Thermal History of the Earth: On the Importance of Surface Processes and the Size of Tectonic Plates

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Abstract

Geochemical constraints on mantle temperature indicate a regular decrease by around 250 K since 3 Ga. However models of Earth's cooling that rely on scaling laws for thermal convection without strong plates are facing a thermal runaway backwards in time, due to the power-law dependence of heat loss on temperature. To explore the effect of surface dynamics on Earth's cooling rate, we build a 2D temperature-dependent model of plate tectonics that relies on a force balance for each plate and on Earth-like parameterized behaviors for the motion, creation and disappearance of plate boundaries. While our model predicts the expected thermal runaway if plate boundaries are fixed, we obtain an average cooling rate consistent with geochemical estimates if the geometry of plate tectonics evolves through time. For a warmer mantle in the past, plates are faster but also longer (and less numerous) so that the average seafloor age and resulting heat flux always remain moderate. The predicted increase in the number of plates forwards in time is in good agreement with recent plate reconstructions over the last 400 Myr. Our model also yields plate speed and subduction area flux consistent with these reconstructions. We finally compare the effect of parameters controlling mantle viscosity and individual plate speeds to the effect of localized surface processes, such as oceanization and subduction initiation. We infer that studies of Earth's thermal history should focus on surface processes as they appear to be key control parameters.

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Key Points:

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7	• 2D temperature-dependent plate tectonic reorganizations are simulated over 3 Gyr
8	• Archean thermal catastrophe is avoided even with faster plate tectonics in the past
9	• Renewal of plate boundaries is key to Earth's thermal evolution over short and
10	long timescales

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11 Abstract

Geochemical constraints on mantle temperature indicate a regular decrease by around 12 250 K since 3 Ga. However models of Earth's cooling that rely on scaling laws for ther-13 mal convection without strong plates are facing a thermal runaway backwards in time, 14 due to the power-law dependence of heat loss on temperature. To explore the effect of 15 surface dynamics on Earth's cooling rate, we build a 2D temperature-dependent model 16 of plate tectonics that relies on a force balance for each plate and on Earth-like param-17 eterized behaviors for the motion, creation and disappearance of plate boundaries. While 18 our model predicts the expected thermal runaway if plate boundaries are fixed, we ob-19 tain an average cooling rate consistent with geochemical estimates if the geometry of plate 20 tectonics evolves through time. For a warmer mantle in the past, plates are faster but 21 also longer (and less numerous) so that the average seafloor age and resulting heat flux 22 always remain moderate. The predicted increase in the number of plates forwards in time 23 is in good agreement with recent plate reconstructions over the last 400 Myr. Our model 24 also yields plate speed and subduction area flux consistent with these reconstructions. 25 We finally compare the effect of parameters controlling mantle viscosity and individual 26 plate speeds to the effect of localized surface processes, such as oceanization and sub-27 duction initiation. We infer that studies of Earth's thermal history should focus on sur-28 face processes as they appear to be key control parameters. 29

³⁰ Plain Language Summary

The Earth's interior has been cooling over the past 3 billion years. Chemical anal-31 yses of ancient rocks show that the mantle was then about 250 degrees hotter than to-32 day, corresponding to a fairly low amount of heat released until now. However, when the 33 mantle was hotter in the past, it was less viscous, and the dragging forces on tectonic 34 plates were weak: plate motion was probably much faster. Heat from the Earth's inte-35 rior is released mainly at oceanic ridges, where new seafloor is created. The faster the 36 plates, the more heat is released. How so little heat has been released with significantly 37 faster plates in the past? Several authors proposed complex phenomena playing on plate 38 tectonics to slow down plates in the past. Here, we propose a new model including sur-39 face processes controlling plates creation and disappearance, leading to evolving plate 40 sizes. We show that the geometry of plates is a key factor: for a hotter Earth in the past, 41 plates were larger, so that ridges were less numerous and a moderate amount of heat was 42

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released, even if plates were faster. This new paradigm (larger plates in the past) is compatible with observations in geological data.

45 1 Introduction

Reconstructing Earth's thermal history is a challenging issue: the long-standing assumption that the thermal evolution of a planet is controlled by the rheological behavior of its interiors (e.g. Tozer, 1967; Davies, 1980; Nataf & Richter, 1982) cannot be reconciled with petrological and geochemical constraints on mantle temperature in the past. Earth's thermal evolution is commonly studied by a global heat balance between secular cooling, internal heat production H due to a radioactive decay and surface heat loss Q:

$$Mc_p \frac{dT_m}{dt} = H(t) - Q(T_m), \tag{1}$$

where T_m is the mantle potential temperature, M the mass of the Earth, and c_p its av-54 erage thermal capacity, accounting for the isentropic thermal gradient in the mantle and 55 the coupling with core, assuming that mantle and core have similar cooling rates (e.g. 56 Korenaga, 2008). In order to integrate Eq. 1, a first approach consists in using a sim-57 ple convective scaling law for the heat flow Q as a function of the mantle temperature T_m . 58 Such a scaling is usually derived from thermal boundary layer considerations and lab-59 oratory or numerical experiments with an isoviscous fluid (e.g. Howard, 1966) and is writ-60 ten in a dimensionless form as $Nu \sim Ra^{1/3}$, where Nu is the dimensionless heat flux 61 (Nusselt number) and Ra the Rayleigh number of the fluid. As the viscosity of the man-62 tle is highly temperature-dependent (e.g. Karato & Wu, 1993), this scaling implies that 63 the heat flow Q increases exponentially with the mantle temperature T_m , which results 64 in unacceptably high temperatures in the past, implying a totally molten upper man-65 tle in the late Archean (e.g. Davies, 1980; Schubert et al., 1980; Richter, 1985). Abbott 66 et al. (1994) inferred from compositional variations of mid-oceanic ridge basalts that man-67 the temperatures have decreased by about 150 K since the Archean. Herzberg et al. (2010) 68 studied non-arc basalts of late-Archean and Proterozoic age and obtained a maximum 69 potential temperature about 200-250 K higher than the present one at 3 Ga. 70

To obtain these reasonable temperatures in the past, several strategies were proposed. First, the relative importance of radiogenic heating compared to heat loss, known as the Urey ratio Ur = H/Q, plays a major role in the cooling rate (Eq. 1): a high value of Ur helps avoid the Archean thermal catastrophe (e.g. Davies, 1980; Schubert et al.,

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1980) but is inconsistent with geochemical estimates of Earth composition (e.g. Kore-75 naga, 2008). A layered mantle in the past could also slow down mantle's cooling (e.g. 76 Honda, 1995; Butler & Peltier, 2002) but the role of the endothermic phase change be-77 tween the lower- and upper-mantle needs to be exaggerated (Korenaga, 2008). Adding 78 the thermal insulating effect of continents and/or the effect of continental growth on man-79 tle depletion can help prevent a drastic thermal runaway (e.g. Grigné & Labrosse, 2001; 80 Lenardic et al., 2011), but the obtained cooling rates are still decreasing with time which 81 is not consistent with geochemically derived temperature estimates (Herzberg et al., 2010). 82

These previous approaches consider a convective scaling for the heat flow Q as a 83 function of mantle temperature and viscosity in the form $Nu \sim Ra^{1/3}$. Another ap-84 proach consists in lowering the dependence of Nu on Ra. Conrad and Hager (1999) pro-85 posed that the main viscous resistance to mantle convection comes from the bending of 86 the oceanic lithosphere at subduction zones, which renders plate motion less dependent 87 on the viscosity of Earth's interior than a simple convective approach. This idea was ex-88 plored by Sleep (2000) and Korenaga (2003, 2006) to propose thermal evolution mod-89 els where higher temperatures in the past result in slower plates and a reduced heat loss. 90 However, if the correct "bending length" is used in convection models with plate tecton-91 ics (Ribe, 2010), the Archean thermal runaway cannot be avoided by bending dissipa-92 tion only (Gerardi et al., 2019). Korenaga (2011), using a scaling derived from numer-93 ical experiments with strong plates (Korenaga, 2010), proposed a model of Earth ther-94 mal evolution, taking into account the dehydration of the lithosphere through mid-ocean 95 ridges melting, which stiffens the oceanic lithosphere, the possible mantle hydration over 96 time from slab subduction, which has an important role on mantle viscosity (e.g. Hirth 97 & Kohlstedt, 1996; Mei & Kohlstedt, 2000), as well as continental growth for the com-98 putation of the mantle radiogenic heat production. This model is consistent with geo-99 chemical estimates of temperature, but the derived average plate speeds cannot be rec-100 onciled with recent models of plate reconstructions. In his preferred model, Korenaga 101 (2011) obtains a median speed decreasing from $\sim 4 \text{ cm/yr}$ at present to around $3\pm 1 \text{ cm/yr}$ 102 at 2.5 Ga, and the maximum value of the 95th percentile since the Archean is less than 103 4.5 cm/yr at around 500 Ma. This is in contradiction with the two independent mod-104 els of plate reconstructions that go back to Paleozoic, which both suggest average plate 105 speed over 8 cm/yr at 500 Myr, with possible peaks of more than 12 cm/yr in the Pa-106 leozoic (Vérard et al., 2015; Young et al., 2019). Going further back in time, paleomag-107

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netic data showing rapid changes in relative paleolatitudes between individual cratons 108 suggest possible peaks of fast plate motion (from 10 to 100 cm/yr) around 1.1, 2.0 and 109 2.7 Ga (O'Neill et al., 2007), which is also not compatible with continously slow plates 110 before 500 Ma as suggested by Korenaga (2011). This example illustrates that most mod-111 els of Earth's thermal evolution discuss temperature as a function of time in compari-112 son to geochemical estimates, but plate speed, in comparison to geological data and re-113 constructions, is rarely considered. Another problem is that most Earth's thermal mod-114 els do not reflect some important terrestrial observations: not all plates are driven by 115 subduction, strong heat flux variations are coeval with ridge creation or subduction ini-116 tiation, and fast or slow or even immobile plates coexist (present-day plate velocities vary 117 by a factor of 40 (e.g. Argus et al., 2011)). 118

