# Micromagnetic Tomography for Paleomagnetism and Rock-Magnetism

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# Abstract

Our understanding of the past behavior of the geomagnetic field arises from magnetic signals stored in geological materials, e.g. (volcanic) rocks. Bulk rock samples, however, often contain magnetic grains that differ in chemistry, size and shape; some of them record the Earth's magnetic field well, others are unreliable. The presence of a small amount of adverse behaved magnetic grains in a sample may already obscure important information on the past state of the geomagnetic field. Recently it was shown that it is possible to determine magnetizations of individual grains in a sample by combining X-ray computed tomography and magnetic surface scanning measurements. Here we establish this new Micromagnetic Tomography (MMT) technique and make it suitable for use with different magnetic scanning techniques, and for both synthetic and natural samples. We acquired reliable magnetic directions by selecting subsets of grains in a synthetic sample, and we obtained rock-magnetic information of individual grains in a volcanic sample. This illustrates that MMT opens up entirely new venues of paleomagnetic and rock-magnetic research. MMT's unique ability to determine the magnetization of individual grains in a nondestructive way allows for a systematic analysis of how geological materials record and retain information on the past state of the Earth's magnetic field. Moreover, by interpreting only the contributions of known magnetically well-behaved grains in a sample MMT has the potential to unlock paleomagnetic information from even the most complex, crucial, or valuable recorders that current methods are unable to recover.

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<sup>16</sup> Key Points:

17	• Micromagnetic Tomography enables determining, selecting, and interpreting mag-
18	netizations of individual grains in a sample
19	• We obtained magnetic directions and rock-magnetic information from subsets of
20	grains in both a synthetic and a natural sample
21	• Micromagnetic Tomography has the potential to unlock magnetic information from
22	even the most complex recorders that currently goes obscured

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#### 23 Abstract

Our understanding of the past behavior of the geomagnetic field arises from magnetic 24 signals stored in geological materials, e.g. (volcanic) rocks. Bulk rock samples, however, 25 often contain magnetic grains that differ in chemistry, size and shape; some of them record 26 the Earth's magnetic field well, others are unreliable. The presence of a small amount 27 of adverse behaved magnetic grains in a sample may already obscure important infor-28 mation on the past state of the geomagnetic field. Recently it was shown that it is pos-29 sible to determine magnetizations of individual grains in a sample by combining X-ray 30 computed tomography and magnetic surface scanning measurements. Here we establish 31 this new Micromagnetic Tomography (MMT) technique and make it suitable for use with 32 different magnetic scanning techniques, and for both synthetic and natural samples. We 33 acquired reliable magnetic directions by selecting subsets of grains in a synthetic sam-34 ple, and we obtained rock-magnetic information of individual grains in a volcanic sam-35 ple. This illustrates that MMT opens up entirely new venues of paleomagnetic and rock-36 magnetic research. MMT's unique ability to determine the magnetization of individual 37 grains in a nondestructive way allows for a systematic analysis of how geological mate-38 rials record and retain information on the past state of the Earth's magnetic field. More-30 over, by interpreting only the contributions of known magnetically well-behaved grains 40 in a sample MMT has the potential to unlock paleomagnetic information from even the 41 most complex, crucial, or valuable recorders that current methods are unable to recover. 42

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# Plain Language Summary

Our understanding of the past behavior of the Earth's magnetic field relies on our 44 ability to interpret magnetic signals from rocks. Currently, we measure bulk samples con-45 sisting of many magnetic grains at once. Not all magnetic grains are good recorders of 46 the geomagnetic field. The presence of even small amounts of adverse behaved grains in 47 a sample already obscures vital information about the Earth's magnetic field. Here we 48 present and establish a new method that determines magnetizations of individual grains 49 in a sample: Micromagnetic Tomography. This new and exciting method allows to se-50 lect and interpret only magnetizations of grains that are known good recorders in a sam-51 ple. This will unlock magnetic information from even the most complex, crucial, or valu-52 able samples that current methods are unable to recover. 53

# 54 1 Introduction

To understand the behavior of the Earth's magnetic field, and possibly even pre-55 dict its future behavior, it is paramount to understand its past. Our understanding of 56 the behavior of the geomagnetic field arises from magnetic signals stored in geological 57 and archeological materials. They acquire a magnetization when they cool in the Earth's 58 magnetic field, and retain that magnetization over (geological) timescales. Igneous rocks, 59 e.g. lavas, are the only recorders of the direction and the intensity of the field that are 60 available throughout geologic history and all over the globe. Since lavas take snapshots 61 of the state of the Earth's magnetic field for their location and point in time when they 62 cool, frequently erupting volcanic regions with well-dated volcanic products are invalu-63 able archives of past variations in the Earth's magnetic field (e.g.: de Groot et al., 2013; 64 Cromwell et al., 2015; Greve et al., 2017). 65

When a volcano erupts and lava cools on its flanks the lava solidifies to form ex-66 trusive igneous rocks, often of basaltic composition. A small, but significant, portion of 67 the minerals that together constitute these basalts has magnetic properties. Lavas are 68 often regarded to be excellent paleomagnetic recorders, but over the past years evidence 69 piled up that their magnetic signal is often compromised. This has been known for a long 70 time for reconstructions of variations in field strength. Viscous changes in the magnetic 71 signal of natural rocks (e.g.: Shaar et al., 2011; de Groot, Fabian, et al., 2014) or ther-72 mochemical changes during laboratory experiments (e.g.: Fabian, 2009; Shcherbakov et 73 al., 2019) frequently hamper paleointensity experiments (Tauxe & Yamazaki, 2015). But 74 even obtaining a paleomagnetic direction from volcanic samples is not always straight-75 forward, as illustrated by a recent reappraisal of the paleomagnetic signal stored in a stack 76 of lava flows from Steens Mountain (Coe et al., 2014), that falsified a previous interpre-77 tation of a very rapid change in the direction of the Earth's magnetic field during a ge-78 omagnetic polarity reversal (Prévot et al., 1985). 79

Almost all experiments to determine the past state of the Earth's magnetic field from rocks use bulk samples (usually  $\sim 10$  cc) and measure their magnetic moment after series of laboratory treatments. Lavas consist of mixtures of different iron-oxides that vary in size, shape, and chemistry. These iron-oxide grains are the actual magnetic recorders in the samples. Some of these grains record the Earth's magnetic field well; others may not able to provide reliable information on its past state. When measuring a typical pa-

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leomagnetic sample, the magnetic moments of millions of grains are measured simultaneously and result in one magnetic moment for the entire sample. A small amount of
adverse behaved magnetic grains in a sample already hampers any classical experiment
to obtain paleointensities. Therefore, these experiments often fail and success rates as
low as 10-20% are common (Valet, 2003; Tauxe & Yamazaki, 2015). This implies that
for 80-90% of all lavas vital information on paleointensities is lost before it can be uncovered.

The iron-oxide grains in a lava acquire a magnetization that is proportional to the 93 ambient magnetic field during cooling; such magnetizations are referred to as 'thermore-94 manent magnetizations' (TRMs). The magnetic properties of iron-oxide grains vary dra-95 matically due to differences in grain size, shape, chemistry and thermal history as sum-96 marized by Dunlop and Özdemir (1997). The magnetic behavior of very small 'single do-97 main' iron-oxides (30-60 nm) is described by Néel's theory on thermoremanent magne-98 tizations in single-domain ferromagnetic minerals (Néel, 1949, 1955). These grains are 99 magnetically well-behaved; if a sample would consist of only such small grains it would 100 be relatively straightforward to obtain a reliable estimate of both the paleodirection and 101 paleointensity of the Earth's magnetic field using classical paleomagnetic techniques. Un-102 fortunately, iron-oxides in naturally occurring lavas are generally much larger (up to >50103 µm). Not only do these 'multi-domain' grains violate Néel's theory, they also often vi-104 olate Thellier's laws of reciprocity, independence and additivity (e.g.: Thellier & Thel-105 lier, 1959; Coe, 1967; Shcherbakova et al., 2000; Fabian, 2000, 2001; Dunlop, 2011; Tauxe 106 & Yamazaki, 2015). Moreover, these multi-domain grains may be prone to unstable mag-107 netizations over time caused by e.g. viscous reordering of magnetic domains (de Groot, 108 Fabian, et al., 2014), or time and temperature dependent cation reordering (Bowles et 109 al., 2013; Bowles & Jackson, 2016). In contrast to Néel's theory for single domain grains, 110 there currently is no comprehensive, fundamental theory for the processes governing the 111 acquisition and preservation of magnetic signals in multi-domain grains; i.e. their mag-112 netic behavior still is enigmatic – although they make up the vast majority of the rema-113 nence carrying grains in igneous rocks. 114

If we would be able to determine the magnetic moments of individual mineral grains inside a natural sample in a non-destructive way, we could determine which naturally occurring iron-oxide grains record the Earth's magnetic field well, and which are unreliable. This would enable us to select and consider only the magnetic contributions of

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known well-behaved magnetic grains, and reject the contributions of others. Thereby we
could fully unlock the paleomagnetic information stored in all sorts of geological materials, even if large amounts of adverse behaved magnetic minerals are present in the sample. This will provide indispensable data to understand the behavior of the geomagnetic
field on decadal to centennial time scales, and possibly enables predictions of its future
behavior.

