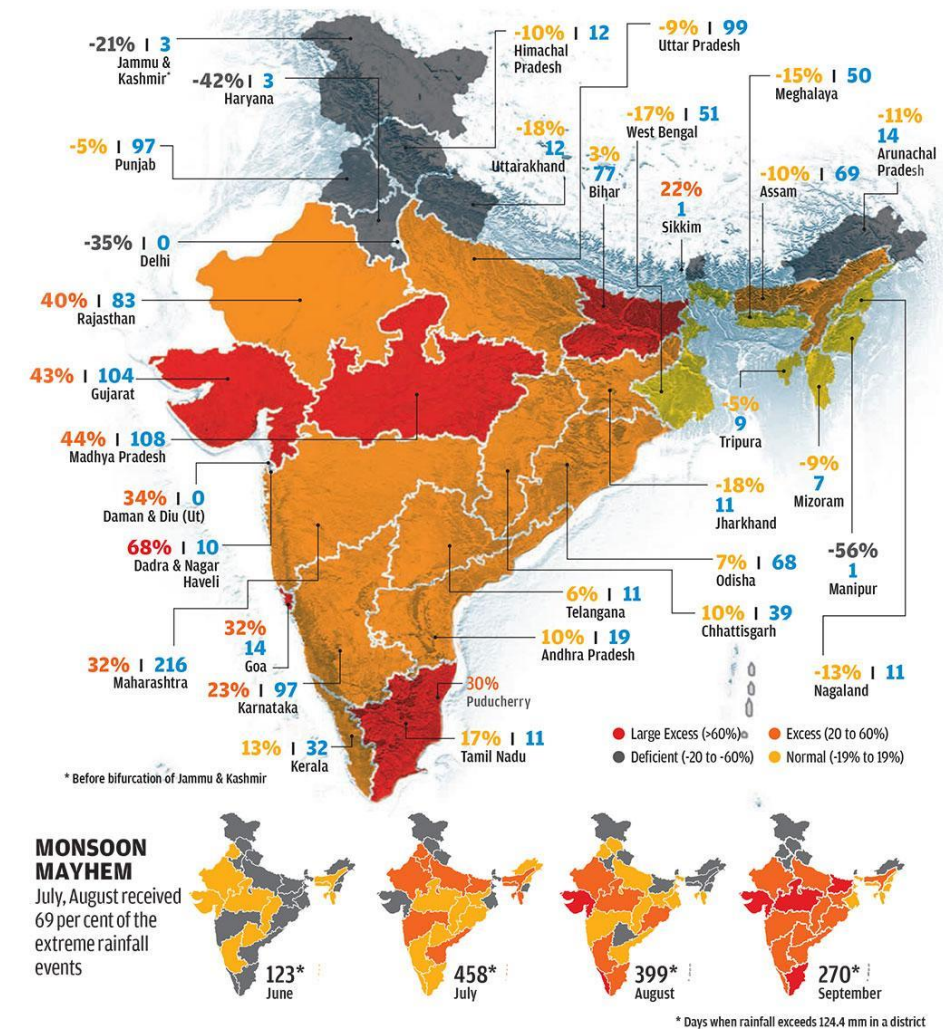
# Motivation



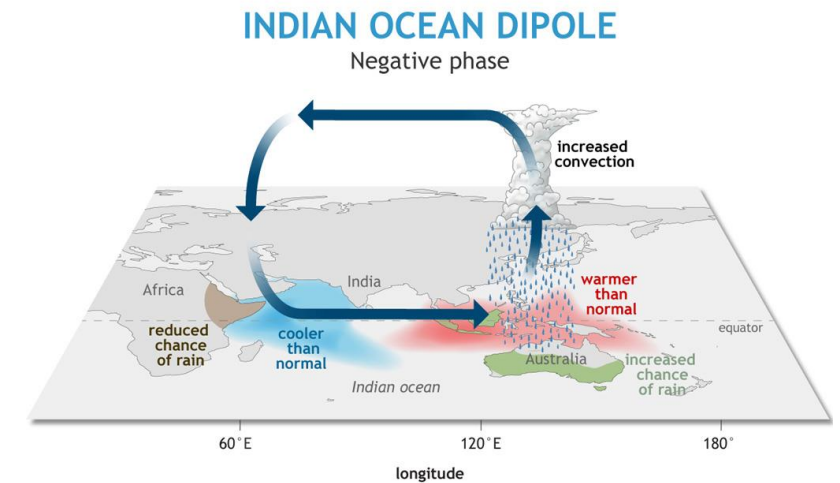
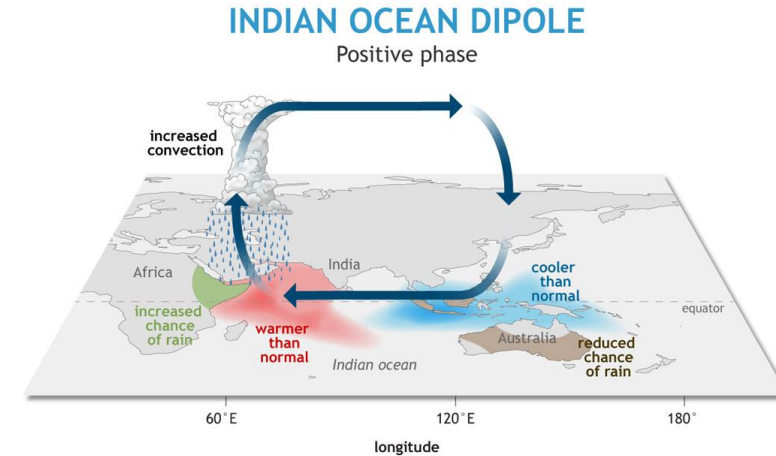
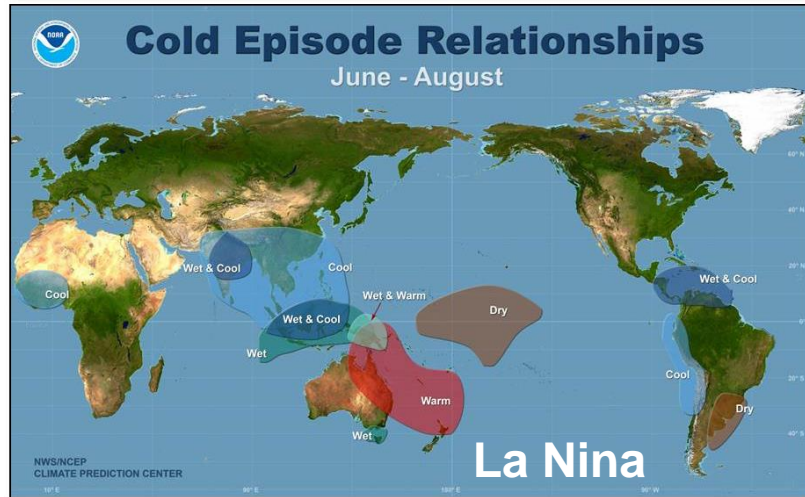
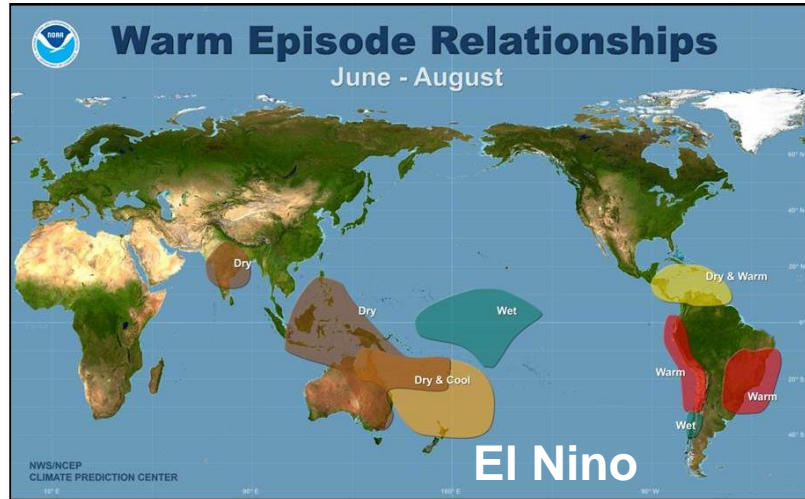
- India receives more than 80% of annual rainfall during the summer monsoon season (June-September)
- Floods occur mostly during this season (Rainfall-runoff basins)
- Understanding and modeling extreme precipitation is crucial for flood risk assessment and mitigation

**UNDER DELUGE** | 57 per cent of the extreme rainfall events this monsoon took place in just six states, including Rajasthan, which alone accounted for nearly 7 per cent