The Composition of ~96 keV W+ in Saturn's Magnetosphere

Stephen Christon^{1,1}, Robert DiFabio^{2,2}, Douglas Hamilton^{3,3}, Donald Mitchell^{4,4}, and Tom Krimigis^{4,4}

¹Focused Analysis & Research ²University of Maryland. University of Louisiana ³University of Maryland ⁴JHU/APL

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Abstract

The plumes of Enceladus produce a cloud of neutral H2O molecules and, via dissociation, OH and O. These neutrals are ionized by charge exchange, solar UV, and electron impacts, producing the thermal water group ions W+ (O+, OH+, H2O+, and H3O+) which become energized in Saturn's magnetosphere. We first separate the components of energetic (~96 keV) W+ using Cassini Charge-Energy-Mass Spectrometer (CHEMS) data from 78 near equatorial main ring current passes (dipole L = 7-16, $\pm 10^{\circ}$ in latitude) in 2004-2010. We find ~53% O+, ~22% OH+, ~22% H2O+, and ~3% H3O+ when averaged over L = 7-16, resulting in a mean water group mass of 16.7 amu. At 7 < L < 21, we find abundance ratios for O+/W+, OH+/W+, and H2O+/W+ that vary little with L. However, while H3O+/W+ is nearly constant at L > 13, H3O+/W+ tends to increase persistently at L < ~10. The large O+ abundance qualitatively agrees with the broad atomic O cloud observed by Cassini and predicted by some models. Our observation of H2O+/W+ > ~20% out to L ~ 21 suggests that neutral H2O spreads throughout the magnetosphere rather than being confined to a narrow H2O torus centered on Enceladus' orbit.

1	The Composition of ~96 keV W^+ in Saturn's Magnetosphere
2	R. D. DiFabio ^{1,2} , D. C. Hamilton ¹ , S. P. Christon ^{3*} , D. G. Mitchell ⁴ , S. M. Krimigis ^{4,5}
3	1. University of Maryland, Department of Physics, College Park, MD, USA
4	2. University of Louisiana, Department of Physics, Lafayette, LA, USA
5	3. Focused Analysis and Research, Charleston, SC, USA
6	4. Johns Hopkins University, Applied Physics Laboratory, Laurel, MD, USA
7	5. Academy of Athens, Athens, Greece
8	
9	*Corresponding author: S.P. Christon, spchriston@aol.com
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11 12	Key Points:
13 14	• On average, for ~96 keV ions, fractional abundances at $L = 7-16$ are $O^+/W^+ \sim 0.53$, $OH^+/W^+ \sim 0.53$, OH^+/W^+ , $OH^+/W^+ \sim 0.53$, OH^+/W^+ , $OH^+/W^+/W^+$, $OH^+/W^+/W^+$, $OH^+/W^+/W^+/W^+$, $OH^+/W^+/W^+/W^+/W^+/W^+/W^+/W^+/W^+/W^+/W$
15	0.22, $H_2O^+/W^+ \sim 0.22$, and $H_3O^+/W^+ \sim 0.03$
16	• The partial number densities O^+ , OH^+ , H_2O^+ and H_3O^+ , peak at dipole $L \sim 9.5$ and the ratios
17	O^+/W^+ , OH^+/W^+ , and H_2O^+/W^+ vary little with L
18	• At L < 13, H_3O^+/W^+ decreases significantly with increasing L, whereas at L > 13 H_3O^+/W^+
19	varies little with L
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27 Abstract

28 The plumes of Enceladus produce a cloud of neutral H₂O molecules and, via dissociation, OH 29 and O. These neutrals are ionized by charge exchange, solar UV, and electron impacts, producing the thermal water group ions W^+ (O^+ , OH^+ , H_2O^+ , and H_3O^+) which become energized 30 31 in Saturn's magnetosphere. We first separate the components of energetic (~96 keV) W^+ using Cassini Charge-Energy-Mass Spectrometer (CHEMS) data from 78 near equatorial main ring 32 33 current passes (dipole L = 7-16, $\pm 10^{\circ}$ in latitude) in 2004-2010. We find ~53% O⁺, ~22% OH⁺, $\sim 22\%$ H₂O⁺, and $\sim 3\%$ H₃O⁺ when averaged over L = 7-16, resulting in a mean water group mass 34 of 16.7 amu. At 7 < L < 21, we find abundance ratios for O^+/W^+ , OH^+/W^+ , and H_2O^+/W^+ that 35 vary little with L. However, while H_3O^+/W^+ is nearly constant at L > 13, H_3O^+/W^+ tends to 36 increase persistently at L < ~ 10 . The large O⁺ abundance qualitatively agrees with the broad 37 38 atomic O cloud observed by Cassini and predicted by some models. Our observation of H_2O^+/W^+ $> \sim 20\%$ out to L ~ 21 suggests that neutral H₂O spreads throughout the magnetosphere rather 39 40 than being confined to a narrow H₂O torus centered on Enceladus' orbit.

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44 Introduction

45 [1] The discovery of OH in Saturn's magnetosphere by the Hubble Space Telescope (HST) 46 indicated that Saturn's magnetosphere contains a significant source of neutral H₂O (Shemansky 47 et al., 1993). Using Voyager and HST observations, Jurac and Richardson (2005) modeled the 48 plasma and neutral particles in Saturn's magnetosphere and predicted that the majority of the H₂O was coming from Enceladus at a rate of $\sim 10^{28}$ H₂O/s, a small moon at ~ 4 R_S (the Saturn 49 50 radius; please note that near the equator, dipole L = 1 is about 1 R_S). The discovery of water 51 plumes in the south-pole region of Enceladus by the Cassini mission confirmed their predictions 52 (Waite et al., 2006; Hansen et al., 2006; Porco et al., 2006). Typical estimates of the plume source strength range from $\sim 1-4 \times 10^{28}$ H₂O/s (Burger et al., 2007; Jia et al., 2010; Dong et al., 53 2011), but some studies suggest that the source strength varies significantly with time and can be 54 as low as ~0.6-0.7x10²⁸ H₂O/s (Saur et al., 2008; Smith et al., 2010). Cassini measurements of 55 the ionized H₂O products (O^+ , OH^+ , H₂ O^+ , and H₃ O^+ , collectively called W⁺) in the plume 56 indicated that H₃O⁺ was an important component of the Enceladus plume's thermal ionosphere 57 58 (Cravens et al., 2009), whereas, at energetic, that is, suprathermal energies, O^+ dominates, followed by OH^+ and H_2O^+ (Krimigis et al., 2005). Sergis et al. (2010) found that (a) the 59 60 contribution of the energetic particles to the total particle pressure becomes significant at >9 R_s 61 and progressively overtakes the thermal plasma beyond 12 Rs, and (b) Saturn's ring current at 62 \sim 8-18 R_s is intense and variable, being primarily inertial, determined by thermal particles, at <8.5 R_s but increasingly pressure gradient-driven by suprathermal particles in its maximum 63 64 region (8 to $12 R_s$) and certainly farther out.

[2] Charge exchange is especially important for both the ions and the neutral particles in Saturn's
inner magnetosphere because of the high neutral gas densities (Mauk et al., 2009). Johnson et al.

68 (2006) concluded that charge exchange reactions between ions and the neutral particles emitted 69 by Enceladus produce a broad OH cloud and leave a narrow H₂O torus centered on Enceladus' 70 orbit (a region roughly collocated with a torus of dust and ice grains called the E-ring, see e.g., 71 Showalter et al., 1991; and Cassidy & Johnson, 2010). Although this model reproduced the OH 72 torus observed by HST, it, along with other models that were based on data prior to the Cassini 73 mission (e.g. Richardson et al., 1998; Jurac and Richardson, 2005), had to be revised. Re-74 analysis of the OH observations by HST revealed that the OH cloud was broader than initially 75 thought (Melin et al., 2009). Additionally, the Cassini Ultraviolet Imaging Spectrograph (UVIS) 76 observed an O cloud twice as broad as the OH cloud (Melin et al., 2009; Persoon et al., 2009; 77 2013). Further, Cassini observations of the plasma electrons (Schippers et al., 2008) and ions 78 (Wilson et al., 2008; McAndrews et al., 2009; Thomsen et al., 2010; Sittler et al., 2008; 79 Holmberg et al., 2012; 2014; 2017; Livi et al., 2014) greatly improved the understanding of the 80 plasma environment in Saturn's magnetosphere, so the dissociation and ionization rates of the 81 neutrals had to be revised.

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83 [3] Interactions of the neutral particles in Saturn's neutral cloud with plasma and solar UV 84 photons, such as charge exchange, electron impact ionization and photoionization, produce O⁺, OH⁺, H₂O⁺, and H₃O⁺ (Ip, 1997; 2000; Johnson et al., 2006; Smith et al., 2010; Cassidy & 85 86 Johnson, 2010; Fleshman et al., 2010a). The combination of these four species is typically called the water group W^+ . H_3O^+ is produced largely by charge exchange reactions in the Enceladus 87 88 torus (Cravens et al., 2009; Fleshman et al., 2010) and was observed to be a prominent W⁺ 89 component at thermal energies during Cassini's Saturn Orbit Insertion (SOI) (Young et al., 2005; 90 Sittler et al., 2008) and during Enceladus flybys (Tokar et al., 2006, 2009; Cravens et al., 2009). 91 However, the overall importance of thermal OH^+ and H_2O^+ , and a diminished importance of 92 thermal H_3O^+ , except possibly near Enceladus and at <4.75 R_s, has recently been demonstrated 93 in a preliminary study by Wilson et al. (2015).

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[4] Electron impact dissociation and photo-dissociation of H₂O and OH are common sources of 95 96 H, OH, and O in Saturn's magnetosphere (e.g., Fleshman et al., 2010a,b), efficiently spreading 97 these neutral species throughout the magnetosphere (e.g. Smith et al., 2010a,b). Outside of ~ 8 R_s, the O cloud predicted by Smith et al. (2010) was not in agreement with the UVIS 98 99 observations (Melin et al., 2009). Assuming the UVIS results are correct, the discrepancy may be 100 the result of neglecting the effect of neutral-neutral collisions in the model, which is another 101 effective mechanism for spreading neutral particles (Farmer, 2009). Cassidy & Johnson (2010) 102 include the effects of neutral-neutral collisions in their model, and their estimates of the O 103 density are in better agreement with the results from Melin et al. (2009). However, the O density 104 from Cassidy & Johnson (2010) is from a factor of ~2-4 less than that estimated by Melin et al. 105 (2009) at ~10 to 20 R_S. Including the collisions between neutrals significantly increased the H_2O 106 density in Saturn's middle and outer magnetosphere. Models that ignore neutral-neutral 107 collisions (e.g., Johnson et al., 2006) predict a narrow H₂O torus centered on Enceladus with a 108 negligible H₂O density outside of 6 R_S, while including the neutral-neutral collisions results in an 109 H₂O cloud with approximately the same density as OH outside of 7 R_s (Cassidy & Johnson, 110 2010).

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112 [5] Ion observations from many Cassini orbits revealed that W^+ is the most abundant ion species 113 in Saturn's equatorial plane from thermal (Thomsen et al., 2010) to suprathermal energies 114 (DiFabio et al., 2011). Initial Cassini Plasma Spectrometer (CAPS) observations from SOI 115 indicated that inside of 10 R_s, the thermal water group consists mostly of molecular ions with an average mass of approximately 18 amu (Figure 16 in Sittler et al., 2008; see also Persoon et al.,
2009). Subsequent analysis of CAPS ion data from two Cassini orbits in 2011 by Wilson et al.
(2015) found a similar value, ~17.6 amu.

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120 [6] The results from our initial analysis of the Cassini Charge-Energy-Mass Spectrometer 121 (CHEMS) data from two years of Cassini orbits at Saturn was reported by Mauk et al. (2009) in their Table 11.3, where 127-145 keV W⁺ was estimated to consist of 46% O⁺, 24% OH⁺, 25% 122 H_2O^+ , and 5% H_3O^+ (see also Difabio, 2012). In the present study, we use the data from CHEMS 123 to separate ~96 keV W⁺ into O⁺, OH⁺, H₂O⁺, and H₃O⁺. The data are now more clearly 124 understood, the fitting procedure used to determine the composition of W⁺ has been refined since 125 126 the analysis reported in Mauk et al. (2009), and the data interval extended, so the results 127 presented here provide a better estimate of the suprathermal W⁺ composition. First, we determine the average W^+ composition in the equatorial ring current region (at L = 7-16 and $\pm 10^{\circ}$ Latitude) 128 129 from 2004-348 to 2010-356, in order to complement DiFabio et al. (2011), the first Cassini study 130 of the long-term variations of the major suprathermal ions in Saturn's magnetospheric equatorial 131 ring current region. Then, extending the radial range to L=21, we present the first examination of suprathermal W⁺ and its compositional component variations with L, which we then compare to 132 133 the thermal ion composition measurements from CAPS reported by Wilson et al. (2015) and 134 model results, including those of Fleshman et al (2013) which provide background in the Wilson et al. analysis. 135

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137 CHEMS Instrument

138 [7] CHEMS uses energy per charge (E/Q) selection followed by time-of-flight (TOF) versus 139 energy measurements to identify positive ions with E/Q = 3-220 keV/e. CHEMS has an overall

field of view of 159° x 4° with the large angle divided into three independent 53° sections called 140 141 telescopes. With the measurement of E/Q, TOF, and kinetic energy with a solid-state detector 142 (SSD) located at the end of the TOF path, the mass, energy and charge state can be determined. 143 The SSD has an electronic threshold of 26 keV. When nuclear defect is included, energy 144 measurements can only be made for protons above 27 keV and oxygen above 47 keV. Herein, 145 we focus on the narrow energy channel at ~96 keV (specifically 95.9 ± 2.9 keV. Vandegriff et al., 2018), which has the lowest W^+ instrumental background, in order to achieve the most 146 effective H_2O^+ and H_3O^+ separation. Below that energy, only the E/Q and mass per charge (M/Q) 147 148 of an ion are determined. See Krimigis et al. (2004) for a more detailed description of the 149 CHEMS instrument. The entire Cassini/MIMI/CHEMS data set and Cassini ephemeris data are 150 publicly available in the Planetary Data System and can be found at http://pds.nasa.gov.

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152 Method of Data Analysis

153 [8] We combine the CHEMS data from 78 of the 82 equatorial ring current passes (L = 7-16; Latitude = -10° to 10°) used earlier by Difabio et al. (2011) to study long term variations of the 154 155 major suprathermal ions at Saturn. We focus our efforts on the main ring current where the 156 highest, most important suprathermal ion fluxes are present (Sergis et al., 2009) in order to separate W^+ into four components: O^+ , OH^+ , H_2O^+ , and H_3O^+ . We focus on the ~96 keV/e E/Q 157 channel of telescope 1 data where all four W⁺ components are best resolved. Suprathermal ions 158 159 at Saturn, at the energies considered here, do not rigidly corotate with Saturn outside of \sim 5-6 R_s 160 (Richardson et al., 1998; Kane et al., 2008), and the observed corotation speeds inside $\sim 6 R_S$ are 161 < ~50 km/s, small compared to the suprathermal ion speeds. Convection speeds, as estimated in 162 the above studies, are up to \sim 50-100 km/s lower than rigid corotation speeds in the equatorial 163 ring current out to 15-18 R_s, so only using telescope 1 does not affect our results significantly.

