# Mapping the thermal structure of southern Africa from Curie depth estimates based on wavelet analysis of magnetic data with uncertainties

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November 23, 2022

# Abstract

Surface heat flow provides essential information on the thermal state and thickness of the lithosphere. Southern Africa is a mosaic of the best-preserved and exposed crustal blocks, assembled in the early late Archean and then modified by a series of major tectono-thermal events, both of Precambrian and Phanerozoic. Understanding the thermal and compositional structure of the southern African lithosphere provides crucial information for the actual causes, processes of lithospheric stability, and modification. Temperature plays a major role in the distribution of the long-wavelength crustal magnetic anomalies. Curie depth, interpreted as the depth to \$580^{(circ)}C, provides a valuable constraint on the thermal structure of the lithosphere. Due to the sparse distribution of surface heat flow data, we examine the degree to which the thermal structure of the crust can be constrained from the Curie depth in southern Africa. The Curie depth is estimated from magnetic anomaly data using spectral methods in combination wavelet analysis; a Bayesian approach is applied to address the uncertainty. Subsequently, the obtained Curie depth is used to estimate the surface heat flow, and the outcome is compared to available heat flow measurements. Unlike other cratonic regions, the shallowest Curie depth and low effective elastic thickness values observed over the Kaapvaal Craton suggest thermal reworking of the cratonic lithosphere in this region.

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# Key Points:

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9	•	Depth to the bottom of the magnetized source over southern Africa via power
10		spectral methods and wavelet transforms are estimated.
11	•	Estimation of heat flow and its uncertainty based on Curie depth are estimated
12		within a Bayesian framework.
13	•	The shallow magmatic provinces along the Kalahari magnetic lineament lead to
14		an underestimation of the Curie depths.

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#### 15 Abstract

Surface heat flow provides essential information on the thermal state and thick-16 ness of the lithosphere. Southern Africa is a mosaic of the best-preserved and exposed 17 crustal blocks, assembled in the early late Archean and then modified by a series of 18 major tectono-thermal events, both of Precambrian and Phanerozoic. Understanding 19 the thermal and compositional structure of the southern African lithosphere provides 20 crucial information for the actual causes, processes of lithospheric stability, and mod-21 ification. Temperature plays a major role in the distribution of the long-wavelength 22 23 crustal magnetic anomalies. Curie depth, interpreted as the depth to 580°C, provides a valuable constraint on the thermal structure of the lithosphere. 24

Due to the sparse distribution of surface heat flow data, we examine the degree 25 to which the thermal structure of the crust can be constrained from the Curie depth 26 in southern Africa. The Curie depth is estimated from magnetic anomaly data using 27 spectral methods in combination wavelet analysis; a Bayesian approach is applied to 28 address the uncertainty. Subsequently, the obtained Curie depth is used to estimate the 29 surface heat flow, and the outcome is compared to available heat flow measurements. 30 Unlike other cratonic regions, the shallowest Curie depth and low effective elastic 31 thickness values observed over the Kaapvaal Craton suggest thermal reworking of the 32 cratonic lithosphere in this region. 33

# <sup>34</sup> Plain Language Summary

The thermal state and thickness of the lithosphere are reflected, among other quantities, in the surface heat flow. While heat flow data are rather sparse, magnetic anomaly maps are widely available and allow, under certain conditions, the estimation of the bottom of the magnetized layer within the lithosphere. Latter can be associated with the 580°C-isotherm (frequently called the Curie depth), therefore allowing inferences on the thermal state of the lithosphere from magnetic data.

Here, we use classical power spectral methods in combination with wavelet anal-41 ysis and Bayesian methods to estimate the Curie depth and its uncertainty from mag-42 netic anomaly maps, and subsequently, use it to estimate the surface heat flow over 43 southern Africa. Comparison with the sparsely available measured heat flow allows 44 us to assess the quality of the estimation and to interpret it with respect to the litho-45 spheric structure. Southern Africa is particularly suitable for such a study due to 46 its well-preserved and well-studied crustal blocks. One outcome of our study is, e.g., 47 that the shallow Curie depths observed over the Kaapvaal Craton suggest a thermal 48 reworking of the old lithospheric structures in this region. 49

# 50 1 Introduction

Estimating the spatial variations in the temperature within the Earth is impor-51 tant to constrain the thermal structure and the rheology of the lithosphere (Audet & 52 Gosselin, 2019). Curie depth estimates, which correspond to the depth where crustal 53 rocks reach their Curie temperature ( $\sim 580^{\circ}$ C for magnetite; Dunlop & Ozdemir 54 (2001)) give independent temperature constraints over an area where magnetic anomaly 55 data are available. Above the Curie temperature, rocks lose their ability to maintain 56 ferromagnetic magnetization (Haggerty, 1978) and become paramagnetic. Therefore, 57 we identify the Curie depth with the depth of the magnetized crust (although the Curie 58 depth reflects a transition zone rather than an exact depth (Haggerty, 1978)). This 59 can provide information on crustal temperatures at depths not accessible by boreholes 60 (Andrés et al., 2018) and, consequently, yieds a valuable constraint for geothermal 61 heat flow (Kaban et al., 2014). 62

The thickness and depth to the base of the magnetized crust (Curie depth) is 63 reflected in the wavenumber content of the magnetic anomaly data. Under certain 64 assumptions, like a fractal magnetization model, the magnetic thickness and depth 65 can be estimated directly from the radially averaged power spectrum of the magnetic 66 anomaly (Bouligand et al., 2009; Maus et al., 1997). Various methods have been pro-67 posed in that direction and have been applied to many regions of the Earth. Typically, 68 magnetic anomaly data are interpolated, gridded, and processed by moving windows 69 approaches to suit such a spectral setup. Li et al. (2017) presents a global Curie depth 70 model based on magnetic anomaly but does not provide the estimated uncertainty of 71 Curie depth. Here, we use a 2-D wavelet approach, in combination with the classical 72 power spectrum setup, where wavelets at different scales are convolved with the entire 73 magnetic anomaly grid to estimate the wavenumber content of the data at particular 74 locations (Swain & Kirby, 2003; Kirby & Swain, 2014; Pérez-Gussinyé et al., 2009; 75 Gaudreau et al., 2019). This avoids the segmentation of the signal into finite-size 76 windows. Additionally, we incorporate a Bayesian framework in order to supply un-77 certainties for the obtained Curie depth estimates (Mather & Fullea, 2019; Mather & 78 Delhaye, 2019). 79

Alternative approaches to classical Curie depth estimation via spectral methods are currently under development (Ebbing, Szwillus, & Dilixiati, 2021). Here we stick to the classical approach but combine it with wavelets and a Bayesian setup to address and quantify at least some of its shortcomings. The focus of the paper is the interpretation of the calculated results of the Curie depth and heat flow estimates in terms of the geological and tectonic setting in southern Africa. We also provide uncertainty metrics to inform the interpretation of the resulting map and its further use.

Despite the importance of Curie depth estimation from magnetic data, the ques-87 tion arises whether the spectral techniques can provide reliable depth estimates and if 88 these estimates represent the Curie isotherms or a structural boundary (Ebbing et al., 89 2009). This is a concern particularly in the stable cratonic lithosphere and when the 90 tectonic domain is overprinted by magmatic intrusions. In the course of the paper, 91 we interpret the estimated Curie depths over southern Africa in terms of geology and 92 tectonics of the region, as well as in the context of the Moho and available heat flow 93 data. Considering the Curie depth as a proxy to the lithospheric thermal structure, we 94 use it to compute the temperature distribution within the crust. Due to limited heat 95 flow values based on direct measurements, and the need for better estimates and best 96 constrain the spatial variation of heat flow, indirect method is applying here. This 97 helps to constrain models of thermally controlled physical properties and processes, particularly where heat flow measurements are sparse (Li et al., 2017). We validate 99 our predictions of geothermal heat flow across southern Africa against surface heat 100 flow data to examine the variations and controls of the crustal thermal architecture, 101 while accepting that the uncertainties remain large. The plethora of publicly available 102 data sets over southern Africa make it an ideal site to study and map the variations 103 of Curie depth and its implications. 104

#### 105

# 1.1 The Tectonic Settings of Southern Africa

The southern African tectonics consists of diverse tectonic terrains with unique 106 characteristics (cf. White-Gaynor et al. (2020) and Figure 1): (1) The main tectonic 107 units are the Archean Cratons that represent the ancient and stable core of the shield. 108 (2) The Cratons are surrounded by mobile belts that were under continuous deforma-109 tion of rifting and accretion during the different orogenic cycles during the Archean, 110 Proterozoic, and continued during the Phanerozoic. (3) Within the Craton and the 111 mobile belts Precambrian terrains exit that has experienced Phanerozoic compressional 112 tectonics, flood basalt volcanism, rifting, and plateau uplifting. On top of these diverse 113

tectonic units exist sedimentary basins that have developed during the Neoproterozoic
and early Palaeozoic times with depth that reach up to 15 km (Fadel et al., 2018)