of the events. Despite accounting for nearly 13 per cent of the extreme rainfall events, the northeastern states, barring Sikkim, had deficit monsoon

India (June 1-September 30, 2019) | Monsoon surplus **10%** | **1,250** Number of extreme rainfall events\*



# Year to year variability of the rainfall over India is driven largely by ENSO and IOD



NOAA Climate.gov



# Data

## Precipitation

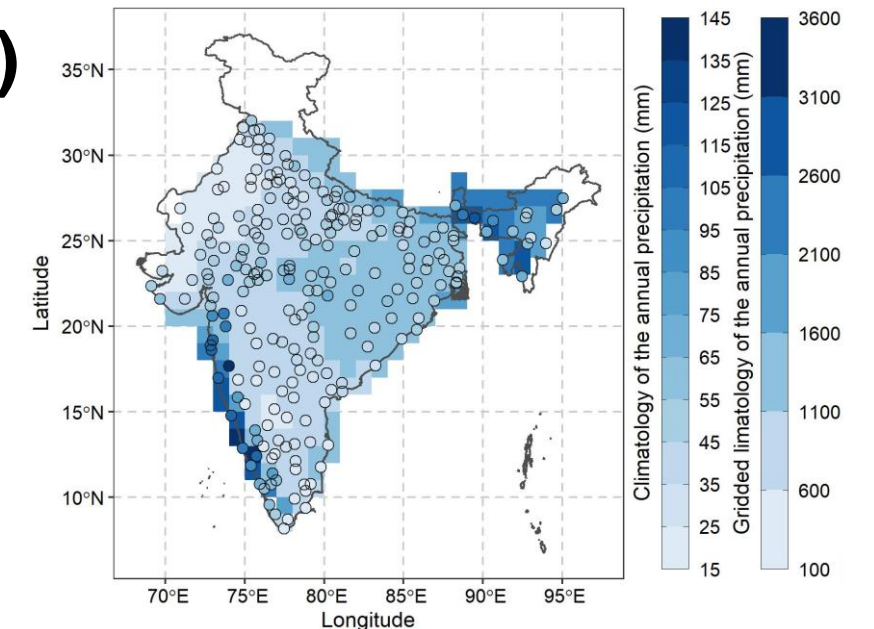
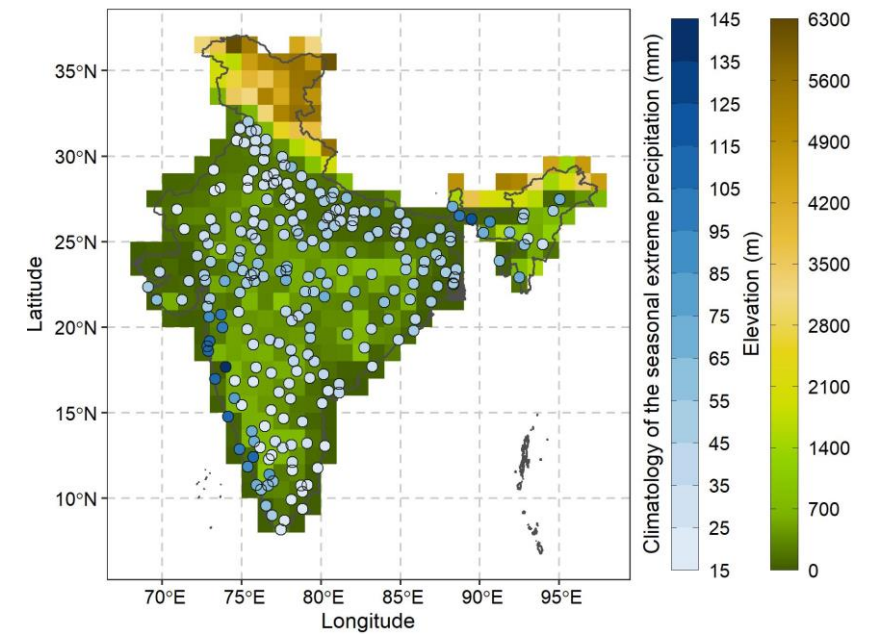
- Daily observed precipitation – The India Meteorological Department (IMD)
- Years: 1951-2017 (67 years), no. of sites 240
- 3-day summer (Jun-Sept) monsoon maximum precipitation

