

A novel wave breaking framework to estimate air-sea gas transfer velocities

Sophia E. Brumer¹ and Christopher J Zappa²

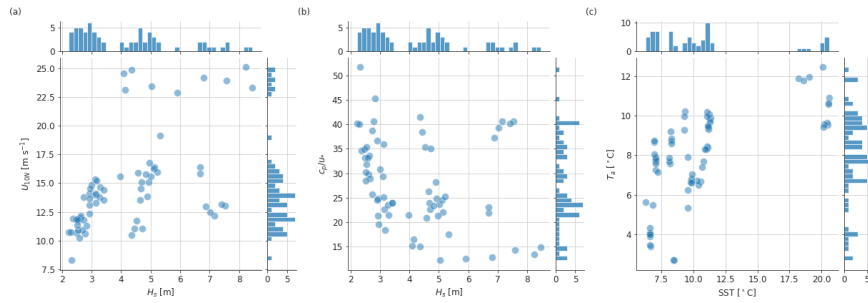
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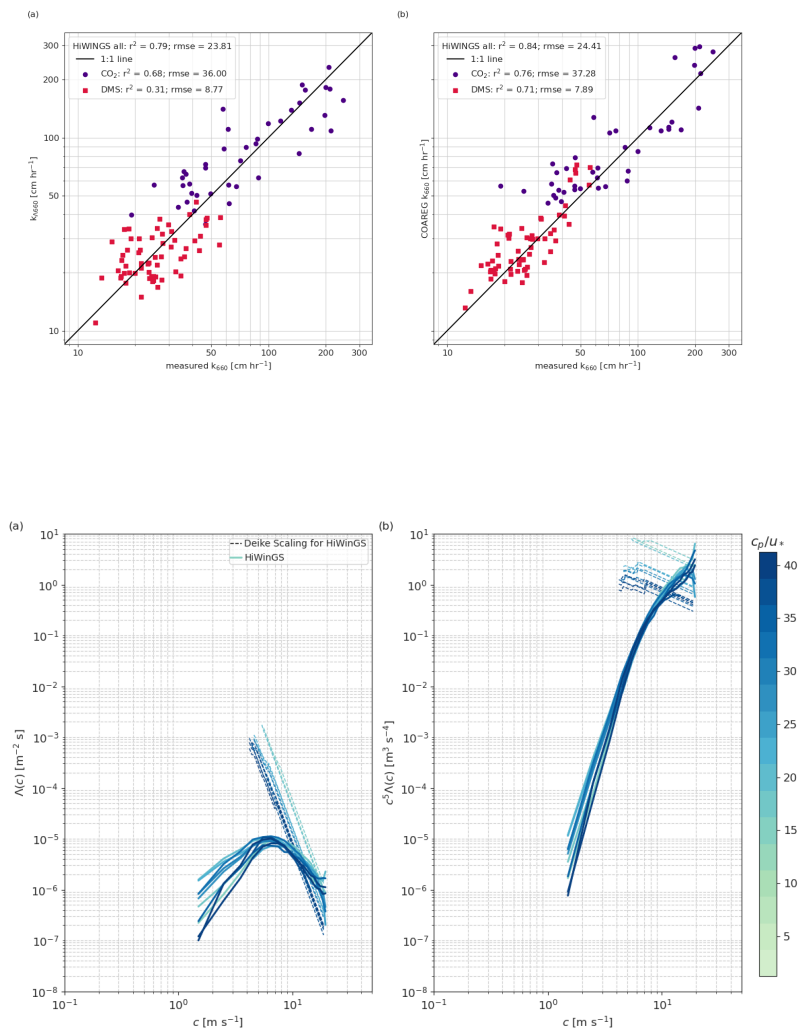
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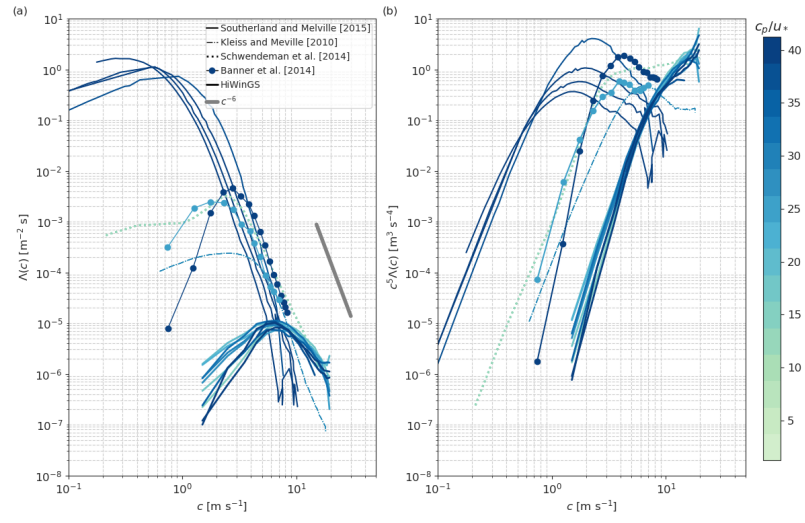
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Abstract

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A novel wave breaking framework to estimate air-sea gas transfer velocities

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Key Points:

- a novel gas transfer velocity parameterization is proposed for wave breaking conditions
- modeling turbulence- and bubble-mediated gas transfer using breaking crest length distribution
- tested using breaking crest length distribution and gas flux measurements from HiWinGS

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Abstract

Parameterizations of gas transfer velocities are needed for climate predictions. Single parameter models typically only include wind dependence and may readily be used in climate studies. Their application is however gas specific and limited to select environments. Mechanistic parameterizations incorporating multiple forcing factors allow modelling the transfer of gases with differing solubilities for a wide range of conditions. A novel framework is put forward to model gas transfer in the open ocean in the presence of breaking waves. It incorporates both the turbulence- and bubble-mediated transfers based on statistics determined from the breaking crest length distribution ($\Lambda(c)$). Testing the mechanistic model with measurements from the HiWinGS field campaign shows promising results for both CO₂ and DMS. Uncertainties remain in the quantification of bubble clouds which are at the core of the formulation of the bubble-mediated transfer.

Plain Language Summary

Predicting climate change relies on models of the transfer of gases across the atmosphere-ocean interface. Traditionally for every gas a different function of wind speed is used to compute its transfer velocity and air-sea flux. These functions are valid only in specific environmental conditions. To improve predictions, models that account for the different transfer mechanisms have to be developed. Ideally they are applicable to any gases regardless of solubility. Such a model is put forward herein. It allows to estimate the transfer velocities based on remote sensing of breaking waves and the wave field accounting for both the transfer due to turbulence and bubbles. The model is tested with measurements from the HiWinGS field campaign and shows promising results for both CO₂ and DMS. Remaining uncertainties and limitations are discussed highlighting the need for open ocean measurements of breaking waves and their associated bubble plume.

1 Introduction

Modelling air-sea gas fluxes is essential for climate predictions and relies on estimates of the gas transfer velocity (k) which is typically parameterized as a function of the 10-m wind speed (e.g. Wanninkhof, 1992; Ho et al., 2011). Large scatter is observed in estimated gas transfer velocities (k) of sparingly soluble gases at high wind speeds where wave breaking dominates upper ocean dynamics (Blomquist et al., 2017; Brumer et al., 2017a). The removal of this scatter by a wind-wave based parameterization (Brumer et al.,

2017a) suggests that k would be better modeled with the inclusion of surface wave breaking rather than wind speed alone.

