Can the Last Interglacial Constrain Projections of Future Antarctic Ice Mass Loss and Sea-level Rise?

Daniel Gilford¹, Erica Ashe¹, Robert Kopp¹, Robert DeConto², David Pollard³, and Alessio Rovere⁴

¹Rutgers University ²University of Massachusetts Amherst ³Pennsylvania State University ⁴Universität Bremen

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Abstract

Previous studies have interpreted Last Interglacial (LIG; $^129-116$ ka) sea-level estimates in multiple different ways to calibrate projections of future Antarctic ice-sheet (AIS) mass loss and associated sea-level rise. This study systematically explores the extent to which LIG constraints could inform future Antarctic contributions to sea-level rise. We develop a Gaussian process emulator of an ice-sheet model to produce continuous probabilistic projections of Antarctic sea-level contributions over the LIG and a future high-emissions scenario. We use a Bayesian approach conditioning emulator projections on a set of LIG constraints to find associated likelihoods of model parameterizations. LIG estimates inform both the probability of past and future ice-sheet instabilities and projections of future sea-level rise through 2150. Although best-available LIG estimates do not meaningfully constrain Antarctic mass loss projections or physical processes through 2060, they become increasingly informative over the next 130 years. Uncertainties of up to 50 cm remain in future projections even if LIG Antarctic mass loss is precisely known (+/- 5 cm), indicating there is a limit to how informative the LIG could be for ice-sheet model future projections. The efficacy of LIG constraints on Antarctic mass loss also depends on assumptions about the Greenland ice sheet and LIG sea-level chronology. However, improved field measurements and understanding of LIG sea-levels still have potential to improve future sea-level projections, highlighting the importance of continued observational efforts.

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Daniel M. Gilford^{1,2}, Erica L. Ashe², Robert M. DeConto³, Robert E. Kopp^{1,2}, David Pollard⁴, Alessio Rovere⁵

 $^1 \mathrm{Institute}$ of Earth, Ocean, and Atmospheric Sciences, Rutgers University, 71 Dudley Road, Suite 205, New Brunswick, NJ 08901, USA.

²Department of Earth and Planetary Sciences, Rutgers University, Piscataway, NJ, USA.
 ³Department of Geosciences, University of Massachusetts, Amherst, MA, USA.
 ⁴Earth and Environmental Systems Institute, Pennsylvania State University, University Park, PA, USA.
 ⁵MARUM, Center for Marine Environmental Sciences, University of Bremen, Germany.

Key Points:

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12	•	Improved Last Interglacial Antarctic mass loss constraints appreciably reduce fu-
13		ture sea-level rise uncertainties, especially at the margins
14	•	Last Interglacial sea-level constraints are increasingly informative with respect to
15		Antarctic mass loss over the next 130 years
16	•	If Last Interglacial sea levels were known precisely, projected 2100 Antarctic mass
17		loss could still have uncertainties of up to ~ 50 cm

Corresponding author: Daniel Gilford, daniel.gilford@rutgers.edu

18 Abstract

Previous studies have interpreted Last Interglacial (LIG; $\sim 129-116$ ka) sea-level estimates 19 in multiple different ways to calibrate projections of future Antarctic ice-sheet (AIS) mass 20 loss and associated sea-level rise. This study systematically explores the extent to which 21 LIG constraints could inform future Antarctic contributions to sea-level rise. We develop 22 a Gaussian process emulator of an ice-sheet model to produce continuous probabilistic 23 projections of Antarctic sea-level contributions over the LIG and a future high-emissions 24 scenario. We use a Bayesian approach conditioning emulator projections on a set of LIG 25 constraints to find associated likelihoods of model parameterizations. LIG estimates in-26 form both the probability of past and future ice-sheet instabilities and projections of fu-27 ture sea-level rise through 2150. Although best-available LIG estimates do not mean-28 ingfully constrain Antarctic mass loss projections or physical processes through 2060, 29 they become increasingly informative over the next 130 years. Uncertainties of up to 50 30 cm remain in future projections even if LIG Antarctic mass loss is precisely known (± 5 31 cm), indicating there is a limit to how informative the LIG could be for ice-sheet model 32 future projections. The efficacy of LIG constraints on Antarctic mass loss also depends 33 on assumptions about the Greenland ice sheet and LIG sea-level chronology. However, 34 improved field measurements and understanding of LIG sea-levels still have potential to 35 improve future sea-level projections, highlighting the importance of continued observa-36 tional efforts. 37

38 1 Introduction

Coastal communities are facing increasing threats from sea-level rise, creating a grow-30 ing need for comprehensive probabilistic projections (Kopp et al., 2014; Kopp, DeConto, 40 et al., 2017; Horton et al., 2018) to inform coastal risks and adaptation practices (Buchanan 41 et al., 2016, 2017; D. J. Rasmussen et al., 2018; Kopp et al., 2019). The single largest 42 source of uncertainty in 21st century global-mean sea-level rise is the Antarctic ice sheet 43 (AIS). Projected AIS mass loss depends on the ice-sheet physics considered, modeling 44 and statistical methodologies, and observational constraints (e.g., Kopp, DeConto, et al., 45 2017).46

There is deep uncertainty in future AIS sea-level contributions, meaning that their 47 full probability distribution is unknown and cannot be estimated or agreed upon by ex-48 perts (Lempert & Collins, 2007). The lack of expert agreement on AIS mass loss pro-49 jections is partially related to unresolved challenges in modeling ice-sheet processes (Fuller 50 et al., 2017; Bakker, Wong, et al., 2017; Bakker, Louchard, & Keller, 2017; Bamber et 51 al., 2019). There is growing consensus that the AIS is threatened by marine ice-sheet 52 instability (MISI; Weertman, 1974; Schoof, 2007), which would lead to accelerated mass 53 loss irreversible on millennial timescales (Golledge et al., 2015; Bulthuis et al., 2019) and 54 skew probability distributions towards fat upper-tails in sea-level projections (Robel et 55 al., 2019). There is some evidence that MISI is already underway in the Thwaites/Pine 56 Island Glacier basins (Joughin et al., 2014; Favier et al., 2014), and western AIS ice dis-57 charge has accelerated in recent years (Gardner et al., 2018; Rignot et al., 2019). Even 58 more uncertain is the role of marine ice-cliff instability (MICI), which has recently been 59 proposed and incorporated as a primary loss mechanism in an ice-sheet model for sea-60 level rise projections (Bassis & Walker, 2012; Bassis & Jacobs, 2013; Pollard et al., 2015; 61 DeConto & Pollard, 2016). 62

MICI is not well understood and is difficult to parameterize. While it has not yet
been observed in Antarctica, there is some modern evidence consistent with cliff instability, such as the documented calving events of Greenland glaciers (DeConto & Pollard,
2016; Parizek et al., 2019). Newly discovered iceberg-keel plough marks also provide evidence for MICI in Pine Island Bay in the early Holocene, ~12,000 years years before
present (ka; Wise et al., 2017). However, a recent reanalysis of DeConto and Pollard (2016)

showed that MICI is not well constrained, and is unnecessary for ice-sheet model pro-69 jections to be consistent with modern and paleoclimate estimates of AIS mass loss (Edwards 70 et al., 2019). Clerc et al. (2019) examined how ice cliffs deform following removal of their 71 buttressing ice shelves. They found that ~ 90 m-tall ice cliffs would have to be lost near-72 instantaneously after shelf collapse to trigger MICI—on longer timescales viscous relax-73 ation dominates the response. Furthermore, Olsen and Nettles (2019) found seismic mea-74 surements of the aforementioned Greenland glaciers were not indicative of subaerial ice 75 cliff failure expected with MICI. These findings cannot preclude MICI as a primary mass 76 loss mechanism in Antarctica, but they demonstrate the paucity of observations to con-77 strain this process. 78

Whether or not major AIS discharge will occur through MISI and/or MICI is crit-79 ical for future impacts on human systems (Oppenheimer & Alley, 2016; Wong et al., 2017; 80 Stammer et al., 2019). But correlations between observed trends and future large-scale 81 mass losses are weak and insignificant (Kopp, DeConto, et al., 2017), signaling that mod-82 ern observations are inadequate for constraining potentially nonlinear AIS contributions 83 to sea-level rise. Instead, the information gap must be filled with analogs from the paleo sea-level record. The Last Interglacial (LIG) period has previously been invoked to 85 inform ice-sheet instabilities and model projections (DeConto & Pollard, 2016; Steig & 86 Neff, 2018), but it may currently be an ineffective constraint (Edwards et al., 2019). In 87 this study we investigate how improved estimates or different interpretations of LIG AIS 88 mass loss may be combined with ice-sheet model ensembles to constrain probabilistic pro-89 jections of future sea-level rise. We specifically choose ice-sheet model simulations which 90 consider the MICI process to complement recent studies using similar methods (DeConto 91 & Pollard, 2016; Edwards et al., 2019). 92

The Last Interglacial ($\sim 129,000$ to 116,000 ka) was a period of higher orbital ec-93 centricity, slightly warmer than present average global mean temperatures, and substan-94 tially warmer polar atmospheric temperatures ($>3^{\circ}C$ warmer than present) and high-95 latitude ocean temperatures (1°C warmer than present) (Capron et al., 2017, and ref-96 erences therein). Accompanying were estimated global mean sea levels (GMSL) about 97 6-9 m higher than present (Dutton, Carlson, et al., 2015), driven by a combination of 98 mountain glacial melt, Greenland and Antarctic ice-sheet mass loss, and thermosteric 99 effects. While the proportional mix of these contributions is uncertain, previous stud-100 ies determined that some portions of the AIS retreated during the LIG (e.g., Scherer et 101 al., 1998; Dutton, Carlson, et al., 2015; Dutton, Webster, et al., 2015). The LIG has his-102 torically been considered an analog for AIS contributions to sea-level rise in warm cli-103 mates (Mercer, 1968; Hansen et al., 1981), but it may not be ideal for examining future 104 climate change, as LIG and modern external forcing mechanisms are fundamentally dif-105 ferent (Capron et al., 2019). 106

Different interpretations and applications of paleo sea-level estimates have led to 107 divergent conclusions about what instability processes could drive future sea-level rise 108 (cf. DeConto and Pollard (2016) and Edwards et al. (2019)). The goal of this study is 109 to develop a framework for analyzing the extent to which the LIG could inform ice-sheet 110 model projections of future AIS mass loss and sea-level rise. We quantify ice-sheet model 111 projections conditioned on multiple LIG estimate distributions, and assess how narrower 112 LIG uncertainties could improve understanding of both ice-sheet instabilities and future 113 sea levels. We also investigate how different assumptions about LIG sea-level evolution 114 influences ice-sheet modeling of future sea-level changes. These analyses provide useful 115 targets and research directions for the paleo sea-level observational and ice-sheet mod-116 eling communities. 117

Ice-sheet models are computationally expensive to run at high resolutions necessary for sufficient accuracy. The number of simulations computationally tractable over a model's parameter space is therefore limited, making it difficult to construct an ensemble large enough to perform comprehensive statistical analyses (which are necessary for

robust probabilistic projections of sea-level rise and coastal risk, e.g. Kopp, DeConto, 122 et al., 2017; D. J. Rasmussen et al., 2020). In this study we develop a statistical "em-123 ulator" designed to mimic the behavior of the ice-sheet model (the "simulator") to fill 124 intermediate solutions that have not been simulated over the ic-sheet model parameter 125 space and time (Kennedy & O'Hagan, 2001; C. E. Rasmussen & Williams, 2006; Bas-126 tos & O'Hagan, 2009). Similar to Edwards et al. (2019), we emulate ice-sheet simula-127 tions of the LIG and the future under a high-emissions scenario. The emulator provides 128 continuous estimates of AIS sea-level contributions over two model parameters directly 129 related to ice-sheet instability processes. We perform Bayesian statistical analyses with 130 emulator output to determine how future Antarctic sea-level contribution projections de-131 pend on LIG constraints. 132

Section 2 provides a detailed overview of the ice-sheet model ensembles, emulation
 methodology, the Bayesian approach, and LIG constraints. Our results in section 3 show
 how current and improved LIG estimates could constrain future Antarctic contributions
 to sea-level rise. We also demonstrate a specific framework application using paleo sea level observations, and discuss our study's implications for future research directions in
 the paleo sea-level community. Conclusions are presented in section 4.