The rate of assembly and dispersal of supercontinents (e.g. Pisarevsky et al., 2014; 119 Condie et al., 2015; Evans et al., 2016) or the lifetime of passive margins (Bradley, 2008) 120 in the Proterozoic are used as information regarding the past rhythm of plate tecton-121 ics. Condie et al. (2015) infer that the decreasing lifespan of passive margins and the in-122 crease in the number of orogens with time suggest that plates were slower in the past, 123 as proposed by Korenaga (2003, 2006, 2011). But a direct relation between the tempo 124 of such tectonic events and the speed of plates would imply that the size of plates did 125 not change through time. However, plate reconstructions suggest an increase in the num-126 ber of plates since 400 Ma (Matthews et al., 2016), which is consistent with numerical 127 models of mantle convection with strong plates (Mallard et al., 2016) (see Discussion in 128 section 4 here). It is then interesting to note that fewer and larger plates in the past may 129 also account for the apparent "slow" past tempo of tectonics events. 130

In the present study, we look into Earth's thermal evolution with aiming at explain-131 ing not only past moderate cooling rates, but also past plate speeds and rates of tectonic 132 events such as continental collisions. We use a 2D model of plate tectonics (MACMA: 133 Multi-Agent Convective Mantle) (Combes et al., 2012) based on a force balance for each 134 plate and on empirical parameterizations to treat local plate reorganizations. The model 135 includes mobile plate boundaries that can collide, vanish or be created, asymmetric sub-136 duction zones and their consequent overriding plates, together with breakable insulat-137 ing continents, bordered by active or passive margins. With this approach, the geom-138 etry of plate tectonics is not fixed but free to adapt as the temperature and plate speeds 139 evolve. Combes et al. (2012) conducted several experiments that yielded moderate cool-140

ing rates comprised between 55 and 110 K/Gyr over the past 3 Gyr, but the initial con-141 ditions and the main parameters of the model were not varied on a wide range of pos-142 sibilities. Here, we present a full analysis of Earth's thermal evolutions obtained with 143 this approach, and compare them with numerous available geochemical and geological 144 data. Our results with fixed plate boundaries exhibit the same thermal catastrophe as 145 the one arising in classical parameterized studies of Earth's thermal history. With evolv-146 ing plate boundaries, conversely, the obtained thermal evolution over 3 Gyr is in good 147 agreement with terrestrial estimates by Herzberg et al. (2010). Plate speed, slab flux and 148 the number of plates also correspond to recent tectonic reconstructions over the Phanero-149 zoic (Vérard et al., 2015; Matthews et al., 2016; Hounslow et al., 2018; Young et al., 2019). 150 The obtained rate of collisions between continents is also slightly increasing over time, 151 as suggested by Condie et al. (2015). These results, consistent with geochemical and ge-152 ological data while plate speed is still simply controlled by the mantle viscosity and de-153 creasing with time, are the consequences of the surface processes (subduction initiations 154 and cessations, and continental cycles) included in our model, that control the evolving 155 geometry of plate tectonics. 156

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2 The MACMA Model

The MACMA (MultiAgent Convective MAntle) framework is a 2D planet covered 158 by mobile plates, with evolving plate boundaries that can be created and eliminated. The 159 conservation of heat is written as Eq. 1, using a uniform temperature for the mantle. Mass 160 and momentum conservations are imposed with a force balance for each plate, consid-161 ering a total of 3 driving forces and 3 resistive forces. The general framework of MACMA 162 is presented in Figure 1. Plate boundaries are ridges and trenches that can both migrate 163 through the oceans. Other elements are continents and staples, which are discontinu-164 ities in oceanic lithosphere ages appearing when two plate boundaries collide. 165

Plate velocities are deduced from a force balance, using a layered mantle (lithosphere, upper mantle and lower mantle). Each layer has a newtonian temperature-dependent viscosity, written as an Arrhenius law using reference values for present-day Earth. Hereafter, the subscript 0 stands for present-day values:

$$\eta_i(T_m) = \eta_{i_0} \, \exp\left(\frac{E}{R} \, \left(\frac{1}{T_m} - \frac{1}{T_{m_0}}\right)\right). \tag{2}$$

- The subscript i stands for the different layers in Earth (i = pl, um or lm for oceanic
- plates, upper mantle and lower mantle respectively), E is the activation energy and $R = 8.314 \text{ J.K}^{-1} \text{ mol}^{-1}$



Figure 1. (A) Force balance used in this study. (B) Initiation of subductions in compressive (B1) and extensive context (B2). When the ocean seafloor age at the passive margin reaches the limit age τ_{subd} , a subduction is created. The compressive case (B1) occurs when the overriding plate moves towards the trench. The symmetrical accretion around the ridge is also schematized. The extensive case (B2) occurs when the overriding plate moves away from the trench: a ridge is created to compensate for the diverging motion of the two plates. (C) Continental breakup: an advective shear force F below the continent is computed and compared to a fixed continental strength $F_{\rm lim}$. If $F > F_{\rm lim}$ the continent can open, at a position that is randomly picked in the yellow zone (middle of continent $\pm 1/3$ of its width a). The subcontinental shear force F (see appendix B) is represented as a function of the age of the continent and of its width a (a=2000, 4000, 8000 or 16000 km). For this computation at present day, the viscosity of the upper mantle is $\eta_{\rm um} = 10^{21}$ Pa.s (for T=1625 K) and the radiogenic heat production is H = 13 TW. For past hotter conditions (chosen to represent the late Archean), we use H = 25.7 TW and $\eta_{\rm um} = 6.7 \times 10^{19}$ Pa.s (for T=1850 K, using the activation energy E=300 kJ.mol⁻¹). (D) Processes for plate boundary eliminations and creations of staples.

is the gas constant derived from the Boltzmann distribution. Parameters used in this 173 study are given in Table 1. 174 The thickness of plates δ as a function of the seafloor age τ is needed in the expres-175 sions of several forces hereafter. From the halfspace cooling model (e.g. Turcotte & Schu-176 bert, 2002), we use 177 $\delta(\tau) = c\sqrt{\kappa\tau}$ (3)178 with κ the thermal diffusivity. We use the prefactor c = 2.1 yielding an oceanic litho-179 spheric thickness of ~ 10 km for $\tau = 1$ Myr and ~ 95 km for $\tau = 80$ Myr. A small scale 180 convection (SSC) mechanism can be used as an option in the MACMA model, in order 181 to limit seafloor thickness after a critical age (for details, see Combes et al. (2012)). 182 2.1 Force Balance 183 The force balance used in this study is presented in Figure 1A. With a 1D geom-184 etry for plates, we express the forces in $N.m^{-1}$. 185 2.1.1 Driving Forces 186 The driving forces are the following: (1) ridge push (RP), (2) slab pull (SP) and 187 (3) slab suction (SS). 188 Following Parsons and Richter (1980), we write 189 $\mathrm{RP} = \alpha \rho q \, \left(T_m - T_s\right) \, \kappa \tau_{\mathrm{max}}$ (4)190 where $\tau_{\rm max}$ is the maximum age of the plate, α the thermal expansivity and $T_m - T_s$ 191 the thermal jump across the lithosphere. 192 Slab pull is due to the excess weight of the cold slab, and we consider this force in 193 the upper mantle only, as was done by Conrad and Lithgow-Bertelloni (2002) and Conrad 194 and Lithgow-Bertelloni (2004): 195

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 $SP = \Delta \rho \ g \ \delta(\tau_{max}) \ \min(Z, d_{um}), \tag{5}$

where Z is the depth reached by the slab and $\delta(\tau_{\text{max}})$ is the thickness of the slab (Eq. 3).

- Following Conrad and Lithgow-Bertelloni (2002, 2004), we consider slab suction (SS) in the lower mantle: descending slabs induce mantle flow that pulls both the sub-
- ducting and the overriding plates towards the subduction zone. SS is expressed as a shear

Table 1. Parameters used in this study. In bold font are the parameters used for the referencecase (see section 3.3). Their effects are studied in section 3.4.