Wave breaking has the potential to considerably impact air-sea exchanges and upper-ocean dynamics (Deike, 2022). It leads to enhanced turbulent kinetic energy (TKE) in the near surface layer resulting in surface TKE dissipation rates (ε) shown to be roughly 5 to 1000 times greater than predicted by wall layer scaling (Agrawal et al., 1992; Gemmrich, 2010; Sutherland and Melville, 2015; Terray et al., 1996). Additionally, air-entraining breaking waves generate bubble clouds that allow for an additional pathway for gas transfer which is particularly important to consider for sparingly soluble gases such as CO_2 (Woolf, 1993).

Efforts have been made to account for the impact of bubbles in physical process based models (Deike and Melville, 2018; Fairall et al., 2011; Liang et al., 2013; Goddijn-Murphy et al., 2016; Asher et al., 1996). Only one of these models explicitly considers the contribution of wave breaking turbulence (Asher et al., 1996; Asher and Wanninkhof, 1998). However, it is reduced to a function of the whitecap cover and 10-m wind speed. None of these models include direct dependence of the transfer to the TKE dissipation due to wave breaking, it is implicitly comprised through dependence on the friction velocity amongst other forcing. While all these variables are inter-linked, it is not always in a straight forward way. The limitations of these models were revealed using the whitecap coverage and the gas transfer velocities of CO_2 and DMS observed during HiWinGS (Blomquist et al., 2017).

Several studies have shown how enhanced turbulence promotes gas transfer (Zappa et al., 2007; Tokoro et al., 2008; Vachon et al., 2010; Esters et al., 2017) but not in relation to breaking waves. Based on measurements of turbulence in the wave-affected and wave breaking layers, Shuiqing and Dongliang (2016) derived a parameterization for the gas transfer velocity in the presence of breaking waves. Their proposed functional form is similar to that of Asher and Wanninkhof (1998) without the bubble-mediated component. It does not directly depend on the turbulent kinetic energy dissipation rate, but rather the air friction velocity, the whitecap cover, and wave age.

Herein, a novel framework to model air-sea gas transfer velocities in the presence of breaking waves is put forth. The proposed framework incorporates both the turbulence- and bubble-mediated transfer. It is based on two statistics derived from the breaking crest

length distribution (Phillips, 1985): the turbulent kinetic energy dissipation rate and the bubble volume flux. Multiple field campaigns in the last decade have demonstrated the existence of a robust link between the breaking crest length distribution to the turbulent kinetic energy dissipation rate following the spectral framework proposed by Phillips (1985) to quantify wave breaking properties. Recently, through a combination of DNS and laboratory observations Deike et al. (2017) have extended the application of the Phillips (1985) framework allowing estimations of bubble cloud properties from the breaking crest length distribution. These advances are at the core of the present framework.

Section 2 provides an outline of the general form of the proposed model followed by a review of Phillips (1985)’s theoretical framework and the work of Deike et al. (2017) which are used for the derivation of quantities key to air-sea gas transfer. The model is tuned using data from the High Wind Gas Exchange Study (HiWinGS) which is shown in section 3. The model is compared to other existing physically-based models in sections 4 where uncertainties and guidelines for future measurements are also discussed.

2 Proposed Gas Transfer Model

The proposed functional form of the k model accounting for the contribution of the turbulence-driven (k_ε) and the bubble-mediated (k_b) transfers is:

$$k = k_\varepsilon + k_b \quad (1)$$

Various mechanistic approaches were suggested by which turbulence promotes the transfer of gases. These invoke concepts of surface renewal (Higbie, 1935; Danckwerts, 1951; Lamont and Scott, 1970; Komori et al., 1993), surface penetration (Harriott, 1962; Atmane et al., 2004) and surface divergence (McCready et al., 1986; Banerjee and McIntyre, 2004; Banerjee et al., 2004; McKenna and McGillis, 2004; Turney et al., 2005) and their application is limited to a constrained set of environmental conditions. Boundary layer scaling arguments also allow to derive k_ε . The flux of gas (F_g) follows Fick’s law of diffusion:

$$F_g = D \frac{\partial C}{\partial z} = \frac{D}{\delta_z} (C_w - \alpha C_a) = k_\varepsilon (C_w - \alpha C_a) \quad (2)$$

Where D is the diffusivity, δ_z a characteristic surface boundary length scale, α the Ostwald solubility coefficient and C_a , C_w the air and water concentrations, respectively. This allows rewriting k_ε as:

$$k_\varepsilon = \frac{D}{\delta_z} \quad (3)$$

Using the Batchelor length scale $\delta_Z \propto \left(\frac{\nu_w D^2}{\varepsilon}\right)^{\frac{1}{4}}$, which is the characteristic turbulent microscale for a passive scalar (Batchelor, 1959), the following relationship between k_ε and ε was derived (Banerjee et al., 1968; Kitaigorodskii, 1984):

$$k_\varepsilon \propto (\varepsilon \nu_w)^{\frac{1}{4}} Sc^{-0.5} \quad (4)$$

where ν_w is the water viscosity, and $Sc(= \nu_w/D)$ is the water-side Schmidt number defined as the ratio of the water viscosity and the mass diffusivity D .

The bubble-mediated transfer is commonly expressed as function of the bubble volume flux (F_a) or the void fraction (v) (Woolf, 1997; Woolf et al., 2007). Neglecting potential collective effects of bubbles Woolf proposed the so-called “independent bubble model”:

$$k_{bind} \propto F_a \alpha^{-1} \left(1 + (\chi)^{1/1.2}\right)^{-1.2} \quad (5)$$

with

$$\chi \propto Sc^{-0.5} F_a \alpha^{-1} \quad (6)$$

It satisfies the two commonly accepted distinct asymptotic behaviours of k_b : 1) for highly soluble gases ($\alpha \gg 1$), where full equilibration is achieved, the bubble-mediated flux is limited by the bubble volume flux and solubility and 2) for very weakly soluble gases ($\alpha \ll 1$), where no equilibration is achieved, the flux does not depend on solubility but on diffusion (see also Keeling (1993); Goddijn-Murphy et al. (2016); ?).

Based on laboratory work by Cipriano and Blanchard (1981), Woolf (1997) first suggests that:

$$F_a = 6.25 \times W \text{ [m(m}^2 \text{ s)}^{-1}] = 2250 \times W \text{ [cm hr}^{-1}] \quad (7)$$

and

$$\chi = \frac{Sc^{-0.5}}{14\alpha} \quad (8)$$

Where W is the total whitecap cover expressed as a fraction. Later in the paper, Woolf uses $F_a = 2450W$ which is the value adopted by subsequent studies. Note that Eq. (8) removes the additional higher order F_a dependence of Eq. (5).

2.1 Phillips’ [1985] Spectral Framework

Laboratory experiments by Duncan (1981, 1983), in which a breaking wave was created by a hydrofoil towed at constant speed and depth, revealed a relationship between

energy dissipated by a steady breaking wave and its speed:

$$\varepsilon_l \propto \frac{\rho_w c_h^5}{g}, \quad (9)$$

where ε_l is the energy dissipation per crest length, ρ_w is the water density, g is the gravitational acceleration, and c_h the speed of a towed hydrofoil which corresponds to the speed of the breaking crest, $c_h \sim c_{br}$.