We only use the CHEMS data that includes an energy measurement from the SSD because of itslower background.

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167 [9] A plot of the SSD energy channel, Essd channel, versus the time-of-flight channel, TOF 168 channel, for all 78 ring current passes combined is shown in Figure 1a. Separating the W⁺ 169 components was found to be easier using the raw channel values. (DiFabio, 2012), so we do not 170 convert Essd channel and TOF channel to Mass (amu) and M/Q (amu/e). We make an Essd 171 channel cut selecting the data between the horizontal red dashed lines shown in Figure 1a and 172 create a TOF channel histogram of the data (see Figure 1b). All four major components of the W^+ group can be identified, although the H_3O^+ appears as a shoulder. These data are from 173 174 CHEMS telescope 1 which has the best heavy ion resolution after signal to noise ratio (DiFabio, 175 2012). We fit these peaks to estimate the abundances of these four species.

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[10] We use the ~96 keV O^{++} (E/Q ~ 48 keV/e) TOF distribution from a different energy step 177 178 (see Vandegriff et al., 2018) as a guide to choosing appropriate fitting parameters for the W^+ species, which overlap. The pre-launch calibration data for ~96 keV O^+ and H_2O^+ are not used 179 180 because the calibration data distributions tend to be narrower than those in the in flight data due to the mono-energetic and unidirectional nature of the calibration beam. Since the O⁺⁺ ions at 181 E/Q = -48 keV/e have the same energy as -96 keV O^+ , the -48 keV/e O^{++} TOF distribution is 182 nearly identical to that of ~96 keV O^+ . We can easily fit the ~96 keV O^{++} since there is no 183 184 overlap from other ion species and use the result in fitting the O^+ .

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186 [11] A TOF histogram of the ~96 keV O^{++} distribution for all 78 equatorial ring current passes is 187 shown in Figure 2. The ~96 keV O^{++} distribution is asymmetric, so a simple Gaussian, such as

188 that used to obtain our preliminary CHEMS data analysis results reported in Mauk et al. (2009), 189 is not the best fitting function. An asymmetric Gaussian fits the central peak of the distribution, 190 where its centroid (the peak's center of symmetry) is at the TOF channel τ_c , which we call the 191 peak's "center". At TOF channels higher than the centroid, the counts decline more slowly than 192 expected for a Gaussian distribution as a result of straggling in the carbon foil (Northcliffe & 193 Schilling, 1970; Gloeckler & Hsieh, 1970), so we must add a small additional term to the 194 Gaussian on the right side of the peak. We refer to this higher-TOF section as the "tail". The 195 functional form we use to fit the count distribution in TOF channel, τ , is

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$$f(\tau) = A \left[e^{-\frac{(\tau - \tau_c)^2}{2\sigma_1^2}} P(-\tau + \tau_c) + \left(e^{-\frac{(\tau - \tau_c)^2}{2\sigma_2^2}} + \frac{(\tau - \tau_c)^2}{100 + [(\tau - \tau_c)^2]} \right) P(\tau - \tau_c) \right]$$
(1)

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This function maximizes at the centroid $\tau = \tau_c$ with an amplitude A. The sigmoid function $P(x) = 1/(1+e^{-x})$ is an approximation to the Heaviside function which is ~0 for x < 0 and ~1 for x > 0. The parameters σ_1 and σ_2 are the Gaussian standard deviations, which we call the "widths", for the $\tau < \tau_c$ and $\tau \ge \tau_c$ sides of the distribution, respectively. The parameter α controls the rate of decline in the tail, in that the function declines as ~ $((\tau-\tau_c)^2)^{(1-\alpha)}$ for $\tau >> \tau_c$.

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[12] Gaussian fits performed by von Steiger et al. (2000) on ion species distributions from the Ulysses Solar Wind Composition Spectrometer, a functionally similar type of instrument, showed (in their Plate A2) that the width to center ratios of the TOF distributions vary slowly, so that differences between species spaced closely in TOF channel, such as O⁺ and H₃O⁺, vary by $\leq 3-4\%$ percent. Therefore, we use the σ_1/τ_c and σ_2/τ_c ratios as fitting parameters rather than σ_1

- and σ_2 . The form of our fitting function is similar to the kappa distribution used by Allegrini et al. (2006) to fit the energy distribution of 1-50 keV ions traveling through thin, carbon foils.
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[13] Using the Levenberg-Marquardt fitting procedure (Press et al., 1989), we use the function given in Equation 1 to fit the ~96 keV O⁺⁺. The best fit (reduced $\chi^2 = 0.73$) is obtained with $\alpha =$ 1.81 and is shown in Figure 2. Then, when fitting the ~96 keV O⁺ distribution, we set its σ_1/τ_c ratio equal to that of the σ_1/τ_c ratio from the ~96 keV O⁺⁺ fit. Because the widths of the molecular ion distributions are not necessarily identical to those of atomic ions, we let the σ_1/τ_c and σ_2/τ_c ratios of OH⁺, H₂O⁺, and H₃O⁺ differ from that of O⁺, but force them to be identical for these molecules, because they are dominated by their heaviest atom, O.

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[14] Although the CHEMS pre-launch calibration data show that the W⁺ tail counts grow with 222 223 increasing M/Q, we were unable to determine how much the α parameter would vary among the 224 four species from the in-flight data. Thus, we assumed that the α parameter is same for all four species. This assumption increases the uncertainty in our estimates of the ion abundances, 225 particularly that of H_3O^+ . In order to determine the sensitivity of our results to the form of the 226 fitting function, we performed three different types of fits on the W⁺ distribution with these 227 228 conditions on α : type 1: asymmetric Gaussian ($\alpha = \infty$), type 2: requiring α to equal the value from the O^{++} fit ($\alpha = 1.81$), and, type 3: allowing α to vary. (We include this discussion 229 230 although, in the results of our analysis, variations of the distributions' tails tended to be of minor importance.) For the first two types, we require the σ_2/τ_c value for O⁺ to equal the results from 231 the $O^{^{++}}$ fits. Since the value of the α parameter affects the value of $\sigma_2,$ we let the O^+ σ_2/τ_c and α 232 233 vary for the third fit. The centers τ_c for all four species and the σ_1/τ_c ratio for the molecular ions

are only allowed to vary in the asymmetric Gaussian fit (type 1). In the type 2 and 3 fits, the centers and molecular ion σ_1/τ_c ratio are forced to equal the values from the type 1 fit. We let the amplitudes A and σ_2/τ_c ratio of the molecular ions vary for all three types of fits.

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[15] Figure 3 shows our best fit (reduced $\chi^2 = 4.0$) of the entire W⁺ distribution, which is found using the type 3 fit and with α =1.90. Numerically integrating each peak from the type 3 fit provides our best estimate of the O⁺, OH⁺, H₂O⁺, and H₃O⁺ counts. We then convert the counts into partial number density and calculate the fractional abundance relative to W⁺. As discussed in the next section, the type 1 and 2 fits are used to determine the upper and lower limits of the H₃O⁺ abundance.

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[16] After obtaining the fits in the main ring current (L = 7-16; Latitude = -10° to 10°), we divide the Cassini passes by L shell and look for variations with L in the L = 7-21 range. When fitting the data by L shell, the statistics are worse, and we only let the amplitudes of the peaks vary, forcing the center τ_c , σ_1 , σ_2 , and α of each species peak to be the same as the results from the L = 7-16 fit. We use a $\Delta L = 1$ for L = 7 to 11 where there are sufficient counts, but we must combine L shells beyond this distance where the counting statistics decline, using $\Delta L = 2$ for L = 11 to 15, and $\Delta L = 3$ for L = 15 to 21.

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253 Results and Discussion

[17] <u>Results and comparison with earlier studies</u>. Table 1 lists the counts from the best fit to the W⁺ distribution plotted in Figure 3 (i.e., the type 3 fit with $\alpha = 1.90$) along with the partial number densities and the relative abundances of the ~96 keV W⁺. The W⁺ group has an average mass of 16.7 amu and consists of ~53% O⁺, ~22% OH⁺, ~22% H₂O⁺, and ~3% H₃O⁺. Since the 258 number of counts in the distribution tails contain only a small percentage of the total counts, our estimates of the O^+ , OH^+ , and H_2O^+ abundances do not vary significantly among the three types 259 260 of fits. The quoted uncertainties for these three species reflect the statistical uncertainties from our type 3 fits. Because H_3O^+ is much less abundant and the tails from the other three species 261 make up a significant fraction of the counts at the location of the H_3O^+ peak, our estimate of the 262 H_3O^+ counts strongly depends on the α parameter. This can possibly introduce a larger 263 systematic error and the quoted H₃O⁺ uncertainties reflect the range of values from our three 264 265 different fits. The asymmetric Gaussian fit with no tail provides an upper limit on the H_3O^+ 266 abundance, while forcing $\alpha = 1.81$, which overestimates the tail counts, provides a lower limit 267 on the H_3O^+ abundance.

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[18] The partial number densities and fractional abundances of the four \sim 96 keV W⁺ components 269 are plotted versus L in Figures 4a and 4b, respectively. Figure 4a shows that all four W⁺ 270 271 components increase similarly at L ~ 8-10, peak at L ~ 9.5, and decrease at L < ~9, but not quite similarly. Figure 4b shows that (a) fractional O^+ , OH^+ , and H_2O^+ vary little from L = 5-21, with 272 each species' variations being statistically insignificant, (b) fractional H_3O^+ is approximately 273 constant at L > ~13, and (c) the enhancement of fractional H_3O^+ probably starts at L ~ 13, but 274 275 certainly only increases monotonically inside of L \sim 11, increasing by almost a factor of \sim 3 above fractional H_3O^+ levels at L > ~13. Paranicas et al. (2008) noted that ~5-100 keV H⁺ and O⁺ 276 277 (products of the magnetospheric processes CRAND and , respectively) populate Saturn's inner 278 magnetosphere episodically, being energized by injections, and concluded that they are then 279 primarily lost to charge exchange in the Enceladus torus as they drift inward. We agree that this interpretation is consistent with our W⁺ radial variations in Figure 4a. The W⁺ components may 280 281 originate from any object in Saturn's magnetosphere before their dispersal and subsequent

282 inward transport from $L \sim 15-20$, but most are currently presumed to originate in Saturn's main 283 rings and the Enceladus neutral torus. On their way inward, the ions' partial number density at a 284 given energy increases, peaking at $L \sim 8-10$, inward of which losses increase as they encounter 285 the neutral torus. Paranicas et al. (2008) demonstrated that energetic/suprathermal O^+ flux 286 decreases persistently in to $L \sim 5.5-6.5$ (depending on magnetospheric conditions), where it then 287 becomes undetectable (see Figure S3 in the Supporting Information). They note that "...The 288 shape of the flux drop off inward to the planet has different behavior on each orbit we have surveyed and is not related to the locations of the moons." They argued that the W⁺ components 289 290 are transformed by the neutral gas cloud in this region which converts the inward drifting ions to 291 energetic neutral atoms via charge exchange. Kollmann et al. (2011) show that ~46 keV H⁺ and ~91 keV e⁻ display differential intensity peaks at ~9 < L < ~10.5 and L ~ 8, respectively (see 292 293 Figure S4 in the Supporting Information), similar to the energetic protons and oxygen in 294 Paranicas et al., with fluxes decreasing in to $L \sim 5-6$. Christon et al. (2014) show that 83-167 keV W⁺, a portion of its straggling tail W⁺_{tail} at ~22–26 amu/e, O_2^+ , and $^{28}M^+$ all display peaks at L ~ 295 9 and decreases in to L ~ 6 (see Figure S5 in the Supporting Information). The fractional W_{tail}^+ 296 varies little outside of L ~ 7, similar to this study's fractional O^+ , OH^+ , and H_2O^+ , and like the 297 fractional H_3O^+ component, the fractional O_2^+ and $^{28}M^+$ abundances vary insignificantly at $L \ge$ 298 299 13, but vary inside L ~ 13. However, rather than increasing as fractional H_3O^+ does, fractional O_2^+ and ${}^{28}M^+$ levels decrease markedly inside L ~ 13, much further than the fractional H₃O⁺. 300 301 Note though, in this study, while the variation is not statistically significant, fractional H_3O^+ is 302 disrupted with respect to its behavior beyond L \sim 15 and starts increasing inside L = 13. 303 Interestingly, the magnetic pressure of Saturn's inner, "core", dipolar magnetic field is rather 304 well ordered out to ~ 10 Rs, with disturbed ordering persisting somewhat out to ~ 13 Rs, beyond 305 which low level disturbed magnetic pressure extends to larger radial distances (Sergis et al.,

306 2010), suggesting that the L < 10 region may be characteristically differentiated from the L > 13 307 magnetosphere. It is apparent that the H_3O^+ is not depleted as much as the other three W⁺ 308 components inside of L ~ 10, suggesting some as yet unidentified, differentiated interaction(s) 309 possibly resulting from this magnetospheric magnetic field transition near L ~ 10 occur near the 310 neutral torus for these ions.

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[19] The energetic O^+ , OH^+ , and H_2O^+ fractional abundances in Figure 4b show no significant 312 313 variation with L from 7 to 21; they do not deviate far from their average values throughout the 314 main ring current. The dashed box encompasses the entire radial and abundance range of the four 315 thermal ion fractional abundances from Wilson et al. (2012). Suffice it to say, most of the 316 thermal ion radial variation is evident at L < 8. Clear depiction of both data sets, not necessary 317 here, is presented in Figure S2 in the Supporting Information. We expect few, if any, correlated variations or processes between the energetic and thermal-W⁺-components as the thermal W⁺ 318 319 components propagate outward from their inner magnetospheric source region, and the suprathermal W⁺ components diffuse inward from their outer magnetospheric acceleration 320 region(s). The suprathermal W^+ components have much wider variation than the thermal 321 components, with O^+ being somewhat more abundant and H_3O^+ being much less abundant than 322 323 either OH^+ or H_2O^+ .

