

Probing changes in frictional state due to normal stress perturbations using controlled-source ultrasonics

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Abstract

We perform a suite of laboratory friction experiments on saw-cut Westerly Granite surfaces and probe frictional state evolution in response to step changes in normal stress. The experiments are conducted with the objective of illuminating the origin of friction memory effects and the fundamental processes that yield friction rate and state dependence. In contrast to previous works, we measure directly the fault slip rate and account for changes in slip rate caused by normal stress perturbations. Further, we complement mechanical data acquisition by continuously probing the faults with ultrasonic pulses. We conduct the experiments at room temperature and humidity conditions in a servo controlled biaxial testing apparatus in the double direct shear configuration. The normal stress perturbations are carried out during steady shearing over a range of shear velocities, from 0.02 - 100 $\mu\text{m/s}$. We report observations of a transient shear stress and friction evolution with step increases and decreases in normal stress. Specifically, we show that shear stress evolves in a two-stage fashion – first linear-elastically, then inelastically in response to the normal stress step. We find that the excursions in slip rate resulting from the changes in normal stress must be accounted for in order to accurately predict fault strength evolution. The effects of induced changes in fault slip rate are also apparent in elastic wave properties. Ultrasonic wave amplitudes increase instantly in response to normal stress steps and then gradually decrease to a new steady state value, in part due to changes in fault slip rate. This decrease is strongly related to accelerated creep at the fault interface. We also demonstrate that steady state amplitudes are a reliable proxy for real contact area (RCA) at the fault interface. Previous descriptions of frictional state evolution during normal stress perturbations have not adequately accounted for large slip velocity excursions. Here, we do so by using the measured ultrasonic amplitudes as a proxy for frictional state during transient shear stress evolution. Our work improves understanding of induced seismicity and triggered earthquakes with particular focus on simulating static triggering and stress transfer phenomena using rate-and-state frictional formulations in earthquake rupture models.

Probing changes in frictional state due to normal stress perturbations using controlled-source ultrasonics

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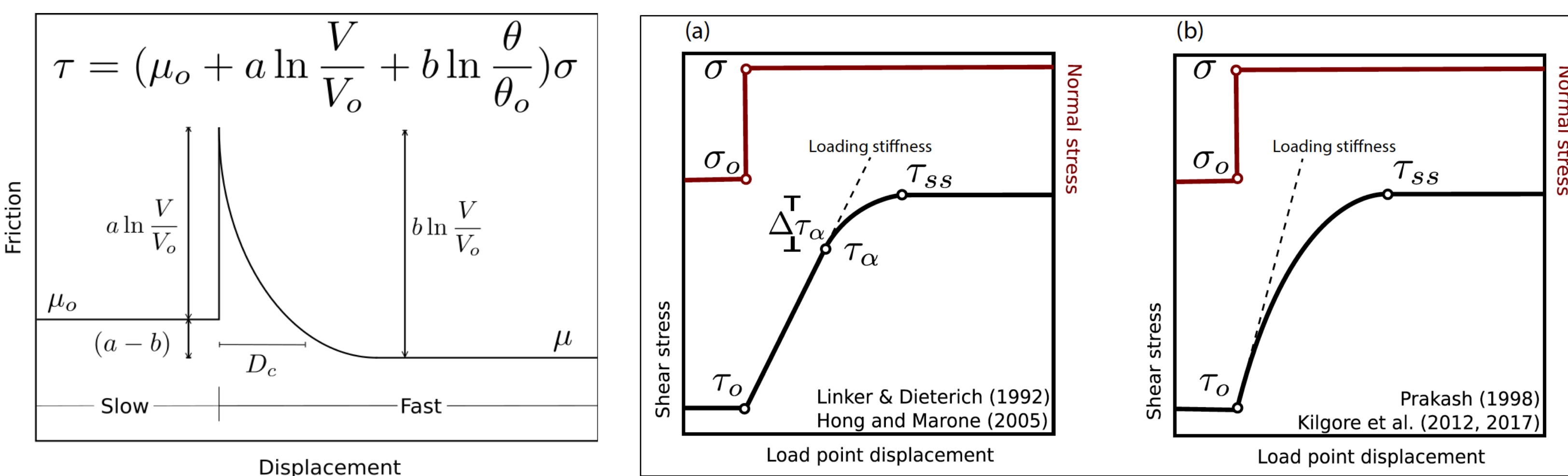
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1. Introduction

