# Resolving the differences in the simulated and reconstructed climate response to volcanism over the last millennium

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#### Abstract

Explosive volcanism imposes impulse-like radiative forcing on the climate system, providing a natural experiment to study the climate response to perturbation. Previous studies have identified disagreements between paleoclimate reconstructions and climate model simulations (GCMs) with respect to the magnitude and recovery from volcanic cooling, questioning the fidelity of GCMs, reconstructions, or both. Using the paleoenvironmental data assimilation framework of the Last Millennium Reanalysis, this study investigates the causes of the disagreements, using both real and simulated data. We demonstrate that discrepancies since 1600 CE can be largely resolved by assimilating tree-ring density records only, targeting growing-season temperature instead of annual temperature, and performing the comparison at proxy locales. Simulations of eruptions earlier in the last millennium may also reflect uncertainties in forcing and modeled aerosol microphysics.

## Resolving the differences in the simulated and reconstructed temperature response to volcanism

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#### **Key Points:**

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• We explore model–proxy disagreement on the temperature response to volcanic 11 eruptions over the past millennium. 12 • Using paleoclimate data assimilation with both real and synthetic data, we show 13 that this discrepancy is due to four main factors. 14 • Over the past 400 years, agreement is found for tree-ring density records at the 15 places and season these proxies record.

#### Plain Language Summary 17

The response to volcanic eruptions is a critical benchmark of the performance of 18 climate models. Previous studies of the past millennium have identified discrepancies be-19 tween model simulations and climate reconstructions regarding the temperature response 20 to volcanic eruptions, raising concerns regarding the source of this mismatch and impli-21 cations for both models and reconstructions. By evaluating the leading sources of dif-22 ferences between simulations and reconstructions, this study shows that accounting for 23 known factors largely bridges the gap. 24

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#### 25 Abstract

Explosive volcanism imposes impulse-like radiative forcing on the climate system, pro-26 viding a natural experiment to study the climate response to perturbation. Previous stud-27 ies have identified disagreements between paleoclimate reconstructions and climate model 28 simulations (GCMs) with respect to the magnitude and recovery from volcanic cooling, 29 questioning the fidelity of GCMs, reconstructions, or both. Using the paleoenvironmen-30 tal data assimilation framework of the Last Millennium Reanalysis, this study investi-31 gates the causes of the disagreements, using both real and simulated data. We demon-32 strate that discrepancies since 1600 CE can be largely resolved by assimilating tree-ring 33 density records only, targeting growing-season temperature instead of annual temper-34 ature, and performing the comparison at proxy locales. Simulations of eruptions earlier 35 in the last millennium may also reflect uncertainties in forcing and modeled aerosol mi-36 crophysics. 37

#### 38 1 Introduction

Volcanic eruptions influence the climate system through their direct effect on short-39 wave radiation entering the earth system and the subsequent response of major modes 40 of ocean-atmosphere variability (Handler, 1984; Hirono, 1988; Robock, 2000; Adams et 41 al., 2003; Mann et al., 2005; Emile-Geay et al., 2008; Schneider et al., 2009; Li et al., 2013; 42 Stevenson et al., 2016). Eruptions therefore offer unique natural experiments with which 43 to probe the fidelity of climate model simulations, understand the response of the ocean 44 and atmosphere circulation to changes in radiative forcing, assess climate system feed-45 backs, and evaluate solar radiation management proposals (Soden et al., 2002; Timm-46 reck, 2012). The sporadic occurrence of large volcanic eruptions means that developing 47 a deeper understanding of their effect on climate necessarily involves analyzing the re-48 sponse to events prior to the instrumental era. 49

Significant disagreements have been identified between paleoclimate reconstructions 50 of the large-scale temperature response to volcanic eruptions and climate model simu-51 lations (D'Arrigo et al., 2013; Schurer et al., 2013; Stoffel et al., 2015). The IPCC AR5 52 (Masson-Delmotte et al., 2013), which summarized the state of knowledge at the time 53 of publication, highlighted a discrepancy in the intensity and duration of the simulated 54 versus proxy-based reconstructed temperature response to explosive volcanism (Fig. 1b). 55 Coupled Model Intercomparison Project 5 (CMIP5)/Paleoclimate Modeling Intercom-56 parison Project 3 (PMIP3) model simulations for the last millennium experiment (Schmidt 57 et al., 2012a) show more cooling, and for a shorter duration, than paleoclimate recon-58 structions (Briffa et al., 2001; D'Arrigo et al., 2006; Frank, Esper, & Cook, 2007; Moberg 59 et al., 2005). Compounding this uncertainty, the precise timing and location of some vol-60 canic eruptions over the last millennium remain unknown (Sigl et al., 2015; Stevenson 61 et al., 2017) as does the magnitude of the radiative forcing (Timmreck et al., 2009). A 62 critical question is whether this mismatch is an artifact of uncertainties in (1) the pa-63 leoclimate proxy observations, (2) the reconstruction process, (3) the forcing estimates, 64 (4) climate model physics, or (5) a combination thereof (Anchukaitis et al., 2012; Timm-65 reck, 2012; D'Arrigo et al., 2013; LeGrande & Anchukaitis, 2015; Stoffel et al., 2015; Steven-66 son et al., 2016). 67

Here we explore four major sources of uncertainty in reconstructions of surface air 68 temperature over the past millennium: spatial coverage, seasonality, biological memory, 69 and proxy noise. We do so in the context of a paleoenvironmental data assimilation (PDA) 70 framework, the Last Millennium Reanalysis (LMR) (Hakim et al., 2016; Tardif et al., 71 2019), which provides an objective basis for combining information from proxies and mod-72 els. We show here that the discrepancy in Fig. 1b is present in our reconstruction (Fig. 73 1c), but that it can be largely reconciled by accounting for the aforementioned sources 74 of uncertainty. 75

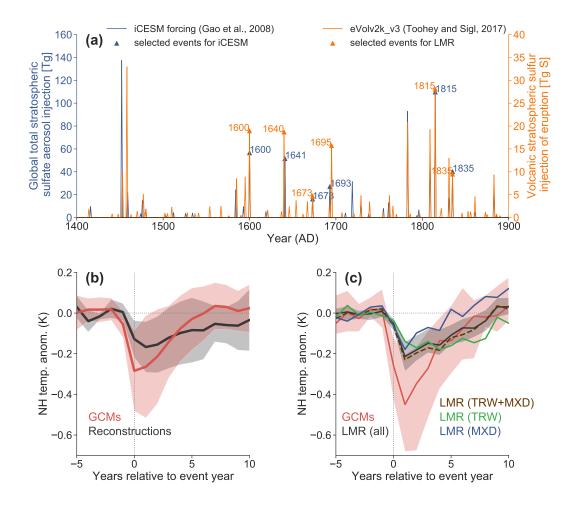


Figure 1. (a) Comparison between the volcanic forcing (Gao et al., 2008) used in the isotopeenabled Community Earth System Model (iCESM) simulation (Stevenson et al., 2019; Brady et al., 2019) and the eVolv2k version 3 Volcanic Stratospheric Sulfur Injection (VSSI) compilation (Toohey & Sigl, 2017). The triangles denote the selected 6 large events between 1400 and 1850 CE. (b) Superposed epoch analysis (SEA) on simulated and reconstructed temperature response to the 12 strongest volcanic eruptions since 1400 AD, reproduced from IPCC AR5 (Masson-Delmotte et al., 2013) Fig. 5.8b. (c) Superposed epoch analysis on annual Northern hemispheric mean temperature (NHMT) simulated by 9 GCMs (Section 2.2, Table S1) and LMR reconstructions assimilating the whole network (solid black curve with shading), the tree-ring network (dashed brown curve), the tree-ring width (TRW) network (solid green curve), and the maximum latewood density (MXD) network (solid blue curve), respectively. The shading encompasses the 5% and 95% quantiles of the ensemble, while the curves indicate the ensemble median (see Text S1 for details about ensemble scheme).