## Potential Temporal Covariates (1951-2017)

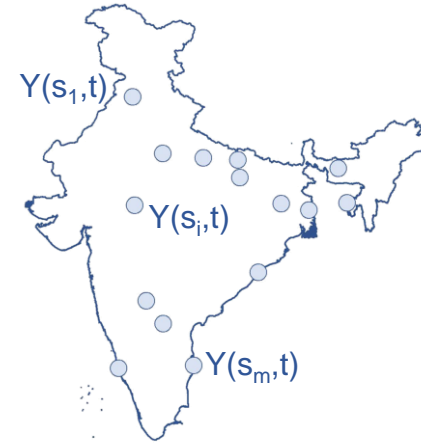
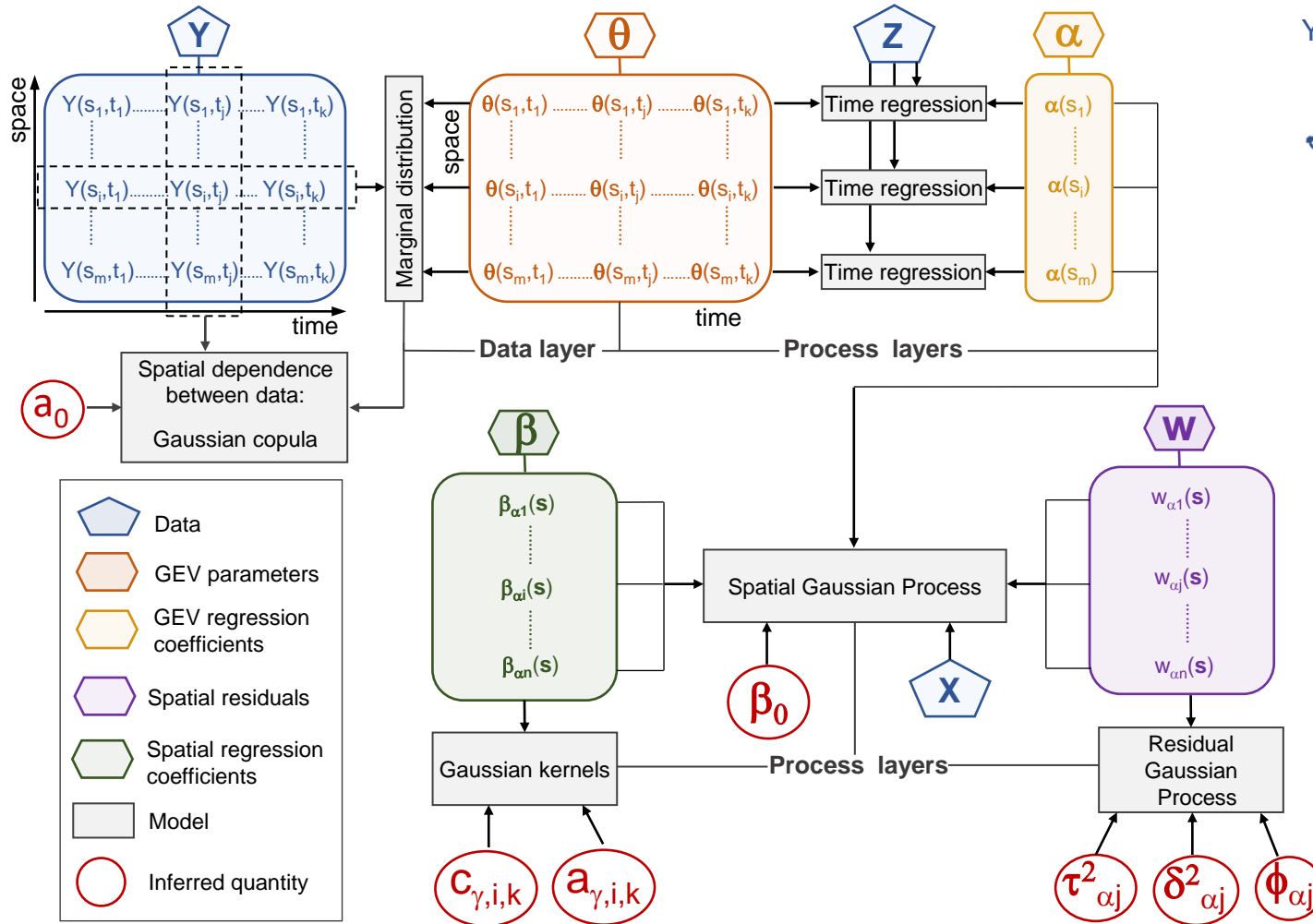
- Climate indices: ENSO, and IOD - NOAA
- Spatial Average Summer Monsoon Precipitation (SASP) – The India Meteorological Department (IMD)
- Monsoon season