Parameter	Symbol	Valu	ıe
Earth's mass	M	5.98×10^{24}	kg
Mantle's mass	$M_{ m m}$	4.08×10^{24}	kg
Continental crust's mass	$M_{\rm cont}$	2.20×10^{22}	kg
Earth's radius	$R_{\rm E}$	6370	km
Upper mantle thickness	$d_{ m um}$	670	km
Lower mantle thickness	$d_{ m lm}$	2230	km
Gravitational acceleration	g	10	$\mathrm{m.s}^{-2}$
Thermal expansivity	α	2×10^{-5}	K^{-1}
Upper mantle density	ρ	3300	$\rm kg.m^{-3}$
Slab density contrast	$\Delta \rho$	65	$\rm kg.m^{-3}$
Present-day oceanic lithosphere viscosity		$\boldsymbol{1.25\times10^{23}}$	Pa.s
Present-day upper mantle viscosity		$5 imes 10^{20}$	Pa.s
Present-day lower mantle viscosity	$\eta_{ m lm_0}$	$5 imes \mathbf{10^{22}}$	Pa.s
Activation energy	E	350	$kJ.mol^{-1}$
Oeanic lithosphere thermal conductivity	k	3	$\mathrm{W.m^{-1}.K^{-1}}$
Thermal diffusivity	κ	$8 imes 10^{-7}$	$\mathrm{m}^2.\mathrm{s}^{-1}$
Earth's average thermal capacity	c_p	1200	$J.kg^{-1}.K^{-1}$
Surface temperature	T_s	273	Κ
Present-day mantle potential temperature	T_{m_0}	1625	Κ
Present-day slabs Stokes velocity in the lower mantle	V_{s_0}	1	m cm/yr
Present-day critical age for subduction initiation		180	Myr
Minimum radius of curvature of plates	R_{\min}	300	km
Continental strength	$F_{ m lim}$	2	$\mathbf{TN}.\mathbf{m}^{-1}$
Subcontinental warming zone thickness	b	350	km

stress exerted on the slab and transmitted to the horizontal plates on both sides of the trench:

$$SS = \eta_{lm_0} \left(\frac{V_{s_0}}{4 d_{lm}}\right) \max(0, Z - d_{um})$$

$$\tag{6}$$

Only the height of the slab in the lower mantle is considered here. V_{s_0} is the present-204 day vertical velocity of the slab in the lower mantle, described as a Stokes velocity (Guillou-205 Frottier et al., 1995; Griffiths et al., 1995; Goes et al., 2011), so that at each time we have 206 $\eta_{\rm lm} V_s = \eta_{\rm lm_0} V_{s_0}$. Eq. 6 is therefore written with present-day values. Considering a fluid 207 loop model (e.g. Grigné et al., 2005), we make the rough approximation that only a quar-208 ter of the drag force of the sinking slab results in suction on each horizontal plate above 209 the plate (factor 4 in Eq. 6). The amplitude of SS is controlled by the choice for the value 210 of V_{s_0} . The factor $1/(4 d_{\rm lm})$ in Eq. 6 yields present-day plate speeds consistent with ob-211 servations when we choose a value for V_{s_0} also consistent with recent estimates of the 212 descent rate of slabs in the lower mantle (see section 2.1.3). 213

The three driving forces RP, SP and SS depend on the depth of slabs and on seafloor ages, but not on the velocities of plates. SP is taken into account only for subducting plates, while SS is considered for both the subducting and the overriding plates.

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2.1.2 Resistive Forces

The resistive forces are: (1) the vertical shear stress on the slabs in the upper mantle (VS), (2) the horizontal mantle drag under the plates (MD) and (3) the bending force (B) (see Figure 1A). They can all be expressed as shear forces, equal to the product of an effective viscosity that accounts for the geometry of the plate, and of the velocity Uof the plate. The equivalent viscosities are denoted hereafter by $\eta_{\rm VS}$, $\eta_{\rm MD}$ and $\eta_{\rm B}$ and their expressions are given in appendix A. The sum of the resistive forces is

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$$VS + MD + B = -(\eta_{VS} + \eta_{MD} + \eta_B) U$$
(7)

2.1.3 Plate Velocity Computation and Choice for Present-day Parameters

²²⁷ Considering a mantle with infinite Prandtl number, the forces exerted on each plate²²⁸ cancel out, which allows to calculate each plate velocity as:

$$U = \frac{\text{RP} + \text{SP} + \text{SS}}{\eta_{\text{MD}} + \eta_{\text{VS}} + \eta_{\text{B}}}$$
(8)

The parameters entering the expressions for the different forces are given in Ta-230 ble 1. We focus the discussion here on the choice for the descent rate of slabs V_{s_0} (en-231 tering the expression of SS) and on the present-day viscosities for the lower mantle $\eta_{\rm lm_0}$, 232 the upper mantle $\eta_{\rm um_0}$ and the oceanic plates $\eta_{\rm pl_0}$, entering the expressions of the re-233 sistive forces and their equivalent viscosities $\eta_{\rm MD}$, $\eta_{\rm VS}$ and $\eta_{\rm B}$. V_{s_0} is estimated from seis-234 mic tomography to be between 1 and 2 cm/yr (Van der Meer et al., 2010, 2018; Čížková 235 et al., 2012; Domeier et al., 2016). In numerical models of a subducting slab in a con-236 vective system, this range of velocity can be obtained if the viscosity of the lower man-237 tle is comprised between 10^{22} and 10^{23} Pa.s (e.g. Kaneko et al., 2019). Geoid and post-238 glacial isostatic adjustments studies, as well as instantaneous models of mantle circula-239 tion coupled to lithospheric plates, suggest that the lower mantle is about 100 times more 240 viscous than the upper mantle (e.g. Faccenda & Dal Zilio, 2017). We therefore choose 241 for the reference model $V_{s_0} = 1 \text{ cm/yr}$, $\eta_{\text{lm}} = 5 \times 10^{22} \text{ Pa.s}$ and $\eta_{\text{um}} = 5 \times 10^{20} \text{ Pa.s}$. 242 For the bending force, we choose a minimum radius of curvature of plates (at the trench) 243 $R_{\rm min} = 300$ km and a lithosphere 250 times more viscous than the upper mantle (Wu 244 et al., 2008; Holt et al., 2015; Behr & Becker, 2018): $\eta_{\rm pl_0} = 1.25 \times 10^{23}$ Pa.s. 245

These parameters yield reasonable plate speeds for present time (see Figure 2). We 246 do not aim at obtaining precise velocities that could be directly compared to actual plates 247 for the present-day Earth, but we are checking here that the force balance gives reason-248 able speeds, with a few typical Earth features: plates driven by significant slab pull are 249 at least thrice faster than non-subducting plates, and there is no direct relation between 250 plates' sizes and their speeds, aside from the observation that plates with speeds larger 251 than $0.75 \text{ deg.Myr}^{-1}$ all have an area smaller than 0.15 steradians (e.g. Forsyth & Uyeda, 252 1975; Argus et al., 2011). 253

Figure 2 shows that for six terrestrial plates whose geometry can be relatively well 254 described in a 2D frame, all bounded by a ridge and a trench (either as the subducting 255 plate or the overriding plate), our force balance yields reasonable results. The speeds of 256 four subducting plates (Juan de Fuca, JF; Cocos, CO; Nazca, NZ and Pacific, PA) can 257 be approximately explained through Eqs. 4 to 8 by their different sizes and variable max-258 imum ages at the trench. The obtained differences between these subducting plates and 259 two non-subducting plates (North America, NA and South America, SA) are also cor-260 rect. Note that the age at the trench and the depth of the slab that are considered for 261 these two non-subducting plates are the values for the plates that NA and SA are over-262



Predicted present-day plates' speeds

Figure 2. Plate velocities obtained with the force balance given by Eq. 8 (black curves), for different ages at the trench (horizontal axis) and different depths reached by the slab. We test sizes of plates corresponding to Juan de Fuca (JF), Cocos (CO), Nazca (NZ), Pacific (PA), North America (NA) and South America (SA). Velocities given by Argus et al. (2011) are shown with horizontal lines and their corresponding 95% confidence limits with shaded area. The length of plates is $L = 2 R_E \arccos(1 - A/(2\pi))$ where R_E is Earth's radius and A the plate area in steradians. The range of ages at the trench tested for each plate is deduced from the oceanic ages map of Müller et al. (2008). For the ridge push force of non-subducting plates, we consider the following ages at the Atlantic passive margins: 180 Myr for NA and 110 Myr for SA.

- riding (PA and NZ, respectively). Their own maximum oceanic ages is considered for
- the term of ridge push (RP) only. The older ages on the Atlantic margins for NA com-
- ²⁶⁵ pared to SA and the fact that NA is overriding younger plates than SA, resulting in lower
- resistive forces |VS| and |B|, can explain the larger value observed for NA.
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2.2 Dynamics of Plate Boundaries

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2.2.1 Velocity of Trenches and Ridges

Simple laws are used to account for the mobility of plate boundaries (see Figure 1B). Trenches are given the velocity of their overriding plates, which undergo the resistive forces acting on the slab. Only plates limited by two ridges have $\eta_{VS} = \eta_B = 0$. As for ridges, we consider symmetric spreading: ridges are given a velocity equal to half the sum of the velocities of the two diverging plates.

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2.2.2 Elimination of Plate Boundaries

When collisions occur between two plate boundaries (trench-ridge or trench-trench), both of them disappear and are replaced by a so-called staple, which marks a former plate boundary that becomes an age discontinuity in the middle of a plate upon collision (see Figure 1D).

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2.2.3 Creation of New Ridges

New ridges may be created in two circumstances: when tension appears on an overriding plate in a subduction zone, and during continental break-up. The former case is illustrated in Figure 1B: when the overriding plate is driven away from the trench, we impose the creation of a new ridge which represents a simplified back-arc basin.