¹³⁹ 2 Models and Methods

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2.1 Ice-sheet Model Simulations

We create ice-sheet model ensembles for the LIG and a future high-emissions sce-141 nario (Representative Concentration Pathway 8.5, RCP8.5; Riahi et al. (2011)). We run 142 simulations with the PSU Ice-sheet model, which has been used in several studies of ice-143 sheet contributions to past and future sea levels (Pollard & DeConto, 2009; DeConto & 144 Pollard, 2016; Pollard et al., 2016, 2017; Kopp, DeConto, et al., 2017; Pollard et al., 2018; 145 Edwards et al., 2019). The model (Pollard & DeConto, 2012) uses a hybrid combination 146 of the vertically integrated shallow ice and shallow shelf approximations for ice flow (de-147 scribed in (Pollard & DeConto, 2012)). Ice flux at freely migrating grounding lines is pa-148 rameterized (Schoof, 2007; Pollard & DeConto, 2009, 2012), while accounting for the but-149 tressing effects of ice shelves. Hydrofracturing from surface melt and structural failure 150 of tall ice cliffs is included (Pollard et al. (2015); DeConto and Pollard (2016), discussed 151 more below). The model simulates internal ice temperatures, with basal sliding and sed-152 iment deformation occurring only where the base is at or near the melt point, and no 153 explicit basal hydrology. A Weertman-type basal sliding law over bedrock is used with 154 the norm of the sliding velocity proportional to the squared norm of the basal shear stress, 155 and spatially dependent coefficients (Pollard & DeConto, 2012). We run the model on 156 a 10 km-resolution grid over the continental Antarctic. 157

Model simulations are an improvement on those of DeConto and Pollard (2016) and 158 reanalyzed in Edwards et al. (2019). Model runs use a sub-oceanic melt scheme newly 159 calibrated following a large ensemble analysis of model performance during the last deglacia-160 tion (Pollard et al., 2016). This improvement, developed for DeConto et al. (2020), re-161 duces the need for a sub-surface ocean temperature bias correction on the West Antarc-162 tic margin by 50% (from 3° C to 1.5° C) relative to (DeConto & Pollard, 2016). Atmo-163 spheric climatologies in future simulations are also improved, as discussed below (cf. DeConto 164 et al. (2020)). 165

LIG equilibrium model simulations are forced by representative oceanic and atmospheric conditions from 130 ka constructed from a synthesis of paleoclimate reconstructions and climate modeling (Capron et al., 2014). We run the simulations for 5,000 years to bring them approximately into equilibrium with this fixed climate forcing; we take the final simulation values (year 5000) as representing the peak AIS mass loss response during the LIG. Emulated peak LIG mass losses are later paired with paleo sea-level estimates to assess whether the LIG could constrain future AIS contributions to sea-level rise (section 2.2–2.4).

Future transient model simulations span 1990–2150 and are reported relative to the 174 year 2000. Following DeConto and Pollard (2016), atmospheric RCP8.5 forcing is time-175 interpolated and log-weighted from regional climate model Antarctic snapshots at vary-176 ing levels of effective CO_2 (1×, 2×, 4×, and 8× preindustrial). Improving on DeConto 177 and Pollard (2016), time-evolving sea-surface temperatures are synchronized in the re-178 gional atmospheric model simulations with subsurface temperatures used in the subsur-179 face melt rate calculations, leading to favorable comparisons with an independent NCAR 180 CESM simulation (DeConto et al., 2020, their Extended Data Figure 1). 181

LIG and future simulation ensembles are constructed by a sampling a 2-dimensional 182 parameter space with a regularly spaced 14×14 grid. The two parameters, CREVLIQ 183 and CLIFVMAX (Supporting Information Table S1), are detailed in DeConto and Pol-184 lard (2016). Briefly, CREVLIQ is the proportional sensitivity of model hydrofracturing 185 to surface liquid, i.e. from rain and meltwater $\left(\frac{m}{(myr^{-1})^2}\right)$; it is substituted for "100" in 186 equation (B.6) of Pollard et al. (2015). As CREVLIQ increases, ice-sheet crevasses deepen 187 more readily with surface liquid accumulation, which increases the chance of hydrofrac-188 turing and removal of buttressing ice shelves. CLIFVMAX is the maximum rate $\left(\frac{km}{vr}\right)$ 189 of horizontal cliff wastage once an ice cliff becomes mechanically unstable and collapses 190 (i.e. under MICI); it is substituted for "300" in equation (A.4) of Pollard et al. (2015) 191 (called "VCLIF" in DeConto and Pollard (2016)). Note that when CLIFVMAX=0 $\frac{\text{km}}{\text{vr}}$ 192 ice cliffs cannot retreat even when they would theoretically fail; in this set of simulations 193 MICI is effectively turned off. 194

Ensembles vary CLIFVMAX and CREVLIQ over a broader range of parameter values than those of DeConto and Pollard (2016) and Edwards et al. (2019): the CLIFV-MAX maximum is 2.6 times larger than in those studies, and the CREVLIQ range 1.3 times larger (Supporting Information Table S1). We expand the parameter value range to explore a greater range of parametric uncertainty, with upper bounds guided by observations (discussed in detail in DeConto et al. (2020)) rather than the arbitrarily assigned bounds of DeConto and Pollard (2016).

Figure 1 shows ensemble timeseries of AIS mass loss in global mean sea-level equivalent from the LIG and RCP8.5 scenario; ensemble member timeseries are color-coded by CLIFVMAX values (timeseries color-coded by CREVLIQ are shown in Supporting Information Figure S1). Figure 1a includes an illustrative range of estimated LIG AIS sea-level contributions (3.1–6.1 m), which was assumed by DeConto et al. (2020) based on reconstructions described in Dutton, Carlson, et al. (2015). This LIG estimate is lower and slightly narrower than that assumed in DeConto and Pollard (2016) and Edwards et al. (2019); this and additional LIG constraints are explored below (section 2.4).

The evolution of LIG simulations (Fig. 1a) suggests that there are distinct ice-sheet 210 mass-loss events (e.g. the accelerated mass loss in some simulations $\sim 1,000$ years into 211 the simulation) in response to constant forcing, depending strongly on model parame-212 ter values. This nonlinear behavior results in a multi-modal distribution of the ensem-213 ble's peak AIS mass loss (section 3). AIS discharge is sensitive to the value of CLIFV-214 MAX on the timescale of centuries, as seen in the first 1,000 years of the LIG ensemble 215 and the entirety of the RCP8.5 simulation (Fig. 1b). The non-monotonic color progres-216 sion of timeseries in Fig. 1a suggests that CREVLIQ plays a more substantial role in ice-217 sheet mass loss under LIG forcing and/or on millennial timescales (Supporting Informa-218 tion Figures S1–S2). 219

Future simulations of AIS mass loss under RCP8.5 forcing are very similar across the ensemble in the early 21^{st} century; 158 of 196 simulations have loss rates within 1 standard deviation of IMBIE2 observed rates over 1992–2017 (15–46 $\frac{mm}{yr}$); IMBIE-Team

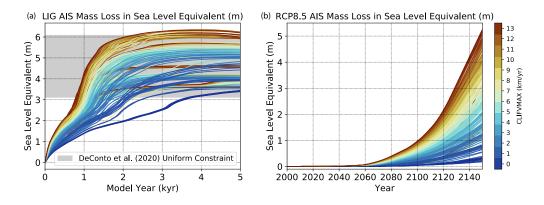


Figure 1. Timeseries of simulated AIS mass losses in sea-level equivalent (m) under (a) Last Interglacial forcing and (b) RCP8.5 forcing over 2000–2150. Simulated timeseries are color-coded by CLIFVMAX values over 0–13 $\frac{\text{km}}{\text{yr}}$. Gray shading in (a) is an illustrative range of estimated LIG AIS sea-level contributions, 3.1–6.1 m, derived in DeConto et al. (2020) and based on the reconstructions of Dutton, Carlson, et al. (2015).

(2018)). In ~2060 ice discharge dramatically accelerates among ensemble members with 223 higher CLIFVMAX values, and simulations markedly diverge. Across the simulations 224 ice loss continues to accelerate through 2100 and well into the 22^{nd} century; 86% of the 225 simulated peak loss rates occur after 2130. By 2150, the ensemble's median rate of sea-226 level equivalent mass loss is 54 $\frac{\text{mm}}{\text{vr}}$, and the median AIS sea-level contribution is 2.3 m. 227 Mean RCP8.5 ensemble AIS sea-level contributions are 42 cm in 2100 and 2.3 m in 2150. 228 These values are lower than DeConto and Pollard (2016) large-ensemble projections (with-229 out bias corrections and with default model parameters, see their Extended Data Ta-230 ble 1) in both 2100 (77 cm) and 2150 (2.9 m). Differences are largely due to model im-231 proved synchronicity in atmospheric forcing, which slows the onset of surface meltwa-232 ter production and ice shelf hydrofracturing by ~ 25 years compared to DeConto and Pol-233 lard (2016). 234

The emulator is trained only on simulations from this single ice-sheet model and 235 with changes only in the parameters discussed above. Other ice-sheet processes or pa-236 rameters that could lead to ice-sheet and ice-shelf stability or collapse have not been in-237 vestigated here. Whereas our methodology is developed with a generalizable emulation 238 and calibration framework, quantitative results in section 3 apply only to this specific 239 ice-sheet model. The LIG could inform additional or alternative physical processes (see 240 section 4) not considered here, and the emulation and calibration framework could be 241 extended to include assessments of LIG constraints on the Greenland ice sheet, calibra-242 tion of other ice-sheet models or ensembles (e.g. ISMIP6, Nowicki et al. (2016); Goelzer 243 et al. (2018)), calibration of different parameters or regions of parameter space, or cal-244 ibration with different paleo sea-level constraints (e.g. the Pliocene). 245

2.2 Emulation

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We train the emulator separately on LIG and RCP8.5 ensembles (\mathbf{z}_{LIG} and \mathbf{z}_{RCP} , respectively) using Gaussian process (GP) regression (e.g. C. E. Rasmussen & Williams, 2006; Ashe et al., 2019). We model the total AIS contributions to GMSL, $f(\theta_1, \theta_2, t)$, as the sum of two terms, each with a zero-mean GP prior distribution:

$$f(\theta_1, \theta_2, t) = f_1(\theta_1, \theta_2) + f_2(\theta_1, \theta_2, t).$$
(1)

The first term, $f_1(\theta_1, \theta_2)$, represents a time-independent function on the parameter space (θ_1, θ_2) , and the second term, $f_2(\theta_1, \theta_2, t)$, represents the temporal evolution. We specify the prior distributions of each term as:

$$f_1(\theta_1, \theta_2) \sim \mathcal{GP}(0, \alpha_1^2 K_1(\theta_1, \theta_2, \theta_1', \theta_2'; \ell_1)), \tag{2}$$

$$f_2(\theta_1, \theta_2, t) \sim \mathcal{GP}(0, \alpha_2^2 K_2(\theta_1, \theta_2, \theta_1', \theta_2'; \ell_2) \cdot K_t(t, t'; \tau)), \tag{3}$$

where θ_1 and θ_2 are values of CLIFVMAX and CREVLIQ normalized by their respec-254 tive maximum values in the simulator ensemble parameter space (Supporting Informa-255 tion Table S1), α_i are standard deviations, ℓ_i are characteristic length scales in the nor-256 malized parameter space, τ is a characteristic time scale and K_i are specified covariance 257 functions. Because the LIG training data are evaluated at a single time point, there is 258 no temporal term and f_2 is excluded from LIG emulator construction. K_i are defined 259 to be Matérn covariance functions with a specified smoothness (shape) parameter, ν , which 260 governs how responsive the function and its realizations are to sharp changes in the train-261 ing data (C. E. Rasmussen & Williams, 2006). The choice of a Matérn covariance func-262 tion allows for non-parametric nonlinear behavior in time and space. For the RCP8.5 263 scenario we set ν to $\frac{5}{2}$ because transient sea-level contributions vary smoothly over the 264 model parameter space and time; for the LIG scenario we set ν to $\frac{1}{2}$ because peak LIG 265 sea-level contributions vary more sharply over the model parameter space. The model 266 form and covariance functions are chosen for a balance of simplicity, minimizing abso-267 lute errors and variance (i.e. model accuracy and precision), and maximizing the like-268 lihood of the training data. Other covariance function and model forms were explored, 269 but are not presented for brevity (Supporting Information Text S2). 270