Phillips (1985) introduced the spectral density of the breaking crest length per unit area $\Lambda(c)$, where c is the breaking wave phase speed. Based on Duncan's experiments, he proposed:

$$\varepsilon = \int S_{ds}(c)dc = \int b(c)\rho_w g^{-1}c^5\Lambda(c)dc \quad (10)$$

where S_{ds} is the spectral dissipation term from the radiative transfer equation that describes the evolution of the wave field and $b(c)$ is the spectral breaking strength.

Recognizing the value of the breaking crest length distribution to infer breaking wave characteristics and subsequently air-sea interaction processes, multiple studies have been undertaken to obtain direct measurements of both $\Lambda(c)$ and ε . The first measurements of $\Lambda(c)$ were made by Phillips et al. (2001) using a marine radar. Later studies have used digital video camera to track breaking waves from stable platforms (Gemmrich et al., 2008, 2013; Schwendeman et al., 2014; Sutherland and Melville, 2013, 2015; Thomson et al., 2009; Zappa et al., 2012) and planes (Kleiss and Melville, 2010). Techniques to derive the breaking crest length distribution from the imagery vary greatly. These are reviewed and discussed in Banner et al. (2014). Here, the initial velocity method is adopted, in which the phase velocity c is equated to a fixed reference velocity that corresponds to initial breaker-front velocity of each breaking event (c_{br}) as was originally chosen by Phillips (1985). The phase speed of the breaking wave has been shown to be closely related to the speed of the breaking crest c_{br} with $c_{br}/c \sim 0.8 - 0.9$. Following Gemmrich et al. (2008, 2013), the breaking crest length distribution $\Lambda(c_{br})$ for a given speed range ($c_{br}, c_{br} + \Delta c_{br}$) is then obtained from:

$$\Lambda(c_{br}) = \sum L_{br}t_{br}/(TA\Delta c_{br}) \quad (11)$$

where L_{br} is the characteristic breaking segment length, t_{br} duration of an individual breaking crest event (based on the time a breaker is tracked in the imagery), A is the area of the field of view, and T the total duration of observation.

2.2 Estimating the turbulent kinetic energy dissipation rate

To estimate the turbulent kinetic energy dissipation rate from the breaking crest length distribution (Eq. 10), one unknown remains: the spectral breaking strength $b(c)$. Wave systems produced in laboratory experiments are narrow-banded and $b(c)$ is assumed to be independent of scale. It was found to vary with wave steepness (Banner and Peirson, 2007; Drazen et al., 2008; Melville, 1994). Ocean waves are however rarely narrow-banded and modeling studies suggest that $b(c)$ may scale with wave age (Romero et al., 2012).

No direct field measurements of $b(c)$ exist to date as $\varepsilon(c)$ has not been tractable in the open ocean. A scale-independent effective breaking strength coefficient (b_{eff}) was thus defined:

$$b_{eff} = \frac{\varepsilon}{\rho_w g^{-1} \int c^5 \Lambda(c) dc} \quad (12)$$

Leading to:

$$\varepsilon(c) = b_{eff} c^5 \Lambda(c) / g \quad (13)$$

Reviewing all existing breaking crest length distribution and coinciding upper ocean dissipation rate measurements, Zappa et al. (2016) determined the following wave-age dependent parameterisation of b_{eff} :

$$b_{eff} = 3.48 \times 10^{-3} - 4.69 \times 10^{-5} \frac{c_p}{u_*} \quad (14)$$

Here c_p is the phase speed of the dominant wave and u_* the air friction velocity.

2.3 Estimating the Bubble Volume flux

Estimation of the bubble volume flux and void fractions are based on relations determined from novel direct numerical simulations (DNS) of three-dimensional breaking waves that resolve bubble scales (Deike et al., 2016). One of the key finding from this DNS study is that total volume of air entrained by a breaking wave (V_a) is directly proportional to the breaking crest length (L_{br}) and the breaking speed to the power 5:

$$V_a = B b_{eff} \frac{L_{br} c_{br}^5}{U_b g^2} \quad (15)$$

Where B is a dimensionless constant, and U_b is a dissipation-weighted vertical mean velocity which corresponds to the average rise velocity of the bubble plume. This relation stems from the core assumption that the global (integrated breaking event's spatio-temporal

extent) work done against buoyancy forces in entraining the bubbles is proportional to the mechanical energy dissipated where $B = 0.1$ is the proportionality factor. U_b scales as the rise velocity in clean water (Woolf and Thorpe, 1991) of a bubble of radius equal to the mean of the bubble distribution. Not knowing the bubble distribution, a constant U_b equal to 10 cm s^{-1} is assumed here based on Asher et al. (1997).

From Eq. 15, a volume flux per unit area (F_a) can be estimated by summing the total volume of air entrained by each breaker observed during a single video recording and dividing by the area of the field of view (A) and the total time of observations (T).

$$F_a = \frac{\sum V_a}{AT} = b_{eff} B \frac{\sum L_{br} c_{br}^5}{AT U_b g^2} \quad (16)$$

Alternatively, F_a may be expressed as a combination of the fifth moment of the breaking crest length distribution and the breaking duration (τ_{br}):

$$F_a = \frac{b_{eff} B}{U_b g^2} \int \frac{1}{\tau_{br}(c)} \Lambda(c) c^5 dc \quad (17)$$

This form assumes that the duration of the breaker is a function of the breaker speed. As proposed by Kleiss (2009), based on laboratory and field data (Thorpe and Hall, 1983; Rapp and Melville, 1990), τ_{br} can be related to the period of the breaking wave which may be expressed in terms of the phase speed c via the deep water dispersion relation:

$$\tau_{br} \propto \frac{2\pi}{g} c \quad (18)$$

Kleiss (2009) suggests $\tau_{br} = 0.25 c_{br}$, thus:

$$F_a = 4 \frac{b_{eff} B}{U_b g^2} \int \Lambda(c) c^4 dc \quad (19)$$

2.4 Calibrating the Model Framework

As it is the case for all existing gas transfer model, several proportionality constants remain to be determined. This can be done by solving:

$$k_\Lambda = \mathcal{A} K_\epsilon + \mathcal{B} K_b \quad (20)$$

Where K_ϵ is equal to the right hand side of the relations in Eq. (4) and

$$K_b = F_a \alpha^{-1} \left(1 + (\mathcal{C} S c^{-0.5} F_a \alpha^{-1})^{1/1.2} \right)^{-1.2} \quad (21)$$

The coefficients \mathcal{A} , \mathcal{B} , and \mathcal{C} should be obtained through least squared error regression using measurements derived transfer velocities of gases of varying solubilities over a wide range of wind and wave conditions.

3 HiWinGS application

The proposed framework was tuned using the gas transfer velocities of CO₂ and DMS derived from the eddy co-variance measurements taken during the 2013 HiWinGS field campaign. Details about HiWinGS can be found in (Blomquist et al., 2017; Brumer et al., 2017a,b; Yang et al., 2014). Breaking waves were monitored through high frequency video recording of 20 minutes in the visible band throughout the daytime. Momentum, heat, and gas fluxes were computed hourly. Figure 1 illustrates the variable space sampled during the experiment where concurrent good quality data is available. Hourly averaged 10-m neutral wind speed (U_{10N}) range from 8.3 to 25.1 m s⁻¹, the significant wave height (H_s) from 2.2 to 8.5 m for wave ages (c_p/u_*) of 12.2 to 51.7. The sea surface (SST) and air (T_a) temperatures ranged 6.3-20.6 and 2.7-12.5°C, respectively with differences, $\Delta T = T_a - \text{SST}$ spanning -10.9 to 1.8°C.