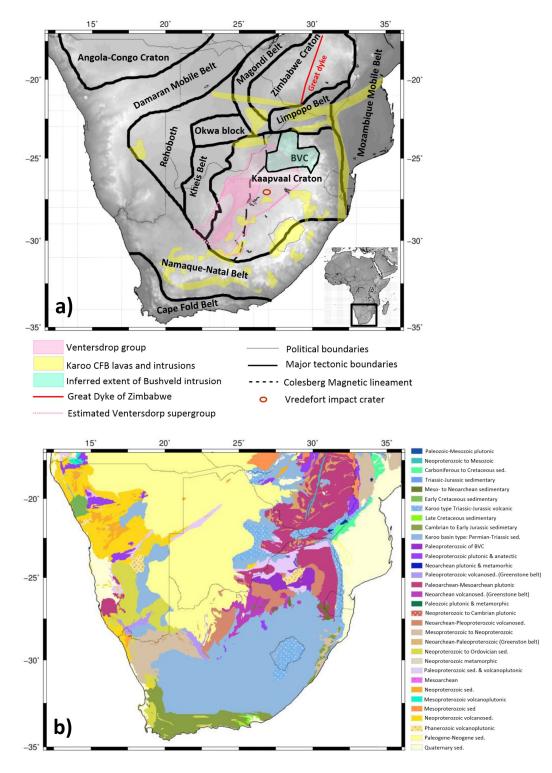
There are three main Cratons within the study area. The Kaapvaal and Zim-116 babwe Cratons formed in the Mesoarchean to Neoarchean and mainly consist of granite-117 greenstone terranes (de Wit et al., 1992). The Limpopo Belt suture the Kaapvaal and 118 the Zimbabwe cratons and the three units together form the greater Kalahari Craton 119 (de Wit et al., 1992). The Limpopo Belt was formed during the Neoarchean collision 120 between the Zimbabwe and Kaapval craton. The last major tectono-thermal events 121 122 that affected the Kalahari Craton were, respectively, the emplacement of the Great Dike Karoo in the Zimbabwe craton in the late Neoarchean (c. 2.6 Ga) (Jelsma & 123 Dirks, 2002), and the formation of the Bushveld igneous complex during the Paleo-124 proterozoic (c. 2.1 Ga) within the Kaapvaal craton (Figure 1; Olsson et al. (2010)). 125 To the northwest of the study area exists the Congo Craton that consists of Archean 126 and Paleoproterozoic rock units that with the oldest record at the northwestern block 127 was formed during the Mesoarchean (Begg et al., 2009; Ernst et al., 2013). The Congo 128 Craton and the Sao Francisco Craton in South America amalgamated together as 129 one unit during the Paleoproterozoic (2.0 Ga) until the breakup of Africa and South 130 America in the Mesozoic (130 Ma; Ernst et al. (2013)). The Rehoboth is one of the 131 poorer-defined regions in the study area with an Archean Nuclei (Van Schijndel et al., 132 2011). 133

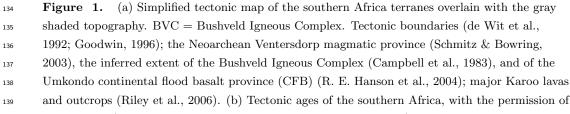
Southern Africa was subjected to continental growth during the Proterozoic due 141 to the accretion of younger blocks to the Archean terranes (Figure 1). A significant 142 part of the Rehoboth province was formed and aggregated around the Archean Nuclei 143 during the Paleoproterozoic (Van Schijndel et al., 2011). Then, the Kheis Belt and 144 Rehoboth Province accreted during the Paleoproterozoic to the western margin of the 145 Kaapvaal Craton (R. Hanson, 2003). After that, the Namagua-Natal Mobile Belt was 146 formed and surrounded the southern margins of the Rehoboth province and Kaapvaal 147 Craton in the Mesoproterozoic (c. 1.2-1.0 Ga; McCourt et al. (2001)). From the 148 northwest to the center of the study area exists the Magondi-Okwa-Kheis belts that 149 are formed during the Paleoproterozoic (2.0-1.8) and accreted due to the Eburnean 150 Orogeny to the northwestern border of the Kalahari Craton (Begg et al., 2009) 151

Within the study area, there are two major Pan-African orogenic belts. The 152 Mozambique Belt originated in the eastern part of the study region during the final 153 assembly of Gondwana, c. 841–632 Ma (R. Hanson, 2003). During the collision of the 154 larger Kalahari Craton and the Congo Craton c. 580–500 Ma, Damara Ghanzi-Chobe 155 belt (hence called Damaran Mobile Belt) emerged in the northwest. The original 156 breakup of Gondwana corresponded with the creation of the c. 180 Ma Karoo major 157 igneous province and the rifting of the Karoo over southern Africa (Duncan et al., 158 1997). The Cenozoic era is characterized by the emergence of the initial rifts caused 159 by the spread of the EARS to the South. Seismically active fault systems indicate that 160 rifting is beginning in the Okavango Rift Zone (ORZ) in northern Botswana (Schmitz 161 & Bowring, 2003), with the East African Rift System potentially extending to central 162 Botswana as well (Fadel et al., 2020). The different tectonic domains with different 163 tectonic history and different ages varying from old Cratonic lithosphere, mobile belts 164 and Phanerozoic rifting and flood basalt volcanism combined with the plateau uplift 165 and the terminus of the East African rift system make southern Africa open laboratory 166 to study and map the variations of Curie depth along different domains with different 167 tectonic history and current thermal status. 168

# $_{169}$ 2 Methodology

There are two steps applied in the course of proposed workflow: first, the Curie depth estimation from magnetic data (described in Section 2.1) and, subsequently,





<sup>140</sup> OneGeology (http://portal.onegeology.org/OnegeologyGlobal/).

the modelling of geothermal heat flow based on Curie depth constraints (described in Section 2.2).

174 2.1 Curie Depth Estimation

Various spectral methods have been proposed and applied to estimate depth to the bottom of the lithospheric magnetization (e.g., Tanaka et al. (1999); Bouligand et al. (2009); Salem et al. (2014); Maus et al. (1997); Chopping & Kennett (2013); Li et al. (2017); Gaudreau et al. (2019)). This depth will be identified with the Curie depth throughout the remainder of this paper. We refer to the recent overview by Núñez et al. (2021) for a comparison of some of the approaches. In the following, we rather briefly describe the specific setup used in our approach.

We assume that the magnetized layer of the lithosphere is confined between two surfaces at depths  $z_t$  (top of the magnetized layer) and  $z_b$  (bottom of the magnetized layer). The thickness of the layer is denoted by  $\Delta z = z_b - z_t$ . Within this layer, we assume the magnetization to be of self-similar nature, described by a fractal parameter  $\beta$ . This yields that the power spectrum  $\Phi_M$  of the underlying magnetization is of the form

$$\Phi_M(k) = Ck^{-\beta},\tag{1}$$

where  $k = |\mathbf{k}|$  and  $\mathbf{k} = (k_x, k_y, k_z)$  is the wavenumber; *C* is some proportionality constant. Given these assumptions, the radial power spectrum  $\Phi$  of the magnetic anomaly corresponding to the previously described magnetization can be expressed by (cf. Bouligand et al. (2009); Maus et al. (1997))

$$\ln\left(\Phi(k_H)\right) = A - 2k_H z_t - k_H \Delta z - \beta \ln(k_H) + \ln\left(\int_0^\infty \left(\cosh(k_H \Delta z) - \cos(k_z \Delta z)\right) \left(1 + \left(\frac{k_z}{k_H}\right)^2\right)^{-1 - \frac{\beta}{2}} dk_z\right), \quad (2)$$

where  $k_H = |\mathbf{k}_H|$  and  $\mathbf{k}_H = (k_x, k_y)$  is the wavenumber in the horizontal plane; A is simply a constant determined by the proportionality constant C of the power spectrum  $\Phi_M$  of the magnetization.

The computation of the radial power spectrum from data is typically done by a windowed Fourier transform of a magnetic anomaly map (the original magnetic data upward-continued to 5-km altitude relative to the WGS84 datum), where an adequately sized square window is moved across the study region (e.g., Bouligand et al. (2009); Li et al. (2017); Wang & Li (2015); Witter & Miller (2017)). Such windowing procedures may lead to 'spectral leakage' that particularly affects the low wavenumbers of the power spectrum. In order to reduce such effects, Gaudreau et al. (2019) have proposed a wavelet approach where they compute the wavelet transform

$$W_{a,\mathbf{b}}[f] = \int_{\mathbb{R}^2} f(\mathbf{r})\psi_{a,\mathbf{b}}(\mathbf{r}) \, d\mathbf{r},\tag{3}$$

of the magnetic anomaly map f at varying scales a (decreasing a indicate an increasing 185 spatial localization of the wavelet  $\psi_{a,\mathbf{b}}$ ). This does not require explicit windowing and 186 all available data can be used for the computation of  $W_{a,\mathbf{b}}[f]$ . The parameter **b** denotes 187 the spatial shift of the wavelet and corresponds to the locations for which we want to 188 evaluate the power spectrum (comparable to the center of the window if one were using 189 a windowed Fourier transform). The scale parameter a of the wavelet transform can 190 be related to a specific wavenumber  $k_H$ , which enables the use of wavelet transforms 191 for the estimation of the radial power spectrum  $\Phi$ , and which is indicated in more 192 detail in Gaudreau et al. (2019); Kirby (2005). We will use their approach to obtain 193 the radial power spectrum from the WDMAM2 magnetic anomaly map (cf. section 194

<sup>195</sup> 3.1 for the description of the used data) based on wavelet transforms. Once the power <sup>196</sup> spectrum is computed from the available data, it can be compared to the theoretical <sup>197</sup> expression in (2) in order to obtain information on the parameters A,  $z_t$ ,  $\beta$ , and  $z_b$ , <sup>198</sup> and the goodness of fit is calculated using the reduced chi-square statistic.

The inherent shortcomings of the power spectrum approach have been discussed 199 extensively in some of the previously mentioned references on Curie depth estima-200 tion: the assumption of the magnetization being self-similar is contradictory to the 201 expression via Fourier integrals (this can be ameliorated by conceiving it in terms of 202 "bandlimited self-similarity"; Maus et al. (1997)); low wavenumber contributions of 203 the power spectrum are difficult to compute reliably from magnetic anomaly data (cf. 204 Bouligand et al. (2009) for an investigation in terms of the windowed Fourier trans-205 form; here, we ameliorate these problems by use of wavelet transforms as in Gaudreau 206 et al. (2019)); the parameters A,  $z_t$ ,  $\beta$ ,  $z_b$  are strongly interrelated, e.g., an increase in 207  $\beta$  can be compensated by a decrease in  $z_b$  (cf. Bouligand et al. (2009) for a study on 208 this; in section 4.1.1 we also briefly comment on this). 209