Rate-state friction (RSF) represents the premier framework used in friction experiments and earthquake rupture models. An illustration of RSF is shown in Fig. 1. Fault behavior in response to velocity perturbations is well understood but the effect of normal stress is poorly quantified. Two contrasting sets of friction evolution have been documented in literature as shown in Fig. 2.



$$\dot{\theta} = 1 - \frac{V\theta}{D_c} \quad (\text{Aging law})$$

$$\dot{\theta} = -\frac{V\theta}{D_c} \ln \frac{V\theta}{D_c} \quad (\text{Slip law})$$

$$\theta = \theta_o \left(\frac{\sigma}{\sigma_o} \right)^{\frac{\alpha}{b}}$$

$$\alpha = \frac{(\tau_{ss} - \tau_o) / \sigma}{\ln \sigma / \sigma_o}$$

Figure 2. On subjecting a fault to a step increase in normal stress from σ_o to σ , (a) a two stage response in shear stress has been documented. Here, the shear stress first increases elastically from τ_o to τ_{α} followed by a non-linear evolution to a steady state value, τ_{ss} . The state evolution formulation for this observation was given by Linker and Dieterich (1992). The parameter ' α ' here quantifies the elastic deformation at the contact junctions and (b) A completely non-linear evolution has been suggested by Prakash (1998) and Kilgore et al. (2012, 2017) where either slip or time is necessary for shear stress evolution.

