

Thermodynamics of Liquid MgSiO_3 at High Pressure and Temperature

Felipe González-Cataldo¹, Francois Soubiran¹, Henry Peterson¹, and Burkhard Militzer¹

¹University of California Berkeley

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Abstract

Studying the properties of the liquid phase of minerals at high pressure is important to understand the structure and evolution of deep magma oceans, as well as guiding high pressure experiments that reach the conditions in the interiors of rocky planets. We use density functional theory molecular dynamics (DFT-MD) and path integral Monte Carlo (PIMC) simulations to generate a consistent equation of state (EOS) for liquid MgSiO_3 that spans across a wide range of temperatures and pressures. We study its thermodynamic properties, such as the heat capacity, and characterize the atomic structure of the liquid. From our simulations, we are able to determine the onset of ionization of the inner electronic shells and relate the thermodynamic properties to the electronic structure. Finally, in order to guide future ramp and shock compression experiments, we derive isentropic temperature-pressure profiles and calculate the shock Hugoniot curve, which is in good agreement with existing experimental data.

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Felipe González-Cataldo¹, François Soubiran^{2,1}, Henry Peterson¹, and Burkhard Militzer^{1,3}.

¹Department of Earth and Planetary Science, University of California, Berkeley, California 94720, USA

²Laboratoire de géologie de Lyon, CNRS UMR 5276, Ecole Normale Supérieure de Lyon, Université Claude Bernard Lyon 1, 46 Allée d'Italie, 69364 Lyon Cedex 07, France

³Department of Astronomy, University of California, Berkeley, California, USA

f_gonzalez@berkeley.edu



1. Summary

- MgSiO_3 is one of the most abundant minerals on Earth's crust.
- Equation of state (EOS) fundamental to study planetary formation and evolution.
- Extreme conditions: ionization of electronic shells modify thermodynamic properties.
- Combining DFT-MD + PIMC we produce a consistent equation of state across a wide range of pressures and temperatures.

