

# Whole Atmosphere Model Simulations of 3-day Kelvin Wave Effects in the Ionosphere and Thermosphere

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November 24, 2022

## Abstract

This paper examines the response of the upper atmosphere to equatorial Kelvin waves with a period of  $\sim 3$  days, also known as ultra-fast Kelvin waves (UFWs). The whole atmosphere model GAIA is used to simulate the UFW events in the late summer of 2010 and 2011 as well as in the boreal winter of 2012/2013. When the lower layers of the model below 30 km altitude are constrained with meteorological data, GAIA is able to reproduce salient features of the UFW in the mesosphere and lower thermosphere as observed by the Aura Microwave Limb Sounder. The model also reproduces ionospheric response, as validated through comparisons with total electron content data from the GOCE satellite as well as with earlier observations. Model results suggest that the UFW produces eastward-propagating  $\sim 3$ -day variations with zonal wavenumber 1 in the equatorial zonal electric field and F-region plasma density. Model results also suggest that for a ground observer, identifying ionospheric signatures of the UFW is a challenge because of  $\sim 3$ -day variations due to other sources. This issue can be overcome by combining ground-based measurements from different longitudes. As a demonstration, we analyze ground-based magnetometer data from equatorial stations during the 2011 event. It is shown that wavelet spectra of the magnetic data at different longitudes are only in partial agreement, with or without a  $\sim 3$ -day peak, but a spectrum analysis based on multipoint observations reveals the presence of the UFW.

# Whole atmosphere model simulations of ultra-fast Kelvin wave effects in the ionosphere and thermosphere

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## Key Points:

- GAIA model simulations of ultra-fast Kelvin wave (UFWK) in the middle and upper atmosphere
- UFWK produces eastward-propagating  $\sim 3$ -day ionospheric variations with zonal wavenumber 1
- First magnetic detection of UFWK in the equatorial electrojet

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15 **Abstract**

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 33 analysis based on multipoint observations reveals the presence of the UFKW.

34 **1 Introduction**

35 Equatorial Kelvin waves are a type of global-scale waves in the atmosphere. In clas-  
 36 sical theory (Matsuno, 1966; Holton & Lindzen, 1968), they travel eastward with per-  
 37 turbations in the zonal velocity and geopotential but with no meridional velocity com-  
 38 ponent. The amplitude is largest at the equator and it decays exponentially with lat-  
 39 itude. Equatorial Kelvin waves propagate vertically upward from the source region in  
 40 the troposphere where they are thought to be excited by latent heating due to tropical  
 41 convection. They are often classified into three categories according to the wave period  
 42 (and hence the zonal phase speed): slow Kelvin waves with periods 10–20 days, fast Kelvin  
 43 waves with periods 5–10 days, and ultra-fast Kelvin waves (UFKWs) with periods 2–  
 44 5 days. In general, a wave with a shorter period and longer wavelength is less suscep-  
 45 tible to dissipation and thus is able to reach higher altitudes. As the wave propagate to  
 46 higher altitudes, it grows in amplitude due to the reduction in atmospheric density. The

47 shortest-period waves, thus UFKWs, can propagate well into the mesosphere and lower  
48 thermosphere (MLT) region before being dissipated. Therefore, UFKWs can be a sig-  
49 nificant source of wave forcing in the upper atmosphere among other global-scale waves  
50 such as tides and planetary waves (Yiğit & Medvedev, 2015; H.-L. Liu, 2016).

51 Equatorial Kelvin waves were first identified in the lower stratosphere from radiosonde  
52 measurements. Wallace and Kousky (1968) found equatorial Kelvin waves with periods  
53  $\sim 15$  days and vertical wavelength of  $\sim 10$  km, which are now known as slow Kelvin waves.  
54 Hirota (1978, 1979) detected fast Kelvin waves with periods  $\sim 10$  days and vertical wave-  
55 length 15–20 km in the upper stratosphere and lower mesosphere using rocket and satel-  
56 lite measurements. Salby et al. (1984) was the first to observe the UFKW. They found  
57 UFKWs with periods  $\sim 4$  days and vertical wavelength  $\sim 40$  km in the mesosphere based  
58 on the temperature data from the Nimbus-7 satellite. Lieberman and Riggins (1997) con-  
59 firmed the presence of UFKWs at altitudes between 65 and 110 km using wind measure-  
60 ments from the UARS satellite. Forbes et al. (2009), using temperature measurements  
61 from the SABER instrument on the TIMED satellite, showed a transition of dominant  
62 waves from fast Kelvin waves (periods 5–10 days and vertical wavelengths 9–13 km) in  
63 the stratosphere to UFKWs (periods 2–3 days and vertical wavelengths 35–45 km) in  
64 the MLT region. Their results also showed that for fast Kelvin waves, the zonal-wavenumber  
65 1 and zonal-wavenumber 2 components are comparable in amplitude, while for UFKWs,  
66 the zonal-wavenumber 1 component is dominant. Vincent (1993) and subsequent stud-  
67 ies (Riggins et al., 1997; Yoshida et al., 1999; Sridharan et al., 2002; Pancheva et al., 2004;  
68 Davis et al., 2012) used wind measurements from meteor radars to examine UFKWs in  
69 the MLT region. UFKW activity is usually observed in short-lived bursts, which last a  
70 few wave cycles. England et al. (2012) and Egito et al. (2018) presented evidence for non-  
71 linear interaction between UFKWs and diurnal tide, which leads to the modulation of  
72 the tidal amplitude with UFKW periodicities. W.-S. Chen et al. (2018) examined the  
73 seasonal variability of the UFKW using SABER temperature measurements during 2002–  
74 2016, pointing out that the upward-propagation of the UFKW is influenced by both the  
75 mesospheric and stratospheric semiannual oscillations. G. Liu et al. (2019), using a sim-  
76 ilar dataset, examined the interannual variability of the UFKW at 110 km. The observed  
77 year-to-year variations were attributed to changes in the solar flux as well as to the quasi-  
78 biennial oscillation and El Niño–Southern oscillation of the atmosphere. Gasperini et al.  
79 (2015, 2018) used the accelerometer data from the Gravity field and steady-state Ocean

80 Circulation Explorer (GOCE) satellite to detect UFKWs in the thermosphere at  $\sim 250$   
81 km altitude, which was shown to be consistent with the UFKWs observed in the MLT  
82 region at the same time.

83 Studies have also shown that the UFKW can affect the ionosphere. Takahashi et  
84 al. (2006, 2007) observed  $\sim 3$  day variations in ionospheric parameters ( $h'F$  and  $foF2$ )  
85 and attributed them to the UFKWs simultaneously detected in the MLT region. G. Liu  
86 et al. (2012) examined global maps of total electron content (TEC) and incoherent scat-  
87 ter radar data during the UFKW event of January 2010. They suggested that the ob-  
88 served spatial and temporal features of the  $\sim 3$  day variations in TEC and electron den-  
89 sity are consistent with the modulation of the equatorial plasma fountain by the UFKW.  
90 Phanikumar et al. (2014) observed TEC variations with UFKW periodicity (3–5 days)  
91 during January–February 2009 and associated them with the major sudden stratospheric  
92 warming (SSW) event that took place at this time. Gu et al. (2014) presented observa-  
93 tions of UFKWs in the temperature and zonal wind in the MLT region, and simultane-  
94 ously in global TEC maps and COSMIC electron density during the year 2011. They  
95 showed that there is a good correspondence between UFKW activity in the MLT region  
96 and that in the low-latitude ionosphere. Abdu et al. (2015) pointed out that the equa-  
97 torial vertical plasma drift velocity at post-sunset times sometimes exhibits  $\sim 3$  day vari-  
98 ations during UFKW events in the MLT region.

99 Numerical models have been used to study excitation, dissipation, and propaga-  
100 tion characteristics of the UFKW. Forbes (2000) used a linear mechanistic model, in which  
101 UFKWs are generated through theoretical wave forcing (as predicted by classical wave  
102 theory) in the lower atmosphere. By running the model with the same wave forcing but  
103 with different background winds, it was demonstrated that the distribution of the zonal  
104 mean wind at the equator plays an important role for the UFKW propagation into the  
105 MLT region. Miyoshi and Fujiwara (2006), using a general circulation model (GCM),  
106 showed that the dissipation of UFKWs in the MLT region and accompanying momen-  
107 tum deposition into the mean flow can make a significant contribution to the intrasea-  
108 sonal variation of the zonal mean zonal wind in that region. Y.-W. Chen and Miyahara  
109 (2012) investigated fast and ultra-fast Kelvin waves generated in a GCM simulation. Both  
110 waves showed vertical propagation from the troposphere to higher altitudes, and they  
111 dissipate in the MLT region ( $\sim 60$ – $80$  km for the fast Kelvin waves and  $\sim 90$ – $110$  km for  
112 the UFKWs). Chang et al. (2010) used the NCAR Thermosphere Ionosphere Mesosphere

113 Electrodynamic General Circulation Model (TIME-GCM) to evaluate the impact of the  
114 UFKW on the thermosphere and ionosphere. Theoretical UFKW forcing was applied  
115 at the lower boundary of the model at  $\sim 30$  km. Their results indicated thermospheric  
116 mass density perturbations of 8–12% at 350 km altitude and low-latitude TEC pertur-  
117 bations of 25–50% in response to the UFKW that has amplitude of 20–40 m/s in the zonal  
118 wind in the MLT region. They also clarified that the thermospheric response is due to  
119 the direct propagation of the wave into the upper thermosphere, while the ionospheric  
120 effects are caused by the modulation of the dynamo electric field. Onohara et al. (2013),  
121 using an ionospheric wind dynamo model, showed that  $\sim 3$  day variations in the equa-  
122 torial vertical plasma drift velocity can be reproduced by forcing the model with a pa-  
123 rameterized UFKW and diurnal tide. Sassi et al. (2013), in their investigation of the Jan-  
124 uary 2009 SSW simulated by the Whole Atmosphere Community Climate Model eXtended  
125 version (WACCM-X), noted an enhancement of the UFKW in the MLT region during  
126 the SSW. Nystrom et al. (2018), based on a TIME-GCM simulation for April 2009, ex-  
127 plained how non-linear interactions between UFKWs and tides can lead to a rich wave  
128 spectrum in the MLT region. Triplett et al. (2019) used the TIE-GCM, which is sim-  
129 ilar to the TIME-GCM but with the lower boundary at  $\sim 97$  km. The model was forced  
130 with a theoretical UFKW at the lower boundary, which was shown to produce TEC per-  
131 turbations of  $\pm 10\%$  at low latitudes.

132 The present study also utilizes a numerical model to examine the UFKW in the  
133 middle and upper atmosphere. Specifically, we use the whole atmosphere model GAIA,  
134 which stands for Ground-to-topside model of Atmosphere and Ionosphere for Aeronomy.  
135 The main objectives of this study are to demonstrate model’s ability to reproduce UFKW  
136 events that actually occurred in the real atmosphere and to understand the nature of  
137 the ionospheric variability caused by the wave activity. In many previous simulations,  
138 the UFKW was generated by artificial forcing inserted at a certain height with a fixed  
139 oscillation period and zonal wavenumber and with a latitudinal structure of perturba-  
140 tions predicted by linear wave theory (Forbes, 2000; Chang et al., 2010; Onohara et al.,  
141 2013; Triplett et al., 2019). An advantage of this approach is to be able to easily isolate  
142 the wave effects by switching on and off the forcing in the model, but the downside is  
143 that it is not possible to make a direct comparison with observations for any particu-  
144 lar event. Only a few numerical studies used realistic forcing based on meteorological data  
145 to drive the UFKW (Sassi et al., 2013; Nystrom et al., 2018). Sassi et al. (2013) were

146 able to reproduce the UFKW observed in the SABER temperature at 100 km altitude  
 147 during January–February 2009. It needs to be remembered, however, that this was achieved  
 148 by constraining the WACCM-X for the entire middle and lower atmosphere (0–90 km)  
 149 with assimilation products. Nystrom et al. (2018) constrained the lower boundary of the  
 150 TIME-GCM at  $\sim 30$  km with meteorological reanalysis data for April 2009 and found  
 151 marked UFKW activity in the MLT region at 90–150 km. However, they did not make  
 152 a direct comparison with measurements. Therefore, it is uncertain at this point whether  
 153 numerical models are capable of reproducing the UFKW in the MLT region in response  
 154 to realistic forcing in the lower atmosphere. Besides, neither Sassi et al. (2013) nor Nystrom  
 155 et al. (2018) investigated the ionospheric response, which still needs to be validated in  
 156 the context of whole atmosphere modeling through direct comparisons with observations.  
 157 This study addresses these issues by the use of the GAIA model and observational data  
 158 from the middle atmosphere and ionosphere, which are described in the following sec-  
 159 tion. Section 3 presents our results regarding the UFKW in the MLT region and iono-  
 160 sphere. The performance of the model is also evaluated therein. In section 4, we discuss  
 161 the nature of the ionospheric variability during times of enhanced UFKW activity, based  
 162 on a case study of the August–September 2011 event. Summary and conclusions are pro-  
 163 vided in section 5.

## 164 **2 Model and Data**

### 165 **2.1 GAIA model**

166 GAIA is a physics-based numerical model of the Earth’s whole atmosphere (e.g.,  
 167 Jin et al., 2011; Miyoshi et al., 2011). The model simulates the dynamics, thermodynam-  
 168 ics, chemistry, and electrodynamics of the coupled atmosphere-ionosphere system from  
 169 the surface to the upper thermosphere/ionosphere. GAIA consists of three models that  
 170 are coupled to one another: a whole atmosphere GCM (Miyoshi & Fujiwara, 2003), an  
 171 ionosphere model (Shinagawa, 2011), and an electrodynamics model (Jin et al., 2008).  
 172 The whole atmosphere GCM has the horizontal resolution  $2.8^\circ$  in longitude and latitude  
 173 and the vertical resolution of a grid per 0.2 scale height, which is sufficient for resolv-  
 174 ing global-scale waves such as equatorial Kelvin waves and tides. The upper boundary  
 175 is at  $1.017 \times 10^{-9}$  hPa, which corresponds to 480–620 km altitude in our simulations. The  
 176 ionosphere model has the upper boundary at  $\sim 2,000$  km altitude. The electron density  
 177 is derived as a sum of the densities of  $O^+$ ,  $O_2^+$ ,  $N_2^+$ , and  $NO^+$ , and TEC is derived by

178 vertically integrating the electron density. The electrodynamics model solves a wind dy-  
 179 namo equation to calculate electric fields and currents in a tilted dipole magnetic field  
 180 configuration under the assumption of equipotential magnetic field lines.

181 The neutral atmosphere below 30 km is constrained with meteorological reanaly-  
 182 sis data provided by the Japan Meteorological Agency (Onogi et al., 2007; Kobayashi  
 183 et al., 2015) using a nudging technique similar to those used by Jin et al. (2012) and Miyoshi  
 184 et al. (2017). In this way, the model takes into account wave forcing from the lower at-  
 185 mosphere to the upper atmosphere including the ionosphere. The model also takes into  
 186 account time-dependent forcing by energetic solar radiation. The daily  $F_{10.7}$  index (Tapping,  
 187 2013) is used as a proxy of the solar EUV/UV flux, which dominates heating and ion-  
 188 ization processes in the upper atmosphere. Geomagnetically quiet conditions are real-  
 189 ized by setting the cross polar cap potential to a low and constant value of 30 kV through-  
 190 out the simulation. Therefore, the day-to-day variability in the model arises from me-  
 191 teorological and solar radiation forcings but not from magnetospheric forcing.

192 A wave analysis was performed to identify UFKWs and other global-scale waves.  
 193 At a given latitude, the amplitude  $A$  and phase  $\phi$  of waves with period  $\tau$  are expressed  
 194 in the following formula:

$$195 \sum_{s=-4}^4 A_s \cos \left[ \frac{\Omega}{\tau} t + s\lambda - \phi_s \right]. \quad (1)$$

196 Here  $\Omega$  is the rotation rate of the Earth ( $=2\pi/\text{day}$ ),  $t$  is the universal time (days),  $\lambda$  is  
 197 the longitude (radians), and  $s$  is the zonal wavenumber. Waves with eastward and west-  
 198 ward phase propagations correspond to  $s < 0$  and  $s > 0$ , respectively, and zonally symmet-  
 199 ric oscillations are  $s = 0$ . In the remainder of this paper, eastward- and westward-propagating  
 200 waves with zonal wavenumber  $s$  are also referred to as E $|s|$  and W $|s|$ , respectively. For  
 201 example, the UFKW is eastward-propagating with zonal wavenumber  $s = -1$  and hence  
 202 an E1 wave. Standing oscillations are, in this case, denoted as S0. For each day, least-  
 203 squares fitting was performed to GAIA data at a given latitude and height using time  
 204 windows that are three times the wave period.

