

A new divergence method to quantify methane emissions using observations of Sentinel-5P TROPOMI

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Abstract

Key points: * A new divergence method is developed to estimate methane emissions based on satellite observations, requiring no a priori emissions. * The applicability of this method in identifying and quantifying sources is proven by a GEOS-Chem simulation with known a priori emissions. * The estimated emissions over Texas (United States) based on TROPOMI observations are evaluated and are found to be robust. Abstract We present a new divergence method to estimate methane (CH₄) emissions from satellite observed mean mixing ratio of methane (XCH₄) by deriving the regional enhancement of XCH₄ in the Planetary Boundary Layer (PBL). The applicability is proven by comparing the estimated emissions with its a priori emission inventory from a 3-month GEOS-Chem simulation. When applied to TROPOMI observations, sources from well-known oil/gas production areas, livestock farms and wetlands in Texas become clearly visible in the emission maps. The calculated yearly averaged total CH₄ emission over the Permian Basin is 3.06 [2.82, 3.78] Tg a⁻¹ for 2019, which is consistent with previous studies and double that of EDGAR v4.3.2 for 2012. Sensitivity tests on PBL heights, on the derived regional background and on wind speeds suggest our divergence method is quite robust. It is also a fast and simple method to estimate the CH₄ emissions globally. Plain Language Summary Methane (CH₄) is an important greenhouse gas in the atmosphere and plays a crucial role in the global climate change. It kept increasing over the last decades. About 70% of CH₄ comes from human activities like oil/gas productions or livestock farms. The recently launched TROPOMI provides an opportunity to estimate the emissions of CH₄ on a regional scale. This work presents a new method to fastly derive CH₄ emissions at a fairly high spatial resolution without a priori knowledge of sources.

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19 satellite observations, requiring no a priori emissions.
- 20 • The applicability of this method in identifying and quantifying sources is proven
21 by a GEOS-Chem simulation with known a priori emissions.
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24 **Abstract**

25 We present a new divergence method to estimated methane (CH₄) emissions from
26 satellite observed mean mixing ratio of methane (XCH₄) by deriving the regional

27 enhancement of XCH₄ in the Planetary Boundary Layer (PBL). The applicability is
28 proven by comparing the estimated emissions with its a priori emission inventory from
29 a 3-month GEOS-Chem simulation. When applied to TROPOspheric Monitoring
30 Instrument (TROPOMI) observations, sources from well-known oil/gas production
31 areas, livestock farms and wetlands in Texas become clearly visible in the emission
32 maps. The calculated yearly averaged total CH₄ emission over the Permian Basin is
33 3.06 [2.82, 3.78] Tg a⁻¹ for 2019, which is consistent with previous studies and double
34 that of EDGAR v4.3.2 for 2012. Sensitivity tests on PBL heights, on the derived
35 regional background and on wind speeds suggest our divergence method is quite robust.
36 It is also a fast and simple method to estimate the CH₄ emissions globally.

37 **Plain Language Summary**

38 Methane (CH₄) is an important greenhouse gas in the atmosphere and plays a crucial
39 role in the global climate change. It kept increasing over the last decades. About 70%
40 of CH₄ comes from human activities like oil/gas productions or livestock farms. The
41 recently launched TROPOspheric Monitoring Instrument (TROPOMI) provides an
42 opportunity to estimate the emissions of CH₄ on a regional scale. This work presents a
43 new method to fastly derive CH₄ emissions at a fairly high spatial resolution without a
44 priori knowledge of sources.

45 **1 Introduction**

46 Methane (CH₄) is the second most important anthropogenic greenhouse gas after
47 carbon dioxide (CO₂) and is also a principal precursor of tropospheric ozone [*Shindell*
48 *et al.*, 2012]. In-situ measurements show a continuous increase of methane over the last
49 decades [*Dlugokencky et al.*, 2009; *IPCC*, 2013; *Saunio et al.*, 2016; *Turner et al.*,
50 2019], with stable concentrations from 2000 to 2006 [*Dlugokencky et al.*, 2009; *Rigby*
51 *et al.*, 2008]. CH₄ has both natural (e.g., wetlands, wildfires, termites) and
52 anthropogenic (e.g., fossil fuels, livestock, landfills and wastewater treatments) sources.
53 About 360 million tons (60 % of the total CH₄) are released through human activities
54 [*Saunio et al.*, 2020]. The relatively short lifetime of CH₄ (about a decade) makes it a
55 short-term target for mitigating climate change by reducing the emissions.

56 Satellite observations of CH₄ provide an efficient way to analysis its variations and
57 emissions at a regional to global scale [*Buchwitz et al.*, 2017; *Lunt et al.*, 2019; *J. D.*
58 *Maasackers et al.*, 2019; *Miller et al.*, 2019; *Zhang et al.*, 2020]. Compared to previous
59 widely used instruments like Greenhouse gases Observing SATellite (GOSAT) and
60 SCanning Imaging Absorption spectroMeter for Atmospheric Cartography
61 (SCIAMACHY, onboard Envisat), the TROPOspheric Monitoring Instrument

62 (TROPOMI) on board the Sentinel 5 Precursor (S5-P) satellite measures CH₄ at an
63 unprecedented resolution of $7 \times 7 \text{ km}^2$ since its launch in October 2017 (upgraded to
64 $5.5 \times 7 \text{ km}^2$ in August 2019) [Veefkind *et al.*, 2012]. Several studies have shown the
65 capability of TROPOMI on identifying and quantifying the sources at a local to regional
66 scale (e.g., [de Gouw *et al.*, 2020; Pandey *et al.*, 2019; Schneider *et al.*, 2020; Zhang *et*
67 *al.*, 2020]). These studies mainly focused on oil/gas leakage events, which show strong
68 signals that can be easily identified, or they are using an inverse modeling relying on
69 an a-priori emission inventory.

70 Freshly emitted air pollutants are usually concentrated around the emission source, in
71 the case of not too high wind speeds [Liu *et al.*, 2020]. Beirle *et al.* [2019] found that
72 the strong gradients near sources of nitrogen oxides (NO_x) are preserved by averaging
73 horizontal fluxes. Therefore, the divergence of horizontal fluxes of nitrogen dioxide
74 (NO₂) plus a sink term can be used to estimate the emissions of NO₂. In our study, we
75 apply a divergence method for deriving CH₄ emissions. The sink term can be ignored
76 for CH₄ because of its relatively long lifetime, which makes it more straightforward to
77 link the divergence to the emission. The divergence works on the product of horizontal
78 fluxes and wind fields, which is independent of a priori emission inventories and
79 models and can be applied at various resolutions regionally or globally.

80 The retrieved CH₄ from satellite observations are the ratios of methane total vertical
81 columns to air density columns (XCH₄), which are strongly affected by the
82 stratospheric abundance. Thus the influence of transportation in the upper atmosphere
83 and of orography should be removed to better distinguish gradients due to emissions.
84 XCH₄ measured by satellites reflects the abundance of the background plus the newly
85 emitted methane because of its around 10-year lifetime. Hence the contribution from
86 the background should be deducted when estimating the emissions.

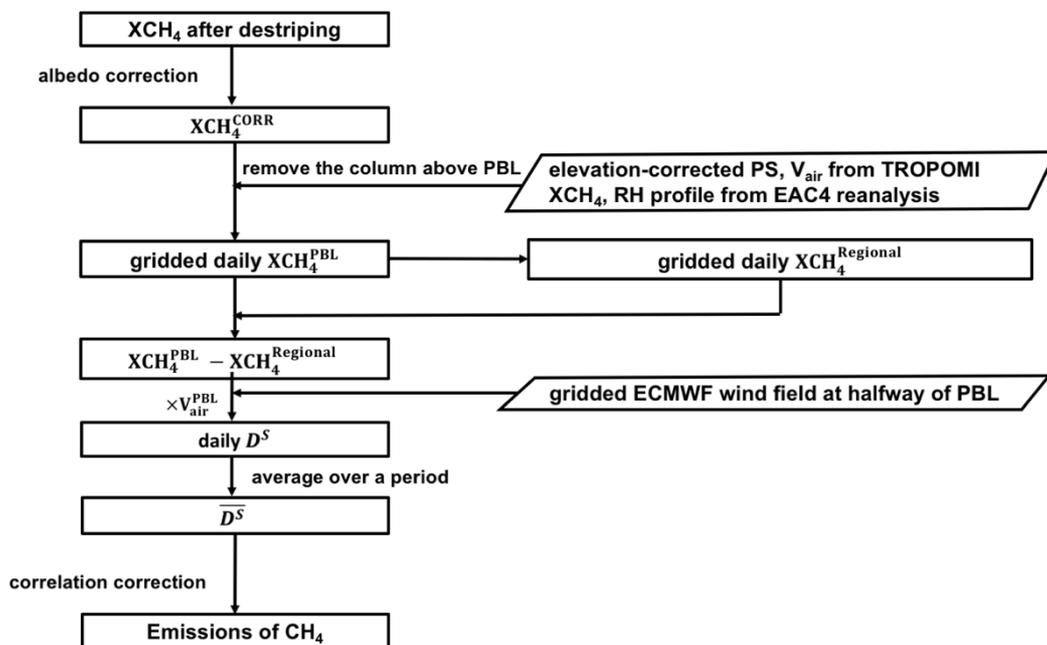
87 In this study, we present a new divergence method to quantify the emission of CH₄ from
88 satellite retrieved XCH₄. The XCH₄ of TROPOMI is first destriped and corrected with
89 albedos at short-wave infrared (SWIR) wavelengths (2305–2385 nm) to improve the
90 data quality. Before applying the method to TROPOMI observations, a 3-month (from
91 July 2012 to September 2012) hourly GEOS-Chem nested model simulation over North
92 America is used to test the applicability of our method. The data quality of the resulting
93 emissions is further analyzed with sensitivity studies and comparisons to the literature.