324

325 [20] The suprathermal H_3O^+ fractional abundance has an average value of ~0.017 at 13 < L < 21 326 and shows no measurable radial dependence. However, at L < 10, the H_3O^+ partial density peak 327 and relative decrease are not as substantial as that of the other W⁺ components, resulting in its 328 fractional abundance increasing to $H_3O^+/W^+ \sim 0.048$ - apparently due to a weaker interaction with 329 the nearer-Saturn environment. One possible cause of this more moderate decrease of H_3O^+ at

lower L might be that the H_3O^+ charge exchange lifetime is longer than those of O^+ , OH^+ , and 330 H_2O^+ , or, alternatively, that H_3O^+ interactions with the negatively charged E-ring grains inside 331 the orbit of Rhea (~8.74 Rs) are weaker than those of O^+ , OH^+ , or H_2O^+ . The fractional 332 333 abundances of suprathermal ions with longer charge exchange lifetimes (smaller cross sections), such as possibly H_3O^+ , would be expected to increase with respect to other ions whose cross 334 335 sections are larger, as losses become more important going inward. Unfortunately, although 336 cross sections for 10's of eV-energy W⁺ ions are available (e.g., Lishawa et al., 1990), to our 337 knowledge, the cross sections for ~10-500 keV water group ions colliding with Saturn's most 338 important thermal neutral cloud atoms and molecules (O, OH, and H₂O) are not all available in 339 the literature. As a result, we can only offer qualitative analysis of the W^+ component charge 340 exchange lifetimes below using available lower energy charge exchange cross sections as a 341 guide. An alternative, independent, and concurrent process contributing to the difference of the H_3O^+ radial dependence might result from varying strengths of interactions between H_3O^+ and 342 the other W⁺ components with the charged E-ring grains. E-ring grains are observed to vary in 343 344 size, from several nanometers up to tens of micrometers and have radially varying charged 345 components, in which negatively charged grains dominate inside the orbit of Rhea, transitioning 346 to both positive and negative within an Rs or so around the orbit of Rhea, and then become 347 preponderantly positive with increasing distance from Saturn outside the orbit of Rhea, as 348 reported, for example, by Wahlund et al. (2005), Sittler et al. (2006), Kempf et al. (2008), Hsu et 349 al. (2013), and Ye et al. (2017). We address both possible scenarios below.

350

351 [21] In Figure 4b we compare our fractional W^+ abundance results at ~96 keV to the range of the 352 preliminary results for the thermal plasma fractional abundances reported by Wilson et al. (2015) 353 in their Figure 3. Both studies analyze near-equatorial data, with a radial overlap at L = 7-10; that

354 is, this study uses L = 7-21 and Wilson et al. (2015) used $R_s = 4.75-10$. Considering the small 7 355 $\leq L \leq 10$ overlap region, the fractional abundance values are somewhat comparable, although the 356 range of fractional suprathermal ion abundances is much greater than that of the thermal ions. 357 Ratio ranges from the two studies and model results from Figures 3 in Fleshman et al. (2013) and 358 Wilson et al. (2015) are listed in Table 2. To date, we are unaware of any models characterizing 359 the energetic/suprathermal water products' distribution, propagation, and/or interactions in Saturn's magnetosphere. The observed OH^+ and H_2O^+ fractional abundances are roughly 360 361 comparable in the two energy ranges, although the thermal population values are somewhat larger. Major differences between the thermal and energetic population O^+ and H_3O^+ fractional 362 abundances are evident: the O⁺ fractional abundance is much larger for the suprathermal ions and 363 the H_3O^+ fractional abundance is much smaller for the suprathermal ions. The thermal ion 364 365 fractional abundances are all between ~ 0.18 and ~ 0.30 , which is about twice the range of the H_2O^+ and OH^+ suprathermal uncertainties. Understanding that acceleration to suprathermal 366 energies is not instantaneous, one might expect for extensive dissociation of the W⁺ molecular 367 species to occur, producing relatively more atomic O⁺. In summation, the suprathermal fractional 368 abundances show little radial variation except for the H_3O^+ increase by a factor of ~3 from L ~ 369 13 to L ~ 7. Of note, the thermal H_3O^+ fractional abundance also shows a large increase with 370 371 decreasing L. However, at thermal energies, the fractional abundances of the other species also 372 show radial variations over the L = 7-10 range with the O^+ and OH^+ increasing and the H₂O⁺ 373 decreasing with increasing L.

374

375 [22] <u>Origin of the suprathermal ions</u>. The majority of Saturn's water group ions are produced by 376 the dissociation and ionization of the neutral H_2O emitted from the Enceladus plumes (Burger et 377 al., 2007; Smith et al., 2010; Cassidy & Johnson, 2010). Since the ions observed here are much 378 more energetic than the thermal ions, we must consider the acceleration and transport processes 379 when comparing our results to the thermal ion observations and neutral cloud models. The most 380 likely acceleration processes are injections (Mauk et al., 2005; Hill et al., 2005; Burch et al., 381 2005; Paranicas et al., 2007; Rymer et al., 2009) and inward radial diffusion (Van Allen et al., 382 1980; Armstrong et al., 1983) conserving the first and second adiabatic invariants. Injection 383 events are a result of the centrifugal interchange instability where narrow "fingers" of hot plasma 384 are injected inward and replace broad, outward flowing cold plasma. Injection events can be 385 grouped into two categories: low energy and high energy (Mitchell, Carbary, et al., 2009). Low 386 energy events originate at L = 9-11 (Rymer et al., 2009), while high energy events originate in 387 the magnetotail (Mitchell, Krimigis, et al., 2009). Acceleration by inward radial diffusion also 388 requires the thermal ions to start in the outer magnetosphere, so the accelerated ions studied here 389 likely reflect the plasma ion composition in the outer magnetosphere, a region not addressed by 390 Wilson et al. (2015).

391

392 [23] The composition of the thermal ions in the outer magnetosphere depends on a number of 393 factors. One is the ionization rate of the neutral particles in the outer magnetosphere. Although 394 possible differences among the neutral species' ionization and dissociation rates prevent us from 395 directly comparing the ion composition to the neutral densities, our results do provide 396 constraints. If a large percentage of the thermal ions in the outer magnetosphere is produced by 397 the ionization of neutrals in this region, then the suprathermal ion composition will closely 398 reflect the neutral particles that were initially ionized in the outer magnetosphere.

399

400 [24] Because the ionization rates are much higher in the inner magnetosphere, we must consider401 the possibility that thermal ions produced in the inner magnetosphere are then transported to the

402 outer magnetosphere where they are accelerated. As discussed above, broad outward flows of 403 cold plasma are consistent with the properties of the centrifugal interchange instability (Hill et 404 al., 2005; Rymer et al., 2008). Electron and ion observations suggest that this outward transport 405 process is not adiabatic and does not cool the plasma (Rymer et al., 2007, 2008; Wilson et al., 406 2008). Therefore, the outward transport of thermal ions followed by acceleration in the outer 407 magnetosphere can produce ions at suprathermal energies. Observations by Cassini UVIS (Melin 408 et al., 2009) and models of the neutral cloud (Smith et al., 2010; Cassidy & Johnson 2010) 409 indicate that the neutral O cloud is much broader than the neutral OH and H₂O clouds. Outside of 410 6 R_s, the neutral O density is larger than that of OH and H₂O, and the neutral O density is about 411 an order of magnitude greater than the other water group neutrals near $\sim 20 R_S$ (Cassidy & Johnson, 2010), whereas, near the orbit of Rhea, $\sim 8.75 \text{ R}_{\text{S}}$, the neutral O to OH (and, likely H₂O) 412 413 density ratio is modeled to be from ~2 to ~3.5 (by Smith et al., 2010 and Cassidy & Johnson, 414 2010, respectively). Since the ionization rates of the neutral particles throughout the 415 magnetosphere are estimated to be approximately the same (Cassidy & Johnson, 2010), we 416 would have expected the suprathermal O^+/OH^+ and O^+/H_2O^+ ratios to be larger than our observed 417 value of ~2.4, because their presumed source is closer to ~20 R_S than ~8.75 R_S .

418

419 [25] It is possible that a large percentage of the ions in the outer magnetosphere is produced 420 inside of 10 R_s , where the difference between densities of neutral O and of neutral molecules is 421 not as large, as noted above, and the ions are then transported to the outer magnetosphere. 422 However, Wilson et al. (2015) find that O⁺ is generally the least abundant water-group ion at 423 thermal energies, not the most abundant water-group ion, as at suprathermal energies. Wilson et 424 al. (2015) reported that the mean mass of thermal water group ions has a mean of 17.56 amu in 425 the radial region of 4.75 to 10 R_s , and decreases with distance from Saturn. On the other hand,

426 the mean mass of suprathermal ions, 16.7 amu, reflects the large percentage of suprathermal energy O^+ , ~2.5 times greater than OH^+ or H_2O^+ throughout $7 \le L \le 16$. Because of the larger 427 428 fractional abundance of molecular ions inside of 10 R_s, the outward transport of these ions would result in a lower O^+/W^+ ratio relative to the neutral O/W ratio. To perform quantitative analysis, 429 430 better constraints on the ion transport rates, production rates, and loss rates are needed. However, our observation that W^+ consists mostly of O^+ is qualitatively consistent with the broad atomic O 431 432 cloud observed by Cassini UVIS (Melin et al., 2009) and predicted by some models (Smith et al., 433 2010; Cassidy & Johnson, 2010; Dialynas et al., 2013). Our observation of nearly equal amounts of suprathermal OH⁺ and H₂O⁺ suggests that neutral H₂O is spread to Saturn's middle or outer 434 magnetosphere rather than confined to a narrow (~2-3 R_s) torus centered on Enceladus' orbit. 435 436 This result supports the conclusions of the Cassidy & Johnson (2010) model, which predicts 437 approximately equal neutral OH and H₂O densities spread outside of 7 R_S. If neutral H₂O were 438 confined to a narrow torus near 4 R_s as suggested by other models (e.g. Johnson et al., 2006; Smith et al., 2010), we would expect very low abundances of suprathermal H_2O^+ compared to O^+ 439 440 and OH^+ .

441

[26] Our results do not rule out the possibility that most of the H_2O^+ is produced near Enceladus' 442 443 orbit and then transported to the outer magnetosphere where it is then accelerated. However, this scenario seems unlikely, because we would expect the suprathermal H_2O^+ fractional abundance 444 to be similar to that of the suprathermal H_3O^+ . Thermal H_3O^+ is the most abundant ion species in 445 446 the Enceladus torus where the majority of it is produced via charge exchange reactions (Sittler et 447 al., 2008; Cravens et al., 2009; Fleshman et al., 2010a). As the H_3O^+ is transported outward, its 448 fractional abundance drops significantly due to its short recombination lifetime in the Enceladus torus (Ip, 2000; Sittler et al., 2008). Because the recombination lifetime of H₂O⁺ is even shorter 449

450 than the H_3O^+ lifetime in the Enceladus torus (Fleshman et al., 2010b), we would expect a 451 similar decrease in the thermal H_2O^+ fractional abundance. Therefore, the production of H_2O^+ in 452 the inner magnetosphere followed by outward transport and acceleration in the outer 453 magnetosphere would probably not result in our observed suprathermal H_2O^+/H_3O^+ ratio of ~7.8. 454 A more detailed model is necessary before this possibility can be conclusively ruled out.

455

456 [27] L dependence at L < -9. We now qualitatively discuss the processes that might cause the 457 large losses of suprathermal ions inside of $L \sim 9$. This is a qualitative discussion because, to our 458 knowledge, relevant functional forms and/or laboratory measurements for the water group 459 suprathermal ions of interest relevant to their interactions with the thermal ions and neutral 460 particles present in the E-ring (or Enceladus torus) and discussed herein do not exist or are not 461 available in the literature. In this discussion, we will also present some measurements at low 462 center of mass, CM, collision speeds because, they are all that exists. Charge exchange and 463 proton-transfer cross sections likely vary among the species studied herein and are probably 464 responsible for most of the observed changes/differences in the relative abundances of the W⁺ constituents. For W^+ constituents, fractional differences appear to be seen only for H_3O^+ , but 465 note that important differences with respect to W⁺ exist for heavier important molecules at 466 467 Saturn (see Figure S5 in the supporting information).

468

469 [28] <u>Charge exchange with neutral gas</u>. Consider the charge exchange reaction involving an ion 470 A⁺ colliding with the neutral B (A⁺ + B \rightarrow A + B⁺ + Δ E), where Δ E is the difference between the 471 ionization energies of A and B. For resonant processes (i.e. Δ E = 0), the charge exchange cross 472 section decreases with energy and behaves like $\sigma = (C-D*\ln(v))^2$, where C and D are constants 473 and *v* is the relative velocity (Dalgarno, 1958). At low velocities, cross-sections of non-resonant 474 collisions are smaller than those of resonant collisions and increase with increasing velocity 475 (Rapp and Francis, 1962). Non-resonant cross sections maximize at a velocity, v_{max} , that can be 476 approximated by the Massey adiabatic hypothesis (Massey, 1949):

477
$$\boldsymbol{v}_{\max} = \frac{\boldsymbol{v}_{o} \left| \Delta \boldsymbol{E} \right|}{h}$$
(2)

478 where $v_0 = 7x10^{-8}$ cm and *h* is Planck's constant. Above this maximum velocity, the non-479 resonant cross section converges with the cross section of the resonant collision. The collision 480 cross section maximizes at higher velocities as the difference in ionization energies increase.

481

482 [29] Although the above relation is only meant for slower collisions, in the absence of related laboratory results and in order to get a sense of any differences that may exist between H_3O^+ and 483 the other W⁺ components, we apply Equation 2 to collisions of the water group ions with atomic 484 485 O, which is ~6 times more plentiful than OH at ~10 R_s as shown by Melin et al. (2009). The 486 ionization energies of O, OH, and H₂O are 13.6 eV, 13.0 eV, and 12.6 eV (Weast, 1968; 487 Wiedmann et al., 1992), respectively, while the ionization energy of H_3O is much less at 5.5 eV (Melin et al., 2005). Using these ionization energies, the collision cross sections of OH⁺ on O 488 and H_2O^+ on O are estimated to peak at $v_{max} \sim 1-2x10^7$ cm/s, while the H_3O^+ on O cross section 489 is estimated to peak near at $v_{\text{max}} \sim 1.4 \times 10^8$ cm/s, an order of magnitude larger. Because the 490 velocities of ~96 keV OH^+ and H_2O^+ are much greater than the velocity at which the cross 491 492 section maximizes, we might expect the charge exchange cross sections of these species to be approximately the same. The cross section of ~96 keV H_3O^+ , however, will not have reached its 493 494 maximum value and will be less than the cross sections of the other three ion species. Therefore, 495 ~96 keV H_3O^+ will have a longer lifetime than the other ~96 keV water group ion species. As a result, the fractional abundance of H_3O^+ should be expected to increase inward, while the 496 fractional abundance of O^+ , OH^+ , and H_2O^+ would not show significant variations. The result of 497

this argument is qualitatively consistent with and provides a reasonable framework for understanding why suprathermal H_3O^+/W^+ increases with decreasing L, and has a very different explanation than that for thermal H_3O^+/W^+ increasing with decreasing L. Hopefully, in future analysis related to these particles in this process, the charge exchange cross sections of these energetic ions will be more fully documented and other reactions, such as dissociation and interactions with charged dust should also be included and modeled for these suprathermal ions in Saturn's magnetosphere.

