

Climb of jogs as a rate-limiting process of screw dislocations motion in olivine dislocation creep

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Abstract

Dislocation recovery experiments were conducted on pre-deformed olivine single crystals at temperatures of 1,450 to 1,760 K, room pressure, and oxygen partial pressures near the Ni-NiO buffer to determine the annihilation rates constants for [001] (010) edge dislocations. The obtained rate constants were comparable with those of previously determined [001] screw dislocations. The activation energies for the motion of both dislocations are identical. This suggests that the motion of screw dislocations in olivine is not controlled by cross-slip but by the same rate-limiting process of the motion of edge dislocations, i.e. climb, at low-stress and high-temperature conditions. The diffusivity derived from dislocation climb indicates that dislocation recovery is controlled by pipe diffusion. The conventional climb controlled model for olivine can be applied to the motions of not only edge but also screw dislocations. The softness of the asthenosphere cannot be explained by the cross-slip controlled olivine dislocation creep.

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dislocation creep**

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11 **Abstract**

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13 temperatures of 1,450 to 1,760 K, room pressure, and oxygen partial pressures near the Ni-NiO buffer
14 to determine the annihilation rates constants for [001] (010) edge dislocations. The obtained rate
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16 activation energies for the motion of both dislocations are identical. This suggests that the motion of
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18 the motion of edge dislocations, i.e. climb, at low-stress and high-temperature conditions. The
19 diffusivity derived from dislocation climb indicates that dislocation recovery is controlled by pipe
20 diffusion. The conventional climb controlled model for olivine can be applied to the motions of not
21 only edge but also screw dislocations. The softness of the asthenosphere cannot be explained by the
22 cross-slip controlled olivine dislocation creep.

23
24 **Keywords:** dislocation recovery, dislocation creep, temperature dependence, climb controlled model,
25 asthenosphere

27 **Introduction**

28 Geophysical observations regarding geoid (e.g. Hager, 1991) and post-glacial rebound (e.g.
29 Peltier, 1998) suggested that a soft asthenosphere underlies a rigid lithosphere. Geodynamic
30 modellings (e.g. Becker, 2017; Craig and McKenzie, 1986) also suggested the same conclusion. The
31 reason for the soft asthenosphere is under debate. Although the simplest explanation is weakening of
32 materials due to the high temperature, results of deformation experiments on dry peridotite implied
33 that the high temperatures are insufficient to explain the softness of asthenosphere (Hirth and

34 Kohlstedt, 2003). Although a popular explanation is hydrous weakening of olivine (e.g. Mackwell et
35 al., 1985; Hirth and Kohlstedt, 2003), it is doubted by recent Si self-diffusion experiments (Fei et al.,
36 2016; Fei et al., 2013) based on the assumption that dislocation creep is controlled by diffusion.
37 Another possible explanation was proposed by Poirier and Vergobbi (1978). They suggested that, if
38 cross-slip of dissociated screw dislocations controls olivine dislocation creep, the estimated upper-
39 mantle viscosity would be one order of magnitude lower than that predicted by the climb controlled
40 model in the stress range from 10 to 100 bar. This potentially explains the softness of the
41 asthenosphere. However, there is no experimental study to test this hypothesis.

42 Neither diffusion nor deformation experiments can identify the rate-limiting process of motions
43 of screw dislocations. Diffusion does not involve motions of dislocations. Although it is theoretically
44 possible to determine the rate-limiting process of dislocation motions by examining the stress
45 dependence of creep rates (e.g. Hirth and Kohlstedt, 2003), the stress ranges in deformation
46 experiments are too narrow. Conventionally used stress exponent of 3.5 for dislocation creep implies
47 a pipe diffusion controlled mechanism (Hirth and Kohlstedt, 2003, 2015). However, those
48 experiments have a stress range only from 100 to 224 MPa. On the other hand, Kohlstedt and Goetze
49 (1974) found that stress exponent increases with increasing stress. Poirier (1985, P.139) found that
50 the stress exponent of olivine single crystal dislocation creep varies from 2.6 to 3.7 in different studies.