# 2.1.1 Bayesian Setup

In what follows, we describe the Bayesian framework that we use to obtain information on A,  $z_t$ ,  $\beta$ , and  $z_b$ . We are interested in posterior distribution  $P(\mathbf{m}|\mathbf{d})$ of the parameters  $\mathbf{m} = (A, z_t, \beta, z_b)$ , provided some input data  $\mathbf{d}$  (in our case, this will be the radial power spectrum  $\mathbf{d} = (\Phi(k_H^1), \ldots, \Phi(k_H^n))$  at various wave numbers  $k_H^1, \ldots, k_H^n$ ; obtained via wavelet transforms of a magnetic anomaly map). Our later illustrations on the obtained Curie depth  $z_b$  (cf. figure 5) represent the mean of this posterior distribution, while the uncertainty is expressed in terms of the variance of the posterior. The classical Bayes formula for the posterior reads as follows:

$$P(\mathbf{m}|\mathbf{d}) \propto P(\mathbf{d}|\mathbf{m}) P(\mathbf{m}),$$
(4)

where  $P(\mathbf{d}|\mathbf{m})$  denotes the likelihood and  $P(\mathbf{m})$  the prior. The prior is chosen to be a uniform distribution, not preferring any particular value of the parameter set. However, for our Curie depth models we fix the depth to the top of the magnetization  $z_t$  (this is done by the sediment thickness provided by CRUST1.0, assuming that the magnetization of sediments is negligible; cf. section 3.3), and we also fix the fractal parameter  $\beta$  (but we run the computations for various fixed  $\beta$  in the range of 1.5 to 4.0, with grid step 0.5, values that have been considered reasonable by earlier geological studies). In other words, our prior only assumes a uniform distribution of the parameters  $\mathbf{m} = (A, z_b)$ . In section 4.1.1, we briefly illustrate the influence of considering  $\beta$ as an additional free parameter in the Bayesian setup. The likelihood is assumed to be a Gaussian distribution whose mean value  $\boldsymbol{\mu}_{\mathbf{m}}$  is provided by the theoretical power spectrum (2) and whose variance  $\boldsymbol{\sigma}_{\mathbf{d}}^2$  is computed from the input magnetic anomaly map. This leads to the following expression of the posterior distribution:

$$P(\mathbf{m}|\mathbf{d}) = C \exp\left(-\sum_{i=1}^{n} \frac{\left|\mu_{\mathbf{m}}^{i} - d_{i}\right|^{2}}{2\left|\sigma_{\mathbf{d}}^{i}\right|^{2}}\right),\tag{5}$$

for some constant C. This distribution is then sampled via a Metropolis-Hasting algorithm in order to obtain the posterior mean and variance of the parameters  $\mathbf{m}$ , in particular of  $z_b$  (cf. Mather & Fullea (2019); Mather & Delhaye (2019) whose code we will be using here).

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# 2.2 Geothermal heat flow

To determine the heat flow distribution, we assume steady state conditions with no lateral variation in material properties and heat production (e.g., Afonso et al. (2019)). Then, Fourier's Law states:

$$K_1 \frac{\partial T(z)}{\partial z} = -q(z), \tag{6}$$

where T is the temperature, z is the depth, and  $K_1$  and q(z) are the thermal conductivity and heat flux, respectively. If initial conditions are provided by knowledge of  $z_b$  as the Curie depth,  $T_c$  as the Curie temperature (~ 580°C) and  $T_0$  as the surface temperature, then the solution of the differential equation above leads to the following expression for the surface heat flow (e.g., Martos et al. (2017)):

$$q_s = \frac{K_1(T_c - T_0)}{z_b} + H_0 h_r - \frac{H_0 h_r^2}{z_b} \left(1 - e^{\frac{-Z_b}{h_r}}\right),\tag{7}$$

where  $H_0$  is the radiogenic heat production, and  $h_r$  is the scale depth at which  $H_0$  decreased to 1/e of its surface value; assuming an exponential decrease of heat production with depth (e.g., Lachenbruch (1970)).

Later on, we refer to this setup as 1-D model or "constant conductivity model" 219 because we assume  $K_1$  to be constant within the entire crust and mantle. The cor-220 responding surface heat flow models indicated in sections 4.2 and 5.1 are computed 221 from (7), using the Curie depth  $z_b$  obtained in section 4.1 and fixing  $H_0 = 2 \mu W/m^3$ , 222  $h_r = 10$ . The outcome is typically indicated for various (but fixed) thermal conduc-223 tivities  $K_1$  (Martos et al., 2017). Furthermore, we provide some basic indicators of 224 uncertainty for the heat flow: we compute  $q_s$  based on  $z_b$  as well as on  $z_b \pm \sigma$  (where 225  $\sigma$  denotes the uncertainty of  $z_b$  as indicated in the results in section 4.1) and provide 226 the maximum of the residuals between the three resulting outcomes as a measure of 227 uncertainty for the surface heat flow  $q_s$ . 228

229

# 2.2.1 Varying thermal conductivities

In addition to the 1-D model from above, we consider a setup where thermal conductivities may vary. We allow different thermal conductivities  $K_1$  and  $K_2$  within the crust and the mantel, respectively. Furthermore, the heat flux is assumed to be purely vertical and each lithospheric column is in thermal equilibrium. Thus, within each column,  $K_1$  and  $K_2$  are constant, but the thermal conductivities are allowed to vary (laterally) among the different columns.

Given this setup, Fourier's law (6) can be used to derive the temperature dependence with respect to depth (e.g., Lösing et al. (2020)), analogously to the 1-D case indicated above. Assuming that no heat is produced within the lithospheric mantle, the temperature in the lithospheric mantle at depth z is expressed as follows:

$$T(z) = T(M) + \frac{q_D}{K_2}(z - M),$$
(8)

where M is the Moho depth and  $q_D$  is the heat flux at the Moho boundary. Within the crust, the temperature can be expressed more generally in the form

$$T(z) = T_0 + \frac{q_s z - \dot{H}(z)}{K_1},$$
(9)

where  $\bar{H}(z) = \int_0^z H(s)ds$ , and H(z) is the total heat production. We assume that the heat production decays exponentially with depth, so that  $H(z) = H_0 \exp(-z/h_r)$ . In this case, (9) is just a rearranged version of (7). The heat flux q(z) at any specific depth z within the crust is equal to the surface heat flux  $q_s$  minus the total heat production, so that we obtain the following simple relation between the surface heat flux  $q_s$  and the heat flux  $q_D$  at the Moho:

$$q_D = q_s - H(M). \tag{10}$$

Equations (8), (9), (10) allow to relate  $q_s$ ,  $q_D$ ,  $H_0$ ,  $K_1$ ,  $K_2$  to the temperatures  $T_0$ ,  $T_c$ ,  $T_{LAB}$  at the surface, at the Curie depth  $z_b$ , and at the Lithosphere-Asthenosphere boundary  $z_{LAB}$ , respectively.

A Bayesian framework almost identical to that in section 2.1.1 can then be used to 239 invert the input  $\mathbf{d} = (T_0, T_c, T_{LAB})$  for the parameters  $\mathbf{m} = (q_D, H_0, K_1, K_2)$  within 240 each lithospheric column (provided that we have knowledge of M,  $z_{LAB}$ , and  $z_b$ ). 241 Opposed to the setup of the 1-D model from before, the thermal conductivities  $K_1$ , 242  $K_2$  are not fixed anymore but will be inverted for jointly with the heat flux  $q_D$  at the 243 Moho and the radiogenic heat production  $H_0$ . For more details, we refer the reader to 244 Lösing et al. (2020), whose code we will be using here. The main quantity of interest 245 to us is the posterior mean of  $q_D$  that allows to obtain the desired surface heat flow 246  $q_{s}$  via (10). 247

The input temperatures are set to the values  $T_0 = 0^{\circ}$ C,  $T_c = 580^{\circ}$ C,  $T_{LAB} =$ 1315°C, as is also done in related works. The underlying Moho depths M and the Lithosphere-Asthenosphere boundary  $z_{LAB}$  stem from the models described in section 3.4, while we use our results from section 4.1 for the required Curie depths  $z_b$ . The uncertainties available for  $z_b$  are used in an identical way as in the 1-D model setup to provide basic indicators of uncertainty for the surface heat flow  $q_s$ . The results are illustrated in section 5.1 and we refer to this setup as "varying conductivity model".

255 **3 Data** 

259

In the following section we describe the datasets used in the study, and any necessary initial data preparation. We limit the model to the continental area, the overview of used data is provided in Table 1.

3.1 Magnetic Data

We used the magnetic data from the recently released World Digital Magnetic 260 Anomaly Map 2.0 (WDMAM 2.0) (Lesur et al., 2016; Catalán et al., 2016). WDMAM 261 2.0 provides a 5km raster (grid) of magnetic anomalies, jointly compiled from marine 262 cruises at sea level and airborne surveys at 5km height. All data are upward-continued 263 to 5-km altitude relative to the WGS84 datum. WDMAM are continuously updated in 264 the framework of an international scientific project, which runs under the auspices of 265 International Association of Geomagnetism and Aeronomy (IAGA) and Commission 266 for the Geological Map of the World (www.wdmam.org). 267

The African magnetic mapping project (Green et al., 1992) led to the SaNaBoZi aeromagnetic grid (Figure 2); the name stands for South Africa, Namibia, Botswana, and Zimbabwe (Stettler et al., 2000). The SaNaBoZi grid and more recently acquired grids over Zambia and Mozambique as well as marine data offshore of South Africa have been compiled and are part of the second version of the WDMAM (Lesur et al., 2016) used in this study (Figure 2).

Here, we will briefly summarizing the regional-scale magnetic features in the 282 study area. The Namaque-Natal domain is characterized by a remarkable, broadly 283 spatially coincident, continental-scale magnetic anomaly, namely, the Beattie Mag-284 netic Anomaly (BMA described by (Scheiber-Enslin et al., 2014; Cornell et al., 2011)) 285 which extends from the western to the eastern coastal margins for more than 1100 286 km. To the North, the Kalahari magnetic lineament (Botswana Geological Survey 287 Department et al., 1978) is characterized by short-wavelength magnetic anomalies 288 which interpreted as the western boundary of the Kaapvaal Craton. This anomaly 289 is one of the most dramatic features in the aeromagnetic image of southern Africa. 290 Within the Kaapvaal Craton, long-wavelength magnetic anomalies are characterizing 291 the Colesberg magnetic lineament. The boundary between the Kaapvaal Craton and 292