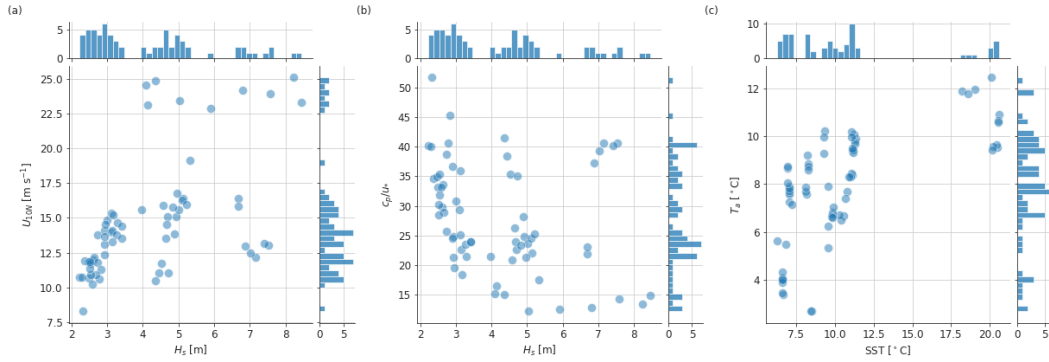


Figure 1. Scatter plots and histograms of (a) the neutral 10-m wind speed (U_{10N}) vs. the significant wave height (H_s), (b) the wave age (c_p/u_*) vs. the significant wave height, and (c) the surface air temperature (T_a) vs. the sea surface temperature (SST)

3.1 Tracking breaking crests

The breaking crest length distributions were determined from over 200 videos taken the starboard side of the flying bridge of the R/V Knorr. For details on the setup see Brumer et al. (2017b). All background gradients present in the images were removed prior to any further analysis. The images were then corrected for lens distortion and re-projected using the roll, pitch, and yaw angles measured by IMUs. Finally, they were interpolated

onto a regular grid with pixel resolution of 0.1 m. The area of the field of view A was $\sim 1100 \text{ m}^2$ and the total duration of observation T was around 19 minutes.

The breaking crest lengths were tracked following the method developed by Gemmrich et al. (2008). In order to bring out the advancing side of the whitecap two consecutive rectified and projected images are differenced. As whitecaps are brighter than the background, the advancing front is distinguishable by high positive values, while the rear side is negative in the differenced image. The differenced images are thresholded based on image intensity (I) using $I/\max(I) > 0.6$ and transformed into binary images where the breaking crests have pixels equal to 1 and the rest is set to 0.

Using Matlab's image processing toolbox, a series of morphological operations are then applied to the binary frames to insure that crest do not contain holes and to link crests that are close together into a single one (details in Supplementary Information (SI)). Finally, each crest is identified and approximated as an ellipse. This allows to determine the coordinates of the center of mass of each crest, as well as the length major and minor axis, their area, and orientation.

At this stage crests that have an area smaller than 1.5 m^2 are removed. The remaining crests are then tracked from one differenced frame to the next. Matching the crests in consecutive differenced frames is based on:

1. propagation direction of the centers of mass of $\pm 90^\circ$ relative to the ship's orientation which was pointed into the wind.
2. a propagation speed less than 1.2 times the phase speed of the waves at spectral peak.
3. change in area and major axis length less than 25%
4. orientations of the major axes within 15°

The theoretical minimum detectable crest advancement speed is dictated by the pixel resolution and the frame rate. A breaking crest can be seen to move from one frame to the next only if it traveled at least the equivalent distance of 1 pixel (0.1 m) in between acquisition (1/20 s). Thus, at the native frame rate only waves traveling at a minimum speed of 2 m s^{-1} are detectable. To reduce the resolvable propagation speed to 1 m s^{-1} , breaking waves were tracked in every other image. Note, however, that the coor-

ordinates of the center of masses are determined within fractions of pixels thus propagation speeds smaller than 1 m s^{-1} can result from the analysis.

3.2 Breaking crest length distributions

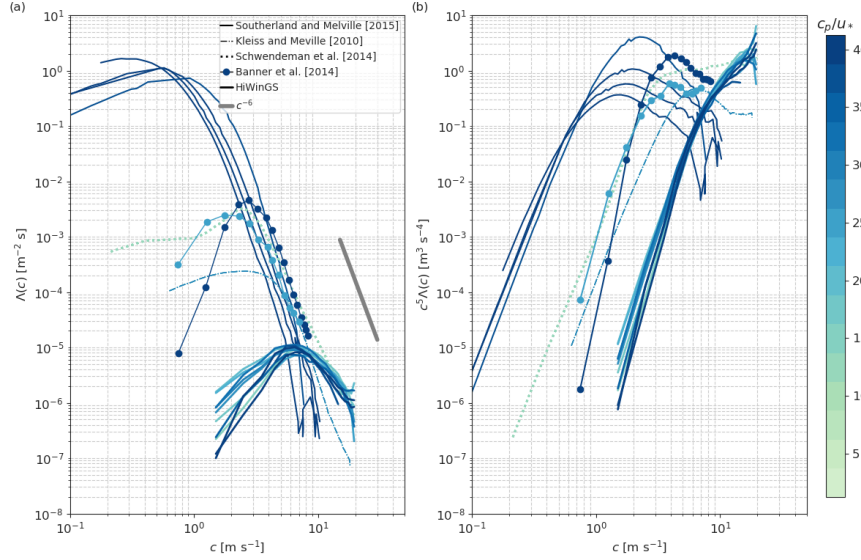


Figure 2. (a) Breaking crest length distributions and (b) their fifth moment as a function of the breaking crest speed color-coded by wave age ($\frac{c_p}{u_*}$).

Figure 2a shows the breaking crest length distributions as a function of the breaking speed computed from the HiWinGS data set color-coded by wave age ($\frac{c_p}{u_*}$). Figure 2b shows their fifth moment. Also shown are some of the previous breaking crest length determined from visible imagery. Much younger seas and higher winds were sampled during HiWinGS than during most of the previous field experiments outlined above. It is also important to note that different analysis techniques were used by the different groups. Only the two RaDyO datasets presented in Gemmrich et al. (2013) were analyzed with the technique used here. Mean breaking crest length distributions from Gemmrich’s analysis are reported in Banner et al. (2014) and shown in 2. The discrepancies arising from the various analysis techniques and choices in independent variables (in particular c_{br}) used to compute the breaking crest length distributions were highlighted by Banner et al. (2014) and will not be discussed further here. Nevertheless, these systematic differences

have to be taken into consideration when comparing the breaking crest length distributions plotted here. The breaking crest length distribution computed from the HiWinGS data follow less closely the theoretical c^{-6} high c_{br} tail than previously published ones. This means that scalings for Λ such as those proposed by Sutherland and Melville (2013) or Deike and Melville (2018) poorly reproduce them (c.f. SI). There is no clear explanation for this discrepancy at this time.