#### <sup>76</sup> 2 Data and methods

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#### 2.1 Paleoclimate data assimilation

We apply the paleoenvironmental data assimilation framework of the Last Millen-78 nium Reanalysis (LMR) (Hakim et al., 2016; Tardif et al., 2019) to both pseudoproxy 79 and real proxy data networks. LMR uses an offline ensemble data assimilation proce-80 dure for multivariate climate field reconstruction (Steiger et al., 2014), where informa-81 tion from a prior expectation of the climate, derived from a climate model, is optimally 82 combined with information from proxy records. The relative weights are determined from 83 the error ratio in these two estimates of the climate, as defined by the update equation 84 in the Kalman filter, which is optimal if the errors are unbiased and normally distributed. 85

The essential components of the procedure are (1) existing climate model data for 86 the prior expectation, which we take from a last millennium simulation from the isotope-87 enabled Community Earth System Model (iCESM) (Stevenson et al., 2019; Brady et al., 88 2019); (2) proxy data networks, which we take from the PAGES 2k phase 2 compilation 89 (PAGES 2k Consortium, 2017, Fig. S1) and the Northern Hemisphere Tree-Ring Net-90 work Development (NTREND) compilation (Wilson, Anchukaitis, Briffa, Büntgen, et 91 al., 2016; Anchukaitis et al., 2017, Fig. S7); and (3) a "forward operator" or proxy sys-92 tem model (PSM), which predicts the proxies given the climate state. Here the forward 93 operator is a linear regression procedure, univariate on annual temperature for corals and 94 ice cores, univariate on seasonal temperature for maximum latewood density records, and 95 bivariate on seasonal temperature and seasonal precipitation for tree-ring width records, 96 as in Tardif et al. (2019). Further details of the LMR data assimilation procedure for pa-97 leoclimate reconstruction may be found in Hakim et al. (2016). 98

This study utilizes a fast implementation of the LMR framework, LMRt (Zhu et al., 99 2019) for computational convenience. As a benchmark, a reconstruction of the spatiotem-100 poral variations of surface temperature over the Common Era is conducted, using iCESM 101 as the model prior and the PAGES 2k network as observations. As expected, the DA 102 procedure yields a substantially better estimate of the temporal variability in the tem-103 perature field than the prior, as quantified by the pointwise correlation with an indepen-104 dent instrumental temperature field (see Section 2.2 below) (Fig. S2c, S2d). This recon-105 struction skill level is comparable to a previous implementation of LMR (Tardif et al., 106 2019), and supported by the similarity between the reconstructed NHMT using both ver-107 sions of the code (Fig. S2a). For a more in-depth evaluation of the LMR framework, see 108 Tardif et al. (2019). 109

To assess the impact of the choice of prior and enable comparison with the LMR version of record (Tardif et al., 2019), we also tested assimilation using the CCSM4 simulation of Landrum et al. (2012) as the model prior. We find virtually identical results, with no significant difference detected in the temperature response to volcanic eruptions after 1400 AD (compare Fig. S2a to Fig. S2b, Fig. 1c to Fig. S14a, and Fig. 4a to Fig. S14b).

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#### 2.2 Simulated and instrumental temperature observations

In order to compare paleoclimate reconstructions to climate models, we consider simulations of past millennium climate from the following models: iCESM and CESM1 (Otto-Bliesner et al., 2015), as well as the PMIP3 models (Schmidt et al., 2012b; Braconnot et al., 2012), including BCC CSM1.1 (Wu et al., 2014), GISS-E2-R (Schmidt et al., 2006), HadCM3 (Gordon et al., 2000), IPSL-CM5A-LR (Dufresne et al., 2013), MIROC-ESM (Watanabe et al., 2011), MPI-ESM-P (Giorgetta et al., 2013), CSIRO (Rotstayn et al., 2012), and CCSM4, as listed in Table S1. We also use two sets of instrumental temperature observations, including the Berkeley Earth instrumental temperature analysis (Rohde et al., 2013) and the Goddard Institute for Space Studies (GISS) Surface Temperature Analysis (GISTEMP) (Hansen et al., 2010). GISTEMP and the gridded precipitation dataset (V6) from the Global Precipitation Climatology Centre (GPCC) (Schneider et al., 2014) are also used for PSM calibration in the bivariate framework of Tardif et al. (2019).

#### <sup>130</sup> 2.3 Superposed epoch analysis (SEA)

Superposed epoch analysis (SEA) (Haurwitz & Brier, 1981) is a frequently used 131 technique to assess the temperature response to volcanic eruptions (Adams et al., 2003; 132 Masson-Delmotte et al., 2013; Rao et al., 2019). It consists of aligning temperature anomaly 133 series to the timing of volcanic eruptions within a fixed time window prior to and fol-134 lowing the event, and averaging these responses to estimate the typical response to erup-135 tions. The IPCC AR5 (Fig. 1b) considered the reconstructed temperature response to 136 the 12 strongest eruptions since 1400 AD. Based on the temporal coverage of available 137 proxies and model simulations, as well as the scientific knowledge of the eruptions, we 138 selected a smaller set of 6 large and well-dated eruption events over the years 1600-1850 139 CE that are consistent in timing in both the volcanic forcing used in iCESM (Gao et al., 140 2008) and the most recent compilation of Volcanic Stratospheric Sulfur Injection (VSSI) 141 (Toohey & Sigl, 2017) (Fig. 1a). For further details about the selection, see Text S3. The 142 LMR response to individual events of the entire millennium is shown in Fig. S10-S12. 143

#### <sup>144</sup> 3 The discrepancy and its causes

Fig. 1b highlights discrepancies between model simulations and reconstructions in 145 three aspects: (1) the magnitude of the peak cooling (2) the timing of the peak cooling 146 (3) the length of the recovery. Specifically, model simulations show a stronger peak cool-147 ing amplitude, a slightly earlier peak cooling, and a shorter recovery interval than the 148 reconstructions. A similar discrepancy pattern can be seen when comparing the LMR 149 reconstruction assimilating the PAGES 2k network to the model simulations (Fig. 1c). 150 Comparing results for solutions assimilating the entire PAGES 2k network [LMR (all), 151 solid dark gray curve] to those assimilating only its tree-ring records [LMR (TRW+MXD), 152 dashed brown curve, we see that most of the reconstructed volcanic cooling originates 153 from the information captured by the tree-ring network. The latter consists of two main 154 observation types: (1) tree-ring width (TRW) and (2) maximum latewood density (MXD). 155 Assimilating these two proxy types separately, however, shows different responses to vol-156 canism: TRW yields a lagged peak cooling year and a more prolonged recovery than MXD. 157 This suggests that the difference between these two proxy types is key to understand-158 ing the different volcanic cooling patterns in reconstructions. 159

Previous studies (Timmreck et al., 2009; Timmreck, 2012; LeGrande & Anchukaitis, 160 2015; Stoffel et al., 2015; LeGrande et al., 2016) have investigated the components of the 161 PMIP3 models that could potentially result in overestimated cooling in simulations. Here, 162 with a focus on proxies and reconstructions, we investigate four factors that we hypoth-163 esize may account for these differences, motivated by prior studies and existing knowl-164 edge of the tree-ring proxy network: (1) spatial coverage (Anchukaitis et al., 2012; D'Arrigo 165 et al., 2013) (2) seasonality (D'Arrigo et al., 2006; Stoffel et al., 2015; Anchukaitis et al., 166 2017) (3) biological memory (Fritts, 1966; Krakauer & Randerson, 2003; Frank, Bünt-167 gen, et al., 2007; Esper et al., 2015; Stoffel et al., 2015; Zhang et al., 2015; Lücke et al., 168 2019), and (4) non-temperature 'noise' (von Storch et al., 2004; Riedwyl et al., 2009; Neukom 169 et al., 2018). 170