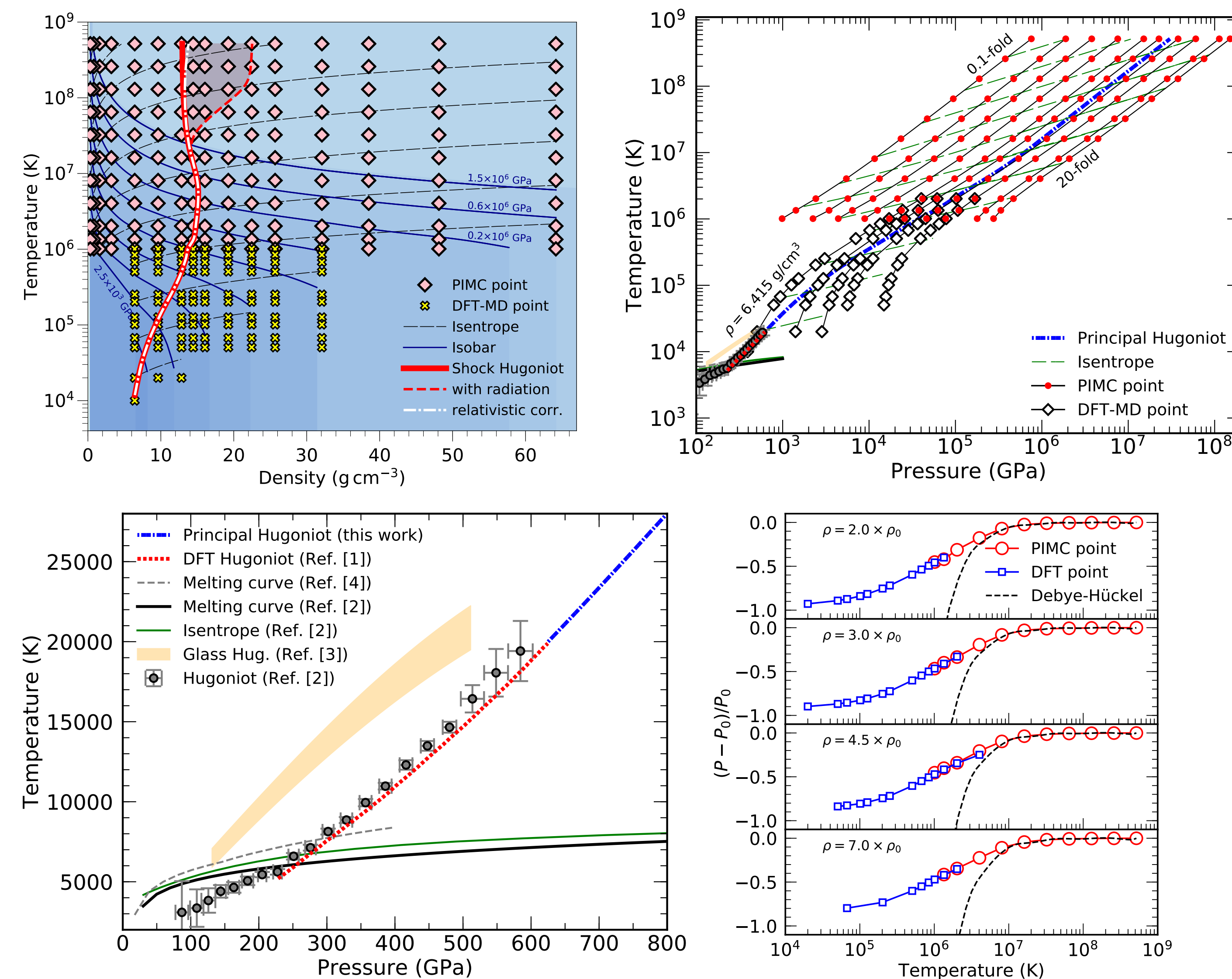


Figure 1: Temperature-density and temperature-pressure conditions of our DFT-MD and PIMC simulations along with computed isobars, isentropes and three principal shock Hugoniot curve that were derived for an initial density of $\rho_0 = 3.207911 \text{ g cm}^{-3}$ ($V_0 = 51.965073 \text{ Å/f.u.}$). The red dashed line corresponds to the Hugoniot curve from Ref. [1], calculated from DFT-MD simulations. Experimental measurement of the principal Hugoniot curve from Ref. [2], an isentrope derived from this experiment (solid green line), and the Hugoniot curve for MgSiO_3 glass [3] (orange region) are shown for reference. The melting line of MgSiO_3 derived from two-phase simulations [4] is shown in dashed grey line, while the melting curve derived from shock experiments [2] is represented by the thick black line. Pressure normalized to the ideal Fermi gas pressure, P_0 .

- ⇒ PIMC + DFT-MD: consistent EOS
- ⇒ Good agreement with the experimental shock Hugoniot curve.
- ⇒ Prediction of a maximum compression ratio of 4.7.

2. Ionization of K shell

Nuclear-electron pair correlation function:

$$N(r) = \left\langle \frac{1}{N_I} \sum_{e,I} \Theta(r - \|\vec{r}_e - \vec{r}_I\|) \right\rangle, \quad (1)$$