3.3 Determining the Framework's Coefficients

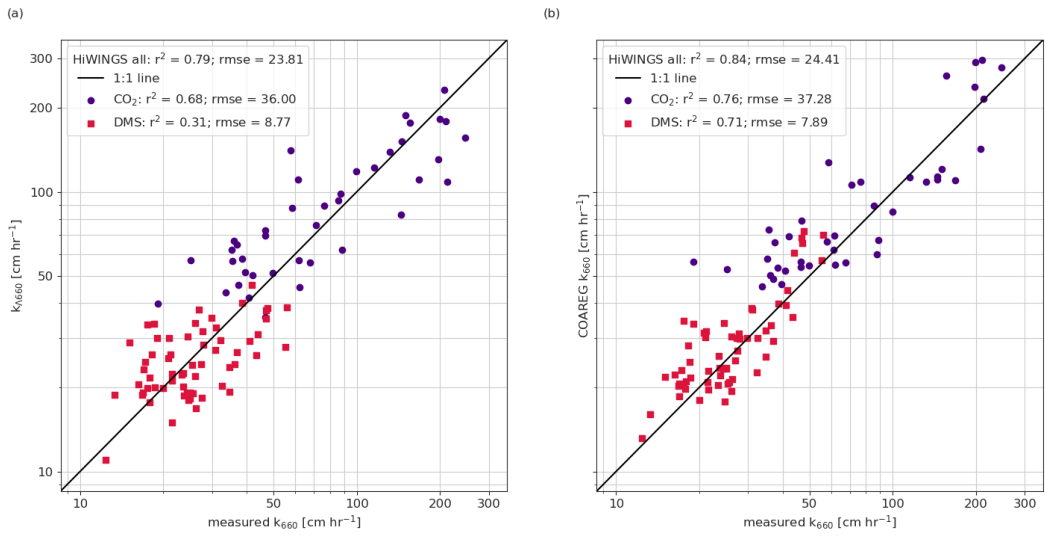


Figure 3. Scatter plots of (a) the k_{Λ} model proposed in Eq. 20: $k_{\Lambda 600} = 0.21K_{\epsilon} + 3.26F_a\alpha^{-1} \left(1 + (0.088Sc^{-0.5}F_a\alpha^{-1})^{1/1.2}\right)^{-1.2}$ and (b) the COAREG model (see SI for equations) versus the gas transfer velocities of CO₂ (purple) and DMS (ruby) estimated from HiWinGS eddy-covariance flux measurements referenced to a Schmidt number of 660.

A non-linear least squares fit of the HiWinGS data within the proposed breaking framework for the gas transfer velocity k_{Λ} (Eq. 20) provides $\mathcal{A} = 0.211 \pm 0.034$, $\mathcal{B} = 3.26 \pm 0.574$, and $\mathcal{C} = 0.088 \pm 0.072$. Variability linked to the b_{eff} parameterization (Eq. 13) was propagated. Results are shown in Figure 3a. k_{Λ} from Equation 20 is able explain 79% of the overall variability in the measurement derived gas transfer velocities. The correlations to the transfer velocities of CO₂ ($r^2 = 0.68$) and DMS ($r^2 = 0.31$) individually are lower than for the overall fit, particularly for DMS. Output of NOAA's

COAREG algorithm (Blomquist et al. (2017); Fairall et al. (2011); equations in SI) for matching measurements are shown in Figure 3b allowing to evaluate the relative performance of the mechanistic model proposed by Eq. 20. COAREG is able to reproduce 76% and 71% of the transfer velocities of CO₂ and DMS, respectively. The root mean square errors of the two models are overall of the same order of magnitude: 23.81 cm hr⁻¹ for the breaking crest length based model and 24.41 cm hr⁻¹ for COAREG for CO₂ and DMS combined. Note that fixing \mathcal{A} using the DMS data assuming no bubble contribution to its transfer ($k = \mathcal{A}K_\varepsilon$) and subsequently determining the other coefficients with the CO₂ data results in poorer fit statistics for DMS while not improving those for CO₂.

4 Discussion

4.1 Comparison to other mechanistic models

The base functional form of the model for k (Eq. 1) is a linear combination of parameterizations of transfer velocities arising from different processes. As such, it follows the form adopted by previous studies (Deike and Melville, 2018; Fairall et al., 2011; Asher and Wanninkhof, 1998). Unlike in COAREG, it does not take into account the air-side transfer and is therefore only applicable to sparingly and less soluble gases. This could explain its poorer performance, particularly for DMS.

No distinction is made between the turbulence-mediated transfer due to wave breaking and other processes as is done in Asher and Wanninkhof (1998); Shuiqing and Dongliang (2016). This is because computing the dissipation using the effective breaking strength gives an integrated estimate of the turbulence in the upper ocean at the given whitecap coverage and wave age. Indeed, b_{eff} was determined from the combination of breaking crest length distribution estimates and measures of the upper ocean turbulence that include both the wave breaking turbulence and the background turbulence (Zappa et al., 2016).

The proportionality coefficient $\mathcal{A} = 0.211 \pm 0.034$ that multiplies K_ε to give k_ε is within the range of those determined in previous studies none of which account for bubbles ($k = k_\varepsilon$). Zappa et al. (2007) suggested $\mathcal{A} = 0.4$ based on data collected in a large tidal river, a macro-tidal estuary, and from a coastal ocean site as well as in a “model” saltwater ocean at Biosphere 2 (Oracle, AZ USA). Later studies by Tokoro et al. (2008) suggest $\mathcal{A} = 0.17$ -0.18 for riverine and coastal environments while Vachon et al. (2010)

determined $\mathcal{A} = 0.39\text{-}0.44$ in freshwater systems. The first open ocean verification of the functional form of k_ε suggest $\mathcal{A} = 0.12\text{-}1.46$ depending on the depth at which the turbulent kinetic dissipation rate measurements were taken and the approach used to extrapolate these measurements to the surface (Esters et al., 2017). Note that in this study different values of \mathcal{A} were determined for CO_2 and DMS as the transfer velocities of these gases cannot be reconciled without taking bubble-mediated transfer into account. While fitting the transfer velocities separately may have led to improved fit statistics, it would defeat the goal of finding an unified model for both if not all gases. Since \mathcal{A} depends on the measurement of ε at the surface and observations vary greatly over the depth that it is evaluated, direct comparison between studies is difficult. As shown in Zappa et al. (2009), the near-surface dissipation can vary several orders of magnitude in the top 50 cm and will have a distinct impact on the gas transfer velocity. The value reported here is one corresponding to an integrated dissipation over the depth of the wave boundary layer roughly equal to the height of the wind-sea.

The form of the bubble-mediated transfer used in Asher and Wanninkhof (1998) could not be used for this study because 1) a wider variety of solubility have to be considered to estimate the coefficients and there are more unknowns than gases available, and 2) it accounts for wave breaking only via W . Asher and Wanninkhof (1998) developed their model using laboratory W which may have led to unrealistic estimates of both the bubble and the wave breaking turbulence mediate transfers. One could easily use the functional form proposed by Merlivat et al. (1993) for the bubble-mediated transfer with the coefficients determined by Asher and Wanninkhof (1998) to estimate K_b in Eq. 20. This however defeats the goal of a purely breaking crest length and sea state dependent model.