505

506 [30] Grain interactions. Grains and dust permeate Saturns magnetosphere, as demonstrated in 507 Figure 5, where we show three distributions of 0.1-3.0 μ grains that Hornáyi et al. (2008) 508 modeled from a continuous scan of grain densities derived from data measured during Cassini's 509 ring-plane crossing on Orbit 7. Their study provides one of the few snapshots of the 510 magnetosphere's grain population. Three different size ranges demonstrate the spatial distribution of grains relative to our overlaid W⁺ measurements in the upper panels. A large measurable 511 512 portion of E-ring grains have either positive or negative charge (e.g., Kempf et al., 2006; Ye et 513 al., 2014). Kempf et al. (2006) found that grains bigger than 2–3 µm detected inside Rhea's orbit $(L \sim 8.75)$ were always negatively charged, whereas grains outside Rhea's orbit were all 514 515 positively charge. Dong et al. (2015) determined that the size distribution of nanometer-sized 516 grains obtained by CAPS (~0.001 µm, herein called dust) suggests that ~1-10 nm sized grains 517 dominate both charge density and number density, at least near Enceladus. Little information is 518 available on total grain population characteristics (from nanometer to micrometer sizes) and their 519 properties throughout Saturn's magnetosphere, except near Enceladus' orbit. Nevertheless, we 520 estimate below whether ion interactions with Saturn's charged grain/dust environment should be 521 considered in addition to Saturn's neutral gas populations, even when exclusion of the grains

might provide acceptable explanations of phenomena in Saturn's magnetosphere without such consideration. The grain interactions we consider here are a possible alternative reason for the difference between the radial profiles of H_3O^+ and the other W^+ components.

525

526 [31] The water-group ions should be attracted to any negatively charged particles, grains or ions, 527 in the dusty plasma through electrostatic attraction, and repulsed by positively charged particles. The W⁺ components' electric dipole moments (∂) for OH⁺, H₂O⁺, and H₃O⁺ have different 528 529 values: 2.32, 2.40, and 1.44 D (debye), respectively (see e.g., González-Alfonso et al., 1983; 530 Vogelius et al., 2004; and Botschwina et al., 1983). For comparison, neutral molecules can have an induced electric dipole moment, two are (up to) $\partial_{OH} = 1.65$ D for OH, Werner et al., 1985, and 531 $\partial_{\rm H2O} = 1.85$ D for H₂O, Dyke & Muenter, 1973), so the H₃O⁺ dipole moment is ~40% smaller 532 than those of OH^+ and H_2O^+ and comparable to induced neutral molecule dipole moments. Given 533 that, H₃O⁺ will be less attracted to the prevalent negatively charged E-ring grains near and inside 534 of Rhea's orbit than the other W^+ components. H_3O^+ would therefore have a longer mean free 535 536 path in the E-ring planetward of Rhea, if not for some distance outside of $L \sim 9$. Some portion of the negatively charged E-ring grains will capture W^+ components, more likely the O^+ , OH^+ , and 537 H_2O^+ than the H_3O^+ . This weakness of the H_3O^+ dipole moment is a possible, as yet unexplored, 538 539 interaction difference with the E-ring material, in addition to the aforementioned possible cross section difference between H_3O^+ and the other W^+ components. The difference in dipole 540 541 moments would result in fewer collisions with and less attraction between charged grains and 542 H_3O^+ than with the other W^+ components.

544 [32] E-ring grain measurements in two different size ranges by Cassini instruments were: (a) ≥ 9 545 µm by design, Cosmic Dust Analyzer, CDA (Srama et al., 2004; 2011; Kempf et al., 2008; and

546 >0.5 by impact identification algorithm, Kempf et al., 2004); (b) \sim 2-10 µm from spacecraft 547 charging, Radio Wave and Plasma Wave Science (RPWS) investigation (Gurnett et al., 2004; Ye 548 et al., 2014; 2016); and (c) ~0.6-3 nm by CAPS, from large energy-per-charge measurements 549 (e.g., Hill et al., 2012; Dong et al., 2015). Only CDA was designed to measure the grains and 550 dust, but the measurements have been compared and appear to be complementary (Meier et al., 551 2014; Dong et al., 2015). Complementary overlays of data from Kempf et al. (2006) and Ye et al. 552 (2014) in the bottom panel of Figure 5 show that grains >0.5 microns detected inside Rhea's 553 orbit, ~8.75 Rs, are mostly negatively charged and grains outside Rhea's orbit were positively 554 charged, with the typical potentials being about -2 V and +3 V, respectively (Figure 1 of Kempf 555 et al., 2006). However, the Ye et al. (2014) data clearly show that some negatively charged 556 grains persist beyond Rhea's orbit. Dust, detected in and near the Enceladus plume with both 557 negative and positive net charges (Hill et al., 2012), likely follows a similar, but more likely 558 complex large scale pattern, than the grains (e.g., Engelhardt et al., 2015), but, to our knowledge, 559 this has not yet been fully investigated. In the Appendix, we estimate the ratio of mean free paths 560 for H_2O^+ near the orbits Enceladus and Rhea (a) in O and OH gas from the models of Cassidy 561 and Johnson (2010), and (b) in 1 and 2 nm dust at expected densities there, using dust (CAPS) 562 and grain (CDA and RPWS) measurements at Enceladus' orbit and values at Rhea's orbit, using 563 CDA's measured radial grain variation and complementary CDA and RPWS data near Rhea's 564 orbit combined with extrapolated dust estimates assuming the same radial variation as grains. The range of estimates for the ratios of H_2O^+ mean free paths in neutral O and OH gas to H_2O^+ 565 566 mean free paths in uncharged grains and dust are neither orders of magnitude apart nor widely 567 divergent from unity, ≈ 1 , where the mean free path estimates are equal; the estimates range 568 instead from ratios of ~ 2 to ~ 0.2 , for dust sizes at 1 and 2 nm, respectively, values slightly below 569 and slightly above those characteristic of the most likely nanograin size (Dong et al., 2015).

570 Therefore, depending on the true gas and grain densities and grain sizes in the E-ring near the 571 orbit of Rhea, in addition to charge exchange interactions, consideration of ion-grain/dust 572 interactions through focused modeling, might be necessary in order to fully understand the radial 573 variations of suprathermal W⁺ component partial densities.

574

575 Concluding Remarks

576 [33] The fractional abundances of suprathermal OH^+ and H_2O^+ are comparable and both consistently near ≈ 0.2 for 7 < L < 21, compared to (a) thermal OH⁺ clearly increasing from ~ 0.23 577 to ~0.3 and and (b) thermal H_2O^+ decreasing somewhat from ~0.31 to ~0.26 from 5 to 10 R_s. 578 579 Over $7 \le L \le 21$, the fractional abundance of suprathermal O⁺ is much larger than the other W⁺ components and the fractional abundance of suprathermal H_3O^+ is much smaller than the other 580 W^+ components. Suprathermal O^+ (H₃O⁺) fractional abundance is larger (much smaller) than 581 thermal O^+ (H₃ O^+) fractional abundance in the ~7-10 R_s radial range. The suprathermal O^+ , OH^+ , 582 and H_2O^+ fractional abundances show no significant variation with L over the range L = 7-21. 583 584 The suprathermal H_3O^+ fractional abundance, with an average value of 0.017, shows no dependence on L at L = 13-21. Inside of L = 13, however, the suprathermal H_3O^+ fractional 585 586 abundance increases substantially to 0.048 at L = 7-8, a factor of 2.8. The radial variations of 587 suprathermal W^+ components are distinctly different from available thermal energy W^+ components radial variations. A full examination of the interesting H_3O^+ variation inside L ~ 9 is 588 589 hampered by both the lack of charge exchange cross sections for suprathermal water-group ions 590 thermal O and H₂O the lack of more comprehensive information. on and

- 591 Appendix 1. Scattering of a water ion in the near-Rhea E-ring
- 592 In simple grazing, elastic collisions, the mean free path of an ion traveling in a neutral gas (or

593 grain field) of interaction distances d is determined, in part, by the ratio of the distance traveled

594 (vt) to the product of the interaction volume ($\Box d^2 vt$) times the number of target particles per unit

595 volume (Nt).

596 We assume that:

- 597 (a) H_2O^+ is the representative ion for the water group;
- 598 (b) O or OH are the most likely neutral gas targets (Cassidy & Johnson, 2010) with ion radius,

599 r_N , and density N_N ;

- 600 (c) The incoming ion (I) and a target (T) neutral particle will interact if they touch, that is, if the
- 601 distance between their centers is $d \le (r_I + r_T)$. The interaction area, or cross section, is $\pi (r_I + r_T)^2$;

and (d) In estimating the varying scenarios, the grain population is characterized by their

603 minimum grain radius, r_G , with $r_G >> r_N$, and density N_G .

A general form of the MFP, given in Chemistry LibreTexts. 4.12: The Frequency of Collisions
between Unlike Gas Molecules (https://chem.libretexts.org, 2019), is:

- vt / $(\pi(r_I + r_T)^2 \text{ vt } N_T)$, where, 606 MFP = speed of the ion through the medium, 607 v = time for the ion to travel the distance vt, 608 t = 609 the radius of the ion, rI = 610 the radius of the target population's particles, r_T , which, for the r_T = 611 neutral gas are $r_{N,O}$, for O atoms, or $r_{N,H2O}$, for H₂O molecules, the 612 populous E-ring neutrals (see the reference list below), and the second most 613 case, E- ring grains, characterized above, and 614 N_{T} the target particle population's density (the same subscripts apply). = 615 For our purpose of obtaining order of magnitude estimates for ions in different media, we simply
- 616 need to examine $\Gamma_{N:G}$, the ratio of the ions' mean free paths in the neutral gas (N) to grain (G)

617 populations, which reduces to:

618 619

620

$$\Gamma_{N:G} = \frac{MFP_{N}}{MFP_{G}} = \frac{vt / (\pi(r_{I} + r_{N})^{2} vt N_{N})}{vt / (\pi(r_{I} + r_{G})^{2} vt N_{G})} \sim \frac{(r_{I} + r_{G})^{2} N_{G}}{(r_{I} + r_{N})^{2} N_{N}}$$
(A1)

If $\Gamma_{N:G} \approx 1$, the ion's MFP in the neutral gas is about the same as it is in the grains. It is easier for the ion to pass through (a) the neutral gas if $\Gamma_{N:G}$ is >> 1, or, vice versa, (b) the grains if $\Gamma_{N:G}$ is << 1. We calculate values for a range of estimated situations below, as detailed information for the grains throughout Saturn's magnetosphere is not complete in order to see if the grains should even be considered as possibly affecting the suprathermal ion populations.

Neutral Gas. For the neutral gas, we use the models of Cassidy & Johnson (2010) and Smith et al. (2010), which is accepted as being a reasonable representation of the neutral gas populations in Saturn's magnetosphere derived from Cassini measurements. Their model shows that while the O and OH number densities, N_0 and N_{OH} , respectively, are nearly equal (to within ~25%) at Enceladus' orbit, N_0 is ~3.5 times higher than N_{OH} at Rhea's orbit. As they are the two most populous neutral species, we perform calculations for both O and OH, because, OH, with ~22% of the plasma density near Rhea, can still produce measurable effects in that region.

Grains and Dust. Saturn's magnetosphere is filled with an icy, dusty plasma, and is the closest 633 634 environment to Earth similar in any way to vast expanses of the interstellar medium. The radial 635 variation of CDA data collected from 2004-200 to 2008-259 for nanometer grains and the fit to it 636 in Figure 11 of Srama et al. (2011) is a clear, comprehensive, long-term display of 637 magnetospheric-scale E-ring grain data. Srama et al. (2011) do not state whether data within 638 several to tens of Enceladus radii, near the moon and its plume, were included in this long-term data set or not, but the display, a data collection intended to represent an overall average 639 640 perspective of the E-ring grains, suggests that near-Enceladus data were not included. To our 641 knowledge, no study E-ring data at/near the orbit of Enceladus, characterizes the azimuthal

642 variation of the grain population in a manner useful in our study. In their Figure 11, Srama et al. (2011) fit the radial variation of CDA densities with a power law, given as $n(r) = 20 (r - 2.8)^{-4.6}$, 643 644 in the range \sim 4.5-19 R_s, for data obtained from 3 to 19 R_s. The n(r) fit is very close to the density 645 averages plotted from ~ 5 to ~ 15 R_S at intervals of 1-3 R_S. The mean density point plotted at < 5646 R_S is far below their n(r) fit, consistent with their statement that, on account of dead time limitations, the CDA counting rates saturated at times near Enceladus' orbit, 3.95 Rs, so that the 647 648 derived number density from those saturated counting rates (as shown) at < -4.5 R_S are a lower 649 limit. The fall-off with increasing radial distance is similar to other reports (see e.g., Ye et al., 650 2016), so we take their fit in this radial range as a reliable representation of average-Enceladus orbit data which does not include the near-moon plume flux and, therefore, representative of the 651 652 overall average E-ring population from ~3.95 - 15 R_s at locations not directly influenced by the 653 Enceladus plume. Therefore, for our purposes, we can estimate the average grain density near the orbit of Rhea, 8.75 R_S, from their n(r) fit in determining $\Gamma_{N:G}$ near Rhea's orbit from 654 655 measurements typically made near the orbit of Enceladus. Their measurements are for 656 micrometer sized grains, whereas most of the grains are at nanometer sizes, at least near Enceladus. The values of $\Gamma_{N:G}$ we obtain (see Tables S1-S3 in the Supporting Information) range 657 658 within a factor of ~3-4 about 1 for characteristic grain sizes of 1 and 2 nm. This is not an 659 exhaustive assessment and only elastic collisions were considered, as well as much of the 660 necessary, relevant information particular to the grains and the gas is not yet well established, 661 nor will be ion the near future. Nevertheless, these estimates are not orders of magnitude higher or lower than unity, they are clustered around ~ 1 , the value at which the H₂O⁺ mean free path in 662 663 the dust/grain populations is approximately equal to that in the neutral gas populations. Finally, 664 this exercise does suggest that, when the extant grain population sizes and gas and grain densities 665 in Saturn's magnetosphere are known: that is, measured, confirmed, and characterized, the effect

- 666 of grains on Saturn's suprathermal ions and various other observables can be established and
- 667 might be found to be of significance.