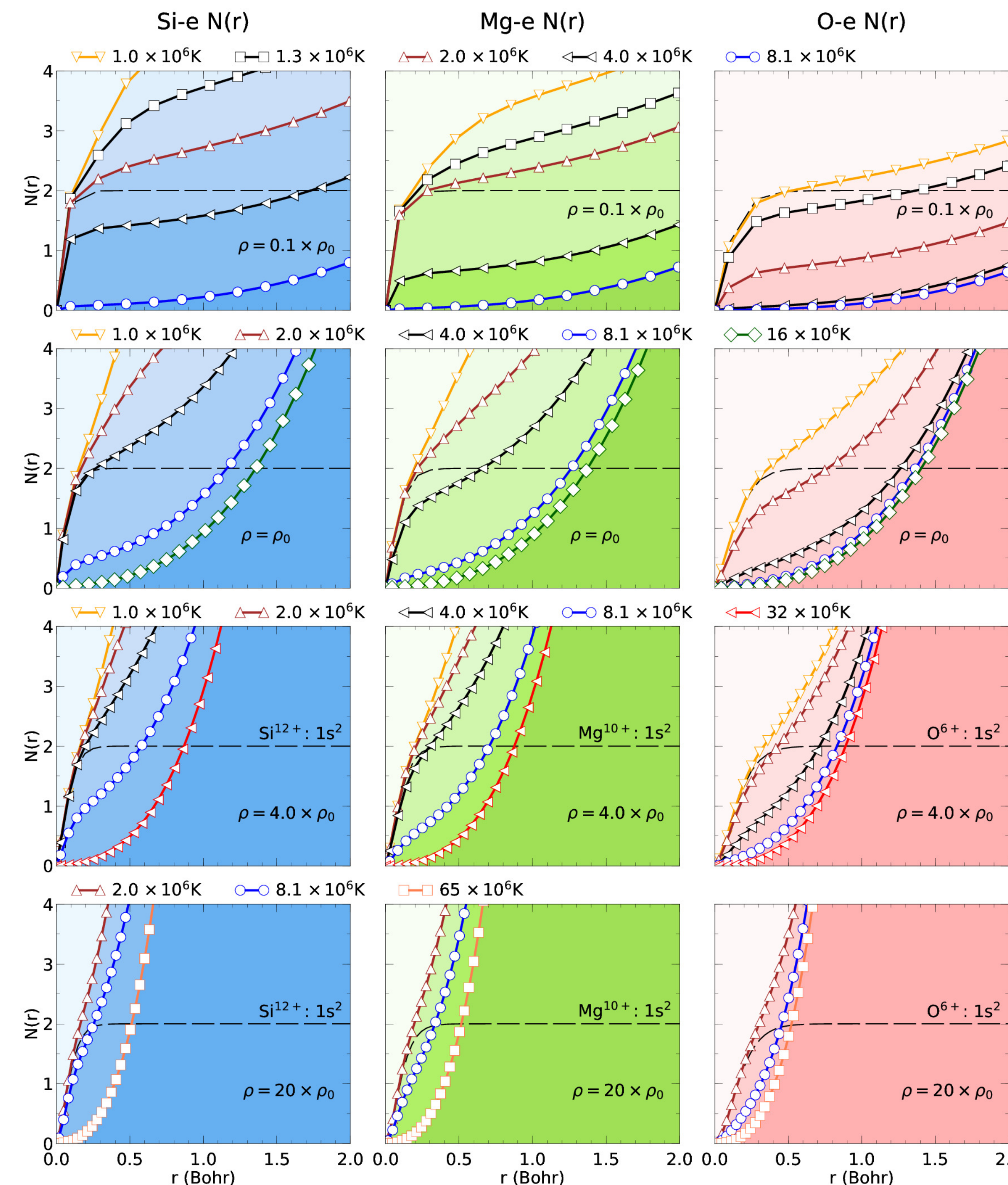


Figure 2: $N(r)$ functions for Mg, Si, and O atoms in the MgSiO_3 system.

Effects of ionization in the heat capacity, $C_v = (\partial E / \partial T)_V$, and Grüneisen parameter, $\gamma = V (\partial P / \partial E)_V = \frac{V}{C_v} (\partial P / \partial T)_V$,