Optimal hyperparameters $(\alpha_i, \ell_i, \text{ and } \tau)$ of the GP emulator are found by max-271 imizing the likelihood of the training simulations (Supporting Information Table S2, C. E. Ras-272 mussen and Williams (2006)). We specify the "nugget" (point-wise variance) of the op-273 timized emulator as 10^{-6} m² because the simulator is deterministic, and the emulated 274 mean should approximately match the training ensemble data across the parameter space 275 and time. We then condition (train) the optimized emulator on the simulator ensembles 276 $(f|\mathbf{z})$ to arrive at a trained model. The trained model predicts continuous sea-level con-277 tributions for LIG and RCP8.5 at parameter values and times between discrete train-278 ing simulations. We refer to this trained model as the "prior" emulator for the LIG ($f_{\rm LIG}$) 279 and RCP8.5 ($f_{\rm RCP}$), before calibrating with LIG constraint distributions (below). We 280 perform leave-one-out analyses to validate the optimized prior emulator following Bastos 281 and O'Hagan (2009) and find it accurately mimics the behavior of the ice-sheet simu-282 lator over the LIG and RCP8.5 scenario (Supporting Information Text S1, Fig. S3–S4). 283

Figure 2 shows the prior emulator mean functions of $f_{\rm LIG}$ and $f_{\rm RCP}$ (contours) for 284 the LIG and RCP8.5 in 2100 over the parameter space, and the corresponding training 285 simulations (circles). There are natural similarities between the emulated sea levels dur-286 ing the LIG and those projected in 2100 under RCP8.5. Ice-cliff collapse and/or hydrofrac-287 turing are clearly relevant drivers of both paleo estimates and future projections by this 288 ice-sheet model (see section 2.3): for relatively large values of CREVLIQ and CLIFV-289 MAX, emulated AIS mass loss is likewise relatively high. Sea-level contributions are also 290 substantially lower when either CREVLIQ or CLIFVMAX are near zero, indicating em-291 ulated sea-levels with these parameter values are not appreciably influenced by either 292 hydrofracturing from surface liquid or mechanically unstable ice-cliff retreat. 293

There are also differences between LIG and RCP8.5 emulator mean functions (Fig. 2, Supporting Information Figure S2). Future projected AIS mass loss is more sensitive to CLIFVMAX than CREVLIQ (cf. Fig. 1b), which becomes more pronounced throughout the early 22nd century (not shown). In contrast, LIG AIS sea-level contributions are sensitive to both CREVLIQ and CLIFMVAX in some regions of the parameter space,

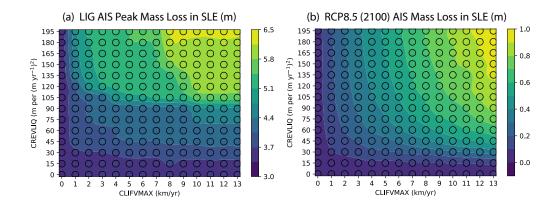


Figure 2. Simulated (filled circles) and mean emulated (contours) AIS mass losses in sealevel equivalent across ice-sheet model parameter space (a) during the Last Interglacial, and (b) projected under an RCP8.5 scenario in 2100.

but are nearly constant in other regions (e.g. where CREVLIQ > 120 and 2 < CLIFV-299 MAX < 7, Fig. 2a). Given prolonged fixed forcing, different AIS sectors can be completely 300 lost regardless of the specific parameter value in these regions of parameter space, re-301 sulting in very similar sea-level contributions. This clustering behavior is much less pro-302 nounced over the modern period of transient and increasing forcing except along fixed 303 values of CLIFVMAX, as shown by its smoothly varying sea-level contributions (Fig. 1b) 304 and Fig. 2b). These differences across the parameter space have important implications 305 for model calibration. In particular, they imply that even if the LIG contributions were 306 known precisely, there may be a limit to their ability to constrain future projections. For 307 example, the region of the parameter space with LIG contributions of ~ 5.2 m (CREVLIQ 308 > 120, 2 < CLIFVMAX < 7) corresponds to AIS sea-level contributions of $\sim 35-65$ cm 309 in 2100 under RCP8.5 forcing (Fig. 2b). This limitation is explored in detail in section 310 3. 311

Having developed a prior emulator trained on the LIG and RCP8.5 scenario ensembles, we generate 10,000 realizations of emulator output (mean and variance) with a two-dimensional Latin-hypercube design over the parameter space. The time-dependent median and probability intervals of the RCP8.5 emulator prior are shown in Figure 3.

2.3 Bayesian Updating

We use a Bayesian updating approach to determine the influence of LIG constraints on future projections of Antarctic contributions to sea-level rise; a glossary of relevant statistical terms is provided in Supporting Information Table S3. Let g_{LIG} and g_{RCP} be the latent AIS sea-level contributions the emulator is designed to predict, at the peak LIG and in the future under RCP8.5 forcing, respectively. We take a uniform prior probability distribution over the input parameter space (θ_1, θ_2) (Supporting Information Table S1).

We seek the probability distribution of future AIS contributions to sea-level rise estimated by the emulator and conditioned on a specified LIG constraint of peak LIG AIS mass loss, y:

$$p(g_{\text{RCP}} \mid y) = p(g_{\text{RCP}} \mid \theta_1, \theta_2) p(\theta_1, \theta_2 \mid y), \tag{4}$$

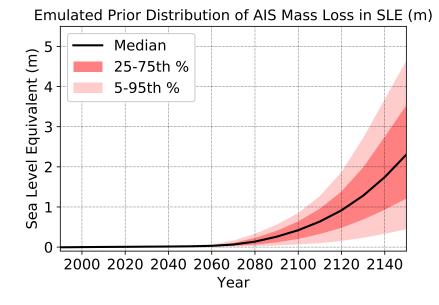


Figure 3. Emulator prior probability distribution of AIS mass loss in sea-level equivalent (m) projected under RCP8.5 forcing over 2000–2150. Shown are the median (solid black line), $25^{\text{th}}-75^{\text{th}}$ (dark red shading), and $5^{\text{th}}-95^{\text{th}}$ percentiles (light red shading) of the distribution.

where $p(g_{\text{RCP}} | \theta_1, \theta_2)$ is the prior distribution of sea-level contributions from the the RCP8.5 emulator (f_{RCP}) , and $p(\theta_1, \theta_2 | y)$ is the posterior probability of the parameters conditioned on a specified LIG constraint (example constraints described in section 2.4). This probability can be decomposed using Bayes' theorem,

$$p(\theta_1, \theta_2 \mid y) \propto p(y \mid \theta_1, \theta_2) p(\theta_1, \theta_2), \tag{5}$$

where $p(\theta_1, \theta_2)$ is the uniform prior probability on the parameter space and $p(y | \theta_1, \theta_2)$ is the likelihood function. Incorporating estimates from the LIG emulator of the true LIG peak AIS mass loss, g_{LIG} ,

$$p(y \mid \theta_1, \theta_2) = p(y \mid g_{\text{LIG}})p(g_{\text{LIG}} \mid \theta_1, \theta_2), \tag{6}$$

where $p(g_{\text{LIG}} \mid \theta_1, \theta_2)$ is the prior distribution of AIS mass loss from the LIG emulator (f_{LIG}) , and $p(y \mid g_{\text{LIG}})$ is the probability distribution of the specified constraint given the unknown LIG peak AIS sea-level contributions. Here $p(y \mid g_{\text{LIG}}) \propto p(g_{\text{LIG}} \mid y)$ because p(y) is the uninformative uniform prior probability distribution of the LIG constraint. Substituting equations (5) and (6) into equation (4) we find

$$\underbrace{p(g_{\rm RCP} \mid y)}_{\rm posterior} \propto \underbrace{p(g_{\rm RCP} \mid \theta_1, \theta_2)}_{f_{\rm RCP}} \underbrace{p(g_{\rm LIG} \mid y)}_{\rm constraint \ dist.} \underbrace{p(g_{\rm LIG} \mid \theta_1, \theta_2)}_{f_{\rm LIG}} \underbrace{p(\theta_1, \theta_2)}_{\rm prior \ on \ \theta_1, \theta_2} , \tag{7}$$

which describes the posterior probability distribution of future AIS sea-level contribution projections conditioned on a specified Last Interglacial probability distribution. Eqn.
(7) implies that the choice of the prior emulator, the prior parameters, and the specified representative LIG constraint distribution each influence posterior projections of fu-

ture AIS contributions to sea-level rise.

We demonstrate the utility of this approach in three ways. First, we explore how future projections are constrained when LIG AIS mass loss is assumed to be precisely known (e.g. to within 10 cm). Following Eqn. (7), we find $p_x(g_{\rm RCP} | y_x)$ as a function of a set of discretized 10 cm-wide bins across the range of the prior LIG emulator given by,

$$y_x = \mathcal{U}(x - 5\,\mathrm{cm}, x + 5\,\mathrm{cm}],$$

where $x = \{2.0 \text{ m}, 2.1 \text{ m}, ..., 6.9 \text{ m}, 7.0 \text{ m}\}$. The associated posteriors of RCP8.5 AIS contributions to sea-level rise, p_x , are a set of comprehensive time-dependent conditional probability distributions given as a function of LIG AIS mass loss. When the conditional probability distributions are integrated over a range of x values with some weighting (i.e. any specified y), the result is a constrained probability distribution of future AIS contributions to sea-level rise.

Second, we examine particular posteriors of RCP8.5 AIS contributions to sea-level 355 rise as a function of several specific LIG constraint distributions, drawn from or adapted 356 from the literature. Third, we analyze how the ice-sheet model projections of future AIS 357 mass loss would be influenced through hypothetical improvements in LIG constraint dis-358 tributions, either by 1) narrowing the range of uncertainty on LIG estimates, or by 2) 359 learning that the LIG AIS sea-level contributions were relatively high (>6 m) or rela-360 tively low (<3.5 m). Each LIG constraint distribution is detailed in the following sec-361 tion. 362

363

2.4 LIG Constraint Distributions

We prescribe a set of LIG constraint distributions, $p(g_{LIG} | y)$, to determine the associated posterior probability distributions of future AIS contributions to sea-level rise, following Eqn. (7). Differences between these example constraints illustrate how alternative specifications and interpretations of LIG AIS mass loss can influence projections of future sea-level rise. Figure 4a shows the probability density of each constraint distribution, along with the LIG emulator prior distribution, $p(g_{\text{LIG}} | \theta_1, \theta_2)$ (which assumes a uniform probability over the model parameter space, as discussed above).

DeConto et al. (2020) uniform distribution (**D20-U**): The uniform constraint of 371 DeConto et al. (2020), $\mathcal{U}(3.1\mathrm{m}, 6.1\mathrm{m})$, is narrower and lower than that of DeConto and 372 Pollard (2016). The primary difference is that the timing of the LIG AIS mass loss peak 373 is assumed to peak earlier, which affects the constraint derivation; we discuss the impli-374 cations of LIG sea-level chronology in detail in section 3.3. The D20-U constraint dis-375 tribution is derived assuming AIS mass loss peaked in the early-LIG, concurrent with 376 global mean sea-level estimates of 6 ± 1.5 m from Dutton, Webster, et al. (2015). Sub-377 tracting off a small Greenland ice-sheet contribution in the early-LIG (1 m, Goelzer et 378 al., 2016; Dahl-Jensen et al., 2013; Helsen et al., 2013) and a thermosteric rise of 0.4 m 379 (McKay et al., 2011), and neglecting early-LIG mountain glacier melt, the residual AIS 380 contribution is estimated as 3.1–6.1 m. Complementing the pass/fail calibration of both 381 DeConto and Pollard (2016) and DeConto et al. (2020), we impose an analogous uni-382 form distribution over 3.1–6.1 m, such that emulated LIG output falling within the con-383 straint is taken as equally likely; emulator output falling outside the constraint is ascribed 384 a probability of zero. 385

DeConto et al. (2020) normal distribution (**D20-N**): Whereas the uniform distribution assumes fixed limits on the LIG constraint but equal probabilities of LIG contributions between 3.1–6.1 m, it is practical to explore the implications of the central value of the estimated LIG distribution being more likely than the bounds. D20-N replaces D20-U with a Gaussian distribution—taking the central value as the mean and the bounds representing 2 standard deviations from the mean—to develop a constraint distribution following $\mathcal{N}(4.6\mathrm{m}, (0.75\mathrm{m})^2)$.