94 **2 Method and Data**

95 Figure 1 shows the flowchart of the procedure to estimate the CH₄ emissions from
96 TROPOMI retrieved XCH₄. It consists of three main steps. First, applying posteriori
97 corrections on XCH₄ to reduce the systematic biases caused by across-track biases and
98 surface albedos. Second, the mean mixing ratios of CH₄ in the PBL (XCH₄^{PBL}) and the
99 corresponding regional backgrounds are derived by subtracting the columns above the

100 PBL, which are estimated by XCH_4 profiles from the Atmospheric Composition
 101 Reanalysis 4 (EAC4) of the Copernicus Atmosphere Monitoring Service (CAMS)
 102 [*Inness et al.*, 2019]. The enhancements of XCH_4^{PBL} are further used to calculate the
 103 spatial divergence and estimate CH_4 emissions.

104



105 Figure 1. The flow chart of using TROPOMI XCH_4 to derive the CH_4 emissions over
 106 a certain period. PS and V_{air} stand for the surface pressure and the total column of air
 107 density used in TROPOMI XCH_4 retrieval. RH is the relative humidity.

108 2.1 Estimate methane emission from TROPOMI

109 There are two additive corrections, the stripe correction and the albedo correction, on
 110 XCH₄ to remove biases caused by the satellite retrieval. The detailed method can be
 111 found in Part A and B of Supplementary Information (SI).

112 The continuity equation connecting the divergence (D), emission (E) and sink (S) for
 113 steady state is: $D = E + S$ [Beirle et al., 2019]. As the lifetime of CH₄ is around 10 years,
 114 the sink term can be ignored, that is: $D = E$. The divergence D works on horizontal
 115 fluxes (F): $D = \nabla F$, where F stands for zonal (F_u) and meridional fluxes (F_v), which
 116 is the product of gridded vertical columns (V) and horizontal wind fields (\vec{w}). For each
 117 day d :

118
$$E_d = \nabla F_d = \nabla(V \cdot \vec{w}) \quad (1)$$

119 Numerical derivatives for D are calculated as the second-order central difference in this
 120 study. We convert XCH₄ to mean mixing ratio in the PBL, XCH₄^{PBL} (denoted by X^{PBL}),
 121 to eliminate the effects of orography and transport in upper atmosphere. The column of
 122 methane in the PBL (V^{PBL}) for day d is derived by:

123
$$V_d^{PBL} = X_d^{PBL} \times A_d^{PBL} \quad (2)$$

124 where A_d^{PBL} is the corresponding air density column in the PBL. Considering the
 125 relatively long lifetime of methane, D in the PBL actually contains the variations of its
 126 background and sources. As D is a linear operator, the daily D_d of the fluxes in the
 127 PBL can be written as:

128
$$D_d = D_d^B + D_d^S \quad (3)$$

129 where D^B is the daily divergence of the background flux and D^S is the daily
 130 divergence caused by sources in PBL, respectively. Combining with Eq. (1) and (2), Eq.
 131 (3) can be written as:

132
$$D_d^S = \nabla((X_d^{PBL} - X_d^B) \times A_d^{PBL} \cdot \vec{w}) \quad (4)$$

133 where X_d^B is the background of X_d^{PBL} . It is hard to know the exact X_d^B , so we use the
 134 regional background (X_d^R) to approximate the X_d^B as will be stated in Sect. 2.2. Eq. (4)
 135 is then written as:

136
$$D_d^S = \nabla((X_d^{PBL} - X_d^R) \times A_d^{PBL} \cdot \vec{w}) \quad (5)$$

137 Equation (5) is applied to the daily variations of CH₄, and the emission is estimated by
138 averaging $\overline{D_d^S}$ over a time period:

$$139 \quad E_d = \overline{D_d^S} = \overline{D_d} - \overline{D_d^R} \quad (6)$$

140 where D^R stands for the averaged divergence of the regional background. However,
141 we found a significant correlation between $\overline{D^S}$ and $\overline{D^R}$ at some locations, which
142 suggest that the derived emissions still contain part of the background. Strong spatial
143 positive correlations R are typically found over areas with complicated terrain where
144 the background is less homogenous.

145 To remove the remaining background, we apply a two-step posteriori correction. First
146 of all, E is multiplied by the empirical “correlation correction factor” (1-R) to reduce
147 the biases caused by regional background.

148 In addition, we find that areas with negative emissions E also have negative $\overline{D^R}$ and
149 divergence of winds ($\overline{D^w}$), implying no significant sources. Thus, secondly, the grids
150 with negative E are set to be zero in the final estimated emissions. The practice of this
151 posteriori correction is presented in Sect. 3.

152 2.2 Calculating the regional enhancement of methane in PBL

153 The entire atmospheric column was divided into only 12 layers in the TROPOMI XCH₄
154 retrieval, which is too coarse to resolve the vertical distribution. To estimate the
155 methane column above the PBL we use model results of EAC4 of CAMS
156 ([https://ads.atmosphere.copernicus.eu/cdsapp#!/dataset/cams-global-reanalysis-](https://ads.atmosphere.copernicus.eu/cdsapp#!/dataset/cams-global-reanalysis-eac4?tab=overview)
157 [eac4?tab=overview](https://ads.atmosphere.copernicus.eu/cdsapp#!/dataset/cams-global-reanalysis-eac4?tab=overview)). It is a global hourly reanalysis of atmospheric composition at a
158 relative high spatial resolution, 0.75° horizontally and 60 layers vertically [Inness *et al.*,
159 2019], which contains no a priori CH₄ emissions. Thus, the spatial distribution of CH₄
160 is solely the result of transport and orography, which will be subtracted from TROPOMI
161 observations to estimate the PBL concentration of CH₄.

162 The surface pressure of each pixel is adjusted by a high-resolution GMTED2010 Digital
163 Elevation map [Hasekamp *et al.*, 2019], and the pressure at each layer of the EAC4
164 XCH₄ profile is recalculated accordingly. The number of dry air molecules in the entire
165 column of the XCH₄ profile is scaled to the total number that is used for the retrieval
166 of the pixel. We do not interpolate the averaging kernel (AK) to the layers of EAC4,
167 because the AK is approximately equal to 1.0 at each layer [Hasekamp *et al.*, 2019]. In
168 this way, we ensure the conservation of air mass for each pixel as well as the high-
169 resolution vertical distributions of methane.

170 Considering the height of the planetary boundary layer (PBLH) from reanalysis or
171 forecast dataset has large uncertainties and is occasionally too shallow, we fixed the
172 PBLH at 500 meters above the ground. XCH_4^{PBL} is obtained by subtracting the column
173 above 500 meters from the ground and dividing the remainder by the corresponding dry
174 air density column. The XCH_4^{PBL} of each pixel is then used to build the daily gridded
175 data at a resolution of 0.25° . In this study, for each grid, daily regional background of
176 XCH_4^{PBL} (XCH_4^R) is defined as the average of the lower 10 percentile of its surrounding
177 ± 5 grid cells ($11 \times 11 = 121$ grid cells in total by taking the current grid cell as the center).
178 The difference between XCH_4^{PBL} and XCH_4^R (Eq. (5)) is finally used to calculate the
179 divergence with wind speeds. Therefore, the system biases between EAC4 and
180 TROPOMI is implicitly removed by subtracting XCH_4^R from XCH_4^{PBL} .

181 The wind field halfway the PBLH close to the overpass time is obtained from the
182 ECMWF. The divergence method works only when transport takes place, i.e. there is
183 at least some wind. In addition, extremely high wind speeds are not favorable for the
184 method that is based on the regional mass balance. Therefore, wind speeds are
185 constrained between 1 m/s to 10 m/s in this study.