669 References

- Allegrini, F., McComas, D. J., Young, D T., Berthelier, J. -J., Covinhes, J., Illiano, J. -M., et al.
- 671 (2006). Energy loss of 1-50 keV H, He, C, N, O, Ne, and Ar ions transmitted through thin
- 672 carbon foils. Reviews of Scientific Instruments, 77(4). https://doi.org/10.1063/1.2185490
- 673 Armstrong, T. P., Paonessa, M. T., Bell II, E. V., & Krimigis, S. M. (1983). Voyager
- observations of Saturnian ion and electron phase space densities. *Journal of Geophysical Research, 88,* 8893-8904. https://doi.org/10.1029/JA088iA11p08893
- 676 Botschwina, P., Rosmus, P., & Reinsch, E. A. (1983). Spectroscopic properties of the
- 677 hydroxonium ion calculated from scep cepa wave functions. Chemical Physics Letters, 102,
- 678 299-306. https://doi.org/10.1016/0009-2614(83)87045-6
- Branscomb, L. M., (1966). Photodetachment cross section, electron affinity, and structure of the
 negative hydroxyl ion. *Physical Review*, *148*, 1, 11-18.
- 681 https://org/doi/10.1103/PhysRev.148.11
- 682 Burch, J. L., Goldstein, J., Hill, T. W., Young, D. T., Crary, F. J., Coates, A. J., et al. (2005).
- 683 Properties of local plasma injections in Saturn's magnetosphere. *Geophysical Research Letters*,
- 684 *32*, L14S02. https://doi.org/10.1029/2005GL022611
- Burger, M. H., Sittler Jr., E. C., Johnson, R., E., Smith, H. T., Tucker, O. J., & Shematovich, V.
- 686 I. (2007). Understanding the escape of water from Enceladus. Journal of Geophysical
- 687 Research, 112, A06219. https://doi.org/10.1029/2006JA012086
- Cassidy, T. A., & Johnson, R. E. (2010). Collisional spreading of Enceladus' neutral cloud. *Icarus*, 209, 696-703. https://doi.org/10.1016/j.icarus.2010.04.010
- 690 Christon, S. P., Hamilton, D. C., Mitchell, D. G., DiFabio, R. D., & Krimigis, S. M. (2014).
- 691 Suprathermal magnetospheric minor ions heavier than water at Saturn: Discovery of ²⁸M⁺
- 692 seasonal variations. Journal of Geophysical Research, 119, 7, pp. 5662-5673.

693 https://doi.org/10.1002/2014JA020010

- 694 Cravens, T. E., McNutt Jr., R. L., Waite Jr., J. H., Robertson, I. P., Luhmann, J. G., Kasprzak,
- 695 W., & Ip, W. -H. (2009). Plume ionosphere of Enceladus as seen by Cassini ion and neutral
- 696 mass spectrometer. Geophysical Research Letters, 36, L08106.
 697 https://doi.org/10.1029/2009GL037811
- Dalgarno, A. (1958). The mobilities of ions in their parent gases. *Philosophical Transactions Royal Society London, Series A., 250*, 426. https://doi.org/10.1098/rsta.1958.0003
- 700 Dialynas, K., Brandt, P. C., Krimigis, S. M., Mitchell, D. G., Hamilton, D. C., Krupp, N. et al.
- 701 (2013). The extended Saturnian neutral cloud as revealed by global ENA simulations using
- Cassini/MIMI measurements. Journal of Geophysical Research, 118, 3027–3041.
 https://doi.org/10.1002/jgra.50295
- 704 DiFabio, R. D. (2012). Spatial and temporal variations of the suprathermal (3-220 keV/e) ion
- 705 composition in Saturn's equatorial magnetosphere (Doctoral dissertation). Retrieved from
- 706 Digital Repository at the University of Maryland, University of Maryland, College Park,
- 707 Maryland, USA. https://drum.lib.umd.edu/handle/1903/12700
- 708 DiFabio, R. D., Hamilton, D. C., Krimigis, S. M., & Mitchell, D. G. (2011). Long term time
- variations of the suprathermal ions in Saturn's magnetosphere. *Geophysical Research Letters*,
- 710 *38*, L18103. https://doi.org/10.1029/2011GL048841
- 711 Dong, Y., Hill, T. W., Teolis, B. D., Magee, B. A., & Waite, J. H. (2011). The water vapor
- plumes of Enceladus. Journal of Geophysical Research, 116, A10204.
 https://doi.org/10.1029/2011JA016693
- 714 Dong, Y., & Hill, T. W. (2013). A study of the charged ice grains in the Enceladus plume with a
- 715 composite size distribution. American Geophysical Union Fall Meeting, abstract, P32B-04.
- 716 2013AGUFM.P32B..04D.

- 717 Dong, Y., Hill, T. W., & Ye, S. -Y. (2015). Characteristics of ice grains in the Enceladus plume
- from Cassini observations. Journal of Geophysical Research, 120, 915-937.
- 719 http://dx.doi.org/10.1002/2014JA020288
- 720 Dyke, T. R., & Muenter, J. S. (1973). Electric dipole moments of low J states of H2O and D2O.
- 721 *Journal of Chermical Physics*, *59*, 3125-3127. https://doi.org/10.1063/1.1680453
- Engelhardt, I. A. D.; Wahlund, J. -E.; Andrews, D. J.; Eriksson, A. I.; Ye, S.; Kurth, W. S.; et al.
- 723 (2015). Plasma regions, charged dust and field-aligned currents near Enceladus. *Planetary and*
- 724 Space Science, 117, 453-469. https://doi.org/10.1016/j.pss.2015.09.010
- Farmer, A. J. (2009). Saturn in hot water: Viscous evolution of the Enceladus torus. *Icarus*, 202,
- 726 280-286. https://doi.org/10.1016/j.icarus.2009.02.031
- Fleshman, B. L., Delamere, P. A., & Bagenal, F. (2010a). Modeling the Enceladus plume-plasma
 interaction. *Geophysical Research Letters*, 37, L03202.
 https://doi.org/10.1029/2009GL041613.
- Fleshman, B. L., Delamere, P. A., & Bagenal, F. (2010b). A sensitivity study of the Enceladus
 torus. *Journal of Geophysical Research*, *115*, E04007. https://doi.org/10.1029/2009JE003372
- 732 Fleshman, B. L., Delamere, P. A., Bagenal, F., and Cassidy, T. (2013). A 1-D model of physical
- chemistry in Saturn's inner magnetosphere. Journal of Geophysical Research, 118, 1567-
- 734 1581. https://doi.org/doi:10.1002/jgre.20106
- 735 González-Alfonso, E., Fischer, J., Bruderer, S., Müller, H. S. P., Graciá-Carpio, J., Sturm, E., et
- 736 al. (2013). Excited OH^+ , H_2O^+ , and H_3O^+ in NGC 4418 and Arp 220. Astronomy &
- 737 Astrophysics, 550, A25, 1-23. https://doi.org/10.1051/0004-6361/201220466
- Hansen, C. J., Esposito, L., Stewart, A. I. F., Colwell, J., Hendrix, A., Pryor, W., Shemansky, D.,
- 739 & West, R. (2006). Enceladus' water vapor plume. Science, 311, 1422-1425.
- 740 https://doi.org/10.1126/science.1121254

- 741 Hill, T. W., Rymer, A. M., Burch, J. L., Crary, F. J., Young, D. T., Thomsen, M. F., et al. (2005).
- Evidence for rotationally driven plasma transport in Saturn's magnetosphere. *Geophysical*

743 Research Letters, 32, L14S10. https://doi.org/10.1029/2005GL022620

- Hill, T. W., Thomsen, M. F., Tokar, R. L., Coates, A. J., Lewis, G. R., Young, D. T., et al.
- 745 (2012). Charged nanograins in the Enceladus plume. Journal of Geophysical Research, 117,
- 746 A05209. https://doi.org/doi:10.1029/2011JA017218
- 747 Holmberg, M. K. G., Wahlund, J. -E., & Morooka, M. W. (2014). Dayside/nightside asymmetry
- of ion densities and velocities in Saturn's inner magnetosphere. *Geophysical Research Letters*,
- 749 *41*, 3717–3723. https://doi.org/10.1016/10.1002/2014GL060229
- 750 Holmberg, M. K. G., Wahlund, J. -E., Morooka, M. W., & Persoon, A. M. (2012). Ion densities
- and velocities in the inner plasma torus of Saturn. *Planetary and Space Science*, 73, 1, 151160. https://doi.org/10.1016/j.pss.2012.09.016
- 753 Holmberg, M. K. G., Shebanits, O., Wahlund, J.-E., Morooka, M., Vigren, E., André, N., et al.
- 754 (2017). Density structures, dynamics, and seasonal and solar cycle modulations of Saturn's
- 755 inner plasma disk. Journal of Geophysical Research, 122, 12,258-12,273.
 756 https://doi.org/10.1002/2017JA024311
- Hood, L. L. (1989). Radial diffusion and losses of energetic protons in the 5 to 12 R_s region of
- 758 Saturn's magnetosphere. Journal of Geophysical Research, 94, A7, 8721-8730.
- 759 https://doi.org/10.1029/JA094iA07p08721
- 760 Horányi, M., Juhász, A., & Morfill, G. E. (2008). Large-scale structure of Saturn's E-ring.
- 761 *Geophysical Research Letters*, 35, L04203. https://doi.org/10.1029/2007GL032726
- 762 Ip, W.-H. (1997). On the neutral cloud distribution in the Saturnian magnetosphere. *Icarus, 126*,
- 763 42-57. https://doi.org/10.1006/icar.1996.5618
- 764 Ip, W. -H. (2000). Thermal plasma composition in Saturn's magnetosphere. *Planetary & Space*

- 765 Science., 48, 755-783. https://doi.org/10.1016/S0032-0633(00)00036-2
- 766 Jia, Y. -D., Russell, C. T., Khurana, K. K., Ma, Y. J., Kurth, W., & Gombosi, T. I. (2010).
- 767 Interaction of Saturn's magnetosphere and its moon: 3. Time variation of the Enceladus plume.
- Journal of Geophysical Research, 115, A12243. https://doi.org/10.1029/2010JA015534
- Johnson, R. E., Smith, H. T., Tucker, O. J., Liu, M., Burger, M. H., Sittler, et al. (2006). The
 Enceladus and OH tori at Saturn. *Astrophysical Journal, 644*, L137.
 https://doi.org/10.1086/505750
- Jurac, S., & Richardson, J. D. (2005). A self-consistent model of plasma and neutrals at Saturn:
- Neutral cloud morphology. Journal of Geophysical Research, 110, A09220.
 https://doi.org/10.1029/2004JA0106635
- Kempf, S., Beckmann, U. Moragas-Klostermeyer, G., Postberg, F., Srama, R., et al. (2008). The
 E ring in the vicinity of Enceladus I. Spatial distribution and properties of the ring particles.
- 777 *Icarus, 193*, 420–437. https://doi.org/10.1016/j.icarus.2007.06.027
- Kempf, S., Beckmann U., Srama, R., Horanyi, M., Auer, S., & Grun, E. (2006). The electrostatic
 potential of E ring particles. *Planetary and Space Science*, 54, 999–1006.
 https://doi.org/10.1016/j.pss.2006.05.012
- Kempf, S., Srama, R., Altobelli, N., Auer, S., Tschernjawski, V., Bradley, et al. (2004). Cassini
 between Earth and asteroid belt: first in-situ charge measurements of interplanetary grains. *Icarus*, 171, 2, 317-335. https://doi.org/10.1016/j.icarus.2004.05.017
- 784 Kollmann, P., E. Roussos, C. Paranicas, N. Krupp, C. M. Jackman, E. Kirsch, and K.•H.
- 785 Glassmeier (2011). Energetic particle phase space densities at Saturn: Cassini observations and
- 786 interpretations. Journal of Geophysical Research, 116, A05222.
- 787 https://doi.org/10.1029/2010JA016221
- 788 Krimigis, S. M., Mitchell, D. G., Hamilton, D. C., Livi, S., Dandouras, J., Jaskulek, et al. (2004).

- Magnetospheric Imaging Instrument (MIMI) on the Cassini Mission to Saturn/Titan. *Space Science Reviews, 114,* 233-329. https://doi.org/10.1007/s11214-004-1410-8.
- 791 Krimigis, S. M., Mitchell, D. G., Hamilton, D. C., Krupp, N., Livi, S., Roelof, E. C., et al.
- 792 (2005). Dynamics of Saturn's magnetosphere from MIMI during Cassini's orbital insertion.
- *Science*, *307*, 5713, 1270-1273. https://doi.org/10.1126/science.1105978
- Lishawa, C. R., Dressler, R. A., Gardner, J. A., Salter, R. H., & Murad, E. (1990). Cross sections
- and product kinetic energy analysis of $H_2O^+-H_2O$ collisions at suprathermal energies. *Journal*

796 of Chemical Physics, 93, 3196-3206; https://doi.org/10.1063/1.458852

- Livi, R., Goldstein J., Burch, J. L., Crary, F., Rymer, A. M., Mitchell, D. G., & Persoon, A. M.
- 798 (2014). Multi-instrument analysis of plasma parameters in Saturn's equatorial, inner
- magnetosphere using corrections for spacecraft potential and penetrating background radiation.

800 Journal of Geophysical Research, 119, 3683–3707. https://doi.org/10.1002/2013JA019616

- 801 Marcus, Y. (2012). Volumes of aqueous hydrogen and hydroxide ions at 0 to 200 °C. Journal of
- 802 *Chemical Physics, 137*, 15, 154501-254501-5. https://doi.org/10.1063/1.4758071
- 803 Massey, H. S. W. (1949). Collisions between atoms and molecules at ordinary temperatures.

804 Rep. Progr. Phys., 12, 248. https://doi.org/10.1088/0034-4885/12/1/311

- 805 Mauk, B. H., Saur, J., Mitchell, D. G., Roelof, E. C., Brandt, P. C., Armstrong, T. P., et al.
- 806 (2005). Energetic particle injections in Saturn's magnetosphere. *Geophysical Research Letters*,
- 807 *32*, L14S05. https://doi.org/10.1029/2005GL022485
- 808 Mauk, B. H., Hamilton, D. C., Hill, T. W., Hospodarsky, G. B., Johnson, R. E., Paranicas, C., et
- al. (2009). Fundamental plasma processes in Saturn's magnetosphere. In M. K. Dougherty, L.
- 810 W. Esposito, & S. M. Krimigis (Eds.), Saturn from Cassini-Huygens (pp. 281-331). B.V:
- 811 Springer. https://doi.org/10.1007/978-1-4020-9217-6_11
- 812 McAndrews, H. J., Thomsen, M. F., Arridge, C. S., Jackman, C. M., Wilson, R. J., Henderson,

- 813 M. G., & Dougherty, M. K. (2009). Plasma in Saturn's nightside magnetosphere and the
- 814 implications for global circulation. *Planetary and Space Science*, 57 (14-15), 1714.