Information about the magnetic state of individual grains in a sample can theo-125 retically be obtained from scans of magnetic anomalies on the surface of a sample, if the 126 spatial resolution permits. The rock-magnetic interpretation of these magnetic surface 127 scans, however, is notoriously difficult. The classical potential inversion problem (Kellogg, 128 1929) states that it is impossible to obtain unique information on the distribution of mag-129 netic sources (i.e. our grains) within a body (i.e. our sample), based on observations of 130 the magnetization outside this body alone. Additional information or assumptions are 131 necessary to characterize the magnetic sources (Lima & Weiss, 2009; Lima et al., 2013). 132 Currently, the interpretation of these magnetic maps is often done by an 'upward con-133 tinuation' of the magnetic measurements: the magnetic signal for the entire sample or 134 region is inferred by calculating the resulting magnetic moment further away from the 135 sample (Blakely, 1996; Lima & Weiss, 2009; Lima et al., 2014; Lima & Weiss, 2016; Fu 136 et al., 2020). This implicitly averages the magnetic contributions present in the region 137 of interest, without the possibility to assess or consider the quality of individual grains 138 as paleomagnetic recorders. 139

We recently overcame the non-uniqueness of the classical potential inversion prob-140 lem by adding the results of an X-ray Computed Tomography (microCT) scan to the re-141 sults of scanning magnetometry (de Groot et al., 2018). The microCT scan determines 142 the exact locations, sizes and shapes of the iron-oxides grains in a sample, which ensures 143 that our inversion routine can now only attribute magnetizations from the surface mag-144 netometry to the magnetic grains in our sample. The additional microCT information 145 therefore enables a unique inversion of the information produced by scanning magnetom-146 etry without the necessity of any further assumptions (Fabian & de Groot, 2019). With 147 this newly developed technique now known as Micro-Magnetic Tomography (MMT) the 148 individual magnetic moments of 20 grains inside a synthetic sample were successfully de-149 termined (de Groot et al., 2018). The synthetic sample used in this study, however, was 150 optimized for success: its concentration of magnetic grains was one to two orders of mag-151

nitude lower compared to natural samples; and pure magnetite grains with a well-defined 152 suite of grain sizes were used - in contrast to the large variation in grain sizes and chem-153 istry of naturally occurring iron-oxides. Given these characteristics of the synthetic sam-154 ple and the amount of grains for which magnetic moments were determined, the MMT 155 study by de Groot et al. (2018) is fore-mostly a proof-of-concept. Here we build on this 156 proof-of-concept and (1) show that the MMT technique is universally applicable by us-157 ing different magnetic scanning techniques, (2) up-scale the technique to be useful for 158 natural (volcanic) samples; (3) show that it is possible to acquire magnetic directions 159 by selecting subsets of grains present in a sample using MMT; and (4) acquire a rock-160 magnetic characterization of grains in a volcanic sample from MMT. This firmly estab-161 lishes MMT as a new paleomagnetic and rock-magnetic technique that is useful to un-162 lock information from samples with complex magnetic behavior that current paleomag-163 netic and rock-magnetic methods are unable to recover. 164

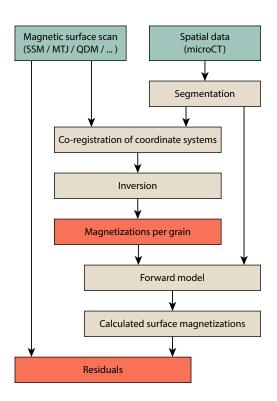
# <sup>165</sup> 2 Micromagnetic Tomography

The MMT technique determines the magnetic moments of individual grains in a 166 sample by inverting a two-dimensional magnetic surface scan of the sample based on the 167 known locations and shapes of the iron-oxide grains as determined by a microCT scan 168 of the sample. The input for any MMT experiment is thus (1) a magnetic surface scan, 169 and (2) a microCT characterization of the sample (Fig. 1). These two data sets must 170 first be co-registered into a common spatial coordinate system, before a mathematical 171 inversion of the magnetic surface scan constrained by the microCT data can produce the 172 magnetic moments of the grains. The accuracy of the inversion results can then be as-173 sessed by determining the residuals left by the inversion. 174

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# 2.1 MicroCT analysis

The locations, sizes, and shapes of the iron-oxide grains in a sample are determined using a microCT scan. This technique produces a three-dimensional image of the X-ray attenuation contrast in a sample, that is often interpreted in terms of variations in density in the sample (Sakellariou et al., 2004; Madonna et al., 2012; Jussiani & Appoloni, 2015). The densities of iron-oxides (e.g. magnetite: 5.2, hematite: 5.3, ülvospinel: 4.8, and ilmenite:  $4.8 \times 10^3$  kg/m<sup>3</sup>) are generally 1.4 to 2 times larger than the densities of other common minerals in basalt (e.g. plagioclases: 2.6-2.8, and pyroxenes  $3.2-3.9 \times$ 



**Figure 1.** Workflow of Micromagnetic Tomography experiments. The input (measurements) is in the green boxes; computational steps are in the tan boxes; and the output is in the red boxes.

10<sup>3</sup> kg/m<sup>3</sup>), although the heavier olivines (3.2-4.4×10<sup>3</sup> kg/m<sup>3</sup>), have a less profound
difference (density data from www.mindat.org). Because of these large density differences between iron-oxide minerals and other minerals and/or (synthetic) matrices present
in a sample, the attenuation contrast in microCT scans generally allows to precisely locate all iron-oxides with volumes above the voxel limit, and also to estimate their shape
and volume within the limits of the voxel representation.

When using microCT data it is up to the interpreter to make selections in the at-189 tenuation contrast spectrum in the sample for the segmentation of individual iron-oxide 190 grains by setting a density threshold above which voxels are deemed to belong to iron 191 oxide grains. The well-defined differences in density between the iron-oxides and the other 192 common minerals in basalt typically yield a bi-modal or multi-modal attenuation spec-193 trum in the microCT analysis, and the minimum separating the high-density peaks from 194 the lower density matrix minerals can be selected as threshold. It is important to set the 195 threshold such that all iron-oxide grains are included in the analysis, even if this implies 196 that some non-magnetic grains are also selected. After all, a grain that is selected can 197

be assigned a (near) zero magnetization by the inversion, but missing an iron-oxide grain 198 in the microCT analysis leads to magnetic anomalies in the magnetic surface scan that 199 cannot be properly assigned to their source. Setting the threshold for the attenuation 200 contrast results in a list of voxels with their spatial coordinates that pass this selection. 201 Groups of adjacent, interconnected, high-density voxels form a precisely localized grain, 202 for which also the size and shape are now approximately known. From these data the 203 volume, center of gravity, and distance to e.g. the surface of the sample can be estimated 204 for each grain individually. 205

The volume uncertainty related to voxel thresholding is difficult to assess because 206 it critically depends on the grain's shape. The fact that a thin iron-oxide plate with large 207 volume but thickness below a fraction of the voxel width  $\epsilon$  would not be recognized shows 208 that the error can be arbitrarily large. For bodies with surface area A and volume V the 209 relative volume uncertainty is in the order of  $A \epsilon / V$ , and thus for sphere-like bodies with 210 diameter D decreases with  $\epsilon/D$ . For the MMT technique the most important informa-211 tion is the location and topological separation of the iron-oxide grain or cluster which 212 will be assigned a separate magnetic moment by the inversion. Only the interpretation 213 of this magnetic moment in terms of a grain's magnetization requires the grain's volume 214 with its much larger uncertainty due to voxel binarization (Heidig et al., 2017). 215

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#### 2.2 Scanning magnetometry

Recent advances in scanning magnetometry techniques such as Scanning SQUID 217 Magnetometry (SSM) (Egli & Heller, 2000; Weiss et al., 2007; Lima & Weiss, 2016), in-218 struments using a Magnetic Tunnel Junction (MTJ) (Lima et al., 2014), and the Quan-219 tum Diamond Microscope (QDM) (Glenn et al., 2017; Farchi et al., 2017; Levine et al., 220 2019; Fu et al., 2020) allow for quantitative measurements of the magnetic field on, or 221 near, the surface of a sample in (sub)micrometer resolution. In theory, results from all 222 these magnetic surface magnetometry techniques can be used for MMT. The proof-of-223 concept of MMT (de Groot et al., 2018) was provided using a SSM, here we present MMT 224 results based on MTJ and QDM measurements. 225

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# 2.2.1 Scanning SQUID set-ups

In scanning SQUID microscopy a SQUID (Superconducting QUantum Interference 227 Device) sensor is used to measure magnetic fields above a sample. A SQUID sensor that 228 consists of a superconducting loop containing Josephson junctions hovers over (or is in 229 contact with) a sample and measures the component of the magnetic flux density per-230 pendicular to its surface (Kirtley & Wikswo, 1999; Reith et al., 2017). SQUID sensors 231 in SSM set-ups can attain effective magnetic moment sensitivities in the order of  $10^{-16}$ 232  $\mathrm{Am}^2$  and are therefore the most sensitive magnetometers to date. This makes them the-233 oretically very suitable for MMT analyses. It is the requirement of superconductivity, 234 however, that puts constraints on the usefulness of scanning SQUID set-ups for MMT. 235

In the SSM set-up used for the proof-of-concept of MMT (de Groot et al., 2018) 236 the sample was submerged with the SQUID sensor in liquid helium. This allows the SQUID 237 sensor to be in contact with the sample and the sample-sensor distance to be in the or-238 der of just 1-2 µm. This allows for a spatial resolution in the order of  $\sim 1$  µm, hence this 239 SSM set-up can exploit the full native sensitivity of SQUID sensors at unsurpassed spa-240 tial resolution. Nevertheless, the sample is measured at a temperature of  $\sim 4$  K – far 241 below its Verwey transition. Therefore this set-up impedes determining magnetizations 242 of naturally occurring magnetic states in a sample at room temperature and is therefore 243 only of limited use for paleomagnetic and rock-magnetic applications of MMT. 244

In other SSM set-ups previously used for paleomagnetic or rock-magnetic appli-245 cations the SQUID sensor is thermally isolated from the sample (e.g.: Egli & Heller, 2000; 246 Fong et al., 2005; Weiss et al., 2007; Lima & Weiss, 2016; Oda et al., 2016). This can 247 only be attained by increasing the sample-sensor distance, in the most recent set-ups this 248 distance can be as little as 200 µm (Oda et al., 2016); hence the spatial resolution limit 249 of such set-ups is in the order of 200 µm. In spite of the major technical achievement to 250 thermally isolate the sample at room temperature from the SQUID sensor at  $\sim 4$  K over 251 just 200 µm, the spatial resolution does not allow for a reliable magnetic inversion for 252 individual grains in natural samples given the concentration of magnetic grains. There-253 fore also the thermally isolated SSM set-ups seem unsuitable for MMT, even consider-254 ing their unsurpassed magnetic sensitivity. 255