Edwards et al. (2019) uniform distribution (E19-U): The uniform distribution used to constrain the LIG Antarctic contributions in the reanalyses of Edwards et al. (2019) is identical to the calibration of DeConto and Pollard (2016) given by $\mathcal{U}(3.5\text{m}, 7.4\text{m})$. We include this constraint to specifically compare our Bayesian calibrated ensembles with the results of Edwards et al. (2019), which used a similar emulation method but employed history matching rather than Bayesian calibration of the original DeConto and Pollard (2016) ice-sheet model ensemble.

Kopp et al. (2009) time slice at 125 ka (K09-125ka): Kopp et al. (2009) compiled 400 a probability distribution of AIS contributions to sea-level rise (extended by Kopp et al. 401 (2013)) by combining a comprehensive database of proxy observations of LIG sea lev-402 els, an age model, and GP regression. Posterior probability distributions of AIS LIG sea 403 levels were estimated over time by conditioning on local sea-level and age measurements. 404 To generate a simple constraint distribution consistent with the LIG ensemble, we take 405 a time slice at 125 ka (5,000 years after the initial time period of forcing, 130 ka, section 406 2.1). This is an overly simplified interpretation of the link between the ice-sheet emu-407 lator and the posterior LIG AIS mass loss distributions, because it assumes that emu-408 lated peak LIG contributions are representative of the synthesized observational record 409 precisely at 125 ka. 410

Kopp et al. (2009) maximum Antarctic contributions during the LIG (K09-Max-411 **3kyrSmooth**): To examine an alternative link between the ice-sheet model simulations 412 and Kopp et al. (2009) constraints, we generate 2,500 samples from the posterior prob-413 ability distribution of mean global sea level conditioned upon sea-level observations and 414 sampled ages from Kopp et al. (2009). This represents an estimate of the distribution 415 of the global mean sea-level maximum from the model in Kopp et al. (2009). Each sam-416 ple is a realization of the evolution of AIS sea-level contributions during the LIG (be-417 tween 129–114 ka). Because these samples can be noisy in time, we smooth each sam-418 ple with a 3 kyr-window boxcar filter (other smoothing windows were explored, but here 419 we focus on 3 kyr for brevity). The constraint distribution is then constructed from the 420 peak (global maximum) Antarctic sea-level contribution of each smoothed sample (as-421 suming each is equally likely), so that it shares an interpretation with the ice-sheet em-422 ulator (section 2.1). 423

424

We also explore two sets of hypothetical LIG constraints.

High and low distributions (LIG AIS<3.5 m and LIG AIS>6 m): We prescribe a set of hypothetical relatively high and relatively low constraints, given by $\mathcal{U}(6.0m, +\infty)$ and $\mathcal{U}(-\infty, 3.5m)$, respectively. The resulting posteriors show how projections of future AIS mass loss could improve if there were a reliable upper or lower bound on LIG AIS mass loss estimates at the margins of the LIG prior distribution.

Sensitivity to reduced uncertainties in LIG estimates (Narrower D20-U): To ascertain how future projections of AIS mass loss could be affected by reduced uncertainties in LIG constraint distributions or improved LIG estimates, we gradually reduce the
range of the D20-U constraint by 10%, 25%, 50%, 75%, and 90% and assess the resulting posterior distributions; the central value (4.7 m) of each constraint is identical to that
of D20-U. Physically-based observational constraints, following a similar narrowing method,
are the focus of the discussion in section 3.3.

For each LIG constraint distribution, we find the associated likelihoods of the model parameters and the posterior probability distributions of projected future AIS contributions to sea-level rise following equations (5) and (7). These constraints are not intended to be exhaustive, but rather illustrative of a range of current or potentially-improved LIG constraints and their usefulness for informing future projections. An advantage of the Bayesian framework is that any specified constraint *y* may be assessed. Note that a uniform constraint distribution broader than the LIG emulator prior will not inform the posteriors of model parameters or future projections.

445 **3 Results**

446

3.1 Conditional Probability Distributions

Figure 4b shows the conditional posterior probability densities of RCP8.5 scenario 447 AIS mass loss in 2100 (contoured on a log-scale), assuming the LIG peak AIS sea-level 448 contributions were known to within 10 cm. Along each column of the horizontal axis (x449 values) the densities sum to one, representing the probability distributions of future AIS 450 mass loss, p_x , in 2100 as a function of the associated 10-cm-wide uniform LIG constraint 451 distributions, y_x (section 2.4). Conditional posterior probability densities in 2150 (Sup-452 porting Information Figure S6) have a similar structure. Figure 4b summarizes the ef-453 ficacy of the Last Interglacial for informing this ice-sheet model's projections of future 454 sea-level rise. 455

The posterior marginal probability distributions of CLIFVMAX and CREVLIQ 456 show the related dependencies of model parameter likelihoods as a function of LIG con-457 straints (Figure 5). The marginal probabilities, $p(\theta_1 \mid \theta_2, y)$ and $p(\theta_2 \mid \theta_1, y)$ are com-458 puted by finding the density of each model parameter as a function of the LIG constraint 459 y_x , integrating over the other model parameter, and normalizing such that along each 460 column of x densities sum to one. Comparison between Fig. 4b and Fig. 5 demonstrates 461 how each LIG estimate informs projections of future AIS mass loss by constraining ice-462 sheet model parameters. 463

LIG contributions are relatively more informative on the extreme margins of the 464 prior distribution than in the interior (Fig. 4, cf. black curve of Fig. 4a). At relatively 465 high and low ends of the prior, there are fewer combinations of ice-sheet model param-466 eter values that produce these sea levels than in the interior (Fig. 5), leading to narrower 467 posteriors in future projections. At the high end of LIG AIS mass loss (>6 m), CLIFV-468 MAX values always exceed 7.5 $\frac{\text{km}}{\text{yr}}$ and CREVLIQ values are likewise relatively high (Fig. 469 5), suggesting MICI—driven by substantial meltwater-driven hydrofracturing and removal 470 of buttressing ice shelves—is important for reaching high LIG losses in this model. Nar-471 row posteriors at the low end of LIG AIS mass loss (<3.5 m) are associated emulator 472 outputs which have little or no mass loss from MICI in this model, i.e. CLIFVMAX<1 473 $\frac{\mathrm{km}}{\mathrm{m}}$ (Fig. 5). We further explore specific future projection posterior distributions asso-474 ciated with these relatively high and low LIG constraints in section 3.2. 475

Conditional RCP8.5 posterior distributions in 2100 associated with intermediate 476 values of LIG AIS mass loss are more broad than at the margins. Even if LIG AIS mass 477 loss were known precisely to within 10 cm, if that value was between 4 and 5.5 m then 478 there would remain a ~ 50 cm range in 2100 projections. For instance, when the LIG con-479 tribution is 4.2 m, the associated posterior 95% credible interval in 2100 is 15-65 cm. 480 This broad range in future projections after applying a precise LIG constraint results 481 from the contrasting sensitivities of the LIG and RCP8.5 to parameter configurations 482 (Supporting Information Figure S2). The LIG AIS mass loss prior distribution is multi-483 modal (Fig. 4a) indicating that different sectors of the Antarctic ice sheet have been com-484 pletely lost; total mass losses in these individual modes are then insensitive to small changes 485 in parameter values, as seen in the regions of the parameter space which have nearly con-486 stant sea-level contributions (Fig. 2a). Comparing with Fig. 5a shows there is a wide 487 range of CLIFVMAX values which result in LIG sea-level contributions between 4 and 488 6 m. But RCP8.5 future AIS mass losses are most sensitive to the CLIFVMAX value 489

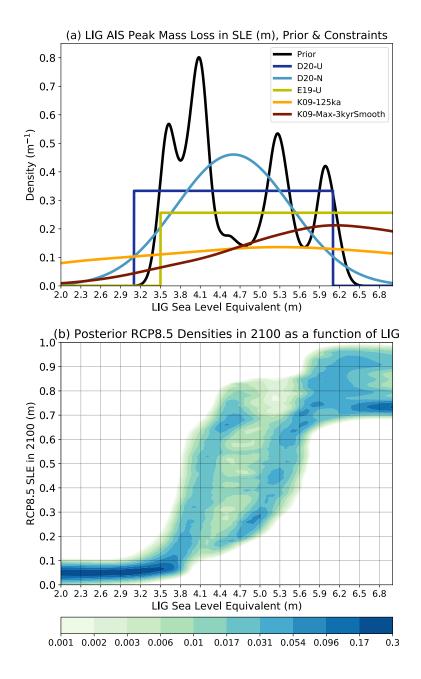


Figure 4. (a) Last Interglacial emulated prior (black curve) and specified constraint (blue, yellow, orange, and red lines curves) probability distributions of Antarctic mass loss in sea-level equivalent (m). (b) Conditional posterior probability densities of Antarctic mass loss in 2100 projected under RCP8.5 forcing (in sea-level equivalent), normalized and plotted as a function of Last Interglacial AIS mass loss in sea-level equivalent (discretized with 10-cm-wide bins, see text).

when CREVLIQ>15 $\frac{m}{(m \text{ yr}^{-1})^2}$ (Fig. 2), and thus have exhibit broad posterior distributions when when LIG sea-level contributions are between 4 and 6 m. LIG contributions scale gradually with CREVLIQ values until CREVLIQ>105 $\frac{m}{(m \text{ yr}^{-1})^2}$, and then LIG con-

⁴⁹³ tributions are associated with broader ranges of CREVLIQ over $105-195 \frac{\text{m}}{(\text{m yr}^{-1})^2}$ (Fig.

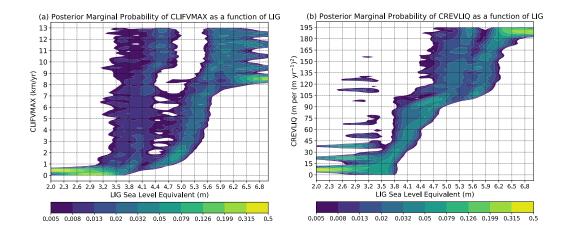


Figure 5. Posterior marginal probability distributions of (a) CLIFVMAX and (b) CREVLIQ, normalized and plotted as a function of Last Interglacial AIS mass loss in sea-level equivalent (discretized with 10-cm-wide bins, see text).

⁴⁹⁴ 5b); future AIS mass loses are relatively insensitive to CREVLIQ in this region of model ⁴⁹⁵ parameter space (Fig. 2).

These varying responses to model parameter configurations most clearly affect RCP8.5 496 projections when the median in 2100 drops from 63 to 32 cm as LIG contributions in-497 crease from 4.6 to 4.8 m (Fig. 4b. This non-intuitive result suggests that in some regions 498 of the parameter space, the model-simulated equilibrium LIG AIS mass loss is influenced 499 by a different physical process than transient RCP8.5 losses. By 2100, RCP8.5 air tem-500 perature anomalies are ~ 2 degrees warmer than the applied LIG forcing and are still in-501 creasing, leading to accelerating AIS mass loss through MICI that is strongly influenced 502 by CLIFVMAX. In contrast, the applied LIG forcing is cooler and fixed, and the LIG 503 ice-sheet equilibrates by losing mass more gradually over a 5,000 period. The slower equi-504 librium response permits CREVLIQ to play a larger role in LIG AIS mass loss, direct-505 ing which sectors of ice eventually become unstable through shelf hydrofracturing over 506 the prolonged period of anomalously warm temperatures (Figure 1). 507

Conditional posterior distributions $(p_x, \text{Fig. 4})$ are a powerful and novel tool for illustrating the links between ice-sheet model projections and paleo observational records. If, for instance, a field measurement showed that LIG AIS contributions were > 5 m, then the densities in Fig. 4 may be integrated across 5 m $\leq x \leq +\infty$ to show that the range of projected RCP8.5 AIS mass loss in 2100 is ~0.2–1.0 m, with a median of 65 cm. We discuss how conditional distributions may be used in the context of particular paleo sealevel observations in section 3.3.