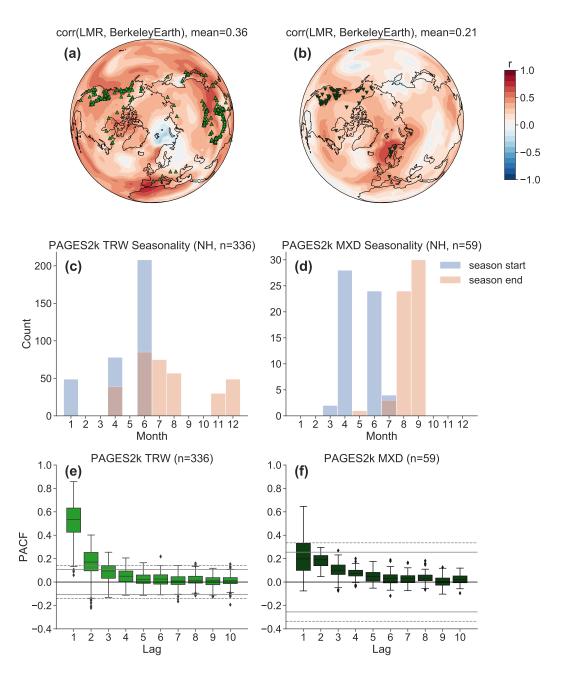


Figure 2. Differences between PAGES 2k TRW and MXD records regarding (a, b) spatial coverage, (c, d) seasonality detected by the algorithm used in Tardif et al. (2019), and (e, f) biological memory quantified by the partial autocorrelation function (PACF). (a) The spatial coverage of TRW network. (c) The optimal seasonality of the TRW network. (e) The PACF of the TRW network. (b), (d), and (f) are are as (a), (b), and (e), respectively, but for the MXD network. The color contours in (a, b) indicate the correlation between the LMR reconstructions and the Berkeley Earth instrumental temperature analysis (Rohde et al., 2013).

#### <sup>171</sup> **3.1 Spatial coverage**

The PAGES 2k network is comprised of 336 TRW records and 59 MXD records 172 over the Northern Hemisphere (NH). MXD records in PAGES2k are mainly limited to 173 North America and Scandinavia, while the TRW records cover both North America and 174 Asia. Evaluating the correlation between the LMR reconstruction and the Berkeley Earth 175 instrumental temperature analysis (Rohde et al., 2013) over the instrumental era over 176 1880–2000, we see that assimilating the TRW network yields a greater improvement over 177 the model prior than assimilating the MXD network (Fig 2a, 2b). Is this difference due 178 to the location or the quantity of each type of proxy record? To investigate this ques-179 tion, we use a pseudoproxy experiment (PPE) (Smerdon, 2011). We set the annual iCESM 180 simulated temperature as our truth, and use it as model prior in the DA framework (a 181 "perfect model" scenario). Pseudoproxies are defined as perfect temperature recorders 182 at three sets of locations: (1) the locales of all the 336 NH PAGES 2k TRW records (2) 183 the locales of randomly picked 50 PAGES 2k TRW records over North America and (3) 184 the locales of randomly picked 50 PAGES 2k TRW records over the NH. 185

The result of assimilating these three pseudoproxy networks is shown in Fig. S3 186 (a, b, and c), showing that better spatial coverage yields a more accurate reconstruction 187 in the PDA framework, with all other things being equal. This is reflected in SEA as well: 188 Fig. 3a shows that assimilating 50 records spread throughout the NH yields a stronger 189 and more accurate peak cooling amplitude than assimilating 50 records concentrated over 190 North America, suggesting that broad spatial coverage is more important than the sheer 191 number of records for resolving peak cooling amplitude. Location does matter to some 192 degree with regard to the large-scale teleconnection patterns, and optimal placement could 193 be determined with the approach of Comboul et al. (2015), yet this is beyond the scope 194 of this investigation. 195

#### 3.2 Seasonality

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An implicit assumption in reconstructing annual temperature with tree-ring prox-197 ies is that growing season temperature is representative of annual temperature (PAGES) 198 2k Consortium, 2017). However, the correlation between summer and annual temper-199 atures in the Northern Hemisphere is high for the oceans but relatively low over conti-200 nents (Fig. S3f), where the tree-ring records are located. Trees register climate primar-201 ily during their growing season, which varies as a function of geography, species, and cli-202 mate (Fritts, 1966; St. George, 2014; St George & Ault, 2014; Wilson, Anchukaitis, Briffa, 203 Büntgen, et al., 2016; Stoffel et al., 2015). Though the PAGES 2k metadata contain some 204 information about the seasonal sensitivity of all proxies, we follow Tardif et al. (2019) 205 and identify optimal seasonal windows of temperature and precipitation for each proxy 206 record from a pool of pre-defined seasonal windows. The windows are optimal in a least 207 square sense, using calibration over the historical period. The start and end month of 208 the growing season (based on temperature) thus identified are shown in Fig. 2c, 2d. While 209 in the Northern Hemisphere both TRW and MXD proxies record largely boreal summer 210 conditions, the optimal seasonality for TRW is often broader but typically less consis-211 tent than that for MXD. 212

As before, we use a PPE to investigate the impact of growth seasonality on the tem-213 perature reconstruction. We generate pseudo-PAGES2k TRW records at their real lo-214 cations as perfect recorders of local summer (JJA) temperature and perform experiments 215 targeting both JJA temperature and annual temperature. As expected, a much better 216 reconstruction is obtained for the boreal summer temperature field than annual temper-217 ature (Fig. S3d, S3e). This is also evident in reconstructions using real proxies and in-218 strumental temperature (Fig. S4). Therefore, summer-sensitive trees can only reconstruct 219 annual temperature to the extent that the summer and annual mean are correlated. While 220

such seasonal effects result in quite different assessments of reconstruction fidelity, this
 difference is hardly noticeable in SEA (Fig. 3b).

#### 3.3 Biological memory

Another important difference between TRW and MXD is biological memory, whereby 224 tree growth reflects the influence of climate in previous years (Fritts, 1966; Krakauer & 225 Randerson, 2003; Frank, Büntgen, et al., 2007; Esper et al., 2015; Zhang et al., 2015; Stof-226 fel et al., 2015). We quantify the persistence in TRW and MXD in the PAGES2k using 227 the partial autocorrelation function (PACF) (Fig. 2e, 2f). As expected (Breitenmoser 228 et al., 2012; Esper et al., 2015; Lücke et al., 2019), we find that biological memory in TRW 229 across the PAGES2k network is large and significant for lag-1 and lag-2, while for MXD 230 it is limited. Comparing the proxy composites and the corresponding average instrumen-231 tal temperature at proxy locales, we see that the MXD composite captures contempo-232 raneous temperature variations, including the accurate timing of cooling events, while 233 the TRW composite appears to smooth interannual variability and integrate tempera-234 tures over 2 to 5 years (Fig. S5a, S5b), leading to lagged and persistent cooling events 235 (Frank, Büntgen, et al., 2007). 236

To investigate the impact of such biological memory on the magnitude of recon-237 structed volcanic cooling, we again turn to PPEs. We simulate a short-term memory ef-238 fect in TRW by designing pseudoproxies as a 5-yr moving average of the annual temper-239 ature simulated by iCESM, as shown in Fig. S5c. Assimilating these smoothed pseudo-240 proxies yields a prolonged temperature recovery and a peak cooling that is both damped 241 and lagged (Fig. 3c, the solid light green curve). We find that this overall result is not 242 sensitive to the precise design of the filter used to construct the smoothed pseudoprox-243 ies, so long as it captures this multiple year climate integration in some way. The po-244 tential additional influence of soil moisture is not directly modeled here, as these lagged 245 relationship are observed in temperature-sensitive TRW chronologies irrespective of the 246 potential additional influence of soil moisture (Franke et al., 2013; Consortium, 2017), 247 which we confirm in sensitivity experiments (Fig. S15). 248

#### 3.4 Proxy system noise

So far, our PPEs have employed noiseless temperature recorders for simplicity (a 250 signal-to-noise ratio (SNR) of infinity, wherein SNR is defined as the ratio of the stan-251 dard deviation of signal and that of noise, following existing practice (Smerdon, 2011)). 252 In reality, of course, proxies are imperfect recorders of climate conditions. To make the 253 PPEs more realistic, we now add uncorrelated Gaussian white noise to the previously 254 described pseudo-PAGES2k TRW records. Using a linear regression procedure, we es-255 timate a SNR around 0.3 (Fig. S6), which is comparable to the estimate of Wang et al. 256 (2014). Since we have already emulated the biological memory utilizing the moving av-257 erage filter, we consider white noise instead of red noise to avoid adding more memory 258 into the pseudoproxies. The addition of noise to the previous case yields a more simi-259 lar SEA pattern (Fig. 3c, solid dark green curve) to the real-world case (Fig. 1c, solid 260 green curve): a more damped and prolonged recovery compared to the noiseless case. 261

Considering the four factors above, we are thus able to simulate the observed discrepancy between modeled and reconstructed NH temperature response to volcanic eruptions. Can this knowledge be used to minimize this discrepancy?