2. Methods

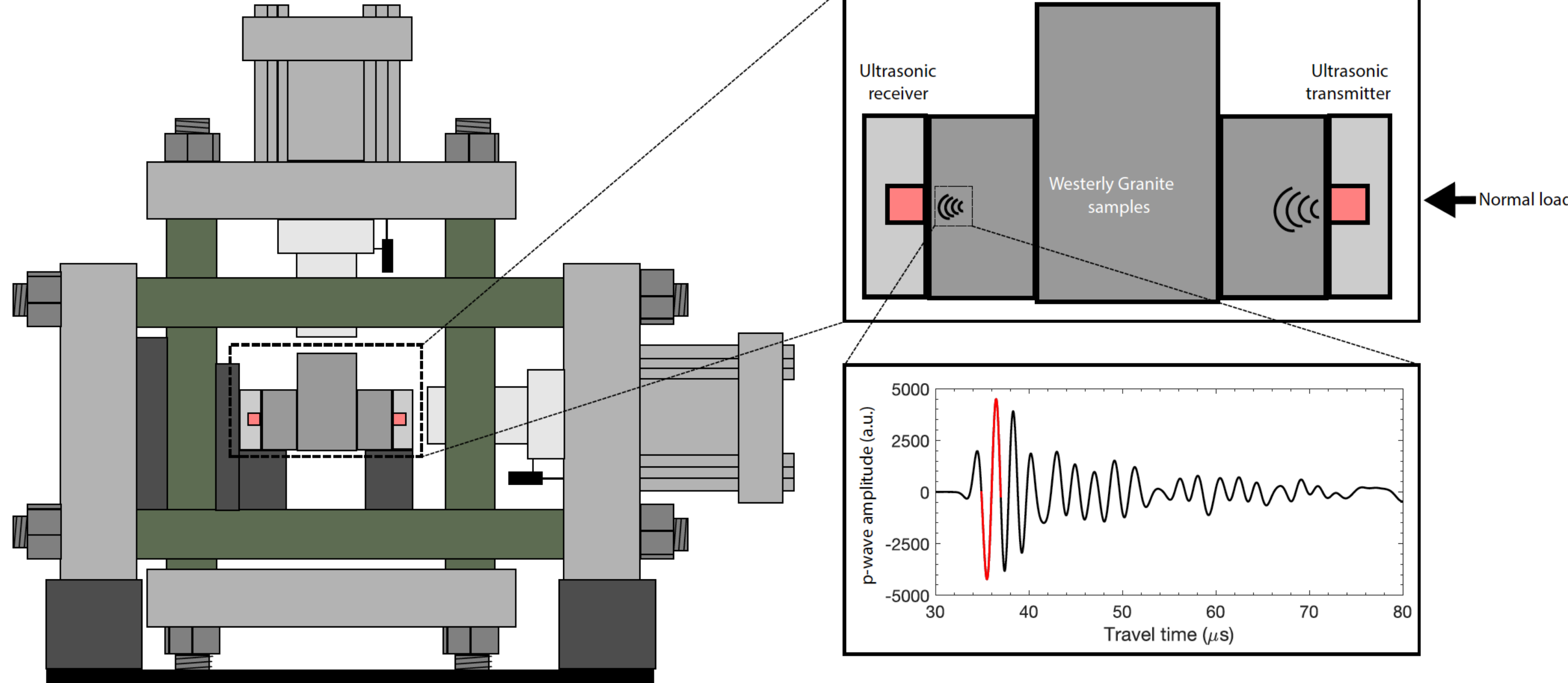


Figure 3. A schematic of the biaxial testing apparatus and Westerly granite blocks used in this study. The setup is instrumented with a load cell and direct current differential transformer (DCDT) transducer in the vertical (shear) and horizontal (normal) stress directions. P-wave polarized piezoelectric transducers on either side of the double-direct shear setup transmit and receive a 500 kHz pulse. A blow-up of a typical wave recorded by the receiver shows the p-wave arrival at ~33 μs. P-wave amplitude is calculated as a peak-to-peak amplitude of the red portion of the waveform.