51 In this study, we conducted dislocation recovery experiments on [001](010) edge dislocations
52 and compared the results with those of [001](010) screw dislocations from Wang et al. (2016). During
53 recovery, dislocations move on the slip plane (glide) and out of the slip plane (climb, cross-slip)
54 successively under the influence of internal stress. Therefore, the activation energy determined by
55 this method represents that of the rate-limiting process of dislocation motions. Although the model

56 from Poirier and Vergobbi (1978) was based on [100] screw dislocations, most of them have edge
57 character at temperature less than 1350 °C (Bai and Kohlstedt, 1992; Wang et al., 2016). On the other
58 hand, the similar density of edge and screw dislocations in [001](010) slip system (Wang et al., 2016)
59 indicates equivalent importance of both types of dislocations in this slip system. Therefore, we focus
60 on this slip system in this study (here after called *c*-dislocations).

61

62 **Experimental Procedure**

63 The same Pakistan olivine and sample preparation procedure as those of Wang et al. (2016) were
64 employed in this study. The composition of olivine was reported by Gose et al. (2010). The
65 experimental setup is similar with that in Wang et al. (2016). The olivine single crystal was orientated
66 by X-ray diffraction and electron backscattered diffraction (EBSD), and then placed in the cell
67 assembly such that the [001] direction and (010) plan are parallel to the shear direction and plane,
68 respectively.

69 Dislocations with the [001] Burgers vector on the (010) plane were produced by experimental
70 deformation using a Kawai-type multi-anvil apparatus at University of Bayreuth. The sample
71 assembly was first pressurized to 3 GPa with a press load of 3.6 MN, and then heated to a temperature
72 of 1,600 K and held for 15 min to sinter crushable alumina. After that, the assembly was further
73 compressed to a press load of 3.9 MN for 15 min to deform the sample. After the deformation, the
74 sample was quenched by switching off the heating power, and then decompressed to room pressure
75 for more than 16 hours. Transmission electronic microscopy (TEM) by Wang et al. (2016) found
76 [001](010) slip system was successfully activated and dominant by this procedure. The ratio of screw
77 to edge dislocations was 3:2, as reported by Wang et al. (2016).

78 The deformed olivine crystals were cut into eight cubic pieces, and paired into four groups, in
79 which the two pieces in each group shared a common (100) plane. One piece from each pair was used
80 to determine the initial dislocation density, while the other was used to determine dislocation density
81 after the annealing. The annealing experiments were conducted at ambient pressure and temperatures
82 of 1,460 to 1,760 K for 35 min to 24 hours using a gas mixing furnace. The oxygen partial pressure
83 was controlled at 10^{-6} - 10^{-8} MPa, which is near the Ni-NiO buffer, using a CO-CO₂ gas mixture. Table
84 1 summarizes conditions of the annealing experiments.

85 Dislocations were observed using oxidation decoration technique (Kohlstedt et al., 1976, Karato
86 1987). The corresponding areas away from sub-grain boundaries on the common (100) plane in the
87 initial and annealed pieces from the same group were observed to determine the change in dislocation
88 densities before and after annealing. Since [001](010) edge dislocations elongate in [100] direction,
89 these dislocations show dots contrast on (100) plane in backscattered images after decoration. The
90 dots per unit area were counted as the dislocation density.

91 The annihilation rate constants were calculated using the second-order dislocation recovery
92 kinetics (Karato and Ogawa, 1982; Kohlstedt et al., 1980; Wang et al., 2016)

$$93 \quad k = \frac{\frac{1}{\rho_f} - \frac{1}{\rho_i}}{t}, \quad (2)$$

94 where ρ_f and ρ_i are the dislocation densities after and before annealing, respectively, and t is the
95 annealing time. Because of the thermally activated process, the dislocation annihilation rate constant
96 is assumed to follow the Arrhenius relationship:

$$97 \quad k = k_0 \exp \left(-\frac{E}{RT} \right) \quad (3)$$

98 where k_0 is a constant, E is the activation energy of dislocation annihilation, T is the temperature,
99 and R is the gas constant.