515

3.2 Future Projections Given Specific LIG Constraint Distributions

Posterior probability distributions of AIS sea-level contributions in 2100 and 2150 516 conditional on each LIG constraint distribution, following Eqn. (7), are shown in Fig-517 ure 6, along with the prior LIG distribution and histograms of the training simulations. 518 Distributions are produced with kernel density estimation assuming a Silverman band-519 width (Silverman, 1986) reduced by 80% to prevent over-smoothing. Distribution quan-520 tiles are presented in Table 1. For reference, the likelihood functions (i.e. $p(y \mid \theta_1, \theta_2))$ 521 of CREVLIQ/CLIFVMAX model parameter sets associated with each LIG constraint 522 distribution are shown in Supporting Information Figure S5. 523

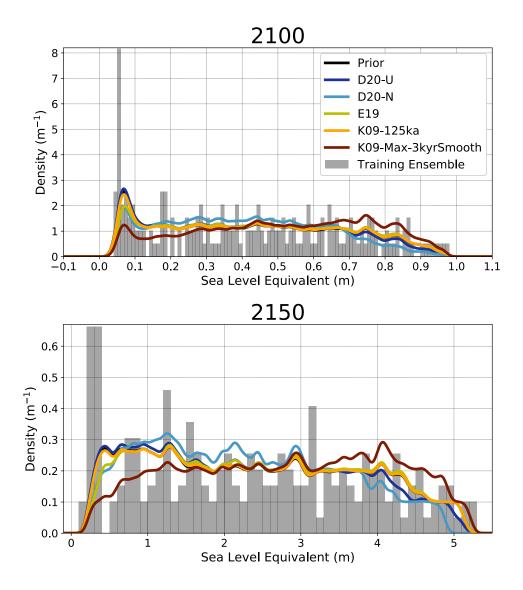


Figure 6. Projected probability distributions of Antarctic ice-sheet mass loss in sea-level equivalent (m) in (a) 2100 and (b) 2150, under RCP8.5 forcing. Distributions are from 10,000 emulator samples and smoothed with kernel density estimation. Shown are the prior RCP8.5 distribution with no constraints (black curves), and distributions under specified Last Interglacial constraints (blue, yellow, orange, and red curves, cf. Figure 4). The ice-sheet model training ensemble is plotted as a histogram scaled for comparison.

From 1990 to 2100, specific LIG constraints (section 2.4) do not very effectively narrow uncertainties in future projections. Quantiles of the prior, D20-U, E19-U, and K09-125ka distributions in 2100 are all within 5 cm (Table 1). D20-N weights the distribution towards the lower end of the projections, dropping the 95th percentile (relative to the prior) by 7 cm. The K09-Max-3kyrSmooth distribution re-weights the projection distribution towards the upper tail (cf. Fig. 4a), raising the median and 75th percentiles by 8–10 cm.

531 CREVLIQ/CLIFVMAX likelihood functions (Supporting Information Figure S5) 532 show that there is no set of parameter values which are consistently unlikely across all

2100 Quantiles	Prior	D20-U	D20-N	E19-U	K09-125ka	K09-Max-3kyrSmooth
5	0.07	0.07	0.07	0.07	0.07	0.09
25	0.20	0.20	0.23	0.23	0.21	0.31
50	0.42	0.40	0.40	0.44	0.43	0.52
75	0.64	0.61	0.58	0.65	0.64	0.72
95	0.85	0.83	0.78	0.85	0.85	0.88
2150 Quantiles	Prior	D20-U	D20-N	E19-U	K09-125ka	K09-Max-3kyrSmooth
5	0.44	0.44	0.51	0.52	0.46	0.63
25	1.21	1.17	1.23	1.30	1.24	1.63
50	2.31	2.21	2.18	2.39	2.32	2.81
75	3.54	3.38	3.22	3.58	3.53	3.88
95	4.65	4.56	4.38	4.66	4.64	4.79

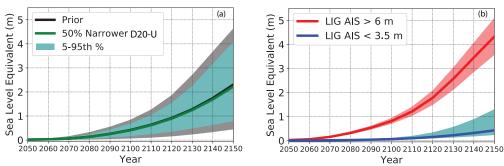
Table 1. Quantiles of projected Antarctic ice-sheet mass loss in sea-level equivalent (m) in 2100 and 2150; each emulated distribution other than the prior is constrained using a specified Last Interglacial probability distribution (section 2.4).

LIG constraints. Thus, interpretations of which regions of model parameters space are 533 viable (and hence, deductions about the related physical processes) will depend entirely 534 on the specific LIG constraint applied. For instance, the E19-U constraint indicates that 535 the least likely parameter sets are where CLIFVMAX values are small (Fig. S5d): about 536 2.6% of the posterior density is is associated with CLIFVMAX $\leq 0.5 \frac{\text{km}}{\text{vr}}$, compared with 537 3.8% if the probabilities were uniformly likely in this region. This result implies that MICI 538 is not ruled out by this constraint, in contrast to the interpretation of Edwards et al. (2019), 539 because under E19-U CLIFVMAX $\leq 0.5 \frac{\text{km}}{\text{yr}}$ is only a little more likely than not. As we drop to even lower values of CLIFVMAX (e.g. 0.1 $\frac{\text{km}}{\text{yr}}$), the emulated outputs conditioned 540 541 on E19-U becomes less and less likely (not shown). However, there remain parameter 542 sets with non-zero likelihoods near CLIFVMAX=0, especially at higher CREVLIQ val-543 ues (Fig. S5d), such that a no-MICI solution also cannot be excluded. The main differ-544 ences between this study and Edwards et al. (2019) are the ensemble structure, as well 545 as enhanced atmospheric climatologies and a reduced ocean bias correction in the train-546 ing simulations (section 2.1). Overall, none of the existing LIG constraints can exclude 547 MICI as a primary loss mechanism (Fig. S5), which requires an estimated LIG AIS mass 548 loss of less than ~ 3.5 m. 549

The LIG emulator prior nearly coincides with (or in some cases is narrower than) 550 the existing LIG constraint distributions. Whereas this indicates that the ice-sheet model 551 is able to faithfully reproduce peak LIG AIS mass losses, it also confirms an existing chal-552 lenge found by Edwards et al. (2019): current LIG estimates are not strong constraints 553 on this ice-sheet model's parameter likelihoods and future projections. 554

In light of this finding, we investigate how LIG constraints *could* inform future pro-555 jections of AIS mass loss and sea-level rise if they were improved, using the sensitivity 556 test constraints outlined in section 2.4; the resulting posteriors are presented in Figure 557 7. In particular, LIG constraints with gradually-reduced ranges have a limit to how ef-558 fective they can be for informing future projections of Antarctic contributions to sea-level 559 rise (Supporting Information Figure S10). 560

Narrowing the D20-U constraint by 50% results in a posterior distribution high-561 lighting an important property of LIG constraints: they become more effective over time 562



Probability Distributions of AIS Mass Loss in SLE (m), conditional on hypothetical improved LIG constraints

Figure 7. Posterior probability distribution medians (solid lines) and 5th-95th percentiles (shading) of AIS mass loss in sea-level equivalent (m) projected under RCP8.5 forcing over 2050-2150. (a) Posterior constrained assuming the D20-U constraint was 50% narrower (green curve/shading) alongside the prior distribution reproduced from Fig. 3 (black curve/shading).
(b) Posteriors constrained assuming LIG AIS sea-level contributions were <3.5 m (blue curve/shading) or >6 m (red curve/shading).

(Fig. 7a). Until ~ 2050 the prior and constrained distribution are nearly identical, then 563 their distributions begin to diverge. AIS mass loss projected by this model becomes in-564 creasingly driven by cliff collapse (or the lack thereof) around 2060, and the LIG esti-565 mate begins effectively constraining both the most unstable parts of the distribution (which 566 have the highest CLIFVMAX values, cf. Figure 1b) and the least. Figure 7a shows that 567 because these solutions diverge over time, the LIG constraint becomes more informative 568 on the absolute values of sea-level contributions over time. In 2100, the 95% credible in-569 terval of the posterior from the 50% narrower D20-U constraint is 14–68 cm, compared 570 to the 7–85 cm interval of the prior (Table 1). In 2150 the constrained 95% credible in-571 terval is 0.71–4.07 m, compared with 0.44–4.65 m from the prior. Thus, even if observation-572 based LIG constraints are of little utility for reducing sea-level projection uncertainties 573 in the near term, they become more meaningful as projections diverge. 574

We also investigate how projected AIS mass loss could change if there were a known 575 upper or lower bound on the LIG estimate. Figure 7b shows how hypothetical estimates 576 of relatively low (<3.5 m) or relatively high (>6 m) LIG AIS mass loss could strongly 577 influence future projections. If the LIG contributions were known to be <3.5 m, the me-578 dian and associated 95% credible interval of RCP8.5 projections in 2100 would be 7 cm 579 and 4-15 cm, respectively. Likewise, if the LIG contributions were known to be >6 m, 580 the associated median and 95% credible intervals of 2100 projections would be 81 cm and 581 68–95 cm, respectively. 582

A striking feature of the posterior distribution associated with LIG AIS mass loss <3.5 m constraint (blue curve/shading in Fig. 7b) is the positive skew emerging over time. nstable ice-sheets which retreat on a reverse-sloping bed have a greater loss rate among ensemble members which have lost more mass than the rate among members which have lost less mass (Robel et al., 2019); this positively skews the mass loss distribution (similarly shown by Nias et al. (2019)).

Notably, interpreting the total AIS mass loss distribution is complicated by different sectors losing mass at different times and rates. As sectors of the ice-sheet lose all of their mass the positive skew disappears (Robel et al., 2019), as seen in the multiple modes of the LIG prior distribution (Fig. 4). The bimodal positively-skewed posterior distribution associated with the 90% narrowed D20-U constraint (Fig. S10) and the weakly skewed prior distribution of RCP8.5 mass loss in 2100 (skew of +0.18, Fig. 6) also de pict this complex behavior.

In contrast, the posterior distribution associated with LIG AIS <3.5 m well-illustrates how different sensitivities to instability can drive skew across an ensemble (Fig. 7b). In 2080 the emulated samples associated with higher model parameter values become unstable, and the skew increases from near zero to +1.8 by 2110; after this initial period of instability the skew remain strongly positive (> +1.3). This behavior also explains how different sensitivities to instability leads to posteriors diverging over time.

602

3.3 Relevance for Paleo Sea-Level Observations

We have used conditional posterior probability distributions (Fig. 4b-5) to show 603 how the LIG informs this model's projections of AIS mass loss. Our results also show 604 how ice-sheet model parameters are linked to estimates of LIG AIS sea-level contribu-605 tions. Concurrently, any improvements in understanding physical processes in the ice-606 sheet will also indicate which LIG contributions are most likely. A main benefit of our approach is that it may inform future research and observational efforts to understand 608 LIG sea levels. Here we apply our emulation and Bayesian updating framework to par-609 ticular paleo sea-level observations, to investigate how assumptions about LIG ice-sheet 610 chronology or improved LIG observations could influence future projections. 611

Determining sea levels during the LIG and closing its peak sea-level budget are chal-612 lenging problems. Field observations have large uncertainties, related to measurement 613 error or confounding processes such as glacial isostatic adjustment (GIA) or mantle dy-614 namic topography (DT) (Hibbert et al., 2016; Austermann et al., 2017; Dendy et al., 2017; 615 Rohling et al., 2017; Capron et al., 2019). Still under debate is whether the LIG exhib-616 ited variability with multiple global sea-level peaks (Kopp, Dutton, & Carlson, 2017; Bar-617 low et al., 2018), indicating short-term fluctuations (e.g., Rohling et al., 2008), or dis-618 tinct out-of-phase mass losses between the Greenland and Antarctic ice sheets (Dutton, 619 Carlson, et al., 2015). Lacking sufficient near-field evidence, the AIS is typically invoked 620 as an uncertain residual contributor. Yet estimated Greenland ice-sheet mass losses dur-621 ing the LIG also have a wide range of interpretations and central estimates (Dutton, Carl-622 son, et al., 2015, their Figure 3), so it is difficult to disentangle the relative roles of Green-623 land and Antarctica. 624

Our method is able to show how these uncertainties in proxy-based reconstructions 625 of LIG sea levels reflect on uncertainties in future AIS contributions to sea-level rise. Here 626 we calculate the 95% credible intervals of AIS sea-level contributions under RCP8.5 forc-627 ing in 2100, varying the LIG AIS uncertainty according to three different scenarios for 628 GMSL. Scenarios are derived from a milestone study by Dutton, Webster, et al. (2015), 629 who used sea-level proxies in the Sevchelles to constrain polar ice sheet mass losses dur-630 ing the LIG. Scenarios are developed to illustrate how individual components of uncer-631 tainty in LIG estimates contribute to projection uncertainties; thus they are not directly 632 related to any of the holistic projections in section 2.4 (though they are most closely re-633 lated to the proxy-driven estimates of the K09-Max-3kyrSmooth constraint). We note 634 that this is a close-to-ideal case study, because Seychelles GIA and DT predictions have 635 relatively small uncertainties. All uncertainties are 1σ and assumed to follow a normal 636 distribution. The scenarios are: 637

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1. Relative sea level coinciding with the highest in situ coral measured by Dutton, Webster, et al. (2015) with high-accuracy surveying techniques. The coral assemblage is interpreted as "likely intertidal" and its elevation is 8±0.2 m above modern sea level.

