

# An Operational EOP Series by Combination of GNSS & VLBI

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November 24, 2022

## Abstract

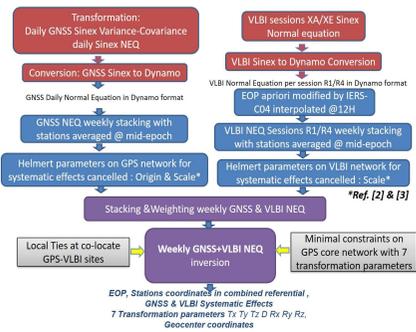
The Earth orientation parameters (EOP), the regular products of IERS Earth Orientation Centre, are computed at daily bases by combination of EOP solutions by different astro-geodetic techniques. At SYRTE we have developed a new strategy of combination using the Global Navigation Satellite Systems (GNSS) and Very Long Baseline Interferometry (VLBI) techniques at normal equation level thanks to the IERS COL-WG [1]. This approach allows to produce the EOP at the daily bases, polar coordinates (x,y) and rates (xr,yr), universal time UT1 and rate LOD, and corrections from IAU200A/2006 precession-nutation mode (dX,dY), simultaneously with station coordinates constituting the terrestrial frame (TRF) and possibly the quasar coordinates constituting the celestial frame (CRF). For studying these EOP solutions continuously with respect to the IERS EOP products, we have developed an operational process which take the recently solution files produced respectively by IGS and IVS international services which are converted at normal equation level. The recorded solutions obtained from GNSS and VLBI combination at weekly bases is recently maintained by SYRTE. The process of this combination are presented and results are analysed.

## Summary

The Earth orientation parameters (EOP), the regular products of IERS Earth Orientation Centre, are computed at daily bases by combination of EOP solutions by different astro-geodetic techniques. At SYRTE we have developed a new strategy of combination using the Global Navigation Satellite Systems (GNSS) and Very Long Baseline Interferometry (VLBI) techniques at normal equation level thanks to the IERS COL-WG [1]. This approach allows to produce the EOP at the daily bases, polar coordinates (x,y) and rates (x<sub>y</sub>,y<sub>x</sub>), universal time UT1 and rate LOD, and corrections from IAU200A/2006 precession-nutation mode (dX,dY), simultaneously with station coordinates constituting the terrestrial frame (TRF) and possibly the quasar coordinates constituting the celestial frame (CRF).

For studying these EOP solutions continuously with respect to the IERS EOP products, we have developed an operational process which take the recently solution files produced respectively by IGS and IVS international services which are converted at normal equation level. The recorded solutions obtained from GNSS and VLBI combination at weekly bases is recently maintained by SYRTE. The process of this combination are presented and results are analysed.

## Strategy



## Data

	GNSS	VLBI
origin	IGS	IVS
ftp	<a href="ftp://igs.ign.fr/pub/igs/products">ftp://igs.ign.fr/pub/igs/products</a>	<a href="ftp://cdsis.gsfc.nasa.gov/vlbi/vlvsproducts">ftp://cdsis.gsfc.nasa.gov/vlbi/vlvsproducts</a>
SINEX format	daily GNSS solution with variance-covariance Matrix	Normal Equation Matrix & Normal Equation Vector
SINEX files	5513 daily files GPS week repro2: 1043 - 1832 1465 daily files GPS week 1832 - 2041	2540 VLBI R1 / R4 sessions from January 2 <sup>nd</sup> 2000 to December 29 <sup>th</sup> 2018

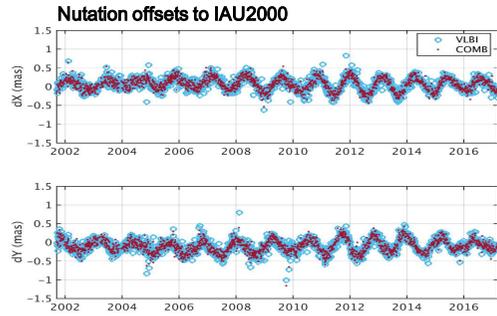
### Combined Series GNSS+VLBI @ EOP-PC produced

series	Pole & LOD	UT & dX, dY
971 GPS week from 1043 to 2033 20 missing weeks	7014 points January 2 <sup>nd</sup> 2000 to December 29 <sup>th</sup> 2018	2249 points January 5 <sup>th</sup> 2000 to December 28 <sup>th</sup> 2018