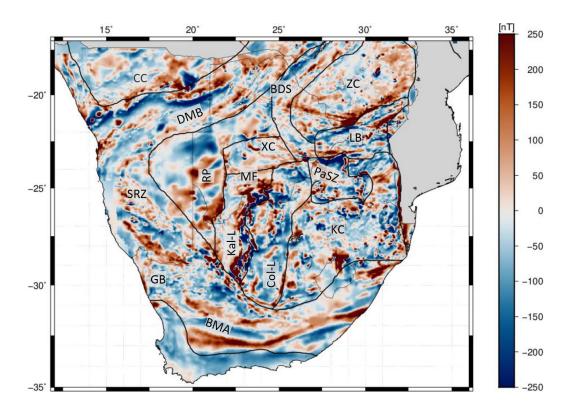


Figure 2. Total Magnetic Intensity (TMI) map of southern Africa from WDMAM2.0 (Lesur 268 et al., 2016) with 2 arc-minute grid spacing (approximately 4 km). The original data are upward-269 continued to 5-km altitude relative to the WGS84 datum. Black lines represent the major tec-270 tonic provinces of southern Africa (de Wit et al., 1992). BMA = Beattie Magnetic Anomaly; 271 BDS = Botswana Dyke System; CC = Congo Craton; Col-L = Colesberg Lineament; DMB = 272 Damaran Mobile Belt; GB = Gariep Belt; KC = Kaapvaal Craton; LB = Limpopo Belt; MF = 273 Molopo Farm; PaSZ = Palala Shear Zone; RP = Rehoboth Province; SRZ = Sinclair-Rehoboth 274 Zone; ZC = Zimbabwe Craton.275

the Limpopo Belt is characterized by a long-wavelength magnetic anomaly associated 293 with the Palala shear zone (PaSZ). Moving to the North, the boundary between the 294 Zimbabwe Craton and Limpopo Belt is relatively well defined from a clear change in 295 the magnetic anomaly across the boundary. Moving towards the west, the magnetic 296 anomalies along the Karoo basalts are shown in Botswana as well as the Botswana 297 dyke swarm. In Namibia, long-wavelength, curvilinear magnetic anomalies are ob-298 served which associated with Sinclair-Rehoboth Zone (Van Schijndel et al., 2011). A 299 weak imprint of the Beattie anomaly is visible even in the satellite lithospheric mag-300 netic field model LCS-1 by Olsen et al. (2017) (Ebbing, Dilixiati, et al., 2021) (see 301 Figure S1 of supplementary material), which confirms its regional significance. 302

#### 303 3.2 Heat Flow Data

The compilation of surface heat flow data used in this work (Figure 3-a) comes 310 from different sources (e.g., Pollack et al. (1993)). Lucazeau (2019) compile all available 311 data in the New Global Heat Flow database (NGHF), which is an extended compilation 312 of earlier heat flow catalogs, associated with meta data attributes with links to original 313 studies. Measurements are, however, irregular in distribution and of varying quality. 314 The quality of heat flow measurements are rated in NGHF. The rating category for 315 each measurement is based on e.g. the variation of heat flow in the borehole where the 316 measurement is performed. Old and questionable measurements are generally assigned 317 a lower rating. According to the NGHF database, most of heat flow data used here 318 have an uncertainty between 10 and 20  $\text{mW/m}^2$  (Lucazeau, 2019) (see Figure S2 of 319 supplementary material). In general, the Kaapvaal and Zimbabwe Cratons have a 320 relatively low heat flow ( $\approx 40-50 \text{ mW/m}^2$ ); these values increase to  $\approx 60 \text{ mW/m}^2$  at 321 the boundary between the Craton and the surrounding Proterozoic and Pan-African 322 mobile belts. Mobile belts surrounding the Kaapvaal Craton exhibit the highest heat 323 flow signatures in South Africa ( $\approx 70 \text{ mW/m}^2$ ), which may be linked to underlying 324 geological, tectonic and crustal compositional controls, particularly related to the heat 325 production of radiogenic material.

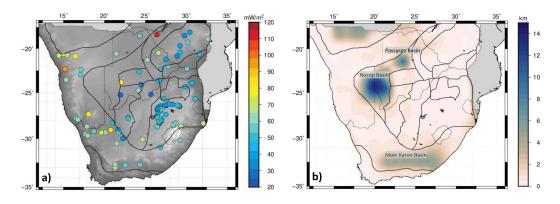


Figure 3. (a) Distribution of heat flow measurements within the study area from the global database (Lucazeau, 2019). The associated uncertainty of measured heat flow is shown in Figure S2. (b) Sediment thickness map of southern Africa extract from global sediment thickness map (Laske et al., 2013) used to constrain the depth of the upper boundary of magnetized layer  $(z_t)$ and fixed prior to the inversion. Major sedimentary basins are presented: Main Karoo Basin (Johnson et al., 1997); Nosop Basin (Wright & Hall, 1990); Passarge Bain (Key & Ayres, 2000a).

## 3.3 Sediment Thickness

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The sedimentary data are extracted from the sediment layers of CRUST1.0 (Laske et al., 2013), defined on a  $1^{\circ} \times 1^{\circ}$  grid, which we project and interpolate onto a rectangular grid with a sampling interval of 4 km to be compatible with the magnetic data resolution. The sediment thickness map in Figure 3-b is used to constrain the depth to the top of the magnetized layer ( $z_t$ ), since sedimentary rocks are expected to be only weakly (para)magnetic (Ellwood et al., 2000) and their overall contribution is considered negligible.

# 3.4 Crustal and Lithospheric Thickness

For the purpose of comparing the bottom of the magnetized layer with the crustal 336 thickness in the study area and to constrain the heat flow calculations from Curie 337 depth, we estimate the Moho depth by inverting the satellite gravity gradients using 338 the seismically constrained non-linear inversion scheme of Uieda & Barbosa (2017) 330 (Figure 4-a). Since large contributions of the heat flow comes from radioactive de-340 cay of elements within enriched crust (Hasterok & Chapman, 2011), considering the 341 crustal thickness in our modelling process can therefore substantially improve heat flow 342 maps. The lithospheric thickness model (Figure 4-b) is derived from the global refer-343 ence model of the lithosphere (Afonso et al., 2019) which is estimated from the joint 344 inversion of satellite-derived gravity gradients, geoid height, and absolute elevation 345 complemented with seismic, thermal and petrological information. 346

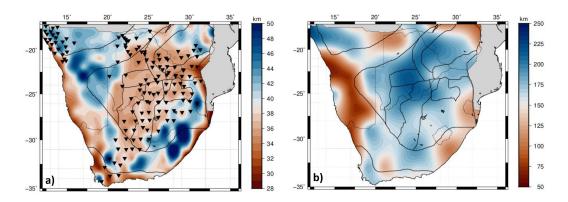


Figure 4. (a) Moho depth of southern Africa from the seimically constrained gravity inversion, the black circles represents the location of seismic stations used to constrain the gravity inversion for Moho depth (b) Lithosphere-Asthenosphere boundary (LAB) depth derived from LithoRef18, the global reference model of the lithosphere (Afonso et al., 2019).

#### 352 4 Results

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We present Curie depth maps and consequently heat flow maps, together with maps of uncertainty.

# 4.1 Curie Depth Estimates

The presented results in this section are shown as maps of the depths to the bottom of the magnetic layer  $(z_b)$ , which will be interpreted as Curie depth, together with the estimated uncertainties. The outcome is based on the procedure described in Section 2.1 and the data from Sections 3.

Data	Reference
<b>Geophysical</b> Magnetic data Heat flow	WDMAM2 (Lesur et al., 2016) NGHF (Lucazeau, 2019; Pollack et al., 1993)
Geometrical Sediment thickness Moho depth Base lithosphere	CRUST1.0 model (Laske et al., 2013) Gravity inversion(Uieda & Barbosa, 2017) with seismic con- straints (Fadel et al., 2020; Youssof et al., 2013) LithoRef18 (Afonso et al., 2019)

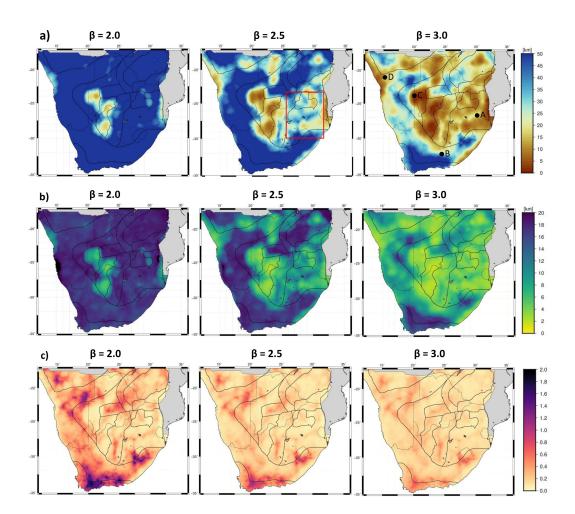
Table 1.	Summary	of datasets and	parameters used	in the modelling process.
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As mentioned earlier, estimating all quantities  $z_b$ ,  $z_t$ , and  $\beta$  simultaneously may lead to ambiguous values for  $z_b$  (illustrated, e.g., in Bouligand et al. (2009)). Therefore, 361 in this study, we fix  $\beta$  to a constant value for the entire study area. However, multiple 362 maps of  $z_b$  created using different (but fixed)  $\beta$  ranging from 2.0 to 3.0, which are 363 typical values estimated in crustal rocks (Maus et al., 1997; Maus & Dimri, 1996; 364 Pilkington & Todoeschuck, 1993) are shown in Figure 5. The top of the magnetic 365 layer  $(z_t)$  is fixed as well and not changed throughout the study. It is constrained by 366 the sedimentary thickness model shown in Figure 3-b, since this layer is most likely 367 weakly magnetic and is assumed to not contribute to the magnetic anomalies. Yet, to 368 provide at least a brief illustration of the influence of fixing these parameters in our 369 setup, we use subsection 4.1.1 to indicate the joint probabilities of the inversion at 370 selected locations when inverting for all three parameters simultaneously. 371

Figure 5 shows the inversion results with fixed parameters as mentioned above. 372 One can observe that an increase of  $\beta$  leads to a substantial decrease of the estimated 373  $z_b$ . This has also been illustrated in the synthetic examples in Section 3.3 of Bouligand 374 et al. (2009). As the  $\beta$  parameter increases from 2.0 to 3.0, the mean  $z_b$  value in the 375 Kaapvaal Craton decreases from 50 to 15 km. The mean  $z_b$  within the Kheis Belt 376 ranges from 25 to 5 km, and in the Zimbabwe Craton, the mean  $z_b$  ranges from 50 to 377 25 km. Along Damara Mobile Belt, the mean  $z_b$  is ranging from 15 to 5 km at the 378 North Botswana, with  $\beta$  increasing from 2.5 to 3.0. The mean  $z_b$  along Namagua-Natal 379 Belt, ranges from 50 to 30 km. However, Figure 5-a also indicates that the patterns 380 of the estimated Curie depth are robust with respect to  $\beta$  (i.e., regions that reveal a 381 shallow Curie depth compared to deeper surrounding regions remain shallow in this 382 relative sense across the whole range of tested values of  $\beta$ ) and, therefore, can provide 383 some reliable geophysical information about the observed Curie depth patterns. 384