**3.5 Reconciling the discrepancy** 

In the present context, noise reflects any non-temperature influence on the proxy
 systems, including other climate influences like soil moisture, or biophysical processes
 that cannot be adequately modeled due due to insufficient scientific knowledge, limited

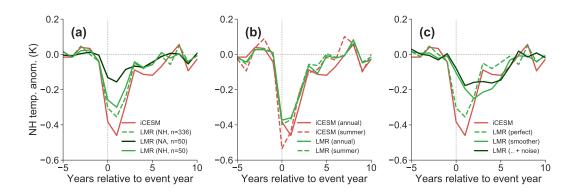


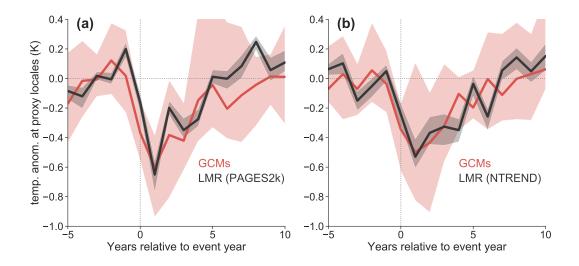
Figure 3. SEA in pseudoproxy experiments, evaluating the impact of (a) spatial coverage, (b) seasonality, and (c) biological memory and noise. (a) the red curve denotes the target, and the dashed light green curve, the solid dark green curve, and the solid light green curve indicate the LMR reconstruction assimilating 336 pseudo-PAGES2k TRW records over the NH, 50 records over North America, and 50 records over the NH, respectively. (b) The solid red curve denotes the annual target, the dashed red curve denotes the boreal summer target, and the green curves indicate the LMR annual and summer reconstructions assimilating the pseudo-PAGES2k TRW network, respectively. (c) The solid red curve denotes the annual target, and the green curves denote the LMR reconstruction assimilating pseudo-PAGES2k TRW as perfect temperature recorders (dashed), and temperature smoothers (solid). The case of smoothed temperature with added Gaussian noise (SNR=0.3) is in dark green. All the reconstruction curves refer to the ensemble median (see Text S1 for details about the ensemble design).

input data, or both. The first three factors can, however, be corrected: to account for 269 the limited spatial coverage, we perform SEA at proxy locations instead of the whole NH; 270 to minimize the seasonal bias, we target boreal summer temperature instead of annual 271 temperature; and to mitigate memory effects, we assimilate MXD records only, leaving 272 out TRW and mixed chronologies. As a result, we are able to almost entirely account 273 for the proxy-model discrepancy in Fig. 1 with the PAGES 2k network (Fig. 4a, Fig S11). 274 The same strategy can be used for other proxy networks. For comparison, applying it 275 to the NTREND network (Wilson, Anchukaitis, Briffa, Büntgen, et al., 2016; Anchukaitis 276 et al., 2017) (Fig. S7) yields similar agreement between simulated and reconstructed tem-277 perature (Fig. 4b, Fig S12). These results stand in sharp contrast to results where spa-278 tial coverage, seasonality, and biological memory are not taken into account (Fig. S8). 279

That the discrepancy in Fig. 1b can be largely reconciled by accounting for known characteristics of the proxy data is reassuring, and bodes well for using volcanic eruptions of the past millennium as a test bed for climate models. We now discuss the broader implications of this result.

#### <sup>284</sup> 4 Discussion

Using recent proxy compilations and climate field reconstruction techniques, we have demonstrated that it is possible to largely resolve the discrepancy between the simulated and reconstructed temperature response to explosive volcanism since 1600 CE. We find that this gap was the result of four main factors: spatial coverage, proxy seasonality, biological memory, and proxy noise. While proxy noise is difficult to account for in modeldata intercomparisons, the first three factors can be, if care is taken in evaluating comparable quantities. In particular, since our reconstructions are more reliable at locations



**Figure 4.** (a) Same as Fig. 1c, after resolving differences in the model and proxy domains associated with seasonality, spatial distribution, and biological memory. (b) Same as (a) but using the NTREND MXD network. A version of this figure showing each model simulation is available in Fig. S9, and one using more eruption events is available in Fig. S13

where proxies are available than at distal locations (Anchukaitis et al., 2017), carrying 292 out the comparison at proxy sites is a simple and effective way to reduce the mismatch. 293 That this is also true in the data assimilation framework (Steiger et al., 2014) suggests 294 that expanding the spatial extent of proxy network is necessary to resolve global-scale 295 patterns. For very large eruptions such as the 1257 Samalas eruption, the 1450s erup-296 tions, and the 1815 Tambora eruption, however, significant mismatches remain between 297 model simulations and reconstructions even when these factors are accounted for (Fig. 298 S11, S12). While this has little impact in a composite over all events (Fig. S13), it war-299 rants discussion. 300

Previous work and our own analysis suggests three major causes: (1) proxy attrition, (2) aerosol microphysics in models, and (3) uncertainties in volcanic forcing.

(1) In the absence of reliable proxy data, offline data assimilation reverts to the model prior for its estimate of climate. This results in generally damped variations in periods of reduced and/or noisy coverage, as seen by comparing the first to second millennium CE in Fig S2a, S2b. Here we have mitigated this problem by focusing on the recent period with relatively high proxy coverage, but it is undoubtedly an ingredient in the mismatch observed for earlier eruptions like Samalas, when relative few proxies are available, especially MXD records (Fig. S1b and S16a).

(2) Some CMIP5-era GCMs produce overly strong responses to volcanic forcing due 310 to unrealistic representation of aerosol microphysics (Timmreck et al., 2009; Timmreck, 311 2012; Stoffel et al., 2015; LeGrande et al., 2016). Both Timmreck et al. (2009) and Stoffel 312 et al. (2015) suggest that the discrepancy is caused by the simplistic assumption used 313 in PMIP3 models that aerosol optical depth is linearly scaled to ice-core sulfate concen-314 tration. This assumption uses the 1991 Pinatubo eruption as the reference, and is is un-315 likely to be valid for many significantly larger eruptions. As shown by Stoffel et al. (2015), 316 accounting explicitly for self-limiting aerosol microphysical processes can reconcile this 317 discrepancy, an idea later confirmed by Guillet et al. (2017) with both documentary and 318 tree-ring data. 319

(3) Many PMIP3 models used the Gao et al. (2008) forcing dataset, where the re-320 constructed Samalas accorsol loading was exceedingly large, and has since been revised 321 downward (Jungclaus et al., 2017). There is also lingering uncertainty as to the mag-322 nitude, timing, and location of two major events during the 1450s (Sigl et al., 2015; Toohey 323 & Sigl, 2017; Hartman et al., 2019). Besides, apparent cooling from a 1761 eruption in 324 some model simulations is actually the result of the misalignment of the 1783 forcing in 325 the uncorrected version of the Gao et al. (2008) forcing (Stevenson et al., 2017). Regard-326 less of changes in physics, the revision in volcanic forcing alone would help to reduce the 327 discrepancy. 328

Progress in representing volcanic forcing (Toohey & Sigl, 2017; Aubry et al., 2019), 329 as well as improvements in model resolution and processes (e.g. active stratospheric chem-330 istry) in PMIP4 (Kageyama et al., 2018) may lead to closer model-data matches in fu-331 ture work. Regardless of these factors, our analysis suggests that a critical ingredient of 332 minimizing the model-reconstruction mismatch is to evaluate simulated temperature at 333 the times and places where it is recorded by the proxy sensors (Anchukaitis et al., 2012). 334 Naturally, past temperature estimates may be improved as well. While this study has 335 focused on the uncertainties in proxy measurements in the context of paleoenvironmen-336 tal data assimilation, more work should be done to reduce sources of uncertainty within 337 the data assimilation method itself, such as the forward operator error, the model prior, 338 and the localization scheme, as the coupling of all these uncertainty sources can poten-339 tially affect the SEA comparison. In particular, forward operators that allow for non-340 contemporaneous influences of the state on the proxies [e.g. time-integration, as is be-341 lieved to be the case for TRW (Fritts et al., 1991; Vaganov et al., 2006)] would enable 342 us to make better use of the information contained in TRW records. While such process-343 oriented models have been developed (Tolwinski-Ward et al., 2011; Evans et al., 2013), 344 their application to the DA context is contingent upon accurate specification of obser-345 vation error variance and correcting for biases in the model prior. Both tasks remain ac-346 tive research areas (Dee et al., 2016). 347