## Spatial Covariates (1° spatial resolution)

- Elevation and Climatology of annual precipitation



# General Bayesian Model Structure



For each time and location

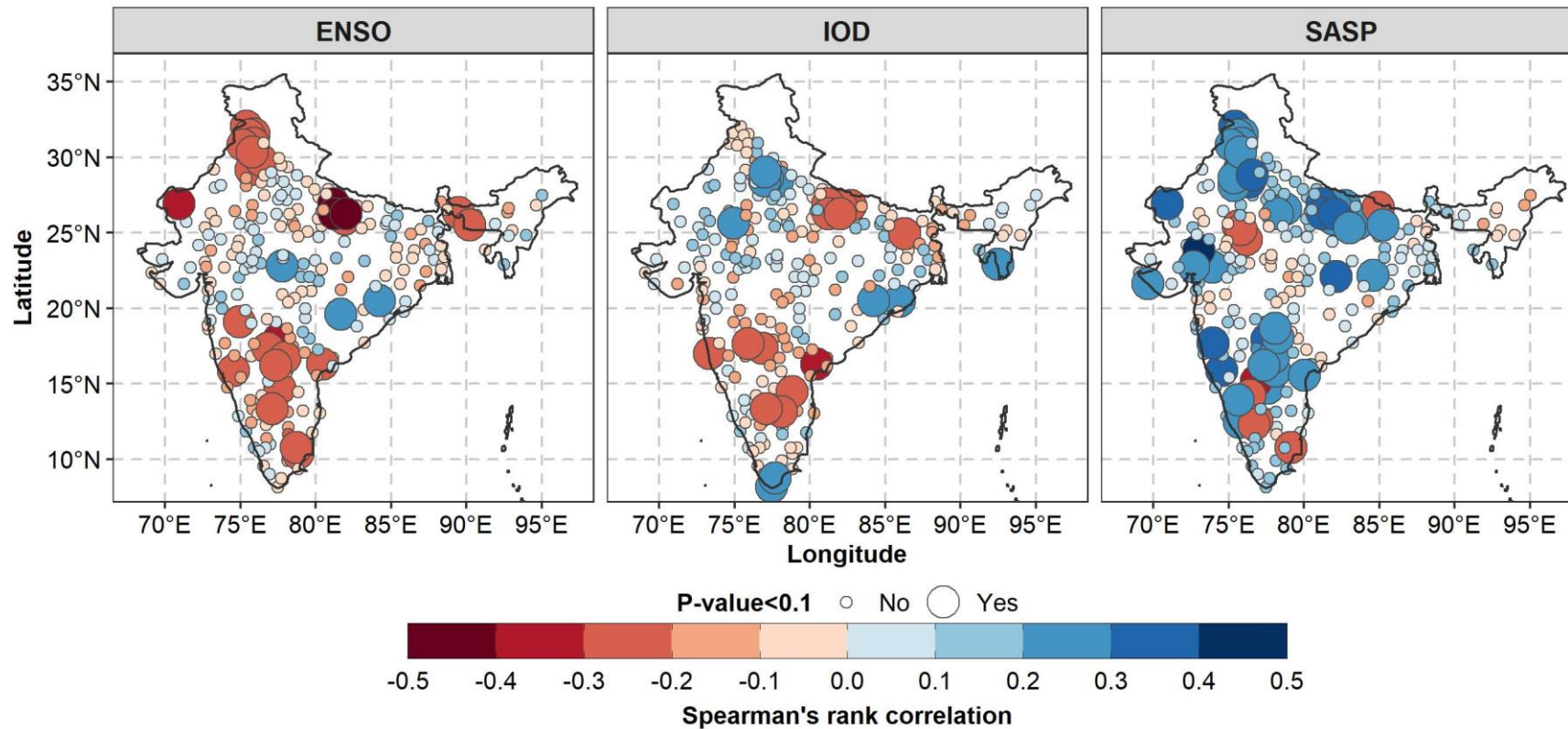
$$y(s_i, t_j) \sim \text{GEV}(\mu(s_i, t_j), \sigma(s_i, t_j), \xi(s_i, t_j))$$

$$\theta(s_i, t_j) = [\mu(s_i, t_j), \log \sigma(s_i, t_j), \xi(s_i, t_j)]$$

For each GEV regression coefficient

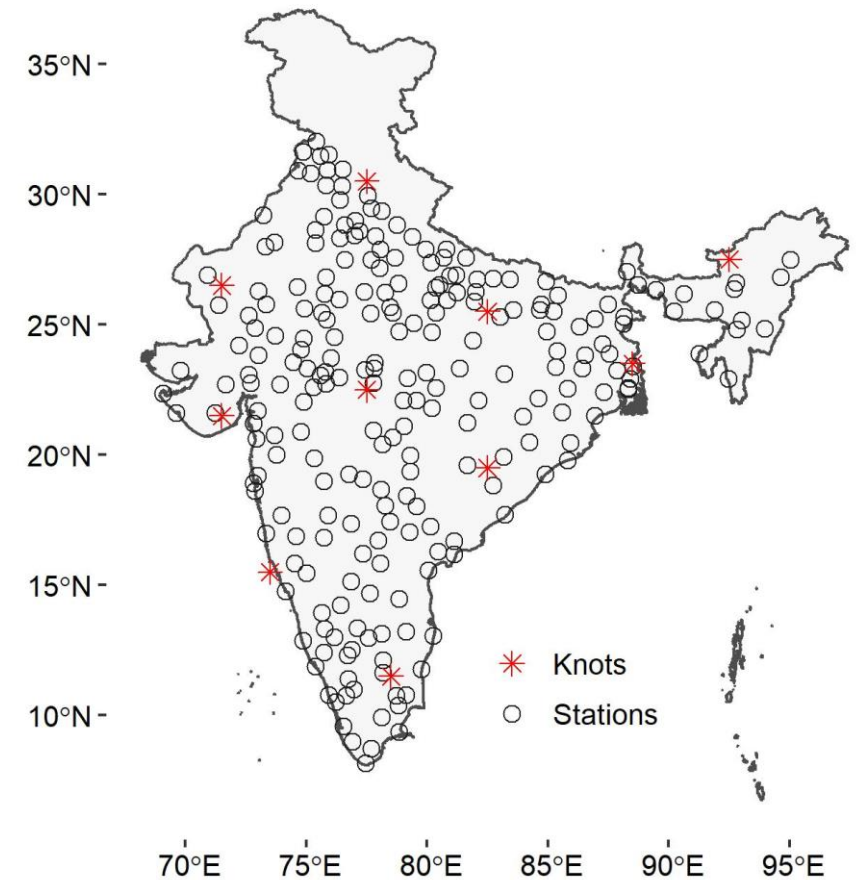
$$\beta_{\gamma}(s) = [\beta_{\gamma_1}(s), \dots, \beta_{\gamma_p}(s)]^T$$