186 2.3 Using a GEOS-Chem simulation to test the method

187 In order to evaluate the feasibility of our method, the case of a model simulated XCH_4
188 is suitable because of known a priori emissions. In this study, we perform a 3-month
189 simulation starting from 1 July 2012 by the GEOS-Chem 12.5.0 (<http://geos-chem.org>)
190 nested model over North America at a resolution of 0.5° lat. \times 0.625° lon. with 47
191 vertical layers extending to the mesosphere. The boundary conditions are provided by
192 GEOS-Chem global simulation at 4° lat. \times 5° lon. using posterior methane emissions
193 and OH levels inverted from GOSAT satellite observations [Lu *et al.*, 2021], and
194 therefore these boundary conditions are unbiased to GOSAT observations outside the
195 domain. Both models are driven by MERRA-2 reanalysis meteorological fields from
196 the NASA Global Modeling and Assimilation Office (GMAO) [Gelaro *et al.*, 2017].
197 The a priori natural emissions include wetlands, open fires, termites and seeps. The
198 anthropogenic emissions are from EDGAR v4.3.2, with fugitive fuel emissions (oil,
199 gas, coal) overwritten by the Scarpelli *et al.* [2020] inventory, and further superseded
200 by the gridded version of Inventory of U.S. Greenhouse Gas Emissions and Sinks from
201 the Environmental Protection Agency (EPA GHGI) over the US [Maasakkers *et al.*,
202 2016]. More information on the model setup can be found in [Lu *et al.*, 2021]. Here we
203 take the results at UTC 18:00, which is close to the overpass time of TROPOMI over
204 the US. We apply our method to these simulations of XCH_4 in the PBL. The XCH_4^{PBL}
205 is the mixing ratio of the column in PBL at the same time. The method to build regional
206 background for each grid follows Sect. 2.2.

207 **3 Results**

208 *3.1 Verification of the method using GEOS-Chem simulations*

209 Figure 2(a-c) shows the spatial distribution of the 3-month average of a priori emissions
210 used in GEOS-Chem simulation, the divergence of XCH₄ enhancement in PBL and the
211 estimated emission. Although the horizontal resolution of the model is much coarser
212 than TROPOMI observations, the sources have been identified (Fig. 2(b)-(c)), even for
213 relatively small emissions less than 2.5 kg/km²/h. For the mountainous and coastal areas
214 that are more complex than typical flat land terrain, the performance of the divergence
215 works fairly well. Some fake signals caused by orography (e.g., in Mexico, convergence
216 over oceans near the coastal) are successfully removed by the posteriori “correlation
217 correction”. The influence from the remaining background is mostly found over the
218 grid cells with R greater than 0.7.

219 We further quantitatively compare the estimated emissions with the a priori emission
220 inventory. The grid cells with emissions > 0 in the a priori inventory have been selected
221 as the reference. The scatter plots in Fig. 2(d) and (e) compare a priori emissions greater
222 than zero and greater than 4 kg/km²/h with their counterparts respectively. Our
223 estimated emissions capture the spatial variability in a priori emissions throughout the
224 full range of emissions ($R^2 = 0.63$). The Reduced Major Axis (RMA) regression shows
225 a slope of 0.87 and an intercept of -0.08 , highly implying the capability of our method
226 in retrieving model emissions using simulated columns. The biases are mainly related
227 to the simplified regional background we used. The big sources (a priori emission
228 greater than 4 kg/km²/h) are much easier to capture by our method ($R^2 = 0.78$, $R = 0.88$).
229 The final result shows the simple regional background removal is simplified but
230 efficient.

231 We also test our method by using the enhancement in the troposphere instead of the
232 PBL (Fig. S5). The estimated emissions show a much weaker correlation with a priori
233 emissions, especially over the areas with complicated orography. The transport in the
234 upper troposphere are intervening with the emission estimates. Therefore, using the
235 enhancement of XCH₄ in the PBL is more suitable to identify and quantify the
236 emissions.

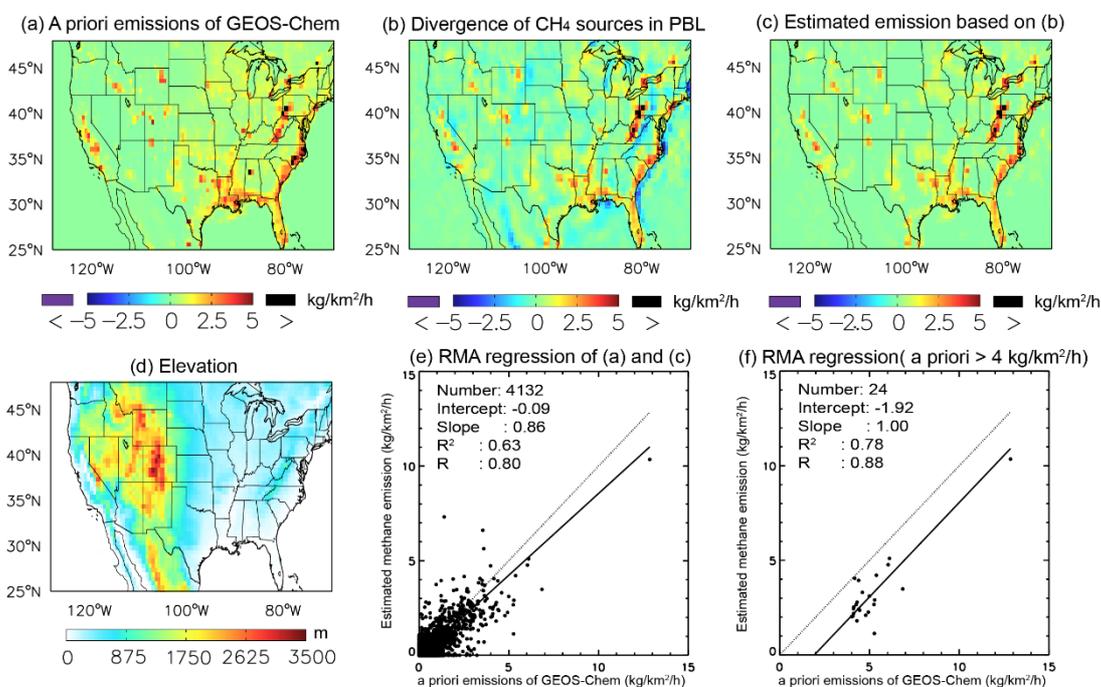
237 *3.2 CH₄ emissions over the US based on TROPOMI*

238 Figure 3(a) presents the spatial distributions of TROPOMI yearly-averaged XCH₄ after
239 destriping and SWIR surface albedo corrections over North America on a 0.25° grid in
240 2019. After converting XCH₄ to XCH₄^{PBL}, the spatial distribution of CH₄ becomes more
241 continuous over mountains in Fig. 3(b). Despite the uncertainty from surface albedo
242 corrections (see more detailed discussion in Part B of SI), enhancements of CH₄ are

243 found over Texas, California and Appalachia regions when comparing to the regional
 244 background (Fig. 3(c)).

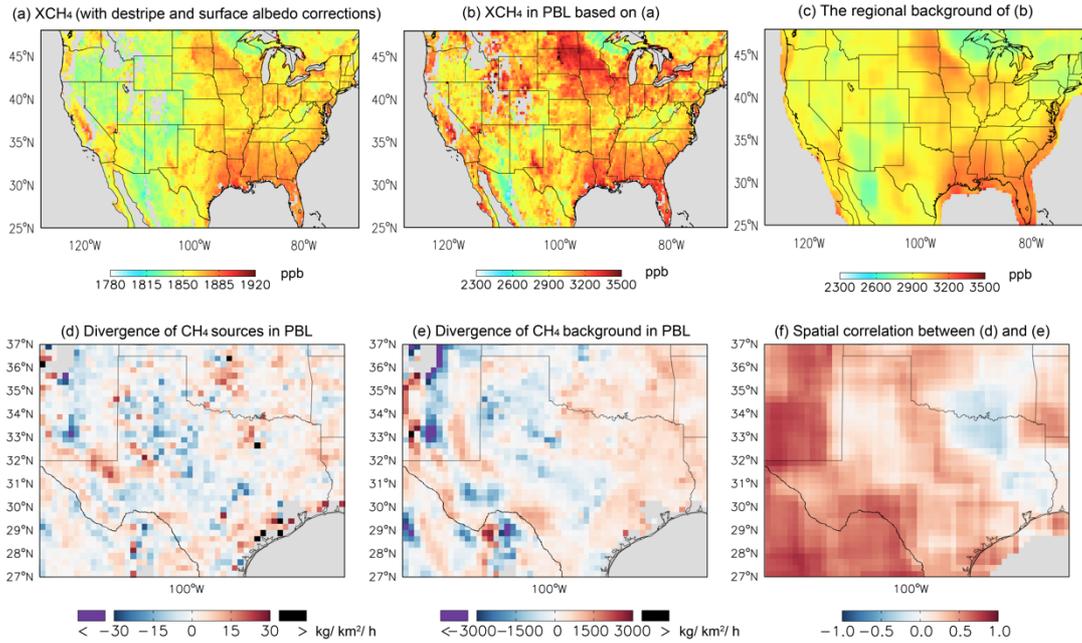
245 Figures 3(d)-(e) show examples of the divergence of sources and of corresponding
 246 regional backgrounds in the PBL over the Texas area, one of the most prolific
 247 petroleum- and gas-producing regions in the U.S., and Fig. 3(f) shows their spatial
 248 correlation. The areas with negative values (convergence) in Fig. 3(d) are also negative
 249 in Fig. 3(e), demonstrating there are no significant sources. In addition, high positive
 250 spatial correlations mainly appear over the areas with complicated orography but few
 251 emissions. On the contrary, the areas with big sources have weak or negative spatial
 252 correlations between sources and regional backgrounds (Fig. 3(f)). Here we apply the
 253 “correlation correction” for grids with R greater than 0.0 to reduce the biases of the
 254 regional background we built.