Continental break-up is shown in Figure 1C: we consider that continents have an insulating effect (e.g. Gurnis, 1988; Guillou & Jaupart, 1995; Coltice et al., 2007; Grigné et al., 2007; Rolf et al., 2012; Whitehead & Behn, 2015), which in turn enhances convective vigor in the upper mantle (e.g. Lenardic et al., 2005; Samuel et al., 2011). We derive a parameterization of the warming rate and subsequent advective motion in a shallow layer below a continent as a function of its width and of the radiogenic heating rate in the mantle. The resulting shear force F, which also depends on mantle viscosity, has

to overcome a fixed yield strength F_{lim} in order for the continent to break up (see Combes 291 et al. (2012) and appendix B for calculation details). This simplified oceanization pa-292 rameterization does not reflect complex interactions between continents and mantle flow 293 (e.g. O'Neill et al., 2009) but yields a physically reasonable behavior as a function of T_m : 294 (1) a plateau in the shear force F is reached after a transient period lasting a few hun-295 dreds of Myr (see Figure 1C), (2) wider continents induce larger shear forces F and are 296 therefore breaking more easily than narrow continents, (3) there is a minimum width for 297 a continent to break, which depends on the chosen value of $F_{\rm lim}$ and on the thermal state 298 of the mantle, and (4) because of a lower viscosity in a hotter mantle, the shear force F299 after a given duration and for a given continental width was lower in the past, imply-300 ing that the minimum size for a continent to break was larger in the past. 301

In their numerical experiments, Heron and Lowman (2014) obtained thermal anoma-302 lies at high Rayleigh number beneath continents extensively ringed by subduction zones. 303 In our model, continental break-ups occur only if the plate that contains the continent 304 is limited by at least one subduction zone. The slab direction and position do not mat-305 ter, i.e. it is not required that the continent is bordered by an active margin. Without 306 this condition in our 2D setting, the new ridge created by continental break-up, which 307 exhibits initially a null ridge push force (seafloor of age zero), would immediately reclose 308 because of the two opposing ridge push forces on either side of the plate. Furthermore, 309 in order to avoid symmetrical configurations that may arise from breaking up the con-310 tinent right in its middle, the rifting position is randomly chosen (see Figure 1C). Our 311 results show temperature anomalies around +15 K, in good agreement with numerical 312 experiments by Yoshida (2013). 313

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2.2.4 Creation of New Subductions

Many processes have been proposed for the initiation of subduction (e.g. McKen-315 zie, 1977; Cloetingh et al., 1989; Mueller & Phillips, 1991; Gurnis et al., 2004; Crameri 316 & Kaus, 2010; Nikolaeva et al., 2011; Levy & Jaupart, 2012), but no analytical formu-317 lation can be integrated at a global scale to simulate a starting mechanism (Gerya & Meil-318 ick, 2011). Here, without considering the mechanical details of seafloor destabilization, 319 we make the assumption that subduction initiation occurs at a certain critical age $\tau_{\rm subd}$. 320 when the negative buoyancy of the oceanic lithosphere exceeds a critical yield strength 321 σ_y which is considered as a constant over time. This negative buoyancy is proportional 322

to $\alpha \rho g(T_m - T_s) \, \delta(\tau)$. Expressing the lithospheric thickness δ as a function of the seafloor age τ (Eq. 3) and equating the critical buoyancy (proportional to $\sqrt{\tau_{\text{subd}}}$, where τ_{subd} denotes the critical age for subduction initiation) at any age to the present-day one, the destabilization occurs when

$$\tau_{\rm subd}(T_m) = \tau_{\rm subd_0} \left(\frac{T_{m_0} - T_s}{T_m - T_s}\right)^2 \tag{9}$$

where τ_{subd_0} is the present-day age for the initiation of subduction, chosen at 180 Myr in our reference case. An additional condition is used: subductions are created only at discontinuities in lithospheric ages (passive margins and staples). It is important to note that the critical age of subduction τ_{subd} is temperature-dependent, which allows the system to adapt its surface behavior to the mantle thermal evolution. $\tau_{subd} = 156$ and 137 Myr when the temperature is increased by 100 and 200 K, respectively.

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2.3 Thermal Balance and Time Evolution

The age of the oceanic lithosphere is tracked using a resolution of 0.25° (27.8 km). New age points are created at ridges, and they are consumed by subduction. At each time step and for every point of the oceanic lithosphere, the seafloor age τ is used to compute the local heat flux $q_{\rm loc}(\tau)$:

$$q_{\rm loc}(\tau) = \frac{k \left(T_m - T_s\right)}{\sqrt{\pi\kappa \tau}}.$$
(10)

This is integrated over the oceanic surface to compute the total heat flow Q. To convert 340 from an angular distance β in our 2D setting to a surface area, we consider that our ge-341 ometry is a great circle slice of Earth and that each plate is a spherical biangle, whose 342 surface area is then $A = 2\beta R_E^2$. Continents are considered as perfectly insulating and 343 have a constant total area equal to 40% of Earth's surface. Mantle temperature T_m is 344 updated using Eq. 1. For the internal radiogenic heat H(t), we consider present-day de-345 pletion throughout Earth's history: continents have a constant total mass $M_{\rm cont}$. De-346 pleted mantle concentrations in the radiogenic isotopes of U, Th and K are then com-347 puted using concentrations in the bulk silicate Earth given by McDonough and Sun (1995) 348 and concentrations in the continental crust given by Rudnick and Gao (2003). Internal 349 heat from radioactive origin then decreases from 31.2 TW at 3 Ga to 13.0 TW at present. 350 An explicit method is used for the time evolution of the model. First, each point 351 (oceanic ages, plate boundaries, staples and continental borders) is advanced using its 352 velocity and a time step dt equal to or less than 5000 years, limited so that no point is 353

moved by more than half the resolution, equal to 0.25° , which is equivalent to applying 354 a Courant-Friedrichs-Lewy condition with a Courant number equal to 0.5. If a collision 355 between two plate boundaries should occur over one time step, dt is again reduced so 356 that a perfect collision is reached without any overlap between elements. A finite dif-357 ference form of Eq. 1 is used to update T_m , and new temperature-dependent viscosities 358 are computed. Driving and resistive forces are updated using the new positions and vis-359 cosities. The plate speed calculation (Eq. 8) and the criteria described in section 2.2 are 360 then used to move points for the next time step. 361

362 3 Results

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3.1 Fixed Plate Boundaries

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3.1.1 Temperature Evolution

All simulations presented in this section are started with an even number of equal-365 sized oceanic plates, all limited by a ridge and a trench where the seafloor age is initially 366 τ = 10 Myr. Continents are not allowed to break up. With these symmetrical initial 367 configurations, all plate boundaries remain perfectly fixed and the thermal evolution is 368 controlled entirely by the speed of permanently subducting plates, itself controlled by 369 temperature-dependent viscosities. More than 150 experiments were carried out with fixed 370 boundaries, initial temperatures ranging from 1700 to 2000 K and initial ages from 400 Ma 371 to 3.0 Ga. We present in Figure 3 only initial states that yield a temperature of 1625 K 372 at present-day. 373

Petrological estimates of the mantle potential temperature of Herzberg et al. (2010) 374 are shown with yellow circles in Figure 3(e). We use MgO contents for non-arc basalts 375 given by Herzberg et al. (2010) and the relation between the mantle potential temper-376 ature and MgO contents given by Herzberg and Asimow (2015). These authors indicate 377 that the uncertainty on MgO contents translates into a possible error of ± 42 K on the 378 obtained mantle potential temperatures. The thermal evolutions that we obtain with fixed 379 plate boundaries exhibit the typical runaway shape and are clearly impossible to recon-380 cile with those estimates. 381

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Figure 3. Configurations with fixed plate boundaries (a, b, c and d) and thermal evolution obtained with these configurations (e). Estimates of mantle potential temperatures derived from MgO contents by Herzberg et al. (2010) are shown as yellow circles. We use the relation $T_m(K) = 1298 + 28.6 \text{ MgO} - 0.084 \text{ MgO}^2$ given by Herzberg and Asimow (2015). (f) Dimensionless representation of the obtained heat flow $Q(T_m)$ as Nusselt number Nu vs. Rayleigh number Ra. The gray area represents the slope of the purely convective relation Nu~Ra^{1/3}. The number of plates varies from 3 to 24.

382 3.1.2 Heat Flux

For the four thermal evolutions obtained with different numbers of plates in Figure 3(e), we compute the heat flux q in a dimensionless form (Nusselt number Nu):

$$Nu = q \frac{(d_{um} + d_{lm})}{k (T_m - T_s)}$$

$$(11)$$

as a function of the Rayleigh number Ra, computed using parameters in Table 1 and Eq. 2 for $\eta_{\rm lm}$ as a function of T_m :

$$\operatorname{Ra} = \frac{\alpha \rho g (T_m - T_s) (d_{\operatorname{um}} + d_{\operatorname{lm}})^3}{\kappa \eta_{\operatorname{lm}}}$$
(12)

The very good fit with the classical relation $Nu \sim Ra^{1/3}$ (Figure 3(f)) demonstrates 389 that the force balance governing the MACMA model can reproduce results obtained in 390 numerical or analogical experiments of isoviscous permanent convection in terms of heat 391 transfer (e.g. Howard, 1966; Turcotte & Oxburgh, 1967). As expected for thermal his-392 tory, a heat loss that depends on mantle temperature and viscosity with this convective 393 scaling results in unacceptably high temperatures in the Archean. We infer that our force 394 balance corresponds to classical parametrizations for permanent convection and can re-395 produce the Archean thermal catastrophe. 396

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3.2 Mobile Plate Boundaries

We now aim at examining the impact of the plate boundary network mobility on 398 the heat flux evolution and the consequent thermal behavior of the mantle, both on a 399 timescale of a few million years and on the long term. Figure 4 shows tectonic events 400 over 40 Myr and the consequences of these events on the seafloor age and on the local 401 heat flux. The simulation started at 3 Ga with an initial temperature of 1850 K. As in 402 the rest of the study, we consider that a simulation is thermally Earth-like when the present-403 day temperature is $T_{m_0} = 1625 \pm 25$ K (e.g. Herzberg et al., 2007). The continental strength 404 is here set to $F_{\text{lim}} = 3 \text{ TN.m}^{-1}$. Figure 4 exhibits plate boundary creations and disap-405 pearances together with their consequences on seafloor ages and oceanic heat flux: 406

⁴⁰⁷ A - 1415 Ma: There is one ridge (R1), one subduction (S1) and two continents (C1 ⁴⁰⁸ and C2). Seafloor ages at the passive margins on the right of C1 and on the left ⁴⁰⁹ of C2 are soon reaching the critical age for the initiation of subduction ($\tau_{subd} \approx 152$ Myr ⁴¹⁰ for T = 1746 K).