# All the potential covariates show regions of strong correlation with summer maximum precipitation



# Model implementation

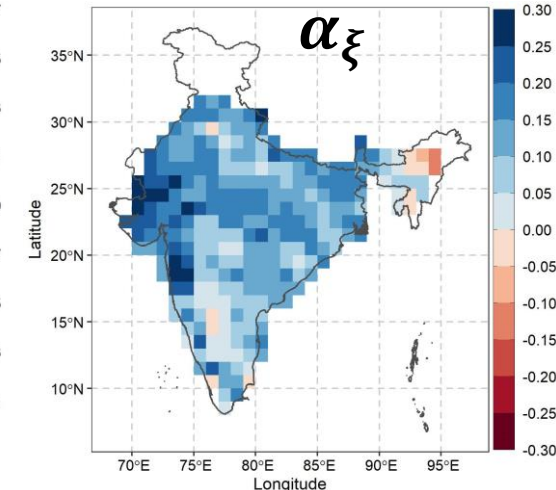
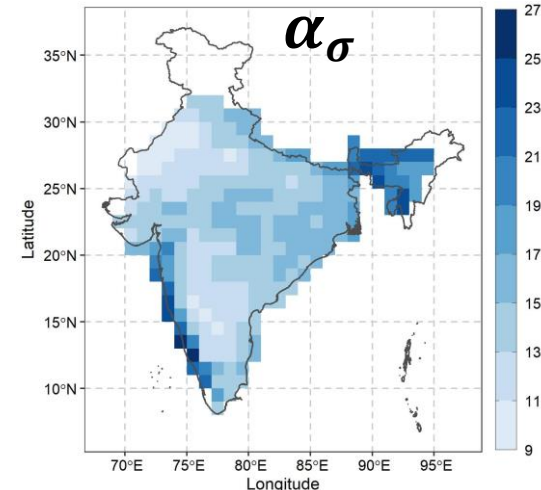
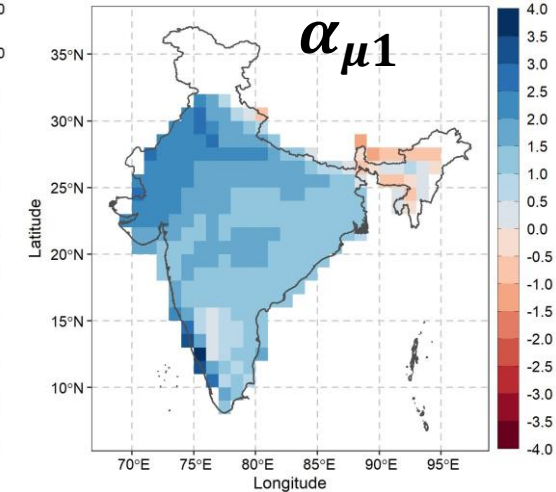
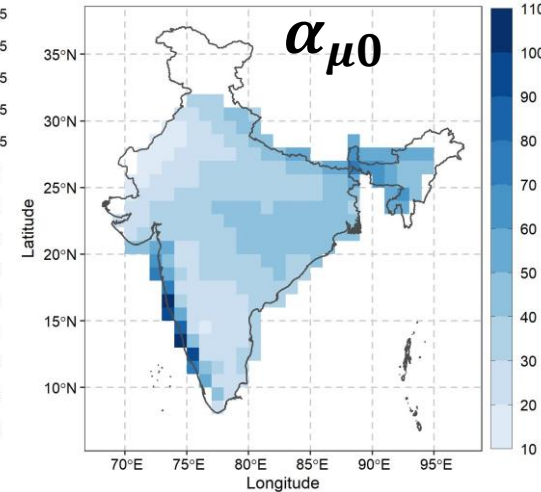
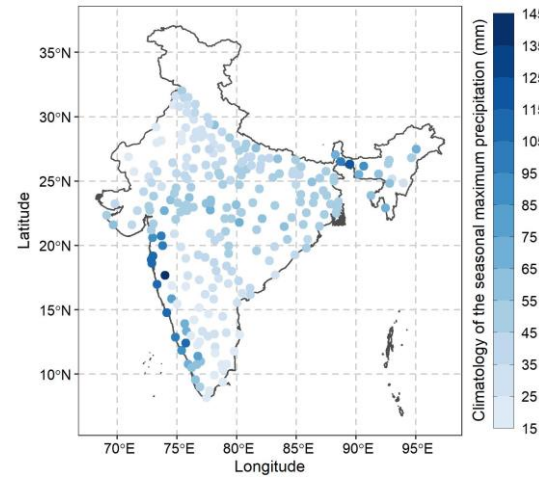
- Temporal covariates selected based on the lowest sum of AIC values at site (MLE)  
→ SASP ( $\alpha_{\mu 1}$ )
- Only location was considered nonstationary
- For the Gaussian kernels, we used 10 knots and group size of 10 (Bracken et al., 2016)
- We used weakly informative normal priors.
- Posterior distributions estimated using the No-U-Turn Sampler (NUTS; Hoffman and Gelman 2014) for the Markov Chain Monte Carlo method (Gelman and Hill 2006).
- 3000 posterior samples (ensembles)