Both Woolf (1997), Woolf et al. (2007) and Goddijn-Murphy et al. (2016) assumed that the left and right hand side terms of Eq. 5 are equal rather than proportional. In both the model proposed herein and COAREG k_b scaling is adjusted through the empirical parameters \mathcal{B} and \mathcal{B}_{COAREG} , respectively. Note that these cannot be set independently from the models' other adjustment constants. \mathcal{B}_{COAREG} further depends on the choice of the W parameterization. Its original value of 1.8 was tuned to the SO GasEx data using the Monahan and O'Muircheartaigh (1980) W parameterization which was shown to highly over estimate W at high wind speeds (Brumer et al., 2017b). Based on the HiWinGS data set, Blomquist et al. (2017) updated \mathcal{B}_{COAREG} to equal 3.8 which

is close to the value found in the present study. Although the same parameterization is at the base of the bubble-mediated transfer in the present framework and in COAREG, \mathcal{B} and \mathcal{B}_{COAREG} are not directly comparable as they depend on the measure of the bubble air volume flux (F_a) used and on χ (Eq. 7). The bubble air volume flux estimated here from the breaking crest length distribution is about twice as large as that computed in COAREG using 2450 W .

Values of these empirical factors are not independent and reflect the uncertainties in the breaking crest length derived statistics. The choice of U_b and B will impact \mathcal{B} and \mathcal{C} which further account for the fact that we are dealing with estimates of the integrated flux of bubble plumes without resolving variations in the bubble size distributions and the flux and lifetime of individual bubbles. The empirical constants \mathcal{A} and \mathcal{B} could be interpreted as efficiencies of the turbulent driven and bubble mediated transfer, respectively. \mathcal{C} encompasses the fact that full equilibration depends on the the limited volume of water between bubbles which is linked to the void fraction. A constant \mathcal{C} does not allow for any variation (sea-state dependent or other) of the void fraction. A form of K_b including a breaking crest length dependent void fraction is derived in SI. It contains more unknowns and results in more scatter.

4.2 Remaining unknowns and limitations

Although the assumed functional form follows the typical approach used in other process based models, it may not be entirely correct. Indeed, it is not the gas transfer velocities that should be combined linearly, but rather the bubble- and turbulence-mediated fluxes ($F_g = F_\epsilon + F_b$). The partial pressure of a gas within a bubble is higher than that in the atmosphere due to the pressure caused by the surface tension of the bubble skin, which can be estimated from the Young-Laplace equation and hydrostatic pressure of the surrounding water. Estimation of this excess pressure a bubble requires knowledge of the bubble size distribution as a function of depth and time.

The formulations of the bubble air volume flux contain several unknowns other than the bubble plume depth discussed above. The first unknown is the bubble cloud constant B which was set to 0.1 in accordance to Deike et al. (2016, 2017). B was determined from laboratory data from Duncan (1981), Lamarre and Melville (1991) and Deane and Stokes (2002) for time averaged volumes of air entrained \bar{V} by a single breaking wave ranging

several orders of magnitude ($10^{-7} < \bar{V} < 10^{-1} \text{ m}^3$). The relationship however does not hold for $\bar{V} < 10^{-5} \text{ m}^3$ and it is unclear how these scale for open ocean conditions. The other unknown is the dissipation-weighted vertical mean bubble plume rise velocity (U_b). A constant U_b of 10 cm s^{-1} was used, corresponding to the rise terminal rise velocity of clean bubble of radius of $450 \text{ }\mu\text{m}$ according to Woolf and Thorpe (1991). It is of the same order of magnitude as the rise velocity measured by Asher et al. (1997) in a sea-water tank which averaged around 8 cm s^{-1} within the first 6 seconds. Deike et al. (2017) proposed the following parameterization for U_b :

$$U_b \sim h/\tau_{br} \quad (22)$$

where h is the height of the wave at the time of breaking. While h is not measured directly it may be approximated as the significant height of the wind-sea (H_{sws}). The proportionality factor has however yet to be established. Since H_{sws} ranges from ~ 0.1 to 8 m and τ_{br} is on the order of $1\text{-}10 \text{ s}$, a proportionality coefficient equal to 1, as suggested by Deike et al. (2017), would lead to rise velocities ranging from a couple of centimeters a second to over a meter a second which is clearly too high.

Choosing a scale dependent U_b such as given by Eq. (22) would make F_a a function of the 5th moment of $\Lambda(c)$ (c.f. Eq. 17). To date there is not enough independent evidence or a sound physical argument to rule on the validity of one formulation over the other. This is also true with regards to the approach taken here versus that of Deike and Melville (2018) whose F_a is a function of the 3rd moment of $\Lambda(c)$. The fundamental difference is that they take a scale dependent $b(c)$ rather than b_{eff} based on the assumption that c_{br} may be related to a wavenumber through the deep water dispersion relation (Romero et al., 2012). Validity of this transformation has however been challenged (Zappa et al., 2016; Banner et al., 2014).

Finally, throughout this framework, a Schmidt number exponent of $\frac{1}{2}$ is used (Eqs. (4), (5)) which is in accordance with open ocean scaling. The exponent was suggested to vary between $\frac{1}{2}$ for wavy, surfactant free conditions to $\frac{2}{3}$ for flat, film covered surfaces. The exponent may therefor need adjustment for coastal applications and other surfactant-influenced surface conditions. The impact of surface-active material on the framework's coefficients (\mathcal{A} , \mathcal{B} , \mathcal{C}) remains unknown.

5 Conclusions

A novel framework to model the gas transfer velocity of sparingly soluble gases under breaking wave conditions in the open ocean is presented herein. It allows for estimations based on the breaking crest length distributions and sea state. As such it is applicable to purely remotely sensed data. Tuned to measurements from the HiWinGS field campaign it performs comparably to the COAREG algorithms. Higher noise in breaking length derived statistics compared to whitecap and friction velocity estimates accounts for relatively poorer results of the breaking crest length dependent model compared to COAREG. Unknowns remain in the formulation of the bubble-mediated transfer as is the case with other physically based models put forward in the literature. Measurements of bubble plumes in the ocean are necessary for further improvement.

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Supporting Information for ”A novel wave breaking framework to estimate air-sea gas transfer velocities”

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1. Text S1 to S4
2. Figures S1 to S2

Introduction

Text S1 provides more details regarding the breaking crest detection and tracking algorithm which should be sufficient to replicate it. It lists the functions of the Matlab image processing toolbox used. Note that the algorithm should be adapted to the spatial resolution of the imagery it is applied on.

Text S2 provides the equation for breaking crest length distribution scalings proposed in the literature (Deike and Melville, 2018; Sutherland and Melville, 2013). Both are based on the same dataset. Deike and Melville (2018) proposed a simplified form which is plotted in Figure S1 for HiWinGS conditions along with the breaking crest length distribution

determined in this study. A poor correspondence between the HiWinGS data and the scaling can be observed which may stem from the fundamentally different way breaking crest length distribution were computed in this study and those from which the scalings were derived. Addressing the difference is an active area of research which goes beyond the scope of this publication.

Text S3 recalls the main equations of the NOAA-COAREG algorithm. These can be found in Blomquist et al. (2017); Fairall et al. (2011) and references therein.