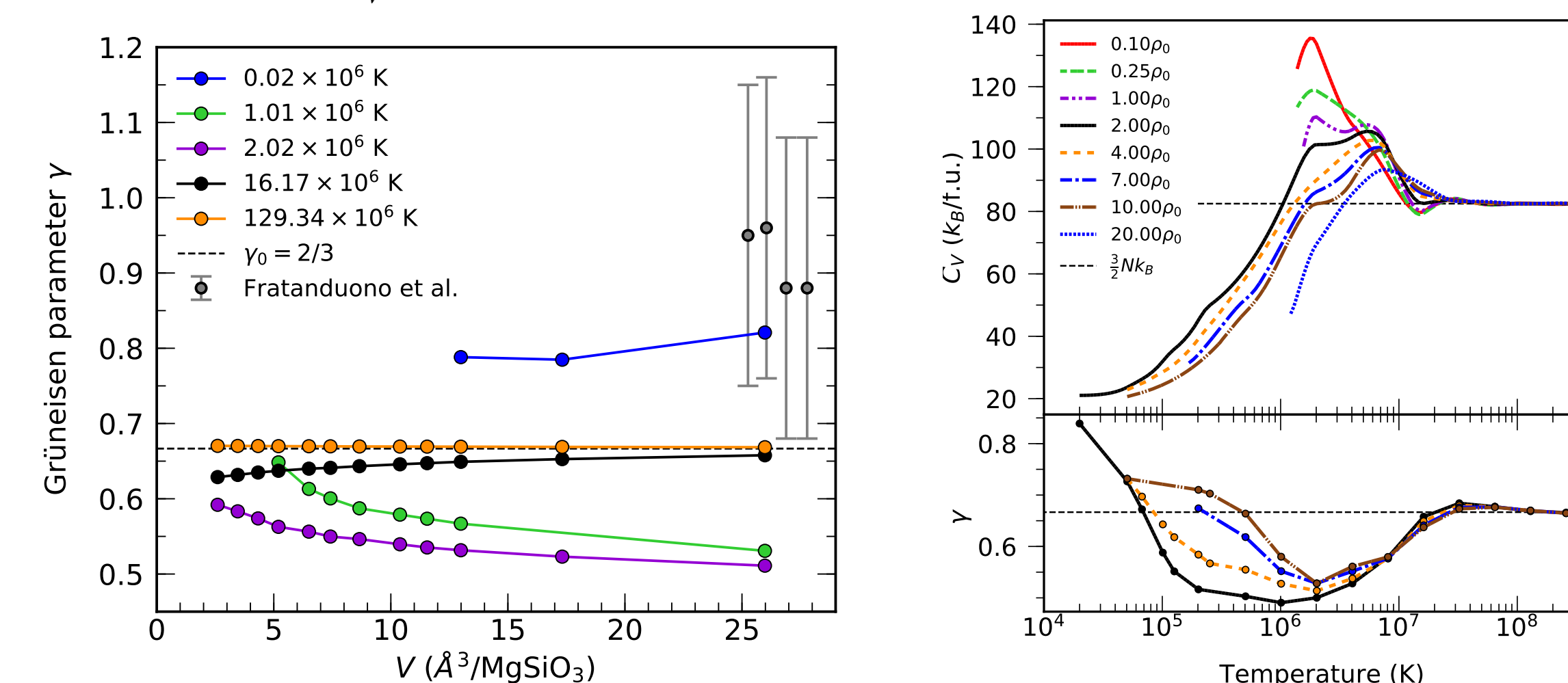


Figure 3: Grüneisen parameter, γ , and heat capacity, C_v as a function of temperature.

3. Hugoniot curves

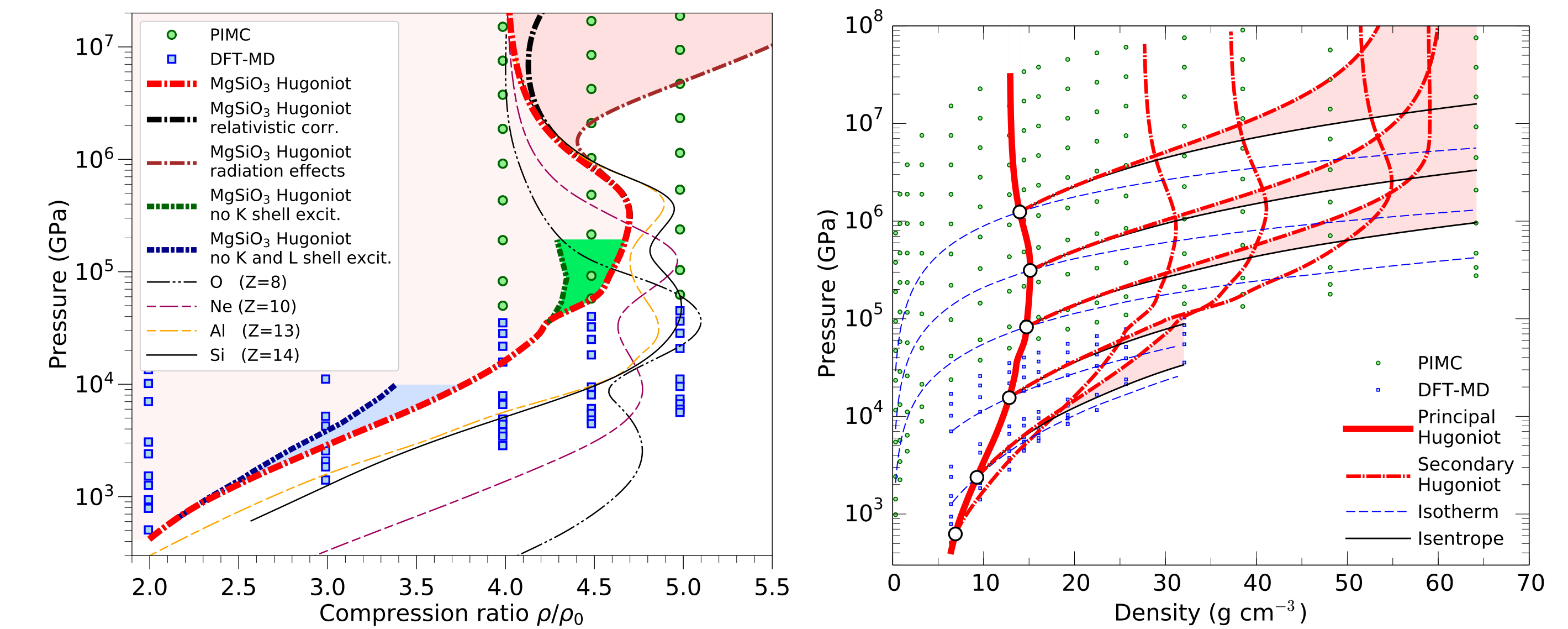


Figure 4: Principal Hugoniot curve, with and without electronic excitations, compared to other materials. Secondary shocks are compared to isentropes, providing a guide for ramp compression experiments.