## 205 **2.2 Geopotential height**

206 The geopotential height (GPH) measurements from the Microwave Limb Sounder  
 207 (MLS) aboard the Aura satellite (Waters et al., 2006; Schwartz et al., 2008) are used to  
 208 identify UFKW events as well as to validate UFKWs reproduced by GAIA. Aura is NASA's

209 ongoing satellite mission. The spacecraft was launched into a sun-synchronous low Earth  
210 orbit on July 15, 2004. The Aura/MLS provides measurements of GPH profiles for pres-  
211 sure levels from 261 hPa ( $\sim 9$  km) to 0.001 hPa ( $\sim 97$  km). Version 4.2 data (Livesey et  
212 al., 2017) during 2004–2019 were obtained from the Goddard Earth Sciences Data and  
213 Information Services Center (Acker & Leptoukh, 2007). A wave analysis was performed  
214 in a similar way as described for GAIA. The reader is referred to Yamazaki and Matthias  
215 (2019) for the detailed description of how the Aura/MLS GPH data were processed for  
216 the wave analysis.

217 It is noted that since the Aura satellite is in a Sun-synchronous orbit, the measure-  
218 ments are limited to two local solar times at  $\sim 1:45$  p.m. and  $\sim 1:45$  a.m. Therefore, the  
219 wave analysis is based on the data at these local times, which contrasts to the wave anal-  
220 ysis for GAIA that includes the data from all local times. Nevertheless, we found good  
221 agreement between the UFKW derived from GAIA GPH including all local times and  
222 that derived from GAIA GPH at local solar times of MLS measurements (i.e.,  $\sim 1:45$  p.m.  
223 and  $\sim 1:45$  a.m), indicating that the limited local-time coverage of Aura/MLS does not  
224 necessarily affect its ability to detect UFKWs. This justifies the comparison of UFKWs  
225 in GPH from Aura/MLS and GAIA (Section 3.1) despite the difference in local-time cov-  
226 erage.

### 227 **2.3 Total electron content**

228 TEC data from ESA’s GOCE mission are used to evaluate UFKW effects in the  
229 ionosphere. The GOCE satellite was launched into a sun-synchronous low Earth orbit  
230 on 17 March 2009 and operated in the thermosphere at an altitude of  $\sim 250$  km until Oc-  
231 tober 2013. The slant TEC was derived from Global Positioning System (GPS) obser-  
232 vations and then converted to the vertical TEC (Kervalishvili et al., 2018). The retrieval  
233 procedure is similar to that used earlier for deriving TEC from the GPS data for the CHAMP  
234 and Swarm satellites (e.g., Noja et al., 2013). A wave analysis was performed separately  
235 for the data from the ascending and descending orbital nodes, at  $\sim 7$  p.m. and  $\sim 7$  a.m.  
236 local solar time, respectively. This is because UFKW effects in the ionosphere are known  
237 to be local-time dependent (Gu et al., 2014). The wave analysis of GAIA TEC data was  
238 also performed separately at each local solar time. The resulting problem of aliasing will  
239 be discussed in 4.1. It is noted that GOCE TEC represents the vertical integration of  
240 the plasma density from the height of GOCE ( $\sim 250$  km) to the height of GPS satellites,

241 which differs from TEC measured at ground level. According to GAIA simulations, TEC  
 242 at 250 km is lower than the ground TEC only by  $\sim 10\%$ .

## 243 **2.4 Geomagnetic field**

244 Ground-based magnetometer data were obtained from five observatories: Huan-  
 245 cayo (12.0°S, 75.3°W), Tatuoca (1.2°S, 48.5°W), Addis Ababa (9.0°N, 38.8°E), Tirunelveli  
 246 (8.7°N, 77.8°E), Yap Island (9.3°N, 138.5°E). These observatories are longitudinally apart  
 247 but they are all located near the magnetic equator (i.e., within  $\pm 3^\circ$  magnetic latitudes).  
 248 Magnetic data from Huancayo and Addis Ababa are provided through INTERMAGNET  
 249 (Love & Chulliat, 2013), while Tirunelveli data are provided by the World Data Cen-  
 250 ter (WDC) for Geomagnetism, Mumbai. The Tatuoca data are provided by Observatório  
 251 Nacional (Morschhauser et al., 2017) and accessible from GFZ Data Services (Soares,  
 252 Matzka, & Pinheiro, 2018). The magnetometer at Yap Island belongs to the global mag-  
 253 netometer network MAGDAS (Yumoto & the MAGDAS Group, 2006) and the data are  
 254 accessible through SuperMAG (Gjerloev, 2012).

255 For each station, the magnetic northward (N) component of the geomagnetic field  
 256 was derived through a coordinate conversion. The data were corrected for magnetic dis-  
 257 turbances associated with large-scale magnetospheric currents, such as the ring current  
 258 and magnetotail current (e.g., Lühr et al., 2017). The correction was performed by sub-  
 259 tracting the external field obtained from the magnetic field model CHAOS-6 (Finlay et  
 260 al., 2016). Furthermore, quiet-day nighttime values were subtracted from the time se-  
 261 ries of N for each station, which removes the magnetic fields originating from the Earth's  
 262 core and lithosphere. The residual field  $\Delta N$  represents magnetic perturbations produced  
 263 by electric currents in the ionosphere. Since the observatories are close to the magnetic  
 264 equator,  $\Delta N$  is dominated by the effect of the equatorial electrojet, which is a narrow  
 265 band of a zonal current along the magnetic equator (e.g., Yamazaki & Maute, 2017). The  
 266 equatorial electrojet is closely associated with the equatorial zonal electric field gener-  
 267 ated through wind dynamo processes in the ionospheric E region (e.g., Alken, 2020).

### 268 3 Results

#### 269 3.1 UFKWs in the MLT region

270 Figure 1 shows the amplitude of the UFKW in GPH at 0.001 hPa ( $\sim 97$  km) in the  
 271 lower thermosphere during 2004–2019. The UFKW amplitude here is defined as the largest  
 272 amplitude of the E1 waves within periods of 2.25–3.75 days. The amplitude tends to be  
 273 largest over the equator and its latitudinal structure is symmetric about the equator. These  
 274 features are consistent with those reported earlier by G. Liu et al. (2019) based on SABER  
 275 temperature data at 110 km during 2002–2018. There are occasionally bursts of wave  
 276 activity with amplitudes exceeding 0.2 km at the equator, which is appreciably larger  
 277 than the typical  $1\sigma$  error in the amplitude ( $<0.05$  km) estimated by Yamazaki and Matthias  
 278 (2019). In what follows, we validate the performance of GAIA in reproducing UFKWs  
 279 in the MLT region. Our focus is on these three events that involve particularly strong  
 280 UFKW activity: (1) September 2010, (2) August–September 2011, and (3) December  
 281 2012–January 2013.

282 Figure 2 presents wave spectra from  $s=-2$  to  $s=+2$  at 0.001 hPa ( $\sim 97$  km) over  
 283 the equator during the September 2010 event. The left panel is derived from the Aura/MLS  
 284 observations while the right panel is from GAIA simulations. Enhanced wave activity  
 285 is seen throughout September 2010 for E1 waves with a period around 2.5 days, which  
 286 can be identified as UFKWs. Other spectral components are mostly on the background  
 287 level below 0.1 km, except there is some W1 wave activity with a period of 4–7 days at  
 288 end of August, which is likely due to the Rossby normal mode, the so-called quasi-6-day  
 289 wave (e.g., Gan et al., 2018; Gu, Ruan, et al., 2018). In Figures 3 and 4, wave spectra  
 290 are plotted in a similar format as Figure 2 but for the August–September 2011 event and  
 291 the December 2012–January 2013 event, respectively. In either case, the GAIA repro-  
 292 duces the temporal variation of UFKW activity well but with slightly lower amplitudes.

293 Figures 5a–5d compare the vertical structures of the observed and simulated UFKWs  
 294 during the August–September 2011 event. The amplitude and phase are derived for the  
 295 E1 wave with a period of 3.0 days. The GAIA captures the height growth and latitu-  
 296 dinal spread of the UFKW amplitude well. The phase structure of the UFKW in the MLT  
 297 region (above 1 hPa) is also well reproduced by GAIA. Similarly good agreement is ob-  
 298 tained between the Aura/MLS observations and GAIA simulations for the September  
 299 2010 event and the December 2012–January 2013 event. Figures 5e–5h show the model-

300 data comparisons of the UFKW amplitudes for these events. It is noted that the Decem-  
 301 ber 2012–January 2013 event involves three discrete bursts of UFKW activity (Figure  
 302 4) and in Figures 5g and 5h we highlight only the event of 7–15 January 2013, in which  
 303 GAIA shows the largest wave activity. The model-data comparisons of the UFKW phase  
 304 for the September 2010 event and the December 2012–January 2013 event are presented  
 305 in the supporting information (Figure S1).

### 306 **3.2 UFKWs in the thermosphere**

307 Since the GAIA model is shown to be able to reproduce UFKW activity in the MLT  
 308 region, which is well above the region constrained by meteorological reanalysis data (0–  
 309 30 km), we now use GAIA to investigate the UFKW activity for the entire atmosphere.  
 310 Figure 6 shows the amplitude and phase of the UFKW in the zonal wind (a, b), merid-  
 311 ional wind (c, d), and temperature (e, f) for the August–September 2011 event. UFKW  
 312 amplitudes in the zonal wind greater than 10 m/s are mainly confined within a latitude  
 313 range of  $\pm 30^\circ$  and an altitude range of 85–150 km. The peak amplitude of 35 m/s is found  
 314 at 103 km altitude near the equator. Amplitudes in the meridional wind are relatively  
 315 small, with the maximum value less than 10 m/s. The amplitude in the temperature reaches  
 316 its maximum value of 14 K at 111 km altitude near the equator. Compared to the zonal  
 317 wind amplitude, the temperature amplitude decays slowly with height above the ampli-  
 318 tude peak. Gu et al. (2014) reported an amplitude of  $\sim 30$  m/s in the zonal wind at 90–  
 319 100 km altitude and 15 K in the temperature at 100–104 km altitude for the same event  
 320 based on TIMED satellite measurements, which is in agreement with the GAIA results.

321 In the low-latitude MLT region, UFKW phases in the zonal wind and temperature  
 322 tend to be horizontally uniform and they show a downward phase propagation, which  
 323 is consistent with the upward energy propagation. The vertical wavelength is  $\sim 40$  km  
 324 for the altitude range of 60–110 km for both the zonal wind and temperature, which is  
 325 in agreement with earlier observations (e.g., Davis et al., 2012). In the upper thermo-  
 326 sphere, above 200 km or so, the phases are largely independent of height. The UFKW  
 327 phase in the meridional wind shows a complex pattern in the low and middle atmosphere  
 328 due to the small amplitude. In the upper thermosphere, the meridional wind phase is  
 329 anti-symmetric about the equator.

330 The vertical and horizontal structures of the UFKW in the zonal wind, meridional  
 331 wind and temperature presented in Figures 6a–6f are in good agreement with those by  
 332 Chang et al. (2010) for an idealized TIME-GCM simulation. Similar results are obtained  
 333 for the September 2010 event and the December 2012–January 2013 event. The UFKW  
 334 amplitudes in the zonal wind are presented in Figures 6g and 6h for these events. In both  
 335 cases, the maximum amplitude in the zonal wind exceeds 30 m/s in the MLT region at  
 336 the equator. Given that the GAIA model tends to underestimate the amplitude in the  
 337 geopotential height in the MLT region (Figures 2–4), the actual zonal wind amplitude  
 338 could be larger. In Figures S2 and S3 of the supporting information, we plot the ampli-  
 339 tudes and phases of the UFKW in the zonal wind, meridional wind, and temperature  
 340 for the September 2010 event and the December 2012–January 2013 event.

### 341 3.3 Ionospheric variability during UFKW events

342 We now turn our attention to the response of the ionosphere to the UFKW. GAIA’s  
 343 capability to reproduce the ionospheric response is verified through comparisons between  
 344 observed and simulated UFKWs in the ionosphere. Ionospheric variability associated with  
 345 the UFKW may be extracted from parameters such as TEC and equatorial zonal elec-  
 346 tric field (EEF) using the formula (1). However, unlike the neutral atmosphere, the re-  
 347 sponse of the ionosphere to the UFKW is highly dependent on local solar time (e.g., Chang  
 348 et al., 2010; Gu et al., 2014). Therefore, fitting of (1) to observational and model data  
 349 is performed at a fixed local solar time. In the following, we present the spectral com-  
 350 ponent corresponding to the UFKW ( $s=-1$ ,  $\tau\sim 3$ ) in the ionosphere, as derived from the  
 351 GOCE TEC observations and GAIA simulations, during the August–September 2011  
 352 event and the December 2012–January 2013 event. Unfortunately, there is a large gap  
 353 in the GOCE data during the September 2010 event, and thus our analysis is limited to  
 354 the other two events.

355 Figure 7 compares the UFKW spectral component in TEC observed by the GOCE  
 356 satellite and simulated by the GAIA model during the August–September 2011 event.  
 357 It is noted that in Figure 7, different color scales are adopted for different panels. The  
 358 top panels (Figures 7a and 7b) present the background TEC at 7 p.m. local solar time,  
 359 which corresponds to the ascending node of the GOCE orbit. These TEC values are cal-  
 360 culated as the zonal and temporal mean within a 9-day moving window, which is also  
 361 the time window used for calculating the amplitudes of the UFKW spectral component

362 in Figures 7c–7f. In both the GOCE and GAIA results, the background TEC has a lo-  
 363 cal maximum on both sides of the magnetic equator, reflecting the equatorial ionization  
 364 anomaly (EIA) structure that is usually formed during the daytime due to the equato-  
 365 rial plasma fountain effect. The background TEC in GAIA is somewhat higher than that  
 366 in GOCE observations, and also the EIA crests are located at higher latitudes in GAIA  
 367 than those derived from GOCE data. This could be due to an overestimation of the day-  
 368 time equatorial zonal electric field in GAIA, in other words, an overestimation of the equa-  
 369 torial plasma fountain effect. It is seen in Figures 7c and 7d that the amplitude of the  
 370 UFKW spectral component in TEC also exhibits a double-peak structure. Local max-  
 371 ima of the amplitude occur at poleward edges of the EIA crests. The maximum ampli-  
 372 tudes are  $\sim 8$  TECU in the GOCE data and  $\sim 6$  TECU in the GAIA model, which cor-  
 373 respond to  $\sim 30\%$  and  $\sim 20\%$  of the background TEC, respectively (see Figures 7e and  
 374 7f).

375 Figure 8 presents model-data comparisons for the December 2012–January 2013  
 376 event. The maximum amplitudes are, again,  $\sim 8$  TECU ( $\sim 30\%$ ) in the GOCE data and  
 377  $\sim 6$  TECU ( $\sim 20\%$ ) in the GAIA model, occurring at poleward edges of the EIA crests.  
 378 The GOCE observations suggest that the ionospheric response is strongest around 5–  
 379 10 February 2013, while in GAIA, the ionospheric response is more pronounced from end  
 380 of December 2012 towards early January. This discrepancy can be attributed to the un-  
 381 derestimation of UFKW forcing during early February 2013 (see Figure 4).

382 It is noted that there was an SSW event in January 2013 (Goncharenko et al., 2013).  
 383 The central date of the SSW was on 7 January (Siddiqui et al., 2018) and associated iono-  
 384 spheric perturbations have been observed in the following days (Goncharenko et al., 2013;  
 385 Jonah et al., 2014). This coincides with the period of enhanced UFKW activity in the  
 386 middle atmosphere (Figure 4) and ionosphere (Figure 9). However, it is unclear if the  
 387 UFKW event in January 2013 is related to the SSW, as UFKW bursts are also observed  
 388 before and after the SSW. The relationship between SSW and UFKW is still under de-  
 389 bate (e.g., England et al., 2012; G. Liu et al., 2012; Sassi et al., 2013; Phanikumar et al.,  
 390 2014).

391 Figure 9 is the same as Figure 7 but for 7 a.m. local solar time, which corresponds  
 392 to the descending node of the GOCE orbit. The GOCE TEC data reveal an enhance-  
 393 ment in the amplitude of the UFKW spectral component at  $0\text{--}20^\circ$  magnetic latitudes

394 during 30 August–7 September 2011. This coincides with the time of enhanced UFKW  
 395 activity observed in the ascending node. The absolute amplitude is small ( $\sim 1.5$  TECU  
 396 at maximum) but the relative amplitude exceeds 10% of the background TEC. The GAIA  
 397 does not reproduce the ionospheric response at this local solar time, possibly because  
 398 of the underestimation of UFKW forcing in the model. Similarly, enhanced UFKW ac-  
 399 tivity ( $\sim 1.5$  TEC,  $\sim 10\%$ ) was observed in the descending node during 29 January–10  
 400 February 2013, and the GAIA model did not reproduce the observation (Figure 4S in  
 401 the supporting information).