Text S4 discusses an alternate formulation of the bubble mediate transfer which accounts for suffocation which may occur in dense bubble plumes. It depends on an additional bubble plume characteristic which may be estimated from breaking crest length distribution and sea state statistics: the void fraction. Related geometric consideration of breaking waves and associated bubble plumes are illustrated in Figure S2. Due to an increased number of unknowns and scatter in results this formulation was not retained for the main framework.

Text S1. Steps of the breaking crest detection and tracking algorithm

1. Intrinsic and extrinsic image correction is applied to the images of a given video (frequency down-sampling is applied in this loop) which are re-gridded onto a regular x,y grid resulting in an image matrix $I(t, x, y)$ where t is the time dimension time
2. This matrix is differences with respect of time: $\text{diff}I = I(2:\text{end}, :, :) - I(1:\text{end}-1, :, :)$
3. $\text{diff}I$ is converted into a binary matrix (1 for advancing crest, 0 for rest) based on an intensity threshold: $BW = \text{im2bw}(\text{diff}I ./ \max(\text{diff}I(:)), 0.6)$
4. Holes are filled using $BW = \text{imfill}(BW, 'holes')$
5. The features in the image are dilated using $BW = \text{imdilate}(BW, \text{strel}('diamond', 10))$
6. Pixels separated by only 1 pixel are connected using : $BW = \text{bwmorph}(BW, 'bridge')$
7. Pixels are set to 1 if at least 5 pixels within a 3x3 neighbouring area are 1, if not they are set to 0 using: $BW = \text{bwmorph}(BW, 'bridge')$
8. Holes are filled $BW = \text{imfill}(BW, 'holes')$
9. The features in the image are eroded using $\text{imerode}(BW, \text{strel}('diamond', 5))$
10. Individual features are identified and labeled: $[L, NO] = \text{bwlabeln}(BW, 8);$
11. Region properties (area, orientation) are computed $L_props = \text{regionprops}(L, 'area', 'orientation')$
12. Only features greater than the chosen area threshold (AreaThresh) are kept and labels are re-assigned: $BW = \text{ismember}(L, \text{find}([L_props.Area] > \text{AreaThresh})); [L, NO] = \text{bwlabeln}(BW, 8)$
13. Breaking crests are tracked from one differenced image pair to the next by matching features that evolve corresponding to to the criterion mentioned in section 3.1.

Text S2. Lambda scaling

Two scalings have been proposed for $\Lambda(c)$ for $c > c_{min}$ assuming a c^{-6} tail:

1. Deike and Melville (2018):

$$\Lambda(c) = 0.25 \frac{g}{\sqrt{gH_s}^3} \left(\frac{c}{\sqrt{gH_s}} \right)^{-6} \left(\frac{u_*}{\sqrt{gH_s}} \right)^{5/3} \quad (\text{S1})$$

$$c_{min} = 0.85 \sqrt{gH_s} \quad (\text{S2})$$

2. Sutherland and Melville (2013):

$$\Lambda(c) = \frac{g}{c_p^3} \sqrt{\frac{u_*}{c_p}} \frac{c}{gH_s} \left(\frac{gH_s}{c_p^2} \right)^{0.1} \quad (\text{S3})$$

Figure S1 show how the scaling of Deike and Melville (2018) for the HiWinGS sea state conditions compares to the imagery derived breaking crest length distribution.

Text S3. The NOAA-COAREG algorithm

The key equations of the NOAA-COAREG algorithm are recalled in the following section. These were published in Blomquist et al. (2017); Fairall et al. (2011) and references therein. The gas transfer velocity is composed of an air- ($1/k_a$) and a water-side resistance ($1/k_w$):

$$k = (\alpha/k_a + 1/k_w)^{-1} \quad (\text{S4})$$

The air-side transfer depends on the air friction velocity (u_*), the atmospheric velocity drag coefficient (C_d), and the Schmidt number for the gas in the air (Sc_a).

$$k_a = u_* / \left(13.3 Sc_a^{1/2} + C_d^{1/2} - 5 + \ln(Sc_a)/(2\kappa) \right) \quad (\text{S5})$$

The water-side transfer is composed of a turbulent molecular transfer (k_{wt}) and a bubble mediated (k_b) one:

$$k_w = k_{wt} + k_b \quad (\text{S6})$$

The turbulent molecular transfer formulation takes the cool skin buoyancy driven transfer at low wind though an empirical function Φ in addition to effects of the tangential wind stress:

$$k_{wt} = u_* / (\rho_w / \rho_a)^{1/2} / \left(13.3 / (\mathcal{A}_{COAREG} \Phi) Sc^{1/2} + \ln(z_w / \delta_w) / \kappa \right) \quad (\text{S7})$$

Here z_w is set to 0.5 and the Schmidt number of the gas in water (Sc) to 660. The cool-skin thickness, δ_w , is computed in the iterative loop of the COARE algorithm as is Φ .

The bubble mediated transfer formulation is that of Woolf (1997):

$$k_b = \mathcal{B}_{COAREG} \times 2450 W \alpha^{-1} \left(1 + \left(14 \alpha Sc^{-0.5} \right)^{1/1.2} \right)^{-1.2} \quad (\text{S8})$$

The whitecap fraction W is parameterized as a function of wave-wind Reynolds number following Brumer et al. (2017):

$$W = 4.48 \times 10^{-6} \left(\frac{u_* H_s}{\nu_w} \right)^{0.90} / 100 \quad (\text{S9})$$

The two adjustment factors \mathcal{A}_{COAREG} and \mathcal{B}_{COAREG} are set to 1.2 and 3.8, respectively, based on the HiWinGS measurements (Blomquist et al., 2017).

Text S4. Accounting for suffocation

The model based on Eq. 5 does not account for the potential “suffocation” effect of bubbles within dense clouds. This effect was suggested to arise from the fact that bubbles evolve within a finite volume of water with relatively small interstitial space which has limited capacity to take up gases, thus restricting the bubble-mediated transfer (Woolf et al., 2007). An alternate form for k_b , labeled as the “dense plume model” was therefor proposed:

$$k_{b_{void}} \propto W \times X \frac{F_{a_{1\%}}}{\alpha} (1 + (X\chi)^{1/1.2})^{-1.2} \quad (\text{S10})$$

with

$$X = \alpha F_{w_{1\%}} / (\alpha F_{w_{1\%}} + F_{a_{1\%}}) \quad (\text{S11})$$

$F_{a_{1\%}}$ is the volume flux of air for 1% whitecap cover, i.e $F_{a_{1\%}} = F_a/W$, which Woolf et al. (2007) set to equal 24.5 cm hr^{-1} . $F_{w_{1\%}}$ is the volume flux of water within bubble plume relative to $F_{a_{1\%}}$ and is related to $F_{a_{1\%}}$ through the void fraction:

$$v = \frac{F_{a_{1\%}}}{F_{a_{1\%}} + F_{w_{1\%}}}. \quad (\text{S12})$$

Thus:

$$F_{w_{1\%}} = \frac{F_{a_{1\%}}}{v} - F_{a_{1\%}} \quad (\text{S13})$$

and

$$X = \frac{\alpha/v + \alpha}{\alpha/v + \alpha + 1} \quad (\text{S14})$$

The void fraction for a given breaking wave (v_{br}) can be estimated from V_a , the surface area of active breaking (A_{br}), which is proportional to the breaking crest length times

the “swept out” length of the breaker ($L_{br} \times c_{br} t_{br}$, see Figure S2), and the depth of the bubble plume (h):

$$v_{br} = \frac{V_a}{A_{br} h} = b_{eff} \frac{B}{U_b g^2} \frac{L_{br} c_{br}^5}{L_{br} c_{br} t_{br} h} = b_{eff} \frac{B}{U_b g^2} \frac{c_{br}^4}{t_{br} h} \quad (\text{S15})$$

The time averaged void fraction is then:

$$\bar{v} = \frac{\sum v_{br} t_{br}}{T} \quad (\text{S16})$$

The bubble plume depth remains elusive, but may be assumed to be proportional to the significant wave height of the wind-sea (H_{sws}) or to the “swept out” length of the breaker ($c_{br} t_{br}$). Figure S2 illustrates the assumed geometry of a plunging breaker and the subsequent bubble plume. Recent work (Cifuentes-Lorenzen et al., 2020) suggests that the peak wave number k_p is a better predictor for the bubble plume depths based on acoustic backscatter measurements due to breaking waves in the Southern Ocean.