255



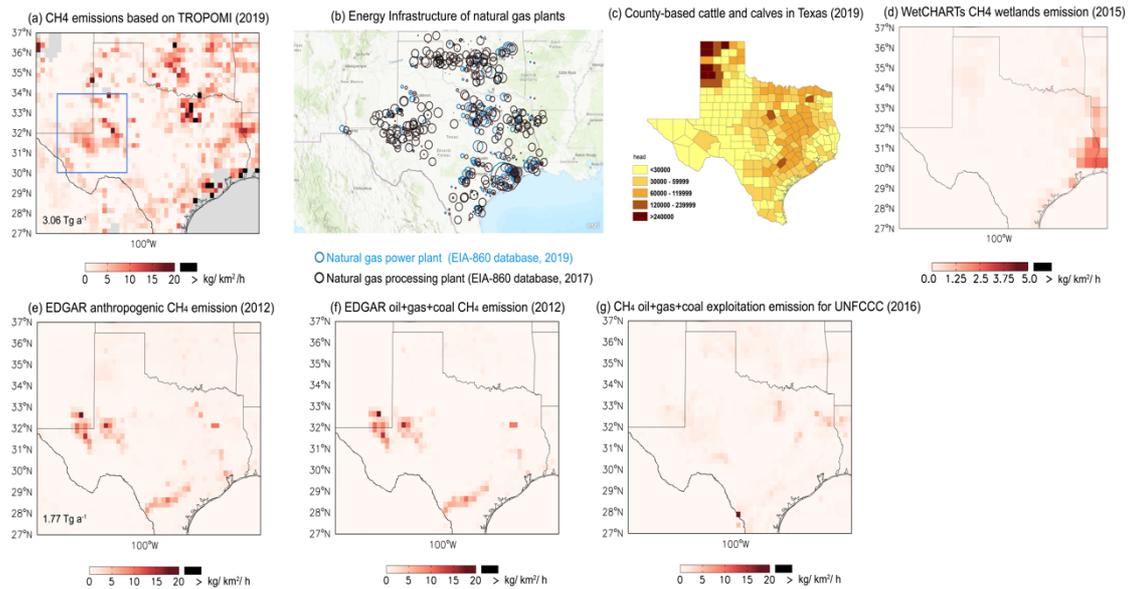
256

257 Figure 2. The spatial distributions of (a) the average of a priori CH₄ emissions used in
 258 GEOS-Chem simulation, (b) the divergence of CH₄ sources in PBL, and (c)
 259 corresponding estimated CH₄ emissions over June-August 2012 on a 0.625° lon. ×
 260 0.5° lat. grid. (d) The elevation map that is generated from GMTED2010 data set. (e)
 261 Scatter plots for emissions between a priori emissions higher than 0.0 kg/km²/h and
 262 estimated CH₄ emissions. (f) As (e) but for a priori emissions that are higher than 4.0
 263 kg/km²/h. Each dot in (e) and (f) represents a grid cell.



264

265 Figure 3. Spatial distributions of yearly averaged (a) XCH₄ with the stripe and surface
 266 albedo corrections, (b) the corresponding XCH₄ in PBL and (c) its regional background.
 267 The divergences of (d) CH₄ sources in PBL and (e) of the regional background in 2019.
 268 (f) The spatial correlation between (d) and (e). For each grid cell, the correlation is
 269 calculated in a domain of 11×11 grid cells, taking the grid cell as center.



270 Figure 4. CH₄ emissions over the Texas area. (a) Our estimated emissions for 2019. (b)
 271 Natural gas power plants (blue circles) and processing plants (black circles) in Texas
 272 (available at: https://www.eia.gov/special/gulf_of_mexico/). The size of each circle
 273 represents the capacity of the plant. (c) County-based heads of cattle and calves in Texas
 274 in 2019 (available at:
 275 [https://www.nass.usda.gov/Statistics_by_State/Texas/Publications/County_Estimates/
 276 ce_maps/ce_catt.php](https://www.nass.usda.gov/Statistics_by_State/Texas/Publications/County_Estimates/ce_maps/ce_catt.php)) (c) EDGAR v4.3.2 for the total anthropogenic emissions in 2012
 277 (available at: https://edgar.jrc.ec.europa.eu/overview.php?v=432_GHG), (d)
 278 WeCHARTs wetland emissions for 2015 [*Bloom et al.*, 2017], (e) EDGAR v4.3.2
 279 anthropogenic CH₄ total emissions for 2012. (f) EDGAR v4.3.2 CH₄ oil+gas+coal
 280 emissions in 2012, and (g) a global inventory of methane emissions from oil, gas, and
 281 coal exploitation that spatially allocates the national emissions reported to the
 282 UNFCCC for 2016 [*Scarpelli et al.*, 2020]. The area enclosed by the solid blue line is
 283 the Permian Basin (30°-34°N, 101°-105°W). The annual total emissions of CH₄ based
 284 on our estimates and EDGAR v4.3.2 over the Permian Basin are embedded in the left
 285 corner of (a) and (e).

286 Our method not only successfully identified the sources in abovementioned well-
287 known oil/gas fields, but also shows the ability to capture the sources from other sectors
288 such as livestock and wetlands. For example, the high CH₄ emissions north of the
289 Permian Bas in Fig. 4(a) are very likely coming from a large number of cattle farms
290 there (Fig 4(b)). Dairy farms or feed yards in this region are typically open lot, and
291 sources of CH₄ are enteric emissions from cattle and emissions of wastewater lagoons.
292 The emission rate of cattle is estimated to be on average 0.211 kg/head/day [Todd *et al.*,
293 2011]. These biogenic emissions do not exist in oil/gas/coal emissions in Fig. 4(f)-(g)
294 but can be found as small contributions to EDGAR v4.3.2 total emissions (Fig. 4(e)).

295 TROPOMI CH₄ retrievals are not available over water, which inevitably leads to
296 uncertainties and limited number of observations near coasts, lakes and bays. However,
297 the natural gas power/processing plants onshore Texas near western Gulf of Mexico
298 (Fig. 4(b)), which shows the energy infrastructures of U.S Energy Information
299 Administration [EIA], are found near the locations of sources shown in Fig. 4(b). It
300 implies that emissions relating to oil/gas productions in the coastal are caught by our
301 divergence method.

302 We further quantify the annual average CH₄ emissions over the Permian Basin
303 (enclosed by the solid blue boundary in Fig. 4(a)). Our estimated emissions in 2019
304 (see baseline settings in Table S1) is 3.06 Tg a⁻¹, which is 42% higher than EDGAR
305 v4.3.2 total anthropogenic emissions in 2012 (1.77 Tg a⁻¹), which can be due to an
306 increase in oil production between 2012 and 2019. Zhang *et al.* [2020] estimated the
307 total emission as 2.9±0.5 Tg a⁻¹ based on the S5P operational TROPOMI CH₄ product
308 [Hasekamp *et al.*, 2019; Landgraf *et al.*, 2019] from May 2018 to March 2019 by using
309 inverse modeling with a priori emissions. The average annual emissions for the time
310 period 2018/2019 based on the TROPOMI/WFMD v1.2 [Schneising *et al.*, 2019]
311 product is reported as 3.18±1.13 Tg a⁻¹ by Schneising *et al.* [2020] using a mass balance
312 method.

313 In addition to testing different surface albedo corrections (see Part B in SI), we designed
314 several other sensitivity tests to discuss the uncertainties of our estimated emissions
315 that are generated from assumptions on the PBLH, the regional background
316 concentration and wind speeds. Table S1 shows the different results for each case and
317 the baseline method, called REF, over the Texas area. The mean, median, maximum
318 and minimum difference relative to REF in Texas are listed. The total emission of each
319 case over the Permian Basin is also quantified (last column in Table S1). Figure S5-S7
320 are corresponding spatial distributions of estimated emissions and the difference with
321 reference to the REF by using different assumptions of PBLH, the regional background
322 and the wind speeds, respectively.

323 PBLHs varying from 300m to 1000m were tested. The influence of the PBLH on the
324 spatial pattern and the total amount of final emissions are small, especially for the cases

325 below 1000m. We also changed the size of the background region from surrounding 3
326 grid cells to 7 grid cells (in each direction), leading to a bias of at most -0.19 Tg a^{-1}
327 for the total emissions of the Permian Basin. As expected, the smaller size of the
328 regional background (e.g. 3 grid cells) lead to a higher regional background over the
329 areas with big sources. Thus, the estimated emissions are decreasing over the emissions
330 clusters while the emissions around them often increase.