402 Gu et al. (2014) analyzed global TEC maps derived from ground GPS data and  
 403 investigated UFKW signatures during 2011. They showed the dependence of UFKW sig-  
 404 natures in TEC on local solar time and magnetic latitude around the time of the August–  
 405 September 2011 event, which gives us the opportunity to further validate the GAIA re-  
 406 sults. We show in Figures 10a and 10c the local solar time and magnetic latitude depen-  
 407 dence of the background TEC and the amplitude of the UFKW spectral component in  
 408 TEC during 27 August–4 September 2011. Therein, the TEC values are evaluated at the  
 409 ground level, not at 250 km altitude as in Figures 7–9. Our results are in good agree-  
 410 ment with those presented by Gu et al. (2014) (see their Figures 5c and 5d).

411 Gu et al. (2014) also presented the dependence of the UFKW amplitude in the elec-  
 412 tron density ( $N_e$ ) on magnetic latitude and on altitude using COSMIC data during 8–  
 413 22 February 2011. In Figures 10b and 10d, we show similar results but for the August–  
 414 September 2011 event. Despite the difference in the time intervals examined, our results  
 415 agree qualitatively with those by Gu et al. (2014) (see their Figures 6a and 6b). In both  
 416 results, the UFKW amplitude in  $N_e$  show local maxima at the poleward and equator-  
 417 ward edges of the EIA crests. This can be understood as a consequence of the equato-  
 418 rial plasma fountain effect. That is, when an eastward dynamo electric field is imposed  
 419 on the dayside ionosphere, not only the electron density at the EIA crests increases but  
 420 also the location of the EIA crests moves poleward (Stolle et al., 2008). Thus, as the zonal  
 421 electric field oscillates due to the UFKW, largest perturbations in the electron density  
 422 tend to occur where the density gradient is most significant, which is not at the EIA crests  
 423 but at their poleward and equatorward edges.

424 Figures 11a and 11b compare the spectra for the observed and simulated TEC at  
 425 7 p.m. local solar time at 250 km altitude near the northern EIA crest during the August–

426 September 2011 event. In both cases, a spectral peak is visible at  $s=-1$  and a period  
 427 of  $\sim 3$  days. A similar peak is found in the spectra for the daytime equatorial zonal elec-  
 428 tric field at 110 km (Figure 11c) and for the equatorial zonal wind at the same height  
 429 (Figure 11d). These results suggest that the equatorial zonal electric field is modulated  
 430 by the zonal wind, and subsequently the plasma distribution in the EIA region is mod-  
 431 ulated by the equatorial zonal electric field. As demonstrated by Yamazaki et al. (2014),  
 432 the zonal wind at 100–120 km altitude in the equatorial region is effective in perturb-  
 433 ing the dayside zonal electric field. The UFKW amplitude in the zonal wind happens  
 434 to be largest in that region (Figure 6), allowing the UFKW to efficiently drive ionospheric  
 435 variability. In Figure 11c, the spectra for the equatorial zonal electric field are computed  
 436 using only the daytime data between 7 a.m. and 5 p.m. local solar time. This is because  
 437 the response of the equatorial zonal electric field to the zonal wind is different during day-  
 438 time and nighttime (Jin et al., 2008). Indeed, spectral patterns are different for daytime  
 439 and nighttime equatorial zonal electric fields, although zonal wind spectra are consistent  
 440 between daytime and nighttime. This is demonstrated in the supporting information (Fig-  
 441 ure S5).

#### 442 **4 Discussion**

443 In the previous section, we have validated GAIA’s ability to reproduce ionospheric  
 444 variability during UFKW events. In this section, we will investigate the simulated UFKW  
 445 signatures in the ionosphere during the August–September 2011 event in more detail.  
 446 We first discuss potential aliasing from other waves and tides into the UFKW spectrum  
 447 component (i.e.,  $s=-1$  and  $\tau\sim 3$  days) in the ionosphere. We then discuss the nature of  
 448 the ionospheric variability during the UFKW event and possible detection of UFKW sig-  
 449 natures using ground-based measurements. To facilitate the discussion, we have performed  
 450 two numerical experiments as summarized in Table 1. In these numerical experiments,  
 451 the neutral component of GAIA is de-coupled from the ionospheric and electrodynam-  
 452 ics models. The atmospheric temperature, winds, and composition are analyzed using  
 453 the Fourier transform and reconstructed with the wave components having zonal wavenum-  
 454 bers from  $s=-5$  to  $s=+5$  only. In the first experiment “LARGE\_WAVES”, the ionospheric  
 455 and electrodynamic models are forced with the reconstructed neutral fields. The main  
 456 difference between the original GAIA simulation and LARGE\_WAVES is that GAIA in-  
 457 cludes the waves that have relatively small spatial scales ( $s>+5$  and  $s<-5$ ), which are

458 excluded in LARGE\_WAVES. Also, GAIA takes into account the feedback process from  
 459 the ionosphere to the neutral atmosphere, which is ignored in LARGE\_WAVES. The sec-  
 460 ond experiment “NO\_UFKW” is the same as LARGE\_WAVES but the E1 waves at pe-  
 461 riods 1.5–4.5 days are removed using the method of (Hayashi, 1971). This eliminates the  
 462 UFKW in the neutral atmosphere and its direct influence on the ionosphere.

#### 463 4.1 Aliasing

464 In Section 3.3, the ionospheric variability associated with the UFKW was evalu-  
 465 ated by fitting the formula (1) to GOCE and GAIA TEC at a fixed local solar time. These  
 466 fits can suffer from aliasing with various combinations of zonal wavenumber  $s$  and pe-  
 467 riod  $\tau$ . Here we discuss and identify potential sources of aliasing, and later we will make  
 468 an attempt to separate the aliasing sources from UFKW signatures in the ionosphere based  
 469 on the controlled simulations, LARGE\_WAVES and NO\_UFKW.

470 Using the local solar time  $t_{LT}$  ( $=t + \frac{\lambda}{\Omega}$ ), a wave  $\cos(\frac{\Omega}{\tau}t + s\lambda)$  can be expressed  
 471 as

$$472 \cos \left[ \left( s - \frac{1}{\tau} \right) \lambda + \frac{\Omega}{\tau} t_{LT} \right]. \quad (2)$$

473 At a fixed local solar time,  $\frac{\Omega}{\tau}t_{LT}$  is a constant, and thus (2) is a function of longitude.  
 474 In principle, the waves that have the same longitudinal dependence are indistinguish-  
 475 able. For the UFKW,  $s=s_u$  ( $=-1$ ) and  $\tau=\tau_u$  ( $=\sim 3$ ), and one cannot distinguish the UFKW  
 476 from other waves that satisfy:

$$477 \left| s - \frac{1}{\tau} \right| = s_u - \frac{1}{\tau_u}. \quad (3)$$

478 For global-scale waves, zonal wavenumber  $s$  needs to be an integer and period  $\tau$  needs  
 479 to be positive. Under these restrictions, there is a series of combinations  $(s, \tau)$  that sat-  
 480 isfy (3). Table 2 lists combinations  $(s, \tau)$  for the waves from which aliasing can occur  
 481 into the UFKW spectral component ( $s_u=-1, \tau_u=2-4$ d) at a fixed local solar time. As  
 482 it turns out,  $\tau$  is negative if  $s < 0$ , so that aliasing does not occur from eastward-propagating  
 483 waves. For  $s \geq 0$ ,  $\tau$  is mostly less than one day. The only wave with  $\tau \geq 1.0$ d is  $s=+2$  and  
 484  $\tau=1.33-2.00$ d. The mixed Rossby-gravity wave, also known as the quasi-2-day wave, is  
 485 westward-propagating with  $s=+2, s=+3$ , or  $s=+4$  (e.g., Gu, Dou, et al., 2018), and thus  
 486 the  $s=+2$  component is a potential source of aliasing. In general, quasi-2-day waves are  
 487 strongest in the summer hemisphere. The  $s=+2$  component in the MLT region attains

488 its maximum amplitude in early August in the Northern Hemisphere and in mid Novem-  
 489 ber in the Southern Hemisphere (Pancheva et al., 2018).

490 None of the waves in Table 2 has an overlap with tidal periodicities ( $\tau=1\text{d}$ ,  $\frac{1}{2}\text{d}$ ,  $\frac{1}{3}\text{d}$ ,  
 491  $\frac{1}{4}\text{d}$ ), thus aliasing from tidal waves do no occur as long as their amplitudes and phases  
 492 stay constant. However, tides in the MLT region are known to be highly variable, and  
 493 their amplitudes and phases can change significantly from one day to the next (e.g., Miyoshi  
 494 & Fujiwara, 2003; Fang et al., 2013). Short-term tidal variability will inevitably contribute  
 495 to the spectral components listed in Table 2. One of the causes of day-to-day tidal vari-  
 496 ability is the non-linear interaction between tides and other waves, which generate sec-  
 497 ondary waves at periods close to tidal periodicities and hence modulate the tides (e.g.,  
 498 Chang et al., 2011; Pedatella et al., 2012). In the following, we consider aliasing by the  
 499 waves generated through the non-linear interaction of the UFKW and tides.

500 According to the theory of Teitelbaum and Vial (1991), the non-linear interaction  
 501 of two global-scale waves can give rise to secondary waves with frequencies and zonal wavenum-  
 502 bers that are the sums and differences of those of the interacting waves. Thus, the non-  
 503 linear interaction between an UFKW  $\cos\left(\frac{\Omega}{\tau_u}t + s_u\right)$  and tidal wave  $\cos(n\Omega t + s\lambda)$  leads  
 504 to secondary waves:

$$505 \cos\left[\left(\frac{\Omega}{\tau_u} \pm n\Omega\right)t + (s_u \pm s)\lambda\right], \quad (4)$$

506 where  $n=1, 2, 3$  represent oscillations with periods corresponding to 1d (diurnal tide),  
 507  $\frac{1}{2}\text{d}$  (semidiurnal tide), and  $\frac{1}{3}\text{d}$  (terdiurnal tide), respectively. In the local-time frame, this  
 508 becomes:

$$509 \cos\left[\left(s_u \pm s - \frac{1}{\tau_u} \mp n\right)\lambda + \left(\frac{\Omega}{\tau_u} \pm n\Omega\right)t_{LT}\right], \quad (5)$$

510 Therefore, at a fixed local solar time, aliasing into the UFKW  $(s_u, \tau_u)$  occurs if

$$511 |s_u \pm s - \frac{1}{\tau_u} \mp n| = s_u - \frac{1}{\tau_u}. \quad (6)$$

512 Since  $s$  and  $n$  are required to be an integer and a natural number, respectively, the only  
 513 possible solution is:

$$514 n = s, \quad (7)$$

515 that is, migrating tides. In other words, secondary waves generated by the non-linear  
 516 interaction of the UFKW and migrating tides cannot be distinguished from the UFKW  
 517 when the wave signatures are sampled at a fixed local solar time. For example, the non-  
 518 linear interaction between the UFKW ( $s=-1, \tau=3\text{d}$ ) and migrating diurnal tide ( $s=+1,$

519  $\tau=1\text{d}$ ) leads to secondary waves with ( $s=0, \tau=0.75\text{d}$ ) and ( $s=+2, \tau=1.5\text{d}$ ), both of which  
 520 can be found in Table 2. In fact, for each wave in Table 2, it is possible to find a pair  
 521 of the UFKW and migrating tide that can be a potential source of aliasing.

522 Aliasing effects are expected to reduce when the wave signatures are sampled over  
 523 a range of local solar time instead of a single local solar time. To confirm this, we gen-  
 524 erated synthetic data by sampling the waves listed in Table 2 over a range of local so-  
 525 lar time (e.g., 9 a.m.–3 p.m.). The amplitude of the UFKW spectral component ( $s=-1,$   
 526  $\tau=3\text{d}$ ) was calculated by fitting (1) to the synthetic data. The derived amplitude is com-  
 527 pared with that calculated with the synthetic data sampled at a fixed local solar time  
 528 (e.g., 12 noon). The amplitude ratio  $\gamma$  is listed in Table 2 for ranges of local solar time  
 529 3h, 6h, and 12h. As expected, aliasing effects are smaller when the data from a wider  
 530 range of local solar time are included in the wave analysis. For instance, aliasing from  
 531 the wave ( $s=+1, \tau=0.40\text{--}0.44\text{d}$ ) can be largely avoided, if the data are included for the  
 532 whole daytime period, which corresponds to a local-time range of 12h.

533 The controlled simulations, LARGE\_WAVES and NO\_UFKW, help us understand  
 534 aliasing effects in the UFKW spectral component that we presented in Section 3.3. Fig-  
 535 ure 12a is the same as Figure 11d but derived from LARGE\_WAVES, showing the zonal  
 536 wavenumber spectrum of the equatorial zonal wind at 110 km during the August–September  
 537 2011 event. It is noted that the wave analysis includes the zonal wind data from all lo-  
 538 cal solar times. The results from GAIA (Figure 11d) and LARGE\_WAVES (Figure 12a)  
 539 are almost identical, indicating that the feedback effect from the ionosphere to the neu-  
 540 tral atmosphere, which is taken into account in GAIA but not in LARGE\_WAVES, does  
 541 not play a significant role for global-scale waves at 110 km. Figure 12b shows the spec-  
 542 trum derived from NO\_UFKW, which eliminates the E1 waves with periods  $\sim 3$  days.  
 543 The spectral pattern is consistent with that of LARGE\_WAVES in Figure 12a except  
 544 for the absence of the UFKW.

545 Figure 12c presents the zonal wavenumber spectrum of the equatorial zonal elec-  
 546 tric field as derived from LARGE\_WAVES. It is noted that the only daytime data (7 a.m.–  
 547 5 p.m.) are included in the wave analysis. The result shows a spectral peak at  $s=-1$  and  
 548  $\tau\sim 3\text{d}$ , in good agreement with the GAIA simulation (Figure 11c). In the NO\_UFKW  
 549 run (Figure 12d), the spectral peak is reduced below the 95% confidence level. These re-

sults suggest that the spectral peak in the daytime equatorial zonal electric field at  $s=-1$  and  $\tau\sim 3\text{d}$  during the August–September 2011 event is directly caused by the UFKW.

Figures 12e and 12f show zonal wavenumber spectra of TEC at 7 p.m. local solar time as derived from LARGE\_WAVES and NO\_UFKW, respectively. The LARGE\_WAVES simulation case reveals enhanced wave activity at  $s=-1$  and  $\tau\sim 3\text{d}$ , which is consistent with the GAIA result (Figure 11b) as well as GOCE observation (Figure 11a). It is interesting to note that wave activity at  $s=-1$  and  $\tau\sim 3\text{d}$  is also seen in NO\_UFKW, which excludes forcing by the UFKW. There are at least three significant peaks in the E1 spectrum at periods 2–4 days. Each peak has a spectral amplitude  $\sim 1.8$  TEC, which is about half the amplitude of the UFKW spectral component in LARGE\_WAVE ( $\sim 4$  TEC). These spectral peaks in NO\_UFKW TEC are due to aliasing from westward-propagating waves with  $\tau\leq 2.0\text{d}$  as listed in Table 2. These results suggest that UFKW activity in the ionosphere observed at a fixed local solar time is contributed not only by the UFKW but also by other waves, such as secondary waves due to the non-linear interaction between the UFKW and migrating tides as discussed earlier.

## 4.2 Ground observer perspective

Up to now, we have mainly considered the ionospheric response to the UFKW from a perspective of the GOCE satellite at a fixed local solar time. We now discuss the wave effect from a ground observer perspective. For a ground observer at a fixed geographical location, the UFKW manifests as a  $\sim 3$ -day oscillation of atmospheric parameters. Therefore, the question is whether the  $\sim 3$ -day variation caused by the UFKW is substantially larger than  $\sim 3$ -day variations due to other causes.

Figure 13a depicts the temporal and longitudinal variations of the equatorial zonal wind at 110 km during 15 August–20 September 2011 as derived from the LARGE\_WAVES simulation. A 24h average was applied to the wind data at each longitude in order to suppress the variations associated with tides with periods less than one day. The zonal wind shows large day-to-day variability about  $\pm 60$  m/s. There is a hint of E1 wave activity with a period of  $\sim 3$  days from end of August towards beginning of September. Figure 13d is the same as Figure 13a but a bandpass filter is applied at each longitude to extract the variations with periods 1.5–4.5 days. Enhanced E1 wave activity is more clearly visible. Figure 13g presents the corresponding result from the NO\_UFKW simulation,

581 which does not include E1 waves with periods of 1.5–4.5 days. In this case,  $\sim 3$ -day vari-  
 582 ability can arise from  $\sim 3$ -day waves with other zonal wavenumbers (i.e., W5–W1, S0,  
 583 E2–E5) as well as from secondary waves due to the non-linear interaction between tides  
 584 and  $\sim 3$ -day waves. In Figure 13g,  $\sim 3$ -day variability is much weaker than in Figure 13d,  
 585 indicating that the UFKW is the leading cause of  $\sim 3$ -day variations for a ground observer  
 586 at a fixed longitude. Similar results were obtained for equatorial zonal winds at lower  
 587 altitudes in the MLT region (not shown here). Thus, it is possible to detect UFKW sig-  
 588 natures using a ground-based instrument such as a meteor radar (e.g., Vincent, 1993).