## Parameters

Parameters	GNSS daily		VLBI R1/R4 sessions	
	Sinex parameters	Initial values	Sinex parameters	Initial values
Polar coordinates	XPO_YPO @12h	IERS EOP 08-C04	XPO_YPO @-04-06h	IERS EOP 14-C04
Polar motion rate	XPOR_YPOR @12h	IERS EOP 08-C04	XPOR_YPOR @-04-06h	0.0
Delta time UT1-UTC	-	-	UT @-04-06h	IERS EOP 14-C04
Length of Day/LOD	LOD @12h	IERS EOP 08-C04	LOD @-04-06h	IERS EOP 14-C04
Nutation offset dX, dY IAU2000/2006 model	-	-	NUT_X_NUT_Y @*05-07h	0.0
Station coordinates	STAX_STAY_STAZ *500 stations @12h	IG08 & IG14 from February 2017	STAX_STAY_STAZ *5 stations /session @-04-06h	ITRF14
Geo-centre	XGC_YGC_ZGC @12h	Set to 0.0	-	-

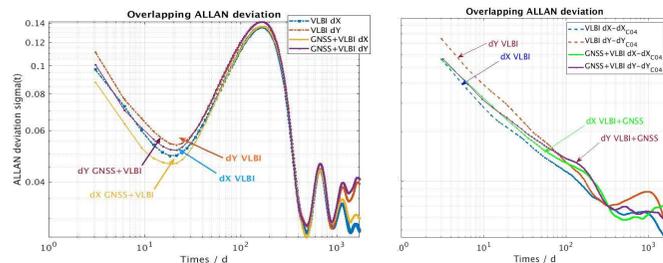
## EOP Combined solution 2000-2019



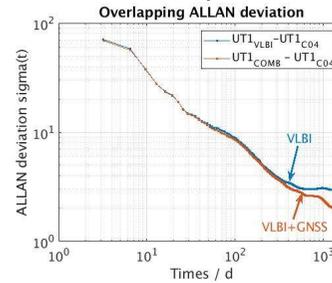
The nutation offsets to IAU2000: some spurious points of the VLBI solution are drawn back closer to the mean when combined to GNSS. Covariance matrices reveal that correlations between nutation parameters and other EOP are systematically - and neatly for EOP rates - improved by the combination.

$$r_{dX_{xp}} = \frac{\text{cov}(dX_{xp}, x_p)}{\sqrt{\text{var}(dX_{xp}) \text{var}(x_p)}}$$

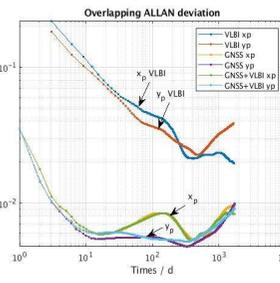
### Stability on the nutation offset corrections wrt. C04, VLBI only & COMB



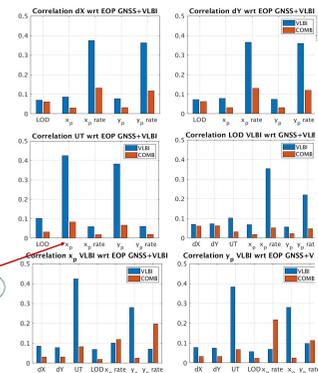
### Stability on the UT1-UTC corrections wrt. C04, VLBI only & COMB



### Stability on the polar motion corrections wrt. C04, VLBI only, GNSS only & COMB



### EOP Correlation for VLBI & COMB



### Correlations between EOP estimated over 2000-2019 for VLBI only and COMB (GNSS+VLBI)

	xp	yp	UT1 μs	LOD	dX	dY
GNSS	35.9	32	-	16.5	-	-
VLBI	113.0	112.2	69.8	18.7	46.8	51.6
COMB	35.2	32.0	68.8	15.5	56.3	60.7

### CHI square of differences to C04

	xp	yp	UT1 μs	LOD	dX	dY
GNSS	0.4	0.4	-	1.6	-	-
VLBI	4.9	6.1	2.2	2.5	1.5	2.4
COMB	0.3	0.3	1.9	1.5	2.2	3.1

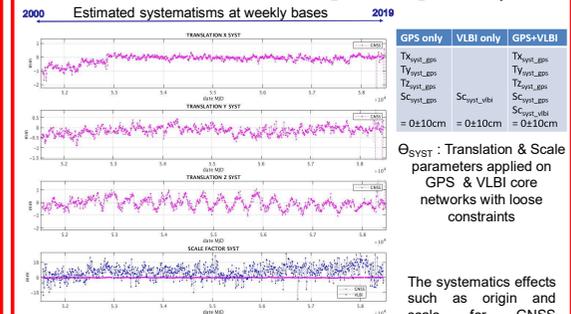
### Median of errors (μs)

	xp	yp	UT1 μs	LOD	dX	dY
C04	67.0	63.0	9.5	15.2	43.0	40.0
IVS	-	-	-	-	17.2	17.4
GNSS	3.8	3.9	-	0.8	-	-
VLBI	27.9	27.5	1.2	2.4	15.6	15.9
COMB	3.6	3.6	1.1	0.8	14.2	14.3

## Combined TRF

### Systematism w.r.t ITRF : Helmert parameters

$$\text{Station positions with systematism: } X_{\text{Tech\_Initial}} = X_{\text{Tech\_new}} + B \cdot \Theta_{\text{Syst}}$$