331 We tested various restrictions on the maximum and minimum wind speed (Figure S8).
332 The influence of wind speed is more complicated. Unlike the tests of PBLH and
333 regional background, different restrictions firstly affect the samplings of days. High
334 wind speeds lead to large uncertainties over areas with complicated terrain. For example,
335 large divergence values near the mountains close to the west of the Permian Basin, are
336 not sufficiently removed with the “correlation correction” (Fig. S8 (a)). The smearing
337 effect by high wind speeds lead to homogenous spatial distributions of XCH_4 in the
338 PBL. The signals of sources are hard to be separated from the regional background. It
339 also indicates that cases with high wind speeds are not handled well by our method, and
340 are therefore excluded. In contrast, constraints on lowest wind speeds have smaller
341 effects on final emissions (Fig. S8 (e)-(f)), because pollutants exhibit much stronger
342 horizontal gradient in calm scenes. But the divergence method works only if
343 transportation related to wind exists, so we set the minimum wind speed at 1m/s.

344 **4 Conclusions**

345 A new divergence method has been successfully developed and applied to estimate CH_4
346 emissions over Texas in North America based on observations of the TROPOMI
347 instrument. The method works fairly well to detect sources of all strengths, proven by
348 using a GEOS-Chem model simulation as an ideal case. Applied to real TROPOMI
349 observations it clearly identifies signals from oil/gas clusters and other sources, such as
350 livestock and wetlands. Further quantification of annual averaged CH_4 emissions over
351 the Permian Basin area is consistent with recent previous studies. The different spatial
352 distributions of emissions in different inventories (ranging from 2012-2019) imply
353 strong temporal variations of emissions in this area. The divergence method we built
354 benefits from TROPOMI’s high spatial resolution and provides a way to quickly
355 estimate CH_4 emission from satellite observation. The method does not need use any a
356 priori information on location of strength of the emissions.

357 Through the sensitivity tests on the PBLH, the regional background and the wind speeds,
358 the uncertainties of estimated emissions could be reduced by constraining their values.
359 High wind speeds cause high uncertainties over areas with complicated terrain. In
360 future work the uncertainties caused by the winds will be reduced when longer records
361 of background concentrations, EAC4 dataset, are available. The higher spatial
362 resolution of the estimated emissions is another aspect to be improved after the new
363 S5P TROPOMI CH_4 dataset will be released.

364 **Acknowledgments**

365 **Competing interests.** The authors declare that they have no competing interests.

366 **Author contributions.** ML, RVA, and MVW designed the experiment. All GEOS-
367 Chem simulations over the US were conducted by XL. ML performed all calculations.
368 The codes for estimating methane emissions are mainly developed by ML and are
369 supported by HE and PV. HK, JW, JS, and JD help to visualize the results. JL provided
370 the script to download the TROPOMI methane L2 file. The wind fields are extracted
371 by HE. YZ and HW help to access the GESO-FP meteorological dataset. All co-authors
372 contributed to review the manuscript.

373 **Data and materials availability:**

374 S5P TROPOMI methane Level-2 dataset is available at: [http://www.tropomi.eu/data-](http://www.tropomi.eu/data-products/methane)
375 [products/methane](http://www.tropomi.eu/data-products/methane)

376 EAC4 of CAMS, which used to be estimated the column above the PBL can be accessed
377 at: [https://ads.atmosphere.copernicus.eu/cdsapp#!/dataset/cams-global-reanalysis-](https://ads.atmosphere.copernicus.eu/cdsapp#!/dataset/cams-global-reanalysis-eac4?tab=overview)
378 [eac4?tab=overview](https://ads.atmosphere.copernicus.eu/cdsapp#!/dataset/cams-global-reanalysis-eac4?tab=overview)

379 Natural gas power plants and processing plants in Texas are available at:
380 https://www.eia.gov/special/gulf_of_mexico/

381 County-based heads of cattle and calves in Texas in 2019 is available at:
382 [https://www.nass.usda.gov/Statistics_by_State/Texas/Publications/County_Estimates/](https://www.nass.usda.gov/Statistics_by_State/Texas/Publications/County_Estimates/ce_maps/ce_catt.php)
383 [ce_maps/ce_catt.php](https://www.nass.usda.gov/Statistics_by_State/Texas/Publications/County_Estimates/ce_maps/ce_catt.php)

384 EDGAR v4.3.2 for the total anthropogenic emissions in 2012 is available at:
385 https://edgar.jrc.ec.europa.eu/overview.php?v=432_GHG

386 WeCHARTs wetland emission in 2015 can be found at: [https://daac.ornl.gov/cgi-](https://daac.ornl.gov/cgi-bin/dsviewer.pl?ds_id=1502)
387 [bin/dsviewer.pl?ds_id=1502](https://daac.ornl.gov/cgi-bin/dsviewer.pl?ds_id=1502)

388 The GEOS-Chem simulation dataset will be upload to the Amazon Drive after this
389 paper is accepted.

390

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Geophysical Research Letters

Supporting Information for

A new divergence method to quantify methane emissions using observations of Sentinel-5P TROPOMI

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24 **This PDF file includes 15 pages containing**

- 25 1. Part A: The stripe correction on XCH₄
- 26 2. Part B: Influence of surface albedo corrections on estimated CH₄ emissions
- 27 3. Figures S1 to S8
- 28 4. Table S1
- 29 5. SI references

30 **Part A. The stripe correction on XCH₄**

31 We apply the stripe correction on XCH₄ to remove across-track biases between the
32 individual viewing angles of the satellite. The stripe correction is determined from Level
33 2 files by first applying a high-pass median filter in the across-track direction and next a
34 high-pass median filter in the time direction (Borsdorff, personal communication 2020).
35 The Level 2 files provide the data in two dimensions as scan lines (temporal direction)
36 and ground pixels (across satellite track and approximately west-east). The first step for
37 creating the stripe correction is performed per orbit. First a smoothed XCH₄ image is
38 computed using a median filter in the across track direction, using the XCH₄ with
39 $qa_value > 0.5$ for each ground pixel and its four eastern and western neighbors. At the
40 eastern and western edge of the swath this number is less, but at least 4 neighboring
41 pixels are taken into account. In this step, online scans with at least 20% valid data are
42 taken into account. The across track striping pattern of the orbit is computed by
43 subtracting the smoothed image from the XCH₄ data and subsequently taking the median
44 in the temporal direction.

45 After computing the stripe pattern for all orbits, a smoothing between the orbits is
46 performed by applying a median of the orbit and its 50 previous and 50 next orbits (note
47 that 100 orbits cover approximately one week of data). Finally, a linear interpolation is
48 performed in temporal direction to compute the striping correction for all orbits,
49 including those for which too little data was available to compute the stripe pattern.

50 As shown in Figure S1, the corrections depend on the TROPOMI ground pixel index and
51 orbit number. The changes of yearly averaged XCH₄ in 2019 before and after destriping

52 are within ± 5 ppb (mean: -0.08 ppb) on a 0.25° grid. Figure S1 shows the difference
53 with time before and after the stripe correction. For most ground pixels, the differences
54 are within 10 ppb.

55 **Part B. Influence of surface albedo corrections on estimated emissions**

56 The current official TROPOMI bias-corrected XCH_4 product (XCH_4^{S5P}) is derived from a
57 second order fit to the ratio of TROPOMI and GOSAT CH_4 as a function of SWIR
58 albedo [Hasekamp *et al.*, 2019; Lorente *et al.*, 2021]. It is defined as:

$$59 \quad XCH_4^{S5P} = XCH_4 (c1 + c2 \cdot A + c3 \cdot A^2) \quad (S1)$$

60 where A is the surface albedo retrieved at the SWIR spectral range and $c1 (=1.0173)$, $c2$
61 $(=-0.1538)$, $c3 (= -0.2036)$ are the correction parameters derived from a second order fit
62 of the ratio of TROPOMI and GOSAT CH_4 as a function of albedo [Hasekamp *et al.*,
63 2019]. Although this posteriori correction reduces the general biases to ground-based
64 TCCON observation, XCH_4^{S5P} is still likely to underestimate over the areas with low
65 albedos and overestimate over very bright surface. These systematic biases can be seen
66 clearly over Northern Africa in Fig S2, which covers a wide range of realistic surface
67 albedos. The positive corrections given by Eq. (S1) for the areas with high albedos (>0.5)
68 lead to high XCH_4^{S5P} comparing to uncorrected XCH_4 (Fig S2 (c)). Thus, the spatial
69 pattern of XCH_4^{S5P} (Fig. S2 (b)) are quite similar to the SWIR surface albedo (Fig. S2 (d)).
70 These biases of XCH_4^{S5P} , caused by the dependence on GOSAT observations and the lack
71 of ground-based observations, have been also found by Lorente *et al.* [2021]. The new
72 fitting function for the coming version becomes independent of GOSAT observations and
73 monotonous (See Figure 4 in Lorente *et al.* [2021]).