589 The results are presented in a similar format for the equatorial zonal electric field  
 590 at 110 km in Figures 13b, 13e, 13h, and 13k, and for TEC at  $20^\circ$  magnetic latitude in  
 591 Figures 13c, 13f, 13i, and 13l. For these ionospheric parameters, the contributions of the  
 592 UFKW (Figures 13h and 13i) and non-UFKW sources (Figures 13k and 13l) are com-  
 593 parable, and the relative contribution of the two depends on longitude. The  $\sim 3$ -day vari-  
 594 ations due to the UFKW and other sources could strengthen or cancel each other de-  
 595 pending on their phases. Thus, a ground observer does not necessarily detect enhanced  
 596  $\sim 3$ -day ionospheric variability even during times of enhanced UFKW activity. The same  
 597 conclusion was reached when the ionospheric parameters at a fixed local solar time were  
 598 analyzed at each longitude. Figure S6 in the supporting information shows plots sim-  
 599 ilar to those in Figure 13 but derived using the equatorial zonal electric field at 12 noon  
 600 local solar time and TEC at 7 p.m. local solar time.

601 It may be noted in Figures 13k and 13l that the amplitude of  $\sim 3$ -day ionospheric  
 602 variations caused by the UFKW depends on longitude. This is, in part, due to the lon-  
 603 gitudinal variation of the geomagnetic field. The Earth’s main magnetic field plays an  
 604 important role for the ionospheric electrodynamics (Takeda, 1996; Cnossen & Richmond,  
 605 2013) and its zonal structure can be imprinted in ionospheric parameters (Yue et al., 2013).  
 606 Since the GAIA model assumes a simple dipole magnetic field that is tilted against the  
 607 Earth rotation axis, the longitudinal asymmetry of ionospheric variations associated with  
 608 the UFKW could be more pronounced in the real geomagnetic field configuration.

### 609 **4.3 Ground-based magnetometer detection of the UFKW**

610 The results presented above suggest that during times of high UFKW activity, an  
 611 enhancement occurs in the spectral component of the ionospheric variability correspond-

612 ing to the UFKW (i.e., period  $\tau \sim 3$  days and zonal wavenumber  $s=-1$ ) (Figures 11 and  
 613 12) but this does not necessarily lead to an enhancement in  $\sim 3$ -day ionospheric varia-  
 614 tions at a fixed longitude due to the presence of other  $\sim 3$ -day variability (Figure 13).  
 615 Keeping this in mind, we examine ground-based magnetometer data during the UFKW  
 616 event of August–September 2011 and discuss the possible detection of UFKW signatures.

617 Figure 14a shows the distribution of the ground-based magnetometers used in this  
 618 study. As mentioned earlier, these five observatories are all located in the vicinity of the  
 619 magnetic equator, and thus the magnetic perturbations in the magnetic-northward com-  
 620 ponent ( $\Delta N$ ) are predominantly due to the equatorial electrojet, which is closely asso-  
 621 ciated with the equatorial zonal electric field. Examples of  $\Delta N$  data are plotted in Fig-  
 622 ure 14b for Huancayo and Addis Ababa. In general,  $\Delta N$  is very small at night because  
 623 of the absence of the equatorial electrojet due to low ionospheric conductivities, and  $\Delta N$   
 624 is usually positive during the day, reflecting the eastward current flow of the equatorial  
 625 electrojet, with a daily maximum around 11 a.m. local solar time. The daily maximum  
 626 values exhibit day-to-day variability, which is mostly due to day-to-day variations of the  
 627 equatorial zonal electric field (Yamazaki et al., 2018).

628 Figures 14c–14g show wavelet power spectra of  $\Delta N$  at different locations. The wavelet  
 629 analysis is based on the technique detailed by Torrence and Compo (1998). A similar  
 630 method has been used in previous studies to examine spectral features of the equatorial  
 631 electrojet and discuss their possible connections with atmospheric waves (e.g., Jarvis,  
 632 2006; Ramkumar et al., 2009; Gurubaran et al., 2011). In our wavelet analysis, the data  
 633 are included for both daytime and night time. The results are similar when the night  
 634 time data are excluded. The wavelet spectrum of  $\Delta N$  at Huancayo (Figure 14d) reveals  
 635 the presence of relatively large  $\sim 3$ -day variations from end of August to beginning of Septem-  
 636 ber 2011. The spectrum at the closest observatory, Tatuoca (Figure 14f), shows a sim-  
 637 ilar pattern but with maximum activity of  $\sim 3$ -day variations on 2 September slightly later  
 638 than that at Huancayo on 31 August. Although the two observatories are less than  $30^\circ$   
 639 apart in longitude, the behavior of the equatorial electrojet could be different as discussed  
 640 in detail by Soares, Yamazaki, et al. (2018). In both Huancayo and Tatuoca results, there  
 641 is a broader spectral peak at 5–10 days. Evidence suggests that geomagnetic activity is  
 642 responsible for these variations. In Figure 14h, the wavelet spectrum is presented for the  
 643 geomagnetic activity index  $Kp$ . The spectral peak around 5–10 days is visible from end  
 644 of August 2011 for the rest of the period. It is known that the equatorial electrojet varies

645 with geomagnetic activity (e.g., Yamazaki & Kosch, 2015; Xiong et al., 2016). The equa-  
 646 torial electrojet is also known to vary with solar activity (e.g., Matzka et al., 2017). We  
 647 plot the wavelet spectrum of the solar activity index  $F_{10.7}$  in Figure 14i. On the time  
 648 scale of our interest, variations of  $F_{10.7}$  are mainly at the period of the solar rotation and  
 649 its harmonics (27, 13.5, and 9 days) and thus would make little contribution to  $\sim 3$ -day  
 650 variations of the equatorial electrojet. The wavelet spectra of  $\Delta N$  for Addis Ababa, Tirunelveli,  
 651 and Yap Island are presented in Figures 14c, 14e and 14g, respectively. They are only  
 652 in partial agreement with one another and with those for Huancayo (Figure 14d) and  
 653 Tatuoca (Figure 14f). For instance, at Addis Ababa (Figure 14c),  $\sim 3$ -day and 5–10 day  
 654 variations, which are identified in the Huancayo and Tatuoca data, are barely visible in  
 655 the wavelet spectrum. The lack of the 5–10 day variations can arise from the fact that  
 656 the response of the equatorial electrojet to geomagnetic activity varies with longitude  
 657 because of local-time differences (e.g., Maute et al., 2015). At Tirunelveli (Figures 14e)  
 658 and Yap Island (Figures 14g), variations at a period of 2–3 days are seen in wavelet spec-  
 659 tra but they occur a few days after those at Huancayo and Tatuoca. These discrepan-  
 660 cies highlight the difficulty to confidently identify the UFKW activity from the magnetic  
 661 data obtained at a single location.

662 Next, the zonal wavenumber spectrum is derived by fitting the formula (1) to the  
 663 daytime  $\Delta N$  data at the five observatories. The zonal wavenumbers only from  $-3$  to  $+3$   
 664 are considered due to the limited longitudinal coverage of the stations (Figure 14a). The  
 665 result presented in Figure 14j reveals a significant peak at periods 2.5–3 days with zonal  
 666 wavenumber  $s=-1$ . This is consistent with the result for the daytime equatorial zonal  
 667 electric field derived from the GAIA model (Figure 11c). We showed earlier that this spec-  
 668 tral peak is directly caused by the UFKW based on controlled simulations (Figures 12c  
 669 and 12d). This is the first time that magnetic signatures of the UFKW in the equato-  
 670 rial electrojet are detected. It supports our hypothesis from the numerical experiments  
 671 that UFKW activity leads to an enhancement of the spectral component in the ionosphere  
 672 with period  $\tau \sim 3$  days and zonal wavenumber  $s=-1$ , although  $\sim 3$ -day variations are not  
 673 necessarily observed at a fixed longitude. This underlines the importance of multipoint  
 674 measurements when UFKW signatures in the ionosphere are investigated using ground-  
 675 based observations. A multipoint-measurement approach was used in the past in attempts  
 676 to observe ionospheric signatures associated with the quasi-2-day wave, quasi-6-day wave,

677 and fast Kelvin wave from the ground (Pancheva et al., 2006, 2008). Our results sup-  
 678 port such an approach for studying the UFKW.

## 679 5 Summary and Conclusions

680 In this study, we use the whole atmosphere model GAIA to simulate equatorial Kelvin  
 681 waves with a period of  $\sim 3$  days, also known as ultra-fast Kelvin waves (UFKWs). We  
 682 examine the UFKW events of September 2010, August–September 2011, and December  
 683 2012–January 2013, which are particularly strong according to the 16 years of geopotential  
 684 height measurements by the Aura Microwave Limb Sounder (MLS) (Figure 1). As  
 685 we constrain the lower layers of GAIA below 30 km with meteorological reanalysis data,  
 686 the model is able to reproduce main characteristics of UFKWs in the mesosphere and  
 687 lower thermosphere (MLT) region as observed by the Aura/MLS (Figures 2–5). Accord-  
 688 ing to the GAIA results, the zonal wind amplitude exceeds 30 m/s in the lower thermo-  
 689 sphere (95–110 km) during these events (Figure 6), which is consistent with the earlier  
 690 observations by Gu et al. (2014) during the August–September 2011 event.

691 GAIA is also able to reproduce wave activity in the total electron content (TEC)  
 692 retrieved from GPS observations by the GOCE satellite at  $\sim 7$  p.m. local solar time (Fig-  
 693 ures 7 and 8). The GOCE data reveal the amplitude of the UFKW spectral component  
 694 being up to 8 TECU (30% of the background) at  $\pm 15^\circ$  magnetic latitudes, while the model  
 695 data show the smaller amplitude up to 6 TECU (20% of the background) at  $\pm 20^\circ$  mag-  
 696 netic latitudes. The GOCE data also show the wave activity at  $\sim 7$  a.m. local solar time  
 697 with the amplitude up to 1.5 TECU (10% of the background), which the GAIA model  
 698 does not capture well (Figure 9). The dependence of the amplitude of the UFKW spec-  
 699 tral component in TEC on magnetic latitude, local solar time, and altitude during the  
 700 August–September 2011 event (Figure 10) is consistent with the earlier report by Gu et  
 701 al. (2014). The TEC response to the UFKW can be explained by the modulation of the  
 702 equatorial zonal electric field (and thus the equatorial plasma fountain) by the zonal wind  
 703 (Figure 11), confirming the earlier finding by Chang et al. (2010).

704 Numerical experiments are performed for the August–September 2011 event to ex-  
 705 amine the nature of the ionospheric variability associated with the UFKW. When the  
 706 UFKW is excluded from the neutral atmosphere, the amplitude of the UFKW spectral  
 707 component ( $s = -1$ ,  $\tau \sim 3$ ) in the ionosphere is substantially reduced (Figure 12). This es-

708 tablishes that the UFKW causes eastward-propagating  $\sim 3$ -day ionospheric variations with  
709 zonal wavenumber 1. The UFKW spectral component in the ionosphere at a fixed lo-  
710 cal time is subject to aliasing from other waves, such as secondary waves due to the non-  
711 linear interaction between the UFKW and migrating tides (Table 2), but the total con-  
712 tribution of those waves to the UFKW spectral component is less than the direct con-  
713 tribution by the UFKW.

714 Numerical results also suggest that it can be difficult for a ground observer to dis-  
715 tinguish between  $\sim 3$ -day ionospheric variations associated with the UFKW and those  
716 caused by other sources, as they have comparable amplitudes even during times of en-  
717 hanced UFKW activity (Figure 13). We highlight this issue using ground-based mag-  
718 netometer measurements of the equatorial electrojet during the UFKW event of August–  
719 September 2011. The wavelet spectra of the magnetometer data at different observato-  
720 ries are only in partial agreement, with or without a spectral peak around 3 days. De-  
721 spite that, the combination of the data reveals the predominance of the wave component  
722 with a period of  $\sim 3$  days and zonal wavenumber  $s=-1$ , corresponding to the UFKW (Fig-  
723 ure 14). This is the first detection of the UFKW in the equatorial electrojet. We em-  
724 phasize that it is important to include measurements from multiple stations when UFKW  
725 signatures in the ionosphere are investigated using ground-based observations.

## 726 Acknowledgments

727 We thank the NASA Goddard Earth Sciences (GES) Data and Information Ser-  
728 vices Center (DISC) (<https://disc.gsfc.nasa.gov/>) for making the Aura/MLS geopo-  
729 tential height data (DOI: 10.5067/Aura/MLS/DATA2008) available. We also thank the  
730 European Space Agency (ESA) for providing the GOCE TEC data, which can be down-  
731 loaded from <http://eo-virtual-archive1.esa.int/GOCE.TEC.html>. The GAIA sim-  
732 ulations were performed using the computer system at the Research Institute for Infor-  
733 mation Technology of Kyushu University. The numerical data used in this study are avail-  
734 able from GFZ Data Services (<http://dataservices.gfz-potsdam.de/portal/>). The  
735 GAIA simulations relied on the meteorological data provided from the Japanese 55-year  
736 Reanalysis (JRA-55) project carried out by the Japan Meteorological Agency (JMA).  
737 The magnetic data for Huancayo and Addis Ababa can be downloaded from the INTER-  
738 MAGNET website ([www.intermagnet.org](http://www.intermagnet.org)). We thank Geophysical Institute of Peru, Ad-  
739 dis Ababa University, and University of Paris for supporting the operation of magnetic

740 field measurements at these observatories. The magnetic data for Tirunelveli can be down-  
 741 loaded from the website at the WDC Mumbai (<http://wdciig.res.in>). We thank the  
 742 Director, Indian Institute of Geomagnetism (IIG), India for making the Tirunelveli data  
 743 available. The Tatuoca magnetic data are accessible from GFZ Data Services ([http://](http://dataservices.gfz-potsdam.de/panmetaworks/showshort.php?id=escidoc:3504909)  
 744 [dataservices.gfz-potsdam.de/panmetaworks/showshort.php?id=escidoc:3504909](http://dataservices.gfz-potsdam.de/panmetaworks/showshort.php?id=escidoc:3504909)).  
 745 The magnetic data for Yap Island can be downloaded from the SuperMAG website ([supermag](http://supermag.jhuapl.edu)  
 746 [.jhuapl.edu](http://supermag.jhuapl.edu)). The geomagnetic activity index  $Kp$  was provided by the GFZ German  
 747 Research Centre for Geosciences (<https://www.gfz-potsdam.de/en/kp-index/>). The  
 748 solar activity index  $F_{10.7}$  was downloaded from the SPDF OMNIWeb database ([https://](https://omniweb.gsfc.nasa.gov)  
 749 [omniweb.gsfc.nasa.gov](https://omniweb.gsfc.nasa.gov)). Wavelet software provided by C. Torrence and G. Compo is  
 750 available at <http://paos.colorado.edu/research/wavelets/>. YY and YM was sup-  
 751 ported by the Deutsche Forschungsgemeinschaft (DFG) grant YA-574-3-1 and the Japan  
 752 Society for the Promotion of Science (JSPS) grant, respectively, under the joint German-  
 753 Japanese project. GBS was supported by Coordenação de Aperfeiçoamento de Pessoal  
 754 de Nível Superior – Brasil (CAPES) – Finance Code 1799579 (PhD research grant).