815 https://doi.org/10/1016/j.pss.2009.03.003

- 816 Meier, P., Kriegel, H., Motschmann, U., Schmidt, J., Spahn, F., Hill, T. W., et al. (2014). A
- 817 model of the spatial and size distribution of Enceladus' dust plume. *Planetary and Space*
- 818 Science, 104, 216–233. http://dx.doi.org/10.1016/j.pss.2014.09.016
- 819 Melin, J., Ortiz, J. V., Martín, I., Velasco A. M., & Lavín, C. (2005). Ground and excited states

820 of the Rydberg radial H3O: Electron propagator and quantum defect analysis. *Journal of*

821 *Chemistry and Physics, 122, 23, 234317-234317-7.* https://doi.org/10.1063/1.1926286

- 822 Melin, H., Shemansky, D. E., & Liu, X. (2009). The distribution of atomic hydrogen and oxygen
- in the magnetosphere of Saturn. *Planetary and Space Science*, 57, 1743-1753.
 https://doi.org/10.1016/j.pss.2009.04.014
- 825 Mitchell, D. G., Carbary, J. F., Cowley, S. W. H., Hill, T. W., & Zarka, P. (2009a). The
- 826 Dynamics of Saturn's magnetosphere. In M. K. Dougherty, L. W. Esposito, & S. M. Krimigis
- 827 (Eds.), Saturn from Cassini-Huygens (pp. 257-279). B.V: Springer.
 828 https://doi.org/10.1007/978-1-4020-9217-6 10
- Mitchell, D. G., Krimigis, S. M., Paranicas, C., Brandt, P. C., Carbary, J. F., Roelof, E. C., et
 al.(2009b). Recurrent energization of plasma in the midnight-to-dawn quadrant of Saturn's
 magnetosphere and its relationship to auroral UV and radio emissions. *Planetary and Space*
- 832 Science, 57, 1732. https://doi.org/10.1016/j.pss.2009.04.002
- Nemeth, Z., Szego, K., Foldy, L., Kivelson, M. G., Jia, X., Ramer, K. M., et al. (2015). The
 latitudinal structure of the nightside outer magnetosphere of Saturn as revealed by velocity
 moments of thermal ions, Annales Geophysicae, 33, 1195–1202.
 https://doi.org/10.5194/angeo-33-1195-2015

- 837 Northcliffe, L. C., & Schilling, R. F. (1970). Range and stopping-power tables for heavy ions.
- Atomic Data and Nuclear Data Tables, 7, 3-4, 233-463. https://doi.org/10.1016/S0092640X(70)80016-X
- 840 Paranicas, C., Mitchell, D. G., Krimigis, S. M., Hamilton, D. C., Roussos, E., Krupp, N., et al.
- 841 (2008). Sources and losses of energetic protons in Saturn's magnetosphere. *Icarus197, 2,* 519-
- 842 525. https://doi.org/10.1016/j.icarus.2008.05.011
- 843 Paranicas, C., Mitchell, D. G., Roelof, E. C., Mauk, B. H., Krimigis, S. M., Brandt, P. C., et al.
- 844 (2007). Energetic electrons injected into Saturn's neutral cloud. *Geophysical Research Letters*,
- 845 *34*, L02109. https://doi.org/10.1029/2006GL028676
- 846 Persoon, A. M., Gurnett, D. A., Leisner, J. S., Kurth, W. S., Groene, J. B, & Faden, J. B. (2013).
- 847 The plasma density distribution in the inner region of Saturn's magnetosphere, *Journal of*848 *Geophysical Research*, 118, 2970–2974, https://doi.org/10.1002/jgra.50182
- 849 Persoon, A. M., Gurnett, D. A., Santolik, O., Kurth, W. S., Faden, J. B., Groene, J. B., et al.
- 850 (2009). A diffusive equilibrium model for the plasma density in Saturn's magnetosphere,
- *Journal of Geophysical Research, 114*, A04211, https://doi.org/10.1029/2008JA013912
- 852 Porco, C. C., Helfenstein, P., Thomas, P. C., Ingersoll, A. P, Wisdom, J., West, R., et al. (2006).
- 853 Cassini observes the active south pole of Enceladus, Science, 311, 1393.
- 854 https://doi.org/10.1126/science.1123013
- 855 Press, W. H., Flannery, B. P., Teukolsky, S. A., & Vetterling, W. T. (1989). Numerical Recipes:
- 856 The Art of Scientific Computing, Cambridge University Press, New York
- 857 Rapp, D., & W. E. Francis (1962). Charge exchange between gaseous ions and atoms. *Journal*
- 858 *Chemical Physics*, 37, 2631. https://doi.org/10.1063/1.1733066
- Richardson, J. D. (1998). Thermal plasma and neutral gas in Saturn's magnetosphere. Reviews of
- 860 *Geophysics*, 36, 501-524. https://doi.org/10.1029/98RG01691

- 861 Richardson, J. D., Eviatar, A., McGrath, M. A., & Vasyliunas V. M. (1998). OH in Saturn's
- 862 magnetosphere: Observations and implications. *Journal of Geophysical Research*, 103, 20245.
- 863 https://doi.org/10.1029/98JE01127
- 864 Rymer, A. M., Mauk, B. H., Hill, T. W., Paranicas, C., André, N., Sittler Jr., E. C., et al. (2007).
- 865 Electron sources in Saturn's magnetosphere. *Journal of Geophysical Research, 112*, A02201.
- 866 https://doi.org/10.1029/2006JA012017
- 867 Rymer, A. M., Mauk, B. H., Hill, T. W., Paranicas, C., Mitchell, D. G., Coates, A. J., & Young,
- B68 D. T. (2008). Electron circulation in Saturn's magnetosphere. *Journal of Geophysical Research*, 113, A01201. https://doi.org/10.1029/2007JA012589
- 870 Rymer, A. M., Mauk, B. H., Hill, T. W., André, N., Mitchell, D. G., Paranicas, C., et al. (2009).
- 871 Cassini evidence for rapid interchange transport at Saturn. *Planetary and Space Science*, *57*,
 872 1779. https://doi.org/10.1016/j.pss.2009.04.010
- 873 Saur, J., N., Schilling, Neubauer, F. M., Strobel, D. F., Simon, S., Dougherty, M. K., et al.
- 874 (2008). Evidence for temporal variability of Enceladus' gas jets: Modeling of Cassini
 875 observations. *Geophysical Research Letters*, 35, L20105.
- 876 https://doi.org/10.1029/2008GL035811
- 877 Schippers, P., Blanc, M., André, N., Dandouras, I., Lewis, G. R., Gilbert, L. K., et al. (2008).
- Multi-instrument analysis of electron populations in Saturn's magnetosphere. *Journal of Geophysical Research*, 113, A07208. https://doi.org/10.1029/2008JA013098
- 880 Sergis, N., Krimigis, S. M., Mitchell, D. G., Hamilton, D. C., Krupp, N., Mauk, B. M., et al.
- 881 (2007). Ring current at Saturn: Energetic particle pressure in Saturn's equatorial
- magnetosphere measured with Cassini/MIMI. Geophysical Research Letters, 34, L09102.
- 883 https://doi.org/10.1029/ 2006GL029223
- 884 Sergis, N., Krimigis, S. M., Mitchell, D. G., Hamilton, D. C., Krupp, N., Mauk, B. M., et al.

2019JA027315R' Saturn Magnetospheric Energetic W⁺ Composition p.39

- (2009). Energetic particle pressure in Saturn's magnetosphere measured with the
 Magnetospheric Imaging Instrument on Cassini. *Journal of Geophysical Research*, 114,
 A02214. https://doi.org/10.1029/2008JA013774
- 888 Shemansky, D. E, Matheson, P., Hall, D. T., Hu, H. -Y., & Tripp, T. M. (1993). Detection of the
- hydroxyl radical in the Saturn magnetosphere. *Nature, 363*, 329-331.
 https://doi.org/10.1038/363329a0
- 891 Sergis, N., Krimigis, S. M., Roelof, E. C., Arridge, C. S., Rymer, A. M., Mitchell, D. G. et al.
- 892 (2010). Particle pressure, inertial force, and ring current density profiles in the magnetosphere
- of Saturn, based on Cassini measurements. Geophysical Research Letters, 37, L02102.
- 894 https://doi.org/10.1029/2009GL041920
- Showalter, M. R., Cuzzi, J. N, Larson, S. M. (1991). Structure and particle properties of Saturn's
 E Ring. *Icarus*, 94, 2, 451-473. https://doi.org/10.1016/0019-1035(91)90241-K
- 897 Sittler Jr., E. C., Andre, N., Blanc, M., Burger, M., Johnson, R. E., Coates, A., et al. (2008). Ion
- and neutral sources and sinks within Saturn's inner magnetosphere: Cassini results. *Planetary*
- and Space Science, 56, 3. https://doi.org/10.1016/j.pss.2007.06.006
- 900 Slater, J. C., (1964). Atomic Radii in Crystals. *Journal of Chemical Physics*, 41, 10, 3199-3204.
- 901 https://org/doi/10.1063/1.1725697
- 902 Smith, H. T., Johnson, R. E., Perry, Mitchell, M. E., D. G., McNutt, R. L., & Young, D. T.
- 903 (2010). Enceladus plume variability and the neutral gas densities in Saturn's magnetosphere.
- Journal of Geophysical Research 115, A10252. https://doi.org/10.1029/2009JA015184
- 905 Srama, R., Ahrens, T. J., Altobelli, N., Auer, S., Bradley, J. G., Burton, M., et al. (2004). The
- 906 Cassini Cosmic Dust Analyzer. Space Science Reviews, 114, 1-4, 465-518.
- 907 https://doi.org/10.1007/s11214-004-1435-z

- 908 Srama, R., Kempf, S., Moragas-Klostermeyer, G., Altobelli, N., Auer, S., Beckmann, U., et al.
- 909 (2011). The cosmic dust analyser onboard Cassini: ten years of discoveries. CEAS Space
- 910 Journal, 2, 1-4, 3-16. https://doi.org/10.1007/s12567-011-0014-x
- 911 Thomsen, M. F., Reisenfeld, D. B., Delapp, D. M., Tokar, R. L., Young, D.T., Crary, F. J., et al.
- 912 (2010). Survey of ion plasma parameters in Saturn's magnetosphere. *Journal of Geophysical*
- 913 Research, 115, A10220. https://doi.org/10.1029/2010JA015267
- 914 Tokar, R. L., Johnson, R. E., Hill, T. W., Pontius, D. H., Kurth, W. S., Crary, F. J., et al. (2006).
- 915 The interaction of the atmosphere of Enceladus with Saturn's plasma. *Science*, *311*, 1409.
- 916 https://doi.org/10.1126/science.1121061
- 917 Tokar, R. L., Johnson, R. E., Thomsen, M. F., Wilson, R. J., Young, D. T., Crary, et al. (2009).
- 918 Cassini detection of Enceladus' cold water-group plume ionosphere. *Geophysical Research*919 *Letters*, *36*, L13203. https://doi.org/10.1029/2009GL038923
- 920 Van Allen, J. A., Randall, B. A., & Thomsen, M. F. (1980). Sources and sinks of energetic
- 921 electrons and protons in Saturn's magnetosphere. Journal of Geophysical Research, 85, 5679-
- 922 5694. https://doi.org/10.1029/JA085iA11p05679
- 923 Vandegriff, J., DiFabio, R., Hamilton, D., Kusterer, M., Manweiler, J., Mitchell, D., et al. (2018).
- 924 Cassini/MIMI Instrument Data User Guide. NASA, Washington, D. C. Available at
 925 http://pds.nasa.gov
- 926 von Steiger, R., Schwadron, N. A., Fisk, L. A., Geiss, J., Gloeckler, G., Hefti, et al. (2000).
- 927 Composition of quasi-stationary solar wind flows from Ulysses/Solar Wind Ion Composition
- 928 Spectrometer. Journal of Geophysical Research, 105, 27,217-27,238.
 929 https://doi.org/10.1029/1999JA000358
- 930 Waite Jr., J. H., Combi, M. R., Ip, W. -H., Cravens, T. E., McNutt Jr., R. L., Kasprzak, W., et
- 931 al.(2006). Cassini ion and neutral mass spectrometer: Enceladus plume composition and

- 932 structure. *Science*, *311*, 1419-1422. https://doi.org/10.1126/science1121290
- 933 Walt, M. (1971). The radial diffusion of trapped particles induced by fluctuating magnetospheric
- 934 fields. *Space Science Reviews*, *12*, *4*, 446-485. https://doi.org/10.1007/BF00171975
- Weast, R. C. (Ed.) (1968). CRC Handbook of Chemistry and Physics, 49th Ed., p. E-71,
 Cleveland.
- 937 Weis, B., Carter, S., Rosmus, P., Werner, H.-J., & Knowles, P. J. (1989). A theoretical
- 938 rotationally resolved infrared spectrum for H_20^+ (X 28 1). Journal of Chemical Physics, 91,
- 939 2818-2833. https://doi.org/10.1063/1.456951
- 940 Werner, H.-J., Rosmus, P., & Reinsch, E.-A. (1983). Molecular properties from MCSCF-SCEP
- wave functions. I. Accurate dipole moment functions of OH, OH⁻, and OH⁺. *Journal of Chemical Physics*, 79, 905-916. https://doi.org/10.1063/1.445867
- 943 Wiedmann, R. T., Tonkyn, R. G., White, M. G., Kwanghsi, W., & McKoy, V. (1992).
- 944 Rotationally resolved threshold photoelectron spectra of OH and OD. Journal Chemical
- 945 Physics, 97, 768-772. https://doi.org/10.1063/1.463179
- Wilson, R. J., Bagenal, F., Cassidy, T., Fleshman, B. L., &. Crary, F. (2015), The relative
 proportions of water group ions in Saturn's inner magnetosphere: A preliminary study, *Journal*
- 948 Geophysical Research, Space Physics, 120, 6624–6632, https://doi.org/10.1002/2014JA020557
- 949 Wilson, R. J., Tokar, M. G., Henderson, R. L., Hill, T. W, Thomsen M. F., & Pontius, D. H.
- 950 (2008). Cassini plasma spectrometer thermal ion measurements in Saturn's inner
- 951 magnetosphere. Journal of Geophysical Research, 113, A12218.
- 952 https://doi.org/10.1029/2008JA013486
- 953 Ye, S.-Y., Gurnett, D. A., Kurth, W. S., Averkamp, T. F., Kempf, S., Hsu, H.-W., Srama, R., &
- 954 Grün, E. (2014). Properties of dust particles near Saturn inferred from voltage pulses induced
- by dust impacts on Cassini spacecraft. Journal of Geophysical Research, 119, 6294-6312.