100

101 **Results**

102 Table 1 shows experimental results together with the annealing conditions. Dislocation density
103 in the samples before deformation is less than $0.0004 \mu\text{m}^{-2}$, which is negligible in comparison with
104 dislocation density after deformation (Table 1). Figure 1 a and b shows back-scattered electron images
105 of decorated dislocations in the corresponding areas in the samples from the same pair before and
106 after annealing, respectively. The *c*-screw dislocations appear as lines and the *c*-edge dislocations as
107 dots on the (100) plane due to their geometries. Decrease in dislocation density was observed by
108 comparing the images before and after annealing. The water contents in the samples before and after
109 annealing were below the detection limit of infrared spectroscopy. The transmission electron
110 microscope images of the dislocation structures after deformation were given in Fig. 4 in Wang et al.
111 (2016).

112 Figure 1c plots the logarithmic rate constants of *c*-edge dislocations annihilation against the
113 reciprocal temperature. The results from the previous dislocation recovery experiments on *c*-screw
114 dislocations (Wang et al., 2016) and from other studies on dislocation recovery kinetics are also
115 plotted in this figure. The dislocation annihilation rate constants of *c*-edge and *c*-screw dislocations
116 are comparable, but those of the *c*-screw are about half orders of magnitude higher than those of the
117 *c*-edge. The temperature dependences for these two dislocations are identical. Their activation
118 energies are $E_{c\text{-edge}} = 400 \pm 20 \text{ kJ/mol}$ and $E_{c\text{-screw}} = 400 \pm 30 \text{ kJ/mol}$ for the *c*-edge and *c*-screw,
119 respectively.

120

121 **Discussion**

122 The identical activation energies of annihilation rate constants of the c -edge and c -screw
123 dislocations indicate that the motions of both dislocations are controlled by the same mechanism.
124 Although many transport properties of olivine exhibit activation energies between 300 to 500 kJ/mol
125 (e.g. Dohmen et al., 2002, 529 ± 41 kJ/mol for silicon self diffusion, 338 ± 14 kJ/mol for oxygen self
126 diffusion), they are distinct from those determined in this study (also see the slope in Fig.3 and
127 references there). The high accuracy in activation energies obtained in previous and this study allows
128 us to distinguish the rate-limiting mechanisms of different processes.

129 The motion of edge dislocations is controlled by climb at high temperatures and low stresses
130 (e.g. Hull and Bacon, 2001; Kohlstedt, 2006). However, motion of a pure screw dislocation does not
131 involve climb because screw segments have no specific slip plane (Hull and Bacon, 2001). Since jogs
132 in screw dislocations has edge character, we propose that the motion of screw dislocation is controlled
133 by climb of jogs (Fig. 2). A screw dislocation can form a jog by cross-slips to overcome obstacles
134 that it meets during glide (Fig.2A and 2B). The slip plane of the jog is defined by its dislocation line
135 (J) and the Burgers vector (b), indicated by the yellow plane. The parent screw dislocation glides in
136 the y direction and therefore, the jog needs to climb in the y direction to move along with their parental
137 dislocation so that the screw dislocation can go through the obstacle (Fig. 2C). This climb of jogs
138 should serve as the rate-limiting process of the screw dislocation motions.

139 It is noted that although the climb of edge dislocation and jog motion of screw dislocation are
140 essentially the same, the density of climbing parts on edge dislocations and that of jogs on screw
141 dislocations may be different, which causes difference in magnitude of rate constants. Thus, only the
142 slope in the Arrhenius plot can be a fingerprint of the essential mechanism of rate-limiting processes
143 in dislocation recovery experiments.