- 1394 Ma: Two new subductions (S2 and S3) were initiated on the borders of con-B -411 tinents C1 and C2. As S2 and S3 are both in an extensive configuration (see Fig-412 ure 1B), new ridges R2 and R3 are created above these subductions. New oceans 413 are expanding around ridges R2 and R3, which results in new zones of high heat 414 flux. Plate 1 and plate 6 (formerly plate 2 in A) are now driven by slab pull and 415 their velocities increase. Old seafloor is thus rapidly consumed. With the increased 416 accretion velocity around R1, the area of young seafloor is extending. These com-417 bined effects increase the total heat loss by more than 83% (from 26.7 to 48.9 TW 418 in 20 Myr). 419
- C 1374 Ma: Continents C1 and C2 collided and subduction S1 disappeared. The former old seafloor at the passive margins of C1 and C2 has now been consumed by
 subductions S2 and S3. Only seafloor younger than 50 Myr is present, resulting
 in a globally high heat loss. As the new oceans centered on R2 and R3 are expanding, ages are becoming older and the total heat loss decreases, but at a slower rate
 than the increase seen between A and B (see Figure 5 for heat flow evolution).
- MACMA allows to simulate long term tectonic evolutions of the seafloor age distribution. The heat loss and temperature evolutions over 3 Gyr are shown in Figure 5, including the episodes described in Figure 4. While the heat loss exhibits irregular and large variations, the temperature shows a much smoother evolution. One peak of heat loss variation, shown in the inset in Figure 5b, is analyzed by studying the seafloor age configuration at 6 times (denoted by letters A to F, with A to C already presented in Figure 4).
- The increase in heat flow around 1.4 Ga (between A and C) was explained above with Figure 4, where the global lowering of seafloor ages is clearly visible. In the inset of Figure 5b, a slow heat flow decrease can be seen between ages C and D, which is due to seafloor ages getting older at passive margins (on the borders of continent C3) and for overriding plates above subduction zones (left of subduction S2 and right of subduction S3). A more marked low is then seen between D and F (timespan is 30 Myr):
- Between D and E: Ridge R1 collides with the subduction S2. In MACMA, such
 a collision results in the disappearance of both R1 and S2, replaced by a staple
 (shown as a small black circle in the panel E of Figure 5c). The small plate located
 between S2 and R1 disappears. In panel D, young seafloor is being consumed by

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Figure 4. Tectonic plates organization, seafloor ages and heat flux over 40 Myr, for a simulation starting at 3 Ga at a temperature of 1850 K. In each panel (A, B and C) corresponding to three different times, the left portion (1) is the great circle representation in polar coordinates and the right portion shows the seafloor age and the positions of interfaces at the surface (2) and the local heat flux q computed from the seafloor age (3). Positions in degrees are positive counterclockwise (pink numbers in A1). R1, R2 and R3 are ridges; S1, S2 and S3 are subduction zones and C1, C2 and C3 are continents. Positions of plates are shown between two white radii in frame (1) and as colored bars between frames (2) and (3): green, red and blue bars indicate plates respectively moving left, moving right or immobile.



Figure 5. (a) Temperature evolution over 3 Gyr. (b) Total heat flow Q, radioactive heating H and number of ridges as a function of time. The inset is a zoom on the heat flow for ages between 1.30 and 1.45 Ga; (c) Seafloor ages at times D, E and F. The times A, B and C are already described in Figure 4. Color scale for seafloor ages is the same as in Figure 4.

the subduction S3 but it is renewed by seafloor creation at R1. Once R1 disappears, the portion of young seafloor located between the staple and S3 on panel
E rapidly vanishes, which accelerates the decrease in heat loss.
Between E and F: Once the staple was subducted, slab pull at subduction S3 is
getting stronger as older seafloor enters the subduction. The plate located between
R2 and S3 accelerates, which results in a wider area of young seafloor around R2
and induces the small local increase in heat loss seen in the inset of Figure 5b.

Figures 4 and 5 illustrate how local surface events such as subduction initiations, 450 ridge creations, plate disappearances or changes in seafloor age at the trench can induce 451 important heat flow variations. Not shown in Figures 4 and 5 is the effect of a continen-452 tal breakup: the result on heat loss is similar to the pattern observed between A and C, 453 with the creation of a new ocean, producing a local pulse of high heat flux. For all cases 454 of heat loss variations that were examined during this study, one or several tectonic re-455 arrangements were observed as the cause of these variations. In Figure 5b, a correlation 456 is clearly observed between the high frequency variations of heat loss and the number 457 of ridges: each ridge creation or disappearance corresponds to an immediate increase or 458 decrease in heat loss, respectively. This short timescale is partly the consequence of our 459 2D geometry: on Earth, actual heat flux variations are due to both the limited lifespan 460 of plate boundaries and the evolving pattern of the seafloor age distribution on a spher-461 ical surface (Labrosse & Jaupart, 2007). 462

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3.3 Comparison to Plate Reconstruction Models

Recent plate reconstructions (e.g. Domeier & Torsvik, 2014; Müller et al., 2016; 464 Vérard et al., 2015; Matthews et al., 2016; Young et al., 2019) give some characteristics 465 of plate tectonics (e.g. plate speed, number of plates, area of subducted material) at most 466 over the last 580 Myr, with increasing incertitude backwards through time. Paleomag-467 netic and paleogeographic data, as well as compilations of the timing of past orogens, 468 are used by Condie et al. (2015) to estimate "plate" speed, actually limited to large con-469 tinents' speed, and the rate of continental collisions since 2.5 Ga. We compare the out-470 puts of our model to some of these data sets. We carried out 200 runs with the param-471 eters indicated in Table 1 (reference case), with varying slightly the initial temperature 472 $(T = 1875 \pm 5 \text{ K})$ and the initial age (3000 \pm 50 Myr). The initial number and posi-473

tions of plate boundaries and continents, as well as the seafloor age distributions, are ran-474 domly pulled so that we have a set of 200 different initial conditions, resulting in 200 dif-475 ferent thermal histories. Runs were started here with 4 continents (of random sizes), but 476 we also carried out experiments with 1, 2 or 8 initial continents (each done over 50 runs), 477 and the results are equivalent, because continents initially gather in one supercontinent, 478 with the transition from several to one continent lasting around 200 Myr. All the runs 479 yield a present-day temperature equal to 1625 ± 25 K. Results are stacked together for 480 each output (temperature, plate RMS speed, continent RMS speed, subduction area flux 481 and number of plates) and we compute percentiles in order to check the possible range 482 of each output. For high mantle temperatures, plate boundaries are fast and colliding 483 with each other before the critical age for subduction initiation is reached anywhere in 484 the model, yielding relatively short phases (10 to 80 Myr) with only one immobile plate, 485 before subduction can be initiated again. As these phases would not occur on the spher-486 ical Earth, where the collision between a ridge and a subduction does not lock the full 487 subduction but triple junctions are possible, we filter out these zero-velocity phases from 488 the stacking of plate and continent speeds. Results are shown in Figure 6. For compar-489 ison, the results obtained with the same parameters for fixed plate boundaries (6 plates, 490 case (b) in Figure 3) are shown with a thin annoted line. Two individual runs among 491 the 200 are shown in the Supporting Information (Figures S1 and S2). 492

Our results are generally consistent with the temperature estimate by Herzberg et 493 al. (2010) (Figure 6(a)). For plate speed (Figure 6(b)) and the area of subducted ma-494 terial (Figure 6(d)), we compare our results to the two existing plate reconstruction mod-495 els extending back into Paleozoic: the model developed at the University of Lausanne 496 (e.g. Vérard et al., 2015) and the models of Müller et al. (2016) (0-230 Ma) and Domeier 497 and Torsvik (2014) (250-410 Ma) combined together by Matthews et al. (2016) and later 498 modified by Young et al. (2019). For plate speed, at the scale of our study, the two mod-499 els are almost equivalent and our median plate speed is in good agreement with them, 500 although exhibiting a very slightly insufficient slowing down since Mesozoic. This is how-501 ever not the case for all individual run (see Supporting Information Figures S1 and S2). 502 For the subduction area flux, Vérard et al. (2015) obtain values that are slightly differ-503 ent from their rate of newly accreted material. In our 2D model, the two values are al-504 ways exactly equal. We therefore plot the data of Vérard et al. (2015) as the average value 505 between their subducted and accreted areas (blue line in Figure 6(d)). The subduction 506

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Figure 6. Long term evolutions obtained over 3 Gyr. Solid lines correspond to the median values over 200 stacked runs, while dark and light gray areas are for 25th-75th and 5th-95th percentiles respectively. (a) Temperature evolution compared to Herzberg et al. (2010). (b-c) RMS value of the speeds of all plates (b) and of the continents alone (c) compared to the results of plate reconstructions and models by Vérard et al. (2015) and Young et al. (2019). Continental speed is also compared to results by Condie et al. (2015). Note that (b) and (c) use the same vertical logarithmic scale. (d) Subduction area flux compared to Vérard et al. (2015) and Hounslow et al. (2018). (e) Number of plates (modified to the number on a sphere, using the method described in appendix C) compared to plate reconstructions data by Matthews et al. (2016). (f) Number of collisions for 16 stacked runs (see text for this choice) compared to Condie et al. (2015). The dashed black line and the solid cyan line are linear regressions respectively for their study and our model over the past 2.5 Gyr only (respective slopes: 1.8 and 1.7 collisions/Ga). Results obtained with fixed plate boundaries (case with 6 plates, equivalent to 22.8 plates on the sphere) are also shown (annoted line). Continental speed is then zero and there are no collisions.