Estimated systematisms at weekly bases

GNSS only	VLBI only	GPS+VLBI
Tx <sub>Wetzell</sub> <sub>GNSS</sub>	Tx <sub>Wetzell</sub> <sub>VLBI</sub>	Tx <sub>Wetzell</sub> <sub>GPS+VLBI</sub>
Ty <sub>Wetzell</sub> <sub>GNSS</sub>	Ty <sub>Wetzell</sub> <sub>VLBI</sub>	Ty <sub>Wetzell</sub> <sub>GPS+VLBI</sub>
Tz <sub>Wetzell</sub> <sub>GNSS</sub>	Tz <sub>Wetzell</sub> <sub>VLBI</sub>	Tz <sub>Wetzell</sub> <sub>GPS+VLBI</sub>
Scale <sub>Wetzell</sub> <sub>GNSS</sub>	Scale <sub>Wetzell</sub> <sub>VLBI</sub>	Scale <sub>Wetzell</sub> <sub>GPS+VLBI</sub>
= 0±10cm = 0±10cm = 0±10cm		

Θ<sub>SYST</sub> : Translation & Scale parameters applied on GPS & VLBI core networks with loose constraints

The systematics effects such as origin and scale for GNSS network and scale for VLBI network are estimated at weekly bases. The station positions resulting are free of these effects and put in a common referential before the combination.

### Minimal constraints: 7 GNSS Transformation Parameters w.r.t. ITRF

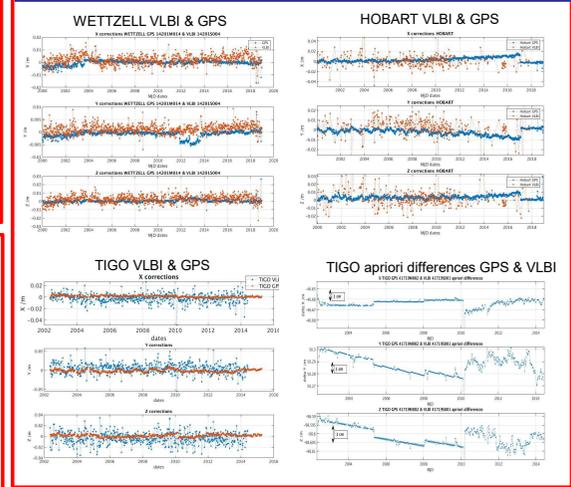
Station positions at weekly bases

$$X_{\text{Tech}} = X_{\text{Tech\_new}} + B \cdot \Theta + [Tx \ Ty \ Tz \ D \ Rx \ Ry \ Rz]^T$$

Minimal Constraints 'Θ' on GPS core stations 2000-2019: mean & rates

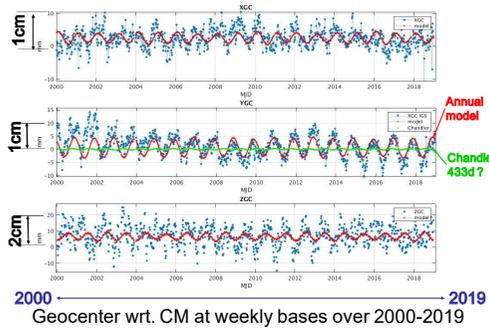
	Tx mm	Ty mm	Tz mm	D mm	Rx mm/y	Ry mm/y	Rz mm/y
GNSS	-0.185 ±0.709	-0.136 ±0.376	-0.028 ±1.021	-0.979 ±0.689	-0.031	-0.0006	-0.010
VLBI	-	-	-	-	+3.624 ±4.205	-1.558	-

### Station coordinates estimation examples



References: [1] Gambis D., Richard J.-Y., Bizouard C., "Why combining at the Observation Level?" REFAG 2010, IAG series 138, Reference for Applications in Geosciences, 111-117  
[2] Sahin M., Variance component estimation applied to satellite laser ranging, Bul Geo Springer-Verlag 1992  
[3] Arnaud Pilet IGN/LAREG thesis « COMBINAISON DE TECHNIQUES DE GÉODÉSIE SPATIALE », Paris 2011

## Geocenter



## Conclusion & Prospects

We dispose of an operational chain now available to produce GNSS and VLBI combination from IERS technique centres at the normal equation level based on the CNES/GRGS DYNAMO software. This combination shows a good consistency with ITRF14 and becomes useful to control the C04 reference series of polar motion in consistency with the official terrestrial frame. Correlations between EOP estimated by VLBI only and by combination are slightly reduced, comparable accuracy are observed on the EOP wrt. GPS & VLBI Station coordinates are simultaneously estimated in consistency with the ITRF. The long duration series of the geocenter could be useful to analyse the geophysical effect involved. Next steps of our project consist to assess the quality of the celestial reference frame, add the Laser technique (SLR, LLR) and the DORIS technique.