74 To avoid the abovementioned biases caused by surface albedos, in this study, a piecewise
75 linear fit to XCH_4 as a function of the corresponding SWIR surface albedo are designed
76 to give a positive correction for low-albedo areas (< 0.1) and a negative correction for
77 high-albedo areas (≥ 0.1). The junction point, where the albedo is equal to 0.1, of the
78 piecewise linear fit functions is obtained from Hasekamp *et al.* [2019]. The advantage of
79 the linear fitting is that the coefficient can be directly treated as correction factor (CF).

80 Therefore, the corrected TROPOMI XCH₄ (XCH₄^{CORR}) is XCH₄ · (1 + CF). CF is obtained
81 as follows:

$$82 \quad \quad \quad CF = CF_1 \cdot (0.1 - A) \quad \quad \quad (A < 0.1) \quad \quad \quad (S2)$$

$$83 \quad \quad \quad CF = CF_2 \cdot A \quad \quad \quad (A \geq 0.1) \quad \quad \quad (S3)$$

84 where CF₁ is the positive-correction coefficient (= 671.0), and CF₂ is the negative-
85 correction coefficient (= -63.5) derived from the two-segment linear fitting.

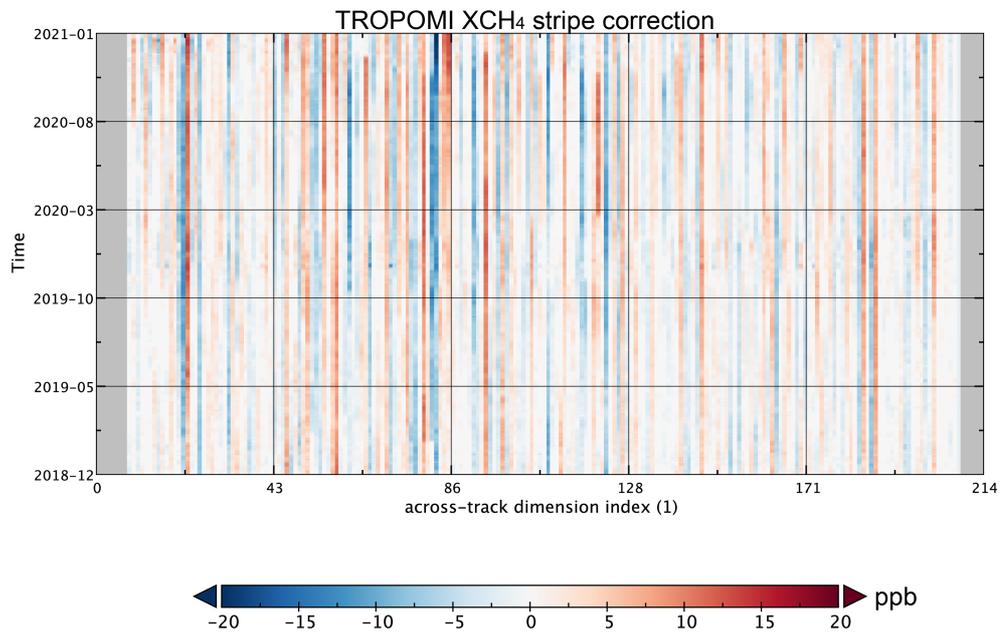
86 The fitting is based on the gridded yearly average of TROPOMI XCH₄ and
87 corresponding SWIR surface albedo in 2019 over the US (the domain is showed in Fig. 2)
88 on a 0.25° grid (the same spatial resolution as the later divergence calculation and the
89 emission estimation). Only XCH₄ retrievals lower than 3000 ppb and with an elevation
90 below 500 m are selected for the fitting. We use gridded data instead of observation
91 pixels to avoid issues with seasonal variations and over-sampling.

92 Figure S3(a)-(b) are the spatial distributions of TROPOMI yearly-averaged XCH₄ after
93 destriping and SWIR surface albedo corrections over the North America on a 0.25° grid
94 in 2019. Some strong enhancements caused by landforms (e.g., rocks and deserts in Utah
95 and Arizona; alluvial accumulation around Mississippi Delta) are clearly seen from Fig.
96 3(a). Figure 3(d) gives a more reasonable spatial pattern over North America. The
97 overestimated XCH₄ due to the bare ground in western U.S. decrease while the
98 concentration over the east coast increase after corrections (Fig. S3(d)). After converting
99 XCH₄ to XCH₄^{PBL}, the spatial distribution of CH₄ becomes more continuous over
100 mountains in Fig. S3(e). Despite the uncertainty from surface albedo corrections,
101 enhancement of CH₄ are found over Texas, California and Appalachia regions when
102 comparing to the regional background (Fig. S3(f)).

103 The third row presents spatial distributions of XCH₄ with the surface albedo corrections
104 of the official S5P operational product (XCH₄^{S5P}). The overestimated XCH₄ due to the
105 bare ground (i.e. high albedo) in western U.S. decrease after both corrections (Fig. S3 (d)
106 and (g)). Relatively big differences in the two corrections are found over the east coast of
107 the U.S., where our results are about ~15 ppb higher than XCH₄^{S5P} over the areas with
108 dark surfaces (albedo < 0.1). The enhancements caused by wetlands over here are much

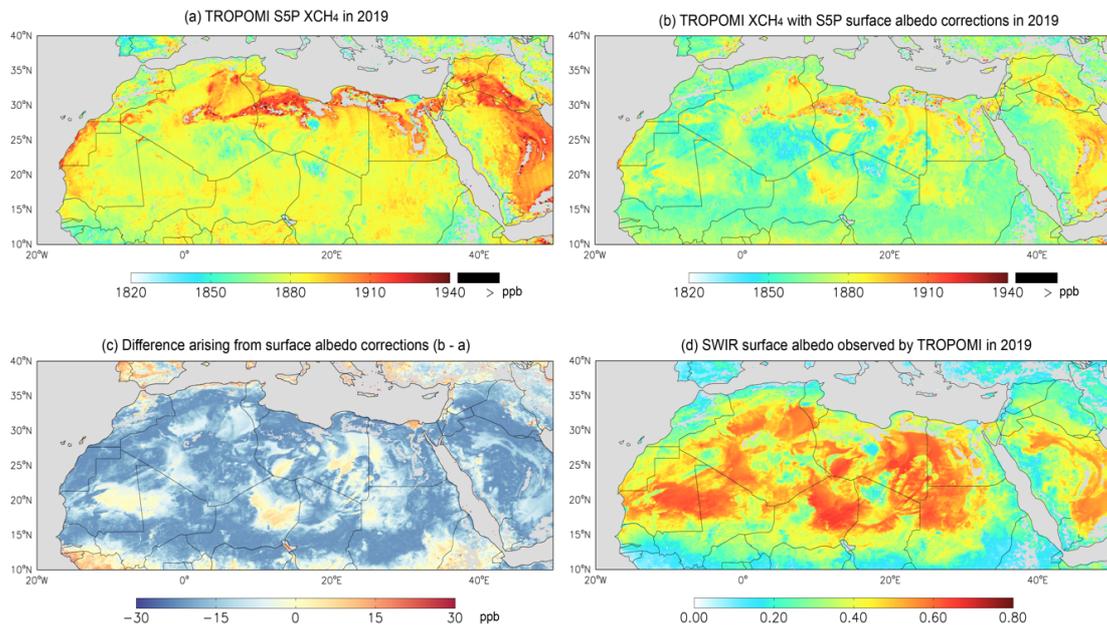
109 clearer in our corrections. The underestimation of XCH_4^{S5P} has also been improved in
110 Lorente et al, [2021].

111 Figure S3 further quantified the difference caused by two different surface albedo
112 corrections over Texas. In general, the locations of big sources are caught in both Fig. S4
113 (a) and (b). Big differences of estimated emissions appear over Mexico and the east of
114 Texas. The big sources near the border of Louisiana and Texas in Fig. S4(b) seem to be
115 biases in XCH_4^{S5P} .