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area flux given by Hounslow et al. (2018), derived from the plate reconstruction models by Müller et al. (2016) and Domeier and Torsvik (2014) combined together by Matthews et al. (2016), is a bit lower (pink line in Figure 6(d)), illustrating the uncertainty in plate reconstructions. The 25-75% range of our 200 runs encompasses both models.

For the speed of continents, we obtain too low values compared to the evolutions 511 given by Young et al. (2019), especially concerning the peak seen by these authors around 512 300-370 Ma (see Figure 6(c)). Young et al. get a continent speed at \sim 13 cm/yr around 513 300-330 Ma, which is outside the 5-95% range of our results for all ages younger than 514 850 Myr. Using paleogeographic and paleomagnetic data, Condie et al. (2015) propose 515 an evolution of "plate speed" (their figure 3), but indicate that their estimate is actu-516 ally done only on large continents, and therefore we plot it against our results for con-517 tinent speed, clearly lower than the RMS on all plates (Figure 6(b)). The 5-95% range 518 of our results encompasses their estimate, although very marginally for ages older than 519 1.5 Gyr and not for their point at 350 Ma. Condie et al. (2015) do not plot the RMS speed 520 of continents as is done by Young et al. (2019) but the weighted-mean (with continents' 521 areas as weights). In Figure 6(c) we use the continent RMS speed for our results. We 522 computed the weighted-mean for comparison: for ages younger than 1 Gyr, the weighted-523 mean for continental speeds is around 20% lower than the RMS speed, and the differ-524 ence is negligible for ages older than 1 Gyr, thereby not rendering our results closer to 525 the estimates of Condie et al. (2015). With our approach, the variability of speeds is clearly 526 larger for continents only (Fig. 6(c)) than for the ensemble of plates (Fig. 6(b)); note that 527 the vertical scale is logarithmic. High continental speeds (over 13 cm/yr) in plate recon-528 structions have been attributed to possible modeling artefacts (e.g. Zahirovic et al., 2015) 529 or discussed as an inadequate choice in the reference frame and in latitude calculations 530 from paleomagnetic data (Condie et al., 2015). Considering the large uncertainty in re-531 constructions prior to the Mesozoic, the high variability of continental speeds and the 532 simplicity of our model (circular geometry and a unique viscosity for the upper mantle, 533 with no continental lithospheric keels), the moderate discrepancy between our model and 534 continental speed data does not rule out our approach. Future work should include im-535 provements in the implementation of continents (adding continental keels with their spe-536 cific viscosity for instance). 537

For the evolution of the number of plates, a direct comparison between our 2D model and actual plate reconstructions on 3D Earth is inadequate. We therefore compute an

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approximate equivalent number of plates on the sphere using the method described in 540 appendix C and plotted in the Supporting Information (Figure S3). For instance, over 541 the 200 stacked runs, the first quartile, median and third quartile for the present-day num-542 ber of plates are 4, 6 and 8, which convert to 8.0, 22.8 and 43.3 on the sphere. With this 543 method, our results are in good agreement with the evolution of the number of plates 544 since late Paleozoic given by Matthews et al. (2016) (Figure 6(e)), but this should be taken 545 with caution as it strongly depends on the method used to extrapolate our results to a 546 spherical geometry. 547

Finally, we compare our results to the evolution of the number of collisions com-548 piled by Condie et al. (2015). Again, our results cannot be directly compared to results 549 on the 2D spherical surface of the Earth. Our 1D Earth's surface contains necessarily 550 less continents, and each continent can only collide with one of its two direct neighbor-551 ing continents. We adopted the following strategy: Condie et al. (2015) obtain a total 552 of 96 collisions between 2.5 Ga and present-day (see their appendix, part 2, column "Col-553 lisional"), while on average, each of our individual run exhibits 6 collisions over this pe-554 riod. We thus added together 16 of our 200 runs, counting the number of collisions per 555 time window of 100 Myr, as is done by Condie et al. (2015), and checked that we had 556 a total of 96 collisions between 2.5 Ga and present-day. Result is shown in Figure 6(f). 557 Between 3 Ga and 2.5 Ga, the steep slope for our study marks the gathering of the ini-558 tial four continents into one supercontinent, before this continent breaks up and colli-559 sions become possible. The general trend for ages younger than 2.5 Gyr is surprisingly 560 similar to the one obtained by Condie et al. (2015), with almost the same linear regres-561 sion slope. Again, this result strongly depends on the chosen strategy to go from a 1D 562 to a 2D surface, but the increasing collision frequency over time is obtained for any in-563 dividual run and for the sum of the 200 runs. This is not in contradiction with the de-564 crease in plate speed obtained at the same time over 2.5 Gyr: with an increasing num-565 ber of plates (and of continents), collisions become more frequent over time even if plates 566 are slowing down. 567

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3.4 Testing MACMA Parameters

Our model is controlled by many parameters (see Table 1) and assessing the individual and interdependent effects of each of them is beyond the scope of the present study. Some parameters were chosen as they correspond to usual estimates and yield ac-

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cepted present-day plates' speeds (see section 2.1.3). Here we focus on parameters whose 572 values are not precisely known: the mantle activation energy E, the viscosities $\eta_{\rm lm_0}$, $\eta_{\rm um_0}$ 573 and $\eta_{\rm pl_0}$, the continental strength $F_{\rm lim}$ and the present-day critical age for subduction 574 initiation $\tau_{\rm subd_0}$. We do not carry a thorough parametric study but vary each param-575 eter around its reference value given in Table 1. The ratio of lower to upper mantle vis-576 cosities $(\eta_{\rm lm_0}/\eta_{\rm um_0} = 100)$ as well as the ratio of oceanic lithosphere to upper mantle 577 viscosities $(\eta_{\rm pl_0}/\eta_{\rm um_0} = 250)$ are kept constant so that cases hereafter are identified only 578 by the lower mantle viscosity $\eta_{\rm lm_0}$. 579

For this study, we choose the initial mantle temperature so that after 3 Gyr of run the obtained present-day temperature is close to the reference one $(T_{m_0} = 1625\pm25 \text{ K})$. We present three outputs: the temperature as a function of age, and the plate RMS speed and the number of plates as a function of temperature (Figures 7 and 8). For each parameter, 50 runs are stacked together, and results are sorted into 10 K bins of temperature.

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3.4.1 Effect of Parameters Controlling Viscosities

The evolution of the viscosities $\eta_{\rm lm}$, $\eta_{\rm um}$ and $\eta_{\rm pl}$ as a function of temperature de-587 pends on the activation energy E (see Eq. 2). As we study cases that are all yielding the 588 same present-day temperature, E affects the factor by which past viscosities are reduced 589 compared to present ones. We test activation energies ranging from 250 to 450 kJ.mol^{-1} . 590 The values 250 and 450 kJ⁻¹ imply that the viscosities are divided by a factor 7.6 and 591 38.5, respectively, when the temperature is increased by 200 K compared to the present-592 day one $(T_{m_0} = 1625 \text{ K})$. In addition, the present-day lower mantle viscosity η_{lm_0} serves 593 as a reference for all viscosities, and varying η_{lm_0} by a certain factor amounts to mul-594 tiply all viscosities (lower mantle, upper mantle and oceanic lithosphere), at all temper-595 atures, by the same value. Compared to the present-day reference value ($\eta_{\rm lm_0} = 5 \times$ 596 10^{22} Pa.s), we test viscosities multiplied by factors ranging from 1/4 to 4. 597

Results are presented in Figure 7, both for evolving plate boundaries and for a fixed configuration (2 continents, 6 plates: case (b) in Figure 3, shown with a black solid line in Figure 3(e) and (f)). The thermal runaway backwards in time occurs in the fixed configuration for all tested values of E and $\eta_{\rm lm_0}$ (Figure 7(a) and (d)). With evolving plate boundaries, all thermal evolutions are consistent with the estimates of (Herzberg et al., 2010). They do not strongly depend on the activation energy E and only slightly on the



Figure 7. Long term evolution of temperature as a function of age (a and d), average plate RMS speed (b and e) and average number of plates (c and f) as a function of temperature (by bins of 10 K), with varying the activation energy E (a, b and c) and the present-day viscosity $\eta_{\rm lm_0}$ (d, e and f). Thick lines with symbols are for evolving plate boundaries while thin ones are for fixed boundaries, considering 6 plates (see Figure 3(b)).

present-day reference viscosity $\eta_{\rm lm_0}$. However, varying the viscosities, either only in the past when changing E or throughout the full evolution when changing $\eta_{\rm lm_0}$, strongly affects the speed of plates: as expected, high viscosities yield lower speeds (see Figure 7(b) and (e)). Speeds obtained with evolving plate tectonics are close to the ones obtained for the same parameters with a fixed configuration.

But with evolving plate tectonics, the number of plates is also affected by a change in the viscosity: a high viscosity implies slower plates, which reaches the critical age for subduction τ_{subd} for a smaller width. The tensive shear force that controls continental break up is also stronger for a higher value of the viscosity, so that continents will break up more easily. A higher viscosity thus results in a larger number of plates (see Figure 7(c) and (f)).