With regard to proxies, we have confirmed that the lagged cooling exhibited in pre-348 vious reconstructions can be explained as the consequence of their using TRW records. 349 Other proxies that integrate climate information over multiple years (e.g. bioturbated 350 sediments) likely have a similar impact in multiproxy reconstructions. Since MXD records 351 are more faithful paleo-temperature sensors than TRW records (Esper et al., 2015, 2018), 352 we join others in calling for increased collection and development of MXD records (Anchukaitis 353 et al., 2017; St. George & Esper, 2019), particularly at locations where they are presently 354 absent or cover only part of the last millennium, e.g. the North American treeline and 355 at high elevations in Asia (Anchukaitis et al., 2017; Esper et al., 2018). 356

While our approach reconciles the discrepancy between model and proxy estimates of the surface temperature to moderate eruptions of the last 400 years, important differences remain for large events like Tambora or Samalas. For such eruptions, improved estimates of the forcing, a more realistic model representation of aerosol microphysics, and – for events sparsely sampled by existing proxy network – an expanded proxy coverage may be necessary resolve extant differences. Future work will help elucidate the relative role of these three factors on this particular comparison.

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<sup>369</sup> fzhu2e/lmrvolc (a placeholder for now, to be filled upon paper acceptance).

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## Supporting Information for "Resolving the differences in the simulated and reconstructed temperature response to volcanism"

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### Contents of this file

1. Text S1: Settings of the LMR framework

2. Text S2: Reconstructions using the Northern Hemisphere Tree-Ring Network De-

velopment (NTREND) network

- 3. Text S3: Choice of eruption key dates
- 4. Text S4: Software

X - 2

5. Figure S1: Data from the PAGES 2k network (PAGES 2k Consortium, 2017) assimilated in LMR.

6. Figure S2: Comparison between different LMR implementations, and between model prior and reconstruction.

7. Figure S3: The pseudoproxy experiments (PPEs) that indicate the impact of spatial coverage and seasonality on the correlation between reconstruction and the pseudo-truth.

8. Figure S4: Impact of seasonality on the correlation between reconstruction and the Berkeley Earth instrumental temperature analysis.

9. Figure S5: Correlation between instrumental seasonal temperature observations and real proxy and pseudoproxy composites.

10. Figure S6: The detected signal-to-noise ratio (SNR) in PAGES2k TRW and MXD records.

11. Figure S7: The Northern Hemisphere Tree-Ring Network Development (NTREND) network.

12. Figure S8: The comparison between the model simulated temperature response and the LMR reconstruction assimilating the whole NTREND network.

13. Figure S9: Superposed Epoch Analysis (SEA) of model simulations and LMR reconstructions of the selected 6 eruption events, with individual simulation plotted out.

14. Figure S10: The temperature response to individual eruptions in LMR reconstructions assimilating the whole PAGES 2k Network and GCM simulations, targeting NHMT. 15. Figure S11: The temperature response to individual eruptions in LMR reconstructions assimilating the PAGES 2k MXD Network and GCM simulations, targeting mean summer temperature at proxy locales.

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16. Figure S12: The temperature response to individual eruptions in LMR reconstructions assimilating the NTREND MXD Network and GCM simulations, targeting mean summer temperature at proxy locales.

17. Figure S13: Superposed Epoch Analysis (SEA) of model simulations and LMR reconstructions of all eruption events listed in Fig. S10.

18. Figure S14: Superposed Epoch Analysis (SEA) of model simulations and LMR reconstructions using CCSM4 as prior.

19. Figure S15: The comparison of the LMR reconstructions using univariate and bivariate forward operator for TRW records.

20. Figure S16: The available PAGES 2k records with start year earlier than 1257 AD, as well as the age of each of the PAGES 2k record.

21. Table S1: Last millennium model simulations considered in this study.

#### Introduction

This supporting information provides supplementary figures cited in the main text, as well as detailed information about the real- and pseudo-proxy reconstructions mentioned in the main text. Text S1 details the settings of our LMR experiments. Text S2 describes the reconstruction experiment using the Northern Hemisphere Tree-Ring Network Development (NTREND) (Wilson et al., 2016; Anchukaitis et al., 2017). Text S3 justifies the choice of eruption key dates. Software tools used for the analysis in this study are acknowledged in Text S4.

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#### Text S1: Settings of the LMR framework

The reconstruction experiments in this study follow the general settings:

• Model prior: the isotope-enabled Community Earth System Model (iCESM) simulation (Stevenson et al., 2019; Brady et al., 2019) is used as the model prior. We have also tested using the CCSM4 last millennium simulation (Landrum et al., 2012) as model prior (Fig. S2a, S14) and no significant difference is detected in the temperature response to volcanic eruptions after 1400 AD.

• Ensemble design: 50 Monte Carlo iterations, each using a different randomly chosen 100-member ensemble states from the model prior, and 75% of randomly chosen available proxy records for assimilation (25% for independent verification). This scheme was chosen and explained in Hakim et al. (2016) to balance the needs of accuracy and uncertainty quantification.

• Localization scheme: the Gaspari-Cohn localization function (Gaspari & Cohn, 1999) is used with a radius of 25,000 km (Tardif et al., 2019).

• Forward operator: As in Tardif et al. (2019), we use seasonal bivariate (temperature and moisture) linear regression for tree-ring width (TRW) records, seasonal univariate (temperature) linear regression for maximum latewood density (MXD) records, and annual univariate (temperature) linear regression for all other proxy types as the forward operator in real proxy experiments. The forward operator is calibrated against the Goddard Institute for Space Studies (GISS) Surface Temperature Analysis (GISTEMP) (Hansen et al., 2010) instrumental observation and the gridded precipitation dataset from the Global Precipitation Climatology Centre (GPCC) (Schneider et al., 2014) over the timespan 1850-2015. In pseudoproxy experiments (PPE) the forward operator changes according to the experiment (see main text), and is calibrated against the model's true state over the same interval.

## Text S2: Reconstructions using the Northern Hemisphere Tree-Ring Network Development (NTREND) network

The Northern Hemisphere Tree-Ring Network Development (NTREND) (Wilson et al., 2016; Anchukaitis et al., 2017) consists of 54 tree-ring chronologies spanning parts of North America and Eurasia. Of those 54 chronologies, 18 are pure maximum latewood density (MXD), 13 are pure tree-ring width (TRW), and 23 are mixed composites of MXD and TRW. The spatiotemporal sampling is shown in Fig. S7a, S7b.

As a benchmark, we first assimilate the whole NTREND network using the expertcurated seasonality, and the superposed epoch analysis (SEA) shows a similar discrepancy pattern as in IPCC AR5 Fig. 5.8b (Masson-Delmotte et al., 2013) (Fig. S8).

Applying our strategy for gap-bridging described in the main text, we assimilate only the 18 pure MXD records, and reconstruct the boreal summer temperature field, and then perform SEA at proxy locales. The result is shown in Fig. 4b (main text), which shows a better agreement between model simulations and the LMR reconstruction. Note that since 18 records are very few, we assimilate all the records in each ensemble member of assimilation, yield quite narrow uncertainty bands.

Text S3: Choice of eruption key dates Because superposed epoch analysis is an averaging operation, it involves a tradeoff between, on the one hand, maximizing the number of eruption key dates to reduce uncertainties, and on the other hand considerations particular to each eruption.

We chose to exclude eruptions after 1850 because the PMIP3 past1000 protocol covers only the period (850-1850), and we wanted to be able to compare the greatest number of simulations to reconstructions.