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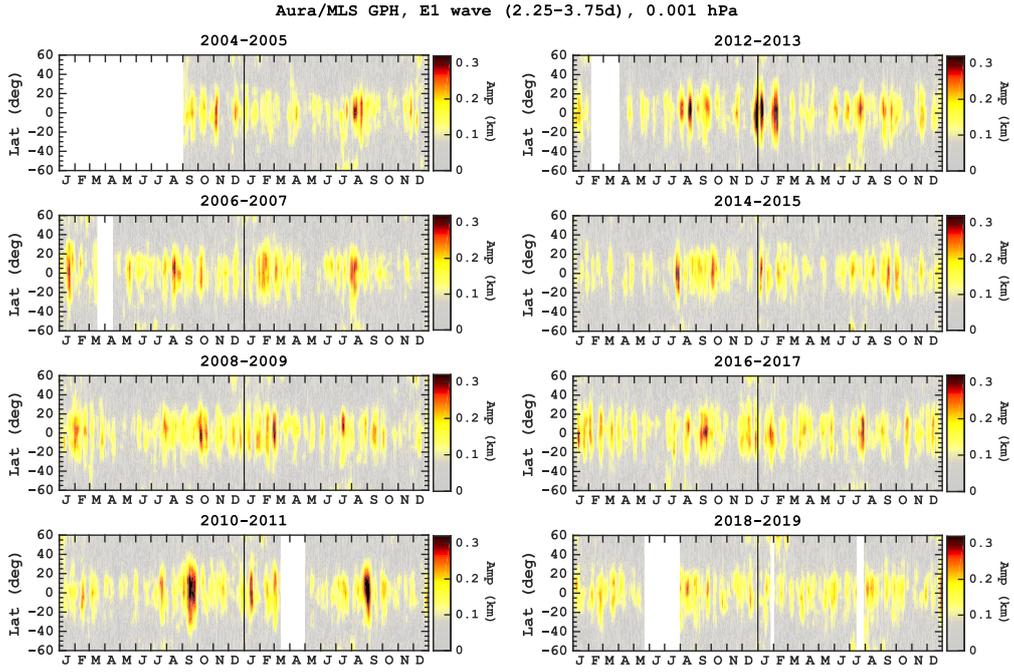
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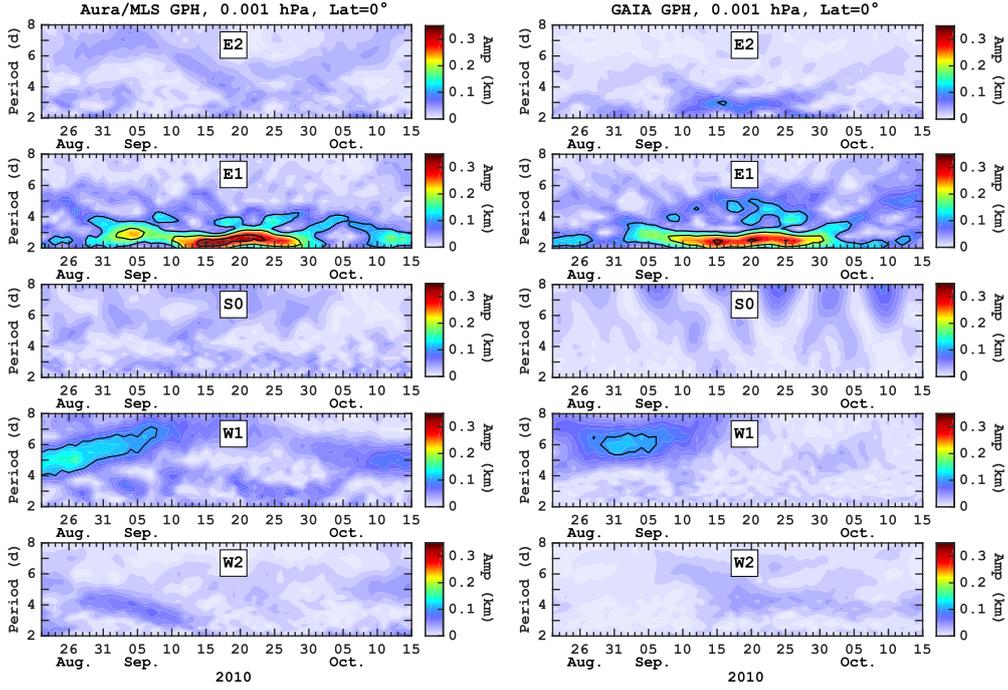
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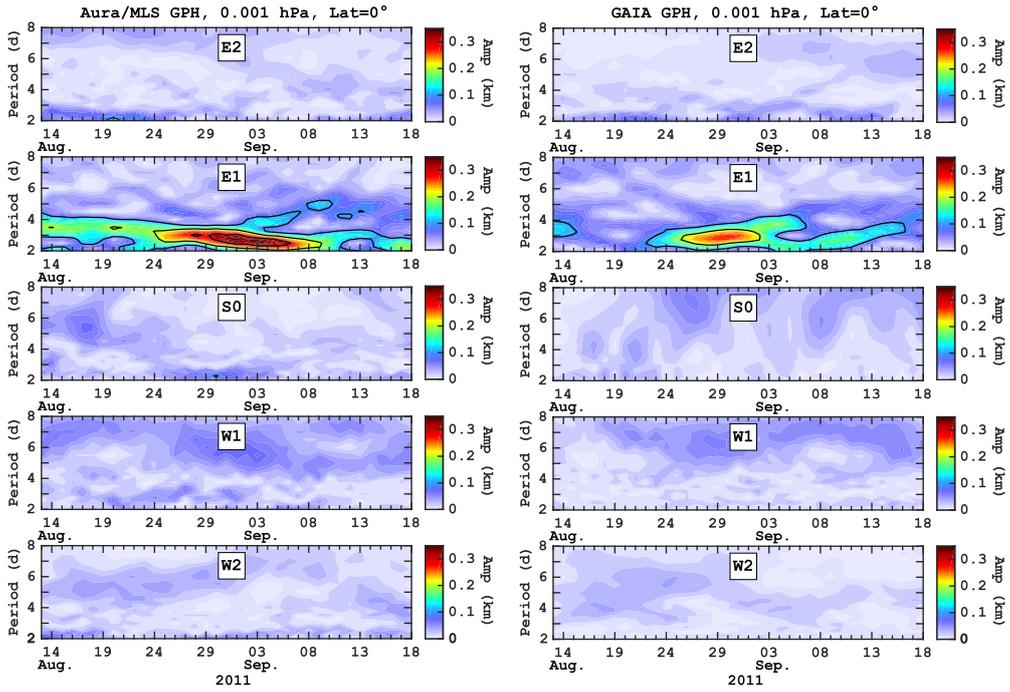
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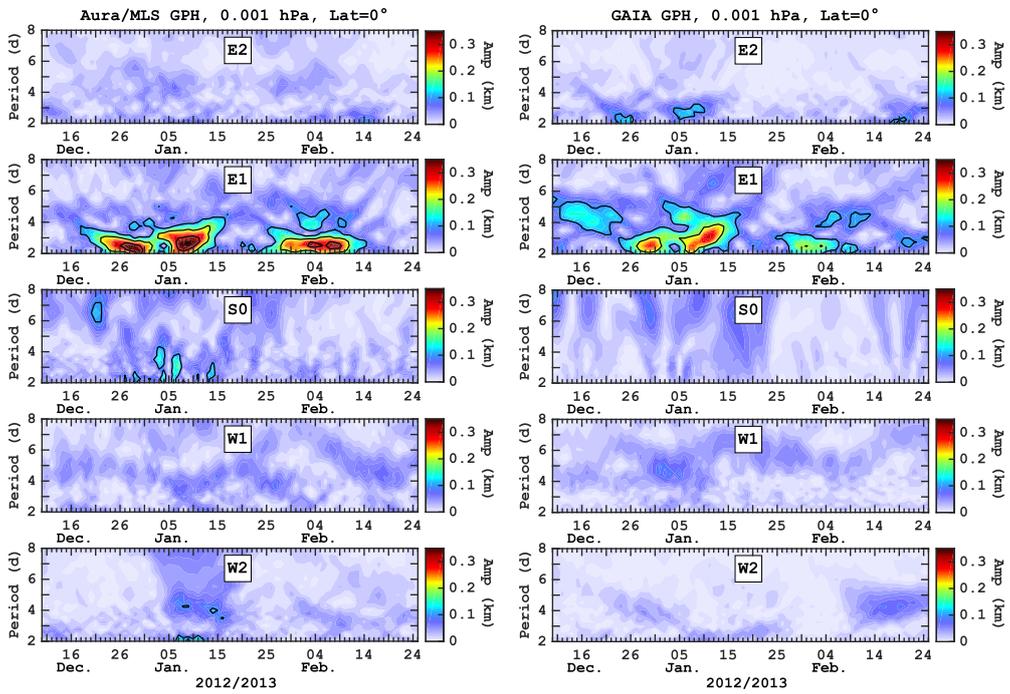
**Figure 1.** Amplitude of the ultra-fast Kelvin wave (UFW) as derived from the geopotential height (GPH) measurements at 0.001 hPa ( $\sim 97$  km altitude) by the Aura Microwave Limb Sounder during 2004–2019. The UFW amplitude is defined as the largest amplitude of the eastward-propagating waves with zonal wavenumber 1 within periods of 2.25–3.75 days.



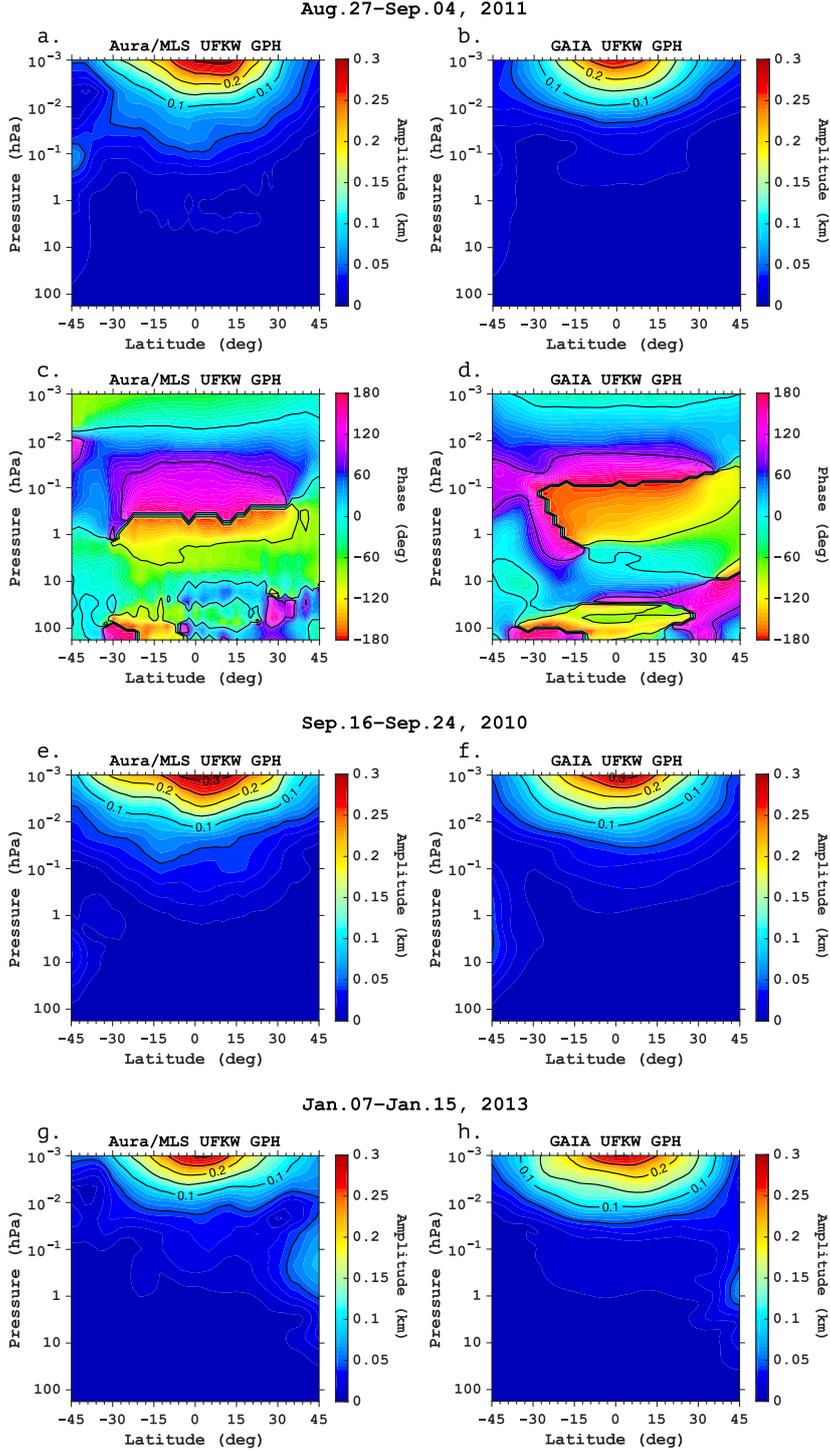
**Figure 2.** Time versus period diagrams of the wave spectrum derived from the geopotential height (GPH) at 0.001 hPa ( $\sim 97$  km altitude) over the equator for zonal wavenumber  $s=-2$  (E2),  $s=-1$  (E1),  $s=0$  (S0),  $s=+1$  (W1), and  $s=+2$  (W2) during the ultra-fast Kelvin wave (UFKW) event of September 2010. The left panels are from the Aura Microwave Limb Sounder measurements while the right panels are from the GAIA model.



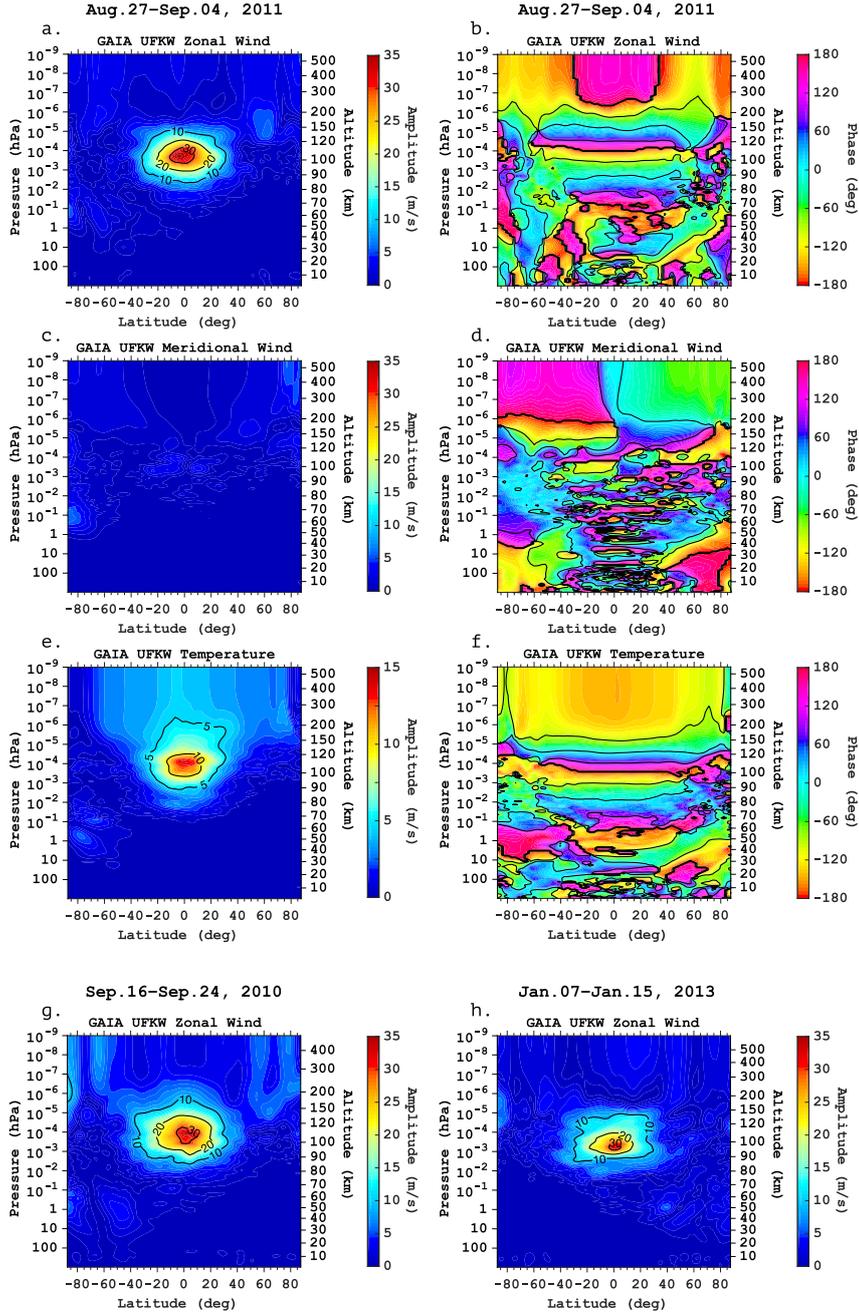
**Figure 3.** Same as Figure 2 except for the ultra-fast Kelvin wave (UFWK) event of August–September 2011.