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# 2.2.2 Magnetic Tunnel Junction scanners

Advances in non-cryogenic scanning magnetometry sensors have led to the devel-257 opment of Magnetic Tunnel Junction (MTJ) sensors that are suitable for paleomagnetic 258 and rock-magnetic applications (Lima et al., 2014). MTJ sensors exploit a quantum phys-259 ical effect by which electrons can tunnel through an ultra-thin insulating layer that is 260 in between two ferromagnetic layers, creating a small current through the sensor. This 261 tunneling effect is governed by the magnetization in the two ferromagnetic layers of the 262 sensor. Therefore the tunneling current, and hence the resistance of the sensor, changes 263 due to variations in the external magnetic field. The major advantage of these MTJ sen-264 sors over typical SQUID sensors is that MTJ sensors operate at room temperature, this 265 makes the expensive and complex cryogenic systems for SSM set-ups superfluous. Nev-266 ertheless, typical MTJ sensors are > 4 orders of magnitude less sensitive compared to 267 SQUID sensors (Lima et al., 2014). This major setback in sensitivity is only partially 268 compensated by the smaller sample-sensor distances that are possible in MTJ set-ups 269 (down to  $\sim 7 \,\mu m$ ). This results in typical effective magnetic moment sensitivities in the 270 order of  $10^{-14}$  Am<sup>2</sup> for the most advanced MTJ set-ups (Lima et al., 2014). The spa-271 tial resolution of an MTJ set-up primarily depends on the actuators used to move the 272 sensor or sample, and is often in the order of  $5 - 10 \ \mu m$ . 273

The sensitivity of the surface magnetometry technique is not a major concern when 274 making scans of synthetic or volcanic material. For the proof-of-concept of MMT (de Groot 275 et al., 2018), the sensitivity of the SSM set-up had to be reduced in favor of dynamic range 276 to properly image the magnetization of the sample. This makes MTJ-based set-ups the-277 oretically very suitable for MMT analyses, primarily because of their small sample-sensor 278 distance and high spatial resolution. In this study we obtained a magnetic surface scan 279 of the same synthetic sample that was used in de Groot et al. (2018), on the MTJ set-280 up at the University of Cambridge. 281

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# 2.2.3 Quantum Diamond Microscope

Recently, an entirely new type of scanning magnetometry was optimized for geological samples: the Quantum Diamond Microscope (QDM) (Glenn et al., 2017; Farchi et al., 2017; Levine et al., 2019; Fu et al., 2020). The QDM uses optical fluorescence in nitrogen-vacancy (NV) centers in a diamond chip to determine the magnetic field above

a sample. The magnetic fields are thus derived from an optical image, hence its theo-287 retical spatial resolution limit is determined by the diffraction limit of the optics. The 288 wavelength of the fluorescence is 600-800 nm; the theoretical limit for the spatial reso-289 lution therefore is  $\sim 350$  nm, depending on the quality of the optical path (Levine et 290 al., 2019). In practice, however, current set-ups attain a spatial resolution of 1.2 µm (Glenn 291 et al., 2017). The sensitivity of the QDM depends on several variables, e.g. the time over 292 which the measurements are done, the thickness of the layer of NV centers in the dia-293 mond, and the characteristics of the optical components used. In general, the sensitiv-294 ity of the QDM may be expected to be better then the sensitivity of MTJ sensors, but 295 does not attain the sensitivity of SQUID sensors (Glenn et al., 2017). 296

An important property and possible draw-back of the QDM for MMT applications 297 is that it needs a bias field to operate (Glenn et al., 2017). During normal operation this 298 bias field is approximately 0.9 mT and its polarity is switched many times. This enables 299 discriminating between remanent (i.e. ferrimagnetic) and paramagnetic/viscous mag-300 netizations. The QDM produces two maps: one of the remanent magnetizations that in-301 herently misses the remanence carried by grains with a coercivity below the bias field; 302 and another with the induced magnetizations by the bias field. Since the iron-oxide grains 303 that carry information on the past state of the Earth's magnetic field generally have co-304 ercivities higher than the bias field currently used (0.9 mT), this property of the QDM 305 does not jeopardize the paleomagnetic interpretation of QDM results. But for some rock-306 magnetic applications such as magnetic viscosity studies, however, this bias field needs 307 to be considered. 308

Since the QDM is theoretically very suitable for MMT analyses, we obtained a magnetic surface scan of the same synthetic sample used for the MTJ analysis and for the proof-of-concept of MMT (de Groot et al., 2018) at the QDM set-up at Harvard University. Furthermore, we obtained a magnetic surface scan from a natural volcanic sample.

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#### 2.3 Co-registration

The two data-sets for MMT, the spatial information on the iron-oxide grains from the microCT analysis and the magnetic surface scan, must be co-registered in the same coordinate system for a reliable inversion. This co-registration consists of a 'mapping'

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of the magnetic surface scan in the x and y-coordinates of the microCT data, and de-318 termining the sample-sensor distance, or scan height, the z-coordinate. For the SSM and 319 MTJ data the locations of the iron-oxides closest to the surface as produced by the mi-320 croCT scan are manually aligned with the largest magnetic anomalies present in the mag-321 netic surface scan. Since the QDM is an optical acquisition technique, it is possible to 322 make an optical image of the surface of the sample in exactly the same coordinates as 323 the magnetic scan is made in. This greatly eases the tedious, manual process of map-324 ping the two data-sets. 325

The sample-sensor distance, or scan-height, is often even more difficult to determine. But, since magnetic moments decay with the third power of distance, it is of utmost importance to have a good estimate of this parameter. The SSM sensor in the proofof-concept was in contact with the sample, hence the sample-sensor distance can be estimated with precision. For the MTJ and QDM set-ups this distance is derived from the actuators that are used to move the sensor (MTJ), or the sample (QDM), and may be less precise, depending on the actuators used.

## 2.4 Inversion

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The combination of microCT data and magnetic surface scans enables to uniquely 334 reconstruct the magnetic moments of individual iron-oxide grains in a sample, provided 335 that they are spatially sufficiently separated. A grain is defined as a group of intercon-336 nected voxels in the microCT scan; each grain is considered to be uniformly magnetized. 337 For the inversion each grain is mathematically isolated inside a small sphere  $\Omega^i$ ,  $i = 1 \dots N$ . 338 These spheres cannot intersect, i.e. they are pairwise disjoint. This implies that when 339 grains are spatially not sufficiently separated, or when grains are intertwined, these grains 340 can only be placed inside a sphere together and their magnetic moment is solved for as 341 one. A number N spheres  $\Omega^i$  are now considered to be magnetic source regions inside 342 a larger sphere  $\Omega$ . In a slightly simplified version, the underlying theorem for the inver-343 sion (Fabian & de Groot, 2019) guarantees that the radial magnetic field component  $B_r^{\Omega}$ 344 on the sphere  $\Omega$  uniquely defines the radial field components  $B_r^i$ , i = 1...N, on the 345 surfaces of all of the N inner spheres  $\Omega^i$  (Fabian & de Groot, 2019). To apply this the-346 orem in practice, all magnetic sources in a sample have to be identified, and placed into 347 N pairwise separate spheres, such that each magnetic grain lies completely inside one 348 of these spheres, and no magnetic sources are outside them. It is then theoretically pos-349

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sible to identify the magnetic dipole moment of each of the N spheres from a precise measurement of  $B_r^{\Omega}$  on a spherical surface around all N spheres.

In practice, the magnetic scanning measurement is performed at finitely many positions on a sufficiently large rectangular planar region  $R \subset \Omega$  above the sample. This rectangle mathematically corresponds to a fraction of an infinitely large sphere, which is chosen large enough, such that the field component  $B_r^{\Omega}$  outside R is negligibly small. Conceptually, the inversion proceeds through the following steps:

- 1. Define the scan surface R and the centers and sizes of the N spheres  $c_i$ ,  $i = 1 \dots N$ that contain all sources. These spheres are determined by assuming that all magnetic sources are identified by density anomalies in the microCT data.
- 2. Measure  $B_r^{\Omega}$  on R with sufficient resolution and accuracy.
- 361 3. Use the unique continuous (Fabian & de Groot, 2019) inversion operator

$$B_r^\Omega \to B_r^i$$

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to calculate the radial component on the surface  $\Omega^i$  of the *i*-th sphere.

4. Decompose  $B_r^i$  in spherical harmonics to isolate its dipole moment  $m_i$ .

This conceptual procedure shows that in case of sufficient accuracy and resolution the dipole moments  $m_i$  are uniquely defined, and can be recovered with arbitrary precision. Because the recovery essentially involves a downward continuation of the radial field from the larger sphere  $B_r^{\Omega}$  to each smaller sphere  $B_r^i$ , it substantially amplifies noise and requires extremely precise and accurate data to succeed (e.g. Blakely, 1996).

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#### 2.4.1 Inversion routine

The practical inversion routine used here is described in de Groot et al. (2018). It 370 exploits the more detailed geometric information from the microCT to obtain a repre-371 sentation of the shapes of individual grains as a union of a small number of rectangu-372 lar boxes (i.e. cuboids). Each grain  $P_i$ , i = 1, ..., N, is described as a union of  $n_j$  cuboids 373  $C_{i,j}$  with  $j = 1, \ldots, n_j$ , each of which is homogeneously magnetized with magnetiza-374 tion  $M_i$ . For each scanning point  $r_k$ ,  $k = 1 \dots K$  the forward model equation calcu-375 lates the magnetic flux through the sensor on the surface of the sample generated by each 376 cuboid  $C_{i,j}$  as function of its magnetization vector  $\mathbf{M}_{\mathbf{i}} = (M_{i,1}, M_{i,2}, M_{i,3})$ . The sum 377

- provides the total flux  $F_k$  as a linear function of the 3 N parameters defining all vectors
- $\mathbf{M}_{i}$ . Thereby the forward model defines a  $K \times 3N$  design matrix **A** which transforms
- 380 the vector

$$\mathbf{v} = (M_{1,1}, M_{1,2}, M_{1,3}, M_{2,1}, M_{2,2}, M_{2,3}, \dots, M_{N,2}, M_{N,3})$$

<sup>381</sup> into the measured flux signals

$$\mathbf{F} = (F_1, F_2, F_3, \dots, F_K),$$

according to the forward equation

$$\mathbf{F} = \mathbf{A}\mathbf{v}.$$

The inversion is performed by calculating the Moore-Penrose pseudoinverse  $\mathbf{A}^+$  (Moore, 1920; Penrose, 1955) and applying this to the vector  $\mathbf{F}_{\text{MMT}}$  of the measured values of  $F_k$  via

$$\mathbf{v}_0 = \mathbf{A}^+ \mathbf{F}_{\mathrm{MMT}}$$

By definition of the pseudoinverse, for K > 3N this returns the vector  $\mathbf{v}_0$  of all magnetizations for the least-square fit of the measured values by assuming a homogeneous magnetization for each grain.