144 Since climb is controlled by diffusion, the diffusivities derived from annihilation rate constants,
145 D^R (based on Karato and Ogawan, 1989) were compared with those of silicon and oxygen diffusion
146 in olivine (Fig. 3). None of these data fit D^R well. Instead, D^R fall between silicon lattice and grain
147 boundary diffusivities. This indicates that the dislocation climb in olivine may be controlled by pipe
148 diffusion. Vacancies, dislocations and grain boundaries are 0-, 1-, 2-dimension defects, the structure
149 distortion near these defects should increase consequently and accordingly, the associated Si
150 diffusivity should increase consequently. In addition, the activation energy of D^R obtained in this
151 study is between those of Si lattice (540 kJ/mol, Dohmen et al., 2002) and grain boundary diffusion
152 (~ 200 kJ/mol, Fei et al., 2015). This is also consistent with the hypothesis that pipe diffusion controls
153 dislocation climb. Although there is no data for the pipe diffusion in olivine, the fact that diffusion
154 coefficient and activation energy of pipe diffusion are between those of lattice and grain boundary
155 diffusion are well established in oxides (Frost and Ashby, 1983, Table 12.1). The low activation
156 energy of oxygen lattice diffusion (~ 340 kJ/mol, Dohmen et al., 2002) rules out the possibility that
157 oxygen diffusion controls dislocation climb.

158

159 **Implications**

160 It was proposed that the softness of asthenosphere can be explained by the cross-slip controlled
161 dislocation creep of olivine (Poirier and Vergobbi, 1978). However, this hypothesis was never tested.
162 The present study demonstrates that motion of [001] screw dislocations is controlled by climb of jogs
163 rather than cross-slip, suggesting that cross-slip model is not applicable for such dislocations in
164 olivine. Although the cross-slip model is based on [100] dislocations, study of [001](010) slip system
165 is more relevant to the asthenosphere conditions. Dislocation structure analyses indicated that most

166 [100](010) dislocations have edge character (Bai and Kohlstedt, 1992, Wang et al., 2016), indicating
167 that olivine dislocation creep cannot be controlled by the motions of [100] screw dislocation. On the
168 other hand, the similar density (Wang et al., 2016) of edge and screw dislocations in [001](010) slip
169 system indicates that both kinds of dislocations are important. Moreover, deformation experiments
170 (e.g. Raterron et al., 2007) suggested that this slip system dominated at high pressure. Therefore, we
171 conclude that cross-slip of screw dislocations cannot control the dislocation creep of olivine and
172 accordingly, it cannot explain the softness of asthenosphere. The climb controlled model can be used
173 in olivine dislocation creep regardless of dislocation characters.

174 The viscosity of asthenosphere extrapolated from dry olivine creep data using climb model is
175 orders of magnitude higher than the estimated value from geophysical observation (Hirth and
176 Kohlstedt 2003). Hydrous weakening of olivine was proposed to explain this discrepancy (e.g.
177 Mackwell et al., 1985; Hirth and Kohlstedt, 2003) but it was disparaged by recent Si diffusion
178 experiments (Fei et al., 2016; Fei et al., 2013). However, this study indicates that pipe diffusion, rather
179 than lattice or grain boundary diffusion, may control the dislocation motions. This may explain the
180 discrepant results between deformation and diffusion experiments. Further studies on the effect of
181 water on the dislocation recovery or pipe diffusion in olivine are needed to identify the effect of water
182 on the olivine rheology and to better explain the softness of the asthenosphere.

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191

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255

256 **Figure and table captions**

257 Figure 1. BEIs showing the dislocation density (a) before and (b) after annealing at 1760 K for 35
258 minutes. The images were taken on the (100) plane. Screw and edge dislocations are lines and dots,
259 respectively, due to the geometries of their dislocation lines. The yellow scale bar represents 2 μm .
260 (c) Logarithmic dislocation annihilation rate constants of c -edge dislocations versus reciprocal
261 temperature. Together plotted are the annihilation rate constants of c -screw dislocations from Wang
262 et al., (2016). The activation energies for both dislocations are identical, i.e. 400 kJ/mol. Previous
263 results on dislocation recovery are also plotted for comparison.