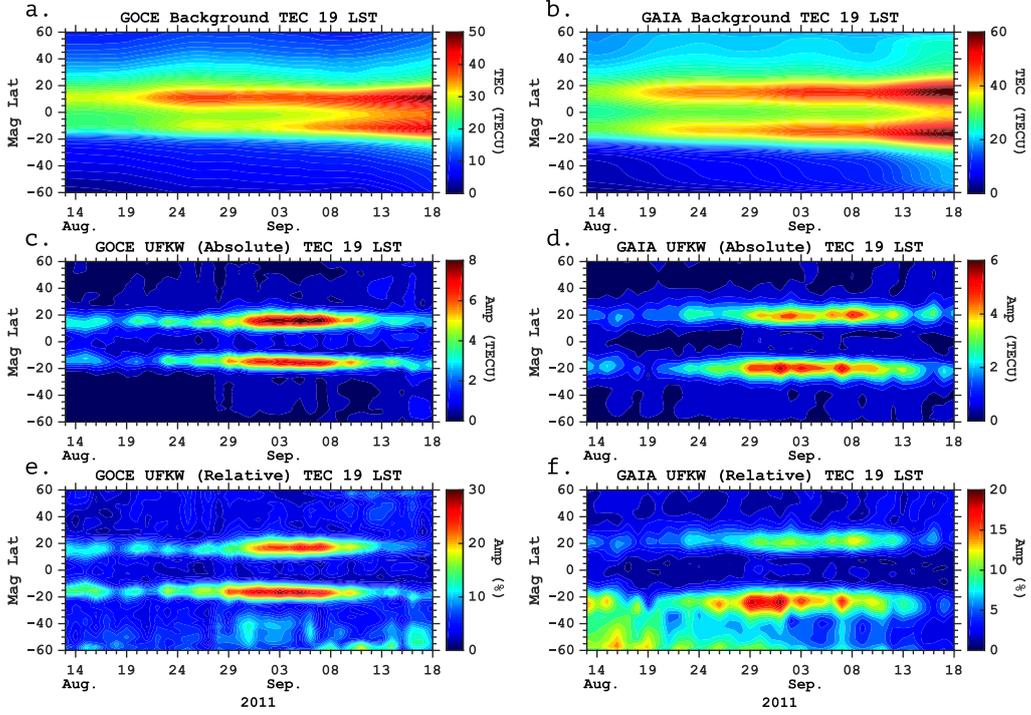
**Figure 4.** Same as Figure 2 except for the ultra-fast Kelvin wave (UFWK) event of December 2012–January 2013.



**Figure 5.** Latitude versus height structures of the ultra-fast Kelvin wave (UFKW) in the geopotential height (GPH) during the August–September 2011 event (a–d), the September 2010 event (e, f), and the December 2012–January 2013 event (g, h). The left panels are from the Aura Microwave Limb Sounder (MLS) measurements while the right panels are from the GAIA model. The panels (a, b, and e–h) show the amplitude while the panels (c, d) show the phase. The vertical range covers the pressure levels from 261 to 0.001 hPa, which corresponds to approximately 9–97 km altitude.



**Figure 6.** Latitude versus height structures of the ultra-fast Kelvin wave (UFKW) in the zonal wind (a, b, g, h), meridional wind (c, d), and temperature (e, f) derived from the GAIA model. The panels (a–f) are for the UFKW event of August–September 2011 event, showing the amplitude on the left and the phase on the right. The panels (g) and (h) show the UFKW amplitude in the zonal wind during the September 2010 event and the December 2012–January 2013 event, respectively. The UFKW is defined as the eastward-propagating wave with a period of 3.0 days and zonal wavenumber 1 for the August–September 2011 event and the December 2012–January 2013 event, while for the September 2010 event, the wave with a period of 2.5 days is considered.



**Figure 7.** Comparison of the total electron content (TEC) at 7 p.m. local solar time derived from the GOCE measurements (a, c, e) and GAIA model (b, d, f). The panels (a, b) show the background total electron content (TEC) as defined here as the temporal and zonal mean calculated at each latitude using a 9-day moving window. The panels (c, d) show the amplitude of the ultra-fast Kelvin wave (UFKW) spectral component in TEC calculated at each latitude using the 9-day moving window. The UFKW spectral component is defined as the largest amplitude of the eastward-propagating waves with zonal wavenumber 1 within periods 2.25–3.75 days. The panels (e, f) show the relative amplitude of the UFKW spectral component in TEC with respect to the corresponding background TEC value. Note that color scales are different for different panels.

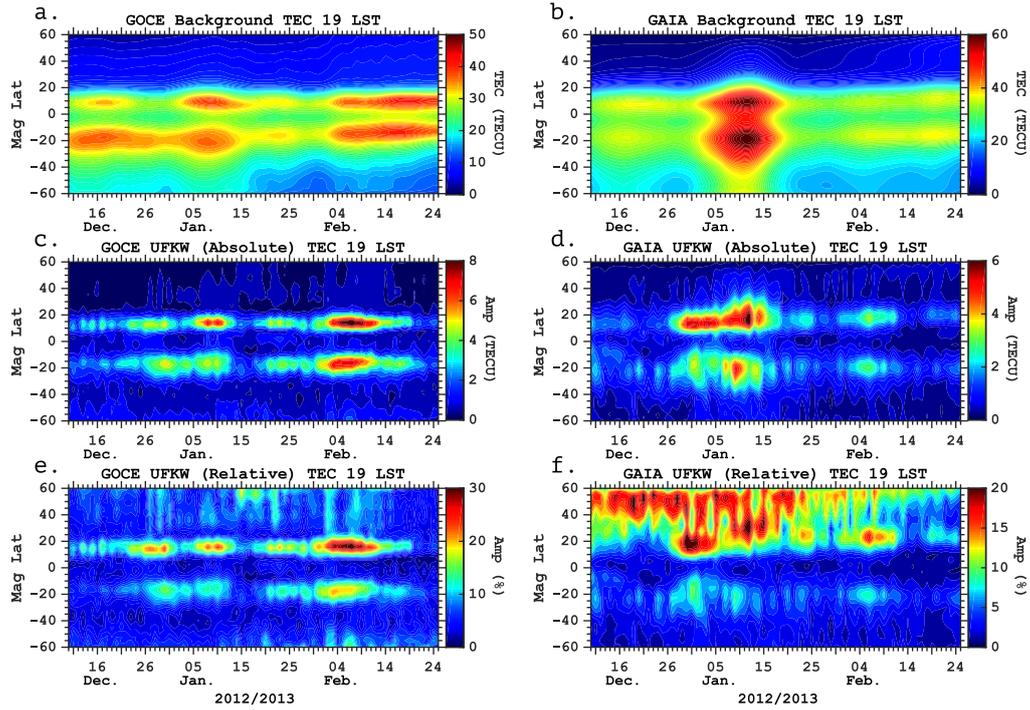


Figure 8. Same as Figure 7 except for the December 2012–January 2013 event.

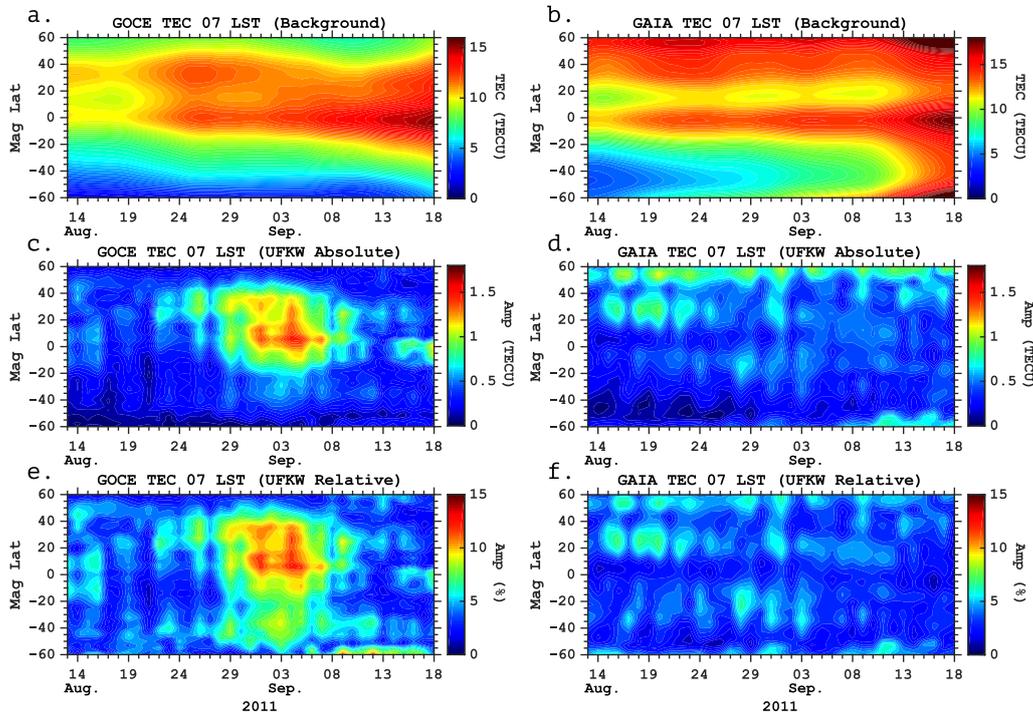
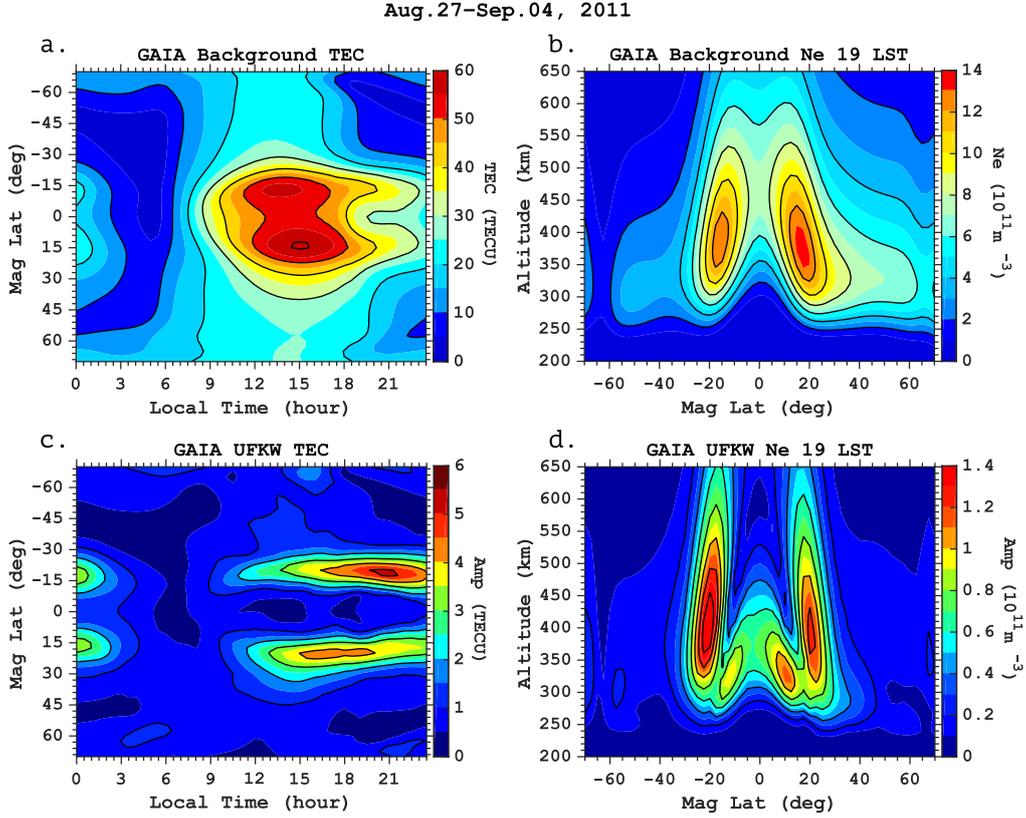
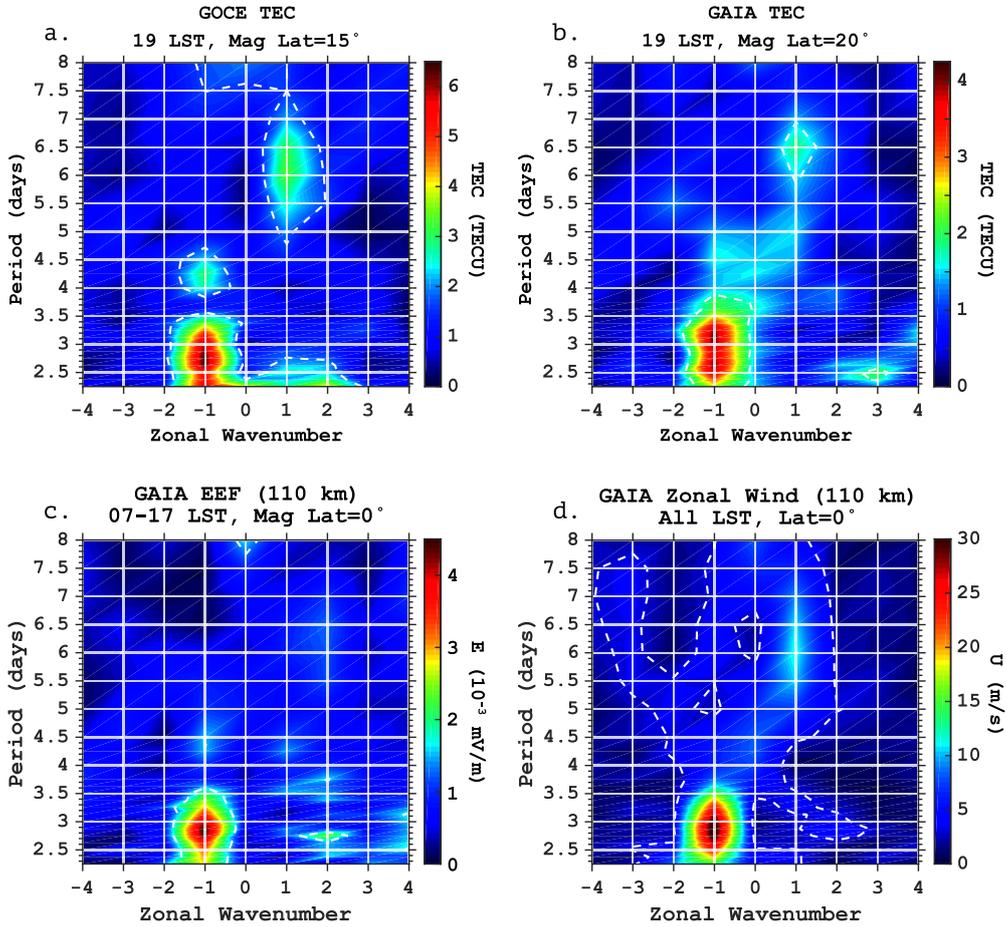


Figure 9. Same as Figure 7 except for 7 a.m. local solar time.



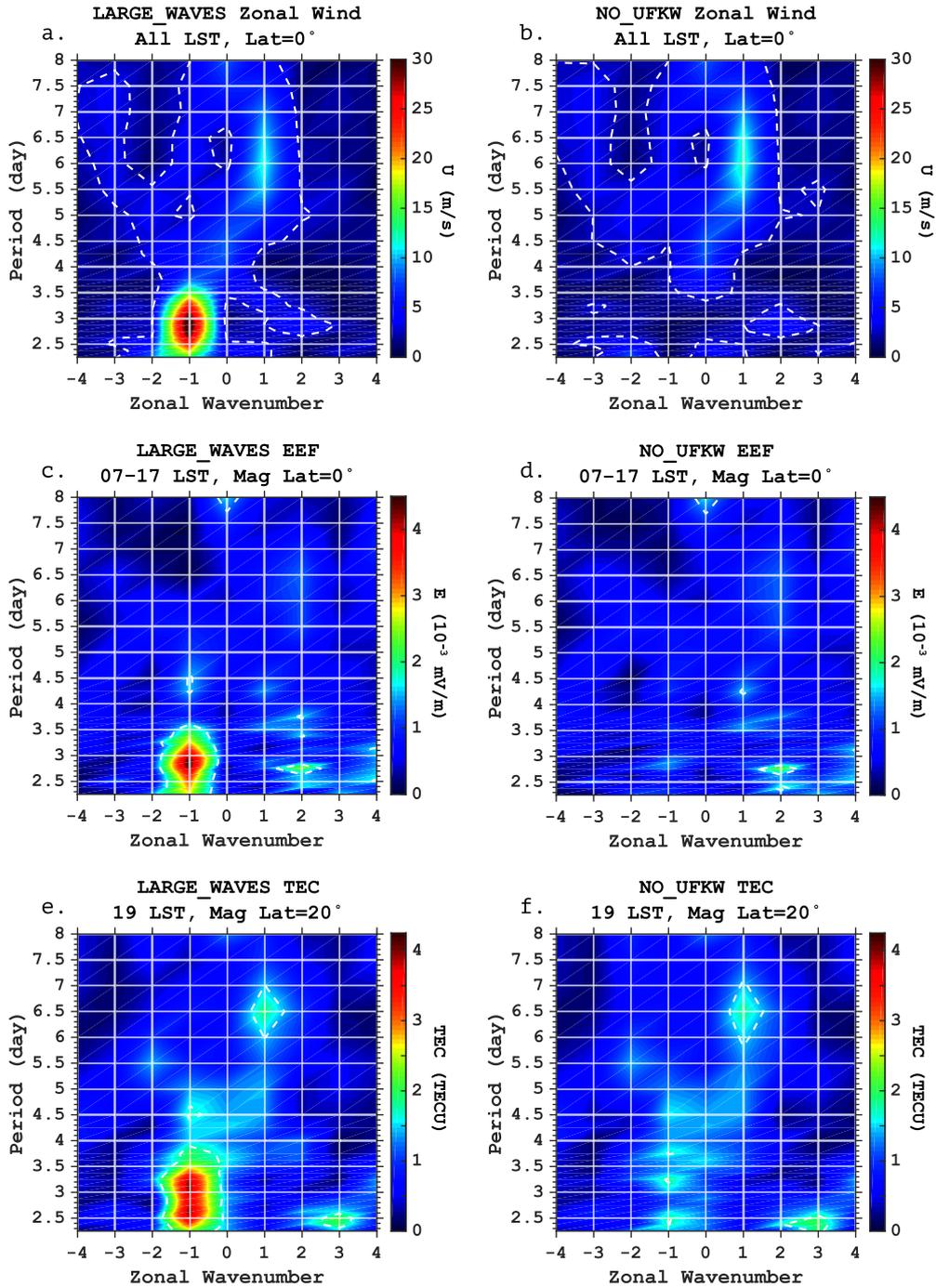
**Figure 10.** Spatial structure of the amplitude of the ultra-fast Kelvin wave (UFKW) spectral component in total electron content (TEC) and electron density ( $N_e$ ) during the August–September 2011 event. (a) Local-time and magnetic-latitude dependence of the background TEC. (b) Magnetic-latitude and height dependence of the background electron density at 7 p.m. local solar time. (c) Same as (a) except for the the amplitude of the UFKW spectral component in TEC. (d) Same as (b) except for the amplitude of the UFKW spectral component in the electron density.