When a cluster of eruptions are close to each other within 10 yrs, we select only the last one to avoid conflating the response of one eruption within the recovery for a preceding event. Note that not all PMIP3 simulations use the same volcanic forcing dataset (Schmidt et al., 2012), and that all differ from the more recent estimates of (Toohey & Sigl, 2017), which is a source of differences between simulations, and between simulations and reconstructions. Also note that neither 1452 nor 1459 (formerly attributed to

X - 6

the Kuwae caldera) is selected. According to Toohey and Sigl (2017), the 1452 event in Gao, Robock, and Ammann (2008) was misaligned and is actually the 1459 event, so one should select the 1452 event instead of the 1459 event for GCM simulations. However, considering that the 1452 event is close to the 1459 event, we chose to skip both to avoid introducing an obvious discrepancy source for the comparison between GCM simulations and LMR reconstructions. Additionally, the 1761 and 1783 events are also skipped due to issue of misalignment according to Stevenson, Fasullo, Otto-Bliesner, Tomas, and Gao (2017) and Lücke, Hegerl, Schurer, and Wilson (2019).

#### Text S4: Software

All the analysis in this study was performed in the open-source Python programming language (Van Rossum & Drake Jr, 1995), version 3.7, with the following packages:

- numpy (van der Walt et al., 2011)
- scipy (Virtanen et al., 2019)
- pandas (McKinney, 2010)
- statsmodels (Seabold & Perktold, 2010)
- matplotlib (Hunter, 2007)
- seaborn (Waskom et al., 2018)

All reconstructions were performed with the Last Millennium Reanalysis fast implementation (LMRt), of Zhu, Emile-Geay, Hakim, Tardif, and Perkins (2019). This implementation yields nearly identical results compared to the official reconstruction (Fig. S2a), but with additional features:

- Greater flexibility
  - Easy installation
  - Easy importing and usage in Jupyter notebooks
  - Easy setup for different priors, proxies, and Proxy System Models (PSMs)

- Faster speed
  - Much faster PSM calibration due to optimization of algorithm
  - Easy parallel computing with multiprocessing and other techniques
- More modular code structure

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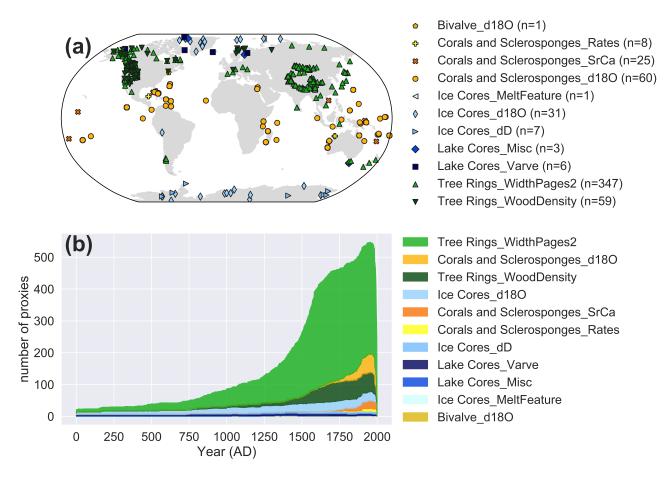


Figure S1. Data from the PAGES 2k network (PAGES 2k Consortium, 2017) assimilated in LMR. (a) Spatial coverage by archive type. (b) Temporal availability by archive type.

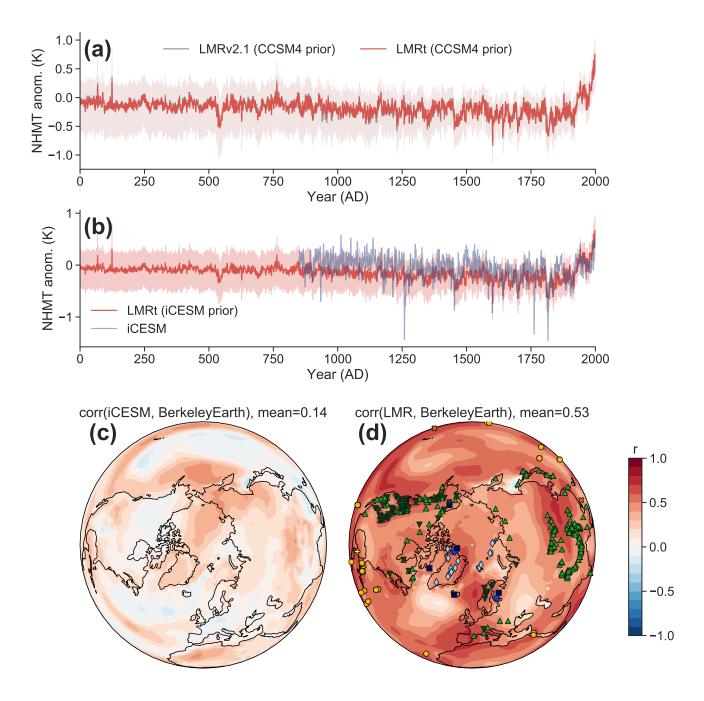


Figure S2. (a) The reconstructed northern hemisphere mean temperature (NHMT) series using the official LMR implementation (Tardif et al., 2019) and the lightweight implementation used in our study LMRt (Zhu et al., 2019), using the same CCSM4 model prior (Landrum et al., 2012) and the PAGES 2k phase 2 dataset (PAGES 2k Consortium, 2017). (b) The LMR reconstructed NHMT series assimilating the PAGES 2k network, along with its model prior, the simulated NHMT series from the isotope-enabled Community Earth System Model (iCESM) (Stevenson et al., 2019; Brady et al., 2019). (c) The correlation between the surface temperature simulated by iCESM and the instrumental observation Berkeley Earth instrumental temperature analysis (Rohde et al., 2013) over 1880 to 2000. (d) Same as (b) but for LMR reconstruction assimilating the PAGES 2k network. The symbols follow that in Fig. S1.

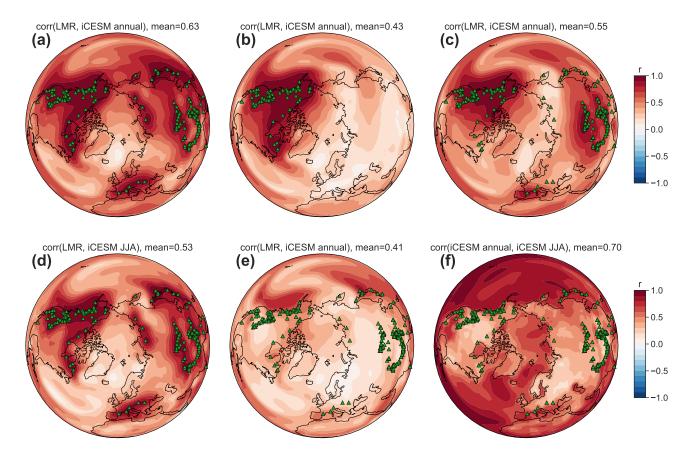


Figure S3. The pseudoproxy experiments (PPEs) that indicate the impact of spatial coverage and seasonality on the correlation between reconstruction and the pseudotruth. (a) The pseudoproxies are generated as perfect temperature recorders of the annual temperature simulated by iCESM, and the whole network is assimilated. (b) Same as (a), but only 50 records over North America (NA) region are assimilated. (c) Same as (a), but only 50 records over North emperature recorders of the summer temperature simulated by iCESM, and summer temperature recorders of the summer temperature simulated by iCESM, and summer temperature field is reconstructed. (e) Same as (d), but annual temperature field is reconstructed. (f) The correlation between annual temperature and summer temperature simulated by iCESM.