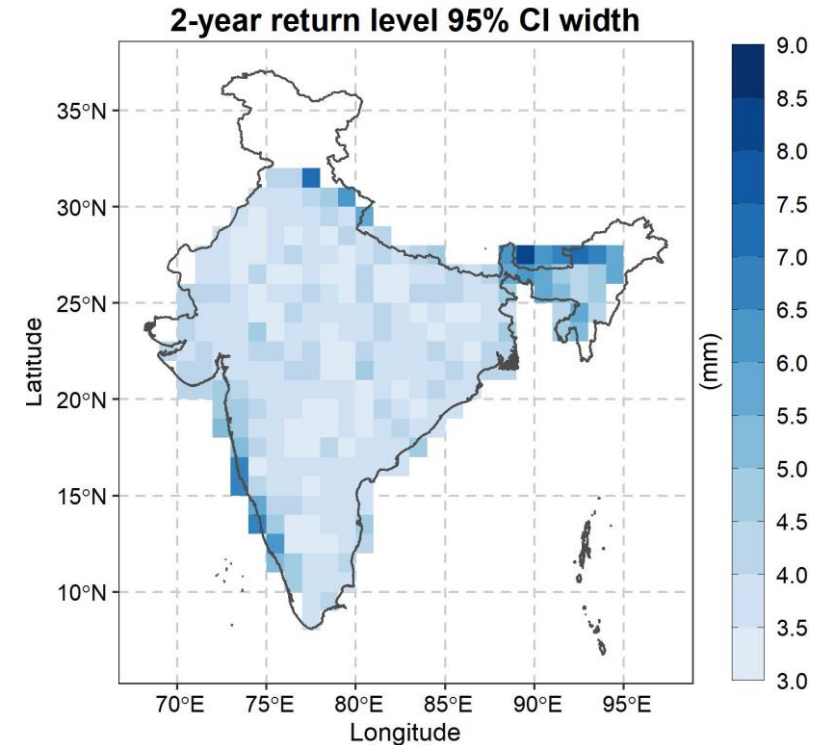
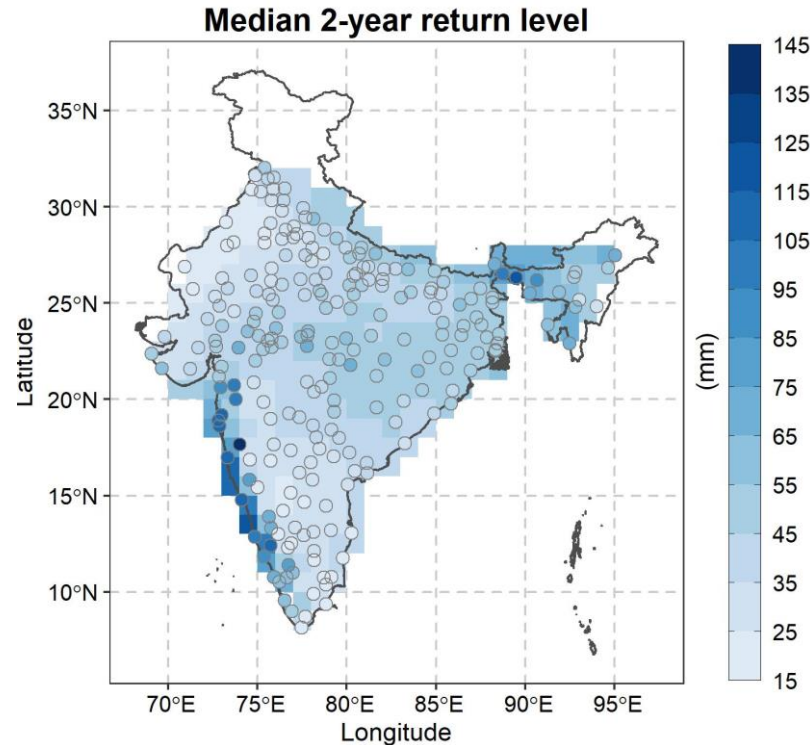
# Posterior distribution of the GEV regression coefficients capture the spatial patterns of the data

- Spatial pattern of the posterior median of the intercept of location parameter ( $\alpha_{\mu_0}$ ) is consistent with seasonal maximum precipitation climatology
- Same pattern for scale parameter ( $\alpha_{\sigma}$ )
- Posterior median of SASP ( $\alpha_{\mu_1}$ ) positive for most of the country except for the region close to the Himalayas
- Posterior median of shape ( $\alpha_{\xi}$ ) does not show any spatial pattern