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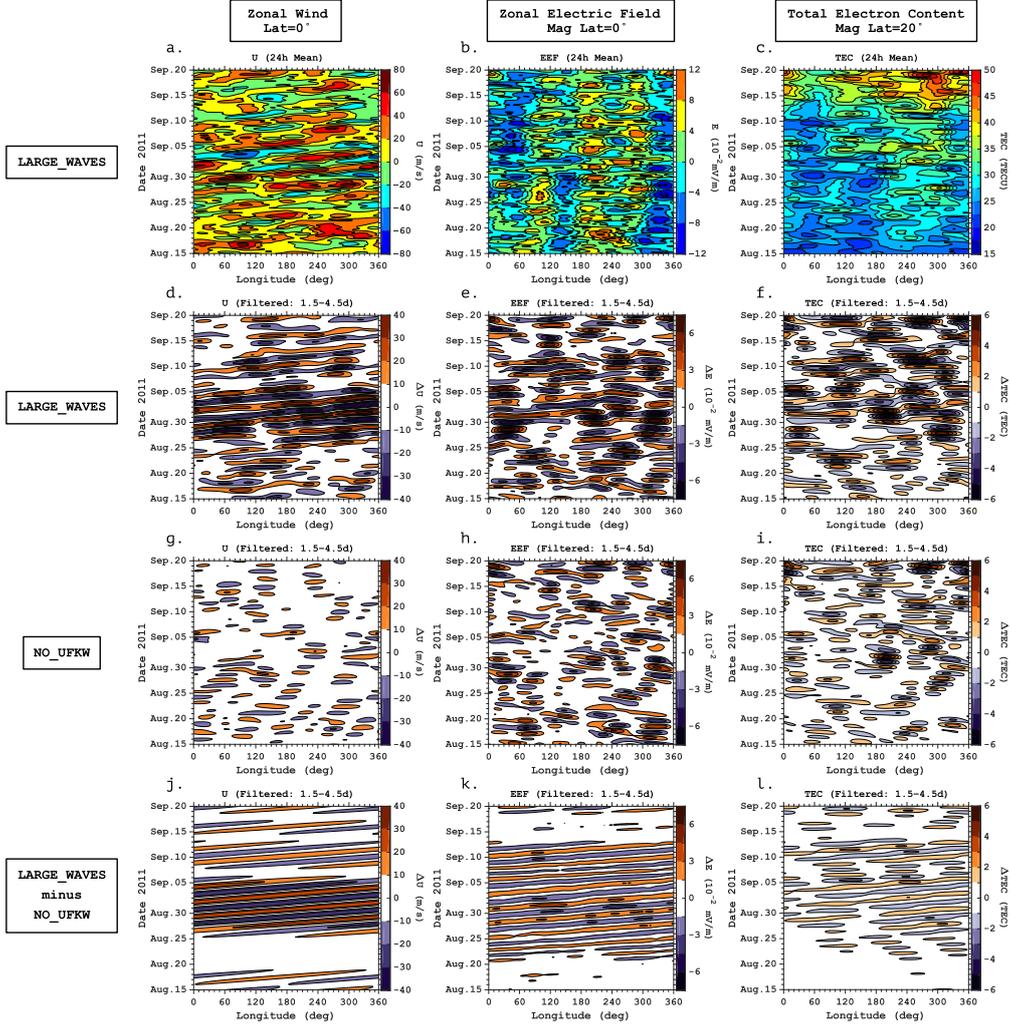


**Figure 11.** Wavenumber versus period spectra during the ultra-fast Kelvin wave event of August–September 2011. The panel (a) is for the total electron content (TEC) derived from the GOCE measurements at 7 p.m. local solar time and 15° magnetic latitude. The panel (b) shows the same as (a) except for TEC at 20° magnetic latitude from the GAIA model. The panel (c) is also from GAIA but for the equatorial zonal electric field (EEF) between 7 a.m. and 5 p.m. local solar time at 110 km altitude. The panel (d) is for the zonal wind at the equator at 110 km altitude. The white dashed lines correspond to the 95% confidence level.

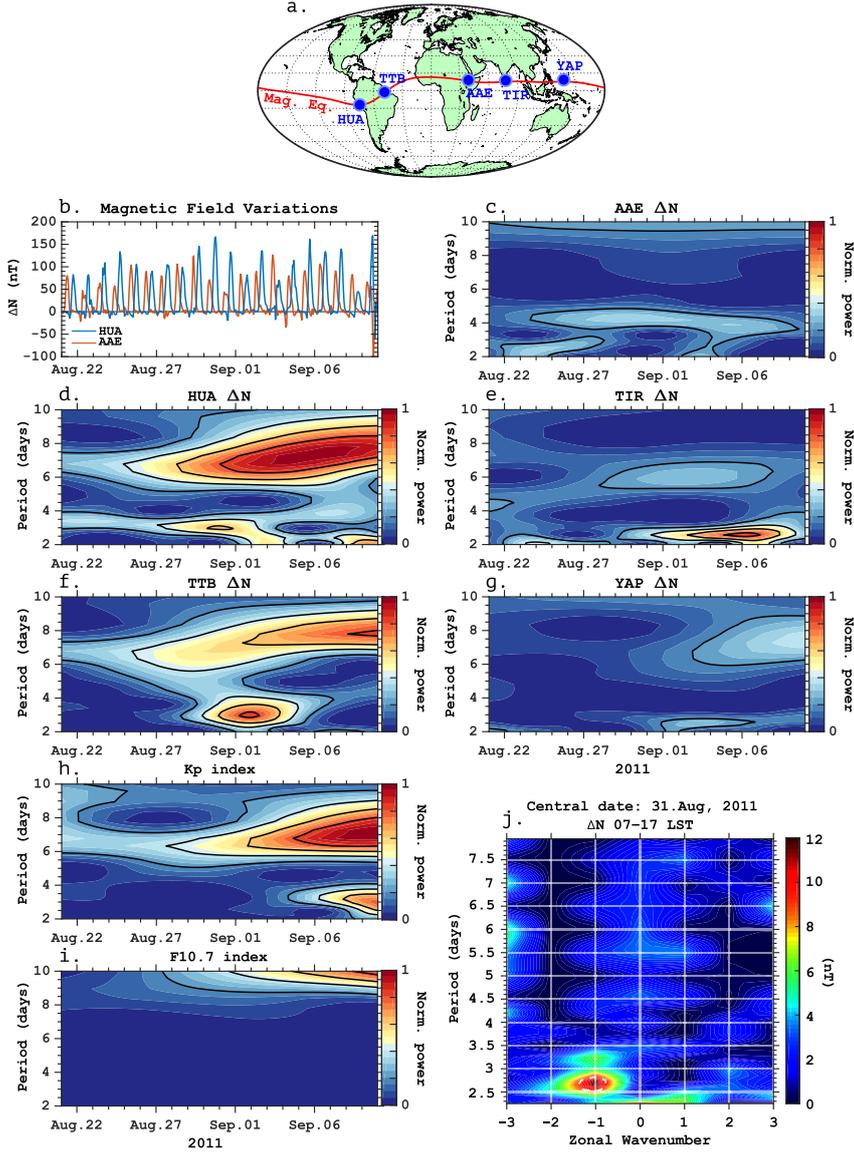
Central date: 31.Aug, 2011



**Figure 12.** Wavenumber versus period spectra during the ultra-fast Kelvin wave event of August–September 2011. The panels (a) and (b) are the same as Figure 11d except for LARGE\_WAVES and NO\_UFKW simulation cases, respectively. The panels (c) and (d) are the same as Figure 11c except for LARGE\_WAVES and NO\_UFKW simulation cases, respectively. The panels (e) and (f) are the same as Figure 11b except for LARGE\_WAVES and NO\_UFKW simulation cases, respectively.



**Figure 13.** (a–c) Longitude versus time diagrams for the 24h mean of (a) the equatorial zonal wind at 110 km altitude, (b) equatorial zonal electric field (EEF) at 110 km altitude, and (c) total electron content (TEC) derived from the LARGE\_WAVES simulation case. (d–e) The same as (a–c) but the 1.5–4.5d bandpass filter is applied at each longitude to extract  $\sim 3$ -day variations. (g–i) The same as (d–e) except for the NO\_UFKW simulation case. (j–l) The difference between LARGE\_WAVES and NO\_UFKW simulation cases, isolating the effect of the ultra-fast Kelvin wave.



**Figure 14.** (a) Locations of the magnetic observatories: HUA=Huancayo; TTB=Tatuoca; AAE=Addis Ababa; TIR=Tirunelveli; and YAP=Yap Island. The red line denotes the magnetic equator. (b) Examples of magnetic field perturbations in the magnetic-northward component ( $\Delta N$ ) at Huancayo and Addis Ababa during 21 August–9 September. (c–g) Wavelet spectra of  $\Delta N$  at different observatories as a function of time and period. Spectral power is normalized to the maximum value at Huancayo. (h) Wavelet spectrum of the geomagnetic activity index  $Kp$ . Spectral power is normalized to the maximum value. (i) Wavelet spectrum of the solar activity index  $F_{10.7}$ . Spectral power is normalized to the maximum value. (j) Wavenumber versus period spectrum of  $\Delta N$  derived from the combination of the daytime  $\Delta N$  data from the five observatories. The white dashed lines correspond to the 95% confidence level.

**Table 1.** The numerical experiments performed in this study and the wave forcing used therein.

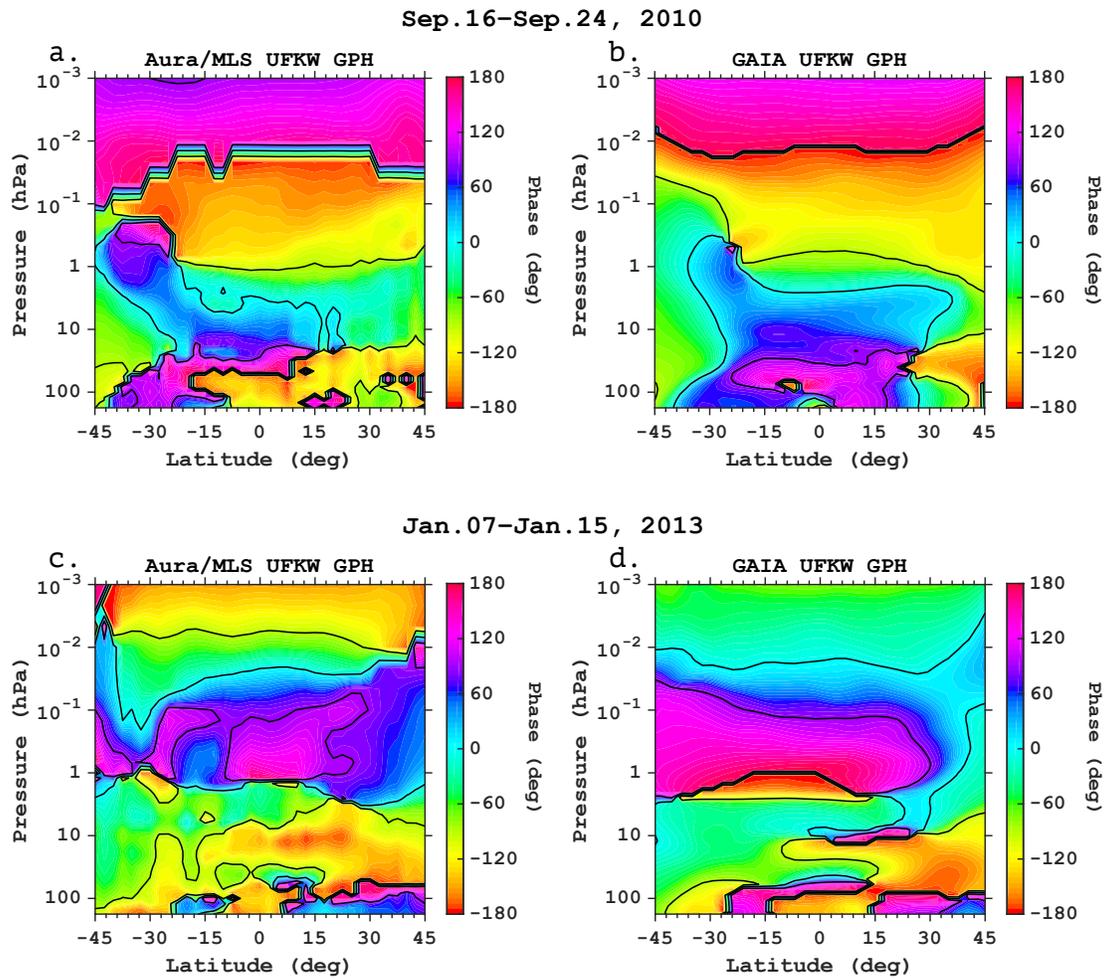
Experiment	Waves
LARGE_WAVES	E5–W5, all periods
NO_UFKW	Same as LARGE_WAVES but excludes E1 with period 1.5–4.5d

**Table 2.** Zonal wavenumber  $s$  and period  $\tau$  (days) of the global-scale waves from which aliasing into the ultra-fast Kelvin wave ( $s=-1$ ,  $\tau=2-4$  days) spectral component can occur when the wave signatures are sampled at a fixed local solar time. Aliasing effects are reduced when the wave signatures are sampled over a range of local solar time (e.g., 3h, 6h, 12h), which is expressed in terms of the amplitude ratio  $\gamma$  with respect to the amplitude calculated by sampling wave signatures at a single local time. Possible sources of aliasing are also indicated, where the X mark represents the non-linear interaction between the ultra-fast Kelvin wave (UFKW) and migrating tides, with S1, S2, S3, S4, and S5 signifying  $n=1$  (diurnal tide),  $n=2$  (semidiurnal tide),  $n=3$  (terdiurnal tide),  $n=4$ , and  $n=5$ , respectively, and the Q2DW standing for the quasi-2-day wave.