The depth to the bottom of magnetisation varies across southern Africa from 20 394 to 50 km beneath Kaapvaal and Zimbabwe Craton, with uncertainties between 3 and 395 12 km, respectively. There is some exception along western part of Kaapvaal Craton 396 which have much shallower depth to the bottom of magnetisation than other Archean 397 Cratons despite the low surface heat flow values. This result may be explained by the 398 fact that we may have modelled only the depth extent of magnetic minerals rather 399 than the depth at which they have reached their Curie points. Furthermore, the very 400 strong magnetic response from Ventersdorp magnetic intrusion (Neoarchean age) may 401 be masking a more subtle signal of the deepest magnetic sources, which may well be 402 less magnetic than this magnetic intrusion. The eastern margin of Kaapvaal Craton 403 is modelled with shallow Curie depth along all the different  $\beta$ . This is probably due 404 to the presence of Karoo lavas along the boundary between Kaapvaal Craton and 405 Mozambique Mobile Belt. The western margin of the Kaapvaal Craton is modelled 406

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**Figure 5.** (a) Maps show the depth to the bottom of magnetic sources  $(z_b)$  based on the aero-385 magnetic data in southern Africa when depth to the top of magnetic sources  $(z_t)$  is set to the 386 sediment thickness from Figure 3-b and for various  $\beta$  (assuming constant  $\beta$  values throughout 387 the study area), illustrating the inverse relationship between the fractal exponent  $\beta$  and  $z_b$ . All 388 maps display similar long-wavelength features that are independent of the values of  $\beta$ . The red 389 box outlines the  $z_b$  along Kaapvaal region. The locations marked by the letters A,B,C, and D 390 correspond to the maps in Figure 6, and Figures S3 : S5. (b) The  $3\sigma$  uncertainty of the mean  $z_b$ 391 in southern Africa. (c) Maps of the reduced chi-square statistic illustrating the fit between the 392 calculated and the theoretical power spectra. 393

by shallow Curie depth which is related to reactivation of the Kheis province during 407 Kibaran orogeny (Thomas et al., 1993). The Kheis Belt consists of basalts and clastic 408 sediments located between the Kaapvaal Craton to the east and the Rehoboth terrane 409 to the west. The Kheis Belt form a distinct highly magnetic feature that extends 410 northwards to the Okwa Block (Hutchins & Reeves, 1980). Toward the Capo Fold 411 Belt, the depth to the bottom of magnetization using different  $\beta$  values is very deep 412 and not logic. But this is also the area with the most significant uncertainty and the 413 highest reduced chi-square. Our Curie depth map with  $\beta = 3.0$  (cf. Figure 5-a) is, 414 for the most part, concordant with the global reference model of (Li et al., 2017) and 415 follows a similar pattern of variation as we observe along Kaapvaal Craton. 416

The uncertainty and reduced chi-square of the fitted parameters associated with 417 the estimated Curie depth are shown in Figures 5-b and c, respectively. Generally, the 418 shallow Curie depths are associated with low uncertainties, and deeper Curie depths 419 have a significantly higher uncertainty. This may be due to difficulties in the estimation 420 of the small wave number portion of the radial power spectrum. Within each map in 421 Figure 5-b, the estimated  $z_b$  uncertainty is high where the  $z_b$  values are deeper than 422 50 km, and decreases with increasing  $\beta$ . The reduced chi-square value in the Kheis 423 Belt and Kaapvaal Craton remains relatively constant in the different inversions, but 424 decreases with increasing  $\beta$  in Damara Mobile Belt and Cape Fold Belt (Figure 5-c). 425 For all  $\beta$  values, the reduced chi-square is highest where is deeper than 50 km. 426

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# 4.1.1 Multiparameter Study for Selected Locations

In this section we briefly want to indicate the influence of fixing the parameter  $\beta$  for selected locations. Namely, we allow all parameters  $\mathbf{m} = (A, \beta, z_b)$  to vary and illustrate their marginal and joint posterior probabilities based on the methodology described in Section 2.1 (the top depth  $z_t$  remains fixed). The four specific locations for this study are those that are indicated by the letters A,B, C, and D in Figure 5-a (representing different tectonic domains within the study area).

In each case, the first step is to estimate the three parameters  $z_b$ ,  $\beta$ , and A 434 simultaneously (Figure 6-a). Subsequently,  $\beta$  is fixed to the mean obtained in this 435 first step and the inversion is done only for the two remaining parameters  $z_b$  and A 436 (Figure 6-b), (see section 4.1 for more details). For the grid cell (A) in the Kaapvaal 437 Craton, the results obtained from the joint inversion of all three parameters give a  $z_b$ 438 of 26.4 km and an uncertainty of 13.2 km. The mean of  $\beta$  is 3.0 with an uncertainty of 439 0.4. Keeping  $\beta$  fixed and running the inversion again, the uncertainty of  $z_b$  reduces to 440 10.4 km with a mean of 29.3 km, analogous to what has been obtained in Figure 5-b. 441 The result for the other three test sites (B, C, and D) are shown in Figures S3:S5 in the 442 supplementary material. The key outcome here is that the mean  $\beta$  obtained during the 443 simultaneous inversion for all three parameters  $z_b$ ,  $\beta$ , and A varies across all four tested 444 tectonic domains. Nonetheless, the obtained  $\beta$  for any of these domains corresponds 445 to one of the  $\beta$  for which the Curie depth has been computed and indicated over entire 446 southern Africa in Figure 5-a. This should be kept in mind when interpreting inversion 447 results for  $z_b$  with fixed  $\beta$ , and the appropriate map should be chosen. 448

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## 4.2 Heat Flow Estimates

In this study, we assume a Curie temperature of the crustal rocks in southern
Africa of around 580°C, which corresponds to the Curie temperature of magnetite
(Dunlop & Özdemir, 2001). The quantitative comparison between Curie depth and
heat flow measurements was performed to validate the results of Curie depth and
evaluate the method to determine it from magnetic data.

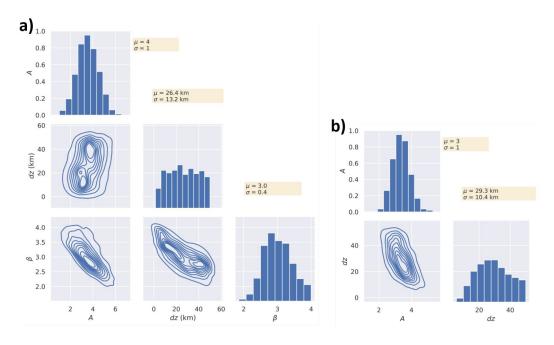


Figure 6. Statistical distribution of model parameters from at location A of Figure 5-a: marginalized and joint posterior distribution from the simultaneous inversion for the parameters  $z_b, \beta$ , and A (a) and for the simultaneous inversion for  $z_b$  and A, with fixed  $\beta = 3.0$  (b). Statistical information on each  $z_b, \beta, A$  is provided in the orange boxes;  $\mu$  is the mean value,  $\sigma$  is the standard deviation. Note that the parameter dz in the above plots indicates  $\Delta z$  in our notation, so that  $z_b = z_t + dz$ .

The distribution of heat flow measurements is shown in Figure 3-a. The heat 461 flow measurements are relatively dense in Kaapvaal and Zimbabwe cratons, with val-462 ues ranging from  $\sim 40$  to  $\sim 60 \text{ mW/m}^2$ , and along mobile belts ranging from  $\sim 55$ 463 to  $\sim 80 \text{ mW/m}^2$ . On the other hand, the rest of the study area suffers from highly scattered and sparse distributions of heat flow measurements. The calculated heat 465 flow values  $q_s$  from the 1-D model in section 2.2, based on equation (7) with  $\beta = 2.5$ , 466 are plotted versus Curie Depth for different thermal conductivities  $K_1$  (cf. Figure 7). 467 We also included measured heat flow values from the global database Lucazeau (2019), 468 plotted against the estimated Curie depths from section 4.1 at the measurement loca-469 tions. Obviously this comparison has a significant degree of variance. Variances in the 470 assumed parameters of the Curie depth modelling procedure (as indicated in Figure 471 5-b), uncertainties of the heat flow measurements, and uncertainties like lithologically 472 bounded vs. thermally controlled magnetisation depths all add to the observed scatter 473 of the fit. Unlike the first two points, the uncertainty due the lack of precise lithological 474 bounds cannot be quantified by any of the existing methods. This is why we discuss 475 in Section 5 the outcome of the Curie depth estimation and the heat flow estimation 476 jointly with the geological situation in southern Africa. Figure 7 shows that in par-477 ticular the shallow Curie depth reveal a large mismatch with the measured heat flow 478 values, implying that these shallow depths might not represent the maximum depth of 479 magnetic layer but correlate with the overprinted magnetic activities. Locally, how-480 ever, the correlation can be quite good. Figure 8 shows an analogous scatter plot, 481 but the  $z_b$  results are restricted to the Kaapvaal Craton, since it has dense heat flow 482 measurements for better comparison. 483

As shown in our previous results, larger  $\beta$  than the correct value can be compensated by shallower  $z_b$ . Consequently, higher estimated heat flow are not necessarily related with the actual thermal state of the study area. Calibration of the results using some actual thermal gradient measurement could help to validate the heat flow results in the future.

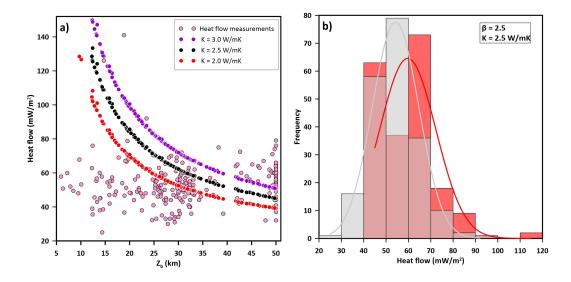


Figure 7. (a) Heat flow as a function of  $z_b$ . The curves plotted are the theoretical heat flow curves for different thermal conductivity 2.0 (red), 2.5 (black), 3.0 (purple). The scattered dots (light pink) represent the measured heat flow from Lucazeau (2019). (b) Frequency of estimated heat flow values (in gray) and of the measured heat flow values (in red).