Due to the geometrical approach of this routine, it produces magnetizations of the 389 grains, i.e. volume normalized magnetic moments. In contrast to magnetic moments, these 390 magnetizations are prone to uncertainties arising from the microCT data processing, such 391 as resolution limits, thresholding and voxel binarizations. Multiplying the magnetiza-392 tions by the same volumes that were used in the inversion procedure yield the magnetic 393 moments of the grains that explain the observed magnetic anomalies in the magnetic sur-394 face scan best. These magnetic moments are insensitive to the uncertainties in the vol-395 ume estimates associated with the microCT data processing. 396

### 397 2.5 Residuals

The accuracy of the inversion can be assessed by calculating the residuals left by 398 the inversion. This is done by assigning all grains their calculated magnetic moment and 399 running a forward model to determine the resulting magnetic map on the surface of the 400 sample. This calculated magnetic surface map is then subtracted from the actual, mea-401 sured, magnetic surface scan. This produces a map of the residuals after the inversion, 402 i.e. a map of the measured magnetic flux on the surface that is not explained by the cal-403 culated magnetic moments of the grains. After an accurate inversion we expect low resid-404 uals; high magnetic anomalies in the residuals often arise from larger grains close to the 405 surface. Their magnetic expressions on the surface of the sample are generally more com-406 plex due to their complex magnetic domain states. Therefore these magnetic anomalies 407 cannot be explained by our assumption of dipolar magnetic moments in the grains. 408

## <sup>409</sup> 3 Obtaining magnetic directions from MMT

To obtain a magnetic direction from magnetizations of individual grains as produced by our inversion routine (section 2.4.1), we first determine the magnetic moments ( $\mathbf{m}$ , in Am<sup>2</sup>) of the individual grains by multiplying their calculated magnetizations ( $\mathbf{M}$ , in A/m) by their volume. We also change the mathematical indices 1, 2, 3 describing the axes of the coordinate system used in section 2.4 to the axes they physically represent: x, y, z; with the x-y-plane as the surface of the sample and z going down into the sample from its surface. The total magnetic moment of the grain is then given by:

$$m_{\rm grain} = \sqrt{m_x^2 + m_y^2 + m_z^2}$$

The magnetic direction is defined by a declination and inclination with respect to the coordinate system of the sample. The declination is defined as the angle with the positive x-axis of the sample in the x-y-plane; the inclination is defined as the smallest angle with the positive z-axis of the sample:

dec =  $\arctan(m_x/m_y)$  and  $\operatorname{inc} = \arcsin(m_z/m_{\text{grain}})$ 

-15-

					or dresso	
			area 1	area 2	area 3	area 4
		magnetic scan	scan			
scanning technique	MTJ	QDM	QDM	QDM	QDM	QDM
sensor geometry	$ellipse^{a}$	square	square	square	square	square
sensor surface $(\mu m^2)$	8.0	1.44	1.44	1.44	1.44	1.44
datapoints $(x, y)$	$91 \times 96$	$170{ imes}166^b$	$126{ imes}126$	$209 \times 230$	$167{ imes}138$	$184 \times 130$
scan height (µm)	33.56	0.9	6.0	6.0	6.0	6.0
step size (µm)	10.0	$6.0^b$	1.2	1.2	1.2	1.2
		spatial information	nation			
microCT resolution (µm)	0.714	0.714	0.675	0.675	0.675	0.675
microCT voxel size $(\mu m^3)$	0.36	0.36	0.31	0.31	0.31	0.31
scan dimensions (x, y, z; µm)	$910{ imes}960{ imes}50$	$1020 \times 996 \times 50$	$150\!\times\!150\!\times\!30$	$250 \times 275 \times 30$	$200\!\times\!165\!\times\!30$	$220 \times 155 \times 30$
number of grains	128	128	11	42	18	20
number of cuboids	19,552	19,552	305	1,192	388	555
grain concentration $(grains/mm^3)$	2,930	2,520	16,300	20,360	18,180	19,550

 $^b$  after subsampling the original QDM scan which has a step size of 1.2  $\mu m$ 

**Table 1.** Details of the MMT inversions

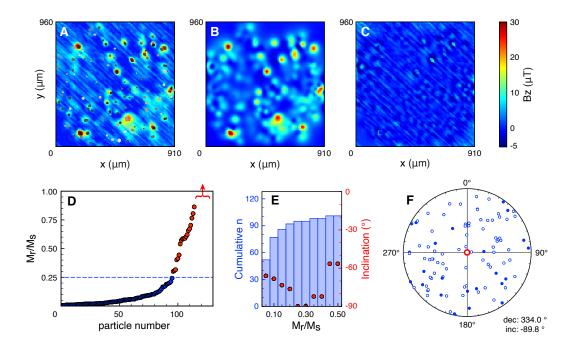


Figure 2. Results of MTJ experiments on the synthetic sample. The 128 grains in the sample are superimposed on the MTJ measurements (in gray-scale, A). The outcome of the forward calculations is in B, the map of the residuals is in C. The theoretical remanence ratios (Mr/Ms) of the individual magnetite grains (see main text) are sorted in increasing order (D). The graph is clipped at the theoretical maximum Mr/Ms ratio of 1; 14 grains with Mr/Ms ratios between 1.08 and 9.45 are not shown, indicated by the red arrow. For cumulative bins of Mr/Ms ratios the cumulative n is plotted together with the resulting inclination for the selected grains (E). For grains with Mr/Ms ratios <0.25 (blue dashed line in D), the resulting direction differs just  $0.2^{\circ}$  from the expected direction. For these grains the distribution of their individual directions is in F (open symbols pointing upwards, closed symbols downwards), with the resulting direction in red.

To calculate the bulk magnetization for the entire sample based on all grains or a sub-set of grains, first the  $m_x$ ,  $m_y$ , and  $m_z$  components of the selected grains are summed into  $\Sigma m_x$ ,  $\Sigma m_y$ , and  $\Sigma m_z$ . Then these parameters are used in the equations above.

424

#### 3.1 A magnetic direction from an MTJ scan

To obtain a magnetic direction using MMT we used the same synthetic sample as used in de Groot et al. (2018). This sample contains 128 magnetite grains with diameters ranging from 5 to 35 µm that are randomly distributed in space (Supplementary

movie 1). First, we gave it an Isothermal Remanent Magnetization (IRM) with a pulsed 428 magnetic field of 1 T perpendicular to the surface of the sample, to give the sample a 429 known magnetic state by suspending the sample in a Lakeshore Vibrating Sample Mag-430 netometer at the University of Cambridge and briefly switching on the field. The sam-431 ple was scanned in the MTJ set-up at the University of Cambridge directly after giving 432 the sample its IRM. The entire surface of the sample was scanned with a step size of 10 433  $\mu$ m, yielding 8736 data points, with a scan height of 33.56  $\mu$ m (Table 1). The scan shows 434 some scanning artifacts in the scan direction, identified as diagonal stripes (Fig. 2A). 435 The MTJ scan shows large positive magnetic anomalies, up to  $> 30 \ \mu$ T, and much smaller 436 negative anomalies, down to  $< -5 \ \mu\text{T}$ . This differs from the observations in de Groot 437 et al. (2018), where the positive and negative magnetic anomalies seem more symmet-438 rical distributed around  $0 \ \mu T$ . This can be explained by the much larger scan height used 439 in the MTJ scan: 33.56 µm vs 2 µm for the SSM set-up used in de Groot et al. (2018). 440 Since the scanner is further away from the magnetic sources, the magnetic expression 441 of the sources represent more their 'far-field' (i.e. dipolar) nature. Moreover, the MTJ 442 scan was made after giving the sample an IRM, while the magnetic states in de Groot 443 et al. (2018) represent a more natural magnetic state. Hence the grains were much stronger 444 and more uniformly magnetized during the MTJ scan. 445

The co-registration between the MTJ and microCT results was done manually by 446 aligning the locations of the grains closest to the surface to the strongest magnetic anoma-447 lies in the MTJ scan (Fig. 2A). The co-registration was accurate and allowed for a proper 448 inversion; magnetizations were obtained for all 128 grains in the synthetic sample (Sup-449 plemental Table 1). The results of the inversion were used as input for a forward model 450 (Fig. 2B) which yields a close representation of the magnetic surface scan (Fig. 2A). This 451 leads to generally very low residuals (Fig. 2C). The diagonal scanning artifacts in the 452 MTJ scan are the most prominent feature in the residuals, hence the inversion is insen-453 sitive to these, and they are not propagated into the calculated magnetizations per grain. 454

From this dataset alone it is difficult to label magnetizations of individual grains 'reliable' or 'unreliable'. In the future, this could be done by e.g. determining the magnetizations of individual grains after series of magnetic treatments. Nevertheless it is possible to provide a first-order assessment of the accuracy of the magnetizations produced here by considering the theoretical remanence ratios (Mr/Ms) of the individual grains. These can be estimated by dividing the remanent magnetization (Mr) of the individual