264

265

266 Figure 2. A schematic diagram showing the jog-climb controlled motion of a screw dislocation. (a)
267 The screw dislocation (blue line) is elongated in the x direction, which is parallel to its Burgers vector
268 \mathbf{b} , and glides in the y direction. The blue dot represents the obstacle that the screw dislocation meets
269 during glide. (b) A jog (red segment) elongated in the z direction is produced on the screw dislocation
270 in order to overcome the obstacle. This jog has an edge nature with the same Burgers vector \mathbf{b} as the
271 parental screw dislocation. The yellow area indicates the glide plane of the jog, which is normal to
272 the y direction. (c) The jog has to climb out of its glide plane in order to move along with its parental
273 screw dislocation.

274

275 Figure 3. Logarithmic diffusivity derived from dislocation annihilation rate constants of c -edge and
276 c -screw dislocations versus reciprocal temperature. Together plotted are Si and O lattice and
277 grainboundary diffusivities.

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280 Table 1. Summary of experiment conditions and results.

281

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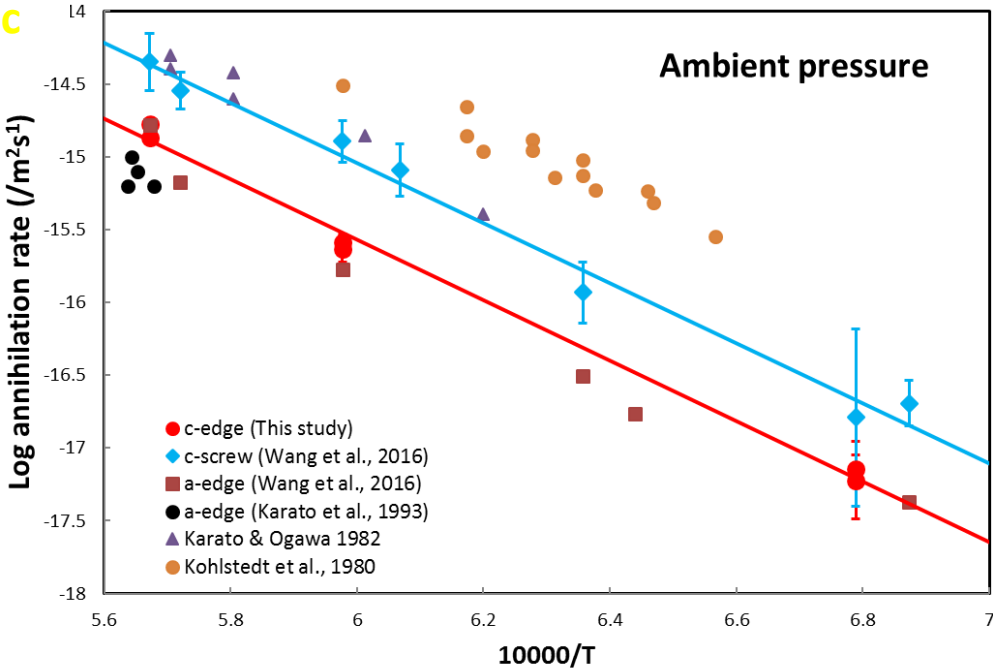
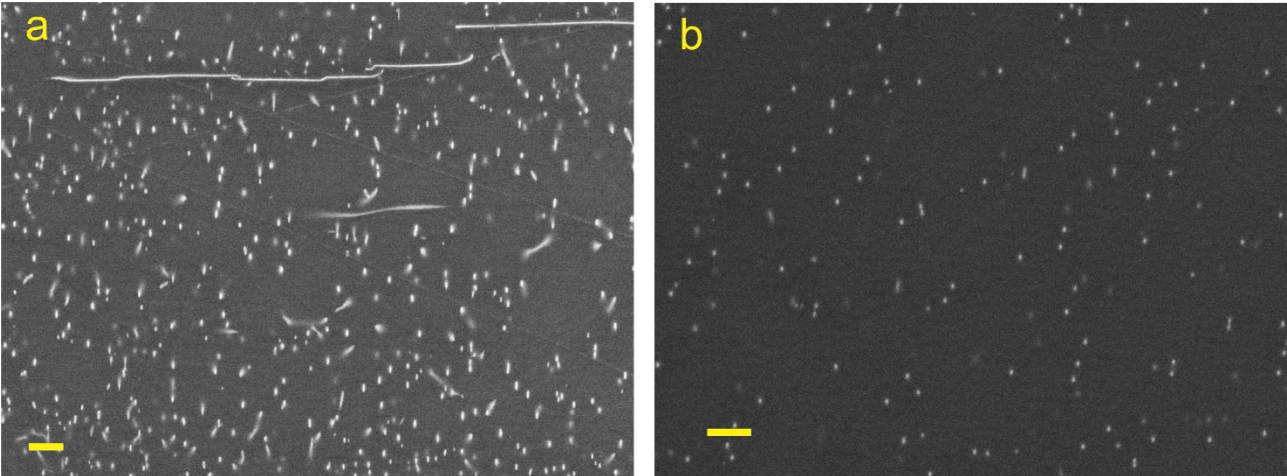
[001](010) edge dislocation						
Sample	T (K)	Annealing time (h)	$\log(f_{o_2} , 10^5$ Pa)	$\rho_i (\mu\text{m}^{-2})$	$\rho_f (\mu\text{m}^{-2})$	$\log(k, \text{m}^2\text{s}^{-1})$
Z1643-1	1763	0.58	-4.9	1.60 ± 0.13	0.29 ± 0.01	-14.87 ± 0.03
				0.97 ± 0.13	0.22 ± 0.01	-14.77 ± 0.03
Z1643-2	1673	2.5	-5.7	1.49 ± 0.04	0.36 ± 0.06	-15.63 ± 0.09
				1.13 ± 0.12	0.31 ± 0.03	-15.58 ± 0.05
Z1643-3	1473	24	-7.7	1.33 ± 0.15	0.73 ± 0.05	-17.14 ± 0.09
				0.35 ± 0.03	0.29 ± 0.01	-17.22 ± 0.27