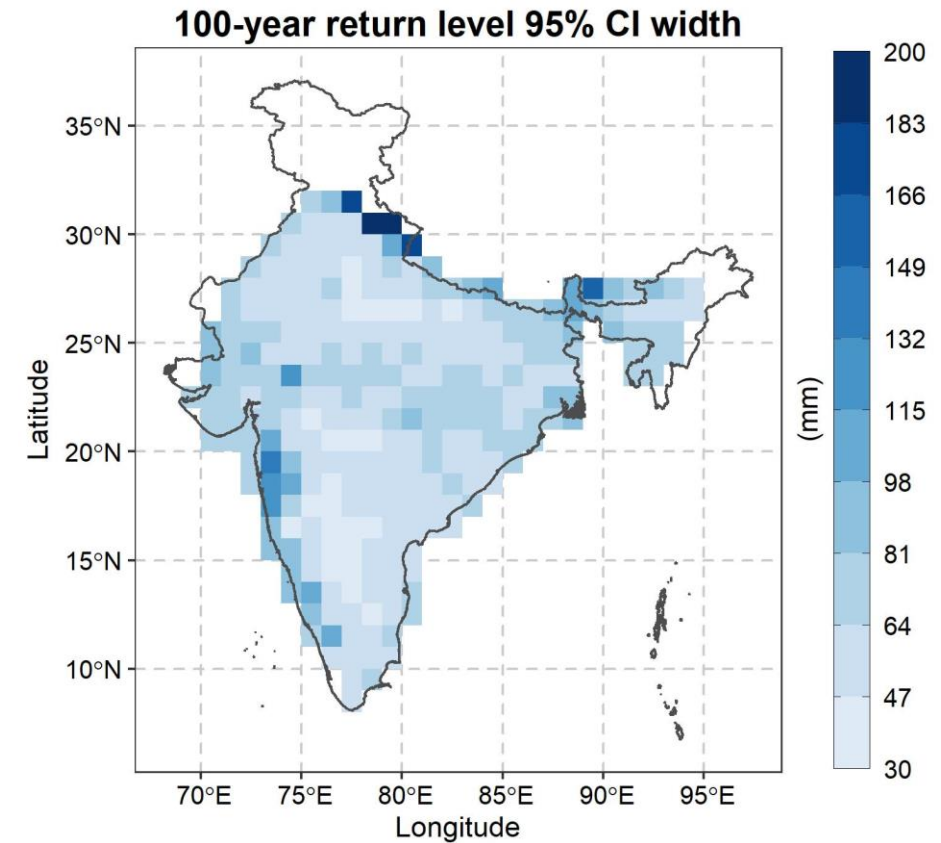
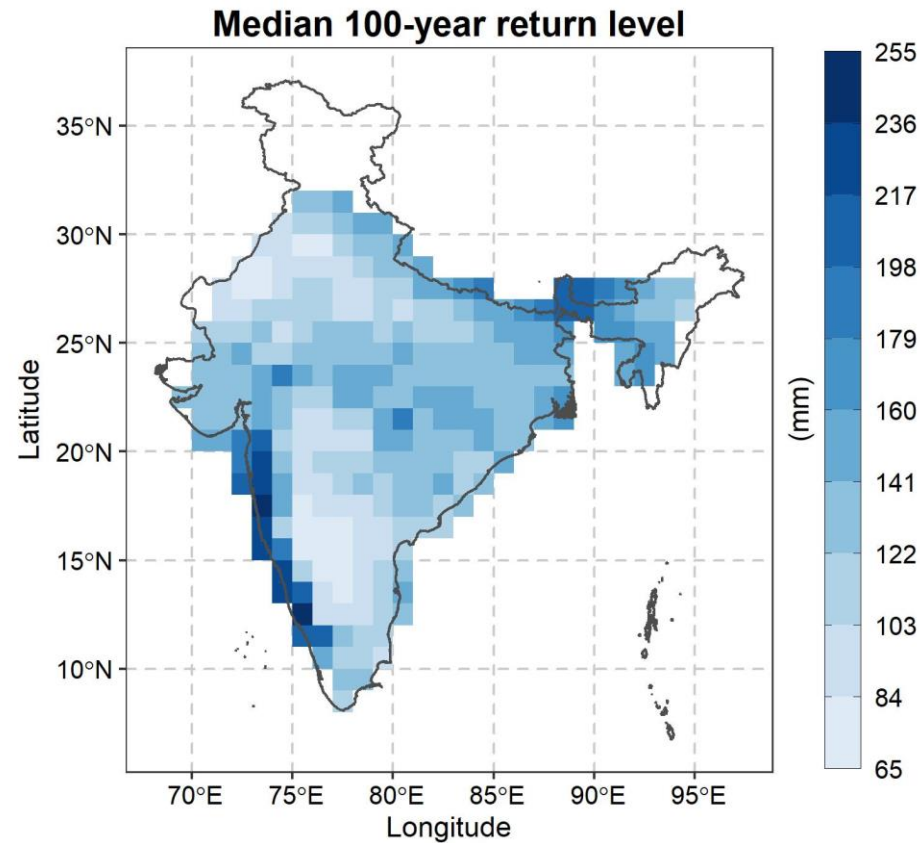
# Median of 2-year return level maximum precipitation captures the spatial patterns of the data

- BHM capture the spatial patterns of the observed summer maximum precipitation
- Small uncertainty for most of the domain with high values in the west coast and the mountain region close to the Himalayas



# Median of 100-year return level maximum precipitation

- Similar pattern to the climatology of the observed summer maximum precipitation and the median of 2 years return level