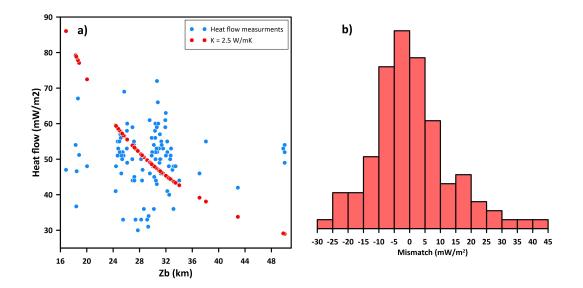


Figure 8. (a) Heat flow as a function of  $z_b$ . Same as in Figure 7, but restricted to the Kaavaal Craton. (b) Frequency of mismatch between the estimated and the measured heat flow.

# $_{495}$ 5 Discussion

In this section, we first discuss the correlation between the mapped Curie depth
 and heat flow measurements (section 5.1), followed by discussing the benefits of varying
 the thermal parameters in modelling heat flow, we then note the limitations associated
 with the used methodology.

The relationships of our results to compilations of thermal estimates for the 504 southern Africa highlight both areas where our depth to the bottom of magnetisation 505 matches the expectations of Curie depth and areas where it does not. Such differences 506 may indicate areas where our understanding of the thermal regime is incomplete, or 507 could arise from differences in geology resulting from processes such as major tectonic 508 events changing magnetic mineralogy. Comparing the estimated Curie depths with 509 the magnetic data shows the following: the shallow  $z_b$  areas generally correspond to 510 the short-wavelength dominated anomalies, such as in the magnetic signature of Kheis 511 Belt and the Kalahari magnetic lineament (Figure 2); (Botswana Geological Survey 512 Department et al., 1978). On the other hand, areas mapped with deep  $z_b$  generally 513 correspond with the areas dominated by long-wavelength anomalies, such as the Beat-514 tie continental scale Magnetic Anomaly (BMA; (Scheiber-Enslin et al., 2014; Cornell et 515 al., 2011)). Along the Okavango Rift Zone in the north-western part of Botswana,  $z_b$ 516 is shallow ranging from 8-15 km which is coincident with the thermal perturbation of 517 Okavango Rift (Leseane et al., 2015) and crustal thinning (Fadel et al., 2020). The first 518 obvious observation was that the very shallow Curie depth in the middle of Botswana 519 fell into the part of the sedimentary basins (Passarge and Nosop Basin) which are 520 intruded by Xade complex and Okwa block (cf. Figure 1). Along the Molopo Farm 521 ultra basic intrusion (Key & Ayres, 2000b), the Curie depth is shallow ranging from 522 15 - 20 km with  $\beta$  value 2.5. Toward eastern part of Botswana, the Curie depth is 523 deep, which coincide with the Zimbabwe Craton and the old belts in this area. In 524 South Africa, the Kaapvaal Craton and Venterschorp group magamtic intrusion are 525 very visible in the magnetic anomaly map (cf. Figure 2), and this is reflected in the 526  $z_b$  maps (cf. Figure 5-a). Along Venterschorp group magamtic intrusion, the  $z_b$  values 527 that are distinctly shallower than the rest of the southern Africa: when  $\beta$  is set to 528 3.0, the average  $z_b$  is ranging from 0-5 km. In contrast with Kaapvaal Craton: when 529  $\beta$  is set to 2.5, the average  $z_b$  is 30 km. Along Kalahari magnetic lineament, similar 530 long-wavelength features for all values of  $\beta$  are shown, indicating that these patterns 531 are robust and have geophysical significance. One could interpret the shallow  $z_b$  along 532 Kalahari magnetic lineament as a lithological contact that represents the base of the 533 magnetized crust, and that is shallower than the actual Curie depth (Blakely, 1988); 534 however, there is no magmatic activity recorded along this area. A more reasonable 535 explanation is that there is a strong change in lithology and geological history resulting 536 in a different  $\beta$  value for the Kaapvaal Craton, and this is consistent with the heat 537 flow modelling (cf. figure 9-a). Recently (Gard & Hasterok, 2021) have determined the 538 Curie depth globally using satellite magnetic model LCS-1 (Olsen et al., 2017) from 539 spherical harmonic degree 16 to 100 which is corresponding to wavelength of  $\sim 400$ 540 km using the equivalent source magnetic dipole method. They obtain deeper  $z_b$  along 541 the Kheis Belt and the Kalahari magnetic lineament, due to the very long wavelengths 542 dominating the used magnetic data which do not reflect the shorter wavelengths as-543 sociated with the remarkable magnetic signature of the Kheis Belt (cf. Figure 9-b). 544 Perhaps the most striking feature of the  $z_b$  maps in Figure 5 is the sharp transition 545 between shallow (~ 20 km) and erroneous deep (> 50 km)  $z_b$  values which coincides 546 with the thrust Fault separating between Namaqua-Natal Belt and Cape Fold Belt. 547 Recent S-wave tomography and body wave tomography have demonstrated that this 548 thrust faults is a crustal-scale structural feature that defines a major change in the 549 geology (White-Gaynor et al., 2020; Celli et al., 2020). At all  $\beta$  values, the Cape Fold 550 Belt shows high reduced chi-square values and high uncertainties, therefore indicating 551 that the estimated Curie depth in this region cannot be obtained reliably. 552

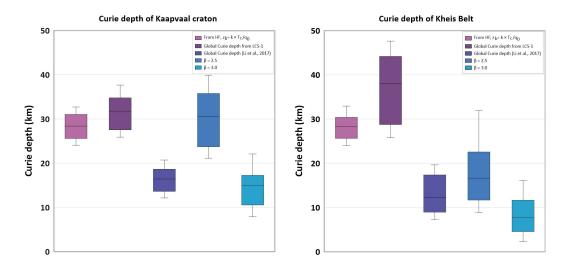


Figure 9. Comparison of estimated Curie depth along (a) Kaapvaal Craton; (b) Kheis Belt from our model using two different  $\beta$  values; global curie depth model (Li et al., 2017); from heat flow measurements, and from global curie depth model by utilising the equivalent source magnetic dipole (Gard & Hasterok, 2021)

#### 5.1 Correlation Between Curie Depth and Heat Flow Measurements

Previous studies have showed that the Curie depths are inversely correlated to the heat flow (Li et al., 2017). We found in (Figure 7) that measured heat flow and the Curie depths estimates seem to be very poorly correlated and in most cases do not match the predictions of the 1-D thermal conductivity model from section 2.2. Locally, however, the situation can be better (e.g., for the Kapvaal Craton as indicated in Figure 8). In the following two subsections, we discuss the 1-D model as well as the model with varying thermal conductivities in some more detail.

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#### 5.1.1 Modelled heat flow from constant thermal conductivities

Figure 10 shows a comparison between heat flow estimated from Curie depth with constant thermal conductivity and heat flow measurements from the most recent compilation Lucazeau (2019).

The estimated heat flow calculated from the global Curie depth model of Li et 565 al. (2017) in the southern Africa displays higher heat flow than our estimates for most 566 study areas (cf. Figure S6). In the Kapvaal Craton, e.g., they suggest an area of high 567 heat flow. The heat flow estimates based on our Curie depth model (with 2 and 2.5  $\beta$ 568 values) (Figure 10-a,b) suggests a zone of relatively low heat flow, in better agreement 569 with the available measurements. This suggests that in spite of the limitations of the 570 method used to calculate the depth to the Curie isotherm, it could be used to provide 571 a lower thermal boundary condition for heat-flow calculations. 572

On the other hand, areas with short-wavelength features – that significantly influence the heat flow field – cannot be resolved adequately. For instance, the Kalahari magnetic lineament at the western part of Kaapvaal Craton is modelled with very high heat flow values and shows large discrepancies to the measured low heat flow values, indicating that the estimated shallow Curie isotherm in this area might have a structural rather than a thermal origin.

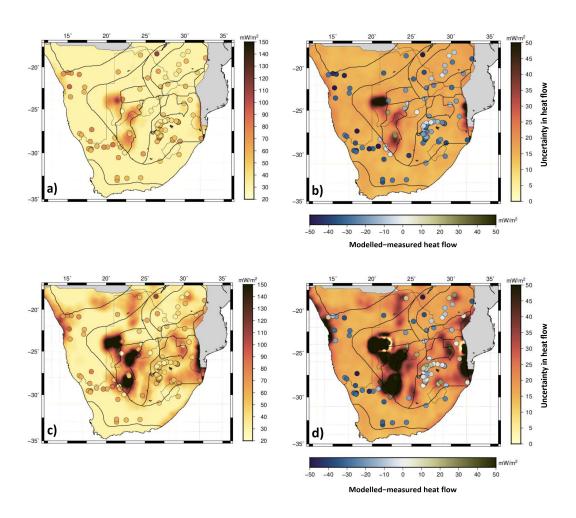


Figure 10. Modelled heat flow using the 1-D heat conductive model with laterally constant thermal conductivity (k= 2.5 W/mK) at the Curie depth estimated when (a)  $\beta = 2.0$ ; (c)  $\beta =$ 2.5 overlain with the locations of the measured heat flow data. Uncertainty of heat flow determined from an ensemble of model simulations for the estimated Curie depth with  $\beta = 2.0$  (b); with  $\beta = 2.5$  (d) overlain with the locations of the difference between modelled and measured heat flow.

# 5.1.2 Modelled heat flow from varying thermal conductivities

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In Figure 11 we indicate the outcome for the heat flow similar to Figure 10, but this time allowing varying conductivities within the Bayesian framework described in section 2.2.1 and Lösing et al. (2020).