2. While scenario 1 is illustrative of very small uncertainties in LIG sea-level estimates, it is also incomplete because it does not account for departures from eustasy due

- 644to GIA and sea-level fingerprints. These were calculated by Dutton, Webster, et645al. (2015) using model results from Dutton and Lambeck (2012) and Hay et al.646(2014). Using these estimates, Dutton, Webster, et al. (2015) calculated LIG GMSL647rise was 7.6±1.7 m.
- Austermann et al. (2017) showed that mantle DT and ocean subsidence effects must
 be accounted for (each with large uncertainties), before GMSL can be calculated
 from field data. Here we use their model results for the Seychelles to illustrate how
 accounting for DT and ocean subsidence influences paleo GMSL estimates and their
 uncertainties. Subtracting ocean subsidence (-1.4 m) and DT as modelled in Austermann
 et al. (2017) (-0.8±1.8m) from scenario 2, we calculate LIG GMSL rise was 9.2±2.5
 m.

For each scenario, we calculate LIG AIS sea-level contributions by subtracting the 655 contributions of the Greenland Ice Sheet (GrIS), mountain glaciers and thermal expan-656 sion following the budgetary approach of Dutton, Carlson, et al. (2015). First, we as-657 sume that the GrIS and thermosteric contributions to LIG sea level are known (2 m and 658 1 m, respectively), with no error. We compare with the assumption that, instead, GrIS 659 contributed $2 \text{ m} \pm 1.5 \text{ m}$ to LIG GMSL, as shown in Dutton, Carlson, et al. (2015, Fig-660 ure 3). We set the contributions from mountain glaciers and thermosteric expansion to 661 1 m (Dutton, Carlson, et al., 2015), with arbitrary uncertainties of ± 0.2 m. 662

This exercise (Figure 8A–C) shows that, regardless of AIS mass loss during the LIG, 663 any LIG constraint can only substantially reduce uncertainties in this ice-sheet model's projected AIS sea-level contributions if the following two conditions are met: 1) sea-level 665 data and departures from eustasy are known with $\pm 1\sigma$ uncertainties of a few decime-666 ters and 2) GrIS and thermal expansion uncertainties are small (<1 m). Constraints on 667 other models could be stronger or weaker, depending on the particular relationship be-668 tween their parameters and ice-sheet evolution. This could be considered discouraging 669 for the communities working on these topics, i.e. the large intrinsic uncertainties that 670 characterize GrIS and proxy-based ESL estimates may seem insurmountable. We instead 671 note that this knowledge gap provides a unique opportunity to do innovative, timely and 672 important research that feeds directly into the open research questions in the paleo sea-673 level and ice-sheet communities (Capron et al., 2019). 674

Results further suggest that the storyline of LIG sea-level evolution has a strong 675 influence on whether the LIG is able to constrain future sea-level changes. Greenland 676 and Antarctic sea-level contributions are inextricably linked during the LIG: knowledge 677 or evidence about one will inform the other, as shown by assuming LIG total GMSL es-678 timates of 7.5 ± 0.5 m in Figure 8D. Resulting relatively high or low AIS estimates are 679 similar to the hypothetical constraint posteriors in Fig. 7b. The links between the ice 680 sheets imply that 1) efforts to improve estimates of GrIS can directly inform future AIS 681 sea-level projections, and that 2) the timing of LIG GrIS loss compared with LIG AIS 682 loss is pivotal (Kopp, Dutton, & Carlson, 2017). Storylines where GrIS and AIS mass 683 losses peak simultaneously have a very different interpretation from those where ice-sheet losses peak several thousand years apart (Rohling et al., 2019) and imply different AIS 685 projected contributions to future sea-level rise. 686

The mismatch between transient future ice-sheet mass loss and peak LIG mass loss 687 limits the effectiveness of the LIG as a constraint. Historically, studies of the LIG have 688 focused primarily on gathering geological evidence of peak LIG GMSL, in part because these are less challenging measurements to make in the field. But comparing the mod-690 eled LIG and future timeseries in Fig. 1 shows the transient onset of LIG losses most 691 closely mirrors future losses, with similar dependencies on model physics and parame-692 ters. Both improved transient (rather than equilibrium) ice-sheet model runs and qual-693 ity estimates of the LIG onset period are highly desirable for constraining AIS changes 694 and future sea-level rise. Sampling biases and the requirement for precise chronologies 695

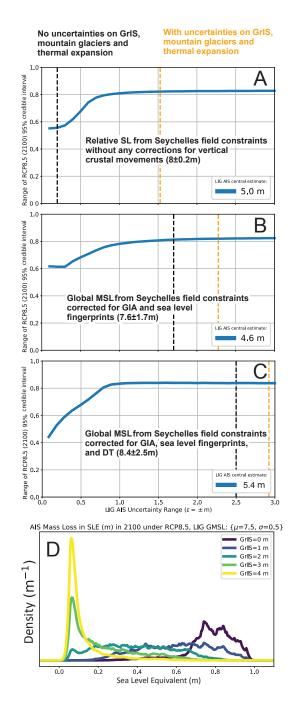


Figure 8. (A–C) Range of 95% credible intervals of future AIS sea-level contributions in 2100 under RCP8.5 forcing (m) conditional on three scenarios of LIG AIS contributions with a central estimate (blue curves) and Gaussian 1σ uncertainties (see text); combined total GrIS and thermosteric mean contributions are taken to be 3 m. Black dashed curves show the total field uncertainties excluding those from GrIS and thermosteric contributions; orange dashed curves include GrIS and thermosteric uncertainties. (D) Probability density functions of AIS contributions in 2100 under RCP8.5 forcing, conditional on LIG global mean sea levels of 7.5±0.5 m, and mean GrIS sea-level contributions varying over 0–4 m.

have to this point thwarted these efforts. But as a coherent picture of LIG sea levels emerges,
 combining LIG constraints with probabilistic distributions from ice-sheet models—as this
 study has done—will improve the precision of future sea-level projections.

⁶⁹⁹ 4 Summary and Conclusions

This study applied Bayesian methods to emulate and calibrate an ice-sheet model 700 to evaluate the ability of LIG AIS mass loss to constrain sea-level rise projections un-701 der RCP8.5 forcing. Ice-sheet model training ensembles were developed considering the 702 marine ice-cliff instability (MICI) process, with ensembles spanning over a broader range 703 of model parameter values than previously explored (DeConto & Pollard, 2016). A set 704 of proposed specific LIG constraint distributions (several of which have been previously 705 used to calibrate ice-sheet model projections) were also employed to explore their effec-706 tiveness for constraining future AIS mass loss. The emulator was combined with LIG 707 paleo sea level field measurements to illustrate how improved LIG observational estimates 708 could potentially narrow uncertainties in future Antarctic ice sheet projections. 709

Results explicitly show how estimates of LIG AIS mass loss could inform which pa-710 rameter values are most likely in this ice-sheet model, which in turn informs future pro-711 jections (2000–2150). However, LIG AIS sea-level contributions themselves are not well 712 constrained (e.g., Düsterhus et al., 2016), and not all LIG estimates inform future pro-713 jections equally. For instance, if LIG contributions were known to be <4 m, then MICI 714 is very unlikely to be a primary loss mechanism in the future Antarctic mass loss pro-715 jected by this ice-sheet model. Likewise, if LIG contributions were known to be >6 m, 716 the ice-sheet model emulator projects that substantial future mass losses associated with 717 MICI are likely. In either case, uncertainties in future projections from this model would 718 narrow considerably, but some uncertainty would remain because peak LIG Antarctic 719 mass losses have somewhat different sensitivities to ice-sheet model parameters than fu-720 ture changes do. LIG observations which inform the upper and lower limits of the mod-721 eled prior distribution would be valuable for improving future projections (in the con-722 text of this specific model and ensemble). Because ice-sheet model parameter likelihoods 723 and LIG sea-level estimates are closely linked, evidence of constraints on one informs the 724 other. For instance, if there are indications that MICI is not a viable loss mechanism, 725 results here indicate that peak LIG Antarctic sea-level contributions were likely <4 m. 726

Consistent with the findings of Edwards et al. (2019), posterior distributions cal-727 ibrated with a Bayesian approach show that currently best-available LIG constraints (which 728 have previously used to calibrate ice-sheet model projections, e.g., DeConto & Pollard, 729 2016; Edwards et al., 2019) are inadequate to restrict a wide range of model parameter 730 values. Consequently, this study can neither confirm nor exclude MICI as a primary driver 731 of AIS mass loss. However, because the ice-sheet model projections of future AIS mass 732 loss diverge over time—especially after 2060 when MICI begins strongly accelerating mass 733 loss—LIG constraints which are uninformative in the near term become more informa-734 tive on longer time scales (through 2150). 735

Conditioning future AIS mass losses on peak LIG sea level exposes direct links be tween paleo sea-level reconstructions and future sea-level rise. Improvements in field mea surements, reductions in uncertainties from glacial isostatic adjustment or dynamic to pography, and better chronologies of Antarctic and Greenland ice-sheet retreat during
 the LIG could all reduce uncertainties in future projections. These results provide strong
 motivation and support for continued collaborations between the paleo sea level and ice sheet communities.

Past studies of LIG sea level have focused primarily on peak global mean sea levels, as they are more readily and reliably measurable, and because it is difficult to establish accurate and precise sea-level chronologies (Dutton, Carlson, et al., 2015). But

peak LIG Antarctic ice-sheet mass losses are not necessarily representative of the tran-746 sient changes the Antarctic ice-sheet may experience in the coming decades and centuries. 747 This mismatch between the future and the past limits the applicability of LIG constraints 748 on future Antarctic mass loss. Even if LIG Antarctic contributions were known precisely 749 $(\pm 5 \text{ cm})$, there would still be decimeter-scale uncertainties in projections of future Antarc-750 tic contributions to sea-level rise. An alternative approach could be to pursue additional 751 field observations detailing or inferring Antarctic changes during the LIG onset, to pro-752 vide improved constraints on projections of future AIS contributions to sea-level rise. Im-753 proved LIG chronologies and observations of LIG Greenland ice-sheet changes could also 754 reduce future projection uncertainties. 755

This study considered a single ice-sheet model and explored the MICI process. Other 756 processes (such as the oceanic melt factor, basal sliding coefficients, the timescale of iso-757 static rebound, etc.), other considerations (such as the Last Interglacial forcing applied 758 or emissions scenario), or a broader model ensemble prior (e.g. over more parameters 759 values and more unique parameters using advanced computational approaches, such as 760 a Latin Hypercube or Sobol sequence, or a "grand-ensemble" design like that suggested 761 by Edwards et al. (2019)) are beyond the scope of this work, but could be explored with 762 the methodological approach developed here. 763

There is a maximum possible constraint that the LIG can provide to inform ice-764 sheet model sensitivities to climate warming and future sea-level rise (e.g., Capron et al., 765 2019, and references therein). Uncertainties in ice-sheet physics and observational ev-766 idence currently limit the capability of the LIG to meaningfully constrain sea-level rise 767 projections over the coming century. Despite these limitations, this study has specifically 768 illustrated how models, emulation, and Bayesian calibration may be combined to inter-769 pret and guide paleo sea-level observational constraints. A major ongoing research ob-770 jective is to continue strategically gathering field observations, in order to improve un-771 derstanding and estimates of LIG sea levels. Such improvements, along with continued 772 integration with modeling and statistical methods, will increase confidence in the physics 773 and projections of Antarctic contributions to sea-level rise over the coming centuries. 774

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Supporting Information for "Could the Last Interglacial Constrain Projections of Future Antarctic Ice Mass Loss and Sea-level Rise?"