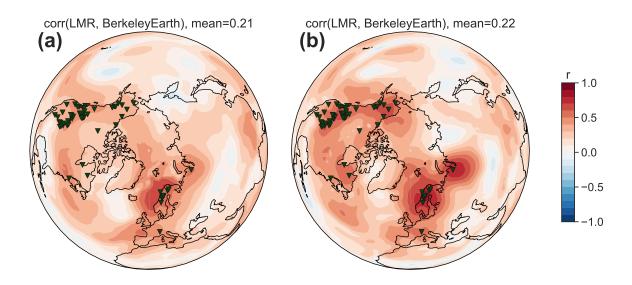
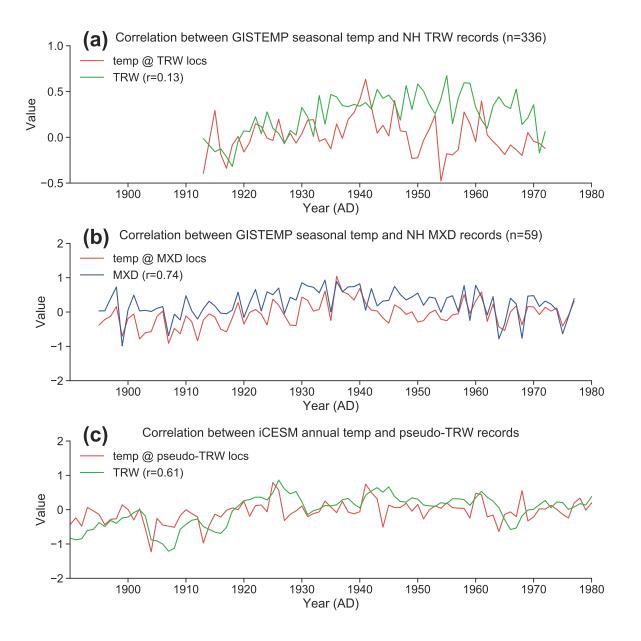


Figure S4. Impact of seasonality on the correlation between the reconstructions assimilating the MXD network and the Berkeley Earth instrumental temperature analysis (Rohde et al., 2013). (a) Reconstructing annual temperature (b) Reconstructing summer temperature. Note that both experiments use real, not pseudo, proxies.

Model Experiment ID iCESM (Stevenson et al., 2019; Brady et al., 2019) \_ b.e11.BLMTRC5CN.f19\_g16.001 CESM1 (Otto-Bliesner et al., 2015) BCC CSM1.1 (Wu et al., 2014) past1000\_r1i1p1 GISS-E2-R (Schmidt et al., 2006) past1000\_r1i1p1 HadCM3 (Gordon et al., 2000) past1000\_r1i1p1 IPSL-CM5A-LR (Dufresne et al., 2013) past1000\_r1i1p1 MIROC-ESM (Watanabe et al., 2011) past1000 r1i1p1 MPI-ESM-P (Giorgetta et al., 2013) past1000 r1i1p1 CSIRO (Rotstayn et al., 2012) past1000\_r1i1p1 CCSM4 (Landrum et al., 2012) past1000\_r1i1p1

Table S1. Last millennium model simulations considered in this study

X - 18



**Figure S5.** (a) The NH TRW composites compared to the seasonal observational temperature, the Goddard Institute for Space Studies (GISS) Surface Temperature Analysis (GISTEMP) (Hansen et al., 2010), at proxy locales. (b) Same as (a), but for MXD. (c) The composite of the pseudoproxy that is generated as temperature smoother with a 5-yr moving average filter, compared to the iCESM simulated temperature at the proxy locales.

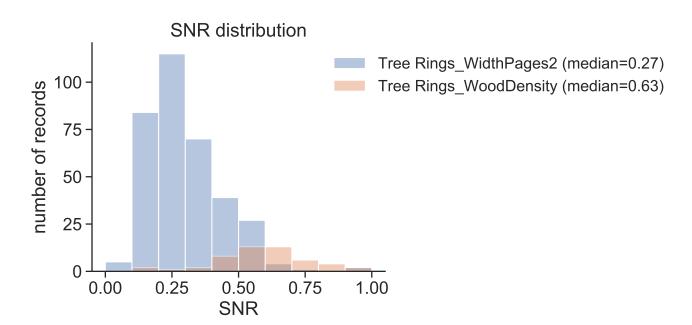
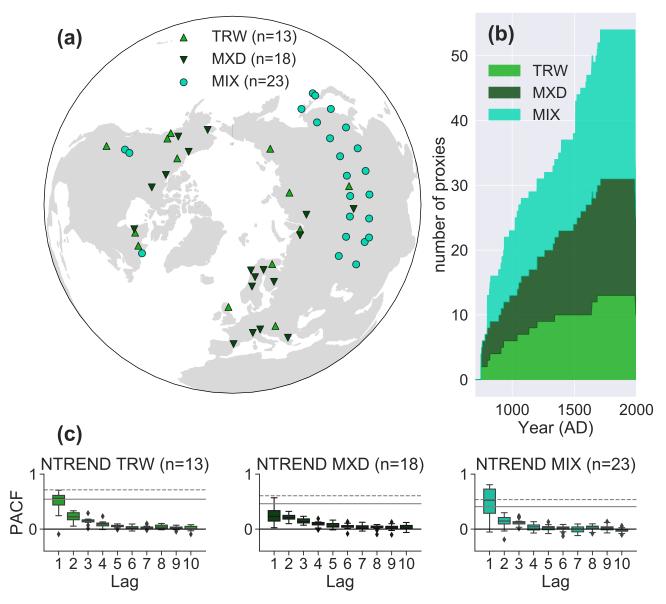


Figure S6. The signal-to-noise ratio (SNR) in TRW (Tree Rings\_WidthPages2) and MXD (Tree Rings\_WoodDensity) records detected by the forward operator calibration procedure (see Text S1 for details) that follows (Tardif et al., 2019) in LMR, with curated pre-defined seasonal windows. Higher SNR indicates more fraction of signal can be explained by seasonal temperature and moisture via bivariate and univariate linear regression.





**Figure S7.** The Northern Hemisphere Tree-Ring Network Development (NTREND) (Wilson et al., 2016; Anchukaitis et al., 2017). (a) The spatial coverage of each proxy type. (b) The temporal availability of each proxy type. (c) The partial autocorrelation function (PACF) up to lag-10 for each proxy type.

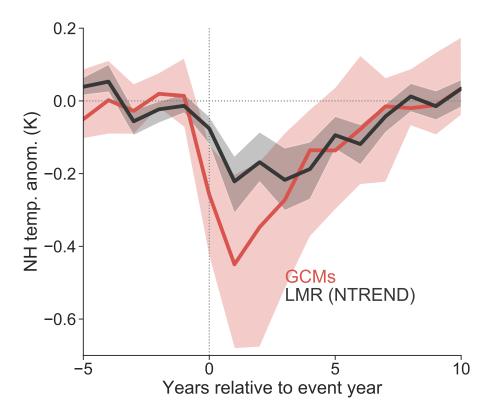
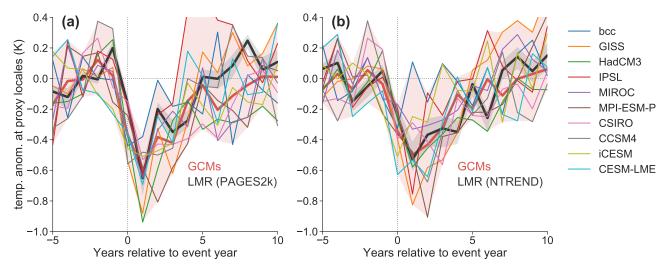
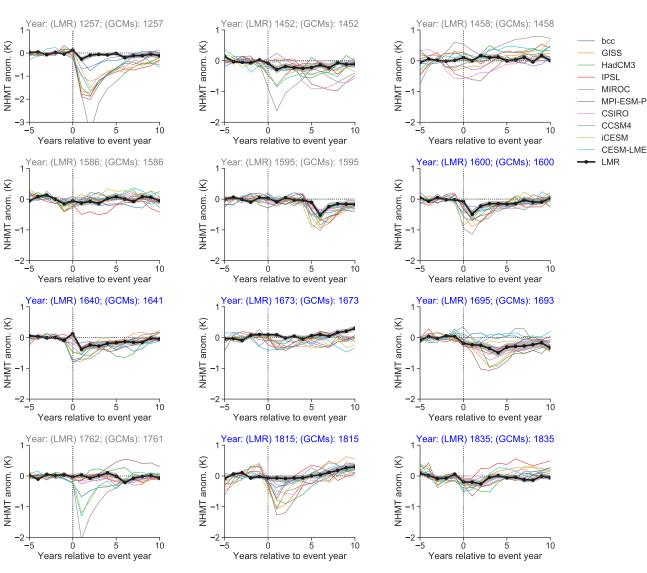