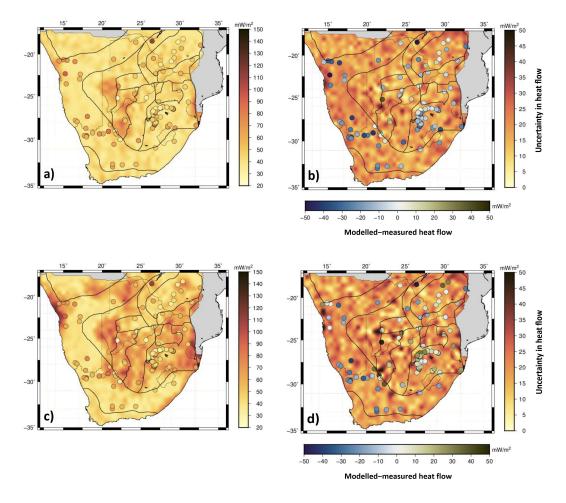


Figure 11. Modelled heat flow in Southern Africa and its uncertainty. Heat flow distribution calculated from the setup in section 2.2.1 and Lösing et al. (2020) for the estimated Curie depth with  $\beta = 2.0$  (a); with  $\beta = 2.5$  (c). Uncertainty of heat flow determined from an ensemble of model simulations for the estimated Curie depth with  $\beta = 2.0$  (b); with  $\beta = 2.5$  (d) overlain with the locations of the difference between modelled and measured heat flow.

The mantle heat flux  $q_D$  (Figure S7) correlates strongly with the LAB depths. A similar pattern is observed for crustal heat production, which correlates with the Moho depth. In addition, there is a strong linear relation between heat production and heat flow, which has been demonstrated empirically in Roy et al. (1968) (for more details, see Figure S7).

<sup>599</sup> Both, heat production and the calculated heat flow (Figure S7) strongly resemble <sup>600</sup> the Curie isotherm (Figure 5-a). In areas of deeper Curie depths down to 40 km the <sup>601</sup> heat flow is between 30 and 40 mW/m<sup>2</sup> with low heat production below 1.0  $\mu$ W/m<sup>2</sup>. <sup>602</sup> In shallower Curie depth regions between 15 and 20 km, the heat flow reaches up to <sup>603</sup> 100 mW/m<sup>2</sup> and exhibits higher heat production rates around 2.5  $\mu$ W/m<sup>2</sup>.

Two Curie depth models (with different  $\beta$  values 2.0 and 2.5) have been tested 604 (Figure 11), with use of a fixed Moho depth and LAB (Figure 4). The Moho depth 605 has an influence on the crustal heat production, i.e., a thin crust is compensated with 606 higher rates of heat production. It is noticeable that the heat flow is most affected by changing the Curie depth and the spatial distribution of the heat flow is mirrored by 608 the Curie isotherm. For example in Cap Fold Belt we observe areas of low heat flow, 609 correlating with unrealistic deep Curie depths. These areas also correspond to higher 610 uncertainties of curie depth estimation and high chi-square values. The remaining 611 inverted thermal parameters (Figure S7) do not show significant differences from  $\beta =$ 612 2.0. The spatial distribution of the modelled heat flow in Figure 11 shows similar 613 patterns in most places as the modeled heat flow presented in Figure 10, although 614 the latter used laterally constant heat production rates with a surface value of  $H_0 =$ 615  $2.5 \ \mu W/m^2$  and constant crustal thermal conductivity of 2.5 W/mK. The two models 616 are greatly comparable and the average residual heat flow between the inversion with 617 variable heat production (Figure 11) and the laterally constant heat production results 618 (Figure 10) is approximately  $\pm 4 \text{ mW/m}^2$ , indicating the strong influence of the Curie 619 isotherm for the heat flow calculation. Along the Kalahari magnetic lineament, the 620 inversion results in Figure 11 show lower heat flow values, resulting from using laterally 621 variable thermal conductivity and heat production values. 622

Both modelled heat flow using the two different approaches (laterally constant or variable heat production) show some degree of agreement compared to the measured heat flow values, however, with large discrepancies in most places. The possible origins of that are shown below:

- The shallow, spatially large magmatic provinces that run parallel to the Kalahari magnetic lineament can cause Curie depths to be underestimated;
- magmatic rocks with a large magnetic field may intrude and cover a less magnetic metamorphic basement and extremely weakly magnetic basin sediments;
- instead of giving a depth to the bottom of the magnetic source, the spectrum approach can give a depth to the bottom of magnetization that corresponds to the base of the dominant unit, i.e. the volcanic rocks, and in this case the thickness of superficial rocks might then be estimated;
- notwithstanding the possibility of other geological restrictions, the assumption
   that the depth to the bottom of the magnetic source is temperature-controlled
   (i.e. it reflects the Curie isotherm).
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# 5.2 Comparison of Crustal Thickness With Curie Depths

Most early studies considered the mantle to be nonmagnetic (Wasilewski et al., 1979; Wasilewski & Mayhew, 1992); however, recent studies (Ferré et al., 2014) argue for the occurrence of a magnetized upper mantle in certain geological contexts. Here we make the approximation that, if the uppermost mantle is magnetized, its susceptibility is likely much lower than that for crustal rocks, and therefore, we consider a maximum Curie depth of 50 km.

A comparison between the crustal thickness and Curie depth is presented in Figure 12. Negative values represent Curie depth values deeper than the Moho and positive values represent areas where the Curie depth is shallower than the Moho. Figure 12-a shows negative values in large areas, meaning the calculated Curie depth is deeper than the gravity inverted Moho depth (cf. Figure 4) for large areas if  $\beta = 2.0$ . If  $\beta = 2.5$ , as indicated in Figure 12-b, the calculated Curie depth is shallower than Moho depth for a fairly large portion of the investigated area.

However, whilst in general the Earth's mantle does not contribute to the magnetic signal (due to its weak magnetization and high temperature conditions), in some

cases the Curie depth may indeed lie within the mantle. This occurs where metallic 654 magnetic phases in the mantle beneath old and tectonically stable crust (Cratons; 655 Ferré et al. (2014) or subduction regions; Blakely et al. (2005)) contribute to mantle 656 magnetization. In these settings the crust-mantle boundary should not be considered 657 an absolute magnetic boundary (Ferré et al., 2014). This implies that if in a given 658 region the Moho depths are shallower than the deepest magnetic layer, a magnetic 659 mantle at temperatures below the Curie temperature may be considered. However, 660 even in these cases the upper mantle susceptibility will be more than 1-2 orders of 661 magnitude smaller than the overlying crust. This is not considered in current spectral 662 methods for Curie depth estimation and any Curie depths below Moho depths are 663 ruled out or interpreted as a structural rather than a thermal source. 664

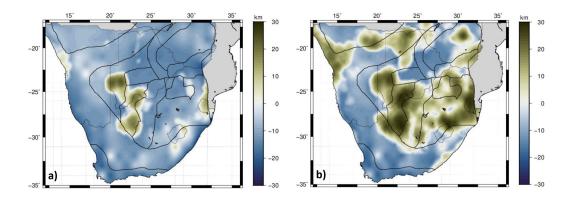


Figure 12. Comparison of Curie depth and depth of the crust-mantle boundary (the Moho depth) derived from gravity inversion with seismic constraints, (a) with  $\beta = 2.0$  and (b) with  $\beta$ = 2.5. Negative values show areas where the estimated Curie depth is deeper than the estimated Moho depth, and positive values are where the Curie depth is shallower than the Moho depth.

Figure 12-a shows that the magnetic bottom extends deeper than the Moho discontinuity, reaching the upper mantle and indicating that the Curie depth results with  $\beta = 2.0$  is not realistic in most places along the study area. Figure 12-b shows in large area that the Curie depth is shallower than the Moho depth and it correlates well with the uncertainty map for Curie depths, assuming  $\beta = 2.5$ . The areas where the Curie depth is deeper than the Moho are associated with high uncertainties in the Curie depth (cf. Figure 5-b).

# 676 6 Conclusions

The study estimates the Curie depth  $z_b$  over southern Africa using wavelet transforms of magnetic data in combination with a Bayesian setup. The sedimentary layer thickness used to constrain  $z_t$  remains fixed in the inversion and we test various values for the fractal parameter  $\beta$ , which very roughly characterizes the structure of the underlying crustal magnetization. The uncertainty in Curie depth estimation is provided along the entire study area, using probabilistic Bayesian inference method and to show the statistical distribution of the model parameters.

We observe correlations of shallow  $z_b$  with the distribution of magmatic rocks at the western boundary of Kaapvaal Craton, which is consistent among different  $\beta$  values, indicating that the modelled  $z_b$  might correspond to the base of highly magnetized young volcanic rocks instated of Curie temperature isotherm. We further used the estimated Curie depth to model surface heat flow, in a setup with assumed constant thermal conductivity as well as with varying thermal conductivities. The modelled heat flow matches heat flow data to a reasonable degree of uncertainty, except in regions where magmatic intrusions are presented (e.g., Kalahari magnetic lineaments). The spectral analysis of magnetic anomaly data may be better suitable to hotter settings, where shallow Curie depth estimates are more robust, and in the oceans, where magnetization is likely to be uniform.

<sup>695</sup> Our results raise a major future directions of improvement. It may be possible to <sup>696</sup> use additional constraints on  $z_b$  by considering available heat flow measurements into <sup>697</sup> the inversion process, which impose physical bounds on the predicted Curie depth via <sup>698</sup> thermal models.

#### 699 Acknowledgments

MS and CG have been partially funded by BMWi (Bundesministerium für Wirtschaft 700 und Energie) within the joint project 'SYSEXPL - Systematische Exploration', grant 701 ref. 03EE4002B. IF have been funded by Nederlandse Organisatie voor Wetenschap-702 pelijk Onderzoek (NWO), grant ALWGO.2019.054. All grid files and maps were cre-703 ated using Generic Mapping Tools (GMT) version 5 (Wessel et al., 2013). The scientific 704 color map was used in this study to prevent visual distortion of the data and exclu-705 sion of readers with color vision deficiencies (Crameri et al., 2020). The aeromagnetic 706 data is available at (http://wdmam.org/) (Lesur et al., 2016). The sediment thick-707 ness model is available at (http://igppweb.ucsd.edu/~gabi/crust1.htm) (Laske et 708 al., 2013). The heat flow data are available at (http://www.heatflow.org/) (Lu-709 cazeau, 2019). The wavelet analysis and Curie depth estimation were performed us-710 ing the open-source software PlateCurie, freely available at (https://github.com/ 711 paudetseis/PlateCurie) (Audet & Gosselin, 2019). Tectonic ages of the southern 712 Africa used with the permission of OneGeology (http://portal.onegeology.org/ 713 **OnegeologyGlobal**/). The resulting Curie depth and it is uncertainties and the mod-714 elled heat flow can be found at (https://doi.org/10.5281/zenodo.5070470). All 715 the used data and the modeling software are cited within the manuscript and listed in 716 the references. 717

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# Supporting Information for "Mapping the thermal structure of southern Africa from Curie depth estimates based on wavelet analysis of magnetic data with uncertainties"