Daniel M. Gilford^{1,2}, Erica L. Ashe², Robert M. DeConto³, Robert E.

Kopp^{1,2}, David Pollard⁴, Alessio Rovere⁵

¹Institute of Earth, Ocean, and Atmospheric Sciences, Rutgers University, 71 Dudley Road, Suite 205, New Brunswick, NJ 08901,

USA.

²Department of Earth and Planetary Sciences, Rutgers University, Piscataway, NJ, USA.

³Department of Geosciences, University of Massachusetts, Amherst, MA, USA.

⁴Earth and Environmental Systems Institute, Pennsylvania State University, University Park, PA, USA.

⁵MARUM, Center for Marine Environmental Sciences, University of Bremen, Germany.

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Introduction

This supporting information provides underlying details on the ice-sheet model ensemble, emulator construction, validation, and sensitivity tests, as well as supplemental figures of timeseries color-coded by CREVLIQ, comparisons between the Last Interglacial and RCP8.5 ensembles across the model parameter space, conditional posterior distributions in 2150, and ice-sheet model parameter likelihoods as a function of LIG constraint distribution. We note that the ice-sheet model ensembles are constructed with a model version updated since DeConto and Pollard (2016), but predating that of DeConto et al. (2020). As such, the results herein are not representative of the most current results with the latest physical model, but are illustrative of how ice-sheet models may be combined with statistical/machine learning methods and paleoclimate evidence to (a) constrain projections of future Antarctic ice-sheet contributions to sea-level rise, and to (b) identify how improved paleo sea level estimates could inform projections. A glossary of key study terms is included at the end, for reference.

CLIFVMAX $\left(\frac{\text{km}}{\text{yr}}\right)$	CREVLIQ $\left(\frac{m}{(myr^{-1})^2}\right)$
0	0
1	15
2	30
3	45
4	60
5	75
6	90
7	105
8	120
9	135
10	150
11	165
12	180
13	195

Table S1. Ice-sheet model parameter values used to construct a 14×14 grid composing 196 members for the Last Interglacial and RCP8.5 scenario ensembles.

Table S2. Optimized hyperparameters of the GP models (Eqn. 1–3) found by maximizing the log-likelihoods, given the training ensembles.

Ensemble	$\alpha_1^2 \ (m^2)$	ℓ_1^2	$\alpha_2^2 \ (m^2)$	ℓ_2^2	τ (yr)
LIG	17.048	45.698			
RCP8.5	2731.8	2.7567	1.830	0.50121	95.52198

Text S1. Emulator Leave-one-out Analyses

To assess whether the Gaussian process (GP) model emulator accurately mimics the ice-sheet simulator, we perform a leave-one-out (LOO) analysis following a modification of the methodology of Bastos and O'Hagan (2009). We calculate the individual standardized prediction errors as,

$$D_j^I = \frac{z_j - E[f(\theta_1, \theta_2)_j | \mathbf{z}_{\backslash \mathbf{j}}]}{\sqrt{V[f(\theta_1, \theta_2)_j | \mathbf{z}_{\backslash \mathbf{j}}]}}$$
(S1)

X - 4

where $\mathbf{z}_{\backslash j}$ is the vector composed all of training ensemble members in \mathbf{z} except z_j at the *j*th location in model parameter space (i.e. the value with a fixed $[\theta_1, \theta_2]$ from Table S1, removed for the LOO process), and $E[\cdot]$ and $V[\cdot]$ are the expectation (mean function) and variance, respectively, of the optimized emulator conditioned on $\mathbf{z}_{\backslash j}$. For RCP8.5, *f* and $\mathbf{z}_{\mathbf{RCP}}$ are a function of time, and hence D_j^I is also time-dependent. The LIG emulator, $\mathbf{z}_{\mathbf{LIG}}$, and the LIG standardized prediction errors have no time dependency. Errors are shown for the LIG in Figure S3 and the RCP8.5 scenario (in 2000, 2050, 2100, and 2150) in Figure S4.

Standardized errors are expected to follow a standard Student-t distribution. Errors which consistently exceed ± 2 (the 95% credibility interval) indicate a conflict between the emulator and simulator (Bastos and O'Hagan 2009). We find that the LIG and RCP8.5 emulators performs well, with nearly all errors falling within the confidence interval. Emulator skill degrades slightly over the time in the RCP8.5 scenario as the training data sea-levels disperse when instabilities drive mass loss (section 3.2), creating less densely packed training information in time and parameter space. 5/196, about 2.5%, of the errors exceed +2 in 2150. These poorly performing emulator estimates are located near the exterior of parameter space, where θ_1 and θ_2 are high, and there is less surrounding training information to constrain the emulator prediction (behavior which is typical of trained Gaussian process models, Rasmussen and Williams 2006).

Across time and both training ensembles, standardized emulator errors are less than ± 2 in over 99% of points tested. One concern might be whether these errors indicate emulator variances are too large relative to the mean (i.e. whether the model is underconfident), driving low values of D_j^I . The RCP8.5 emulator very accurately predicts relatively small (near-zero) and broadly similar changes in mass loss across the whole parameter space; this contributes to the model's excellent standardized agreement through 2050 (Fig. S4, top panels). As the distribution of

ice-sheet mass begins to diverge around 2060 (Fig. 3) and emulator skill drops marginally (as discussed above), the model evolves toward an error distribution more consistent with the expected standard Student-t distribution. Overall, the time-independent variance of the RCP8.5 emulator is always <0.0004 m² across the model parameter space, such that the model standard deviation is always <2 cm.

The LIG emulator variance is plotted in Figure S7; values span over 0–0.016 m² across the ice-sheet model parameter space. The associated GP model standard deviation is 11 cm on average, $\sim 3\%$ of the range of the LIG emulator output. The model may therefore be slightly underconfident, which could affect our study results/conclusions in two ways. First, a model with too high variance would result in less confidence in model parameters given a specific LIG constraint (i.e. less polarized likelihoods, Fig. S5), so that the LIG is less informative for the MICI process. Second, higher variance results in a broader prior distribution than may be warranted. However, one of the strengths of the Bayesian approach (section 2.3) is the ability both include and quantify the uncertainty of the emulator (as in Fig. S7), so some variance in the final model is justified. Ultimately, the final model described in the main text captures the key behavior of the training data, and had the smallest variances of any model explored (cf. Text S2).

Overall, performance is consistent with that of another recently published ice-sheet model emulator (Edwards et al. 2019, their Extended Data Figure 6), which was trained on a different version of the same ice-sheet model (e.g., Pollard and DeConto 2012). We conclude the emulator is able to accurately predict simulator responses across the LIG and RCP8.5 scenarios with appropriate uncertainties.

Text S2. GP Model Selection and Sensitivity to Covariance Function

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There are infinitely many possible model forms, specifications, optimization targets, etc. to consider for an emulator (Rasmussen and Williams 2006). The "final model" (described in the main text) represents the best model based on several metrics: model simplicity, likelihood maximization, and minimizing of prediction errors (described above in Text S2) and model uncertainty (i.e. posterior variance).

We assessed different covariance forms: squared-exponential functions (sometimes called the radial basis function), nonstationary linear (sometimes called dot-product) functions, and Matérn functions with shape parameters (ν) of $\frac{1}{2}$, $\frac{3}{2}$, and $\frac{5}{2}$. We also evaluated various combinations of these functions, and experimented with specifying them along the individual axes of the training data (θ_1 , θ_2 , and time). For instance, we considered the complex form,

$$K(\theta_1, \theta_2) \sim Linear(\theta_1) * Mat\acute{ern}_{\nu = \frac{5}{2}}(\theta_1) + Linear(\theta_2) * Mat\acute{ern}_{\nu = \frac{5}{2}}(\theta_2) + Mat\acute{ern}_{\nu = \frac{5}{2}}(\theta_1, \theta_2).$$

Trained models produced log-likelihoods similar to (or sometimes even higher than) the final model. But when optimized, each of these models required a variance (fit uncertainty) larger than the final model (Fig. S7) in order to match the training data (cf. Text S2). Under such circumstances, the optimized model is underconfident, and a nugget of 10^{-6} m is a strong requirement that is inconsistent with the optimized model variance. We present one such model as an example below and discuss the implications.

To demonstrate the emulator sensitivity to the choice of covariance function, we specify an alternative set of covariance functions, f_1^* and f_2^* , which replace f_1 and f_2 in Eqn. (??):

$$f_1^*(\theta_1, \theta_2) \sim \mathcal{GP}(0, \alpha_1^2 K_{1,\theta_1}(\theta_1, \theta_1'; \ell_{1,\theta_1}) \cdot K_{1,\theta_2}(\theta_2, \theta_2'; \ell_{1,\theta_2})),$$
(S2)

$$f_{2}^{*}(\theta_{1},\theta_{2},t) \sim \mathcal{GP}(0,\alpha_{2}^{2}K_{2,\theta_{1}}(\theta_{1},\theta_{1}';\ell_{2,\theta_{1}}) \cdot K_{2,\theta_{2}}(\theta_{2},\theta_{2}';\ell_{2,\theta_{2}}) \cdot K_{t}(t,t';\tau)),$$
(S3)

where there are four distinct covariance functions, $K_{i,\theta}$, each with a unique and trainable length scale specified along either CLIFVMAX (θ_1) or CREVLIQ (θ_2), $\ell_{i,\theta}$. Because the model form is

different, the hyperparameters which share an interpretation with Eqn. (1)— α_i and τ —need not have the same optimized values as those of the final model (Table S2). Following the procedure described in sections 2.2–2.3, this alternative model is optimized and conditioned on the training simulations, and its posterior distributions are found conditional on LIG constraints.

The Last Interglacial prior distribution of this alternative model form is presented in Figure S8 alongside the final model prior (reproduced from Fig. 4a) and the LIG training ensemble histogram. The alternative model prior distribution is broader than that of the final model prior distribution, driven by a larger variance. The LIG alternative model's average standard deviation is 25 cm, more than twice that of the final model, which smooths out some of the multi-modal features of the LIG prior distribution. The training ensemble exhibits a multi-modal distribution (more consistent with the prior of the final model), suggesting the alternative model contributes less information about AIS mass loss from individual sectors than indicated by the original ice-sheet model simulations.

Likewise, the alternative model of the RCP8.5 emulator has greater uncertainty, with a timeconstant standard deviation of ~ 5 cm and a width of the 95% credibility interval between 2000 and 2060 of 20 cm (a period where the full range of simulated mass loss is 0–7.7 cm). Given these increased uncertainties, emulated behavior such as the instability-driven skew in Fig. 7b (given a relatively low LIG constraint) disappears, suggesting the alternative model is less physical. The alternative model posterior distributions of RCP8.5 AIS mass loss as a function of LIG constraints are shown in Figure S9. Comparing with Fig. 4b, posterior distributions have substantially broader projections if the LIG was known precisely (to within 10 cm). This degrades the informative power of LIG constraints on the margins of the prior distribution (i.e. high or low values, Fig. 7b), because the baseline uncertainty more than doubles. Hence, the final model more accurately captures the multi-modal behavior of the LIG training ensemble and is more precise in its predictions.

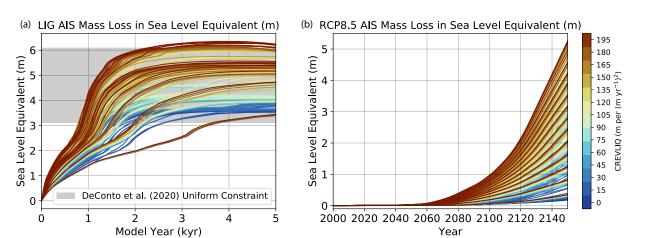


Figure S1. As in Fig. 1, except timeseries are color-coded by their CREVLIQ values over $0-195 \frac{\text{m}}{(\text{myr}^{-1})^2}$.