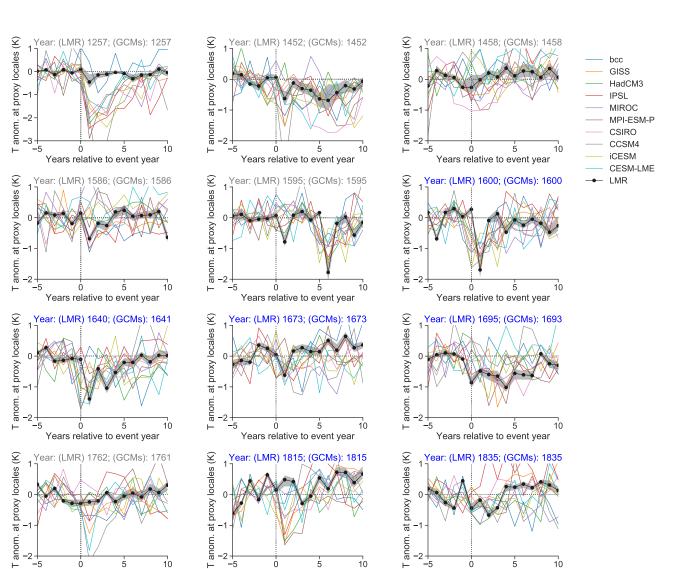
Figure S8. The comparison between the model simulated temperature response and the LMR reconstruction assimilating the whole NTREND network. SEA applied on the annual NHMT over the whole NH.



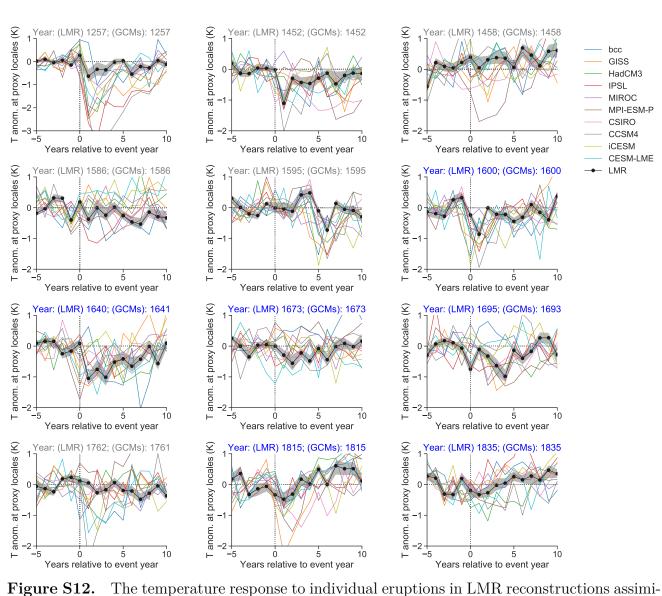
**Figure S9.** Similar to Fig. 4 (main text), but with the result of each model simulation plotted out.



**Figure S10.** The temperature response to individual eruptions in LMR reconstructions assimilating the whole PAGES 2k Network and GCM simulations, targeting NHMT. The blue title denotes the 6 eruption events that are selected for SEA in our study.



 $\frac{\tilde{\xi}}{\tilde{\xi}} - 2 \underbrace{\int_{-5}^{\tilde{\xi}} \underbrace{f}_{\text{Years relative to event year}}^{\tilde{\xi}} 10}_{\text{Years relative to event year}} \underbrace{\tilde{\xi}}_{\text{Years relative to event year}}^{\tilde{\xi}} - 2 \underbrace{\int_{-5}^{\tilde{\xi}} \underbrace{f}_{\text{Years relative to event year}}^{\tilde{\xi}} 10}_{\text{Years relative to event year}} \underbrace{\tilde{\xi}}_{\text{Years relative to event year}}^{\tilde{\xi}} - 2 \underbrace{\int_{-5}^{\tilde{\xi}} \underbrace{f}_{\text{Years relative to event year}}^{\tilde{\xi}} 10}_{\text{Years relative to event year}} \underbrace{\tilde{\xi}}_{\text{Years relative to event year}}^{\tilde{\xi}} \frac{1}{2} \underbrace{f}_{\text{Years relative to event year}}^{\tilde{\xi}} \frac{1}{$ 



lating the NTREND MXD Network and GCM simulations, targeting mean summer temperature at proxy locales. The blue title denotes the 6 eruption events that are selected for SEA in our study.

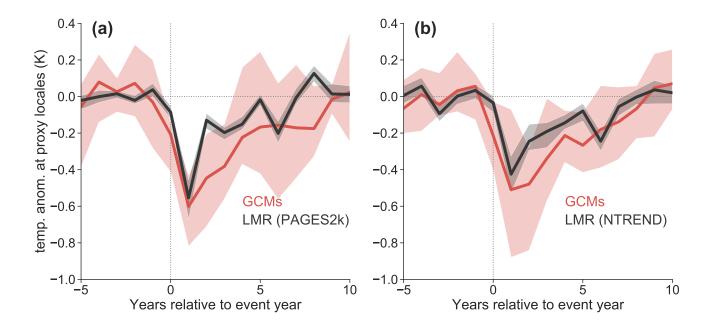


Figure S13. Same as Fig. 4 (main text), but SEA takes all eruption events listed in Fig. S10.

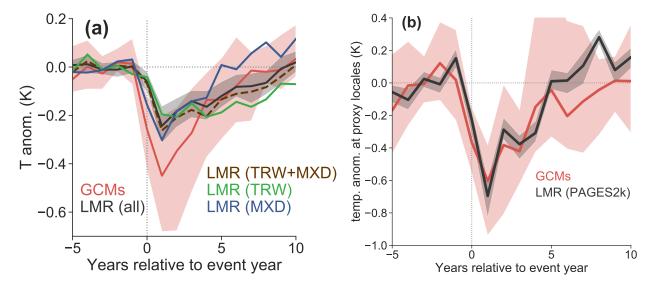
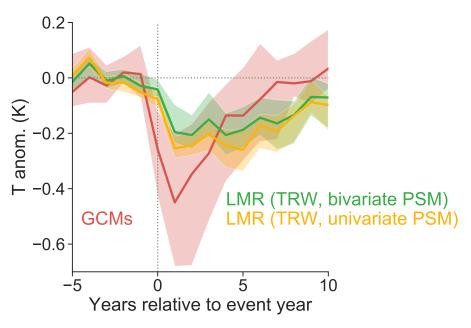
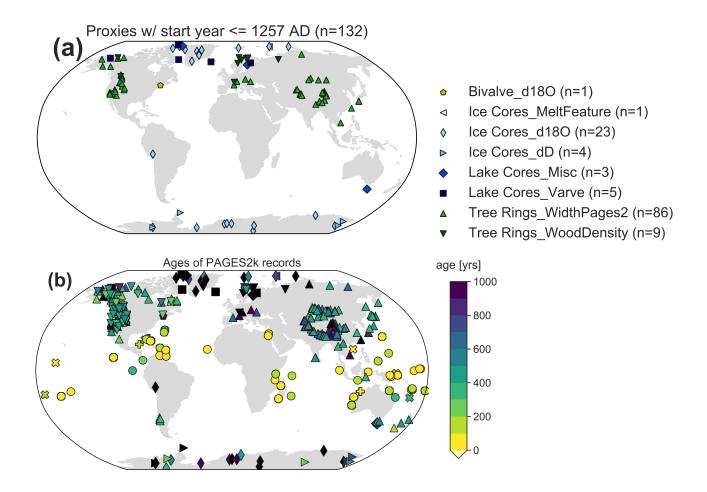


Figure S14. (a) Same as Fig. 1c (main text), but using CCSM4 as prior. (b) Same as Fig. 4a (main text), but using CCSM4 as prior.



**Figure S15.** Same as Fig. 1c (main text), but using CCSM4 as prior and only showing the reconstructions assimilating the PAGES2k TRW network, with both bivariate and univariate forward operator calibration. The comparison indicates that moisture information does not alleviate the issue of lagged response to volcanism in TRW records.



**Figure S16.** (a) Same as Fig. S1a, but for proxies with start year older than or equal to 1257 AD. The shapes and colors denote each proxy type. (b) Ages of PAGES2k records. The shape is same as in (a), while the colors denote different ranges of age.