284 * different ρ_i and ρ_f in each sample correspond to different areas

285

286 Figure 1.

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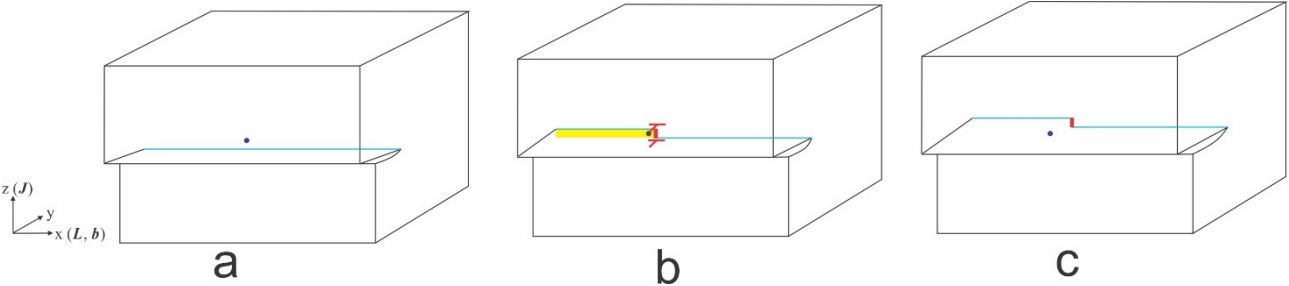


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291 Figure 2.



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