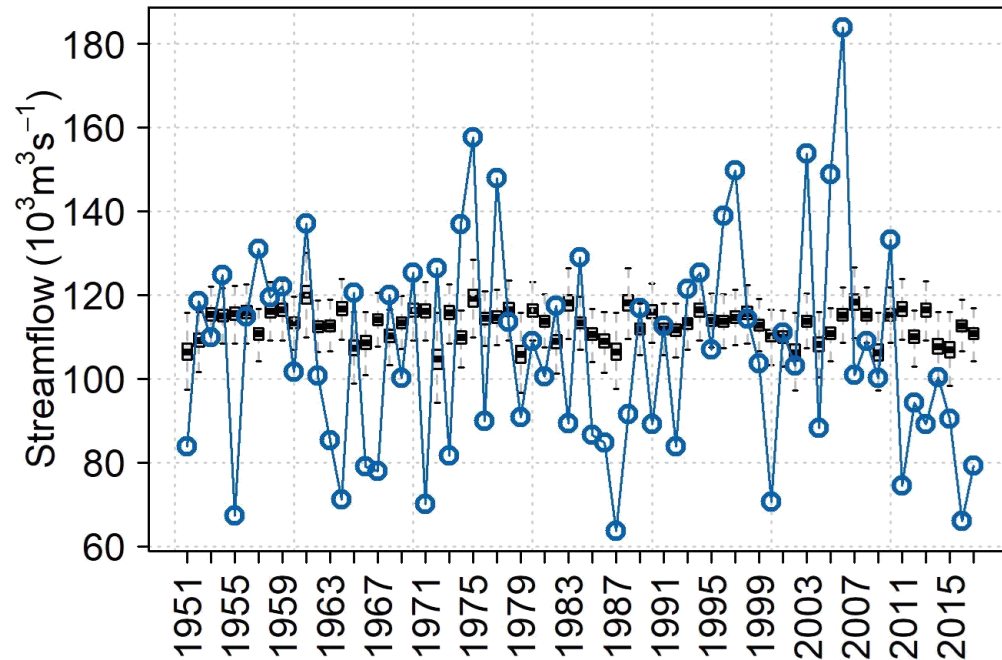


# Time series of return levels

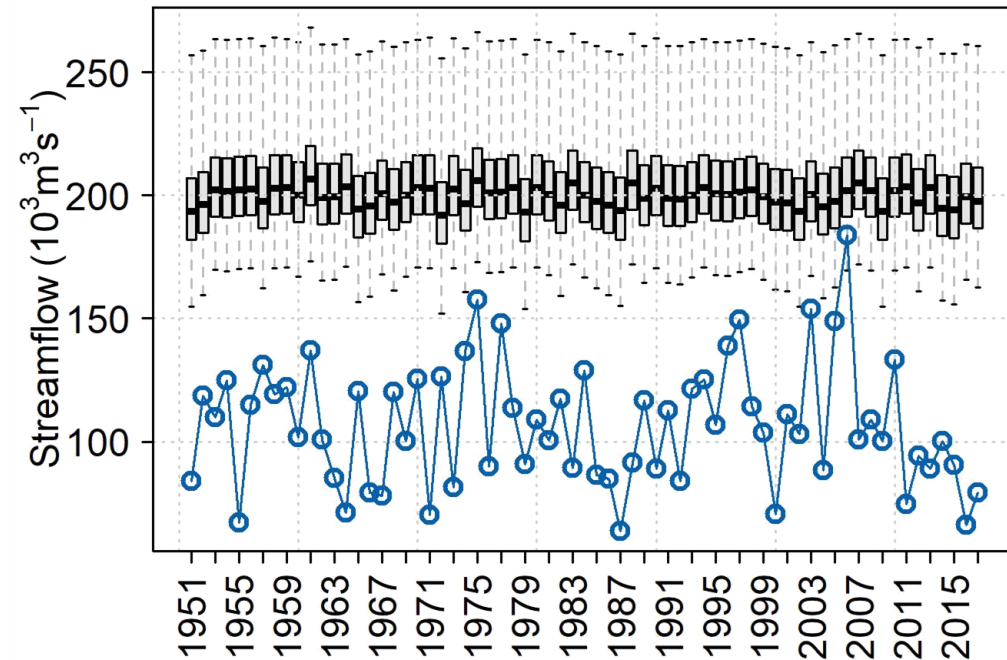
- BHM can generally capture the temporal variability of the data



2 years return level



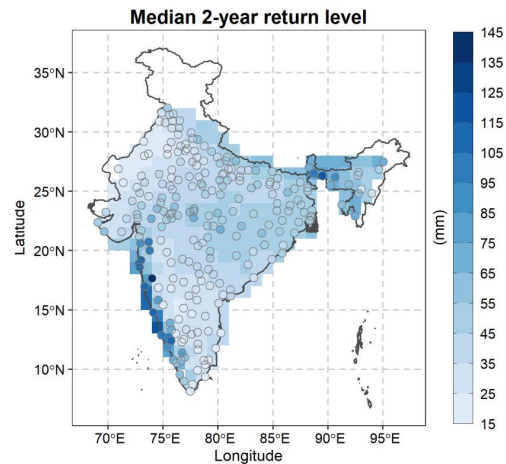
100 years return level



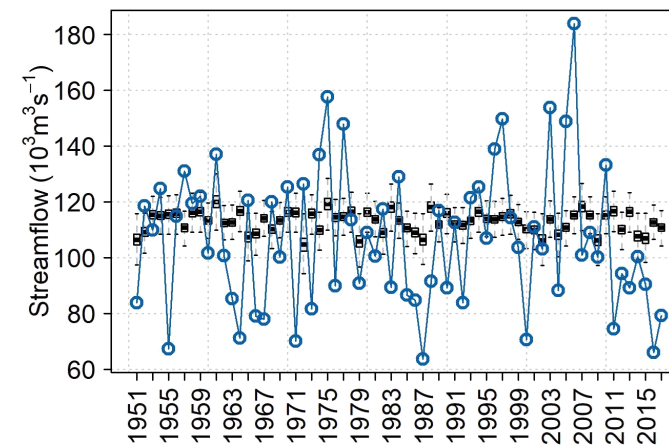


# Conclusions

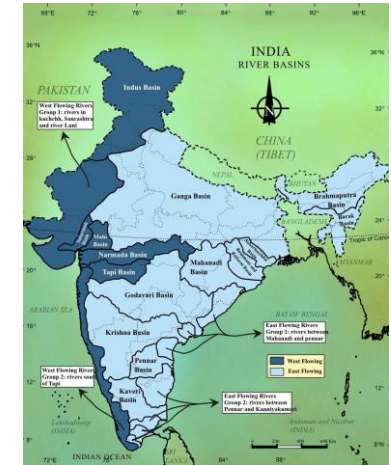
Captures the spatial pattern of the data



Provides temporal variability of the data by considering nonstationarity



The framework can be applied regionally to improve the results by considering tailored covariates



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