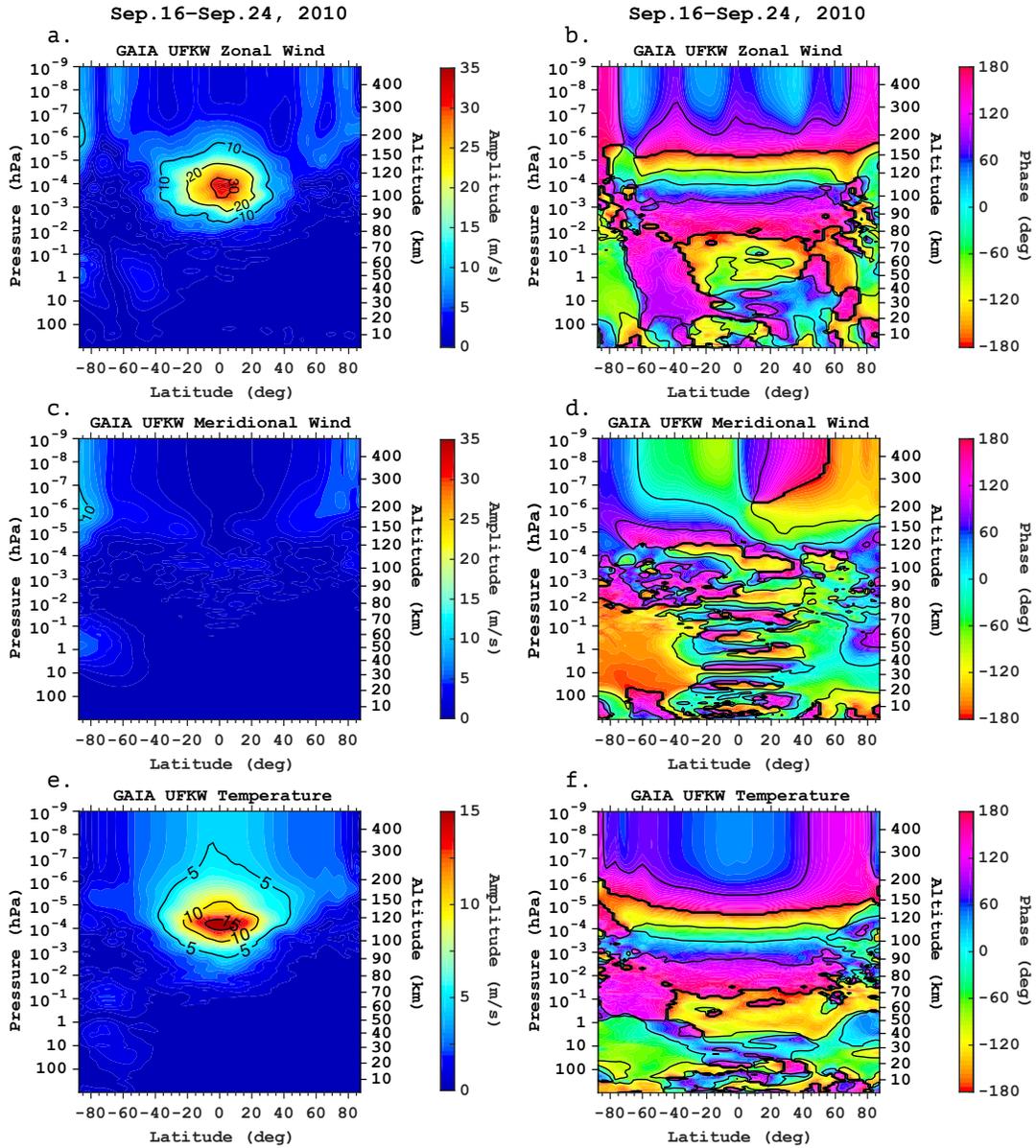
$s$	$\tau$	$\gamma_{3h}$	$\gamma_{6h}$	$\gamma_{12h}$	Possible sources
0	0.67–0.80	0.97	0.90	0.64	UFKW×S1
+1	0.40–0.44	0.90	0.64	0.00	UFKW×S2
+2	1.33–2.00	0.97	0.90	0.64	Q2DW, UFKW×S1
+2	0.29–0.31	0.78	0.30	0.21	UFKW×S3
+3	0.57–0.67	0.90	0.64	0.00	UFKW×S2
+3	0.22–0.24	0.64	0.00	0.00	UFKW×S4
+4	0.36–0.40	0.78	0.30	0.21	UFKW×S3
+4	0.18–0.19	0.47	0.18	0.13	UFKW×S5

**"Whole Atmosphere Model Simulations of 3-day Kelvin Wave Effects in the Ionosphere and Thermosphere"**Y. Yamazaki<sup>1</sup>, Y. Miyoshi<sup>2</sup>, C. Xiong<sup>1</sup>, C. Stolle<sup>1,3</sup>, G. Soares<sup>4</sup>, A. Yoshikawa<sup>5</sup><sup>1</sup>GFZ German Research Centre for Geosciences, Potsdam, Germany<sup>2</sup>Department of Earth and Planetary Sciences, Kyushu University, Fukuoka, Japan<sup>3</sup>Faculty of Science, University of Potsdam, Potsdam, Germany<sup>4</sup>Observatório Nacional, Rio de Janeiro, Brazil<sup>5</sup>International Center for Space Weather Science and Education, Kyushu University, Fukuoka, Japan**Introduction**

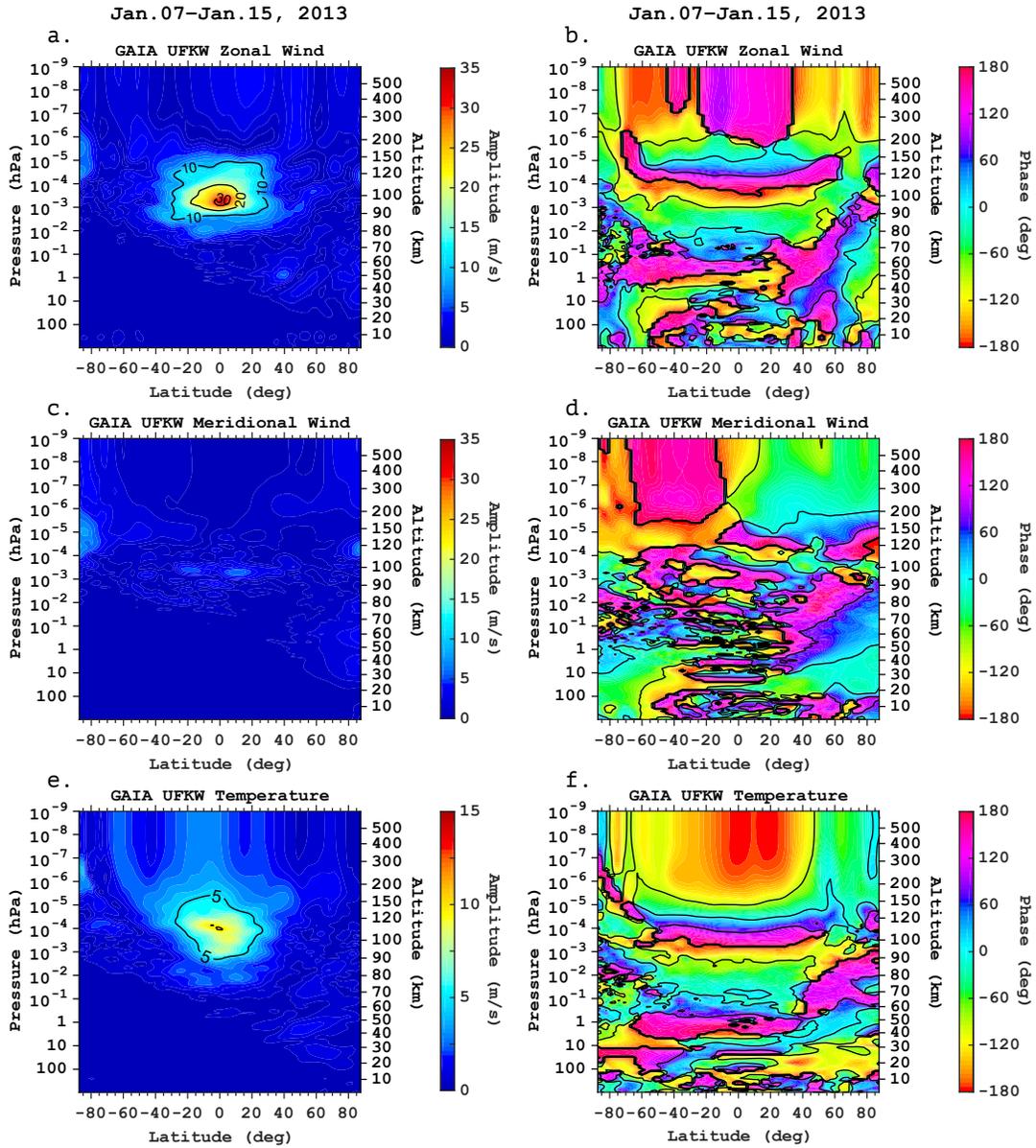
This study focuses on ultra-fast Kelvin waves simulated by the whole atmosphere model GAIA (=Ground-to-topside model of Atmosphere and Ionosphere for Aeronomy) as well as those observed by the GOCE (=Gravity field and steady-state Ocean Circulation Explorer) satellite. The supplementary figures cover results not necessarily included in the paper but useful to understand the complete picture.



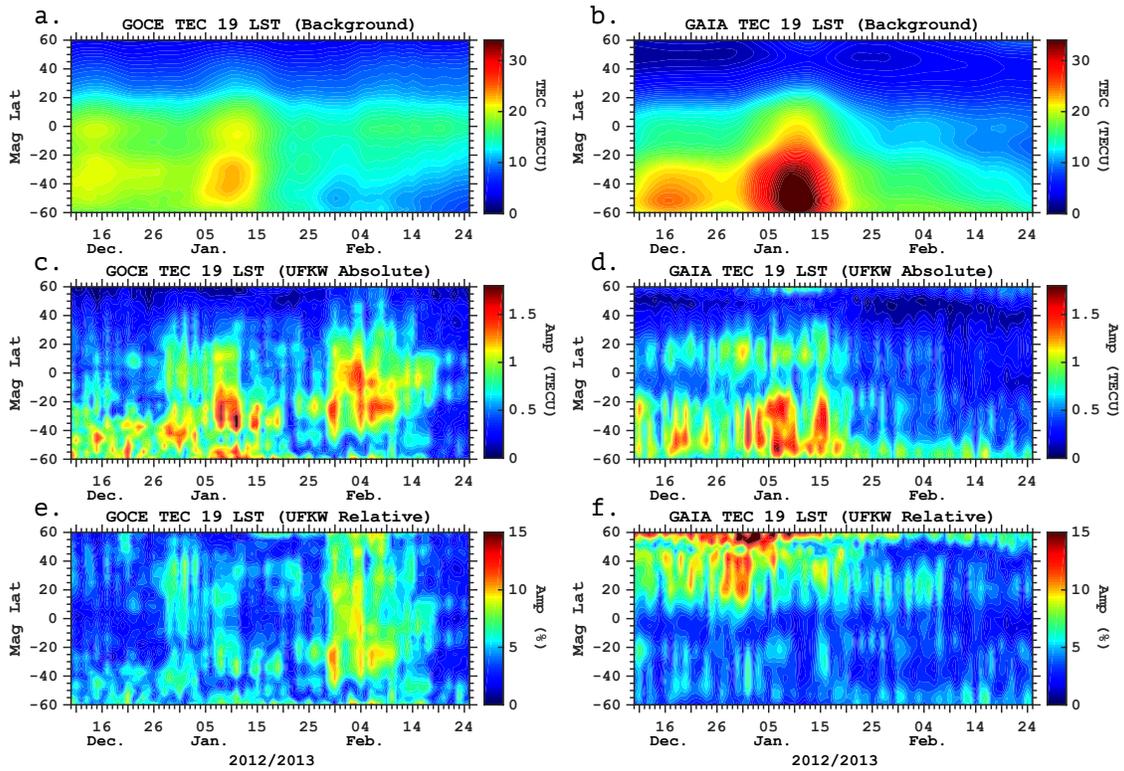
**Figure S1.** Latitude versus height structures of the ultra-fast Kelvin wave (UFWK) phase in the geopotential height (GPH) during the September 2010 event (a, b) and the December 2012–January 2013 event (c, d). The left panels are from the Aura Microwave Limb Sounder (MLS) measurements while the right panels are from the GAIA model.



**Figure S2.** Latitude versus height structures of the ultra-fast Kelvin wave (UFKW) in the zonal wind (a, b), meridional wind (c, d), and temperature (e, f) derived from the GAIA model during the September 2010 event. The left and right panels show wave amplitudes and phases, respectively. The UFKW here is defined as the eastward-propagating waves with a period of 2.5 days and zonal wavenumber 1.

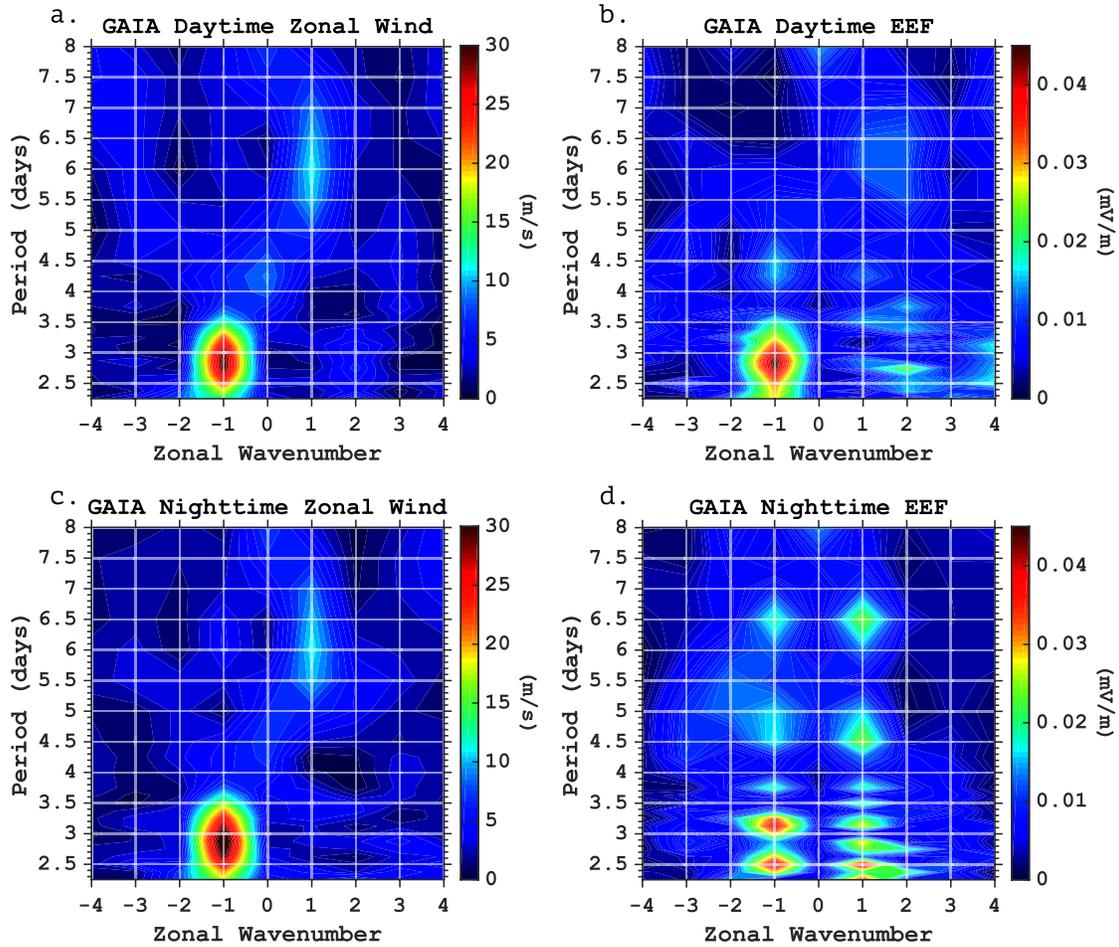


**Figure S3.** Same as Figure S2 except for the December 2012–January 2013 event. The UFKW here is defined as the eastward-propagating waves with a period of 3.0 days and zonal wavenumber 1.



**Figure S4.** Comparison of the total electron content (TEC) at 7 a.m. local solar time derived from the GOCE measurements (a, c, e) and the GAIA model (b, d, f). The panels (a, b) show the background total electron content (TEC) as defined here as the temporal and zonal mean calculated at each latitude using the 9-day moving window. The panels (c, d) show the amplitude of the ultra-fast Kelvin wave (UFKW) in TEC calculated at each latitude using the 9-day moving window. The UFKW amplitude is defined as the largest amplitude of the eastward-propagating waves with zonal wavenumber 1 within periods 2.25–3.75 days. The panels (e, f) show the relative amplitude of the UFKW in TEC with respect to the corresponding background TEC value. Note that color scales are different for different panels.

Central date: 31.Aug, 2011



**Figure S5.** Wavenumber versus period spectra derived from GAIA during the ultra-fast Kelvin wave event of August–September 2011. The panel (a) is for the equatorial zonal wind at 110 km altitude during the daytime between 6 a.m. and 6 p.m. local solar time. The panel (b) is for the equatorial zonal electric field (EEF) at 110 km altitude during the daytime between 6 a.m. and 6 p.m. local solar time. The panel (c) is the same as panel (a) except for the nighttime from 6 p.m. to 6 a.m. local solar time. The panel (d) is the same as panel (b) except for the nighttime from 6 p.m. to 6 a.m. local solar time.