The three estimates are then given by:

1. assuming $h \propto H_{sws}$ (e.g., Rapp and Melville, 1990; Lamarre and Melville, 1991; Baldy and Bourguel, 1987):

$$\bar{v} \propto \frac{b_{eff} B}{H_{sws} T U_b g^2} \sum c_{br}^4. \quad (\text{S17})$$

2. assuming $h \propto c_{br} t_{br}$ (e.g., Deike et al., 2016):

$$\bar{v} \propto \frac{b_{eff} B}{T U_b g^2} \sum \frac{c_{br}^3}{t_{br}}. \quad (\text{S18})$$

3. assuming $h \propto f(k_p)$:

$$\bar{v} \propto \frac{b_{eff} B}{f(k_p) T U_b g^2} \sum c_{br}^4. \quad (\text{S19})$$

Note that all three forms are independent of the breaking crest length and cannot be expressed in terms of moments of the breaking crest length distribution. They are however

straight forward to determine from the imagery during the processing to obtain $\Lambda(c)$. In light of recent modeling advances (Romero, 2019), breaking crest length distribution dependant formulations are of higher interest to the community. What is more, Eq. S10 contains more uncertainties than Eq. 5). Using the right hand side of Eq. S10, with the void fraction estimated based any of the above equations instead of K_b leads to very poor overall correlations ($r^2 \sim 0.1$) on account of the large scatter in \bar{v} .

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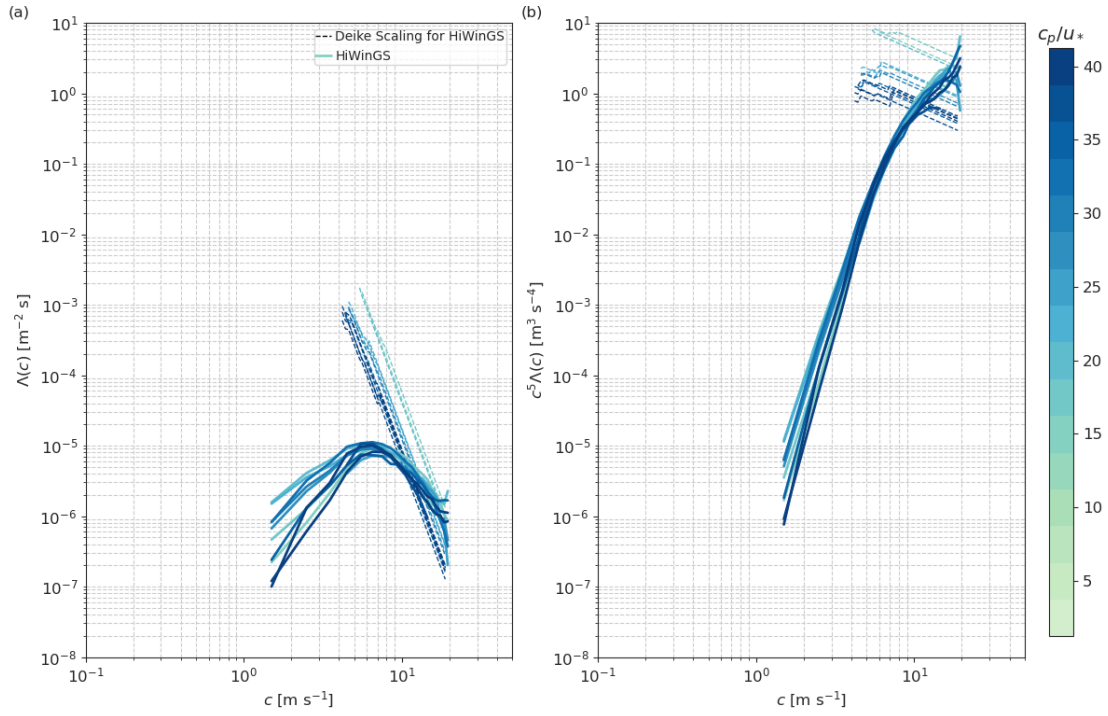
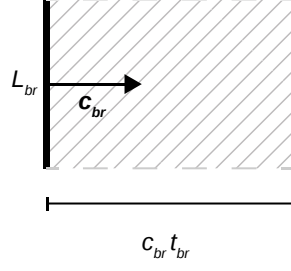


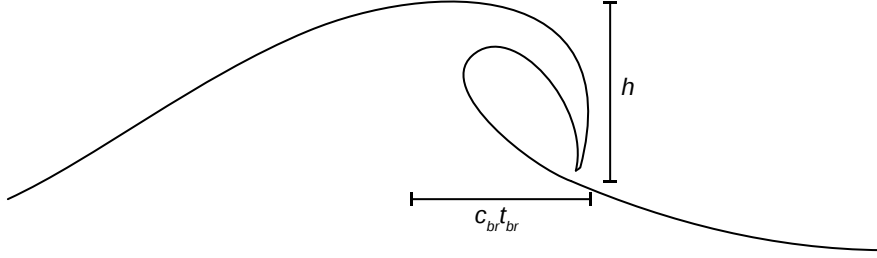
Figure S1. (a) Breaking crest length distributions and (b) their fifth moment as a function of the breaking crest speed color-coded by wave age ($\frac{c_p}{u_*}$). The HiWinGS data is plotted in solid lines while the corresponding Deike and Melville (2018) scaling is in dashed lines.

(a) Top View



(b) Side view of a plunging breaker

(1) Pre breaking



(2) Post breaking

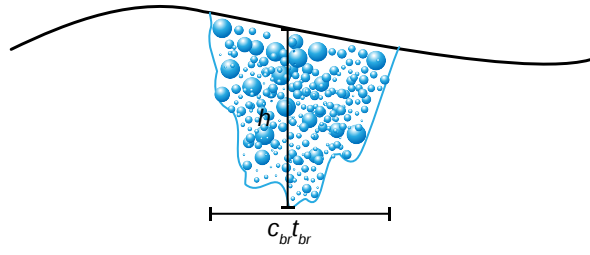


Figure S2. Sketch illustrating (a) the assumption that the swept out area is related to the length of breaking L_{br} , the translation $c_{br}t_{br}$ and (b) the assumed geometry of (1) a plunging breaker, and (2) the subsequent bubble plume.