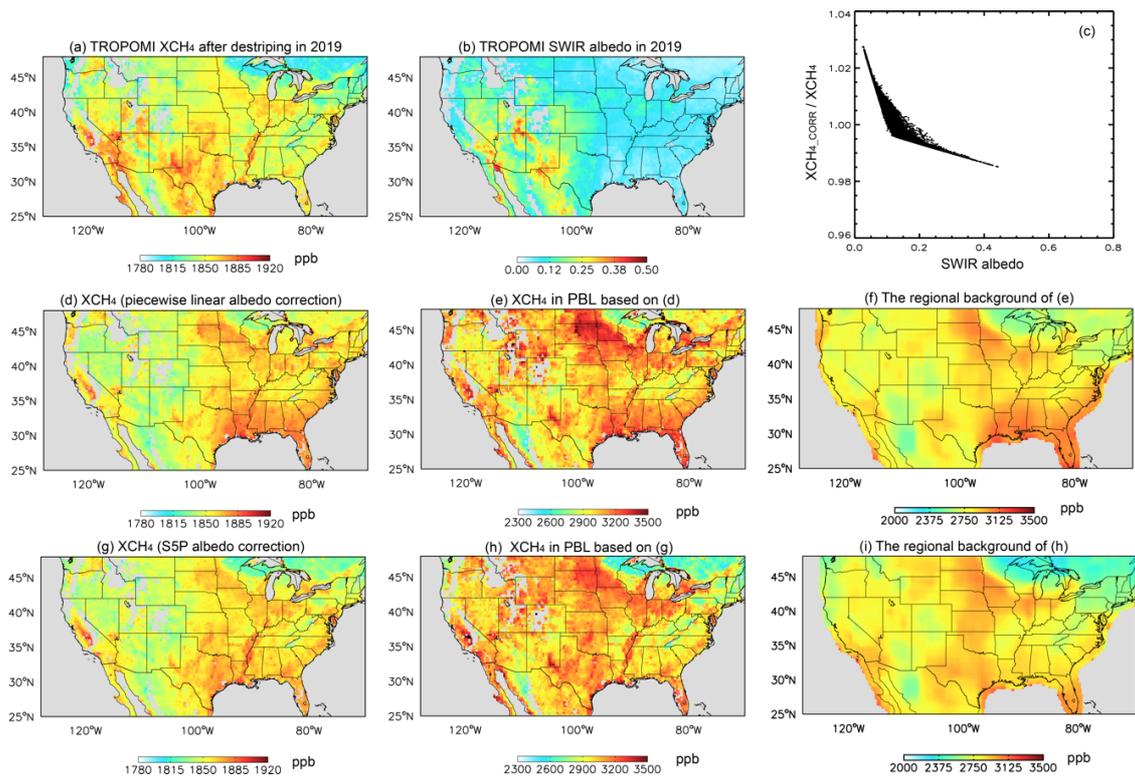


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117 **Figure S1.** The difference over time before and after the stripe correction.

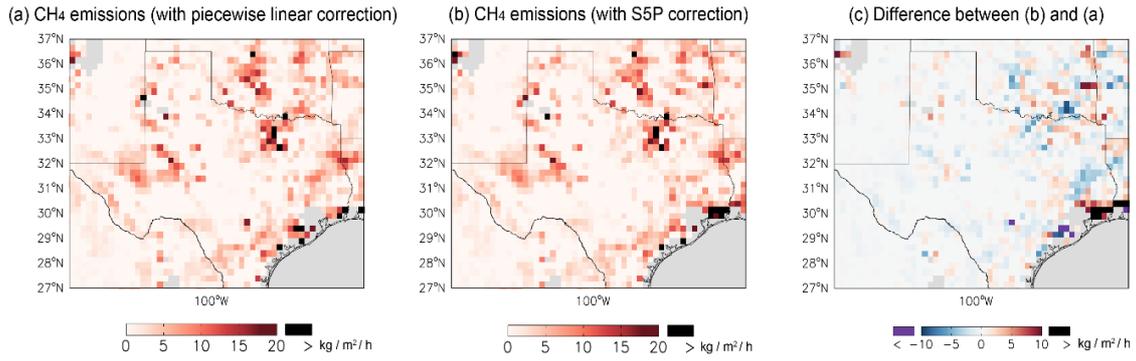


119 **Figure S2.** The spatial distributions of yearly averaged (a) XCH₄, (b) XCH₄^{S5P} and (c)
 120 their difference in 2019 on a 0.25° grid. (d) The TROPOMI observed SWIR surface
 121 albedos that is used to correct XCH₄.



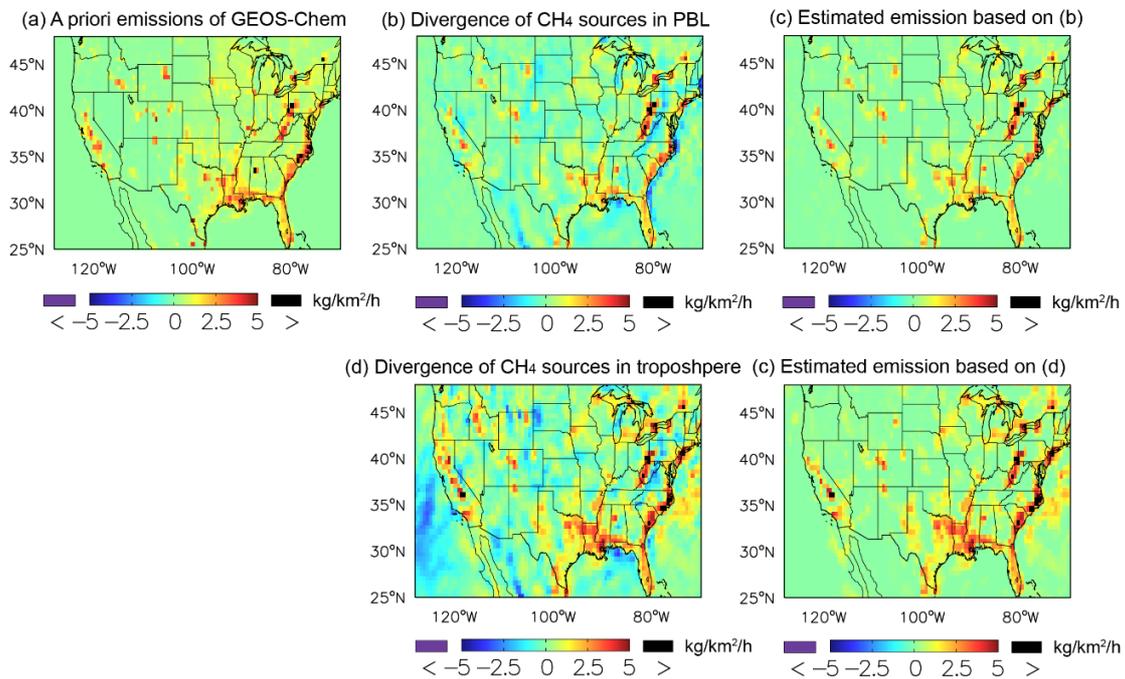
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123 **Figure S3.** Yearly averages of (a) TROPOMI XCH₄ after destriping and (b) TROPOMI
 124 SWIR surface albedo in 2019 on a 0.25° grid. (c) The scatter plots of the ratios of
 125 XCH₄_{CORR}/XCH₄ and SWIR surface albedos. Each dot represents a grid cell in (a) and
 126 (b). Yearly averages of (d) XCH₄ with segment linear surface albedo corrections, (e) the
 127 corresponding XCH₄ in PBL and (f) its regional background. (g)-(i) are similar to (d)-(f)
 128 but for XCH₄ with S5P surface albedo correction.

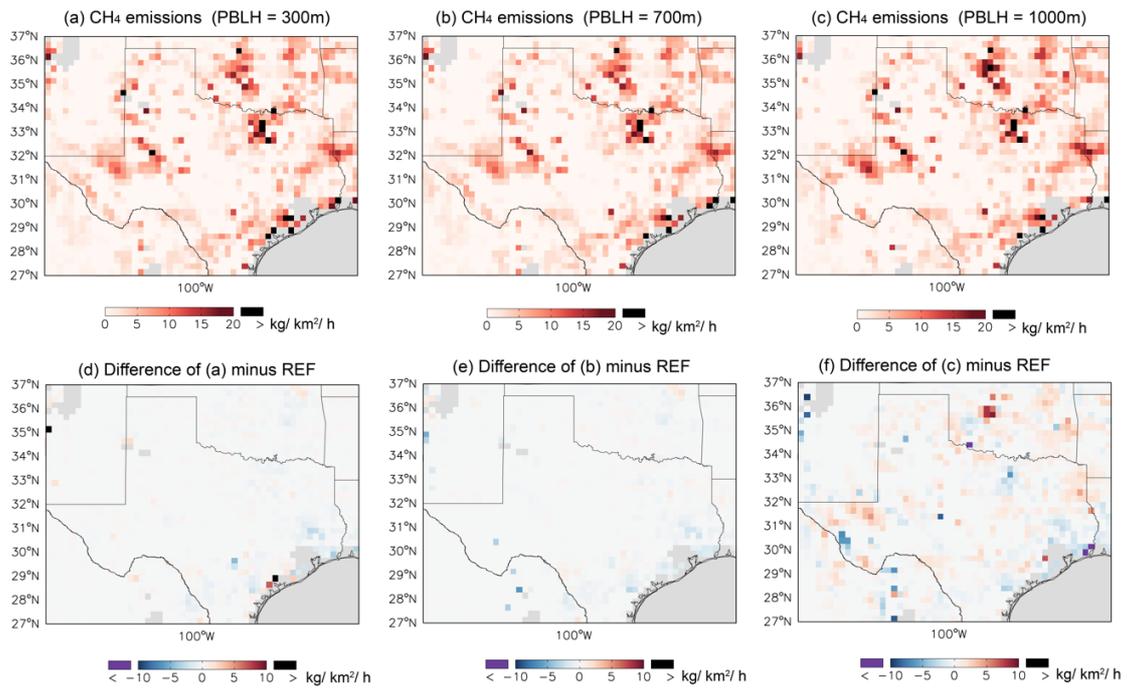


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130 **Figure S4.** The estimated CH₄ emissions based on (a) XCH₄^{CORR}, (b) XCH₄^{S5P} and (c) their
 131 difference in 2019 on a 0.25° grid.