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grains as produced by the inversion, by their theoretical saturated magnetization (Ms) 461 (Fig. 2D). Since the grains in the synthetic sample are pure magnetite grains, their the-462 oretical saturation magnetization is  $480 \text{ kAm}^{-1}$  (Dunlop & Özdemir, 1997). It is impor-463 tant to note that we use the volume estimates of the grains as produced by the microCT 464 analysis to determine both the Mr and Ms values. The uncertainties associated with the 465 manual tresholding and voxel binarizations during microCT data interpretation there-466 fore propagate into the calculated magnetizations. Nevertheless, the volumes for all grains 467 were obtained in a single workflow using one threshold. Since our analysis based on the 468 Mr/Ms ratios is comparative in nature the absolute uncertainties in volume estimates 469 are somewhat suppressed in our analysis. Moreover, the resulting magnetic directions 470 for subsets of grains in the sample are based on the individual magnetic moments of grains 471 that are insensitive to the uncertainties in the volume estimates. 472

Most grains have low Mr/Ms ratios, as expected since the grains in the synthetic 473 sample have diameters ranging from  $5-35 \mu m$ . Some grains, however, have Mr/Ms ra-474 tios that are much larger than expected, i.e. well above 0.5, and some Mr/Ms ratios are 475 even higher than the theoretical limit of 1. For these grains it is most likely that the in-476 version did not produce accurate estimates of the magnetization, and they should be ex-477 cluded from calculating the magnetic direction for the entire sample. Besides this the-478 oretical maximum, there is no theoretical value for the cut-off for the Mr/Ms ratios to 479 select the grains that should be included in calculating the magnetic direction. We there-480 fore took an iterative approach to select the grains based on their Mr/Ms ratios that yield 481 a resulting magnetic direction closest to the applied magnetic field. Furthermore the re-482 sulting direction should be insensitive to the addition of small numbers of grains to the 483 ensemble - i.e. adding one or two grains should not have a major effect on the result-484 ing direction. Since we know that the expected paleodirection is perpendicular to the 485 surface we expect an inclination of  $-90^{\circ}$ , with any value for the declination. We calcu-486 lated the magnetic direction for grains based on their Mr/Ms ratio, starting with grains 487 with Mr/Ms ratios  $\leq 0.05$ . We then added grains based on their Mr/Ms ratio in bins 488 of 0.05, until the Mr/Ms ratio reached 0.5. This results in pairs of number of grains in-489 cluded (n) and the resulting inclination (Fig. 2E). For the grains with Mr/Ms ratios  $\leq$ 490 0.25, the resulting inclination is  $-89.8^{\circ}$ , with a declination of  $334.0^{\circ}$ . This is just  $0.2^{\circ}$ 491 off of the expected direction (Fig. 2F). For the next bin, with Mr/Ms ratios  $\leq 0.35$  (the 492 bin between 0.25 and 0.30 has no additional grains), three additional grains are included 493

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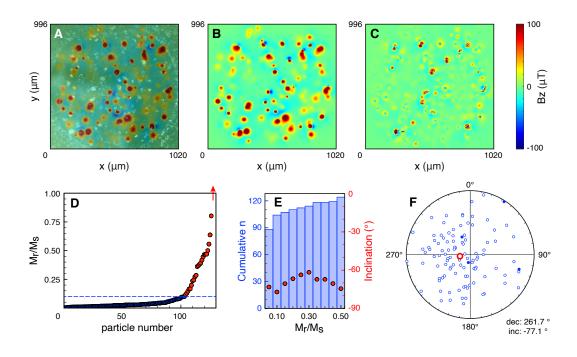


Figure 3. Results of QDM experiments on the synthetic sample. The optical microscopy image is in the background in gray-scale (A), the map of the magnetic flux density perpendicular to the surface (in color) is super-positioned with 50% transparency. The outcome of the forward calculations is in B, the map of the residuals is in C. The theoretical Mr/Ms ratios of the individual magnetite grains (see main text) are sorted in increasing order (D). The graph is clipped at the theoretical maximum Mr/Ms ratio of 1; one grain with a Mr/Ms ratio of 2.42 is not shown, as indicated by the red arrow. For cumulative bins of Mr/Ms ratios the cumulative n is plotted together with the resulting inclination for the selected grains (E). For grains with Mr/Ms ratios <0.10 (blue dashed line in D), the resulting direction is closest to the expected direction. For these grains the distribution of their individual directions is in F (open symbols pointing upwards, closed symbols downwards), with the resulting direction in red.

in calculating the magnetic direction. These three grains have a large influence on the

- resulting inclination, making the resulting direction very sensitive to individual grains
- and therefore unstable (Fig. 2E). Moreover, Mr/Ms ratios up to 0.25 are plausible for
- grains with diameters ranging from 5–35 µm (e.g.: de Groot, Dekkers, et al., 2014; Mon-
- <sup>498</sup> ster et al., 2018).

499

# 3.2 A magnetic direction from a QDM scan

To test the performance of MMT using different magnetic surface scanning tech-500 niques we repeated the experiment with the MTJ using the QDM at Harvard Univer-501 sity (Table 1). We used the same synthetic sample again, and gave it a 1 T IRM field 502 perpendicular to its surface using an ASC Impulse Magnetizer (IM-10-30) at Massachusetts 503 Institute of Technology. The magnetic surface scans were made the same day. Since the 504 QDM also produces an optical image of the sample in the same coordinate system as the 505 magnetic scan, the mapping between the QDM scan and the spatial data from the mi-506 croCT scan was relatively easy (Fig. 3A). The sample-sensor distance in the QDM is much 507 smaller compared to the MTJ scan, the magnetic anomalies are therefore larger ( $\sim 100$ 508  $\mu T$  for the QDM, compared to ~ 30  $\mu T$  for the MTJ). The inversion yielded magneti-509 zations for all 128 grains in the sample (Supplemental Table 2). These magnetizations 510 were used to make a forward calculation of the surface magnetization (Fig. 3B), and a 511 map of the residuals left by the inversion (Fig. 3C). The residuals are low, although there 512 are prominent and complex anomalies over some grains, usually grains closer to the sur-513 face. These observations are explained by the smaller sample-sensor distance of the QDM 514 compared to the MTJ: complex, non-dipolar, structures are only observed in close prox-515 imity of the grains. To interpret the resulting magnetic direction for the entire sample 516 we followed the same workflow as for the MTJ scan. First, the Mr/Ms ratios were cal-517 culated for the individual grains using their theoretical Ms of  $480 \text{ kAm}^{-1}$ . More than 518 100 grains have an Mr/Ms ratio <0.10. Since we used the same grain volumes for the 519 MTJ and QDM data analyses, this implies that the magnetizations of the grains (and 520 hence their Mr/Ms ratios) from the QDM scan are generally somewhat lower than those 521 from the MTJ scan (Fig. 3D). Again, we use bins of 0.05 for the Mr/Ms ratios and cal-522 culate the resulting inclination (Fig. 3E). For the set of grains with Mr/Ms ratios be-523 tween 0 and 0.10 the inclination is  $-77.1^{\circ}$ , this is closest to the expected inclination of 524  $-90^{\circ}$  for any of the Mr/Ms ratio bins up to 0.5, but still  $-12.9^{\circ}$  off. The declination 525 for this resulting direction is 261.7 °. Furthermore, the number of grains with a direc-526 tion in the upper hemisphere (i.e. with a direction more than  $90^{\circ}$  off of the applied mag-527 netic field) is 24 for the MTJ experiment and only 4 for the QDM experiment (compare 528 Figs. 2F and 3F). This implies that the distribution of the directions of the individual 529 grains seems narrower for the results using the MTJ scanner compared to the QDM re-530 sults. 531

It is currently difficult to explain the differences between the MTJ and QDM stud-532 ies using the same sample and magnetic treatment in more detail. These differences may 533 have experimental reasons, e.g. the smaller sample-sensor distance in the QDM leads to 534 detecting more complex magnetic signals and our assumption to solve for dipolar mag-535 netizations may be violated. Furthermore, the IRM imparting field was applied directly 536 preceding the MTJ scan at the University of Cambridge; while for the QDM experiment 537 the sample had to be transported from Massachusetts Institute of Technology to Har-538 vard. Although the sample was measured on the QDM within hours after applying the 539 IRM, the additional time and handling of the sample before the QDM scan might have 540 given potential viscous processes more time to evolve. There can also be a rock-magnetic 541 reason for the observed differences: the coercivities of some grains may be (partially) very 542 low, so their signal would be (partially) canceled by the switching bias field applied in 543 the QDM (0.9 mT), leading to lower total magnetizations in the QDM experiment. Nev-544 ertheless, it is encouraging to see that the resulting magnetic directions from both the 545 MTJ and QDM experiments are close to the expected direction, and that it is possible 546 to select and consider the contributions of individual grains in a sample. 547

## 4 Rock-magnetic information from a volcanic sample

The concentration of magnetic grains in the synthetic sample is about one order 549 of magnitude lower than the concentration or magnetic grains in naturally occurring lavas 550 (Table 1). To test whether MMT is also capable of determining magnetizations of in-551 dividual grains in a natural sample we subjected a Hawaiian lava to an MMT study. We 552 drilled a small core with a diameter of 3 mm from a standard thin section with a sam-553 ple thickness of 30 µm from the 1907 flow of the Kilauea (site HW03 from de Groot et 554 al. (2018)). Our sample was taken from the same paleomagnetic drill core as the sam-555 ple used in ter Maat et al. (2018) where the chemical, physical, and magnetic states of 556 several individual iron-oxide grains were thoroughly assessed with e.g. Scanning Elec-557 tron Microscopy, Electron Back-Scatter Diffraction, Magnetic Force Microscopy, and Micro-558 probe analyses. The sample was polished using a colloid silica suspension prior to the 559 magnetic scans to remove surface magnetizations due to mechanical polishing (see Sup-560 plementary Fig. 9 in de Groot, Fabian, et al. (2014)). The magnetic surface scan was 561 made with the QDM at Harvard University. We did not apply any magnetic treatment 562 to the sample beforehand; the magnetizations of the grains therefore most likely resem-563

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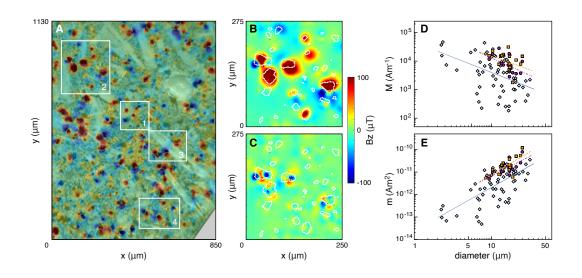


Figure 4. Results of QDM experiments on a volcanic sample (HW03, see main text). The optical microscopy image is in the background in gray-scale (A), the map of the magnetic flux density perpendicular to the surface (in color) is super-positioned with 50% transparency. The QDM data of area 2 (A) is in B, with the outlines of the iron-oxide grains as identified by microCT in white. The residual after the inversion to produce the individual magnetic moments per grain (C) are generally low and non-uniform, indicating a proper inversion result. The magnetizations (D) and magnetic moments (E) of grains with Mr/Ms ratios  $\leq 0.10$  (see main text) are plotted as function of their diameter as blue diamonds, with their linear trend line in blue. The results of de Groot et al. (2018) are also included for comparison: the magnetizations after applying an Anhysteretic Remanent Magnetization (ARM) with a bias field of 40 µT in orange squares / dashed trend line.