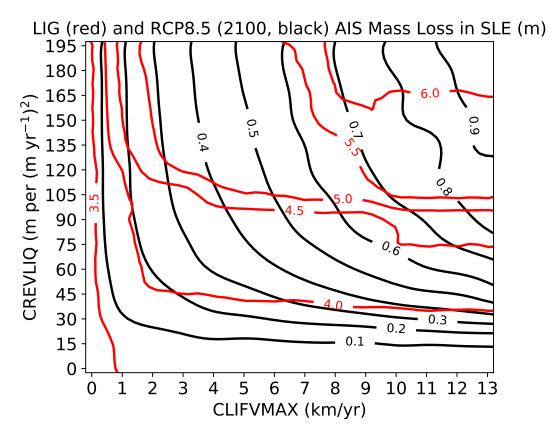


Figure S2. Contours are identical to the mean emulated sea-level contributions from the Antarctic ice sheet in Fig. 2, but with LIG and RCP8.5 contours overlapping for comparison.

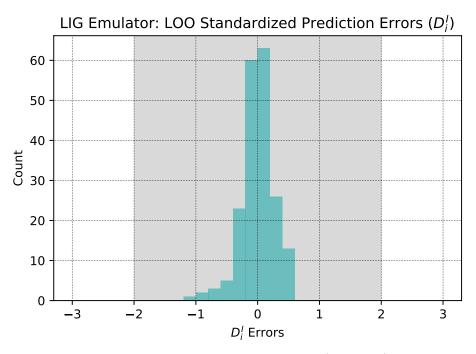
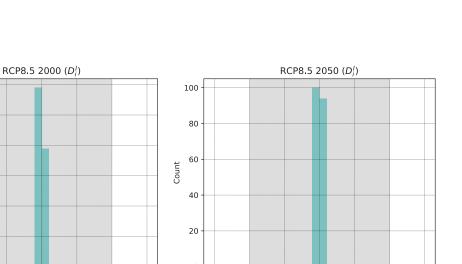


Figure S3. Histogram of standardized prediction errors (Eqn. S1) from leave-one out analyses performed with the Last Interglacial emulator. Errors $< \pm 2$ (gray shaded region) indicate the emulator is able to properly represent the ice-sheet model (cf. Bastos and O'Hagan, 2009).



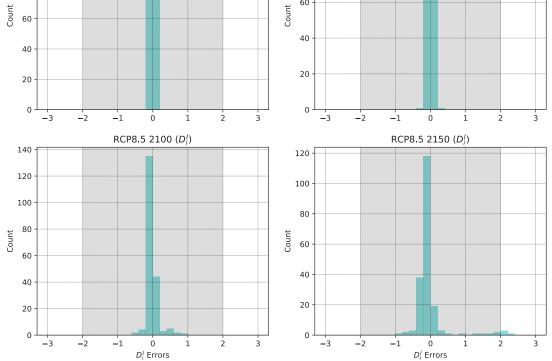


Figure S4. As in Fig. S3, but for the RCP8.5 emulator in 2000, 2050, 2100, and 2150.

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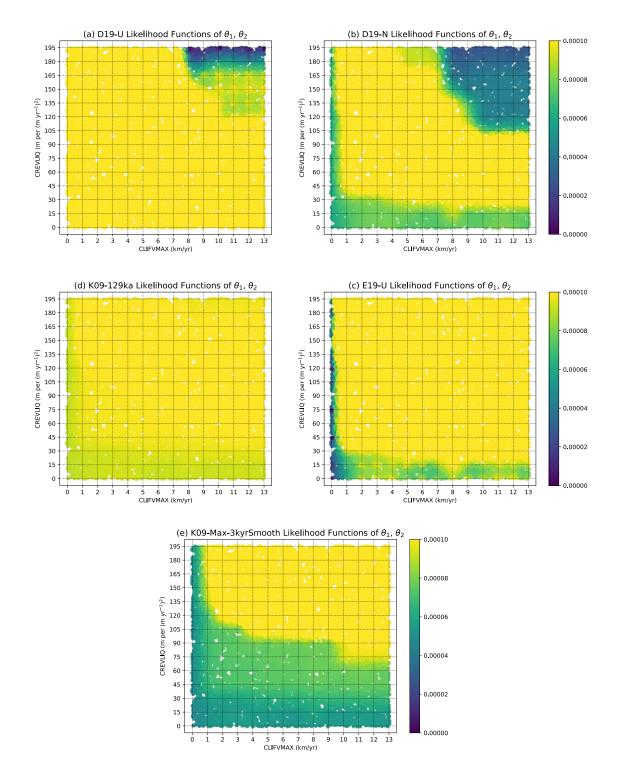


Figure S5. The posterior probabilities of CREVLIQ/CLIFVMAX latin-hypercube sampled pairs across the range of the model ensemble parameter space (cf. Table S1), conditional on specified constraints on Last Interglacial Antarctic Ice-sheet sea level contributions (cf. Figure 4a). The colorbar saturates at it upper extent.

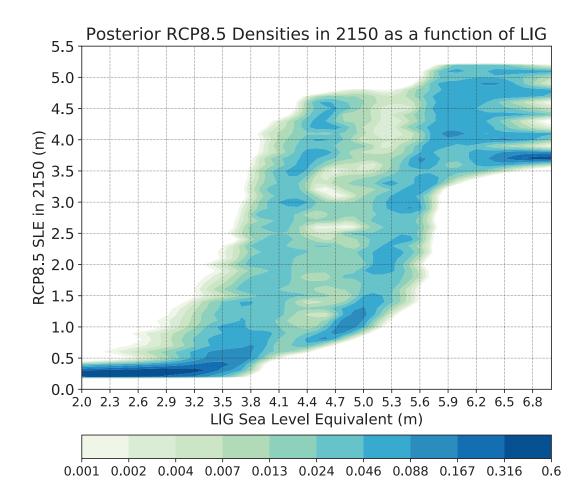


Figure S6. As in Fig. 4b, except for 2150.

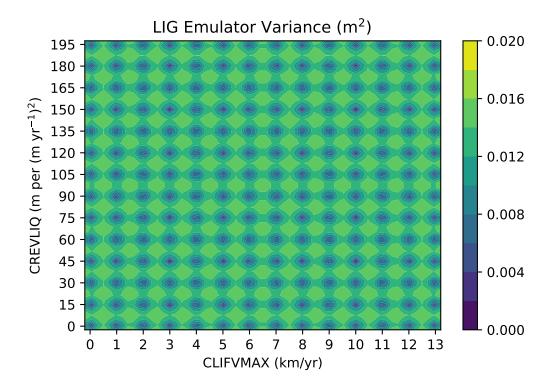


Figure S7. Last Interglacial emulator variance (m^2) over the ice-sheet model parameter space.

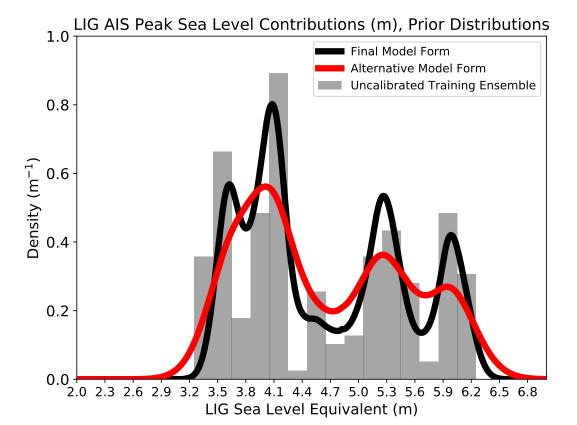


Figure S8. Last Interglacial emulated prior reproduced from Fig. 4a (black curve), compared with the emulated prior from an alternative model (red curve) defined with the covariance functions given in Eqn. (S2–S3). The training ensemble is shown as a histogram scaled for comparison.

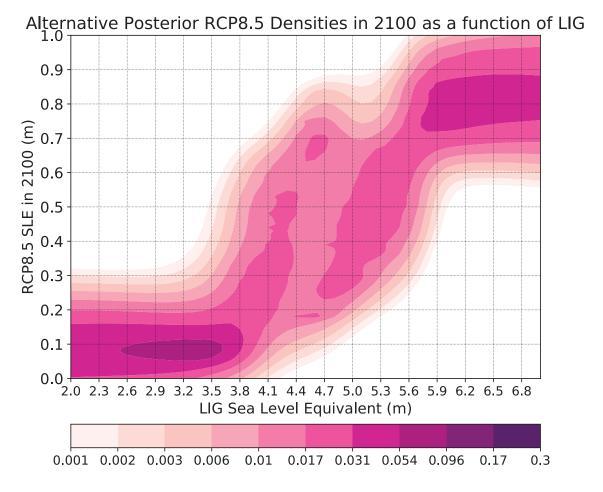


Figure S9. As in Fig. 4b, except normalized conditional posterior probability densities are plotted as a function of Last Interglacial AIS mass loss emulated with an alternative model defined with the covariance functions given in Eqn. (S2–S3).

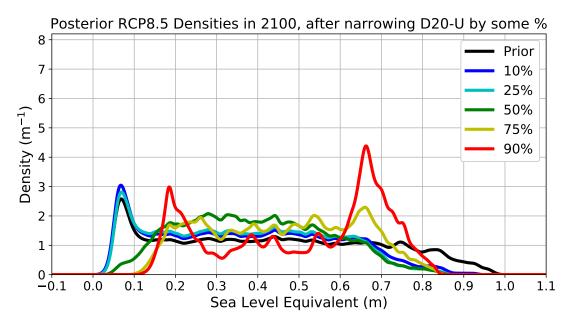


Figure S10. As in Fig. 6, except posteriors are constrained assuming the D20-U constraint was 10%, 25%, 50%, 75% or 90% narrower (blue, cyan, green, yellow and red curves, respectively).

Table S3.	Glossary —Definitions of relevant terms.
Torm	Mooning

Term	Meaning
Bayesian statistics	(in contrast to frequentist or classical statistical inference) is a theory based on the Bayesian interpretation of probability where probability expresses a degree of belief in an event. Bayesian methods compute a posterior probability of a model or parameter through the use of a prior probability distribution of the model or parameter times a likelihood function using Bayes' theorem
Bayesian updating	the process of using new information to improve on previous estimates. One uses the posterior distribution of one model as the prior distribution of a new model. For example, the posterior distribution on the parameters, (θ_1, θ_2) , is used as the prior distribution in the future projection model
Conditional probability	the distribution of a random quantity, given (assuming, or as a function of) a particular value of another (latent) random quantity
Covariance function	defines prior beliefs about the relationship between one or more variables or parameters in a Gaussian process, as a measure of how much they change together
Gaussian process (GP)	a generalization of the multi-variate Gaussian distribution to continuous parameter space, which is fully defined by its mean function and covariance function; GP regression provides an analytically-tractable solution when adopting the assumption of normality for all distributions
Hyperparameter	parameter of a GP model prior distribution
Latent	unobserved or hidden (e.g., the true values of AIS mass loss)
Likelihood	the probability of observing the data as described by the fitted model; also known as the sampling or data distribution; a conditional distribution that is a function of unknown parameters for observed data
Marginal distribution	unconditional probability distribution of a random quantity, found by integrating over all values of the conditional distribution

Table S3 (continued).

Term	Meaning
Non-parametric	not involving any assumptions as to the functional form
Posterior probability	the probability distribution of an unknown quantity, conditional on (or assuming/given) observed data; In this study these are, 1) the future AIS sea-level contribution projections over time conditioned on a specified Last Interglacial estimate distribution, and 2) the distribution of the model parameters (CREVLIQ and CLIFVMAX) given specific LIG constraints
Prior probability	(of an uncertain quantity—e.g., parameter or model) uses a priori beliefs about the quantity before some evidence or data is taken into account; the prior is combined with the probability distribution of new data to yield a posterior distribution. The prior can be subjective or uninformative (such as a uniform distribution) to minimize the impact on Bayesian statistics