133 **Figure S5.** The spatial distributions of (a) the average of a priori CH₄ emissions used in
 134 GEOS-Chem simulation, (b) the divergence of CH₄ sources in the PBL, and (c)
 135 corresponding estimated CH₄ emissions over July-September 2012 on a 0.625° lon. ×
 136 0.5° lat. grid. (d)-(e) are similar to (b)-(c) but for the results using XCH₄ in the
 137 troposphere.



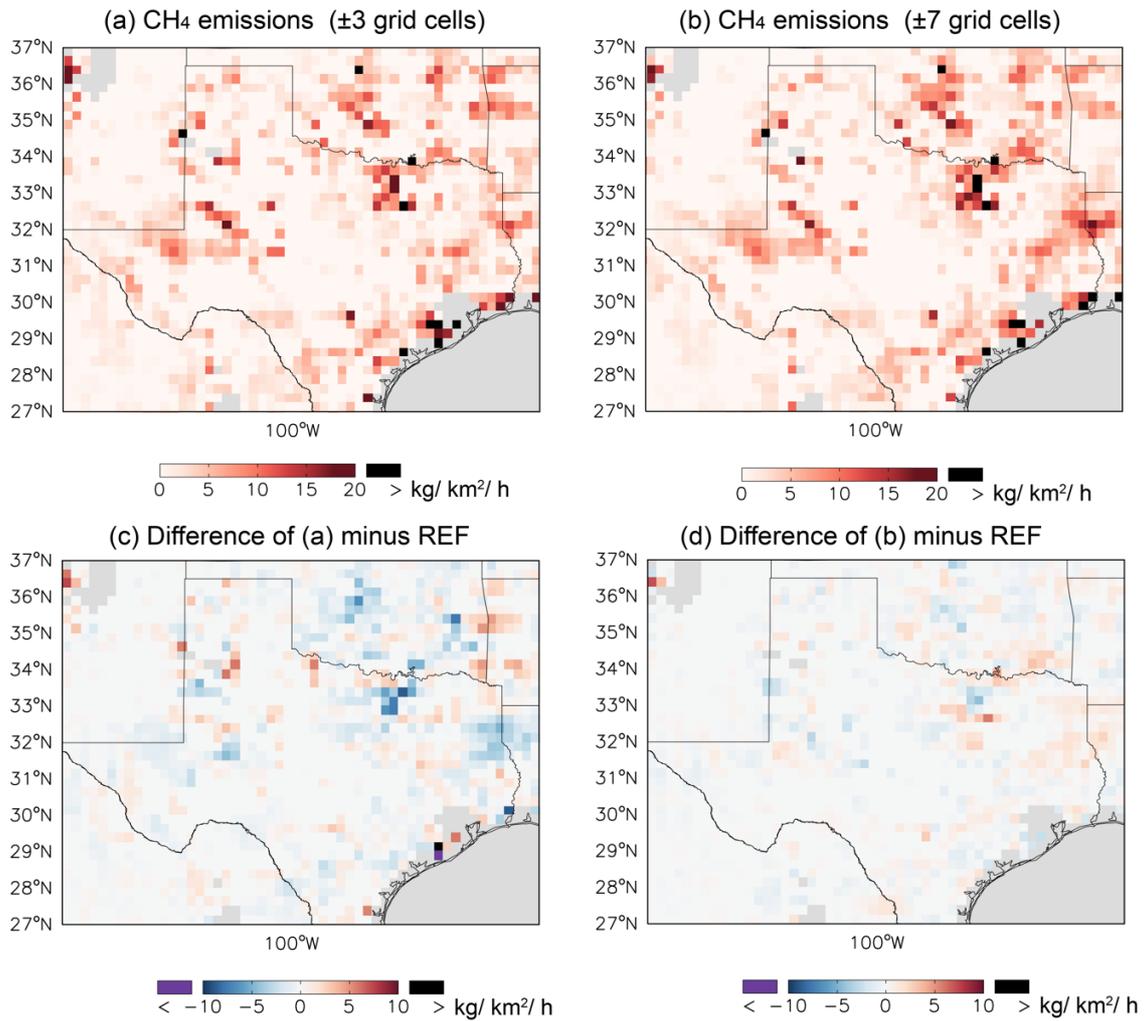
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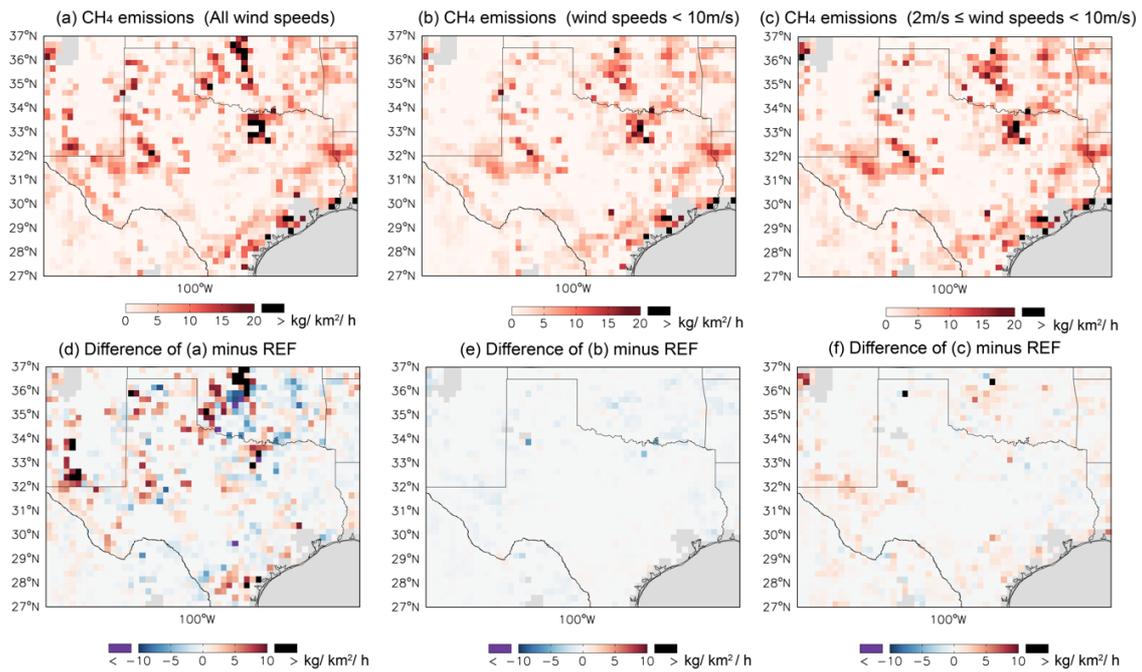
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Figure S6. Results of different assumptions on PBLH. (a)-(c) are CH₄ emissions estimated with (a) PBLH = 300 m, (b) PBLH = 700 m, (c) PBLH = 1000 m and. (d)-(f) are corresponding differences of (a)-(c) minus REF.



142 **Figure S7.** Results of different assumptions on the size of the background region from (a)
 143 surrounding 3 grid cells to (b) 7 grid cells (in each direction). (c)-(d) are corresponding
 144 differences of (a)-(b) minus REF.



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Figure S8. Results of different assumptions on the constraints of wind speeds (V). (a)-(c) are CH_4 emissions estimated with (a) all V , (b) $V < 10$ m/s, (c) $2 \text{ m/s} \leq V < 10$ m/s. (d)-(f) are corresponding differences of (a)-(c) minus REF.

Table S1. Results of sensitivity studies.

REF: $1 < V < 10$ m/s; PBLH = 500m; Background: ± 5 grid cells; 3.06 Tg a^{-1}

Difference with reference to REF ¹	Mean (kg/km ² /h)	Medium (kg/km ² /h)	Min (kg/km ² /h)	Max (kg/km ² /h)	Total emission of Permian Basin ⁴ (Tg a ⁻¹)
Wind speeds (m/s)					
V < 10	-0.2	-0.1	-10.4	1.44	2.82
2 < V < 10	0.5	0.3	-4.7	14.7	3.78
All	0.1	0.0	-29.8	30.5	3.60
PBLH (m)²					
300	-0.05	0.0	-4.5	6.8	3.06
700	-0.1	-0.02	-6.2	1.9	3.04
1000	0.07	0.1	-22.4	9.2	3.37
Background³					
± 3 grid cells	-0.3	-0.2	-12.0	11.2	2.87
± 7 grid cells	0.0	0.0	-4.4	7.1	3.00

149 ¹ The value of mean, medium, minimum and maximum is the difference with the
 150 reference (REF) in the domain (27°-37°N, 106.5°-93°W) of Fig. 4.

151 ² The PBLH is the height above the ground.

152 ³ The tested parameter is the number of surrounding grid cells that are used to generate
 153 the background.

154 ⁴ The domain of the Permian Basin is 30°-34°N, 101°-105°W, shown in Fig. 4(a)

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