<sup>564</sup> ble a natural magnetic state. The iron-oxide grains in the sample were obtained from <sup>565</sup> a microCT scan done at the Nanotom-S at TU Delft. The spatial resolution in this scan <sup>566</sup> is  $\sim 0.7 \mu m$ .

We used the optical image of the QDM to map the magnetic surface scan on the spatial data of the iron-oxide grains obtained by the microCT scan. To reduce computation time the inversions were done for four small areas of the sample (Fig. 4A). We obtained magnetizations for all 91 grains inside the four areas. The residuals left by the inversion are low compared to the residuals reported for the synthetic sample (Fig. 4C), and are again dominated by complex magnetizations arising from grains close to the surface of the sample.

To assess the reliability of the inversion results we again calculated the theoreti-574 cal Mr/Ms ratio for each grain, using the Ms of pure magnetite. The naturally occur-575 ring grains in Hawaiian lavas are generally rich in Ti; Curie balance experiments on sis-576 ter samples from site HW03 exhibit a gradual decay of the magnetization with temper-577 ature, with Curie temperatures around 250 and  $450^{\circ}$ C that are not very well expressed 578 (de Groot et al., 2013; ter Maat et al., 2018). Replacing Fe by Ti in the iron-oxide solid 579 solutions lowers the Ms values (Readman & O'Reilly, 1972; Dunlop & Özdemir, 1997). 580 It is therefore safe to assume that the Ms of pure magnetite is overestimating the real 581 Ms value for most of the grains in the sample, leading to artificially low Mr/Ms ratios 582 for our volcanic sample. 583

From the 91 grains in the inversions, 16 grains have Mr/Ms ratios higher than the 584 theoretical maximum of 1. These grains were thus not properly resolved by the inver-585 sion and were rejected. Building on the experience with the QDM results for the syn-586 thetic sample and given that the Ms value for magnetite is overestimating the true Ms 587 values for our grains, we deem the grains with Mr/Ms ratios >0.10 suspect. These grains 588 are not considered further in our analyses. This leaves 62 grains for which the magne-589 tizations are now known. These magnetizations are plotted against the diameters of the 590 grains that are obtained from the microCT analysis (Fig. 4D). Since the volume of the 591 grains is known, their magnetic moments can be calculated and plotted as function of 592 their diameter as well (Fig. 4E). 593

The natural sample was not magnetically treated prior to the QDM measurements, the magnetizations are therefore most likely resembling a natural magnetic state. In de

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Groot et al. (2018) the pure magnetite grains in the synthetic sample were also either 596 untreated prior to the SSM measurements (in purple in Fig. 4D and E), or analyzed af-597 ter applying an Anhysteretic Remanent Magnetization (ARM) with a bias field of  $40 \ \mu T$ 598 to the sample (in orange in Fig. 4D and E). The magnetic states in de Groot et al. (2018) 599 therefore also resemble a natural magnetic state and can be meaningfully compared to 600 the magnetic states of our natural sample. The magnetizations of the grains in the nat-601 ural sample are on average lower than the magnetizations for the synthetic sample. This 602 is explained by the grains being enriched in Ti in the natural sample, lowering their mag-603 netizations. The trends in magnetization and magnetic moment as function of diame-604 ter, however, are remarkably similar for the natural sample compared to the trends re-605 solved for the pure magnetite grains in de Groot et al. (2018). 606

#### 5 Discussion

Building on the proof-of-concept of MMT (de Groot et al., 2018), we showed that it is possible to obtain a magnetic direction from a subset of grains in a synthetic sample, and derive magnetic information from individual grains in natural volcanic sample. Here we will first discuss the technical characteristics and limitations of MMT, and then its potential for both paleomagnetism and rock-magnetism.

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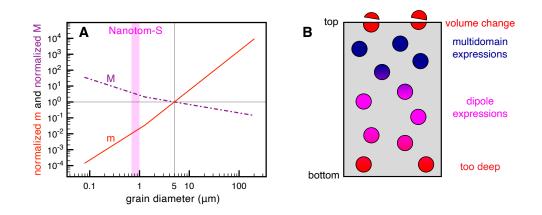
# 5.1 Spatial characterization of the grains

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#### 5.1.1 Detecting all iron-oxides

The spatial characteristics of all iron-oxide grains in the sample are determined from 615 a microCT scan. For a reliable inversion it is important that all magnetic sources are 616 properly identified, otherwise not all magnetic surface anomalies can be attributed to 617 their source. Being able to detect all potentially magnetic iron-oxides depends on select-618 ing the proper threshold in the microCT scan above which grains are deemed iron-oxides, 619 and the resolution of the microCT scan. Since the iron-oxides have a distinct density con-620 trast to most other minerals present in volcanic samples, and also to artificial matrices 621 such as epoxy, the attenuation spectrum from the microCT scan is often bi- or multi-622 modal. Selecting the low between two modes is often straight-forward, but the thresh-623 old should be chosen conservatively such that all iron-oxides in the sample are selected. 624 As de Groot et al. (2018) already noted, selecting the proper attenuation threshold para-625

-25-



**Figure 5.** The spatial characterization of magnetic sources in a sample. The magnetization (M, in purple) and magnetic moment (m, in red) of spherical grains arising from a thermoremanent magnetic state vary as function of their diameter (A). The data are normalized to the values for a 5 µm grain. The detection limit of the Nanotom-S microCT is in pink. Figure adapted from Fig. 7.10 in Tauxe (2010), based on data presented in Dunlop and Özdemir (1997). How well MMT can determine the magnetization of the grains (represented by the circles) depends on their depths in the sample (B). The grains at the surface are cut during sample preparation and therefore loose their natural magnetization (top grains, in red); the magnetic expression of shallow grains may represent a complex 'multidomain' magnetic configuration (in blue); the magnetic expression of somewhat deeper grains represent their far-field, dipolar, magnetic moment (in pink); and the magnetic anomalies arising from grains that are too deep in the sample (in red) may be too weak to be properly inverted into the magnetization of the grain.

doxically was easier for the volcanic sample with less distinct density differences between the grains, than for our synthetic sample with large differences in density between the matrix and the magnetite grains. The smaller differences in density most probably suppress adverse beam hardening effects and therefore boundaries between grains are better defined in the scans.

The resolution of the microCT used here and in de Groot et al. (2018), the Nanotom-631 S at TU Delft, is  $\sim 0.7 \,\mu\text{m}$ , so it inherently misses grains that are below  $\sim 1 \,\mu\text{m}$  (Fig. 632 5A). The grains in the synthetic sample that we used were sieved to be larger than 3  $\mu$ m, 633 but in natural samples many grains with sizes between the superparamagnetic thresh-634 old of 30-50 nm (Dunlop & Özdemir, 1997) and the resolution limit of the Nanotom-S 635 may be present. Such smaller grains, however, have not been observed on a large scale 636 in the Scanning Electron Microscopy, Microprobe, and Magnetic Force Microscopy ex-637 periments on sister specimens of our HW03 sample (ter Maat et al., 2018), while these 638 techniques do have the necessary resolution to detect much smaller grains than the mi-639 croCT used in this study. Furthermore, it is important to keep in mind that relatively 640 small grains that may be missed by the microCT analysis have relatively little contri-641 bution to the total magnetic signal of volcanic samples. Although the TRM of a grain 642 with a diameter of 100 nm is 28 times higher than the TRM of a grain with a diame-643 ter of 5  $\mu$ m (Fig. 5A); when the volumes of these grains are taken into account and their 644 magnetic moments (m) are considered, the magnetic moment of the 5 µm grain becomes 645  $4.5 \times 10^3$  times larger than the magnetic moment of the 100 nm grain. This implies that 646  $4.5 \times 10^3$  grains of 100 nm have to be uniformly magnetized to produce the same mag-647 netic moment as one grain with a diameter of 5  $\mu$ m. In a natural sample where grains 648 are not uniformly magnetized, however, it is more likely that  $10^5$  to  $10^6$  100 nm grains 649 are necessary to produce the same net moment as one 5 µm grain. This illustrates that 650 the larger grains can very well be dominant in the overall magnetic signal of a sample. 651

Current advancements in microCT scanners allow for resolutions down to ~ 100 nm, this is very close to the superparamagnetic threshold of 30-50 nm for magnetite grains (Dunlop & Özdemir, 1997). This implies that it is already technically possible to detect iron-oxides down to volumes where their contributions to the total magnetization of the sample becomes de facto negligible compared to the contributions of larger grains. Hence it is already possible to detect all (relevant) iron-oxides in natural samples, although the field of view of scans with such high resolution is often relatively narrow and many scans

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should be combined to characterize the necessary amount of iron-oxide grains for pale-

660 omagnetic interpretations.