3. Results

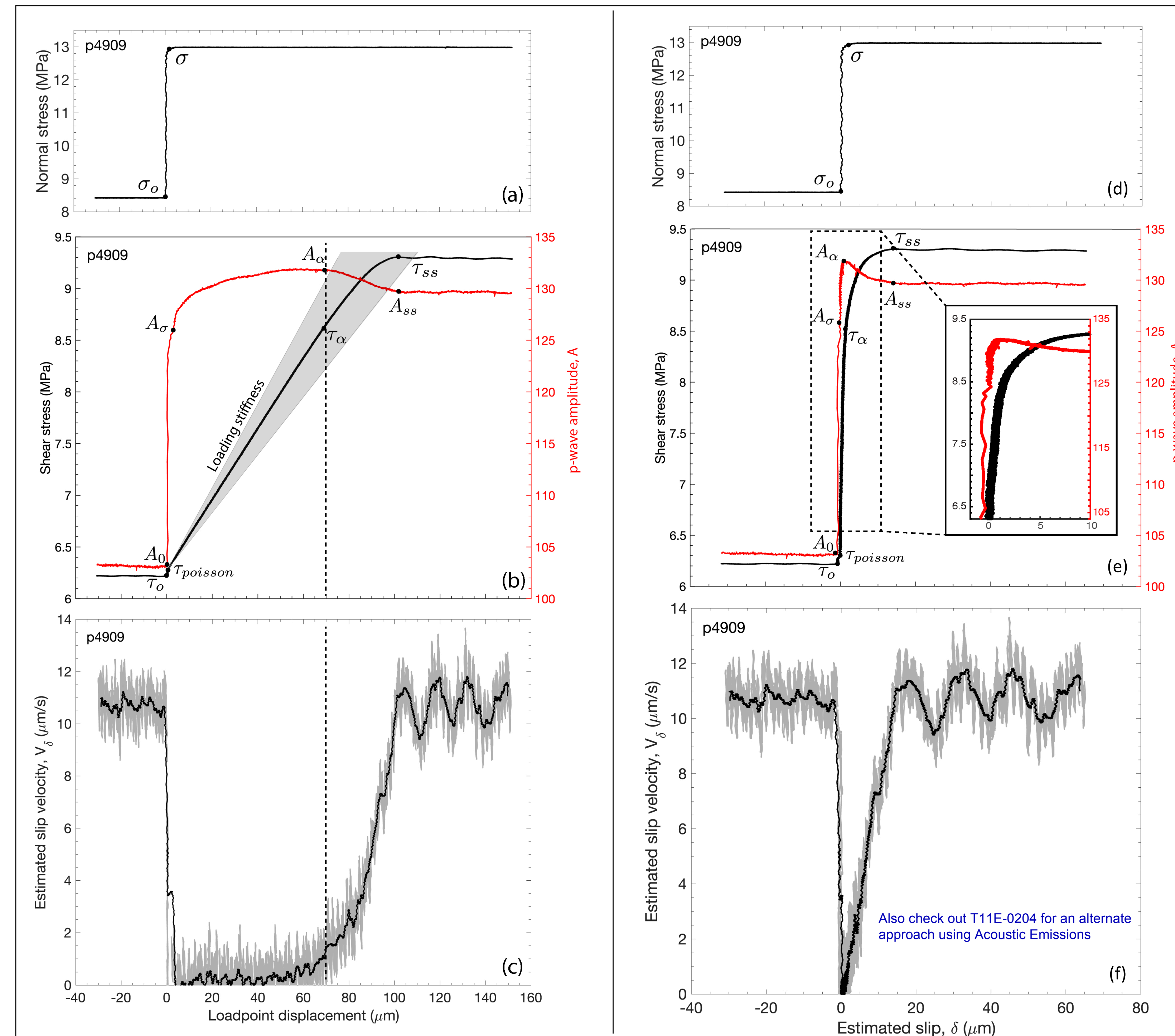


Figure 5. (a) Normal stress step up from 8.4 MPa to 13 MPa (b) The corresponding shear stress increase with load point displacement (black) and acoustic amplitude (red) increase over the same displacement scale. The shaded grey area is the error in calculating load point stiffness (refer to manuscript) and (c) the slip velocity decreases from ~11 μm/s to ~0 μm/s during the normal stress step, as the p-wave amplitude increases. The onset of accelerated fault creep corresponds with a decrease in p-wave amplitude to a steady state value. Panels (d) through (f) express the normal stress, shear stress, amplitude and fault slip velocities as functions of slip.

4. Is ultrasonic amplitude a proxy for real contact area?

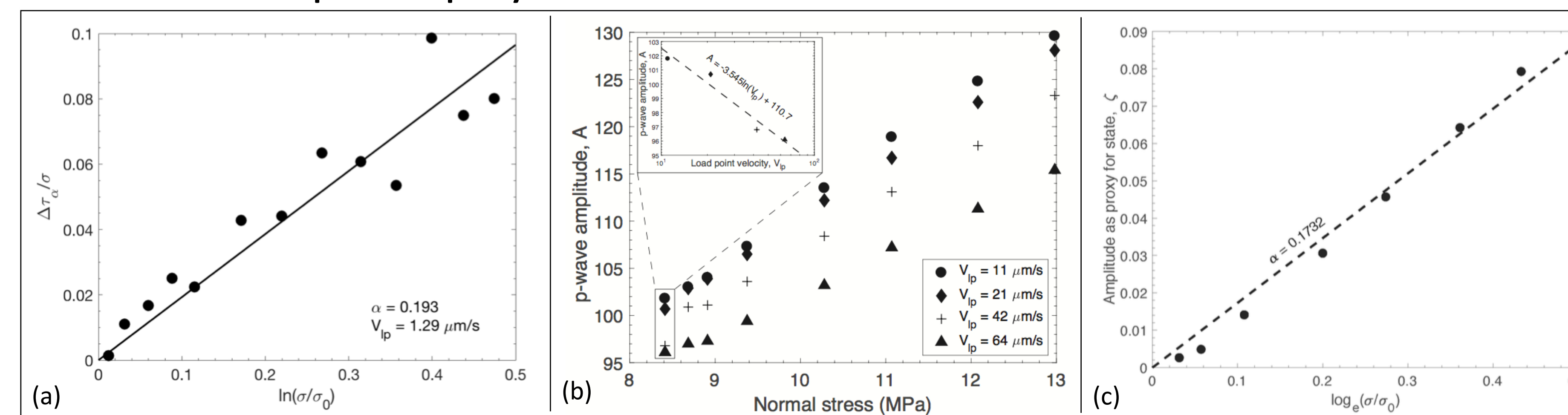


Figure 6. (a) Frictional state evolution term ' α ' constrained from stress data (b) Ultrasonic amplitude varies linearly with normal stress and inverse log-linearly with load-point velocity (inset) (c) Slope of amplitude assumed as proxy for state is equal to ' α ' for normal stress steps