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Contents of this file

1. Figures S1 to S7

July 13, 2021, 1:10pm



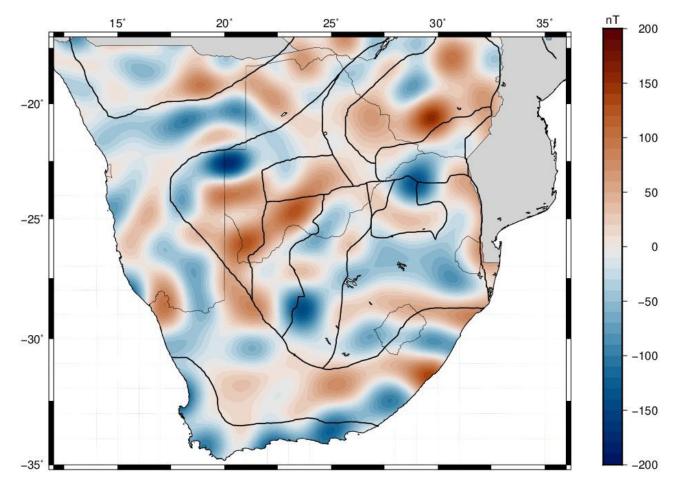
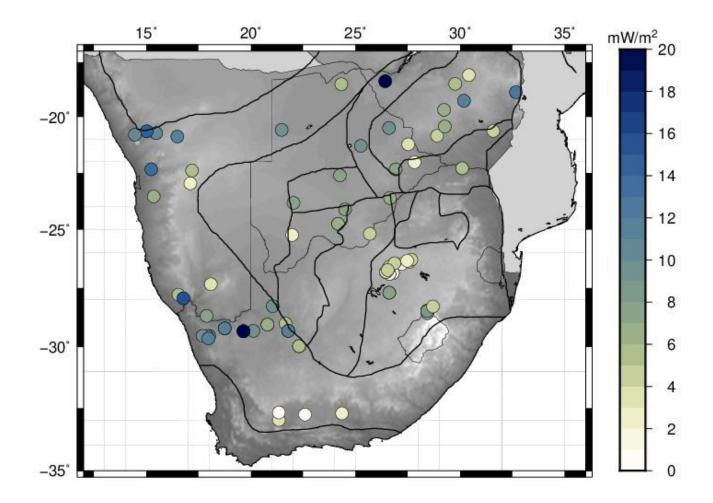


Figure S1. Lithospheric magnetic anomaly of Southern Africa derived from Satellite model LCS-1 (Olsen et al., 2017)

# July 13, 2021, 1:10pm



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Figure S2. Uncertainty for the measured heat flow data (Lucazeau, 2019).

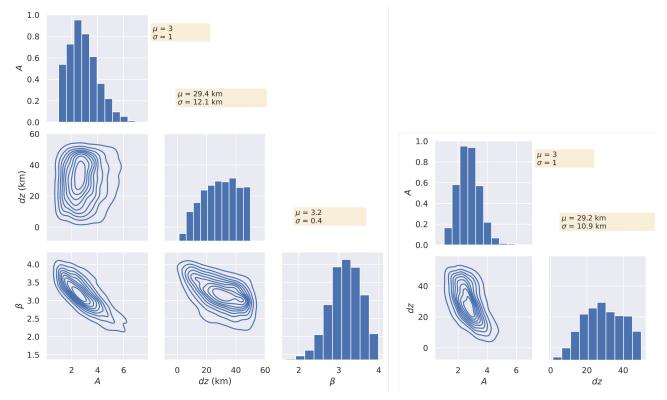


Figure S3. Statistical distribution of model parameters from at location B of Figure 5-a: marginalized and joint posterior distribution from the simultaneous inversion for the parameters  $z_b$ ,  $\beta$ , and A (right panel) and for the simultaneous inversion for  $z_b$  and A, with fixed  $\beta = 3.0$ (left panel). Statistical information on each  $z_b$ ,  $\beta$ , A is provided in the orange boxes;  $\mu$  is the mean value,  $\sigma$  is the standard deviation. Note that the parameter dz in the above plots indicates  $\Delta z$  in our notation, so that  $z_b = z_t + dz$ .

July 13, 2021, 1:10pm





<sup>z</sup>ρ 20

0

2 5 0 40 60 1 3 10 20 10.0 12.5 0 40 5.0 7.5 20 dz (km) β Α dz A Figure S4. Statistical distribution of model parameters from at location C of Figure 5-a: marginalized and joint posterior distribution from the simultaneous inversion for the parameters  $z_b$ ,  $\beta$ , and A (right panel) and for the simultaneous inversion for  $z_b$  and A, with fixed  $\beta = 3.0$ (left panel). Statistical information on each  $z_b$ ,  $\beta$ , A is provided in the orange boxes;  $\mu$  is the mean value,  $\sigma$  is the standard deviation. Note that the parameter dz in the above plots indicates  $\Delta z$  in our notation, so that  $z_b = z_t + dz$ .

July 13, 2021, 1:10pm

1.0

0.8 0.6 0.4

> 0.2 0.0 60

40 (ma) *zp* 

0

4

3

1

<del>م</del> 2

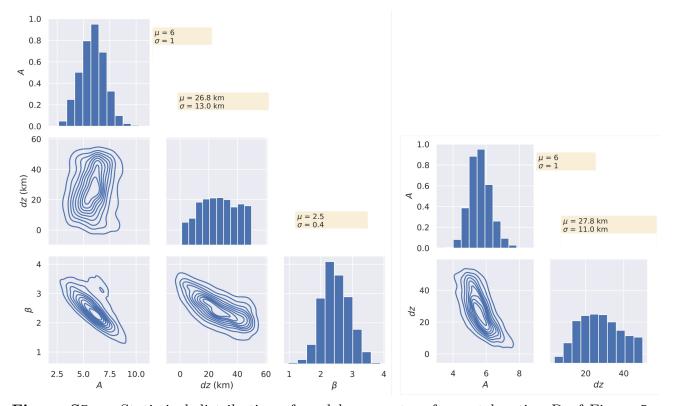
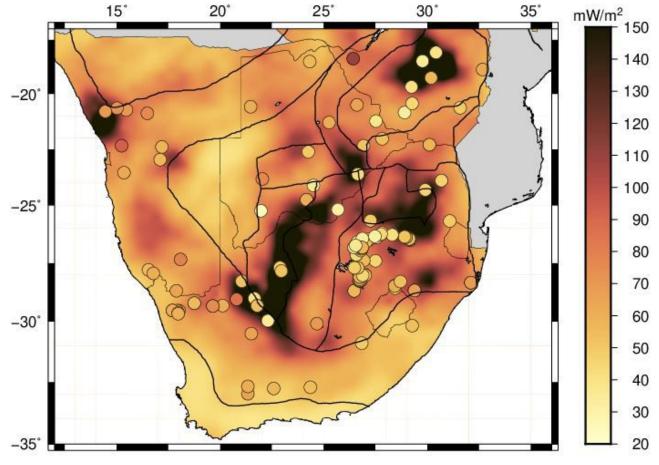


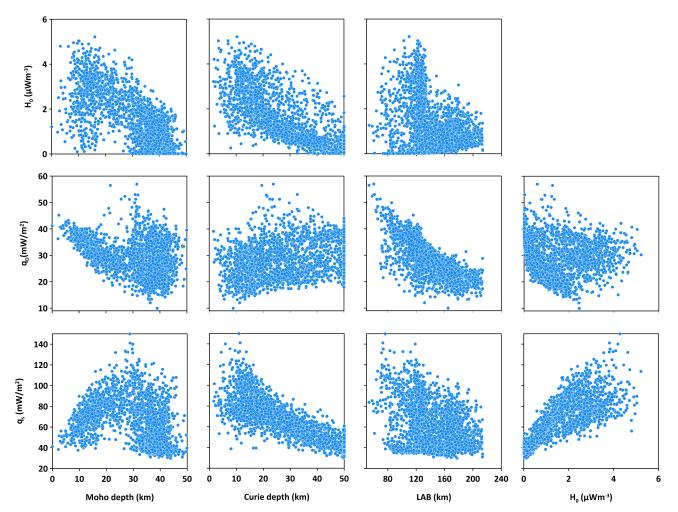
Figure S5. Statistical distribution of model parameters from at location D of Figure 5-a: marginalized and joint posterior distribution from the simultaneous inversion for the parameters  $z_b$ ,  $\beta$ , and A (right panel) and for the simultaneous inversion for  $z_b$  and A, with fixed  $\beta = 3.0$ (left panel). Statistical information on each  $z_b$ ,  $\beta$ , A is provided in the orange boxes;  $\mu$  is the mean value,  $\sigma$  is the standard deviation. Note that the parameter dz in the above plots indicates  $\Delta z$  in our notation, so that  $z_b = z_t + dz$ .

July 13, 2021, 1:10pm



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Figure S6. Heat flow distribution calculated from the global Curie depth model proposed by (Li et al., 2017) using laterally constant thermal conductivity (k= 2.5 W/mK) overlain with the locations of the measured heat flow data.



**Figure S7.** Correlations between different input and output parameters resulting from the heat flow modelling for a setup with varying thermal conductivities (cf. section 5.1.2 in the main text and (Lösing et al., 2020)) as a scatter plot. The figure shows a correlation between Curie depth with heat flow and heat production. LAB is correlated with mantle heat flux, and a linear correlation between heat flow and heat production is revealed.

July 13, 2021, 1:10pm

Li, C., Lu, Y., & Wang, J. (2017). A global reference model of curie-point depths based on EMAG2. *Sci. Rep.*, 7, 45129.

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- Lösing, M., Ebbing, J., & Szwillus, W. (2020). Geothermal heat flux in antarctica: assessing models and observations by bayesian inversion. Frontiers in Earth Science, 8, 105.
- Lucazeau, F. (2019). Analysis and mapping of an updated terrestrial heat flow data set. Geochemistry, Geophysics, Geosystems, 20(8), 4001-4024. doi: 10.1029/2019GC008389
- Olsen, N., Ravat, D., Finlay, C. C., & Kother, L. K. (2017). Lcs-1: a high-resolution global model of the lithospheric magnetic field derived from champ and swarm satellite observations. *Geophysical Journal International*, 211(3), 1461–1477.

July 13, 2021, 1:10pm