661

#### 5.1.2 Variation in iron-oxides

Not all iron-oxide grains do have remanent magnetizations at room temperature. 662 The Ti-rich end-members of the titanomagnetite and titanohematite solid solutions (ülvospinel 663 and ilmenite, respectively), for example, have Curie temperatures  $< -100^{\circ}$ C (Readman 664 & O'Reilly, 1972). To make it even more complex, Scanning Electron Microscope (SEM) 665 studies show that large iron-oxide grains in natural lavas often exhibit several regions 666 of different composition or show exsolution lamellae (e.g.: de Groot, Dekkers, et al., 2014; 667 Greve et al., 2017; Monster et al., 2018). This is certainly the case for our volcanic sam-668 ple, HW03 (de Groot et al., 2013), as illustrated with a sister specimen taken from the 669 same paleomagnetic drill core that was used to prepare the sample in this study from 670 by ter Maat et al. (2018). In this study it was confirmed that zones that are identified 671 as ilmenite by Scanning Electron Microscope, Electron Back-Scatter Diffraction, and Mi-672 croprobe analyses are indeed non-magnetic at room temperature by Magnetic Force Mi-673 croscopy. Currently it is impossible to spatially discriminate between magnetic and non-674 magnetic zones inside grains with the microCT techniques we used. Therefore many of 675 the grains in our natural sample will have non-magnetic zones; i.e. their 'magnetic grain 676 size' is often smaller then the physical grain size detected by microCT analysis. This im-677 plies that the volumes used to estimate the magnetizations of individual grains are of-678 ten larger than the regions that actually carry a magnetization in the iron-oxide grains, 679 leading to estimates of the magnetizations that are too low. This effect, however, does 680 not impact the magnetic moments of the grains, since they are insensitive to their vol-681 umes. 682

The grains in both our synthetic and volcanic sample are mostly spherical in shape. 683 From SEM studies it is known that in many lava samples that produce accurate pale-684 ointensities dendritic iron-oxide grains are the dominant magnetic carrier (e.g.: Cromwell 685 et al., 2015; ter Maat et al., 2018). It is postulated that individual branches of dendritic 686 grains act as small, individual, magnetic grains, with a favorable magnetic behavior com-687 pared to larger spherical grains. Because of resolution limits and noise effects such as 688 beam hardening these dendritic grains are more difficult to characterize by microCT anal-689 yses. Moreover, it is currently unclear how the magnetic behavior of dendritic grains should 690

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<sup>691</sup> be modeled in an MMT inversion. Dendritic grains therefore currently pose a challenge <sup>692</sup> to be properly resolved in MMT studies.

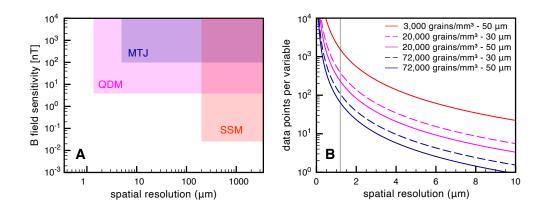
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#### 5.1.3 Spatial limitations as function of depth

The MMT technique determines magnetizations of all grains in the sample from 694 a magnetic surface scan of such a sample. The expression of a grain's magnetization on 695 the sample's surface decays as function of depth in the sample to the power of three. This 696 implies that the depth of a grain dictates how well MMT can resolve its magnetization 697 (Fig. 5B). Grains on the surface of a sample are cut during sample processing and pol-698 ishing. Therefore their volume changed and their natural magnetization is lost. For grains 699 close to the surface but not physically altered during sample processing we often observe 700 complex magnetic anomalies on the surface of the sample (e.g. Fig. 3C). We explain these 701 as expressions of multidomain configurations in the grains. These complex anomalies in 702 the magnetic surface scan violate our assumption to assign a dipolar magnetization to 703 each individual grain, hence they are often left in the residuals after the inversion. It is 704 debatable how well the dipole estimate actually represents the magnetization of grains 705 in this zone of 'multidomain expressions' (Fig. 5B). For deeper grains the magnetic ex-706 pression on the surface represent more a 'far-field' magnetization - i.e. a dipolar mag-707 netic configuration. For this zone of 'dipole expressions' MMT is able to reliably deter-708 mine the dipole moment of individual grains. For even deeper grains the magnetic ex-709 pression on the surface of the sample becomes so weak that it becomes impossible to re-710 liably invert for their magnetizations. 711

The specific depths of the different zones depend mostly on the sample-sensor dis-712 tance and the noise-level/sensitivity of the magnetic scan used. This is best illustrated 713 by comparing our MTJ experiment (with a scan height of  $33.56 \mu$ m) to the QDM study 714 (with a scan height of  $6 \mu m$ ) on the same synthetic sample. In the MTJ experiment there 715 are hardly complex magnetic anomalies left in the residuals (Fig. 2C), while they are ev-716 ident in the residuals of the QDM scan (Fig. 3C). The larger scan height of the MTJ 717 leads to detecting more of a far-field magnetic expression of the magnetization of the shal-718 lower grains, and therefore a better approximation of their dipole fields. The zone of 'mul-719 tidomain expressions' (Fig. 5B) is thus much smaller (if not absent) in the MTJ exper-720 iment. The inversion of the MTJ experiment, however, assigns more unrealistically large 721 magnetizations to mostly deeper grains in the sample (compare Fig. 2D and Fig. 3D). 722

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**Figure 6.** The resolution of the magnetic surface scan. Three potential scanning magnetometry techniques for MMT have different specifications for spatial resolution and B field sensitivity (A) (with data from: Lima et al., 2014; Glenn et al., 2017; Oda et al., 2016; Fu et al., 2020). The theoretically available number of data points per variable that is to be solved by the MMT inversion is governed by the concentration of grains in the sample, the thickness of the sample and the spatial resolution (i.e. step size) of the magnetic scan (B). The theoretically available number of data points per variable sample (3,000 grains/mm<sup>3</sup> - 50 µm), and different grain concentrations and sample thicknesses for volcanic samples. The typical spatial resolution of the QDM (1.2 µm) is indicated by the gray line.

723	These are explained by the large scan height of the MTJ: the total source-sensor distance
724	can be $>80~\mu\mathrm{m}.$ This implies that the anomalies arising from deeper grains as measured
725	by the MTJ sensor are very weak. This makes it difficult for the inversion to reliably de-
726	termine their dipole magnetization; a weak magnetic anomaly often 'disappears' in the
727	noise level of the magnetic scan - generally leading to overestimates of the dipole mag-
728	netizations of these deeper grains. The zone of 'dipolar expressions' allowing for success-
729	ful dipole inversions in the MTJ data is thus closer to the surface than for the QDM scan.

730

# 5.2 Scanning magnetometry

We demonstrated that the MMT technique can be used with different magnetic surface scanning techniques. The potential of each of these techniques for MMT is governed by their spatial resolution and sensitivity (Fig. 6A). The necessary spatial resolution of the magnetic scan is dictated by the concentration of magnetic grains in the sample and the sample thickness (Fig. 6B). Considering that grains are randomly distributed in a

sample and grains can be in very close proximity to each other, and may also be located 736 above and below each other, not all grains are very well separable in a magnetic surface 737 scan. A higher concentration of grains in a sample obviously leads to more magnetically 738 obscured grains. The MMT inversion performs best if the system is vastly over-determined 739 - i.e. when there are many data points in the magnetic surface scan per variable to solve. 740 To provide a dipole magnetization for a grain the three orthogonal axes of the magne-741 tization have to be solved for; the amount of variables in the system is therefore three 742 times the amount of grains present in the sample. 743

There are 128 individual magnetic grains in our synthetic sample; this implies a 744 concentration of  $\sim 3,000$  grains/mm<sup>3</sup>. The concentration in the natural volcanic sam-745 ple is highly variable throughout the sample. For the four regions that we analyzed the 746 concentration is  $\sim 20,000 \text{ grains/mm}^3$  (Table 1). When the entire microCT scan of the 747 sample is considered, the average concentration is much higher:  $\sim 72,000$  grains/mm<sup>3</sup> 748 (de Groot et al., 2018). Given the thickness of the samples (Table 1) we can calculate 749 the theoretical amount of data points in a magnetic surface scan per variable to solve 750 as function of the resolution of the magnetic scan (Fig. 6B). The spatial resolution of 751 the MTJ scan was 10 µm, which was sufficient to determine individual magnetizations 752 for grains in the synthetic sample (the red line in Fig. 6B). For volcanic samples, how-753 ever, the amount of data points per variable quickly drops to < 10 for a spatial reso-754 lution of 10 µm, even for a sample that is 'only' 30 µm thick. The MMT inversion strug-755 gles to determine the magnetizations of individual grains in this case, certainly if grains 756 are physically not well separated in the sample. The spatial resolution that can be at-757 tained with the QDM set-up, 1.2  $\mu$ m (Glenn et al., 2017), yields > 70 data points per 758 variable, also for the volcanic sample configurations (Fig. 6B). This provides the nec-759 essary amount of data points for a well-posed MMT inversion. To summarize, while the 760 MTJ technique is well-suited for MMT inversions for samples with relatively low con-761 centrations of magnetic grains, the QDM set-up currently is the best magnetic scanning 762 technique for MMT analyses on natural volcanic samples. 763