5. Numerical modeling of normal stress steps

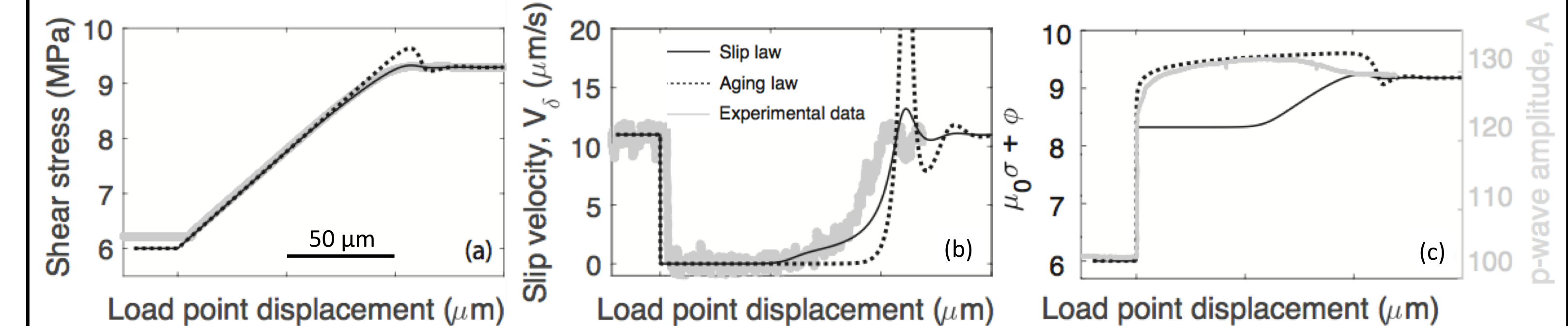


Figure 7. Numerical models of the Slip law match experimental data well for (a) shear stress and (b) slip rate but (c) ultrasonic amplitude is better modeled by Aging law state

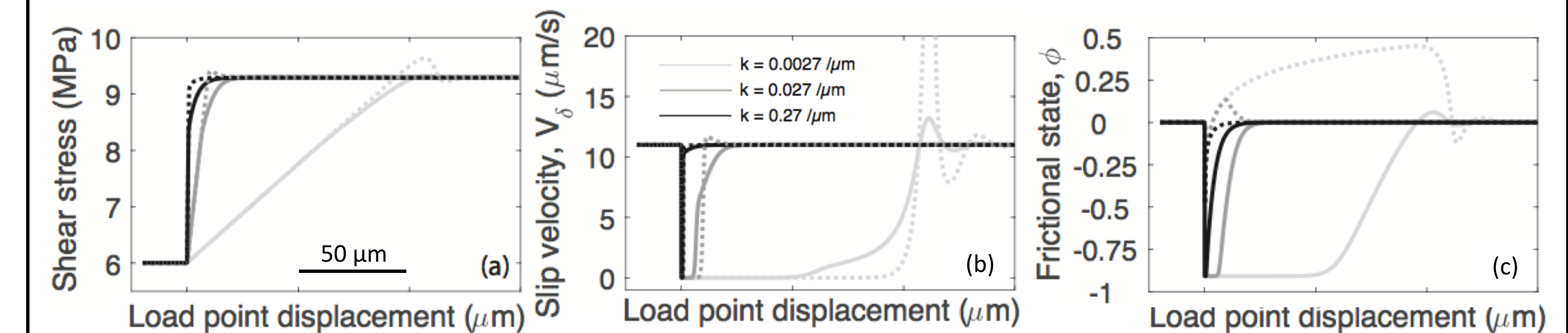


Figure 8. Aging and Slip law models of normal stress steps are asymptotically similar at high stiffnesses for (a) shear stress (b) slip rate and (c) frictional state