- 956 https://doi.org/10.1002/2014JA020024
- 957 Young, D. T., Berthelier, J.-J., Blanc, M., Burch, J. L., Bolton, S., Coates, A. J., et al. (2005).
- 958 Composition and dynamics of plasma in Saturn's magnetosphere. *Science*, 307, 1262-1266.
- 959 https://doi.org/10.1126/science.1106151
- 960 Ye, S.-Y., D. A. Gurnett, W. S. Kurth, T. F. Averkamp, S. Kempf, H.-W. Hsu, R. Srama, and E.
- 961 Grün (2014), Properties of dust particles near Saturn inferred from voltage pulses induced by
- 962 dust impacts on Cassini spacecraft, J. Geophys. Res. Space Physics, 119, 6294-6312,
- 963 doi:10.1002/2014JA020024
- 964 Ye, S.-Y., W. S. Kurth, G. B. Hospodarsky, T. F. Averkamp, and D. A. Gurnett (2016). Dust
- 965 detection in space using the monopole and dipole electric field antennas, J. Geophys. Res. Space
- 966 Physics, 121, 11,964–11,972. doi:10.1002/2016JA023266.
- 967

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- 972 and Cassini ephemeris data are publicly available in the Planetary Data System and can be found
- 973 at http://pds.nasa.gov. We thank M. Chaplin for useful discussions.

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976 Figure Captions

978 Figure 1. (a) Essd channel, the Solid State Detector (SSD) energy channel number, versus TOF channel, the time-of-flight channel number of the ~96 keV W^+ . (b) The ~96 keV W^+ TOF 979 980 channel count histogram for the data in the Essd channel range indicated by the horizontal red 981 dashed lines in (a). Data from 78 equatorial ring current passes from 2004 to 2010 are summed. 982 These data are from CHEMS telescope 1 which has the best heavy ion resolution (DiFabio, 983 2012). Figure 2. ~96 keV O^{++} (E/O = 48 keV/e) TOF Channel count distribution for all 78 equatorial 984 985 ring current passes from 2004 to 2010 (L = 7-16, Latitude = -10° to 10°) combined. The solid red 986 line represents the best fit to the distribution using Equation 1 (See text). We use an asymmetric 987 Gaussian to fit the counts near the center of the distribution and add a small correction to the

988 Gaussian on the right side to fit the counts in the "tail."

Figure 3. Best fit of the \sim 96 keV W⁺ distribution. The fits to each individual species are shown along with the sum of the four fits (red). The data are from CHEMS telescope 1.

Figure 4. (a) The partial number density of energetic, 96 keV, water group components versus L.

(b) The fractional abundance of 96 keV water group components versus L. The error bars of O^+ ,

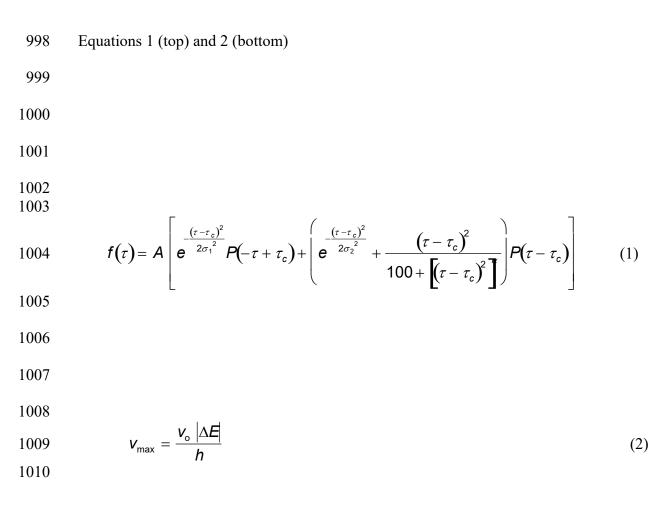
993 OH^+ , and H_2O^+ represent the statistical uncertainties from the best fit. The error bars of H_3O^+

994 represent the spread of values from our three different fits (see text).

995 Figure 5. (top 3 panels) The water-group fractional abundances plotted over model E-ring grain

996 (Hornáyi et al., 2008) and OH density (Jurac et al., 2005) information. (bottom panel) Grain

997 charge information from Kempf et al. (2008) and Ye et al. (2014).



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- 1011 Table 1: Partial number density and relative abundance of the four major ~96 keV W^+ 1012 components in Saturn's equatorial ring current region (L = 7-16)^a.
- 1013

Species	Counts	Partial Number Density (x10 ⁻⁶ cm ⁻³)	Fraction of W^+	
O^+	14400	23.4 ± 0.7	0.53 ± 0.02	
OH^+	5743	9.6 ± 0.4	0.22 ± 0.01	
H_2O^+	5607	9.7 ± 0.4	0.22 ± 0.01	
H_3O^+	690	$1.2 \pm 0.4, -0.48^{b}$	0.028 +0.01, -0.012 ^b	

- 1014
- 1015
- 1016

1017 a The abundances are determined using the results from our best fit ($\alpha = 1.90$). The uncertainties

1018 of O^+ , OH^+ , and H_2O^+ reflect the statistical uncertainties from our fits.

1019 b The H_3O^+ uncertainty reflects the range of values from our three fits (see text).

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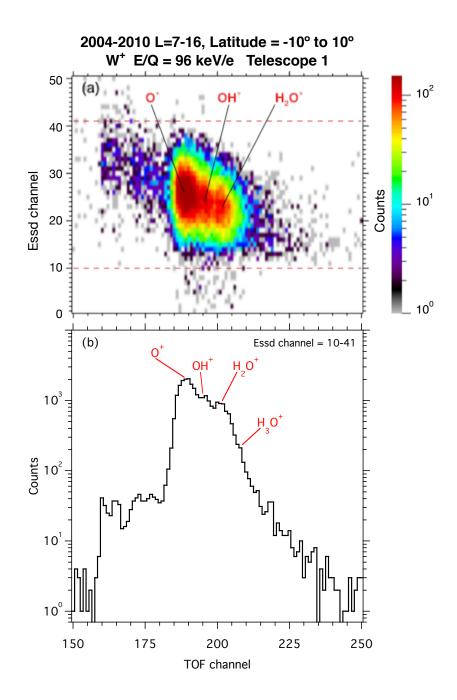
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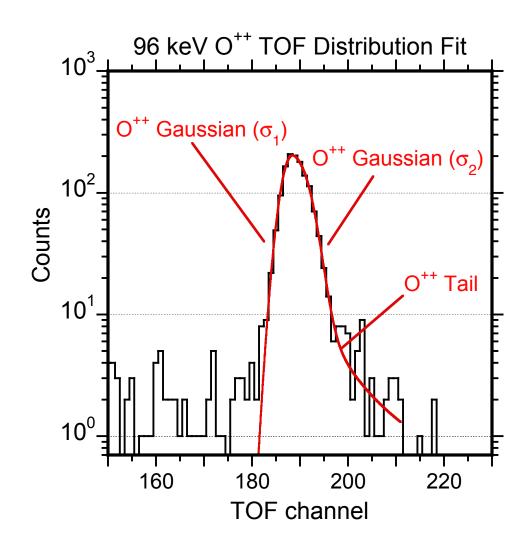
1022 Table 2:	Component to Total* W ⁺	Fractional Abundance	Ratio Comparisons

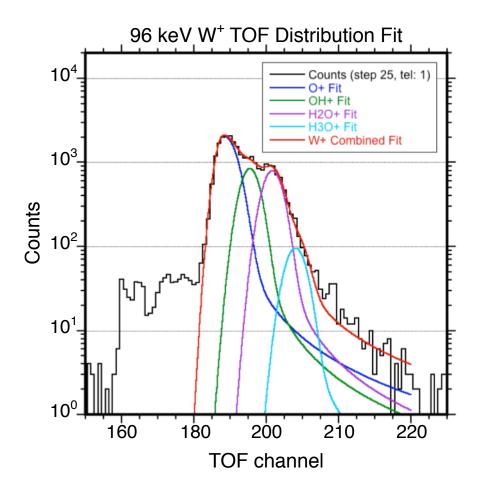
W ⁺ Analysis	O^+/W^+	OH ⁺ /W ⁺	H_2O^+/W^+	H_3O^+/W^+
This Study (Suprathermal Ions) $(\sim 7 \le L \le \sim 16)$	0.52-0.55	0.20-0.22	0.22-0.22	0.047-0.023
Wilson et al. (2015) (Thermal Ions) $(\sim 7 \le L \le \sim 10)$	0.20-0.24	0.28-0.30	0.29-0.28	0.23-0.18
Fleshman et al. (2013) (Model) $(\sim 7 \le L \le \sim 10)$	0.24-0.33	0.19-0.22	0.29-0.26	0.28-0.19

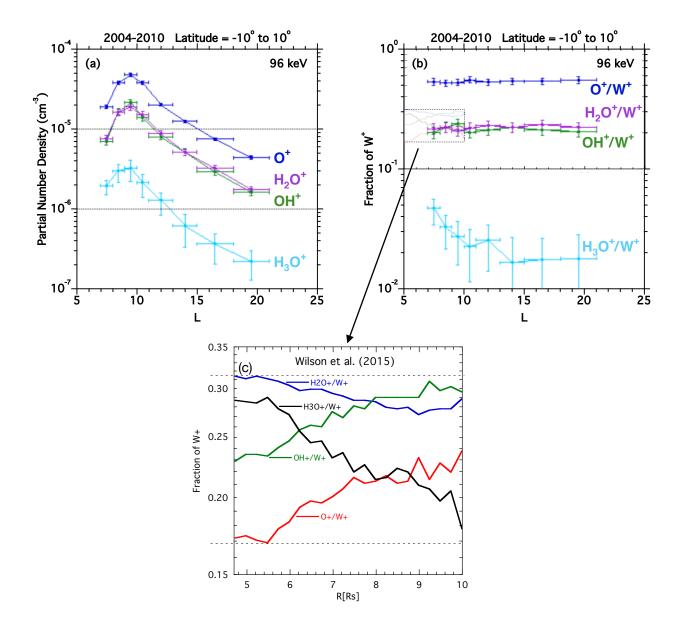
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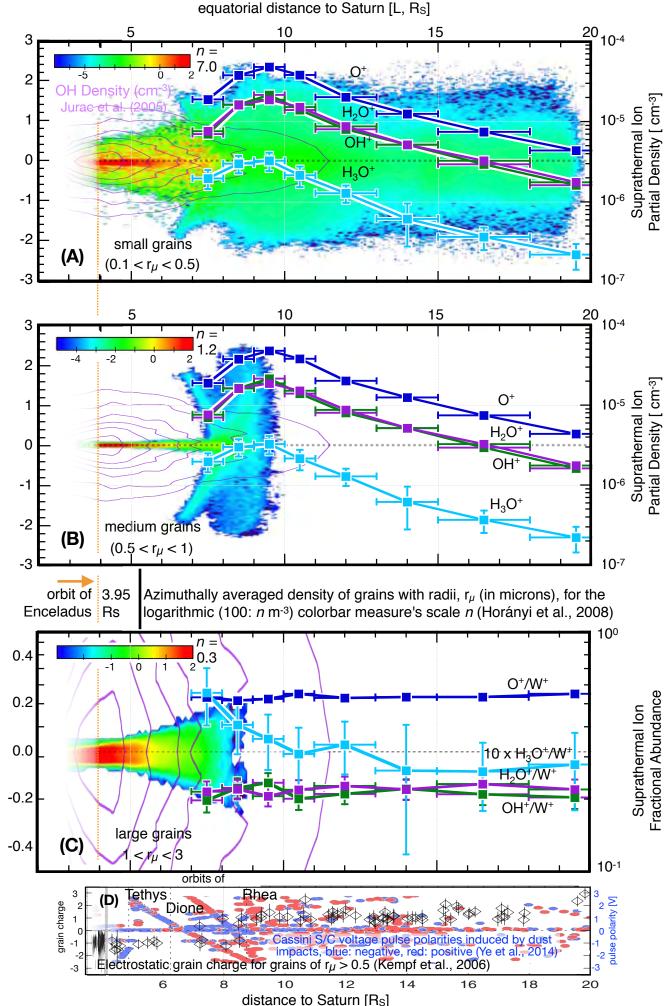
* $[W^+] = [O^+] + [OH^+] + [H_2O^+] + [H_3O^+]$, the W⁺ population is the sum of the O⁺, OH⁺, H₂O⁺, and H₃O⁺ populations











height above equator [Rs]



Journal of Geophysical Research, Space Physics

Supporting Information for

The Composition of 96 keV W⁺ in Saturn's Magnetosphere

R. D. DiFabio^{1,2}, D. C. Hamilton¹, S. P. Christon^{3*}, D. G. Mitchell⁴, S. M. Krimigis^{4,5}

1. University of Maryland, Department of Physics, College Park, MD, USA

2. now at : University of Louisiana, Department of Physics, Lafayette, LA, USA

3. Focused Analysis and Research, Charleston, SC, USA

4. Johns Hopkins University, Applied Physics Laboratory, Laurel, MD, USA

5. Academy of Athens, Athens, Greece

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Table S1.	Molecular	Ionic Radi	us and Diam	eter Information

= 3.9e-18

 $(r_{I+}r_{N})^{2}N_{N}$

		====Radiu	ıs, r _I ======	==Diameter======	====Reference===
H_3O^+	hydroxonium (hydronium)	0.100 nm	= 100.0 pm	0.200 nm = 200.0 pm	(MCa;Marcus, 2012)
H_2O^+	water ion	0.138 nm	= 138.0 pm	0.276 nm = 276.0 pm	(MCa)
H_2O^o	water(diameter)	1.38 Å	= 138.0 pm	2.75 Å = 275.0 pm	(MCc)
OH^+	hydroxyl	1.032 Å	= 103.2 pm	2.064 Å = 206.4 pm	(NIST)
OH	$r_{OH-} (r_{OHo} \pm 0.002 \text{ A})$		= 103.7 pm	= 207.4 pm	(Branscomb, 1966)
OH-	hydroxide	0.970 Å	= 97.0 pm	1.94 Å = 194.0 pm	(NIST)
OH		0.110 nm	= 110.0 pm	0.220 nm = 220.0 pm	(MCb)
OH^{o}	hydroxyl radical		= 103.5 pm	= 207.0 pm	(average: OH ⁺ ,OH ⁻)
O°	oxygen atom	60pm	= 60.0 pm	= 120.0 pm	(Slater, 1964)

References:

Chaplin, M. (2019), Water Structure and Science, London South Bank University (http://www1.lsbu.ac.uk/water/water structure science.html). MCa: Chaplin19a: http://www1.lsbu.ac.uk/water/hydrogen ions.html MCa: "H₃O⁺ has an effective ion radius of 0.100 nm, ... less than that of the H₂O molecular radius (0.138 nm)." MCb: Chaplin19b: http://www1.lsbu.ac.uk/water/ionisoh.html MCc: http://www1.lsbu.ac.uk/water/water molecule.html Marcus, Y. (2012). Volumes of aqueous hydrogen and hydroxide ions at 0 to 200 °C. Journal of Chemical Physics, 137, 15, 154501-254501-5. https://doi.org/10.1063/1.4758071 Branscomb, L. M., (1966). Photodetachment cross section, electron affinity, and structure of the negative hydroxyl ion. Physical Review, 148, 1, 11-18. https://org/doi/10.1103/PhysRev.148.11 Slater, J. C., (1964). Atomic Radii in Crystals. Journal of Chemical Physics, 41, 10, 3199-3204. https://org/doi/10.1063/1.1725697 _____ Figure 4 of Cassidy & Johnson (2010): neutral density at Rhea's orbital distance O-density(at Rhea) ~70/cc OH-density(at Rhea) ~20/cc (a) (b) $r_1 + r_N(O H_2O^+) = (138+60)e-12 = 198e-12$ $r_1 + r_N (OH H_2O^+) = (138+97)e-12 = 235e-12$ (a) (b) $(r_{I+}r_N)^2 N_N = (198e-12 m)^2 x 70/cc$ $(r_{I+}r_{N})^{2} N_{N} = (235e-12 m)^{2} x 20/cc$ = 2.7e-18 $(r_{I+}r_N)^2 N_N$ $\rightarrow \rightarrow (r_{I+}r_N)^2 N_N$ = 1.1e-18 $\rightarrow \rightarrow$ Figure 6 of Smith et al. (2010): neutral density at Rhea's orbital distance, average of Cassini E3 and E5 flybys O-density(at Rhea) ~100/cc OH-density(at Rhea) ~50/cc (d) (c) $r_{I}+r_{N}(O_{H_{2}}O^{+}) = (138+60)e-12 = 198e-12$ (d) $r_1 + r_N(O_H_2O^+) = 138 + 97 = 235e - 12$ (c) $(r_{I+}r_{N})^{2}N_{N} = (235e-12 m)^{2} x 50/cc$ $(r_{I+}r_{N})^{2}N_{N} = 2.8e-18$ $= (198e-12 \text{ m})^2 \text{ x } 100/\text{cc}$ $(r_{I+}r_{N})^{2}N_{N}$

 $\rightarrow \rightarrow$

 $(r_{I+}r_{N})^{2} N_{N}$

Table S2. Grain Size and Density Information

```
Srama et al. (2011): give n(r) = 20(r - 2.8)<sup>-4.6</sup> for grain density falloff (best fit at 3.95-8.73 R<sub>s</sub>)

Enceladus: 20 (3.95 - 2.8)<sup>-4.6</sup> = 10.515258 : 10.5

Rhea: 20 (8.73 - 2.8)<sup>-4.6</sup> = 0.005559. : 5.56e-3

Grain/dust density scale factor: 0.005559/10.515258 = 0.000529 ~ 5e-4

(e) grain size = 1.0 nm = 0.3e-9 = 1000e-12 m, from Fig.10, Dong et al. (2015)

(f) grain size = 2.0 nm = 2.0e-9 = 2000e-12 m, from Fig.10, Dong et al. (2015)

grain density@Rhea = 2000 x 5e-4 = 1, from Fig.11a, Dong et al. (2015); Fig.11,Srama et al. (2011)

(e) 1.0 nm grains: r_1+r_G = 138 + 1000 = 1138e-12

(r_1+r_G)^2 N_{G(1)} = (1138e-12)^2 * 2000 * (1) * 5e-4

\rightarrow \qquad (r_1+r_G)^2 N_{G(2)} = (2138e-12)^2 * 1000 * (1) * 5e-4

\rightarrow \qquad (r_1+r_G)^2 N_{G(2)} = 2.3e-18

(g) 4.0 nm grains: r_1+r_G = 138 + 4000 = 4138e-12

(r_1+r_G) N_{G(4)} = (4138e-12)^2 * 200 * (1) * 5e-4

\rightarrow \qquad (r_1+r_G) N_{G(4)} = (4138e-12)^2 * 200 * (1) * 5e-4
```

Table S3. Mean Free Path Ratio ($\Gamma_{N:G}$) Calculations for H₂O⁺ in neutral gas (a-d) and grains (e,f) †

(*::e, 1 nm)	(*::f, 2 nm)	(*::g, 4 nm)
a: 1.3e-18/2.7e-18 = 4.81e-1	a: 2.3e-18/2.7e-18 = 8.52e-1	a: 1.7e-18/2.7e-18 = 6.29e-1
b: $1.3e-18/1.1e-18 = 1.18e0$	b: $2.3e-18/1.1e-18 = 2.09e0$	b: $1.7e-18/1.1e-18 = 1.55e0$
c: 1.3e-18/3.9e-18 = 3.33e-1	a: 2.3e-18/3.9e-18 = 5.90e-1	a: 1.7e-18/3.9e-18 = 4.36e-1
d: $1.3e-18/2.8e-18 = 4.64e-1$	b: $2.3e-18/2.8e-18 = 8.21e-1$	b: $1.7e-18/2.8e-18 = 6.07e-1$
or roughly,		
		a: [O] ~ [4 nm] ~ 0.63 ~ 1/2
b: $[OH] \sim [1 \text{ nm}] \sim 1.2 \sim 1$	b: $[OH] \sim [2 \text{ nm}] \sim 2 \sim 2$	b: $[OH] \sim [4 \text{ nm}] \sim 1.6 \sim 1 1/2$
c: [O] ~ [1 nm] ~ 0.33 ~ 1/3	c: [O] ~ [2 nm] ~ 0.6 ~ 1/2	c: [O] ~ [4 nm] ~ 0.44 ~ $1/2$
d: [OH] ~ [1 nm] ~ 0.46 ~ $1/2$	d: $[OH] \sim [2 \text{ nm}] \sim 0.8 \sim 1$	d: $[OH] \sim [4 \text{ nm}] \sim 0.61 \sim 1/2$

† https://chem.libretexts.org/Bookshelves/Physical_and_Theoretical_Chemistry_Textbook_Maps/Book%3A_Thermodynamics_and_Chemical_Equilibrium_(Ellgen)/04%3A_The_Distribution_of_Gas_Velocities/4.12%3A_The_Frequency_of_Collisions_between_Unlike_Gas_Molecules

Sample Calculation for a::e at Rhea:

$A_{N} = (198e-12 \text{ m})^{2}$ $N_{N} = 70/cc$	$A_{G} = (113)$ $N_{G} = 200$	/			
$\Gamma_{N:G} = \frac{N_G \mathbf{x} \mathbf{A}_G}{\dots} =$		ie-4 x (1138e-12 m) ²		1.3	0.48
$N_{N} \ge A_{N}$	70.	x (198e-12 m) ²	2.744e-18	2.7	

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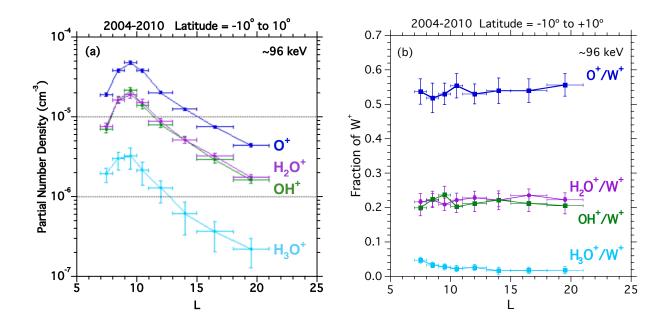


Figure S1 (see Figure 4). (a) The partial number density of energetic, ~96 keV, water group components versus L. (b) The fractional abundance of ~96 keV water group components plotted linearly versus L. The error bars of O^+ , OH^+ , and H_2O^+ represent the statistical uncertainties from the best fit. The error bars of H_3O^+ represent the spread of values from our three different fits (see text).

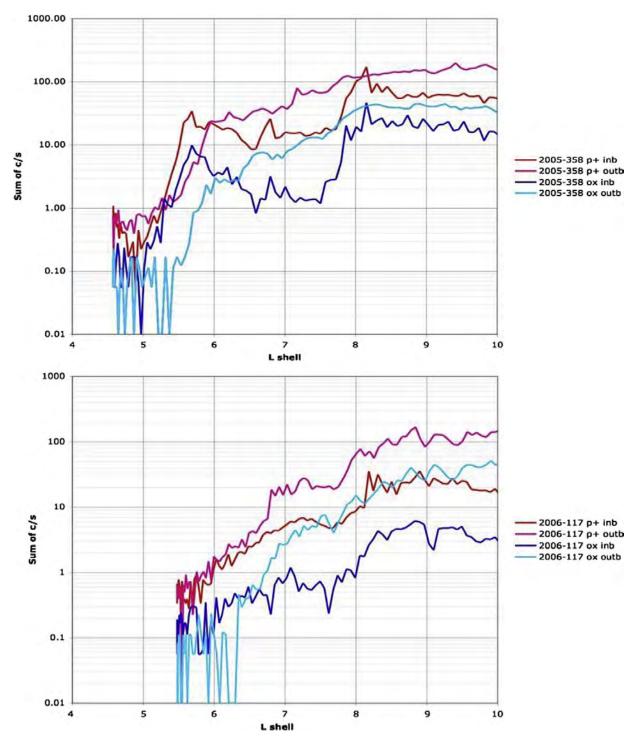


Figure S2. Figure 5 from Paranicas et al. (2008)

Fig. 5. Summed count rates for the periods in Fig. 3 (top) and Fig. 4 (bottom). The inbound and outbound data are plotted separately with the proton sum red and the oxygen sum blue. The proton (oxygen) sum is over the CHEMS energy range 3–220 (8–220) keV.

Figure S3. Figure 1 from Kollmann et al. (2011)

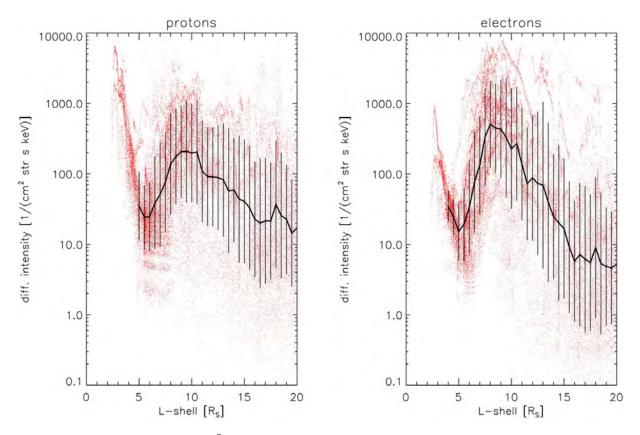


Figure 1. Differential intensities \overline{j} of (left) protons and (right) electrons. Protons have mean energies of 46 keV, and electrons have mean energies of 91 keV; both species have equatorial pitch angles of $\alpha_0 = 10^{\circ} \pm 10^{\circ}$. The red points represent single measurements taken between July 2004 and June 2010 (with exceptions, see section 2). The black solid line is the logarithmic average of these points within intervals of 0.5 R_S width. Error bars show the associated 1σ standard deviations. The increase of intensities for L < 5 is caused by penetrating background and does not represent particles at the mentioned energies.

Figure S4. Figure 4 from Christon et al. (2014)

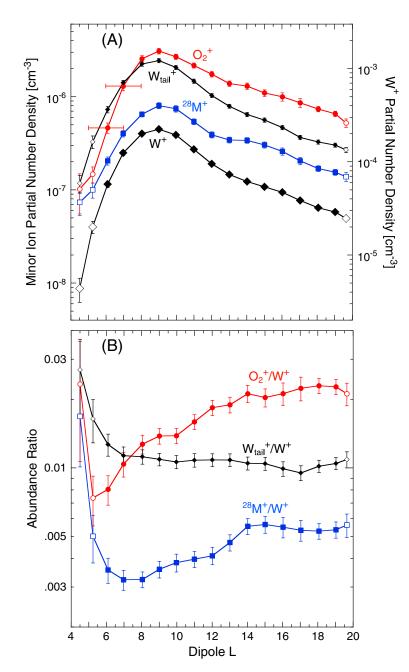


Figure 4. Running dipole *L* averages stepped every integer *L* value (with a 2 R_s window) of (a) W^+ and minor ion partial number densities, PNDs, where the right-side scale for W^+ is offset by several orders of magnitude to facilitate comparison with the minor ions and (b) abundance ratios of minor ions relative to W^+ . The running averages are collected on strict integer *L* bounds and plotted at the mean distance of the average. Uncertainties shown are standard error of the means for ease of statistical comparison. Open symbols at *L* < 6 identify data currently undersampled when compared to the other *L* intervals. Open symbols at *L* > 19 identify data that may be affected by proximity to the magnetopause.



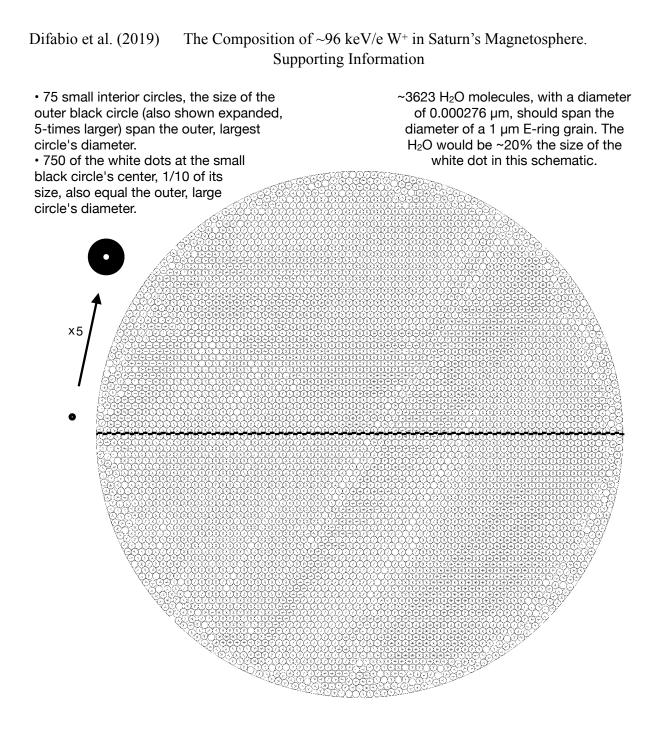


Figure S5. In order to visualize relevant ion-grain cross section scale sizes, we show an example of a large circle packed with 5000 small circles (E. Specht, 2018, The best known packings of equal circles in a circle, http://hydra.nat.uni-magdeburg.de/packing/cci/cci.html#cci5000) to represent a 1 μ m E-ring grain. These interior circles are the same size as the exterior black circle that represents an enlarged version of a H₂O⁺ molecule propagating into the E-ring region. An actual H₂O relative to a 1 μ m E-ring grain is ~20% smaller in this comparison than the white dot size shown. Other E-ring targets are the OH molecular ions and both larger and smaller dust grains, charged both positively and negatively inside ~9 Rs (near the orbit of Rhea).