The cooling rate is controlled by the oceanic heat flux, itself computed from the seafloor age distribution. Faster plates, with a fixed size, exhibit young oceanic ages and

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thus a high heat loss. But with our approach for evolving plate boundaries, viscosities 617 do not affect only the speed of plates but also their size, as can be expected if subduc-618 tion initiation and ridge creation through continental breakup are phenomena where vis-619 cous stresses have to overcome a given yield strength. Varying the viscosities produces 620 two opposite effects: increasing the viscosity slows down plates but decreases their size 621 (i.e. increases their number), so that the average seafloor age does not vary much and 622 the cooling rate is not strongly affected by a change in the viscosity parameters (E or 623 $\eta_{\rm Im_0}$). One may note here that temperature evolution alone is not sufficient to assess the 624 effect of physical parameters on mantle cooling dynamics. 625

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3.4.2 Effect of Parameters Controlling Oceanization and Subduction Initiation

The continental strength F_{lim} controls the time needed for continents to breakup 628 (see appendix B). We test values ranging from half the reference one to infinity (conti-629 nents never break up). τ_{subd_0} is the present-day critical age for subduction initiation and 630 we test values ranging from 140 to 220 Myr. The values 140 and 220 Myr yield a crit-631 ical age for subduction initiation equal to 106 and 167 Myr, respectively, for a temper-632 ature 200 K higher than the present-day one (see Eq. 9). Results are shown in Figure 8. 633 Varying these two parameters, $F_{\rm lim}$ and $\tau_{\rm subd_0}$, does not modify the plate speed as 634 a function of temperature (see Figure 8(b) and (e): note that lines for evolving or fixed 635 plate boundaries cannot be distinguished), but it strongly affects the average cooling rates. 636 This is due entirely to the change in the geometry of plates: a lower continental strength 637 or a younger critical age for subduction both imply a larger number of plates and plate 638 boundaries at all temperatures. With no change in the plate speed, this necessarily gives 639 overall younger seafloor ages and a more efficient heat loss. For the range of tested pa-640 rameters here, the obtained thermal evolutions are all compatible with the estimates of 641 Herzberg et al. (2010). $\tau_{\rm subd_0}$ and $F_{\rm lim}$ cannot be more constrained by our study. More 642 insight in the mechanisms of oceanization and subduction initiation would be necessary. 643 Subduction initiation probably depends on many surface factors, such as sedimentary 644 loading or variable thickness of the continental crust (e.g. Nikolaeva et al., 2011; Levy 645 & Jaupart, 2012). Similarly, a unique continental strength $F_{\rm lim}$ cannot account for lo-646 cal structural inheritance. Although our parameterization here is simple, we show that 647



Figure 8. Long term evolution of temperature as a function of age (a and d), plate RMS speed (b and e) and number of plates (c and f) as a function of temperature, with varying the continental strength F_{lim} (a, b and c) and the present-day critical age for subduction initiation τ_{subd_0} (d, e and f).

a fairly wide range of τ_{subd_0} and F_{lim} , that could account for geographical variations, can yield a reasonable thermal history.

650 4 Discussion

In our 2D model of evolving plate tectonics, plate velocities are controlled by the 651 balance between driving forces (slab pull, ridge push and slab suction) and viscous re-652 sistive forces (horizontal mantle drag, vertical viscous shear on slabs and bending dis-653 sipation for subduction zones). For individual plates with fixed boundaries (one ridge 654 and one permanent subduction), this force balance yields a scaling for the heat flux as 655 a function of temperature equivalent to the one obtained with isoviscous convection mod-656 els in a fixed geometry (runaway relation $Nu \sim Ra^{1/3}$, see Figure 3). When plate bound-657 aries are free to move, collide, be created and disappear, plate speed follows approximately 658 the same scaling as a function of temperature as for fixed convective cells (see Figure 7(b, 659 e) and 8(b, e)), but the thermal evolution is completely changed. We obtain a moder-660

ate heat loss over 3 Gyr, with large fluctuations on a short timescale that can be linked
to rearrangements of plate tessellation (see Figure 5) and a reasonable thermal evolution on a long timescale (Figure 6(a)). In our model, the moderate heat flux obtained
even with a strong temperature-dependence of plate speed is to due to the increase in
the number of plates over time: a warm mantle in the past implies large plates, and seafloor
ages remain thereby sufficiently old to yield a moderate heat loss even in the Archean
and early Proterozoic.

The idea of longer and thus less numerous plates in the past may seem counter-668 intuitive. Recently, Mallard et al. (2016) rather suggested an elongation of plates over 669 time as the mantle cools down, which prompted Matthews et al. (2016) to attribute the 670 smaller number of plates they obtain prior to the Cenozoic (see orange line in Figure 6(e)) 671 to the lack of seafloor preservation which hinders reconstructions of small plates. From 672 3D spherical models of mantle convection with a visco-pseudoplastic rheology that self-673 consistently generates plate boundaries, Mallard et al. (2016) observe that a higher yield 674 stress generates longer plates. With our approach, a higher yield stress is equivalent to 675 an older critical age for subduction initiation. In our model, at a given temperature, choos-676 ing a higher value of τ_{subd_0} yields a smaller number of plates (see Figure 8(f)), but the 677 number of plates is still increasing with time, which is contrary to the interpretation made 678 by Mallard et al. (2016). Their statistical study is based on a few number of snapshots 679 from steady-state simulations which is not per se a model of Earth's thermal evolution. 680 They infer that with time, the lithosphere becomes comparitively stronger relative to de-681 clining mantle forces, and that a colder mantle would therefore correspond to a relative 682 higher yield stress. However, the assertion that mantle forces are declining when the man-683 the cools down is puzzling, as the decrease of convective vigor over time means that ve-684 locities are indeed decreasing, but mantle viscosity is increasing and the latter effect is 685 the stronger of the two for a terrestrial activation energy. Considering that mantle forces 686 can be approximated by the product of the viscosity η and a characteristic velocity U, 687 it can be shown that 688 1 /0

$$\frac{\eta U}{\eta_0 U_0} = \left(\frac{\Delta T}{\Delta T_0}\right)^{2/3} \left(\frac{\eta}{\eta_0}\right)^{1/3} \tag{13}$$

with using the classical scaling for convective velocity $U \sim Ra^{2/3}$ (Turcotte & Schubert, 2002). A 200 K increase in temperature compared to present day results in a 2.3fold decrease of mantle forces ηU (for E=350 kJ.mol⁻¹). As a result, longer plates for a comparatively higher yield stress in simulations by Mallard et al. (2016) are actually

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⁶⁹⁴ also pointing to a smaller number of plates in the past, as is observed by Matthews et ⁶⁹⁵ al. (2016) and obtained in our study (Figure 6(e)).

It has been argued that the lifetime of passive margins was a proxy for the tempo 696 of plate tectonics (Silver & Behn, 2008; Condie et al., 2015). Bradley (2008) compiled 697 geological and geochemical data in the Phanerozoic and Proterozoic to estimate the lifes-698 pan of passive margins over time, and showed that Precambrian passive margins may 699 have survived longer than Phanerozoic ones. Several authors infer that this suggests slower 700 plate tectonics in the past (Korenaga, 2011; Condie et al., 2015), but the geometry of 701 the plate network was not considered: a longer lifespan of tectonic entities such as pas-702 sive margins is also possible when plates are longer. With fewer plate boundaries, oro-703 genic cycles that destroy passive margins are less frequent, so that even with faster plates 704 in the past, our approach is consistent both with a longer survival of passive margins in 705 the late Archean and Proterozoic and with an increasing number of collisions with time 706 (Figure 6(f)). 707

We show that surface parameters controlling the oceanization process (continen-708 tal strength $F_{\rm lim}$) and subduction initiation (present-day critical age $\tau_{\rm subd_0}$) are govern-709 ing Earth thermal evolution (Figure 8) in our model because they regulate the geom-710 etry of plate tectonics, without affecting plate speeds. On the other hand, parameters 711 controlling the viscosity (reference present-day viscosity η_{lm_0} and activation energy E) 712 have a strong control on plate speed, but almost no effect on thermal evolution because 713 they also have an effect on plate length which opposes the one on plate speed in terms 714 of seafloor age and heat loss (Figure 7). When assessing the validity of a model of Earth 715 thermal evolution, it is thus important to use available constraints not only on temper-716 ature, but also on plate speeds and sizes, even if those data are available only through 717 the Phanerozoic. 718

Future studies should focus on the two processes that create new plate boundaries. Our criterion for subduction initiation may indeed be challenged: numerous processes have been proposed for the onset of subduction (e.g. McKenzie, 1977; Cloetingh et al., 1989; Mueller & Phillips, 1991; Gurnis et al., 2004; Crameri & Kaus, 2010; Nikolaeva et al., 2011; Levy & Jaupart, 2012; Ulvrova et al., 2019) and relying simply on the ratio between the negative buoyancy of the oceanic lithosphere and a fixed yield stress (Eq. 9) does not reflect the complexity of this key terrestrial process. Continental breakup is also simplified in our model, with an approach relying on a parameterized scaling for the di-verging force below insulating continents as a function of time and of mantle viscosity.