6. A microphysical model for contact area variations during normal stress steps

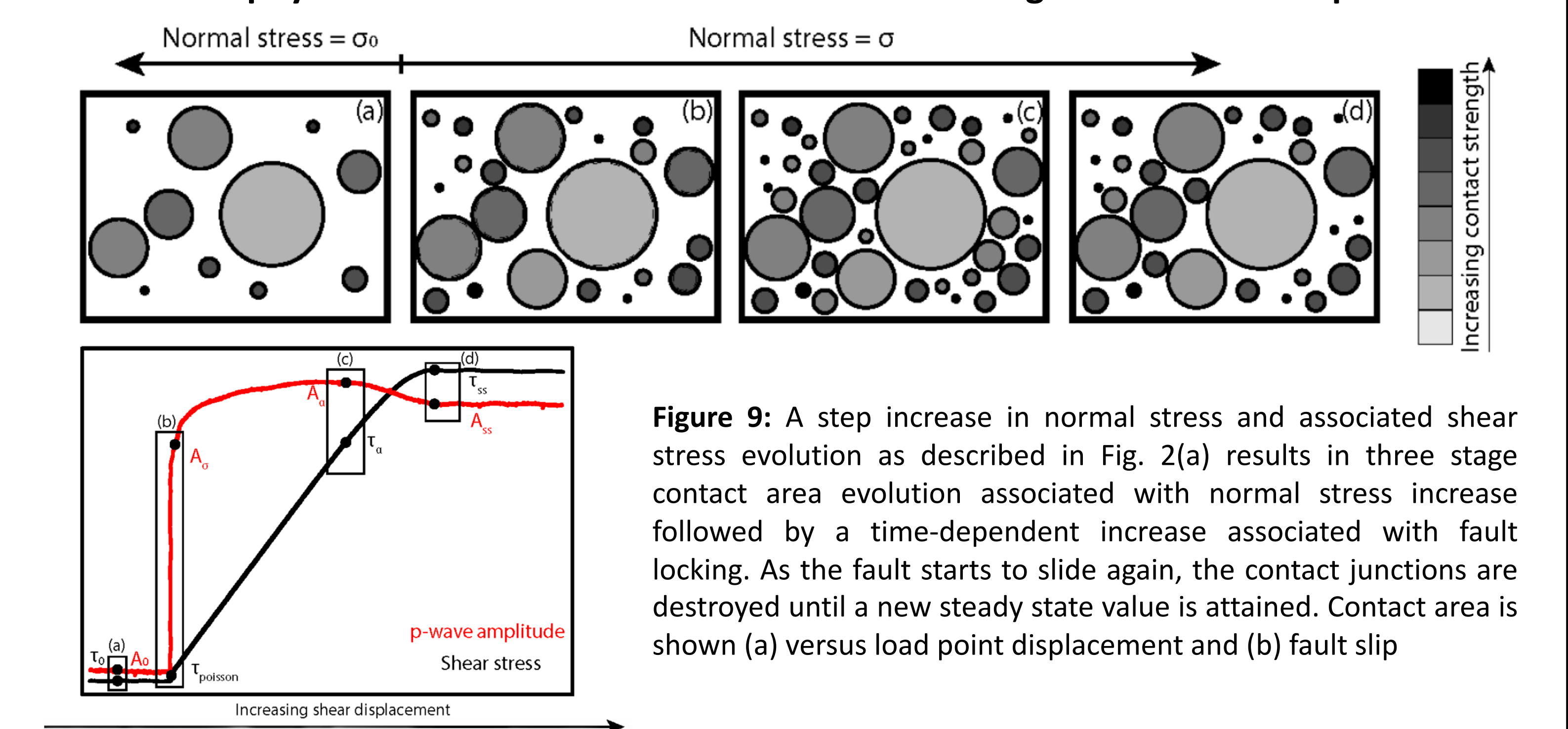


Figure 9: A step increase in normal stress and associated shear stress evolution as described in Fig. 2(a) results in three stage contact area evolution associated with normal stress increase followed by a time-dependent increase associated with fault locking. As the fault starts to slide again, the contact junctions are destroyed until a new steady state value is attained. Contact area is shown (a) versus load point displacement and (b) fault slip

7. Conclusions

- An interplay of apparatus stiffness & large normal stress steps produces an elastic-inelastic shear stress response due to a large slip rate excursion on the fault.
- Large stiffnesses result in a small rate excursion and associated elastic increase which may be unresolved (eg. Prakash, 1998; Kilgore et al., 2012)
- Ultrasonic amplitude could illuminate the evolution of real contact area during shearing.
- The real contact area and steady-state frictional state appear to vary in a complex manner during the normal stress step, and this variation is related to accelerated fault creep.

References

- Hong and Marone (2005). *Geochemistry, Geophysics and Geosystems*. doi: 10.1029/2004GC000821
- Kilgore et al. (2012). *Journal of Applied Mechanics*. doi: 10.1115/1.4005883
- Kilgore et al. (2017). *Journal of Geophysical Research: Solid Earth*. doi: 10.1002/2017JB014049
- Linker and Dieterich. (1992). *Journal of Geophysical Research*. doi: 10.1029/92JB00017
- Prakash. (1998). *Journal of Tribology*. doi: 10.1115/1.2834197

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