764

### 5.3 The rock-magnetic potential of MMT

The study of rock-magnetic processes governing the acquisition and storage of complex magnetizations in Earth materials has kept track with the pace of technological advances in magnetic scanning techniques. In the 1980s and 1990s the resolution and sen-

sitivity of scanning magnetometry only allowed for characterizing magnetic domain con-768 figurations inside large magnetic grains. This was done by making Bitter patterns (e.g. 769 Halgedahl, 1987, 1991), using the magneto-optical Kerr effect (e.g. Ambatiello & Sof-770 fel, 1996; Ambatiello et al., 1999), or with Magnetic Force Microscopy (e.g. Williams et 771 al., 1992; Pokhil & Moskowitz, 1996, 1997; Foss et al., 1998; de Groot, Fabian, et al., 2014). 772 These studies yielded valuable insights in the way large iron-oxides get and stay mag-773 netized. Simultaneously, theoretical studies modeled the magnetic behavior of large iron-774 oxide grains by taking a more fundamental approach to rock-magnetism (e.g. Moon & 775 Merrill, 1984, 1985; Song Xu & Merrill, 1989, 1990). More recent technological advances 776 took magnetic imaging down to atomic scales. Both Electron Holography (e.g. Harri-777 son et al., 2002; Feinberg et al., 2006; Almeida et al., 2014; Almeida, Muxworthy, Kovács, 778 Williams, Nagy, et al., 2016; Almeida, Muxworthy, Kovács, Williams, Brown, & Dunin-779 Borkowski, 2016) and X-ray Photoemission Electron Microscopy (e.g. Bryson et al., 2014; 780 Nichols et al., 2016) allow for a magnetic characterization at nm-scale and yielded in-781 dispensable information on the internal magnetic behavior of naturally occurring min-782 erals. The development of MERRILL, an open source software package for three-dimensional 783 micromagnetics (Conbhuí et al., 2018), enabled computationally assessing the magnetic 784 behavior of relatively small ( $< 1 \mu m$ ) grains. 785

Despite the aforementioned progress the interpretations of magnetic surface scans 786 was still often two-dimensional; relied on an upward continuation (Blakely, 1996; Lima 787 & Weiss, 2009; Lima et al., 2014; Lima & Weiss, 2016; Fu et al., 2020); or needed other 788 additional assumptions. By adding a spatial characterization of the magnetic sources in 789 the sample, the MMT technique overcame this classical inversion problem (Kellogg, 1929) 790 and now allows for characterizing the three-dimensional magnetic moment of individ-791 ual grains inside a sample. It is important to emphasize that the magnetic surface scan-792 ning techniques used in this study are non-destructive. MMT experiments can thus be 793 repeated after laboratory treatments on the sample. This opens up entirely new venues 794 for rock-magnetic research: now the magnetic state of individual grains can be assessed 795 as function of magnetic treatment, size, shape, and possibly chemistry. This will lead 796 to valuable insights in which grains are capable of recording the Earth's magnetic field 797 and retaining that information over geologic time, and which grains should be avoided. 798

<sup>799</sup> Building on a recent proof of uniqueness for microCT assisted potential field in-<sup>800</sup> versions using spherical harmonics (Fabian & de Groot, 2019), it was shown that MMT

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also allows to invert for higher order descriptions of the magnetic state of individual grains 801 in a sample (Cortés-Ortuño et al., 2021). Beyond the dipolar magnetic moments, the quadrupole 802 and octupole descriptions provide insight in the complexity of the magnetic stray fields 803 of individual grains in a sample. While the non-uniqueness of the classical potential in-804 version problem (Kellogg, 1929) once again implies that it is impossible to directly in-805 vert for the internal domain structure of individual grains without further a priori con-806 straints, the higher-order descriptions of their stray field can help to assess the complex-807 ity of the internal magnetic structure of individual grains (Cortés-Ortuño et al., 2021). 808 This may eventually bridge the gap between magnetic imaging techniques and compu-809 tational micromagnetic models, and enable the development of a comprehensive, fun-810 damental theory for the processes governing the acquisition and preservation of magnetic 811 signals in multi-domain grains in the future. 812

813

# 5.4 The paleomagnetic potential of MMT

When we are able to identify which grains are good paleomagnetic recorders, and 814 which are the bad ones, it becomes possible to use MMT to its full potential and obtain 815 paleomagnetic information from only the most reliable recorders in a sample. The ac-816 quisition of magnetizations in iron-oxides is a statistical process. For small, single-domain 817 grains the moments of  $10^6$  to  $10^8$  grains must be considered before the direction and in-818 tensity of the resulting magnetic moment represent the direction and intensity of the am-819 bient magnetic field at the time of cooling (Berndt et al., 2016). When measuring bulk 820 samples this happens implicitly, standard size paleomagnetic samples contain in the or-821 der of  $10^8$  to  $10^9$  magnetic grains, and the bulk signal is a statistical ensemble of the mag-822 netizations of all these grains together. 823

Berndt et al. (2016) used Néel's theory on thermoremanent magnetizations in single-824 domain ferromagnetic minerals (Néel, 1949, 1955) for their estimations. Single domain 825 grains cannot optimize their internal domain structure, as larger multi-domain grains 826 can. During acquisition of their magnetization multi-domain grains statistically end up 827 in a local energy minimum, with an associated domain configuration. But these grains 828 have many possible local energy minima and domain configurations. Depending on the 829 nature and strength of the imparting field the local energy minimum more or less rep-830 resents the imparting magnetic field. In our experiments to determine a magnetic direc-831 tion from subsets of grains in our synthetic sample, we strongly magnetized our sample 832

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by giving it an IRM at 1 T. We showed that it is possible to obtain an average direction that is only 0.2° to 12.9° off of the direction of the applied field (Figs. 2F and 3F), after selecting grains with low remanence ratios from 128 grains in the sample. The IRM acquisition is generally reported to be 100 times more efficient than TRM acquisition (e.g. Fuller et al., 1988). This could imply that for TRMs in multi-domain grains 10<sup>4</sup> to 10<sup>5</sup> grains may already provide meaningful paleomagnetic information derived from subsets of individual grains in a sample, although this is currently highly speculative.

To assess whether it is both empirically and computationally possible to use MMT 840 to determine naturally occurring paleodirections and paleointensities we assume that we 841 need to sum the magnetic moments of  $10^5$  grains from a sample. With a concentration 842 of 72,000 grains/mm<sup>3</sup> in a volcanic sample (de Groot et al., 2018) and a sample thick-843 ness of 50  $\mu$ m, there are 3,600 grains per mm<sup>2</sup> of such a sample. This implies that 28 844 mm<sup>2</sup> of sample would be sufficient. This is challenging, but not impossible for our cur-845 rent magnetic scanning and microCT analyses. The current inversion routine, however, 846 is not optimized for computational efficiency, yet. Hence, we are currently limited to in-847 vert only small parts of a sample (e.g. Fig. 4), with low numbers of grains (<100). More-848 over, the inversions are performed on a modest quad-core desktop computer. By opti-849 mizing the code for a multi-core machine and using a computational cluster it is possi-850 ble to gain one to two orders of magnitude in speed. The computational demands can 851 be further decreased by using the full potential of the recent proof of uniqueness for mi-852 croCT assisted potential field inversions using spherical harmonics (Fabian & de Groot, 853 2019). A new inversion algorithm based on this concept promises to reduce the quadratic 854 dependence of calculation time on the number of grains in the current inversion algo-855 rithm to an almost linear dependence, which will greatly reduce computational time. To 856 summarize, ongoing developments allow for an increase of at least three orders of mag-857 nitude in computational speed. This makes it possible to invert for  $> 10^5$  grains and 858 enables determining magnetic directions and intensities from individual grains in a sam-859 ple. 860

A unique feature of MMT is the possibility to derive paleomagnetic information from subsets of grains in the sample. Here we used a rather crude selection criterion for the grains based on their remanence ratios. It is important to emphasize once more that the magnetic surface scanning techniques used in this study are non-destructive. This implies that it is possible to mimic traditional paleomagnetic experiments such as step-

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wise demagnetization, or paleointensity experiments, while interpreting the magnetiza-

tion of individual grains. Also, these traditional paleomagnetic experiments may pro-

vide additional information on how to discriminate between grains with good and bad

magnetic recording properties, further testifying to the paleomagnetic potential of MMT.

870

# 6 Conclusions and Outlook

We showed that MMT is capable of determining magnetic moments of individual 871 grains in both synthetic and natural samples using different magnetic scanning techniques. 872 Thereby MMT is established as a paleomagnetic and rock-magnetic technique and it opens 873 up entirely new venues of paleomagnetic and rock-magnetic research. Nevertheless, two 874 significant challenges remain before MMT can be used to its full potential. First, the res-875 olution of the microCT scan must be increased to detect all grains of interest, potentially 876 down to the superparamagnetic threshold of  $\sim 50$  nm. Second, the computational power 877 should become sufficient to solve for the large amounts of grains necessary for a proper 878 statistical analyses of the magnetic moments obtained for individual grains. When these 879 two issues are resolved, MMT's unique ability to determine the magnetization of indi-880 vidual grains in a nondestructive way will enable a systematic analysis of how naturally 881 occurring iron-oxides record and retain information on the past state of the Earth's mag-882 netic field. These insights in which materials are reliable recorders of the ambient mag-883 netic field and which should be avoided are vital for the paleomagnetic community, and 884 adjacent communities using paleomagnetic data such as tectonic studies, studies of the 885 deep Earth, and (magneto-)stratigraphy. 886

By selecting only the contributions of known magnetically well-behaved grains in 887 a sample MMT enables obtaining reliable paleomagnetic information from even the most 888 complex, crucial, or valuable paleomagnetic recorders. This includes lavas that form an 889 indispensable archive of geomagnetic field variations. Fully unlocking this archive is vi-890 tal for our understanding of the short-term variability of the Earth's magnetic field. The 891 potential of MMT, however, is not limited to lavas; paleomagnetic information from even 892 more unique materials can also be retrieved. This includes e.g. the oldest rocks on Earth 893 to shed light on the origin and evolution of the Earth's core; meteorites to unravel the 894 conditions during the formation of our Solar system; and maybe even lunar samples to 895 elucidate its origin and evolution. 896

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Author contributions: LVdG designed the studies and wrote the manuscript together 905 with KF; ABé did the QDM study on a volcanic sample; ABé and MEK did the QDM 906 study on the synthetic sample; DCO and TvL contributed to the inverse data process-907 ing and computational workflow; RFF did the QDM measurements; CMLJ did the MTJ 908 study with the help of RJH; ABa did the MicroCT analyses. The authors declare no com-909 peting interests. 910

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