Recently, Patočka et al. (2020) showed that the role of heat flow coming from the 728 core should not be neglected, while we considered the same cooling rate for the mantle 729 and the core (Eq. 1). A future study should include the non-zero heat flow coming from 730 the core, and a parameterized model of core cooling could be coupled to our model. Our 731 treatment of continents is also a simplification: they are perfectly insulating and their 732 total surface area is fixed. The latter point is not critical here as our simulations start 733 at 3 Ga and many models of continental crust growth predict that the present-day con-734 tinental fraction was reached in less than 1 Gyr (e.g. Armstrong, 1991; Rosas & Kore-735 naga, 2018). But the possibility of continental growth, with the coeval depletion in ra-736 dioactive elements, coupled to the subduction rate that can be tracked with our approach, 737 could bring an additional constraint to our model. 738

The only parameter controlling the evolution of the viscosities in our model so far 739 is temperature (Eq. 2), while water concentration has a non-negligible effect on viscosi-740 ties (e.g. Hirth & Kohlstedt, 1996; Mei & Kohlstedt, 2000). The possible stiffening ef-741 fect of dehydration of the oceanic lithosphere can slow down plates and strongly affect 742 Earth's thermal evolution (Korenaga, 2006). The feedback between mantle hydration 743 and heat loss was studied by Crowley et al. (2011) and Korenaga (2011), but with a pa-744 rameterized approach that does not explicitly address the effect of the viscosity on the 745 geometry of plate tectonics. As individual parametrizations for local processes can be 746 added in our model, testing for the effect of mantle hydration over time through the sub-747 duction of hydrated oceanic crust is possible, in order to discuss the feedback between 748 viscosities, plate speeds and plate sizes. 749

Even though our simple model yields a thermal history consistent with geochem-750 ical constraints and plate reconstructions, the additional complexities recently consid-751 ered to solve the "thermal catastrophe" paradox, such as heat flow from the core (Patočka 752 et al., 2020) and mantle hydration over time (Crowley et al., 2011; Korenaga, 2011) are 753 not ruled out by our approach, but we infer that the effect of those complexities on the 754 geometry of plates should be studied. Studying the control that a parameter exerts on 755 the speed of plates only, without verifying the effect on their geometry, is not sufficient 756 to understand the role of this parameter on Earth's thermal evolution. 757

758 5 Conclusion

We propose a model of Earth's thermal history relying on a simple force balance 759 for individual plate speed and on behavioral laws for the motion, creation and destruc-760 tion of plate boundaries, based on present-day observations. The viscosity of the man-761 the exerts the main control on plate speeds in our model, as in isoviscous convective cells. 762 This yields a thermal runaway if plates have fixed sizes. With the additional motion of 763 plate boundaries, which collide, disappear and are created when a given yield strength 764 is overcome, we obtain a moderate temperature evolution consistent with geochemical 765 estimates over the past 3 Gyr, an increasing rate of collisions between continents also 766 in agreement with paleogeographic reconstructions since the Archean, and a slowdown 767 of plates and increase in their number that match recent plate reconstructions over the 768 Phanerozoic. We infer that localized surface processes that control the geometry of plate 769 tectonics are key to understand Earth's thermal evolution. 770

771 Appendix A Equivalent Viscosities for Resistive Forces

The vertical viscous shear VS on descending slabs is taken into account in the upper mantle only, and the characteristic width of the sheared zone is $d_{\rm um}/2$ (Grigné et al., 2005), which gives

VS =
$$-\eta_{\rm um} \left(\frac{U}{d_{\rm um}/2}\right) \min(Z, d_{\rm um}).$$
 (A1)

Writing VS = $-\eta_{\rm VS} U$ yields

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$$\eta_{\rm VS} = 2 \left(\frac{\min(Z, d_{\rm um})}{d_{\rm um}} \right) \eta_{\rm um}$$
 (A2)

where Z is the depth reached by the slab.

For the horizontal mantle drag MD, we consider that the whole mantle is sheared.

- We denote by U_i the horizontal velocity at the interface between the upper and lower
- mantle. Considering that the viscous shear is continuous across this interface, we have

$$\eta_{\rm um} \left(\frac{U - U_i}{d_{\rm um}} \right) = \eta_{\rm lm} \left(\frac{U_i}{d_{\rm lm}} \right). \tag{A3}$$

⁷⁸³ The horizontal drag is

$$MD = -\eta_{um} \left(\frac{U - U_i}{d_{um}}\right) L$$
(A4)

where L is the length of the plate. Eliminating U_i with Eq. A3 and writing $MD = -\eta_{MD} U$ gives an equivalent viscosity

$$\eta_{\rm MD} = \left(\frac{d_{\rm um}}{\eta_{\rm um}} + \frac{d_{\rm lm}}{\eta_{\rm lm}}\right)^{-1} L.$$
 (A5)

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We use the expression for bending dissipation given by Buffett (2006):

$$B = -\frac{2}{3} \eta_{pl} \left(\frac{\delta(\tau_{max})}{R_{min}}\right)^3 U$$
(A6)

where $\delta(\tau_{\text{max}})$ is the thickness of the lithosphere at the trench, given by equation (3).

⁷⁹¹ Writing
$$B = -\eta_B U$$
 yields

$$\eta_{\rm B} = \frac{2}{3} \left(\frac{\delta(\tau_{\rm max})}{R_{\rm min}} \right)^3 \eta_{\rm pl}. \tag{A7}$$

⁷⁹³ Appendix B Divergence Force under Continents

We consider advection created by the warming and consequent upwelling of the mantle under insulating continents. The affected zone has a thickness denoted by b, and ais the width of the continent (see Figure 1C). Hereunder, the excess temperature due to continental insulation and internal heating is denoted by ΔT_h and the advective horizontal velocity under the continent by u_h . Heat conservation, taking into account advection with a uniform velocity u_h under the continent and internal heat H, can be written

$$\rho c_p \left(\frac{d\Delta T_h}{dt} + 2u_h \ \frac{\Delta T_h}{a/2} \right) = H. \tag{B1}$$

⁸⁰² Denoting by w_h the vertical velocity below the continent, mass conservation implies w_h $(a/2) = u_h b$. The below is between the boundary driving force and the since the strengthere are strengthere.

The balance between the buoyancy driving force and the viscous shear stress, given by

Turcotte and Schubert
$$(2002)$$
, is

$$\alpha \rho \ g \Delta T_h \ (a/2) \ b \ w_h = \eta_{\rm um} \left(\frac{b \ w_h^2}{a/2} + \frac{(a/2) \ u_h^2}{b} \right). \tag{B2}$$

Using mass conservation to eliminate w_h , this yields

$$u_h = \frac{(a/2) \gamma}{2\eta_{\rm um}} \Delta T_h \tag{B3}$$

where γ is a "thermal stress" (in Pa.K⁻¹) given by:

$$\gamma = \frac{2b \ \alpha \rho g}{\left(\frac{a/2}{b}\right)^2 + \left(\frac{b}{a/2}\right)^2}.$$
(B4)

Eq. B1 becomes

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$$\frac{d\Delta T_h}{dt} + \frac{\gamma}{\eta_{\rm um}} \Delta T_h^2 = \frac{H}{\rho c_p}.$$
(B5)

With the initial condition $\Delta T_h = 0$ for t = 0, the solution is

$$\Delta T_h(t) = \Delta T_{\text{max}} \tanh\left(\frac{t}{t_{\text{warm}}}\right)$$
 (B6)

814 where

$$\Delta T_{\max} = \sqrt{\frac{\eta_{\rm um} \ H}{\gamma \ \rho c_p}} \qquad \text{and} \qquad t_{\rm warm} = \sqrt{\frac{\eta_{\rm um} \ \rho c_p}{\gamma \ H}}.$$
 (B7)

The excess temperature ΔT_h under the continent can reach a maximum equal to ΔT_{max} and the characteristic warming duration is proportional to t_{warm} (ΔT_h is 76% of ΔT_{max} for $t = t_{\text{warm}}$). The shear tensive force exerted by u_h under the continent is then

$$F(t) = 2 \eta_{\rm um} \frac{u_h}{b} (a/2) = \gamma \Delta T_h(t) \frac{(a/2)^2}{b}.$$
 (B8)

Appendix C Conversion of the Number of Plates from a Circle to a Sphere

- For the geometry of MACMA, we denote by $N_{\rm C}$ the number of plates along the circle of radius $R_{\rm E}$. The equivalent number of plates on the sphere of the same radius $R_{\rm E}$ is written as $N_{\rm S}$ hereafter. We consider plates of equal size, defined by the arc angle θ . If there are $N_{\rm C}$ plates in our MACMA model, then this angle is:
 - $\theta = \frac{2\pi}{N_{\rm C}} \tag{C1}$

For small enough 2D polygonal plates, it is obvious that a larger number $N_{\rm S}$ of plates whose size is described by the arc angle θ can be fitted on the sphere than the number $N_{\rm C}$ for 1D plates of size θ . Here, we consider the 2D plates on the sphere to be spherical equilateral triangles, with sides' angles equal to θ and vertices' angles denoted by α . The relation between sides (θ) and vertices (α) angles is

$$\cos(\alpha) = \frac{\cos(\theta) - \cos^2(\theta)}{\sin^2(\theta)}$$
(C2)

The surface area of each triangle is $A = R_{\rm E}^2 (3\alpha - \pi)$, so that the number of triangles that can fitted on the sphere is

$$N_{\rm S} = \frac{4\pi R_{\rm E}^2}{A} = \frac{4\pi}{(3\alpha - \pi)}$$
 (C3)

The conversion from the number of plates $N_{\rm C}$ on the circle to $N_{\rm S}$ on the sphere is thus

done this way: we compute the average arc angle θ from Eq.C1, then deduce the ver-

tices' angle α of triangular plates on the sphere (Eq. C2) and finally compute N_S from

Eq. C3. Note that Eq. C2 is valid only for $\alpha < 2\pi/3$, which corresponds to $N_{\rm C} > 3$ 839 (Eq. C1), so that for $N_{\rm C} \leq 3$ we use $N_{\rm S} = N_{\rm C}$ (see Supporting Information Figure S3). 840 This conversion is a rough approximation, as we consider equal-sized plates with 841 a simple unique geometry. Another choice for this geometry on the sphere would obvi-842 ously yield another result. We chose triangles for the simplicity of the conversion and 843 because a sphere can be entirely tiled by equilateral spherical triangles, which is not the 844 case with spherical caps for instance. The purpose here is only to transform our circu-845 lar geometry to a spherical estimate that can be compared to actual plate reconstruc-846 847 tions.

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Figure 1.

Figure 2.

Predicted present-day plates' speeds

Figure 3.

Figure 4.

Figure 5.

Figure 6.

Figure 7.

Figure 8.