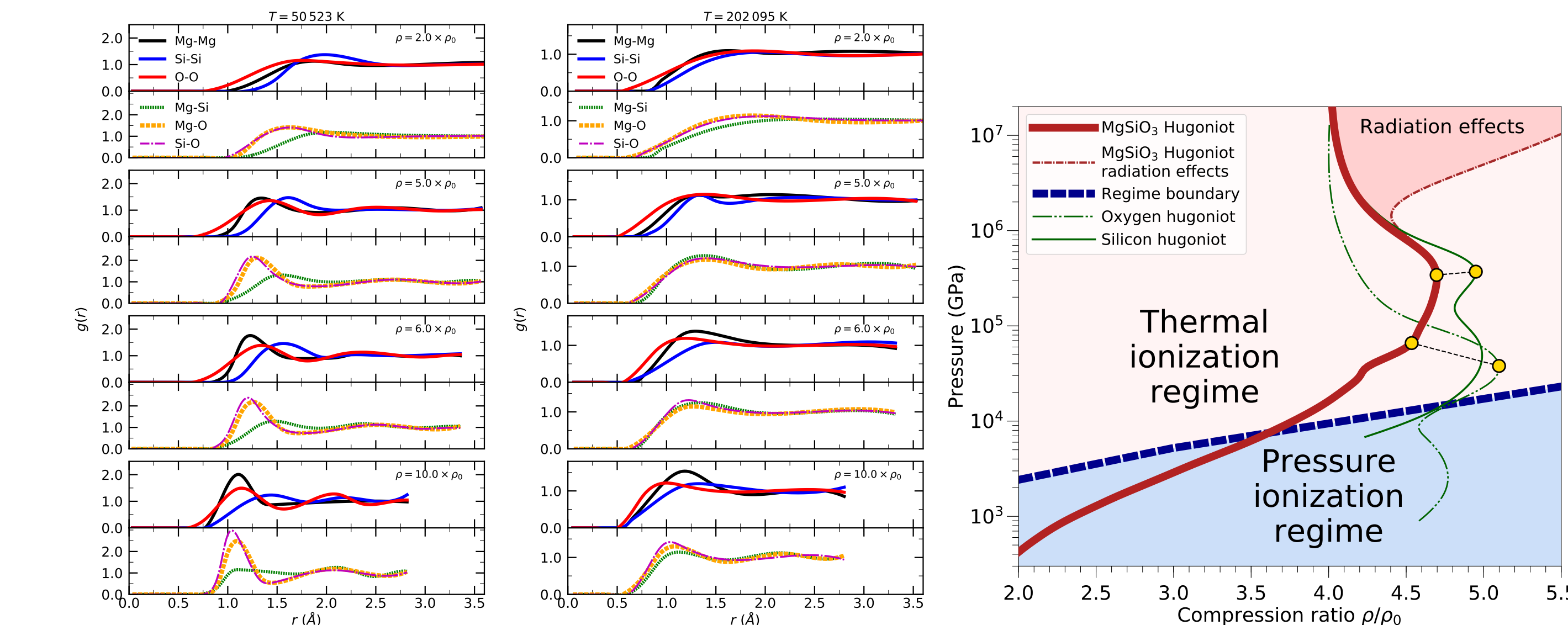


Figure 5: Pair distribution function, $g(r)$, at $5 \times 10^4 \text{ K}$ and $2 \times 10^5 \text{ K}$ for different densities. Pressure ionization regime determined by $\frac{dE}{dV}|_V = 0$ (equiv. to $P/T = (\partial P / \partial T)_V$).

4. Conclusions

1. Hugoniot curve: good agreement with experiments.
2. Consistent EOS (DFT-MD + PIMC).
3. Maximum shock compression ratio: 4.7 ($5.13 \times 10^6 \text{ K}$ and $3.01 \times 10^5 \text{ GPa}$).
4. No L shell ionization peak.
5. Ramp compression: secondary shocks close to isentropes.
6. Full K shell ionization consistent with ideal gas limit.
7. PBE functional can accurately describe MgSiO_3 up to temperatures of $\sim 10^6 \text{ K}$.

References

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